



# Precision Measurements of Electroweak Parameters with Z Bosons at the Tevatron ( $\sin^2\theta_{\text{eff}}^{\text{lept}}$ , $\sin^2\theta_{\text{W}}^{\text{on-shell}}$ , $M_{\text{W}}^{\text{indirect}}$ )



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On behalf of CDF and D0

Blois 1/6/16

Thanks to all CDF & D0 colleagues





## References



Dilepton forward-backward asymmetry of DY leptons  $\rightarrow \sin^2\theta_{\text{eff}}^{\text{leptonic}}$

1. DØ  $e^+e^-$  (9.7 fb $^{-1}$ ) Phys. Rev. Lett. 115, 041801(2015)

$\rightarrow \sin^2\theta_{\text{eff}}^{\text{leptonic}}(M_Z)$

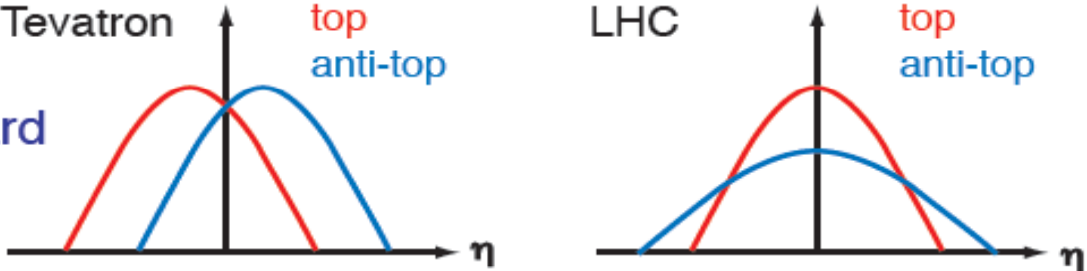
2. CDF  $\mu^+\mu^-$  (9.2 fb $^{-1}$ ) Phys. Rev. D89, 072005(2014):

CDF  $e^+e^- + \mu^+\mu^-$  (9.4 fb $^{-1}$ ) submitted to Phys Rev D 2016

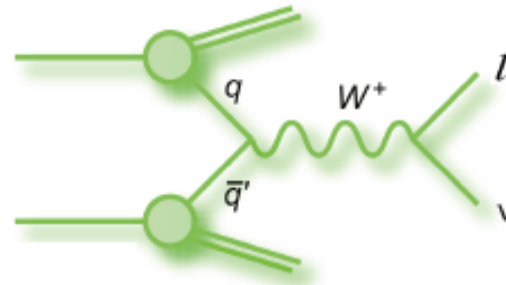
$\rightarrow \sin^2\theta_{\text{eff}}^{\text{leptonic}}(M_Z)$  &  $\sin^2\theta_{\text{eff}}^{\text{on-shell}}$ ,  $M_W$  Indirect

See also A. Bodek et al arXiv:1507.02470

New method: PDF Constraints from Drell-Yan AFB

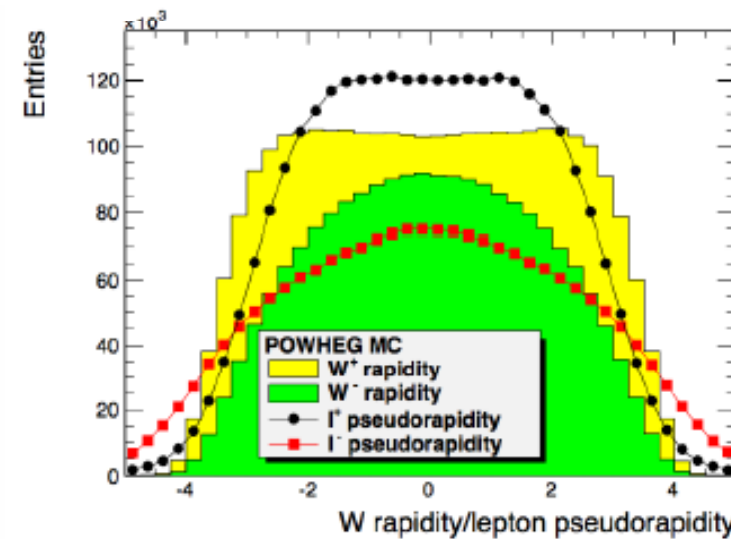
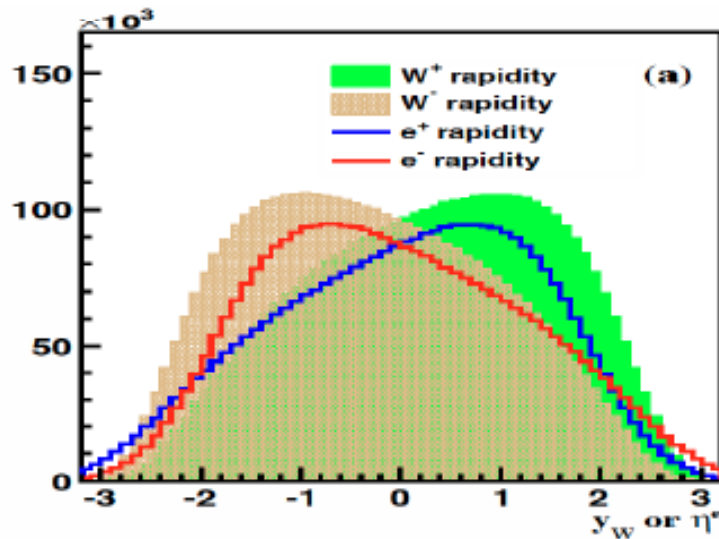
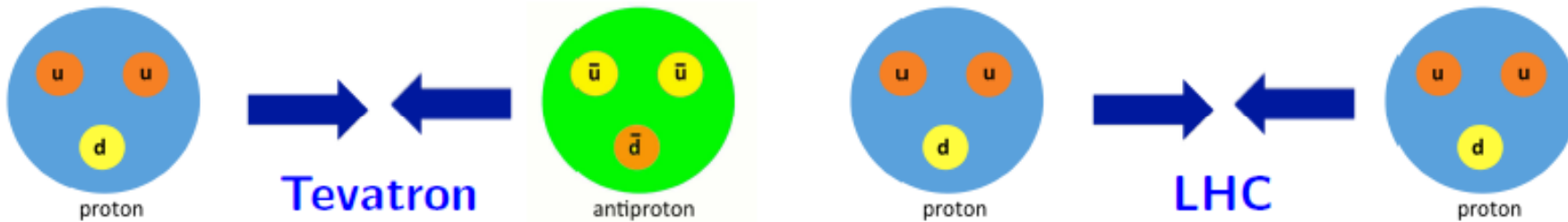
- Different collision energy,  $\sqrt{s_{\text{eff}}}$ 
  - Cross sections
  - Different (QCD) backgrounds
- $p\bar{p}$  collisions instead of  $pp$ 
  - asymmetries; e.g., top, electroweak
- Top quark forward-backward asymmetries:
 
- is an initial CP invariant state ( $B$  physics)
- Complementary! Production processes different mix of  $q\bar{q}$  vs.  $gg$  collisions
  - $t\bar{t}$  spin correlations
- Well understood detector  
(plus lower level of pileup, only getting worse at LHC)
  - $W$  boson mass
  - top quark mass

**Tevatron:** dominated by valence quark production

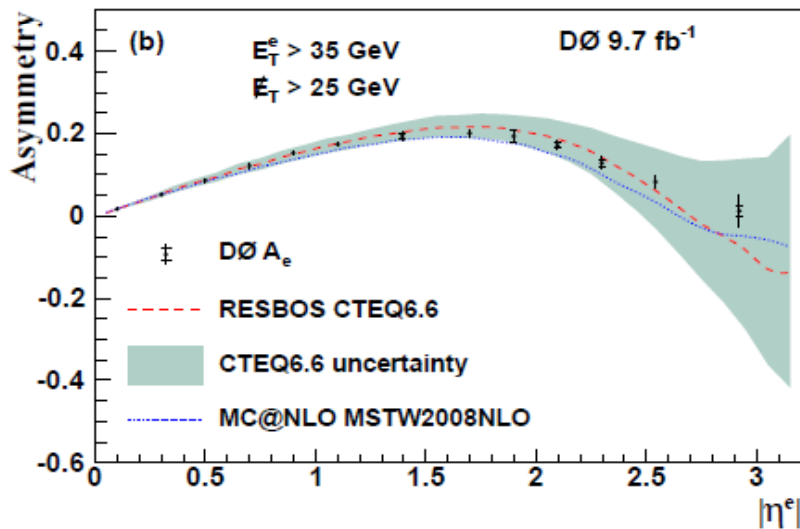


**LHC:** dominated by sea quark and gluon production

Measurement @Tevatron places stringent constraints on the PDFs



Lepton asymmetry: convolution of the W boson charge asymmetry and the V-A decay of the W boson.



