

# TWO TOPICS on TOP QUARKS

**A. WEAK CORRECTIONS  
and SUDAKOV LOGARITHMS**

**B. CHARGE ASYMMETRY  
in HADROPRODUCTION  
and AXIGLUONS**

J. H. Kühn



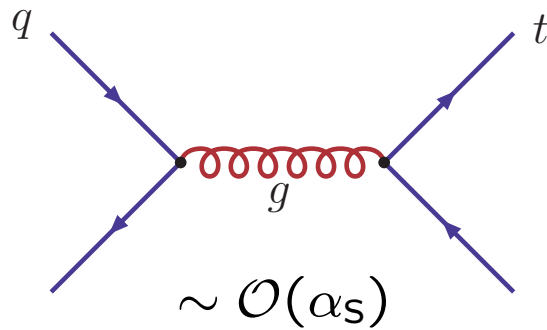
# A. WEAK CORRECTIONS TO TOP PRODUCTION

J.K., Scharf, Uwer: Eur. Phys. J. C45(2006) 139  
Eur. Phys. J. C51(2007) 37

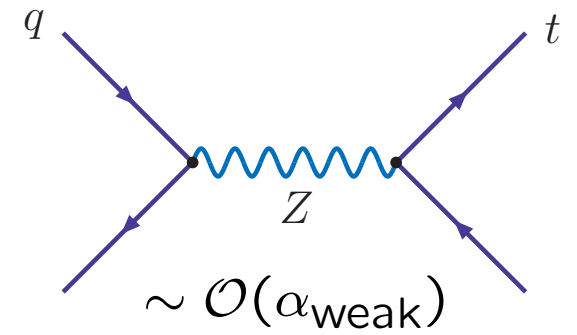
- I. Results at Partonic Level
- II. Tevatron and LHC

# I. Results at Partonic Level

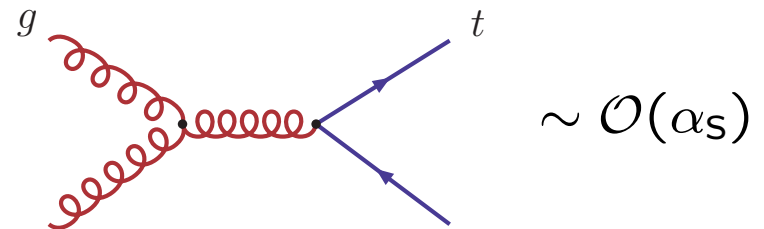
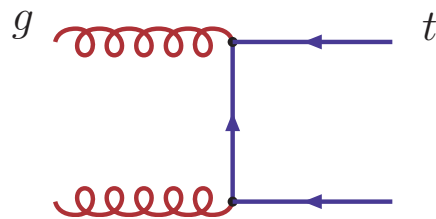
$q \bar{q} \rightarrow t \bar{t}$ :



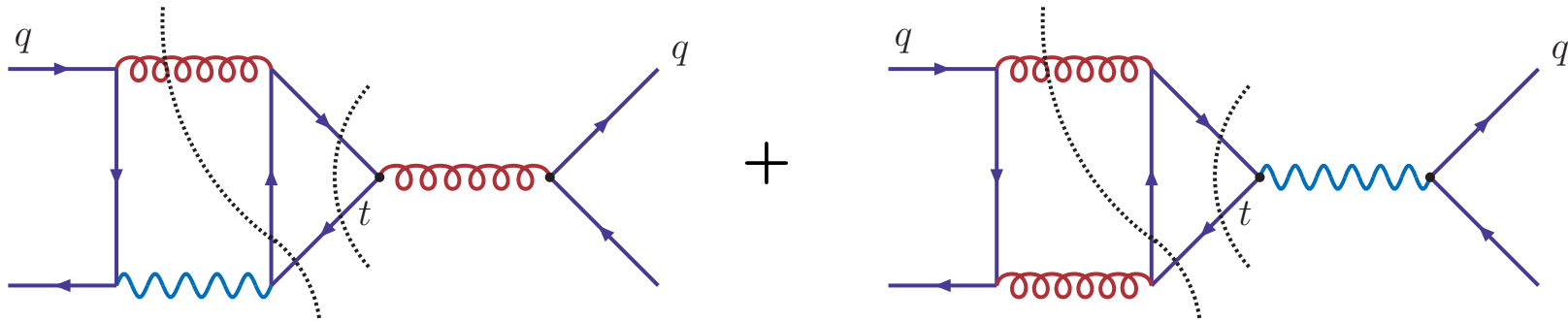
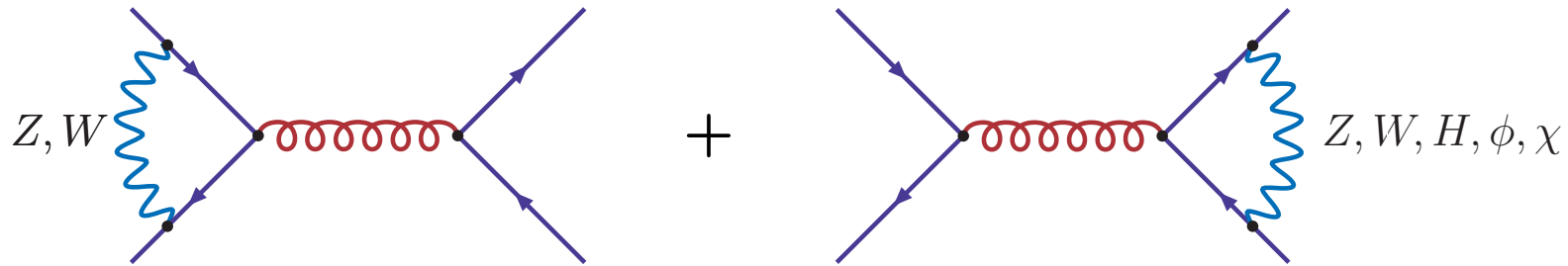
no  
interference  
with



$g g \rightarrow t \bar{t}$ :

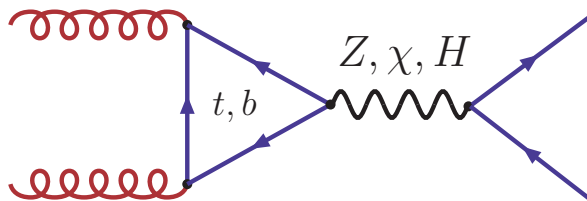
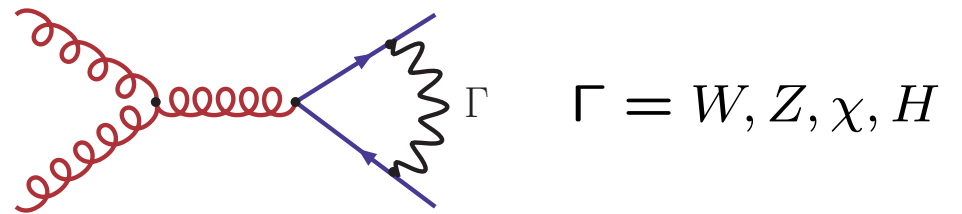
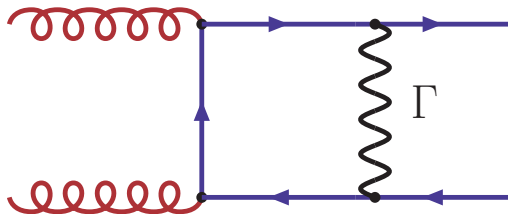
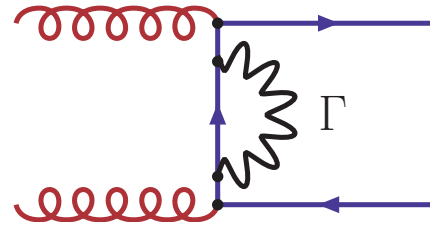
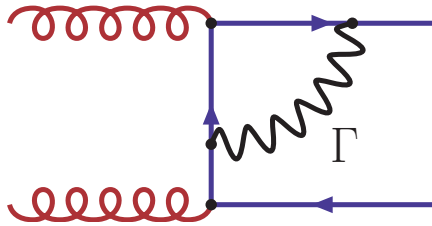


$\mathcal{O}(\alpha_S^2 \alpha_{\text{weak}})$  weak corrections ( $q \bar{q} \rightarrow t \bar{t}$ )



cuts of second group individually IR-divergent

$\mathcal{O}(\alpha_S^2 \alpha_{\text{weak}})$  weak corrections ( $g g \rightarrow t \bar{t}$ )



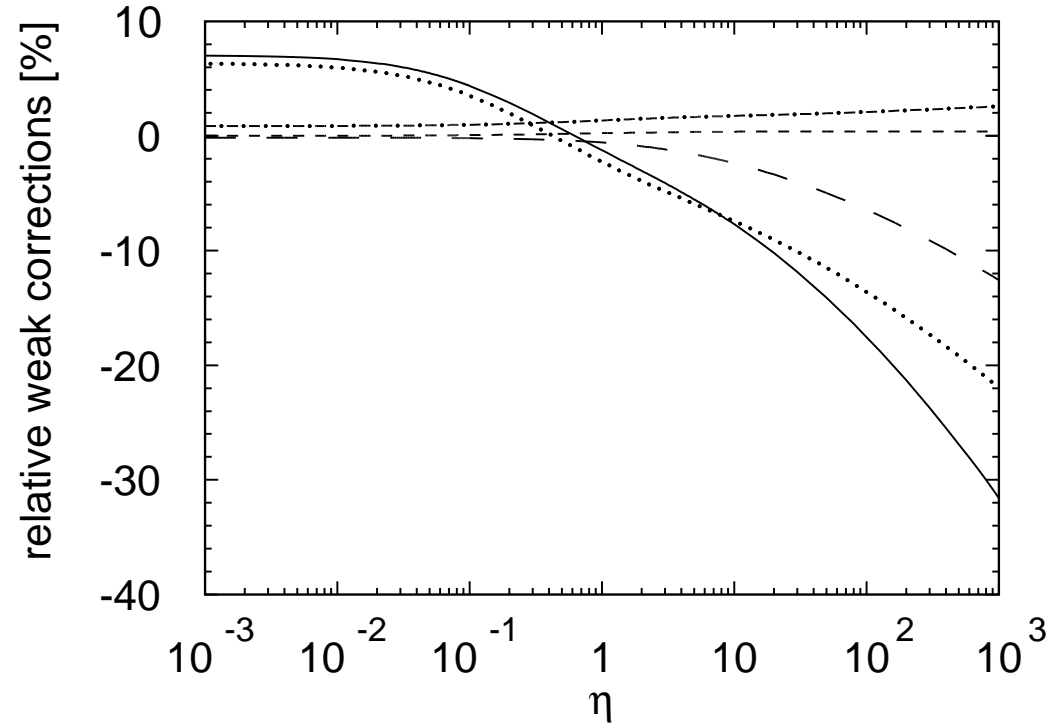
Contribution also from virtual  $Z$ ,  
no pole at  $q^2 = m_Z^2$   
(Yang theorem).

