

# Azimuthal correlations in hadronic collisions from instabilities of the initial state

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Scaling of  $\nu_2$

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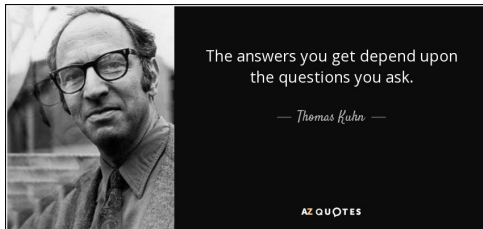
Conclusions

# Could $v_2$ have nothing to do with hydrodynamics?

Hydrodynamics is a very beautiful, consistent, and fruitful theory capable of generating precise quantitative predictions from a (not so small!) set of parameters. The great majority of practitioners in our field are convinced, for good reasons, the correlations observed in heavy ion collisions are hydrodynamical in origin

- An ecology of alternative ideas is always good
- Hydrodynamics also has some unsolved puzzles to deal with!

# A very short detour into philosophy...



Science is done via two basic mechanisms...

**Puzzle-solving within a paradigm** using accepted assumptions to draw conclusions

**Paradigm shifts** questioning the assumptions and trying to look for new ones

Switching typically happens when the "weight of the puzzles" becomes too much and someone finds a set of assumptions that makes them go away A good scientist should be good at both, **a great scientist should know when to switch**

# Elliptic flow $\nu_2$ (Harmonic flow $\nu_n$ )

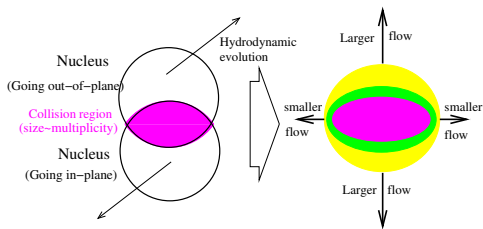


Figure : A geometrical view of elliptic flow.

Elliptic flow is parametrized as the  $n = 2$  Fourier component in the  $p_T$  distribution of the produced particles:

$$\frac{dN}{dp_T dy d\phi} = \frac{dN}{dp_T dy} \left[ 1 + \sum_{n=1}^{\infty} 2\nu_n(p_T) \cos(\phi - \phi_{0n}) \right] \quad (1)$$

# Elliptic flow $\nu_2$ (Harmonic flow $\nu_n$ )

One of the main experimental results in heavy-ion collisions (HIC) is:

*Elliptic flow* { **Def.-** Azimuthal dependence of the particle spectra on the reaction plane  $\phi_{0n}$ .  
**Interpretation.-** As matter in HIC behaves like a “perfect fluid” (extremely low viscosity), initial anisotropies in the collision area produce anisotropies in the collective flow of matter.

The interpretation is reasonable, but scalings in energy and system size of  $\nu_2$  look suspiciously simple compared to the Hydrodynamical picture.

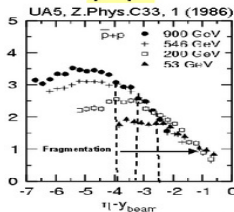
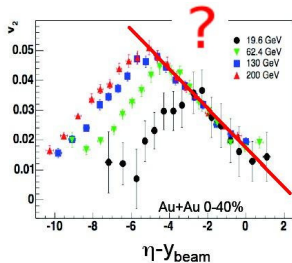
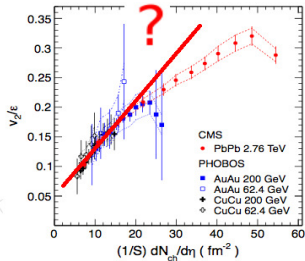
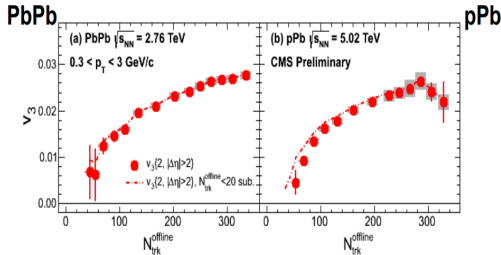
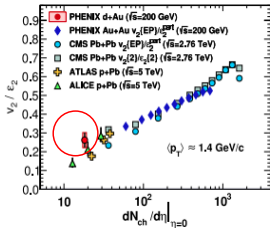


Figure : Elliptic flow  $v_2$  vs. rapidity [2,3].