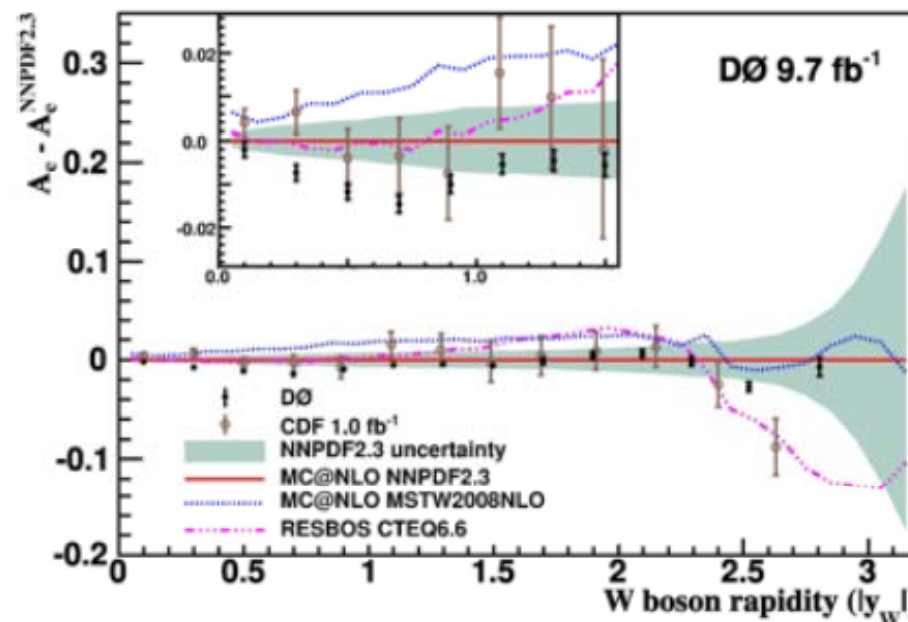
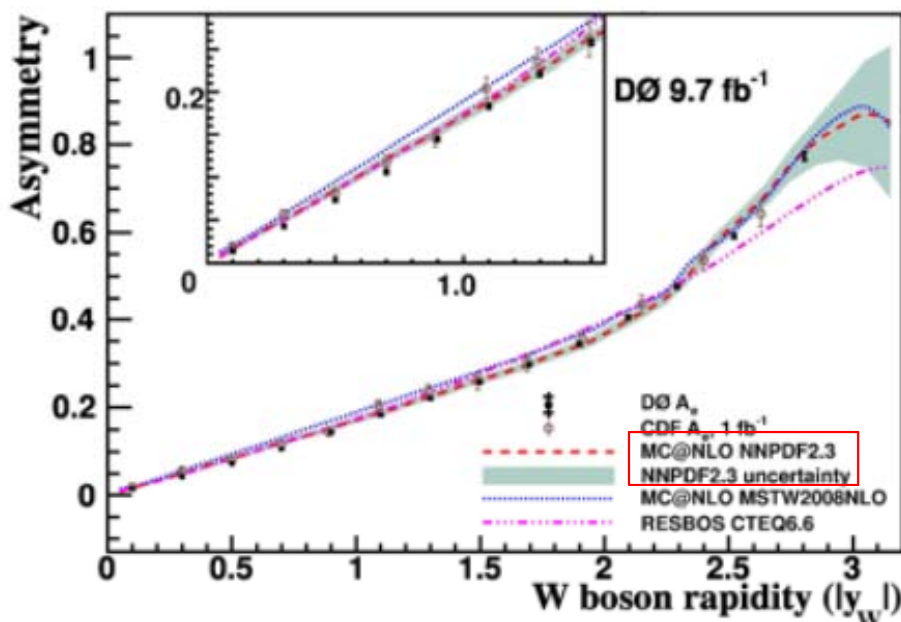
Full D0 dataset (9.7 fb<sup>-1</sup>), electron channel

## Lepton Charge Asymmetry:

Significant gain in precision and in  $\eta$  coverage  
 Most precise measurement of lepton charge asymmetry to date

## W boson production asymmetry:

Potential improvement of PDF models in the  $x$ - $Q^2$  region of interest for W production at Tevatron → will reduce the current PDF uncertainty in the W mass measurement by approximately 30% (down to 2-3 MeV)





# Measuring $\sin^2\theta_W$ and W mass (indirectly) using Z's



- Experimentally interesting situation
- In the SM:  $\sin^2\theta_W = 1 - m_W^2 / m_Z^2$   
 $\sin^2\theta_W$  indirectly measures  $m_W$
- Derive  $\sin^2\theta_{\text{eff}}^{\text{lept}}$  from angular distribution of leptons in Drell-Yan ( $Z/\gamma^* \rightarrow l^+l^-$ ) events.

$$\frac{dN}{d\theta} \approx 1 + \cos^2\theta + A_4 \cos\theta$$

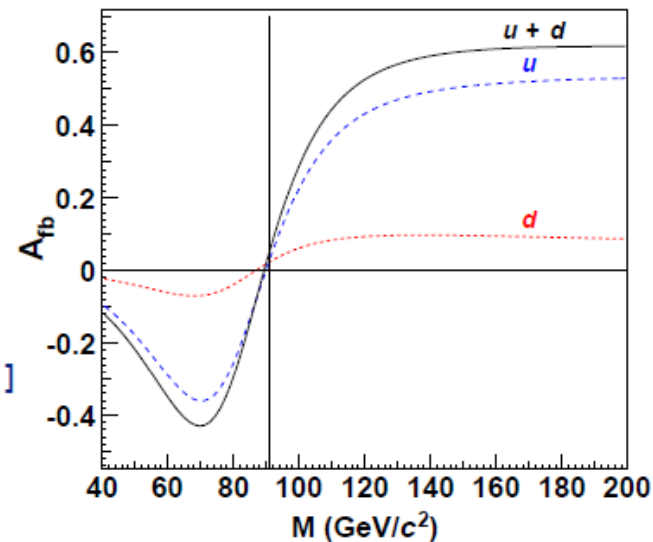
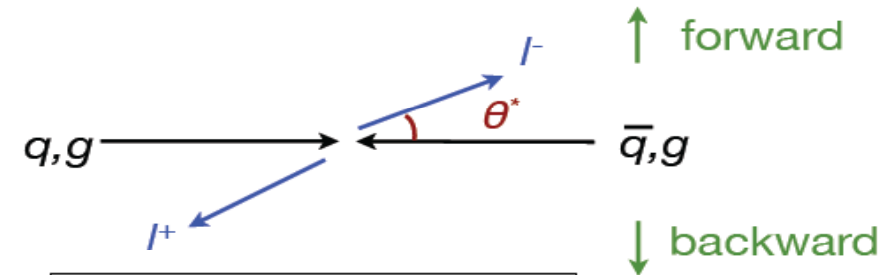
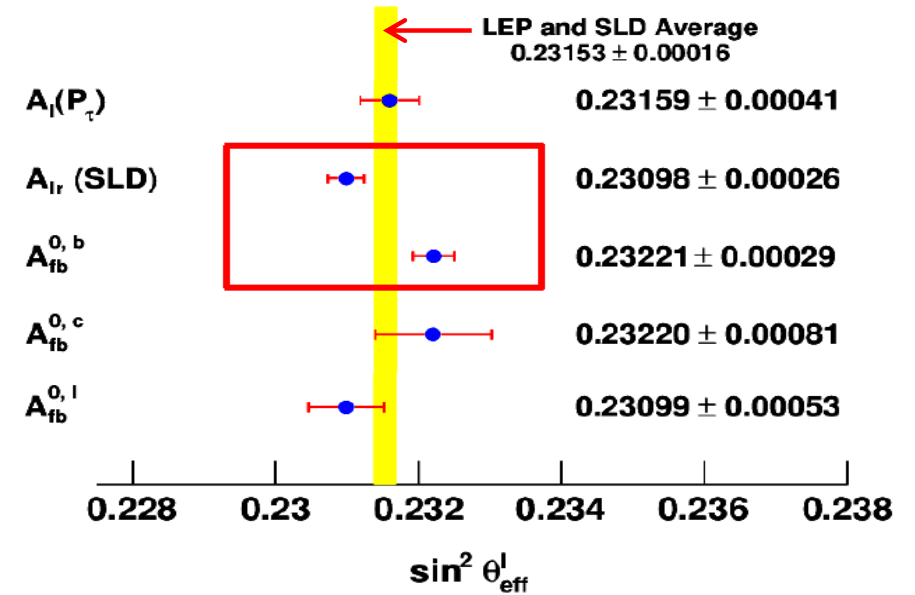
- Forward-backward asymmetry