- analytical & numerical results available
- some disagreements with earlier partial results by Beenakker, Denner, Hollik, Mertig, Sack, Wackerroth 1994
- some discrepancies with Moretti, Nolten, Ross 2006
- in agreement with Bernreuther & Fucker 2005/06

⇒ Partonic results

- $(gZ)$ -box contribution to  $q\bar{q} \rightarrow t\bar{t}$ :  
 proportional to  $I_q^3$   
 $\Rightarrow$  (box contribution)<sub>up-quark</sub> = -(box contribution)<sub>down-quark</sub>  
 $\Rightarrow$  suppression  
 moderately  $\hat{s}$ -dependent
- strong increase of vertex and weak box contributions  
 (“Sudakov-Logs”)
- sizable  $M_h$ -dependence,  
 large effect close to threshold

$$u\bar{u} \rightarrow t\bar{t}$$

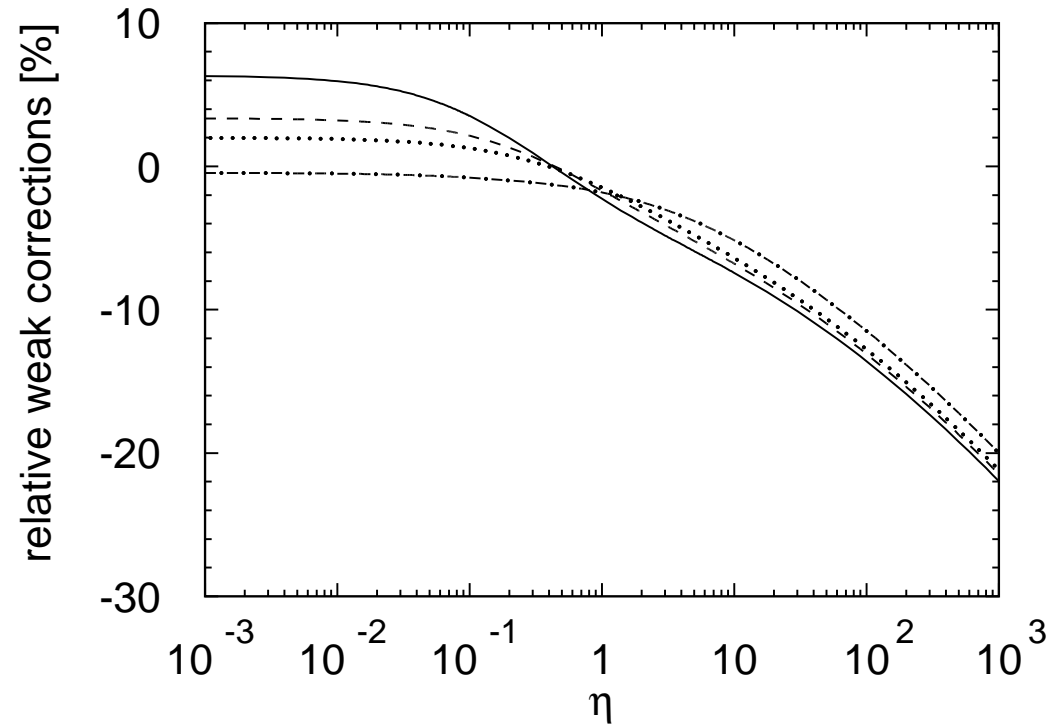


$$\eta = \frac{s}{4m_t^2} - 1$$

Different contributions to the electroweak corrections for incoming up-quarks: Initial vertices (long-dashed), final vertices (dotted), EW-box (dash-dotted), QCD-box (dashed). The sum is shown as a full line.

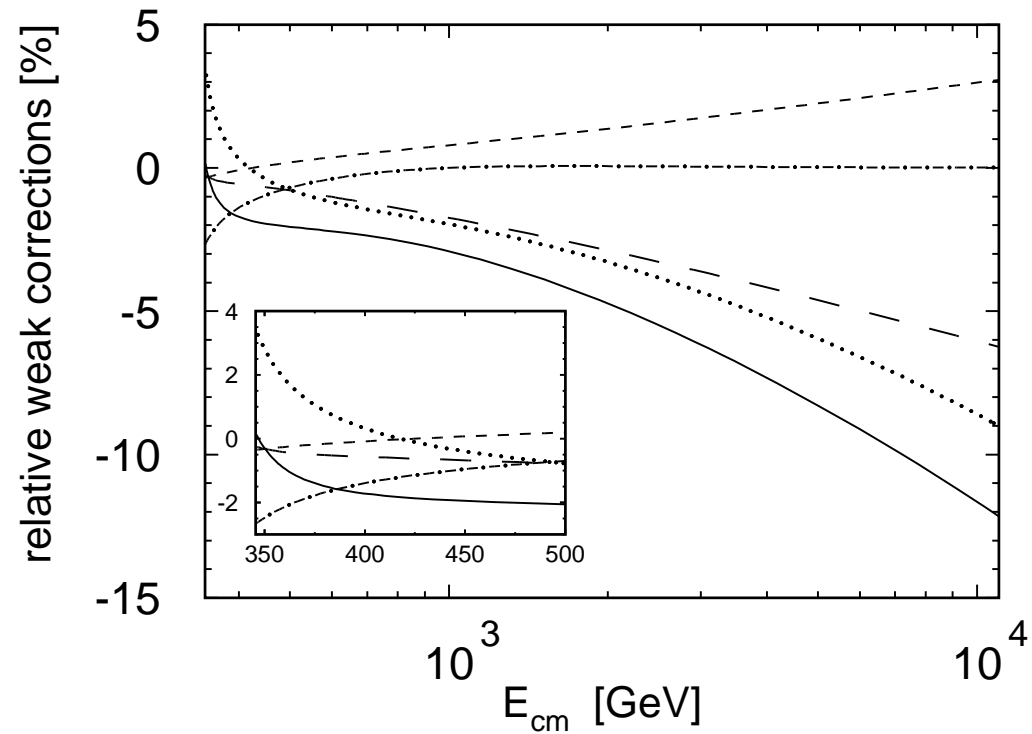


## Higgs Mass Dependence of $q\bar{q} \rightarrow t\bar{t}$



Relative change of the cross section from corrections to the final vertex for different Higgs masses  $m_H = 120$  GeV (full line),  $m_H = 180$  GeV (dashed),  $m_H = 240$  GeV (dotted),  $m_H = 1000$  GeV (dashed-dotted).

$$g\bar{g} \rightarrow t\bar{t}$$



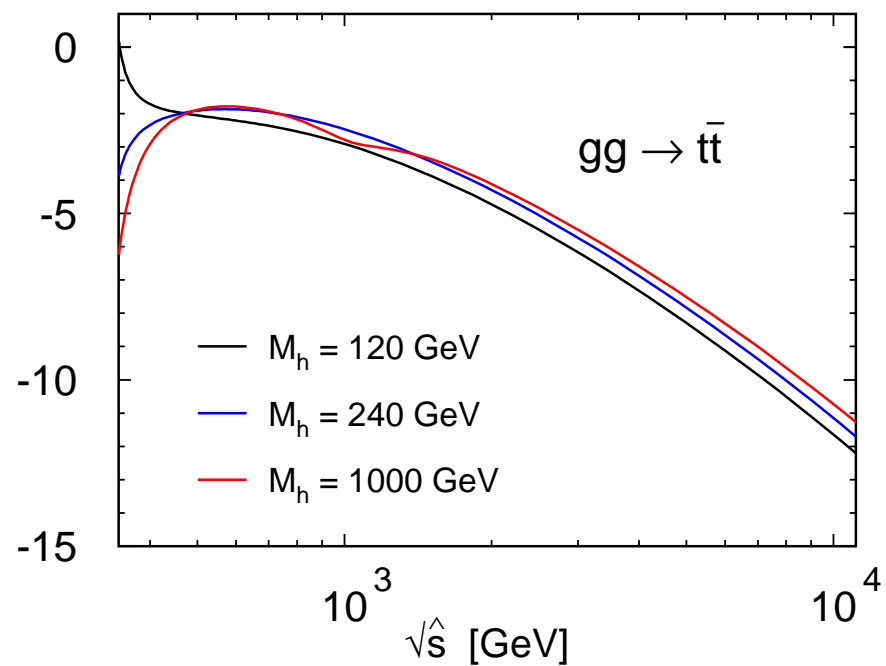
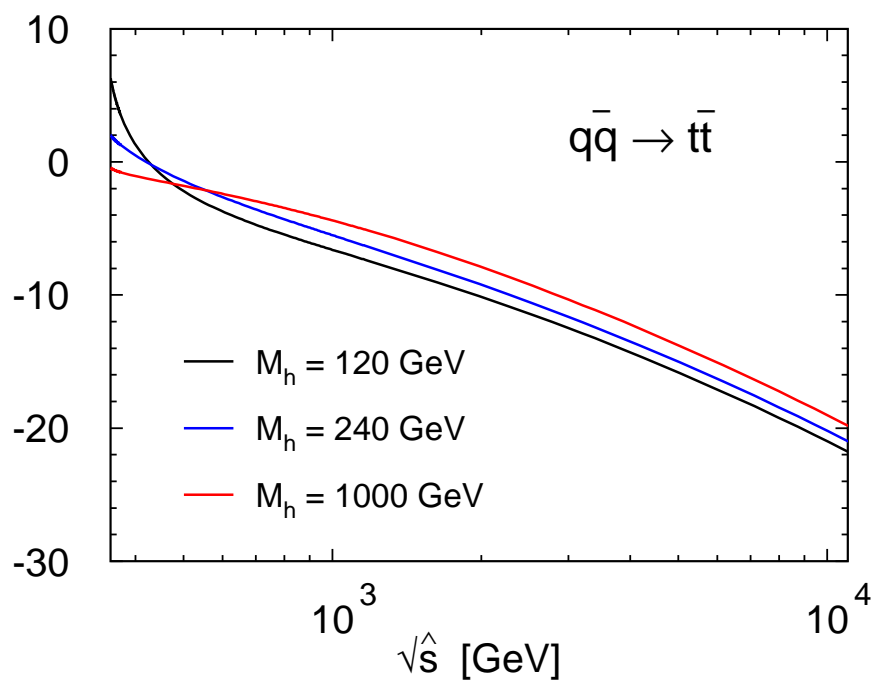
Different contributions to the weak corrections: vertices (long-dashed), self-energies (dashed), boxes (dotted), triangles (dash-dotted). The sum is shown as the full line.

Corrections for  $q\bar{q}$  larger:

Weak charge of  $q\bar{q}$  and  $t\bar{t}$  vs  $g\bar{g}$  and  $t\bar{t}$ .

large corrections for large  $\sqrt{\hat{s}}$

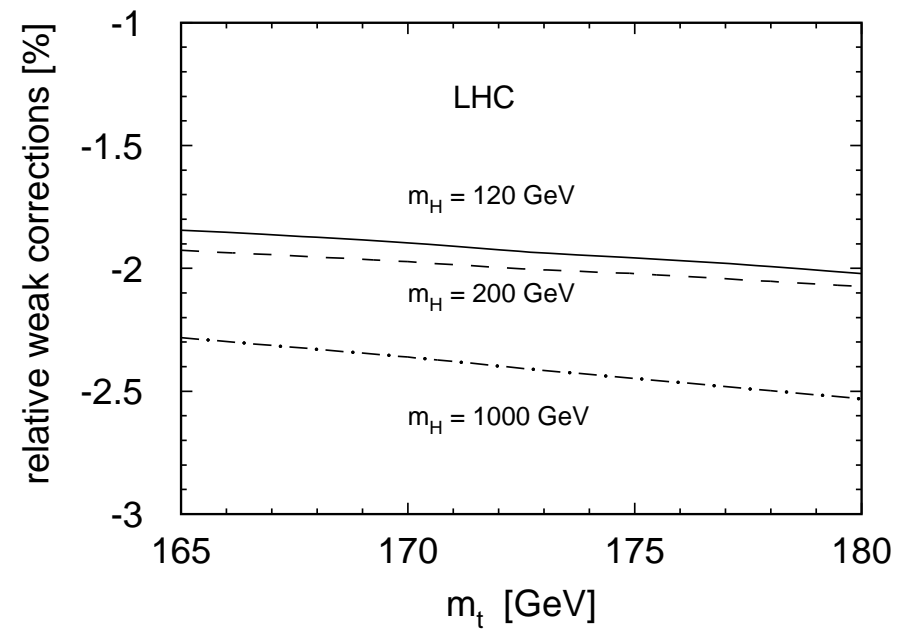
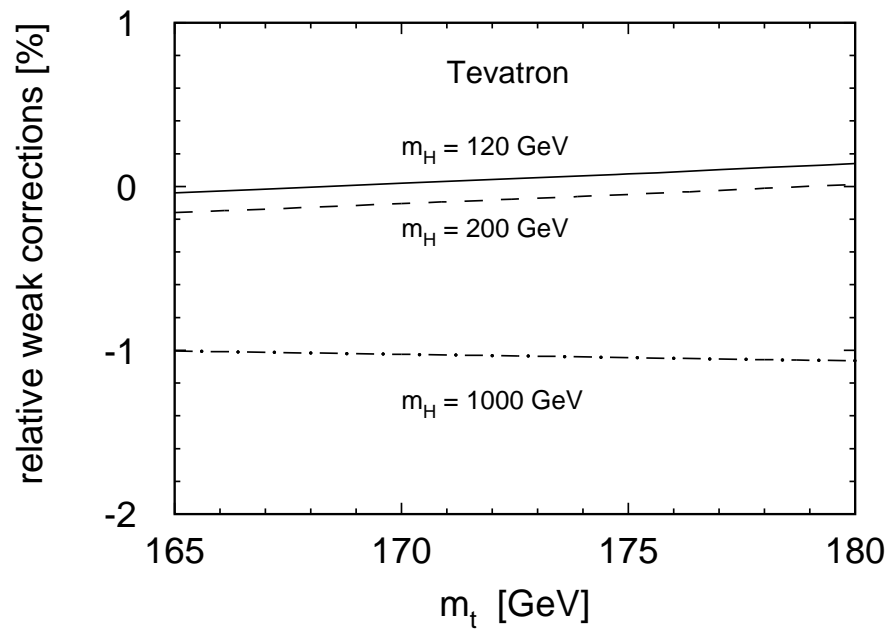
sizable  $M_h$ -dependence