$v_2$  response in region where temperature dramatically changes remarkably smooth, follows  $dN/dy$  exactly (as far as we can tell). EoS,  $\eta/s$  shouldn't.



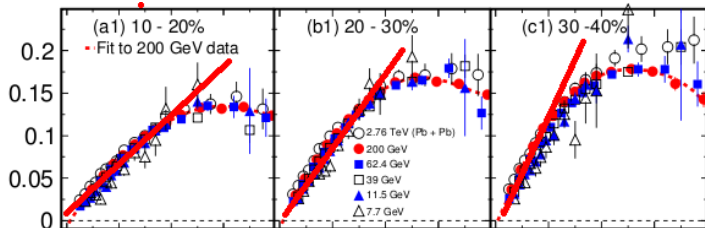
size effects also remarkably absent, down to  $pp$ .

Remember that hydro expansion around small

Knudsen number,  $Kn \sim \eta / (R \times s \times T)$ .

we should scan this, but we dont seem to!





Furthermore, rise in  $\nu_2$  seems entirely due to rise in  $\langle p_T \rangle$   
 !  $\nu_2(p_T)$  nearly constant Not what you'd expect in hydrodynamics or transport!  
 Kestin+Heinz (Hydro), Dunlop+Sorensen (AMPT)

Putting everything together we have

$$v_n(p_T) \simeq \mathcal{O}(1) \epsilon_n \underbrace{F(p_T)}_{\text{universal}}, \quad \langle v_n \rangle \sim \epsilon_n \underbrace{F(\langle p_T \rangle)}_{\langle p_T \rangle \sim \frac{1}{S} \frac{dN}{dy}}$$

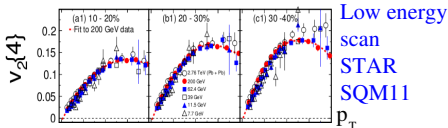
For a non-linear theory such as hydrodynamics we do not expect matrix below to be sparse.

$$\begin{pmatrix} dN/dy \\ \langle p_T \rangle \\ v_n \end{pmatrix} = \underbrace{\begin{pmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \\ \dots & \dots & \dots \end{pmatrix}}_{\eta/s, c_s, \tau_\pi, \dots} \times \underbrace{\begin{pmatrix} T_{\text{initial}} \\ L \\ \epsilon_n \end{pmatrix}}_{\rightarrow N_{\text{part}}, A, \sqrt{s}}$$

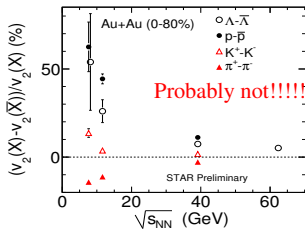
Analytical solutions (Hatta, Noronha, Xiao, GT) confirm this

# Particle species dependence is also strange

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Does this scaling hold by SPECIES?



Note that a lot of these effects do not arise by particle species but only when all species are counted. But

$$v_2 = \frac{\sum_i v_{2i}(T, m) n_i(T, \mu)}{\sum_i n_i(T, \mu)}$$

Why would this cancellation occur?  $\mu$  and  $m$  independent!

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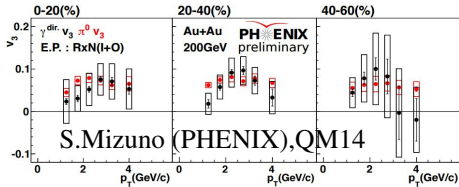
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# Photon vs hadron $v_n$



PHENIX, 1105.4126v2 (PRL)

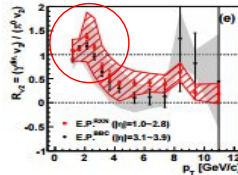


Figure : Photon  $v_3$  vs.  $p_T$  (red) and Proton  $v_3$  vs.  $p_T$  (black) [6]. Direct photon  $v_2$  similar! Why are they the same at low  $p_T$  ?