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{8} A_4$$

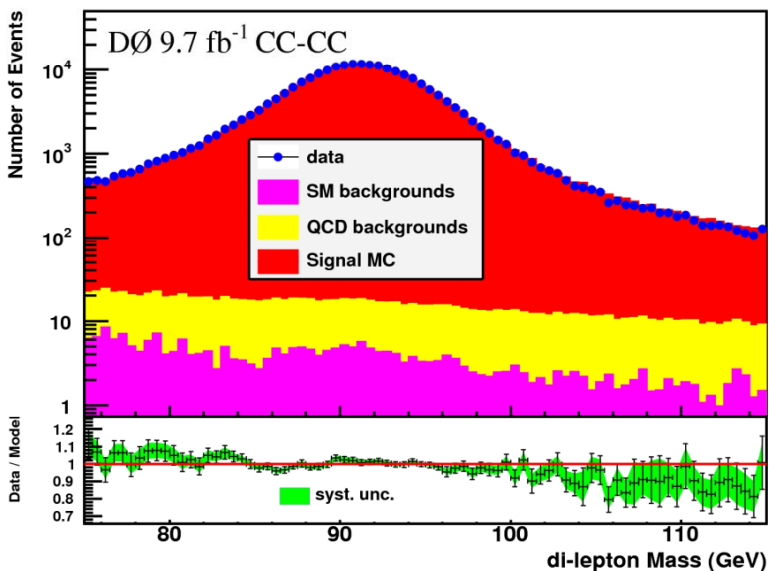
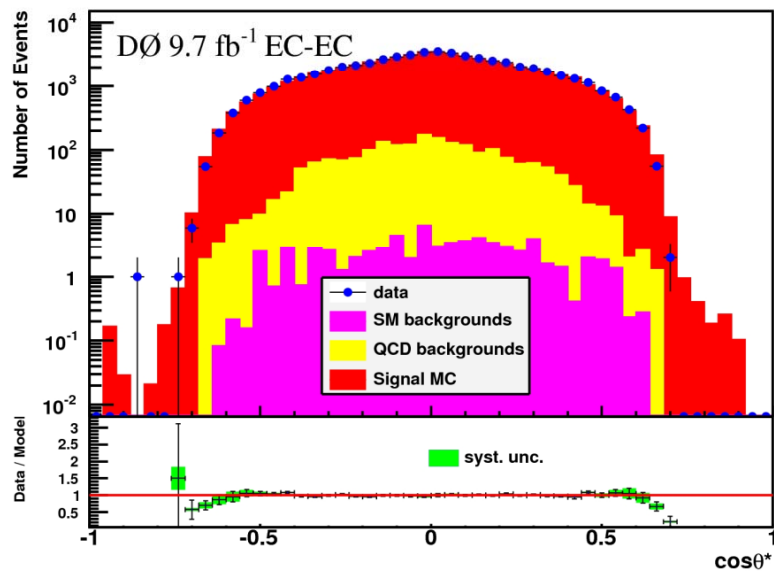
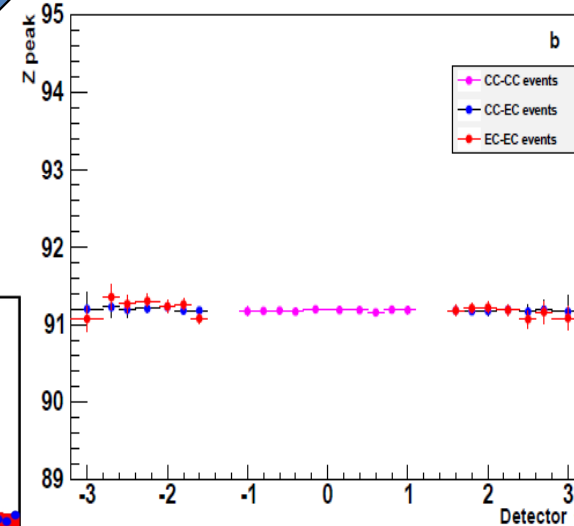
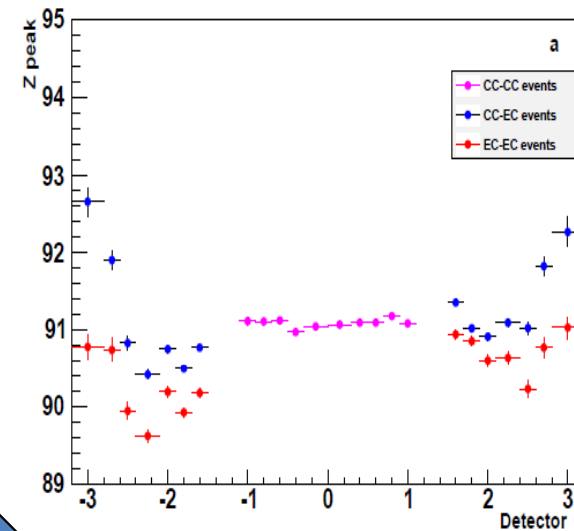
- Measurement  $A_{FB} \rightarrow \sin^2\theta_{\text{eff}}^{\text{lept}}$   
 (effective Z/lepton coupling)

$$\sin^2\theta_{\text{eff}}^{\text{lept}} \approx 1.037 \cdot \sin^2\theta_W \quad [\text{ZFITTER } \kappa_e(\sin^2\theta_W, M_Z) \text{ form factor}]$$

$$\rightarrow \sin^2\theta_W \rightarrow m_W$$



- two electrons with  $p_T > 25$  GeV
- Tight track match requirement
- CC ( $|\eta| < 1.1$ ) and EC ( $1.5 < |\eta| < 3.2$ )
- Use  $75 < M_{ee} < 115$  GeV  $\rightarrow$  560k events
- New Lepton energy calibration
- $\rightarrow$  Apply scale factor as a function of  $L_{\text{inst}}$  first then as a function of  $\eta$
- $M_{ee}$  peak scaled to Z-LEP value in each bin
- Separate calibrations for data and MC





# DØ e<sup>+</sup>e<sup>-</sup> 9.7 fb<sup>-1</sup> sin<sup>2</sup>θ<sub>eff</sub><sup>W</sup> analysis



Corrections are applied to MC to account for:

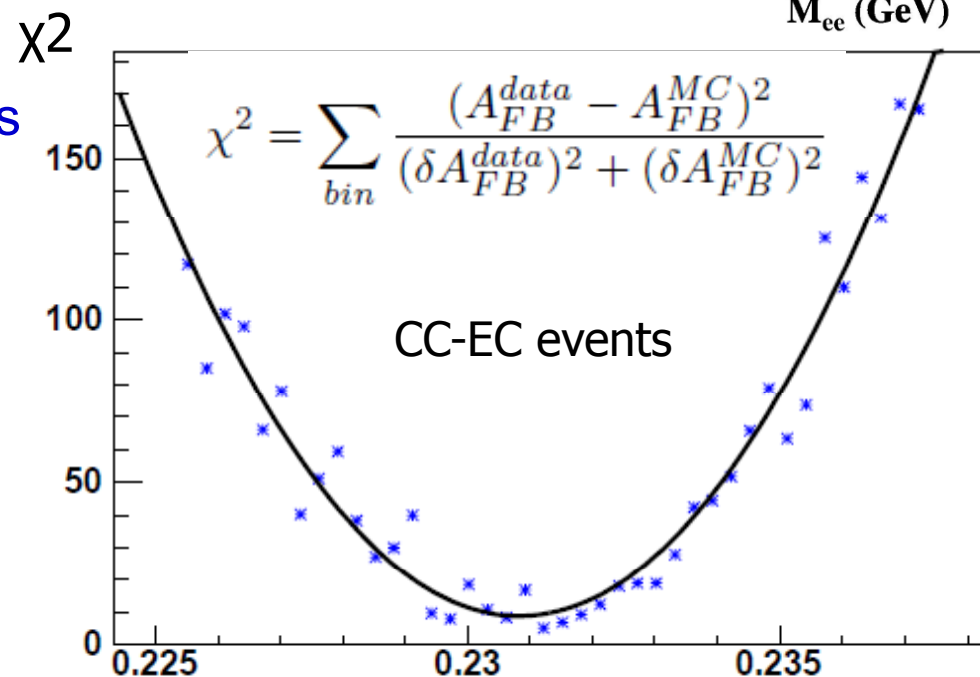
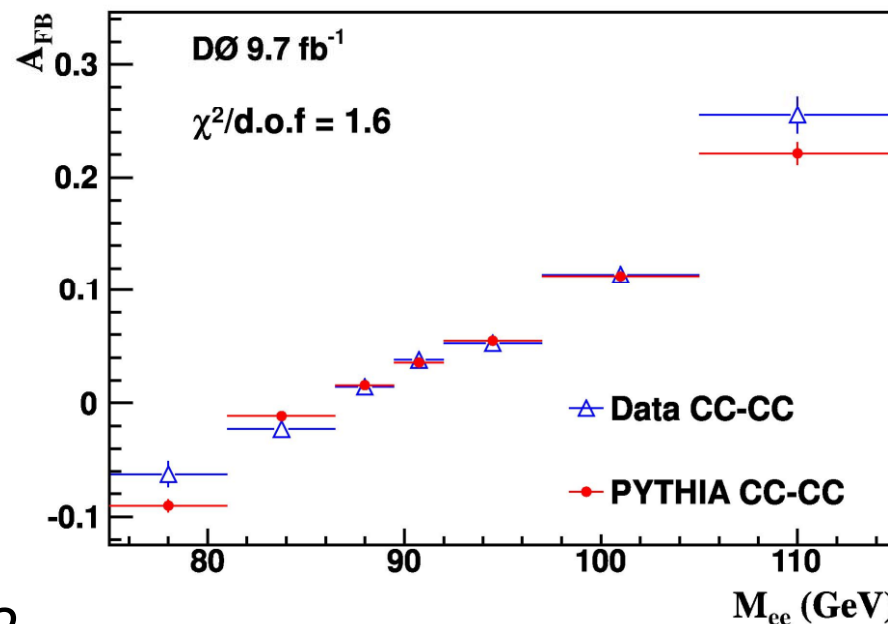
- Smearing of electron energy
- Efficiency corrections in pT(e), η(e)
- L<sub>inst</sub> and z<sub>PV</sub> reweighting to match data
- Higher order effects: NNLO Z pT and y to match RESBOS
- Produce 2D templates of M<sub>ee</sub> and cosθ\* by reweighting default MC (sin<sup>2</sup>θ<sub>eff</sub>=0.232) as a function of sin<sup>2</sup>θ<sub>eff</sub>

Extract sin<sup>2</sup>θ<sub>eff</sub> by fitting raw AFB to templates with different sin<sup>2</sup>θ<sub>eff</sub> values