(relative weak corrections [%])

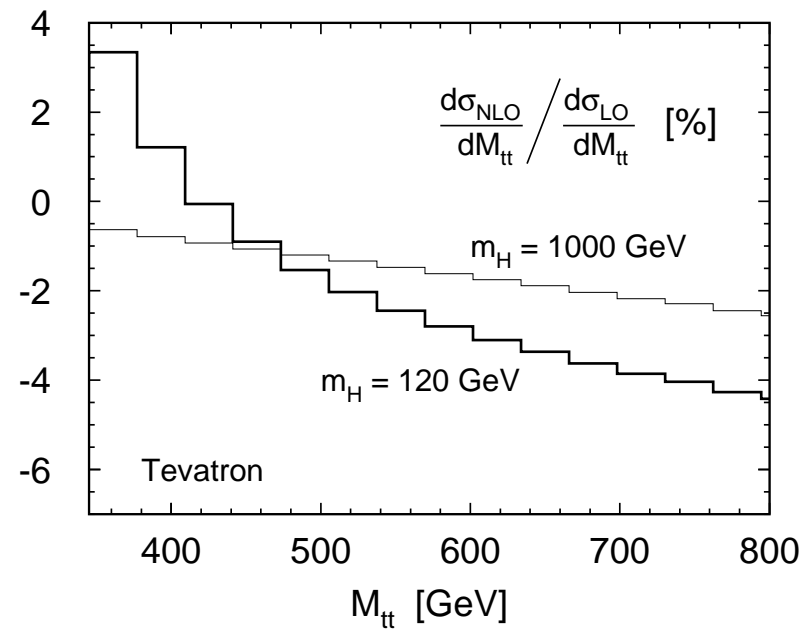
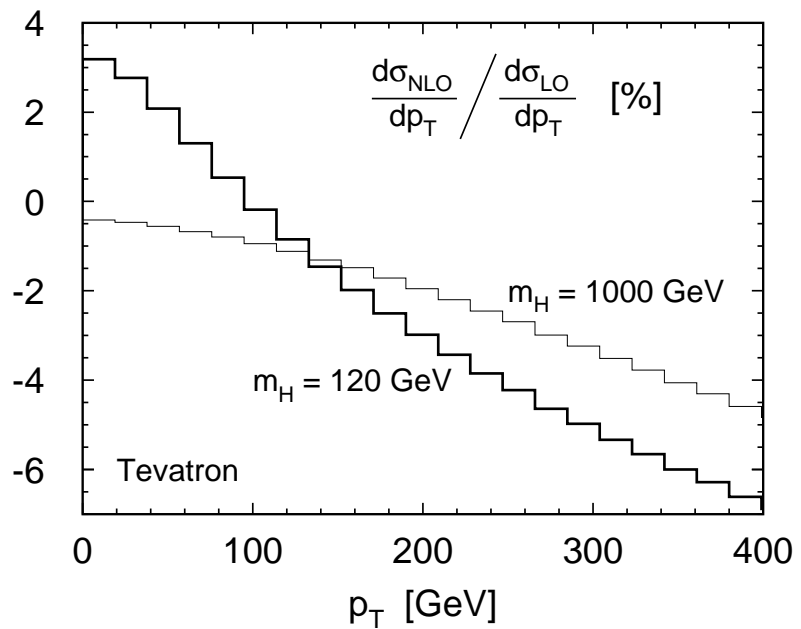
## II. Tevatron and LHC

Small effects for total cross section  
(dominated by  $\sqrt{\hat{s}} \sim 360\text{-}380$  GeV)



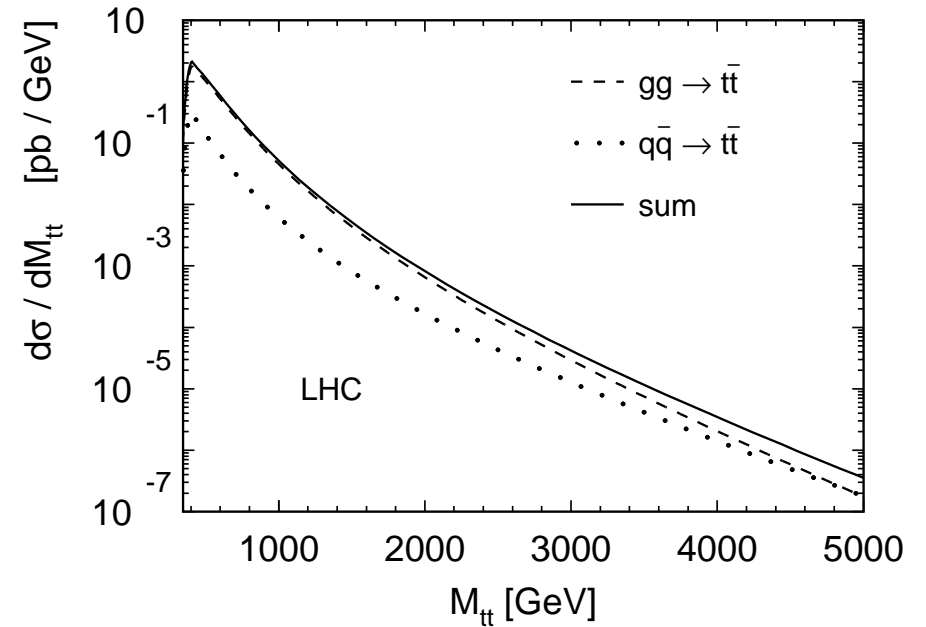
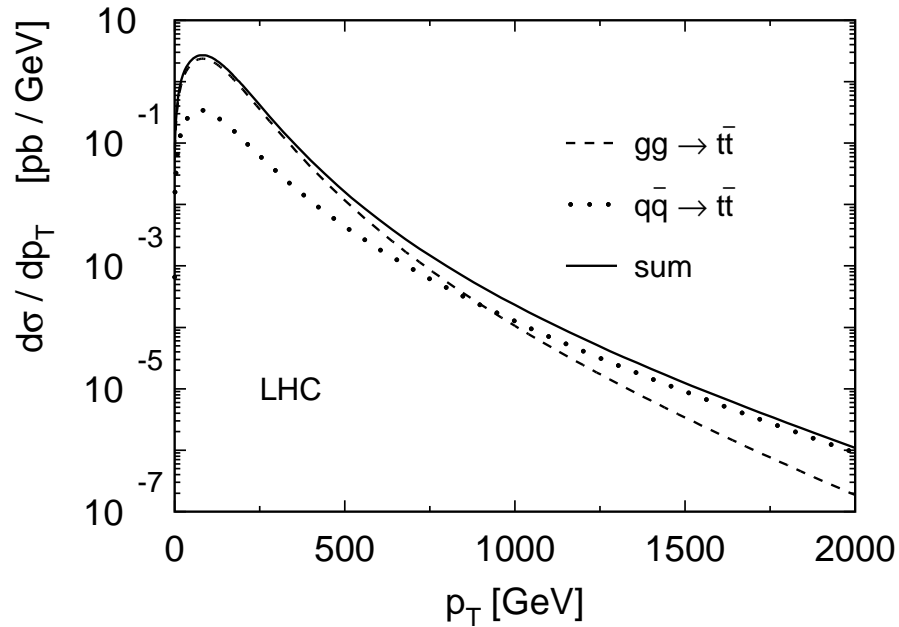
# Sizeable effects for differential distribution

## TEVATRON



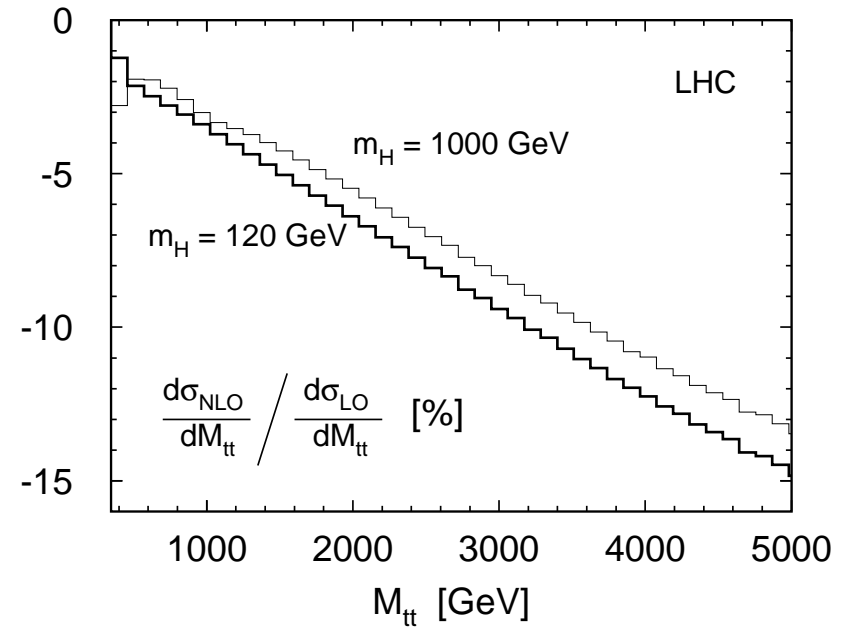
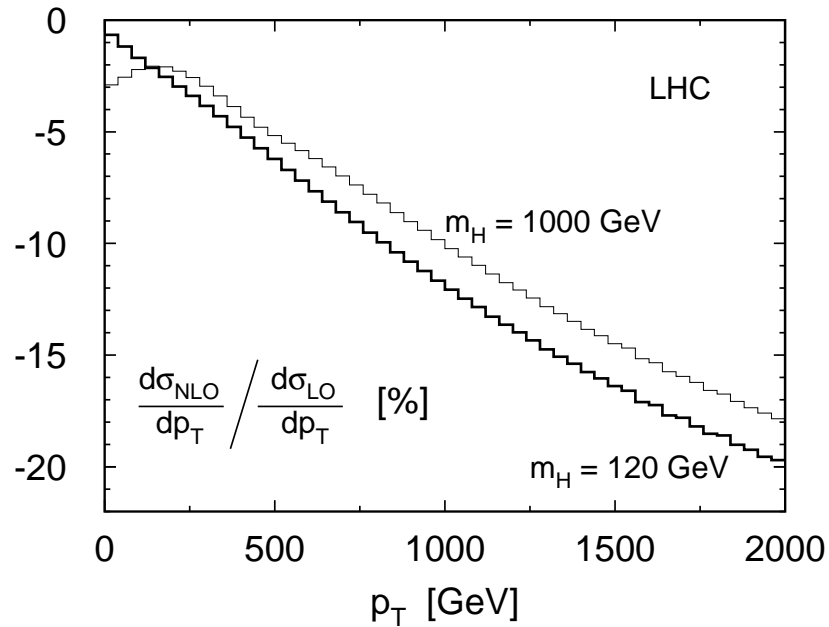
# LHC