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# All these puzzles have (satisfactory?) explanations within the "standard model"

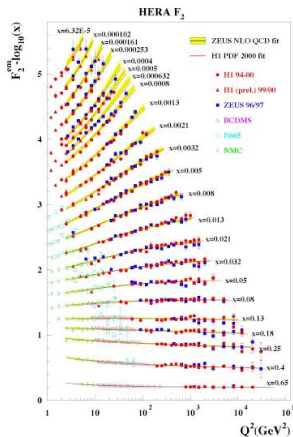
**photons** contaminated by final-state decays, boosted  
by **magnetic field based** mechanisms (**But**  
**why same as hadrons?**)

**small systems** origin of  $v_n$  in small, large systems  
different (CGC/antennae) **but why small**  
**and large systems scale?**

$v_2(p_T)$  vs  $\sqrt{s}$  many effects cancel out

All these are plausible, but not so elegant!

# What I find really funny!



All of these scalings really remind me of the scalings that imposed pQCD/partons over the then popular “bootstrap” models! **no reason within bootstrap for the scaling!**

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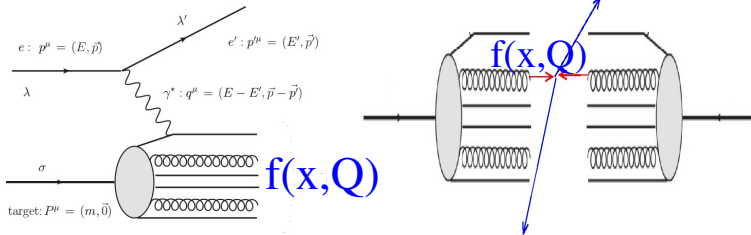
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# Parton distributions

Let's see Deep Inelastic Scattering



$$\frac{dN}{d^3p} = \int f(Q_1, x_1, \theta_1) f(Q_2, x_2, \theta_2) \sigma_{gg \rightarrow j}(xQ_1 - xQ_2, \theta_1 - \theta_2) D_{j \rightarrow i}(z) [xQ_1 - xQ_2]^2 dx_{1,2} dQ_{1,2} dz$$

The *probability* that the struck parton carries a fraction  $x_{Bj}$  of the proton momentum is called *parton distribution function*  $f(x, Q)$ . Same in eA, AA collisions

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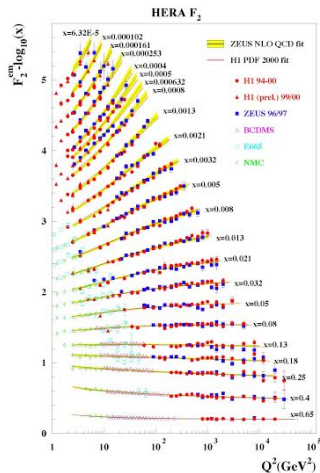
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## Bjorken scaling

Structure functions (PDFs, eventually GPDs) depend on the scale they are measured; i.e.  $x$  and  $Q^2$ . In the perturbative limit dependence on  $Q^2$  is subleading.

As  $p_T \sim Q$  and  $\eta \sim \ln(\frac{1}{x})$ , then scaling of elliptic flow in HIC may resemble Bjorken scaling when adding an angular dependence on the structure functions.





# Let us entertain a crazy idea

What if parton distribution functions became azimuthally asymmetric, but still kept the running we expect from QCD???

$v_2$  of Photons as expected,  $v_n$  would be an initial state effect!

Scaling in  $x, Q$  exactly as expected from Bjorken-like running

Particle species protected by unitarity of the fragmentation function

But there is a reason I called it crazy: PDFs are universal and QCD is azimuthally symmetric!

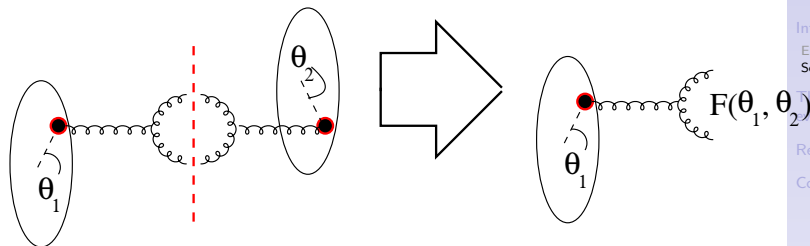
# Could structure functions be azimuthally asymmetric?