- No unfolding: MC is carefully corrected to describe the data

$$\sin^2\theta_{\text{eff}} = 0.23138 \pm 0.00043(\text{stat}) \pm 0.00008(\text{syst}) \\ \pm 0.00017(\text{NNPDF2.3 PDFs})$$

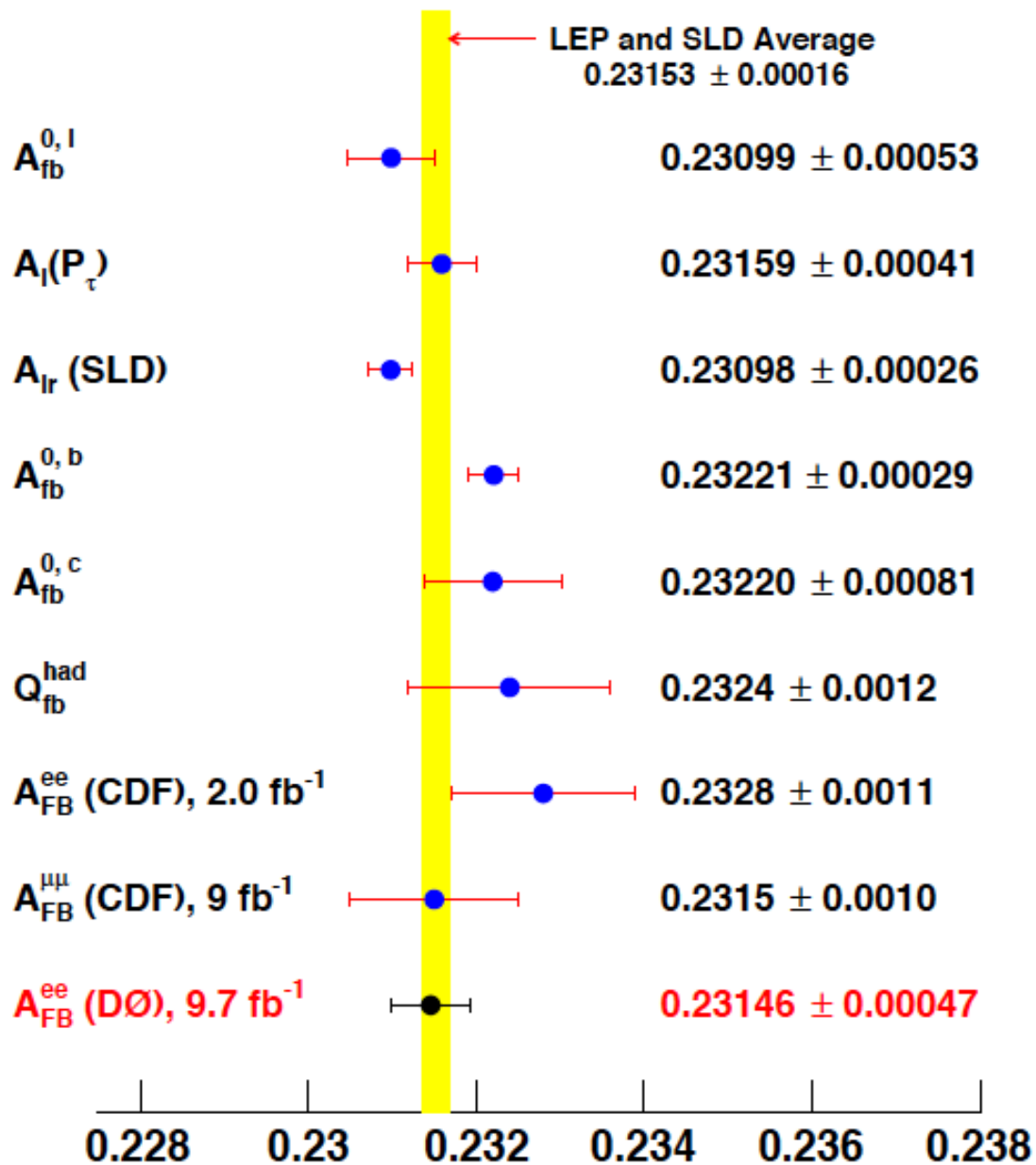
(no EW radiative corrections)







# DØ e<sup>+</sup>e<sup>-</sup> 9.7 fb<sup>-1</sup> sin<sup>2</sup>θ<sub>eff</sub><sup>W</sup> analysis



An approximate way to correct for the flavor dependence of sin<sup>2</sup>θ<sub>eff</sub> from EW radiative corrections is used by the DØ collaboration. This is done by making the following corrections (proposed by Baur and collaborators [8]):

$$\sin^2 \theta_{\text{eff}}^{\text{u-quark}} = \sin^2 \theta_{\text{eff}}^{\text{lept}} - 0.0001$$

$$\sin^2 \theta_{\text{eff}}^{\text{d-quark}} = \sin^2 \theta_{\text{eff}}^{\text{lept}} - 0.0002$$

Change is +0.00008

Final results :DØ ee

sin<sup>2</sup>θ<sub>eff</sub><sup>leptonic</sup> (Mz)

$$= 0.23146 \pm 0.00043 \text{ (statistical)}$$

$$\pm 0.00008 \text{ (systematics)}$$

$$\pm 0.00017 \text{ (PDFs NNPDF2.3 NLO)}$$

$$= 0.23146 \pm 0.00047 \text{ (total)}$$

Situation in 2015



Main improvements are in 4 areas:

Since  $\sin^2\theta_W$  is constant while  $\sin^2\theta_{\text{eff}}$  lept ( $M_{ee}$ , flavor) is not.

Implement Full ZFITTER EW radiative corrections,

- Enhanced Born Approximation (EBA), include full complex form factors implemented in private versions of RESBOS, POWHEG, and LO.  
*Ref Phys. Rev. D 88, 072002 (2013) Appendix A'.*

Precise lepton momentum/energy scale for muons and electrons using a new method- (will also reduce scale error for  $M_W$  measurement)

*Ref: A. Bodek et al. Euro. Phys. J. C72, 2194 (2012)*

Use event weighting method for AFB analyses (systematic errors in acceptance and efficiencies cancel)

Use Drell-Yan forward-backward asymmetry to constrain parton distribution functions - (will also reduce PDF errors for  $M_W$  measurement)

*Ref A. Bodek et al arXiv:1507.02470v2 (2015)*

$\sin^2\theta_W$  (on-shell) is a constant while  $\sin^2\theta_{\text{eff}}$  lept ( $M_{ee}$ , flavor) is not.

Full ZFITTER EW radiative corrections, Enhanced Born Approximation (EBA), include full complex form factors implemented in private versions of RESBOS, POWHEG, and LO)  $\rightarrow$  Phys. Rev. D 88, 072002 (2013) Appendix A'

$g_V^f \gamma_\mu + g_A^f \gamma_\mu \gamma_5$ . The Born-level couplings are

$$g_V^f = T_3^f - 2Q_f \sin^2 \theta_W$$

$$g_A^f = T_3^f,$$

They are modified by ZFITTER 6.43 form factors (which are complex)

$$g_V^f \rightarrow \sqrt{\rho_{eq}} (T_3^f - 2Q_f \kappa_f \sin^2 \theta_W), \text{ and}$$

$$g_A^f \rightarrow \sqrt{\rho_{eq}} T_3^f,$$

$$\text{SM}(\sin^2 \theta_W) \xrightarrow{\text{EWK}} \sin^2 \theta_{\text{eff}}(s) \xleftrightarrow{\text{QCD}} A_4(s),$$

$$\text{AFB} = (3/8) A_4$$

- $T_3$  and  $\sin^2\theta_W \rightarrow$  **effective  $T_3$  and  $\sin^2\theta_W$** : 1-4% multiplicative form factors
- On-mass shell scheme:  $\sin^2\theta_W \equiv 1 - M_W^2/M_Z^2$  to all orders

Accounts for  $\sin^2\theta_{\text{eff}}$  dependence on quark flavor and dilepton mass  
 $\rightarrow$  get  $\sin^2\theta_{\text{eff}}^{\text{leptonic}}(M_Z)$  using  $A_{\text{FB}}$  over a range of dilepton mass



# Precise Energy/Momentum Scale corrections



New technique used for both  $\mu+\mu^-$  and  $e+e^-$  for both data and hit level MC

- 1 : Remove the correlations between the scale for the two leptons by getting an initial calibration using Z events and requiring that the mean  $\langle 1/PT \rangle$  of each lepton in bins of  $\eta$ ,  $\Phi$  and charge be correct.
- 2: Use the Z mass for calibration. The Z mass as a function of  $\eta, \Phi$ , (and charge for  $\mu+\mu^-$ ) of each lepton must be correct
  - Reference for electrons: expected Z mass (post FSR + clustered FSR photons), smeared by resolution (with acceptance cuts).
  - Reference for muons: expected Z mass (post FSR) smeared by resolution (with acceptance cuts).