Relative composition of  $q\bar{q}$  vs  $gg$  induced reactions



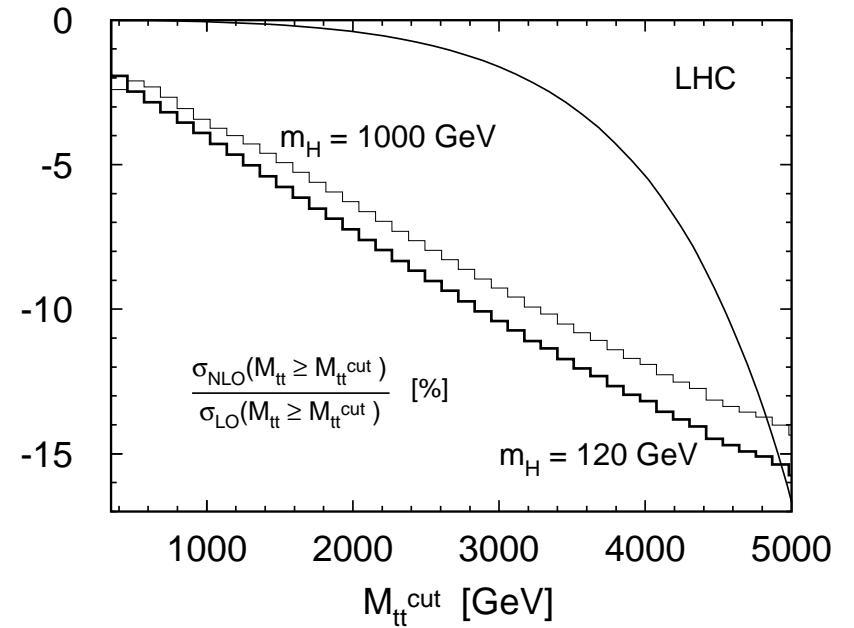
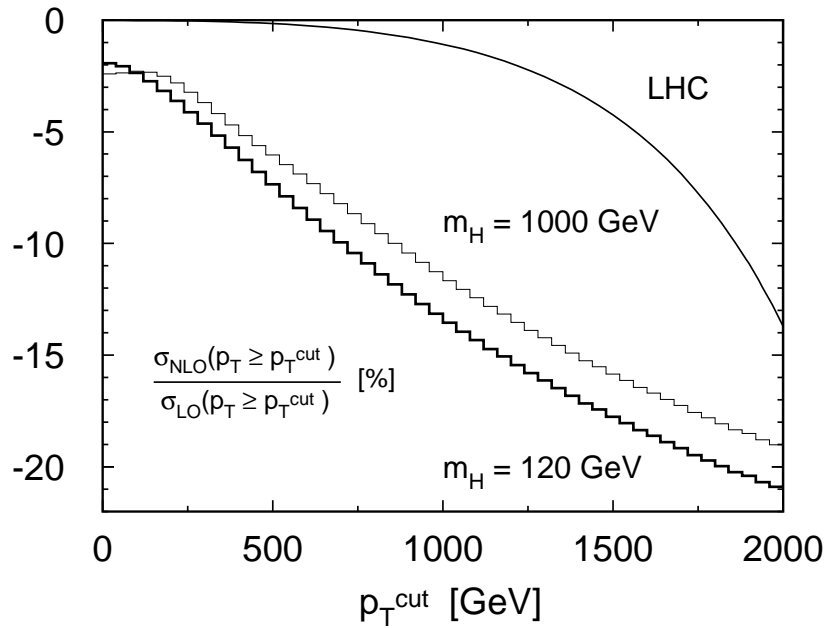
Leading-order differential cross section for the LHC as a function of  $p_T$  and  $M_{t\bar{t}}$ . Shown is the sum (full) and the contributions from gluon fusion (dashed) and quark–antiquark annihilation (dotted).

# LHC



The relative corrections to the  $p_T$  and  $M_{t\bar{t}}$  distribution for the LHC for  $m_H = 120$  GeV (bold histogram) and  $m_H = 1000$  GeV (thin histogram).

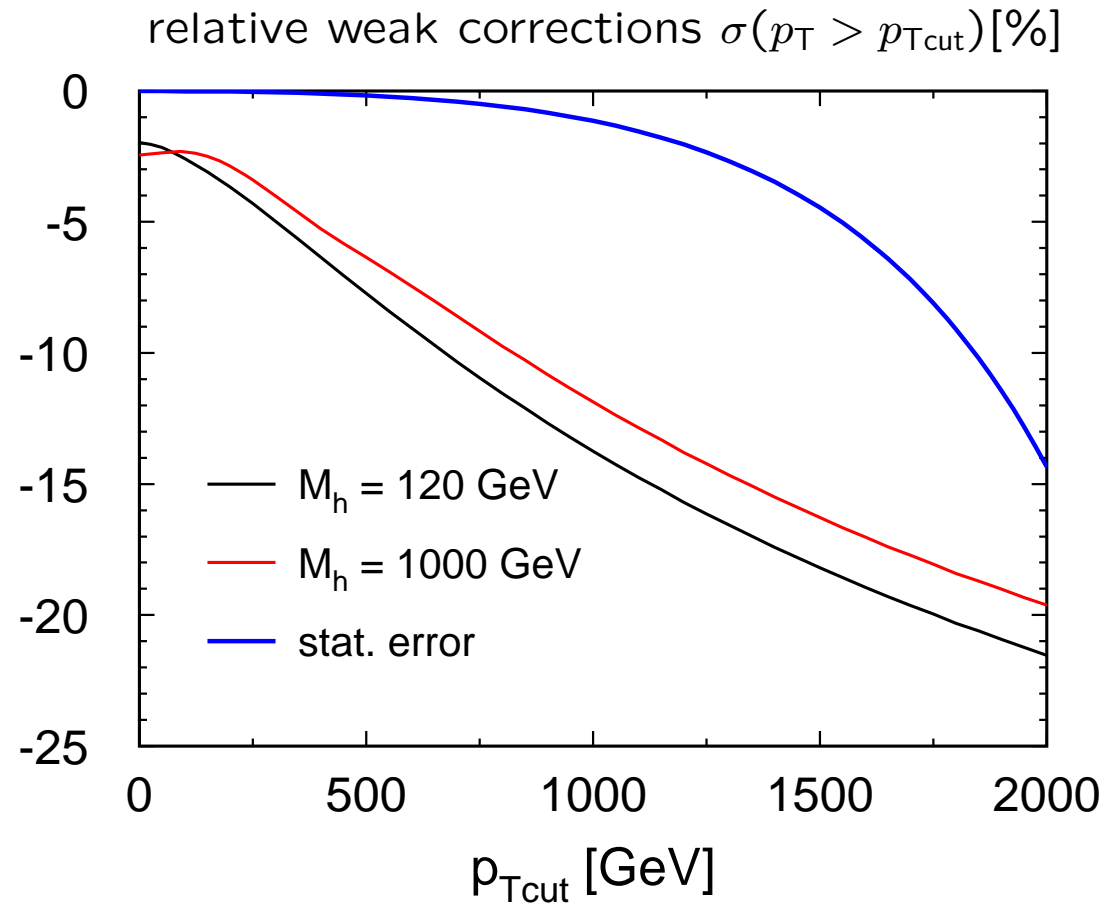
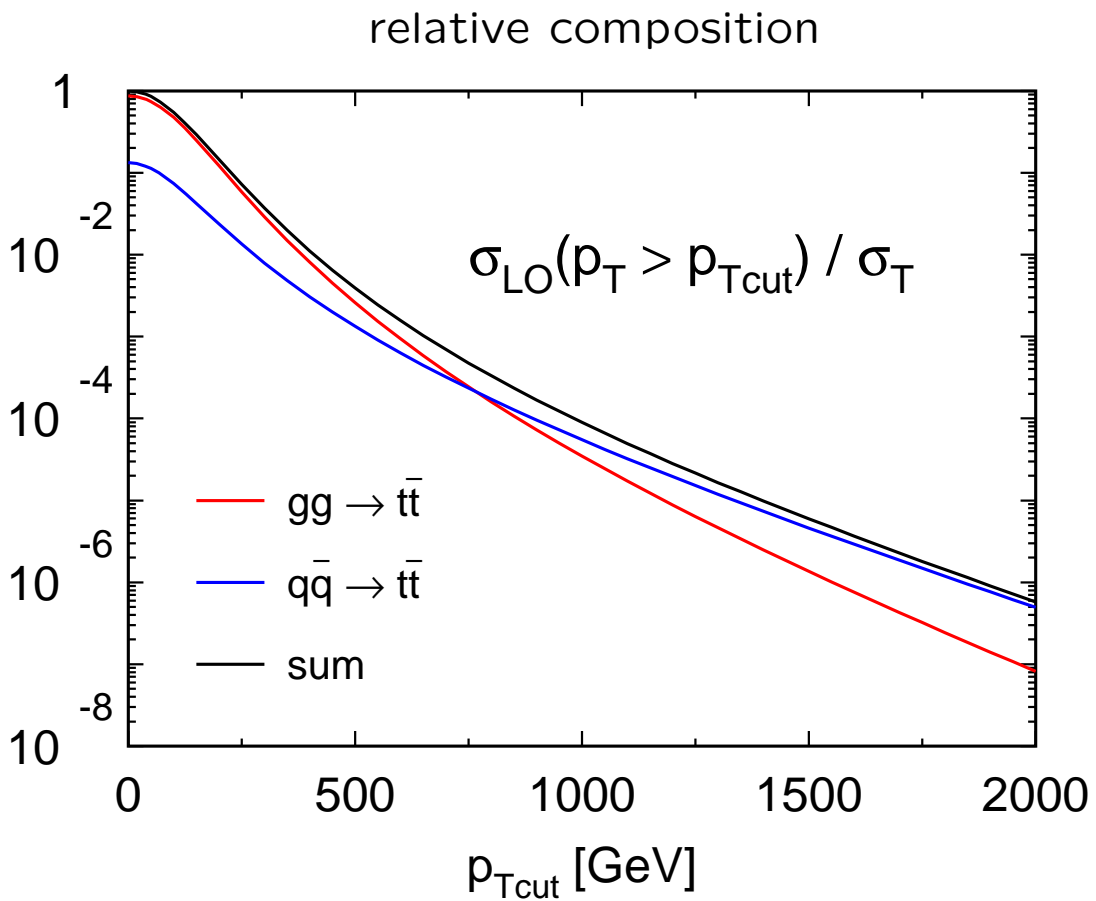
# LHC