- Sivers functions (spin difference gives you an asymmetry)  
Not enough, uncorrelated with geometry
- "Color antennae" and such  
Since antenna point in random directions, **effect always goes away for large systems ("many antennae")**  
I think scaling implies Same origin for pA,AA
- Non-linearities in the full QCD evolution equation.  
Only solution I could think of that does not have these problems. Will shortly describe it now

# Could structure functions be azimuthally asymmetric?

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The running of  $f(x, Q)$  is really an RG equation,  $f(x, Q)$  probe dependent at subleading order in  $\alpha_s$ . At  $\mathcal{O}(\alpha_s^2 \epsilon_n) \ll \nu_n$  (2nd and higher Twist) they should generally be azimuthally asymmetric for extended probes. **Can this small effect be amplified?**

# The GLR-MQ evolution equation

In the dense parton limit, the equation that governs the evolution of parton distribution functions inside hadrons is thought to be given by

$$\frac{Q}{2} \frac{\partial}{\partial Q} \frac{\partial x G(x, Q^2)}{\partial \ln(1/x)} = \frac{\alpha_s N_c}{\pi} x G(x, Q^2) - \frac{\alpha_s^2 N_c \pi}{2 C_F S_\perp} \frac{1}{Q^2} [x G(x, Q^2)]^2 \quad (2)$$

(It is a high  $Q$  limit of an integro-differential (GLR) equation)

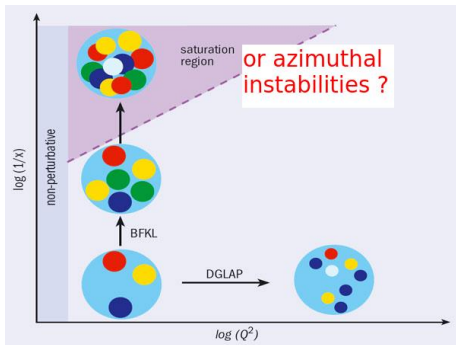
where

$x$ : Bjorken's  $x$

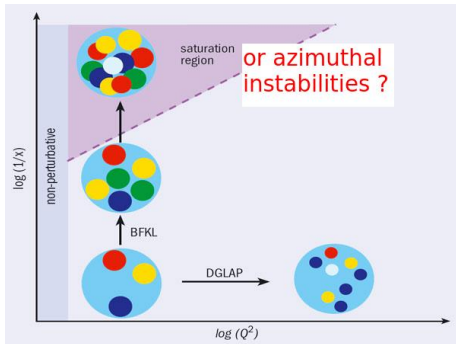
$Q$ : the photon's virtuality

The first term of eq. (2) is the BFKL evolution. This evolution breaks Forissart's bound at low  $x$ .

In order to correct this, a non-linear term is added. If you assume azimuthally symmetric evolution, you get saturation



Saturation together with an RG picture for saturation  
generates JIMWLK action, CGC (**JIMWLK/CGC result** :  
Azimuthally symmetric action, asymmetric  
boundary conditions)



But non-linear 2+1 differential equation *can have instabilities* breaking the underlying symmetry!

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# Our proposal

Adding an angular dependence the GLR-MQ equation and keeping the same limits modify the equations the following way

$$\frac{xQ}{2} \left( \frac{\partial}{\partial Q} + \frac{1}{Q} \frac{\partial}{\partial \phi} \right) \frac{\partial}{\partial x} [xG(x, Q^2, \phi)] = \frac{\alpha_s N_c}{\pi} xG(x, Q^2, \phi) - \frac{\alpha_s^2 N_c \pi}{2 C_F S_{\perp}} \frac{1}{Q^2} [xG(x, Q^2, \phi)]^2$$

(NB: angular ladder effects neglected as a first attempt, will modify this qualitative estimate) As a solution, we try

$$G(x, Q^2, \phi) = G_0(x, Q^2) \left( 1 + \sum_{n=1}^{\infty} u_n(x, Q^2) \cos(n\phi + \beta_n) \right),$$

$G_0(x, Q^2)$  is the azimuthally symmetric solution (i.e. saturation)

# Azimuthal symmetry as a broken symmetry

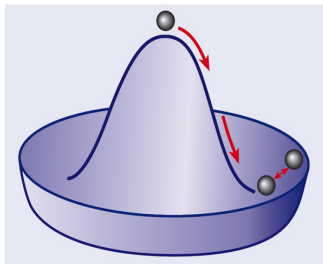


Figure : Elliptic flow  $\nu_2$  vs. rapidity [2,3].