## Use event weighting Method



Event weighting method for  $A_{FB}$  analyses

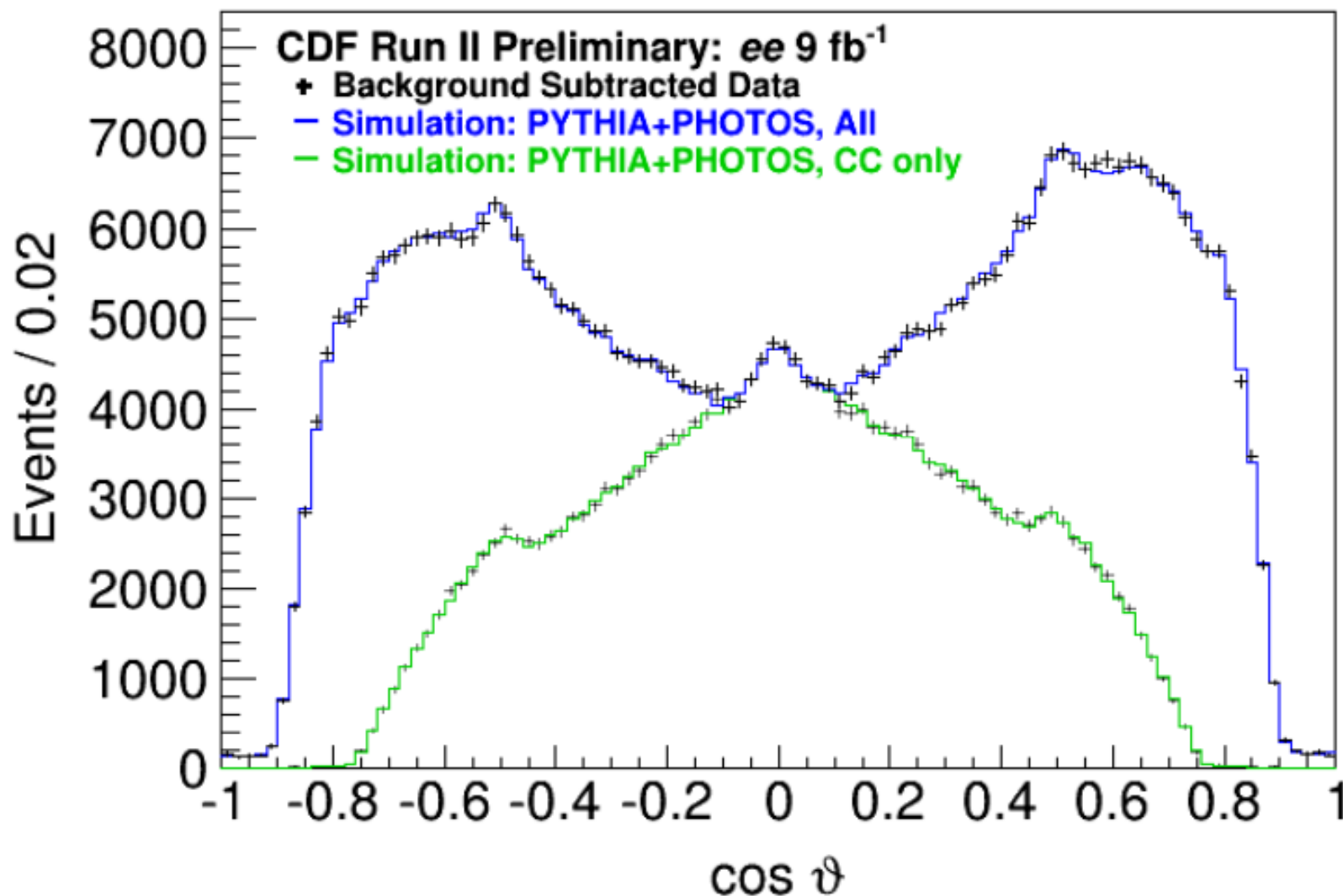
$$dN/d\cos\theta = 1 + \cos^2\theta + A_0(M, P_T) (1 - 3\cos^2\theta)/2 + A_4(M) \cos\theta$$

Angular event weighting is equivalent to extraction of  $A_4(M)$  in bins of  $\cos\theta$ , and averaging the results.

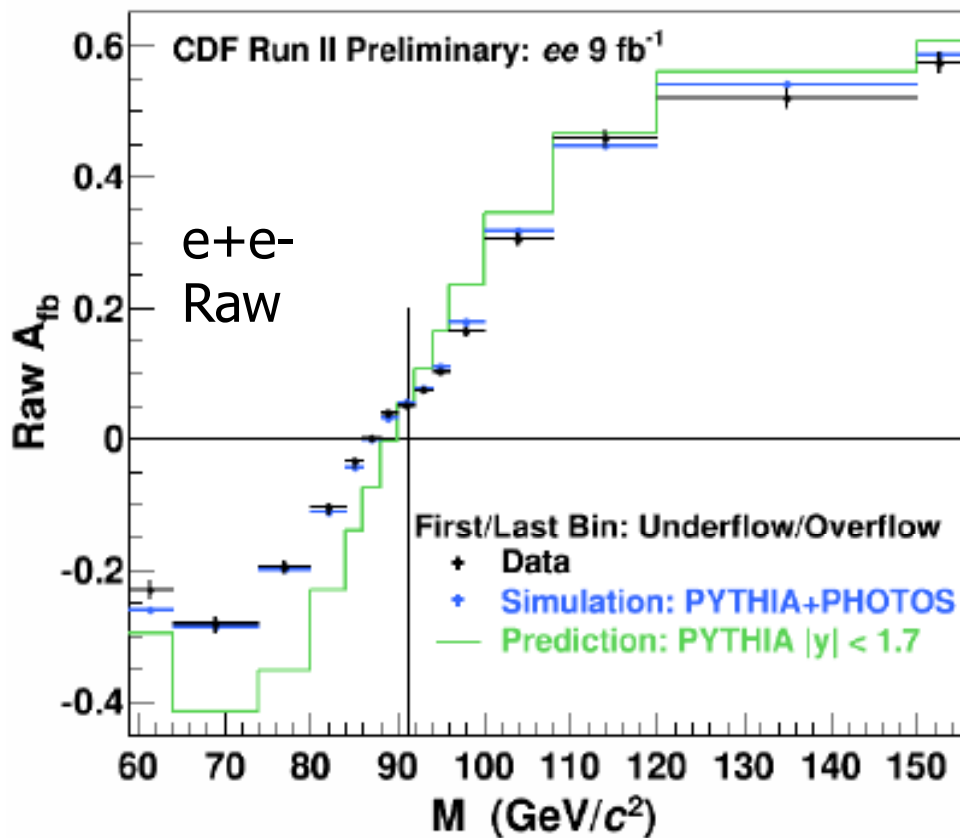
Events at large  $\cos\theta$  provide better determination of  $A_4$ , so they are weighted more than events at small  $\cos\theta$ .

For each  $\cos\theta$  acceptance and efficiencies cancel to first order and the statistical errors are 20% smaller. Then extract  $A_{FB} = (3/8)A_4$

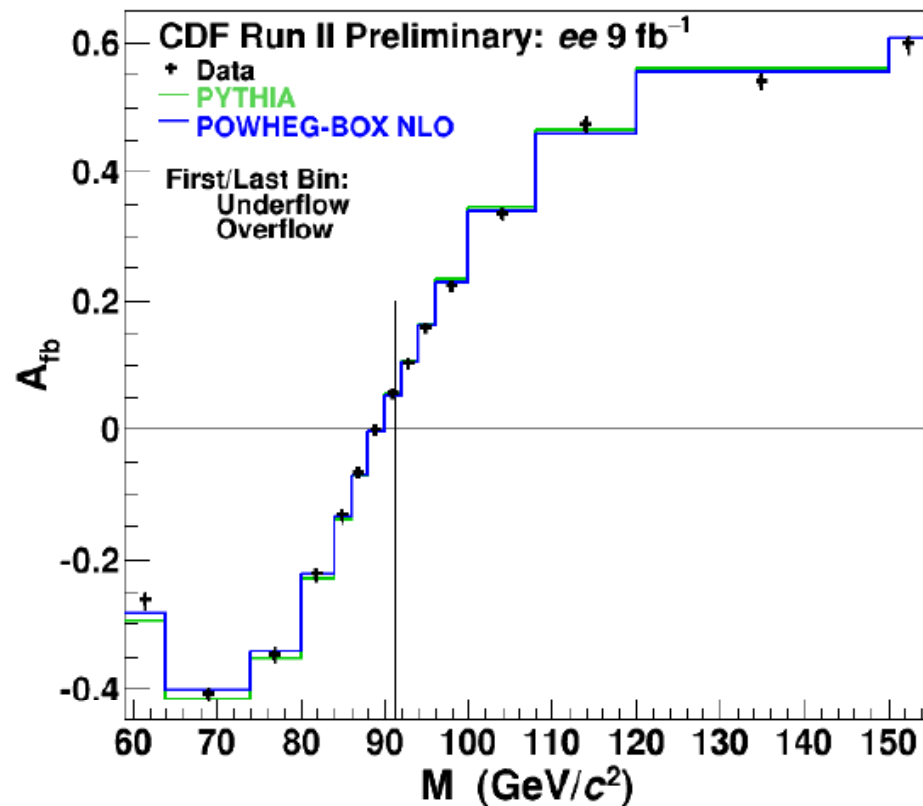
Event weighting does not correct for resolution smearing and final state radiation, which are included later in the unfolding.