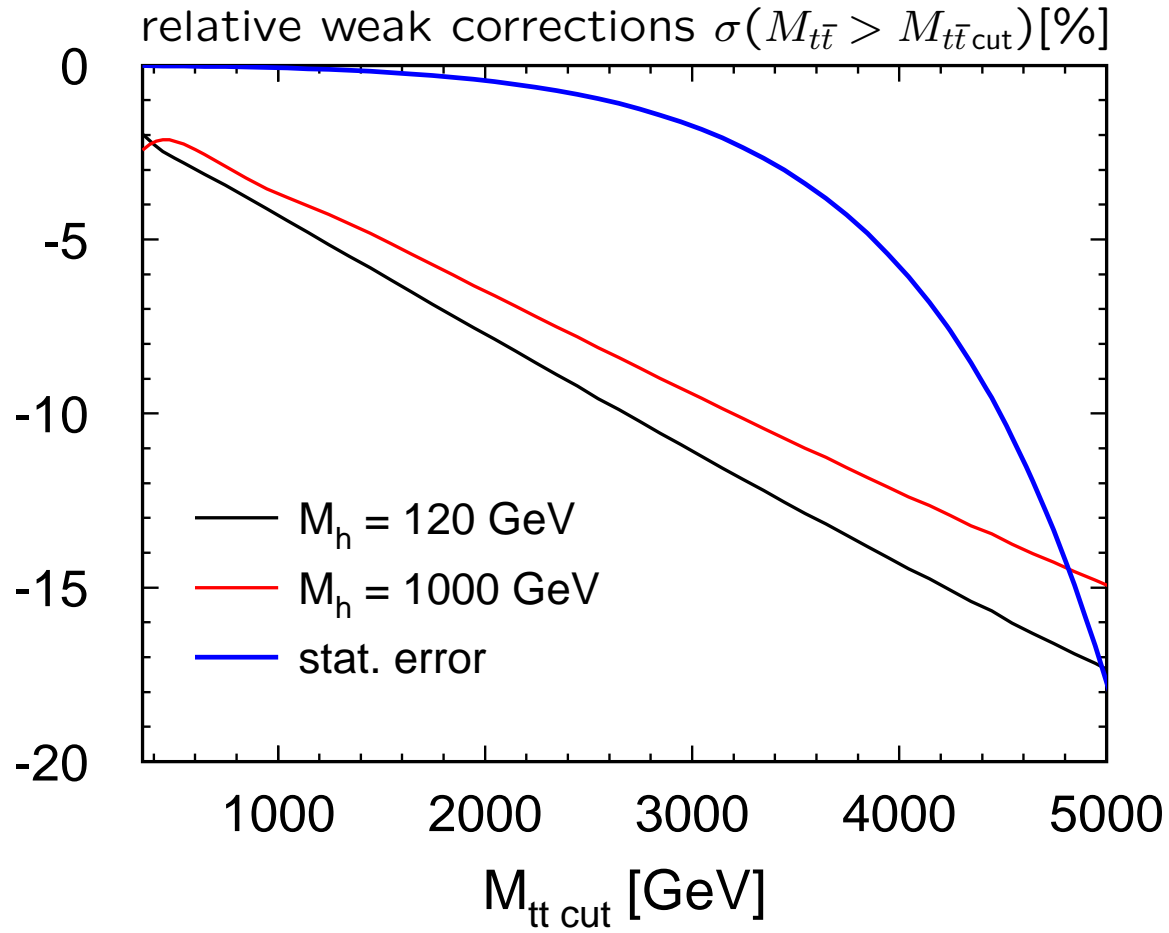
The relative corrections to the  $p_T$  and  $M_{t\bar{t}}$  distributions, integrated from a lower value in  $p_T$  and  $M_{t\bar{t}}$  to the kinematic limit, for the LHC and two Higgs masses ( $m_H = 120$  GeV (bold histogram),  $m_H = 1000$  GeV (thin histogram)). The smooth curve gives an estimate of the corresponding statistical uncertainty for an integrated luminosity of  $200 \text{ fb}^{-1}$ .



# Transverse momentum dependence (LHC)



# $M_{t\bar{t}}$ -dependence (LHC)



## IV. Conclusions on weak corrections

- LHC will explore the TeV-region:  $\hat{s}/M_W^2 \gg 1$
- electroweak corrections amount to  $\mathcal{O}(10\% - 20\%)$  in the interesting kinematic region
- top-quark distributions at large  $\hat{s}$  are strongly modified
- sizable  $M_h$ -dependence for small  $p_T$

# **B. CHARGE ASYMMETRY in HADROPRODUCTION and AXIGLUONS**

J.K., G. Rodrigo: PRL 81, 49 (1998)

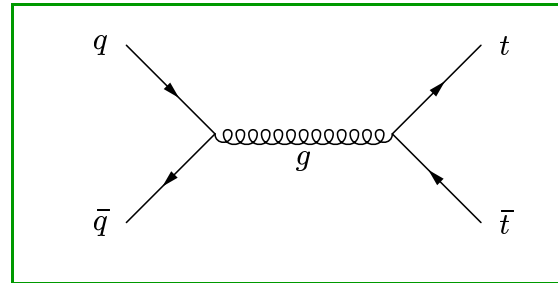
PRD 59, 054017 (1999)

O. Antuñano, J.K., G. Rodrigo: PRD 77, 014003 (2008)

- I. Motivation and Main Idea
- II. Results at Partonic Level
- III. Asymmetries at Tevatron and LHC
- IV. Limits on Axigluons

# I MOTIVATION and MAIN IDEA

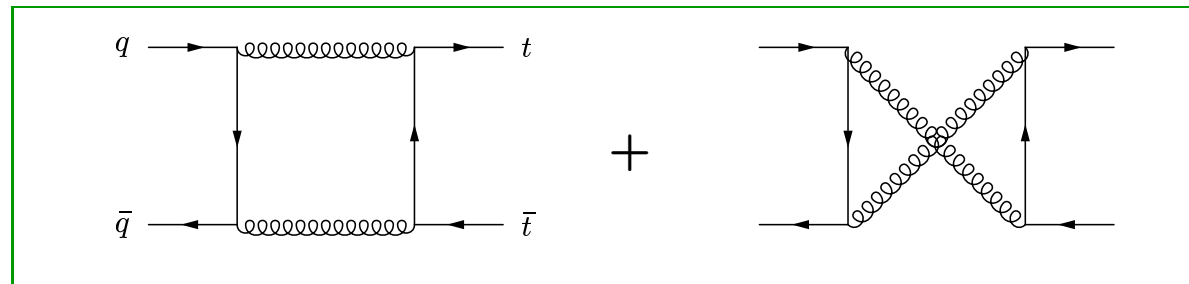
dominant process for  $t\bar{t}$  production ...



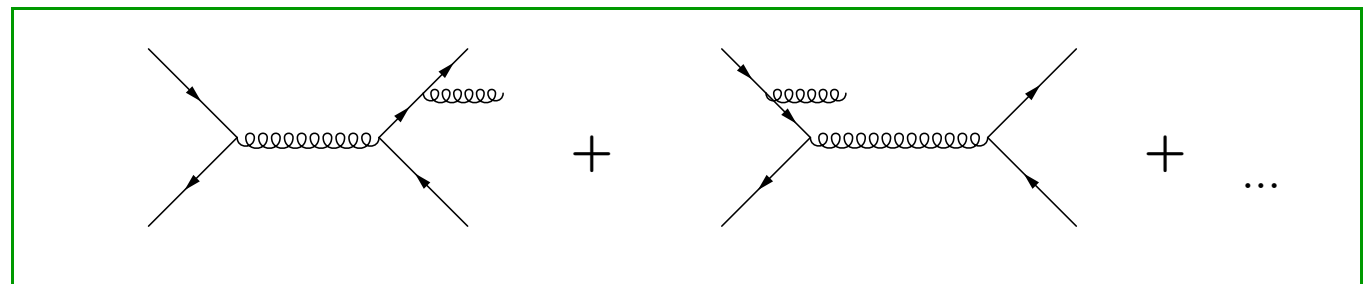
... is symmetric:

$$\frac{d\sigma}{d\cos\hat{\Theta}} \propto \left(1 + \frac{4m^2}{Q^2}\right) + \left(1 - \frac{4m^2}{Q^2}\right) \cos^2\hat{\Theta}$$

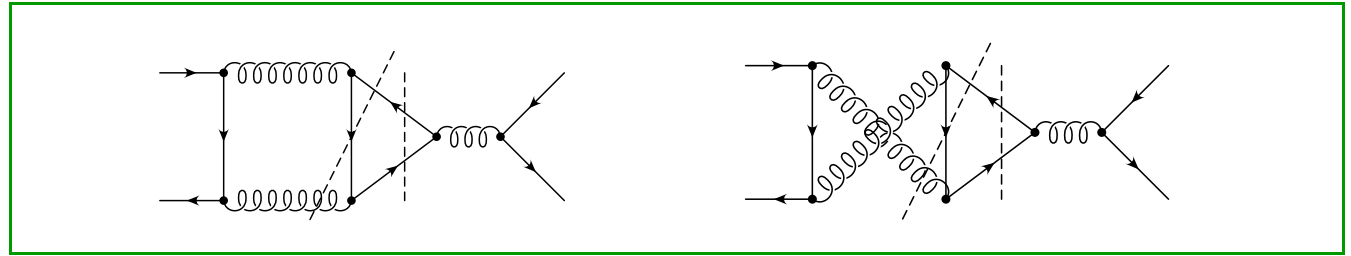
$\mathcal{O}(\alpha_s)$  corrections:  
virtual gluons



real emission



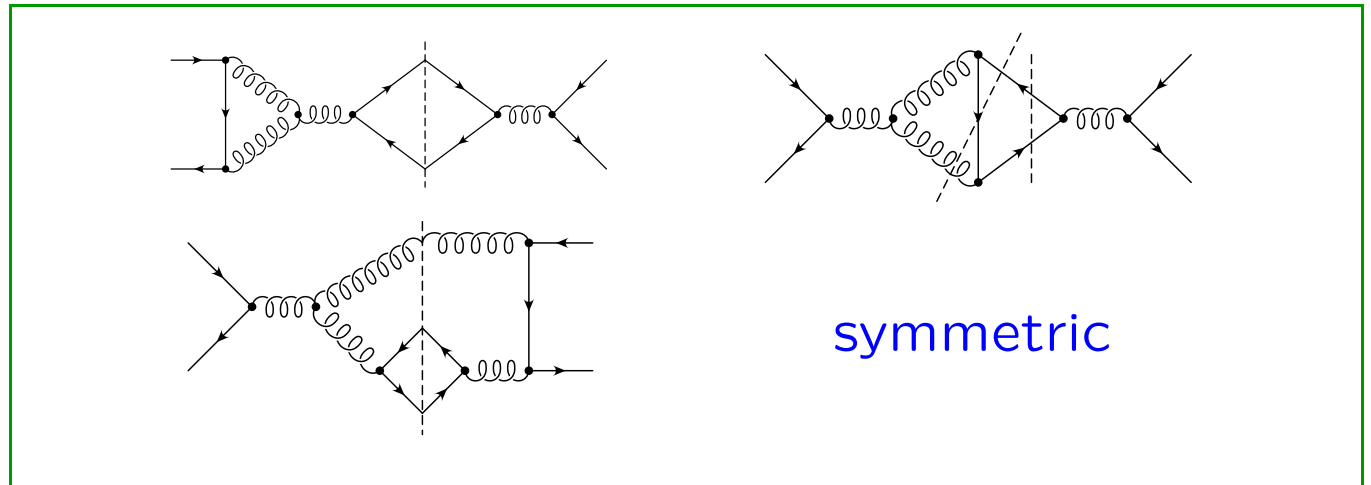
Interference between  
 $C = +1$  and  $C = -1$   
 amplitudes



⇒ charge asymmetry  
 similar to QED!