Arbitrary small tilt (tiny gradients at high  $x$ ) produce large effects at low  $x$ . Different from CGC effects since lagrangian acquires a  $\theta$  dependence (which will need to be added to JIMWLK equation)



# Non-linear evolution can break underlying symmetries



If non-linearities are strong enough, azimuthal symmetries broken dynamically. In hydrodynamics this effect is well-known but exists in most 2+1 non-linear systems

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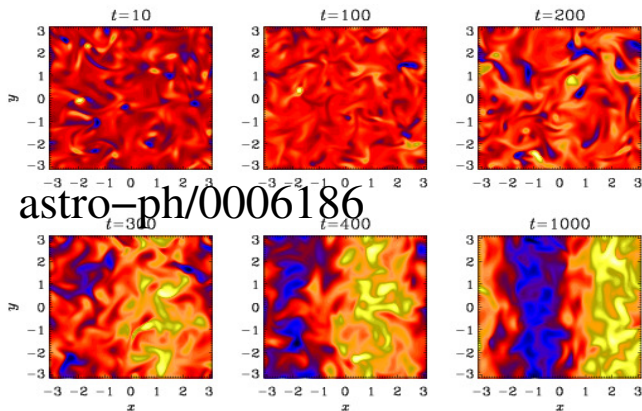
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# 2+1 non-linear evolution equation



For unintegrated in  $x_{\perp}$  General Parton distribution functions we could have: "Inverse cascade": Instabilities go from high frequency (local in transverse space) to low frequency as  $x$  evolves. No "many antennae" problem.

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# Equations for the Fourier coefficients

Working on the limiting case  $Q \ll Q_s(x)$ , we insert the solution with azimuthal perturbations into eq. fully asymmetric GLR-MQ equation and get three linear equations for our Fourier coefficients.

- 1 An infinite set of equations equation that relate the Fourier coefficients with the phases.

$$\sum_k u_k^2(x, Q^2) \cos(2\beta_k) = 0 \quad (3)$$

2 An infinite set of equations regarding only the derivative with respect to  $x$ .

$$x \frac{\partial u_n(x, Q^2)}{\partial x} = -(2\lambda + 1)u_n(x, Q^2)$$

$$+ \frac{N_c \pi}{2C_F S_\perp \alpha_s^2} \frac{1}{Q^2} x^{2\lambda+1} \frac{1}{n} \left[ \sum_k^{n-1} u_k(x, Q^2) u_{n-k}(x, Q^2) \sin(\beta_n - \beta_k - \beta_{n-k}) \right]$$

$$+ 2 \sum_k u_k(x, Q^2) u_{n+k}(x, Q^2) \sin(\beta_n + \beta_k - \beta_{n+k}) \quad (4)$$

### 3 An infinite set of equations that regards derivatives with respect to $Q$ and mixed terms.

$$\begin{aligned}
 (2\lambda+1)\frac{Q}{2}\frac{\partial u_n(x, Q^2)}{\partial Q} + \frac{Q}{2}x\frac{\partial^2 u_n(x, Q^2)}{\partial Q\partial x} &= \frac{\alpha_s N_c}{\pi}u_n(x, Q^2) \\
 + \frac{N_c\pi}{2C_F S_\perp \alpha_s^2} \frac{1}{Q^2} x^{2\lambda+1} &\left[ 2u_n(x, Q^2) \right. \\
 + \frac{1}{2} \sum_k^{n-1} u_k(x, Q^2) u_{n-k}(x, Q^2) \cos(\beta_n - \beta_k - \beta_{n-k}) \\
 + \sum_k u_k(x, Q^2) u_{n+k}(x, Q^2) \cos(\beta_n + \beta_k - \beta_{n+k}) &\left. \right] \quad (5)
 \end{aligned}$$