The error in  $A_{\text{FB}}$  is reduced if we have more acceptance at large  $\cos\theta$ ,  
Standard  $A_{\text{FB}}$  method requires precise knowledge of acceptance and efficiencies.  
Measure  $A_4 \rightarrow A_{\text{FB}}$

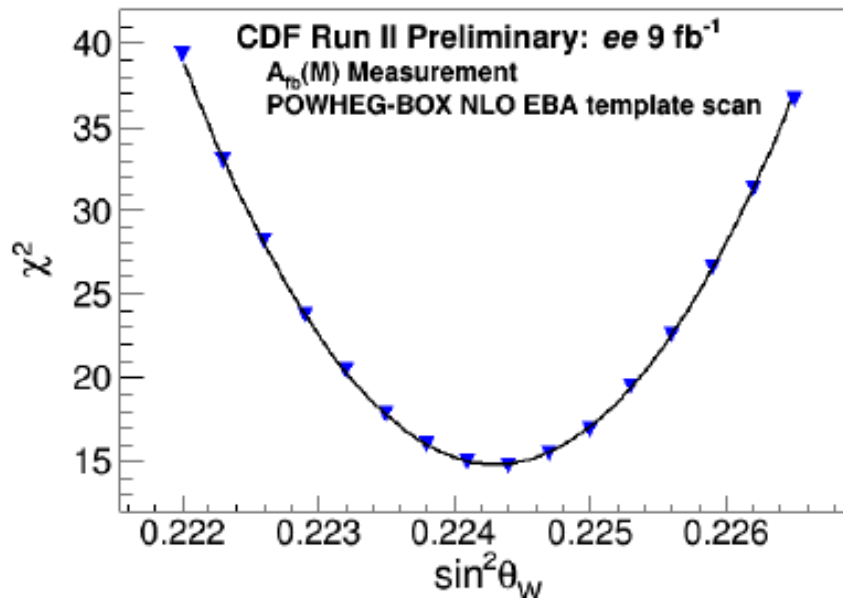


$e^+e^-$ :  $A_{FB}$  Background subtracted  
Raw no corrections



$e^+e^-$ :  $A_{FB}$  unfolded, fully corrected

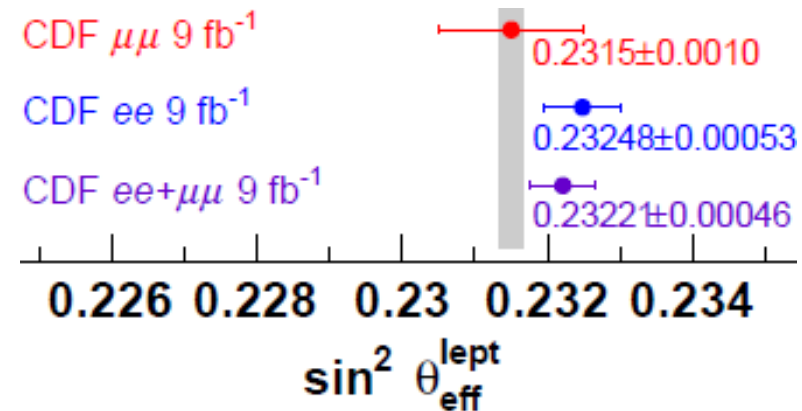
- Comparison  $\chi^2$ :  $\sum_M \Delta A_{fb}(M)^{\nu} \cdot E \cdot \Delta A_{fb}(M)$ 
  - Measurement: Fully corrected  $A_{fb}(M)$
  - Calculated templates:  $A_{fb}(M, \sin^2\theta_W)$  for 16 values of  $\sin^2\theta_W$
  - E: Measurement error matrix
- Extraction of  $\sin^2\theta_W$  from the scan points
  - Fit  $\chi^2(\sin^2\theta_W)$  scan points to a parabola:  $\chi^2_{min} + (\sin^2\theta_W - \sin^2\theta_{W min})^2 / \sigma_{min}^2$ 
    - Assign each scan point  $\chi^2(\sin^2\theta_W)$  an error of 0.1 in the parabolic fit
    - $(\sin^2\theta_{W min}, \sigma_{min})$  are the fit values of  $\sin^2\theta_W$  and its uncertainty
    - $\chi^2_{min} = \text{minimum } \chi^2(\sin^2\theta_W)$  at  $\sin^2\theta_{W min}$  for 15 mass bins



This analysis is repeated with

1. POWEG
2. RESBOS
3. Tree-Level LO

For the POWHEG analysis, the extraction is repeated for all 100 NNPDF3.0 Replicas to get PDF uncertainty





$M_W$  also can be determined indirectly via the relation

$$\sin^2\theta_W^{\text{on-shell}} = 1 - M_W^2 / M_Z^2$$

$\pm 0.00040$  error in  $\sin^2\theta_W$  is equivalent to  $\pm 20$  MeV error in  $M_W$  (indirect)

Both  $\sin^2\theta_W^{\text{on-shell}}$  and  $\sin^2\theta_{\text{eff}}^{\text{leptonic}}$  ( $M_Z$ ) can be extracted from Drell-Yan forward-backward asymmetry ( $A_{\text{fb}}$ ) if we include EW radiative corrections.

→  $M_W^{\text{indirect}}$  can be extracted from  $\sin^2\theta_W^{\text{on-shell}}$

If the SM is correct, then both direct and indirect measurements of  $M_W$  should agree. Deviations may imply the possibility of new physics.

Similarly different measurements of  $\sin^2\theta_{\text{eff}}^{\text{leptonic}}$  ( $M_Z$ ) should also agree and deviations may imply new physics.

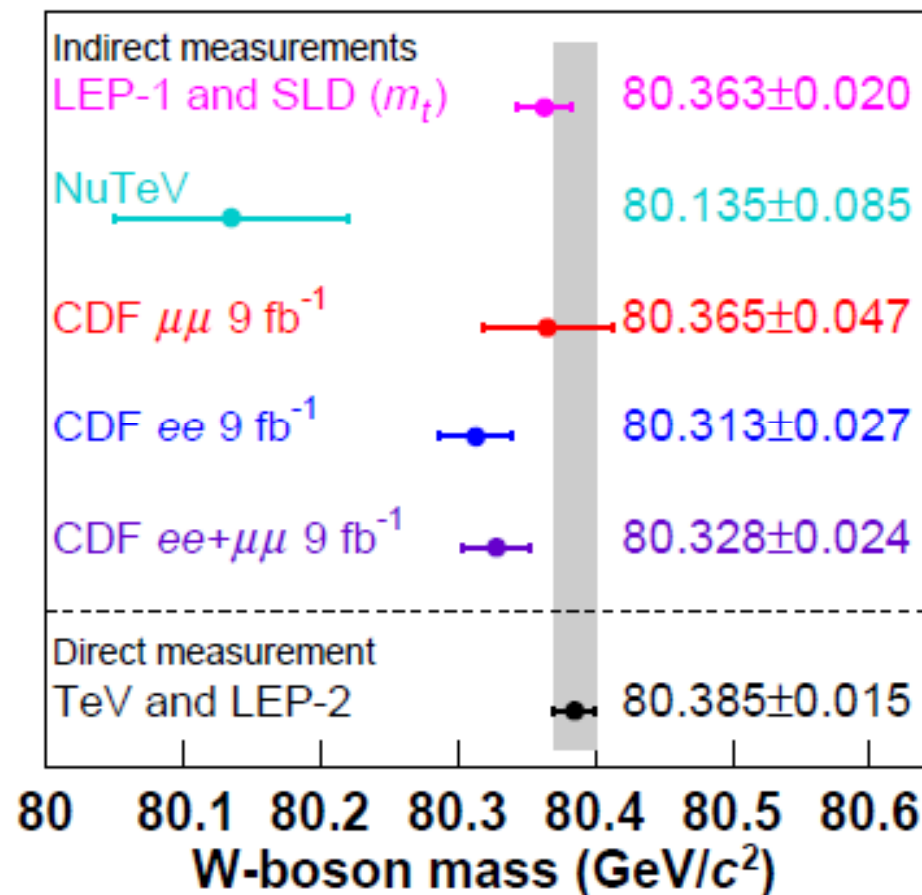
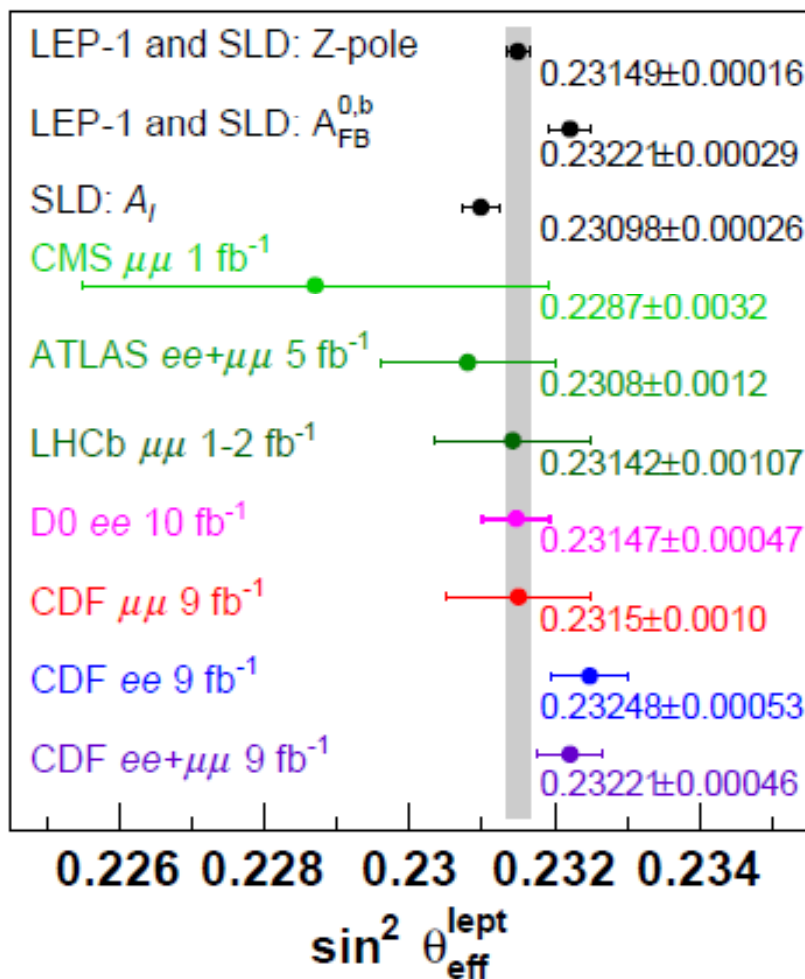


# CDF and DØ results



## Differences between DØ and CDF Analyses

1. CDF uses NNPDF 3.0 PDFs (NNLO) which include LHC data and supersede the NNPDF2.3 (NLO) used by DØ
2. CDF uses full EBA EW rad correction. DØ uses partial Zgrad EW rad corr. Need to resolve these issues before the two results can be combined.