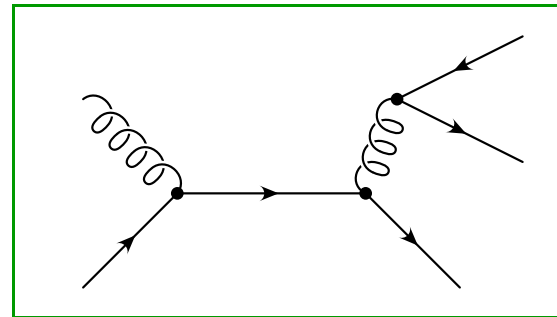
$$d\sigma(q\bar{q} \rightarrow QX) - d\sigma(q\bar{q} \rightarrow \bar{Q}X) \neq 0$$

Nonabelian terms:



similarly (“flavour excitation”)  
 numerically unimportant

$$d\sigma(qg \rightarrow QX) - d\sigma(qg \rightarrow \bar{Q}X) \neq 0$$



real and virtual corrections must be combined to  
obtain sensible (=IR-finite) result

⇒ forward-backward asymmetry of top quarks  
in  $p\bar{p}$  collisions (TEVATRON)

⇒ difference in rapidity distributions between  $t$   
and  $\bar{t}$  in  $pp$  collisions (LHC)

⇒ test of production mechanism

⇒ potential confusion with asymmetry from  
weak production avoided

## Intuitive picture

inclusive cross section

top and light quark in same direction  
preferred coherence with gluon field!

⇒ positive asymmetry for  
inclusive cross section

$t\bar{t}g$

probability for gluon emission enhanced  
if  $t$  and  $q$  in opposite direction

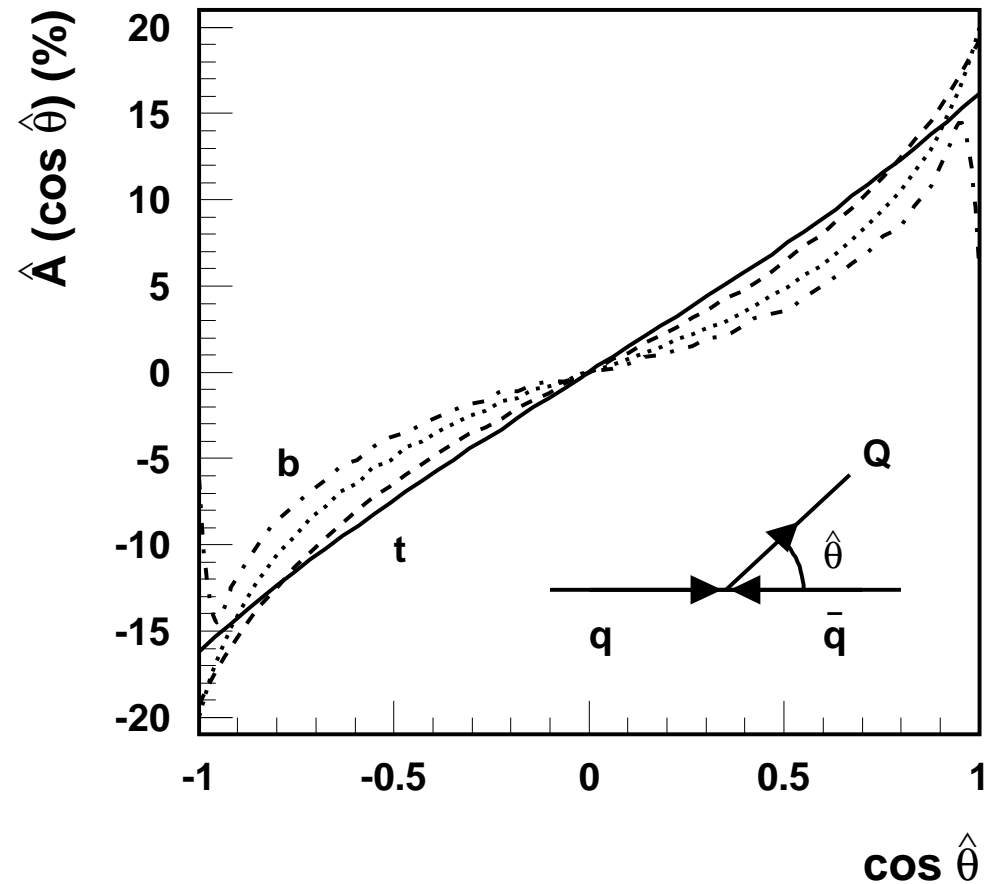
⇒ negative asymmetry for  $t\bar{t}g$   
(tagged events)



## II PARTONIC LEVEL

differential asymmetry  
( $q\bar{q}$  induced)

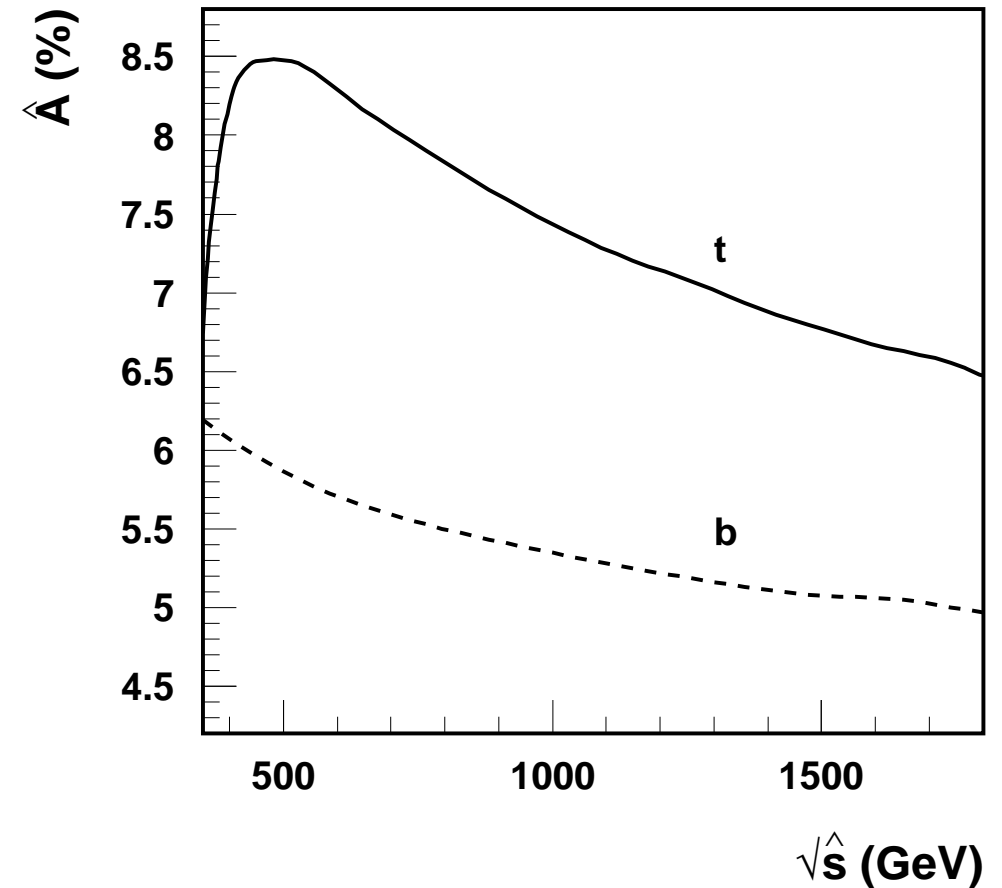
$$\begin{aligned}\hat{A}(\cos\hat{\Theta}) &= \frac{N_t(\cos\hat{\Theta}) - N_{\bar{t}}(\cos\hat{\Theta})}{N_t(\cos\hat{\Theta}) + N_{\bar{t}}(\cos\hat{\Theta})} \\ &= \frac{N_t(\cos\hat{\Theta}) - N_{\bar{t}}(-\cos\hat{\Theta})}{N_t(\cos\hat{\Theta}) + N_{\bar{t}}(-\cos\hat{\Theta})}\end{aligned}$$



integrated asymmetry  
(parton level)

as function of  $\sqrt{\hat{s}}$ :

$$\begin{aligned} & \hat{A}(\cos\hat{\Theta}) \\ &= \frac{N_t(\cos\hat{\Theta} \geq 0) - N_{\bar{t}}(\cos\hat{\Theta} \geq 0)}{N_t(\cos\hat{\Theta} \geq 0) + N_{\bar{t}}(\cos\hat{\Theta} \geq 0)} \\ &= \frac{N_t(\cos\hat{\Theta} \geq 0) - N_t(\cos\hat{\Theta} \leq 0)}{N_t(\cos\hat{\Theta} \geq 0) + N_t(\cos\hat{\Theta} \leq 0)} \end{aligned}$$



### III HADRONIC COLLISIONS

$$p\bar{p} \quad - \quad 1.96 \text{ TeV}$$

dominantly central production:

$$q\bar{q} \rightarrow t\bar{t}$$

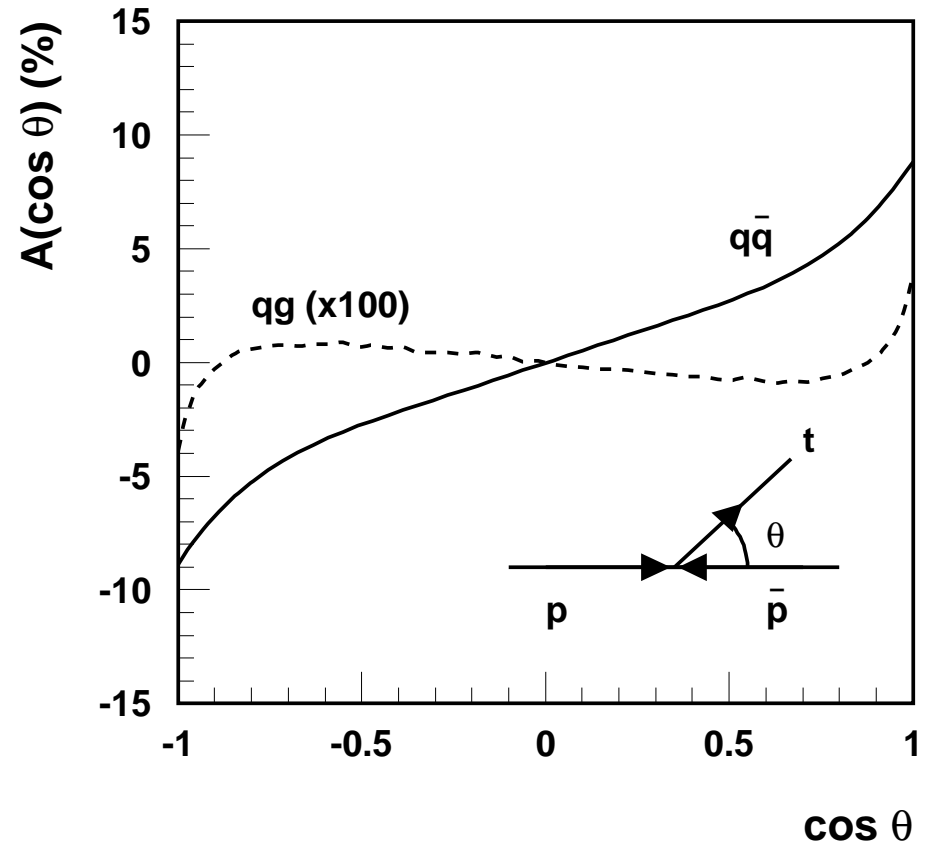
partonic asymmetry



hadronic asymmetry

⇒ Integrated asymmetry

$$\bar{A}_{fb} = 4.5 - 5.7 \% \quad (1.96 \text{ TeV})$$



Differential asymmetry:  $\mathcal{A}(Y)$

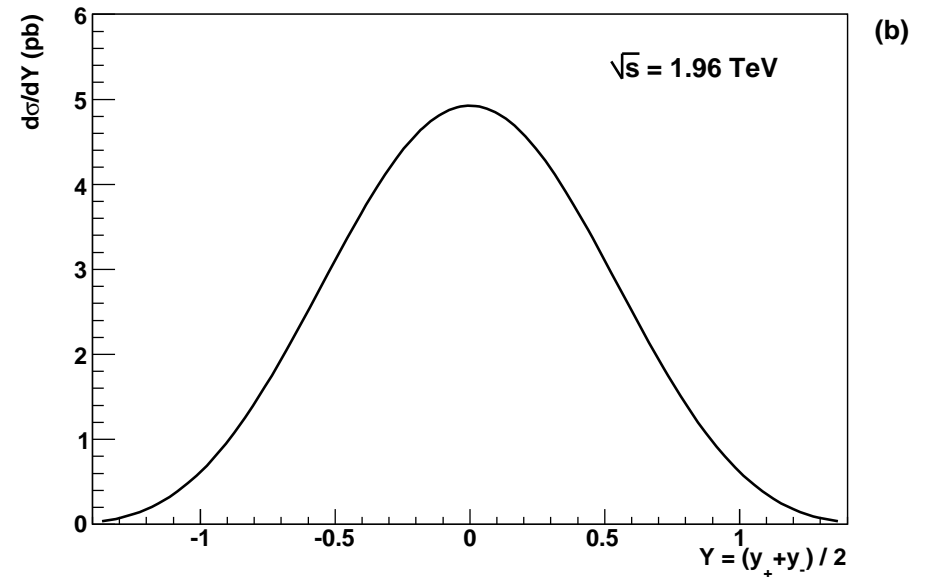
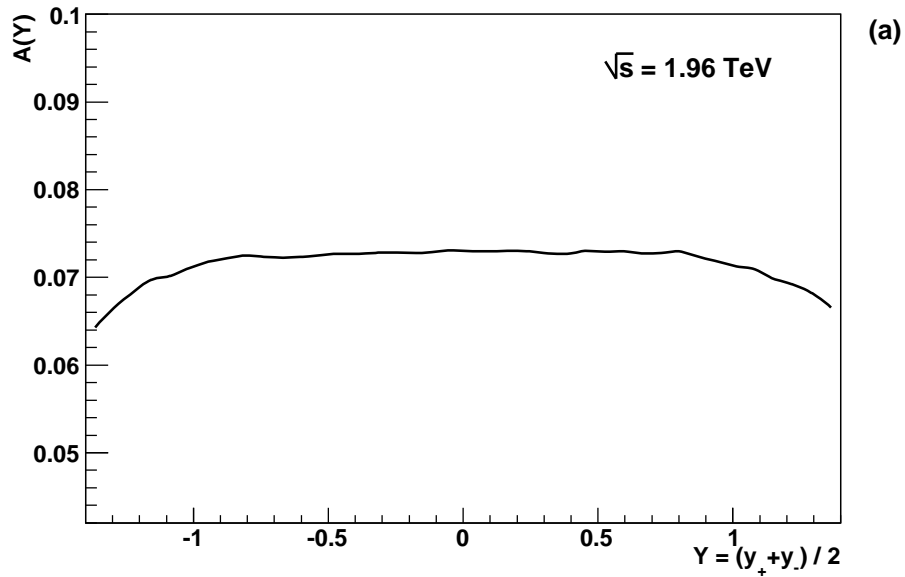
top rapidity  $y_+$  and anti-top rapidity  $y_-$  are known  
(in one event)

Average:  $Y \equiv \frac{1}{2}(y_+ + y_-)$

$$\mathcal{A}(Y) = \frac{N_{ev}(y_+ > y_-) - N_{ev}(y_+ < y_-)}{N_{ev}(y_+ > y_-) + N_{ev}(y_+ < y_-)}$$

nearly equivalent to partonic asymmetry

$Y \hat{=} \text{partonic rest frame!}$



$$\mathcal{A}_{total} \equiv \frac{N_{ev}(y_+ > y_-) - N_{ev}(y_+ < y_-)}{N_{ev}}$$

preliminary Tevatron results:

$$A_{FB} = 0.20 \pm 0.11 \pm 0.05$$

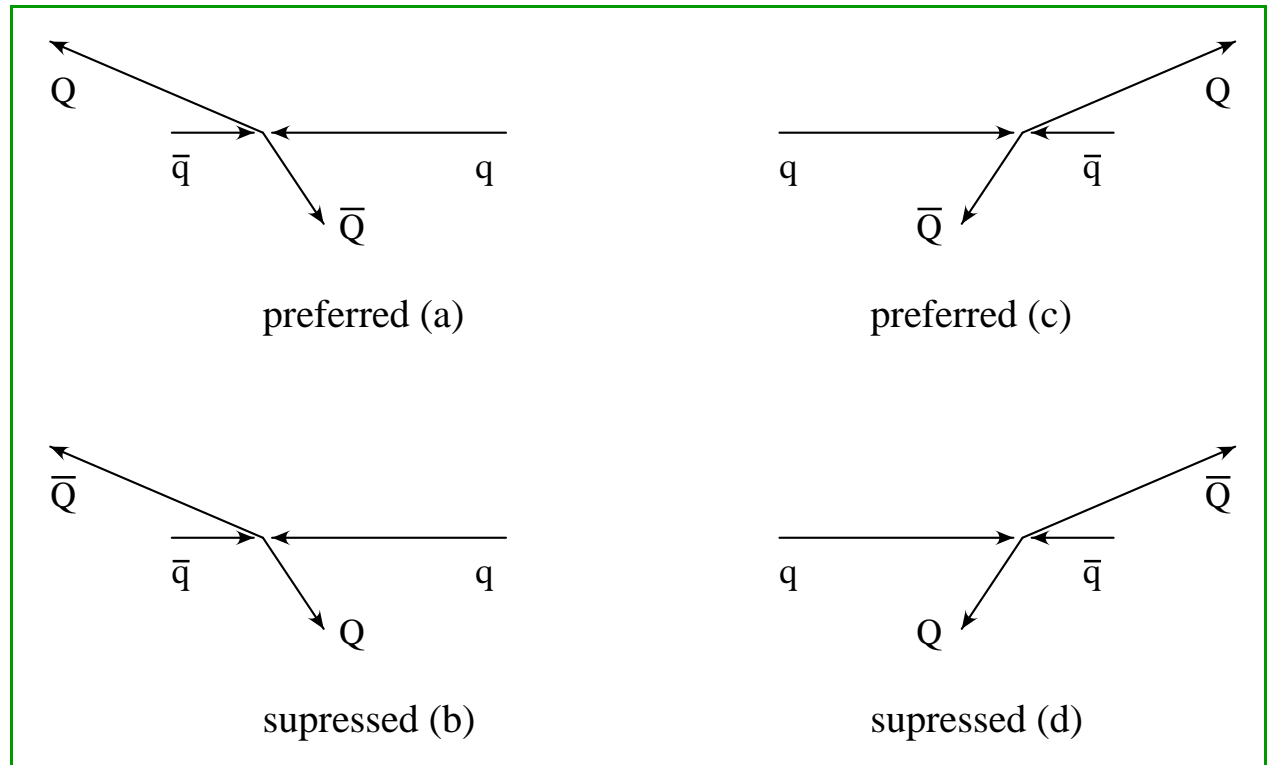
$$A_{total} = 0.23 \pm 0.12 \pm 0.06$$

## Comments

- inclusive asymmetry hardly affected by radiative corrections  
(Almeida, Sterman, Vogelsang)
- $t\bar{t}g$  asymmetry strongly affected by radiative corrections,  
sensitive to cuts (Dittmaier, Uwer, Weinzierl)

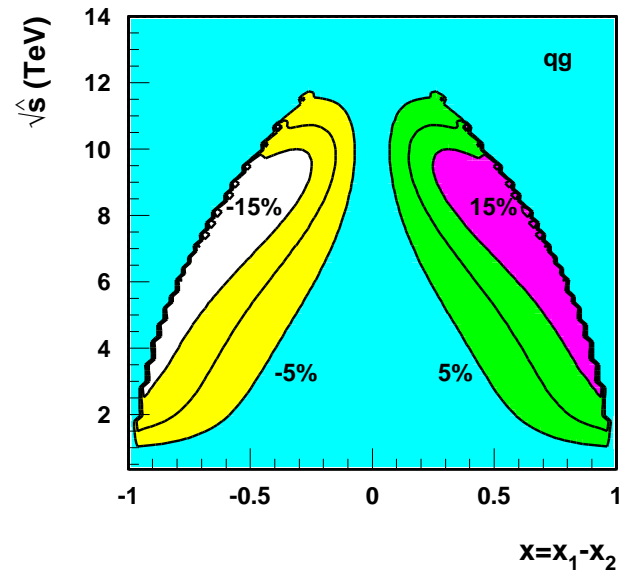
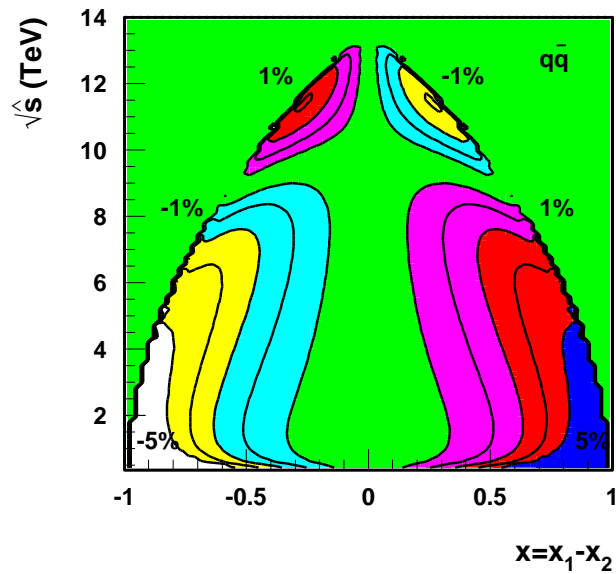
$pp$  – 14 TeV

- no forward backward asymmetry
- slight difference between rapidity distributions of  $Q$  and  $\bar{Q}$  from (small) admixture of  $q\bar{q}$  processes



- ⇒ more  $t$  at large rapidity
- ⇒ more  $\bar{t}$  at small rapidity

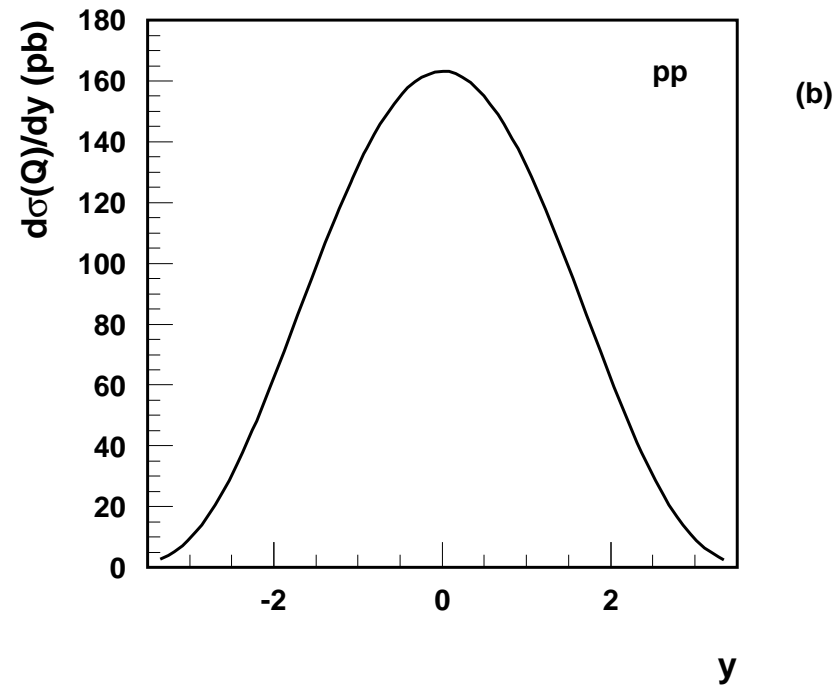
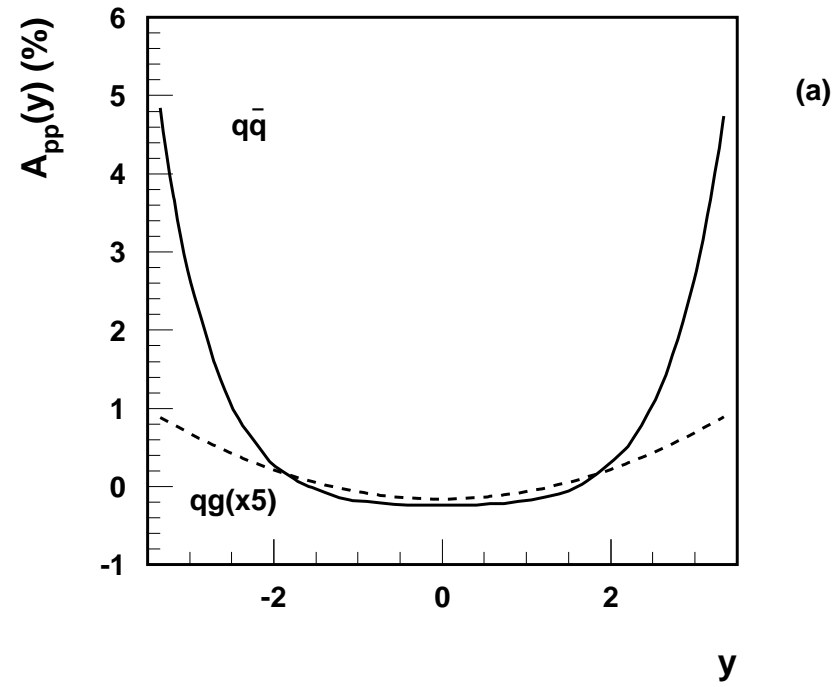
main effect in regions of small cross section



$t\bar{t}$  production in proton-proton collisions (LHC) is forward-backward **symmetric** in the laboratory frame.