As an ansatz we propose

$$u_n(x, Q^2) = \delta_{n,2} \sum_{k=0}^{\infty} A_k \frac{(Bx^C)^k}{k!} Q^{D-2k} \quad (6)$$

then solve the equation linearized in  $u_k$  from initial conditions

$$u_n(\ln x^{-1} \rightarrow 0, Q) \sim \epsilon_n \alpha_s^2$$

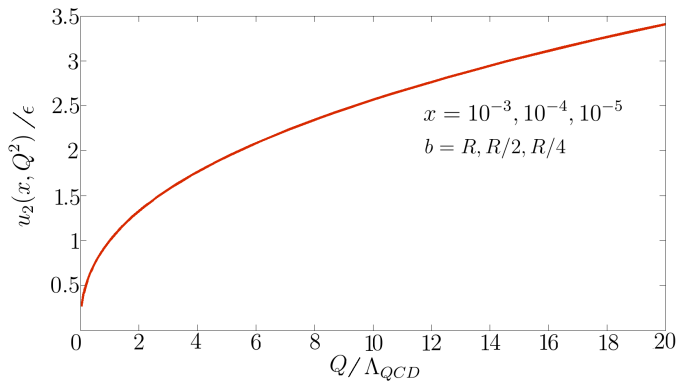
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# Preliminary results



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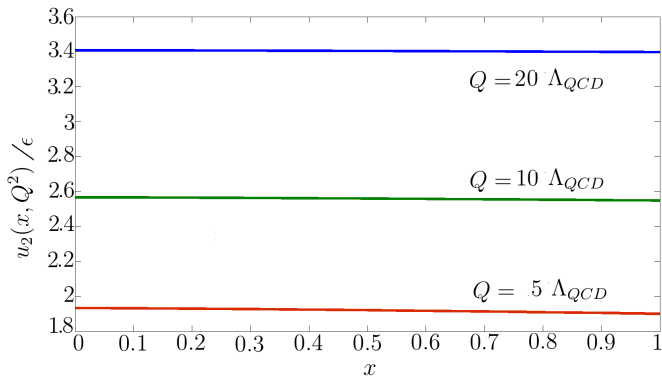
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# Preliminary results: very encouraging

- Near independence of  $u_n(Q, x)$  on  $x$  (all dependence on  $G_0(Q, x)$  which in turn depends weakly on  $Q$  . Just like  $v_2$ )
- Near linear dependence on  $\epsilon_n$  Just like  $v_2$
- near decoupling of fourier modes

Forthcoming: A phenomenological study including factorization and fragmentation

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# What if we were right?

**Relation between  $v_n$**  non-linearities could be more predictive than hydro models, fewer parameters so easier to falsify

**Photon correlations** Correlations between high rapidity photons and mid-rapidity hadrons, pA and AA

**And the ultimate signature** is...

# Ridges/ $v_n$ at the EIC?

CLAS collaboration find azimuthal correlations reminiscent of  $v_n$  but of course no rapidity study...

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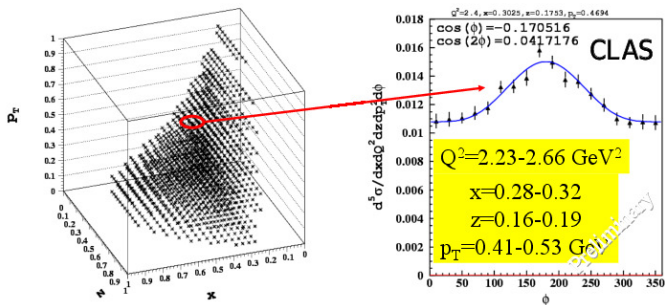
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## Azimuthal asymmetries at CLAS



- Unpolarized Semi-inclusive electroproduction of  $\pi^+$  measured.
- Complete 5-dimensional cross sections were extracted.
- Direct separation of different structure functions.

# Conclusions

- $\nu_2$  scaling similar to scaling of parton distribution functions. **Could they be azimuthally asymmetric?**
- Instabilities in the non-linear regime?
- Work in progress to develop this hypothesis to quantitative test level

## References

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