# W Mass direct Measurement



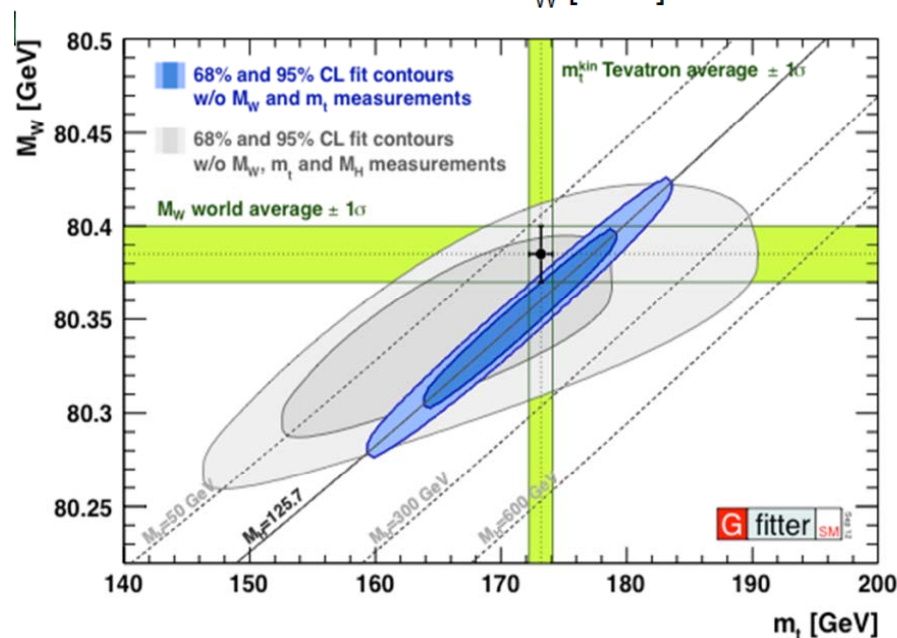
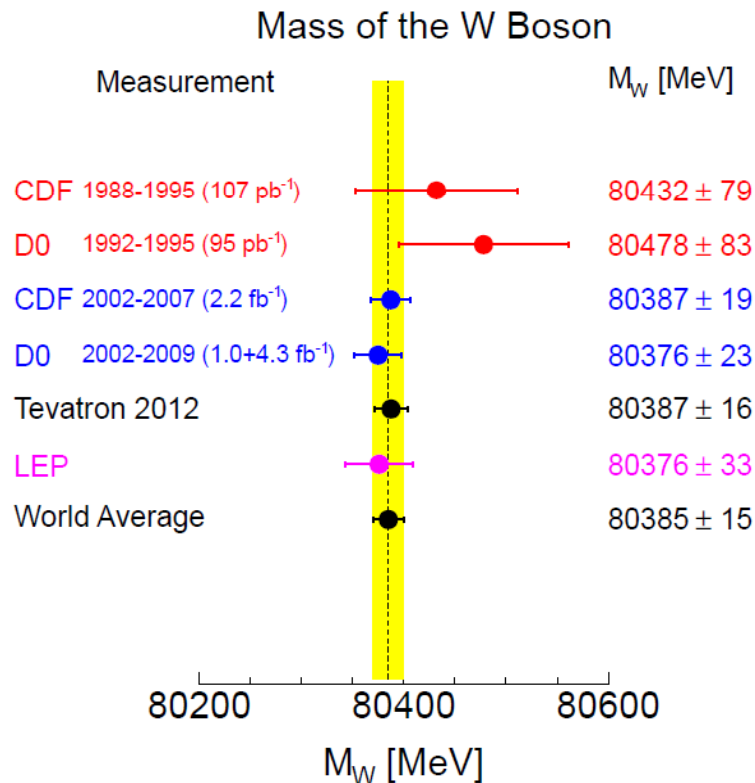
- Tevatron Combination based on CDF (2.2 fb<sup>-1</sup>) and D0 (5.1 fb<sup>-1</sup>) results:

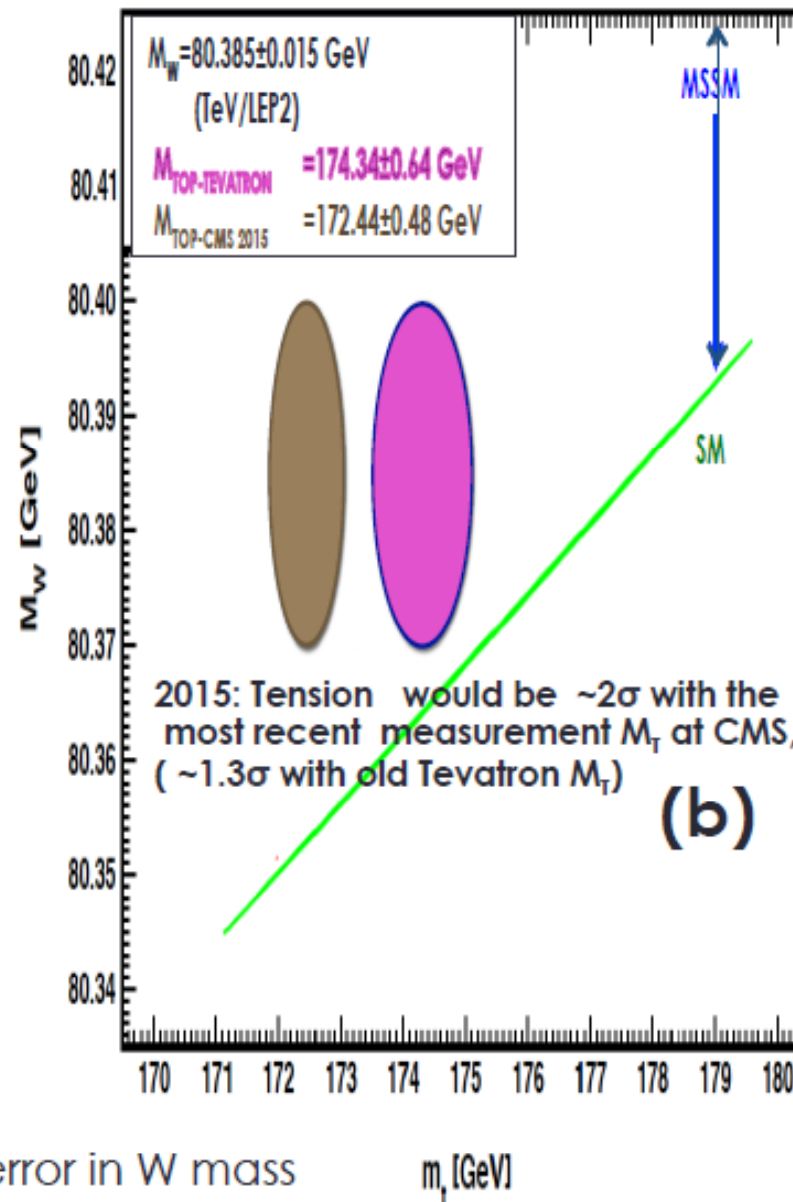
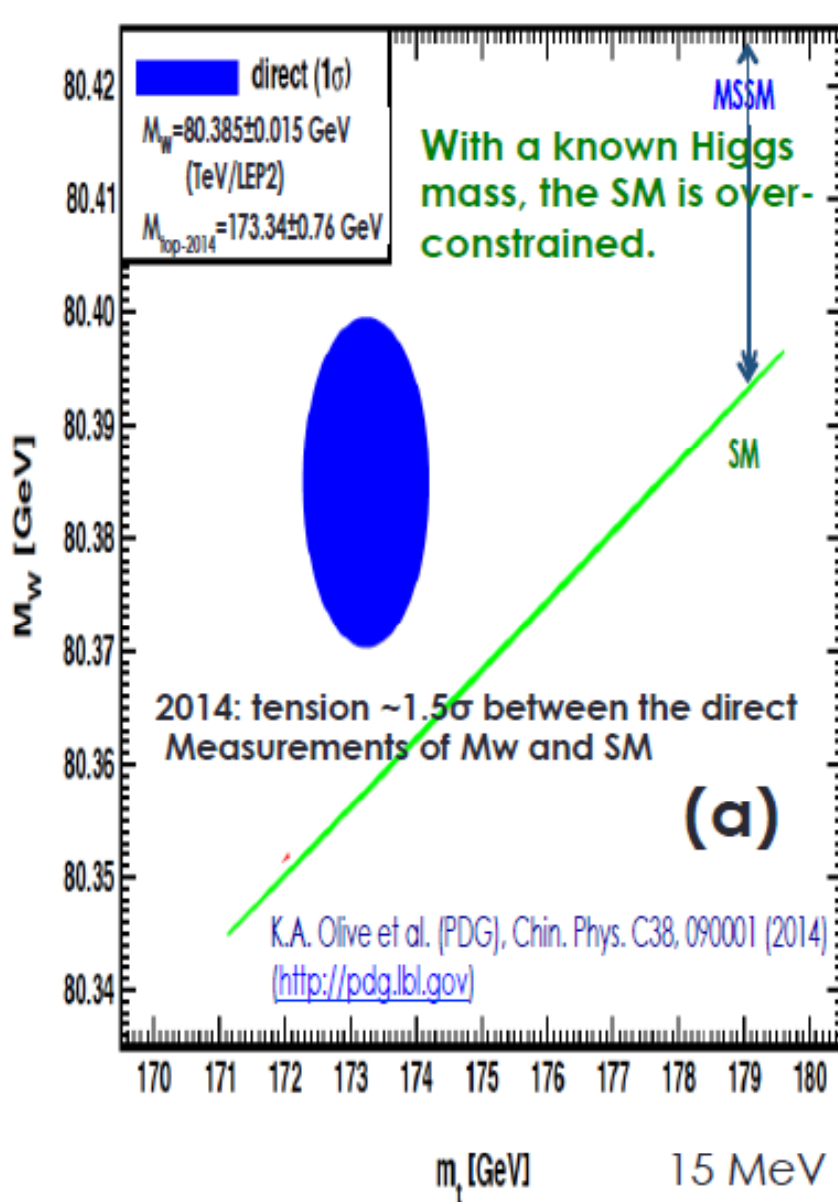
$$M_W = (80387 \pm 16) \text{ MeV}$$