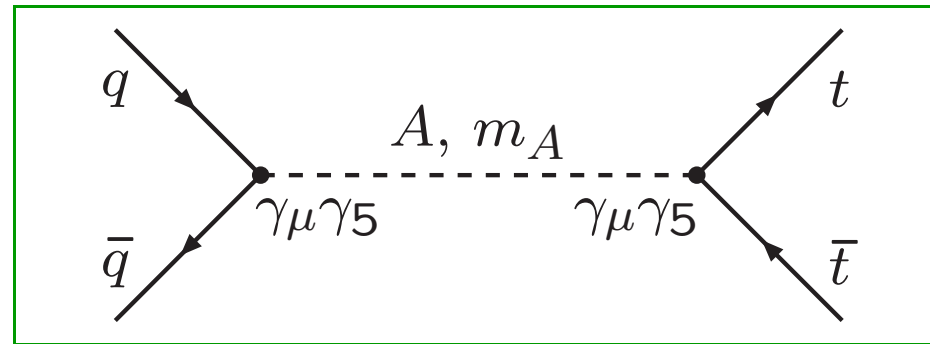
- Select the invariant mass of the  $t\bar{t}(+g)$  system and its longitudinal momentum.
  - For some extreme kinematic regions, large  $x$  and/or large  $\hat{s}$  (in practice  $\hat{s} < 2\text{TeV}$ ), sizable asymmetry reconstruction of the  $t\bar{t}(+g)$  rest frame required!!!



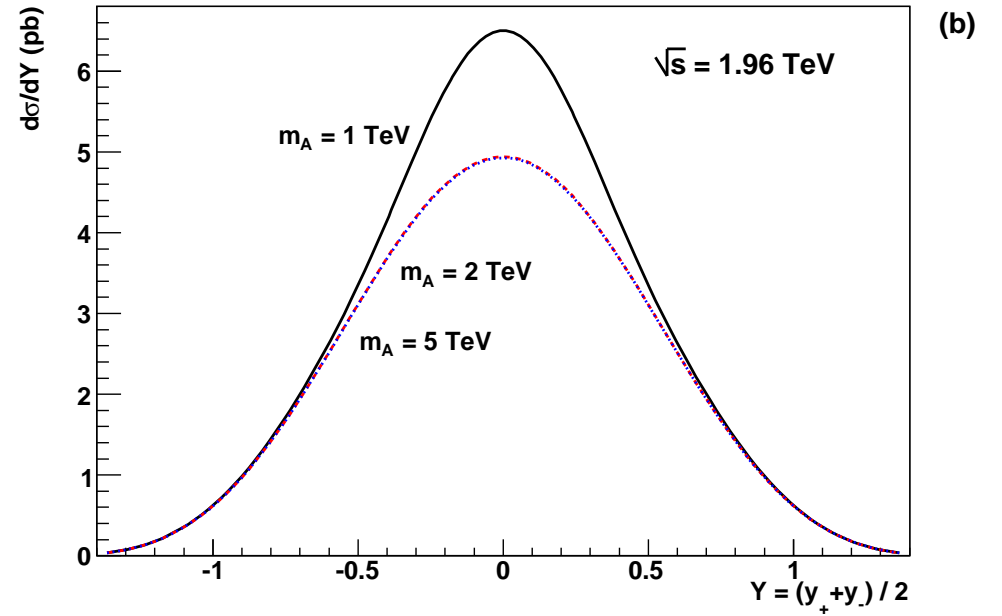
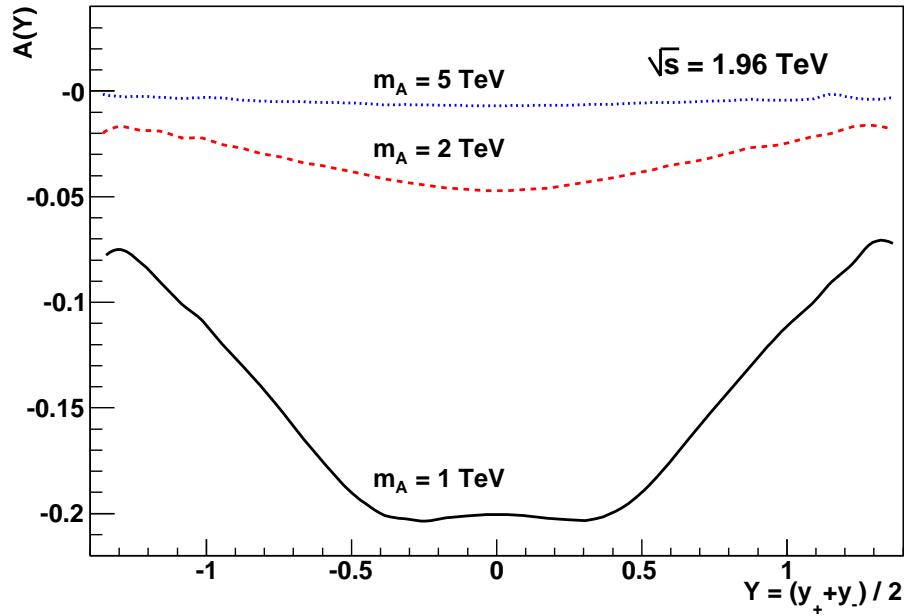


Leading  
order!

## IV Limits on Axiguons

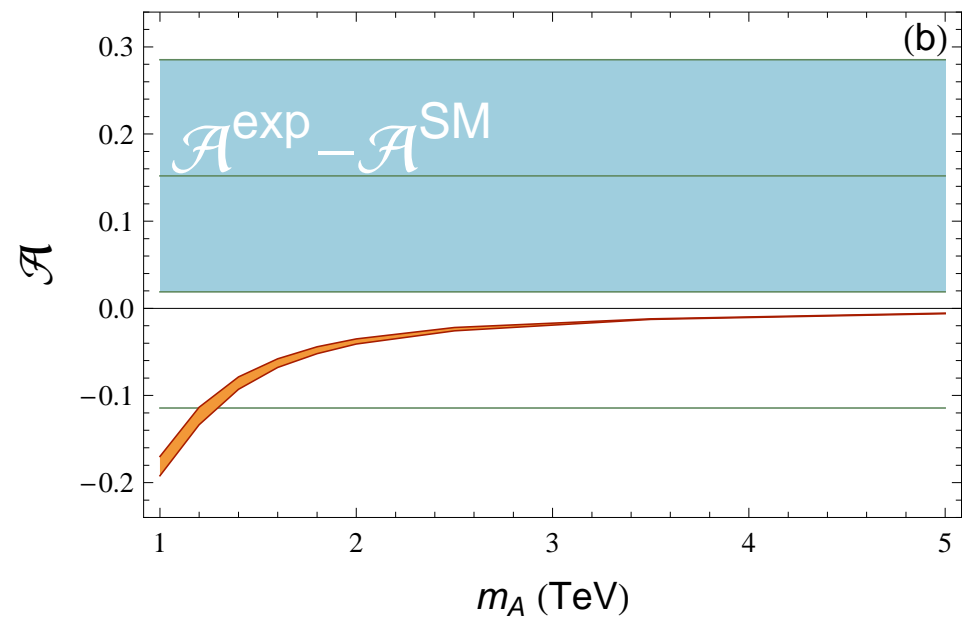
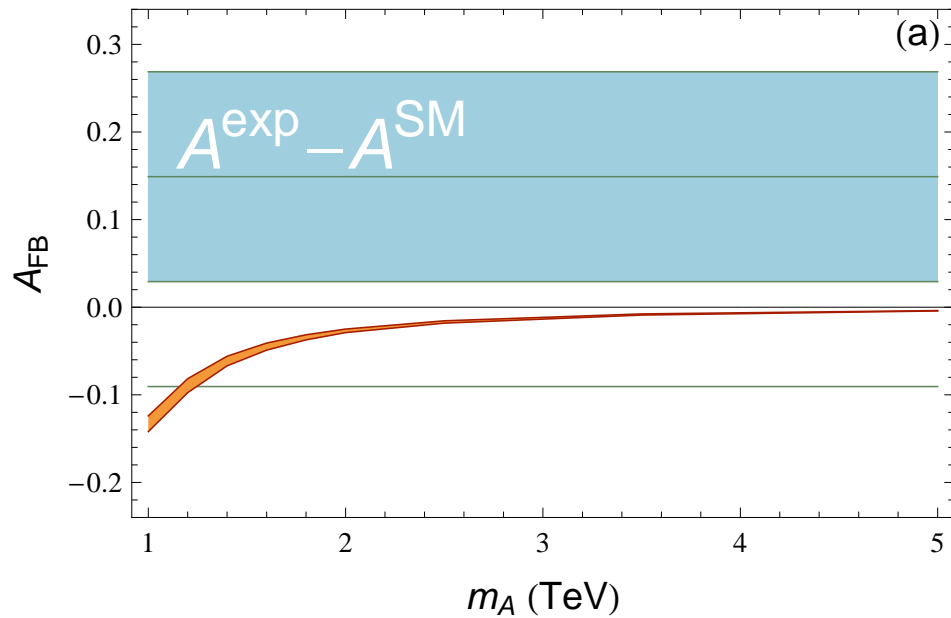


- $\Rightarrow$  modified  $t\bar{t}$  production  
(resonance for  $m(t\bar{t}) = m_A$ )
- $\Rightarrow$  interference with gluon  
 $\rightarrow$  forward backward asymmetry



	QCD	$m_A = 1 \text{ TeV}$	$m_A = 2 \text{ TeV}$	$m_A = 5 \text{ TeV}$
$A_{FB}$	0.051(6)	-0.133(9)	-0.027(2)	-0.0041(3)
$A$	0.078(9)	-0.181(11)	-0.038(3)	-0.0058(4)

Preliminary Tevatron results



$m_A > 1.2$  TeV

at  $2\sigma$

## Summary

- ★ forward backward asymmetry for  $t$  production at TEVATRON  $\sim 7\%$
- ★ important test of production mechanism
- ★ unique possibility for  $p\bar{p}$  collider
- ★ differences between  $t$  and  $\bar{t}$  distributions at LHC mainly in regions of small cross section (large rapidity!)
- ★ access to “new physics” signal for axiguons