→ 0.02% precision!

dominates the World combination (15 MeV)

- Full-data results from both CDF and D0 in progress → further reduction of uncertainties
  - Statistics gain → energy scale uncertainty
  - Extension to forward leptons and PDF improvements will allow significant gain
- Target 10 MeV world average with new CDF and D0 measurements using full statistics.
- Consistency check of the SM (top-W-Higgs)





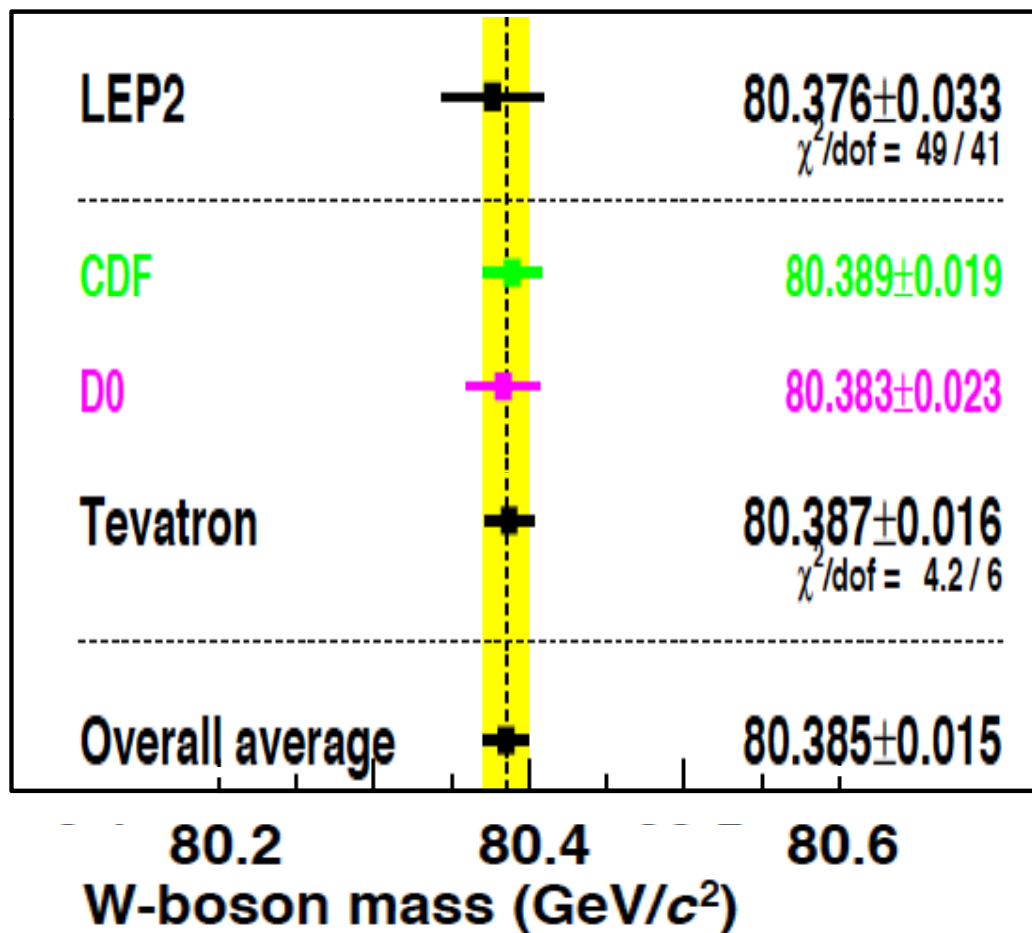


# Direct and Indirect $W$ mass measurements



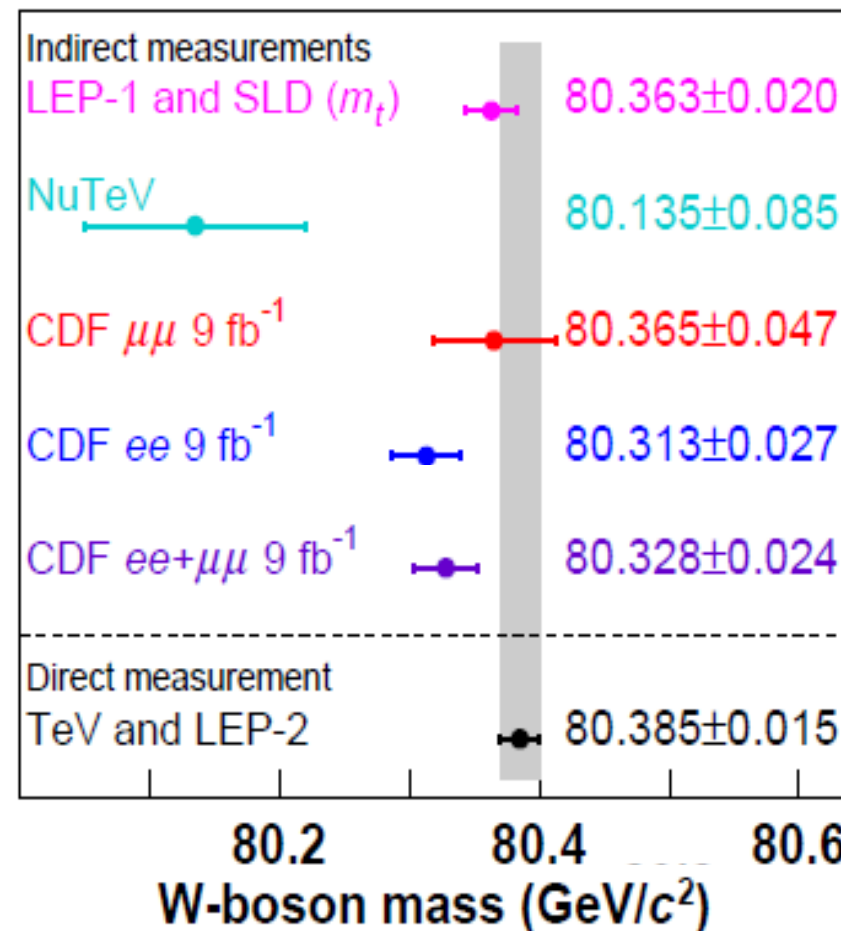
## Direct measurements:

Waiting for update from CDF and D0 on full dataset (currently 2 and 5  $\text{fb}^{-1}$ )



## Indirect measurements:

CDF  $M_W$  24 MeV indirect  $M_W$  uncertainty is similar to CDF  $M_W$  19 MeV direct  $M_W$  uncertainty





# Conclusions / Tevatron Legacy



- The CDF and DZero collaborations are still producing competitive physics results in particular in the electroweak sector
- Currently the Tevatron direct ( $L= 2.2 \text{ fb}^{-1}$ ) and indirect ( $L=9.4 \text{ fb}^{-1}$ ) measurements of  $M_W$  have similar errors. ( $\sim 20 \text{ MeV}$  per experiment)
- Tevatron Run II Legacy measurements of  $\sin^2\theta_W$  and  $M_W$  indirect are in agreement with SM predictions from  $M_H$  and  $M_{\text{top}}$ , and with direct measurement of  $M_W$
- $A_{\text{FB}}(M)$  data can also be used to put additional constraints on PDFs. These constraints will help reduce PDF errors in the ongoing Tevatron Run II Legacy ( $L=9.4 \text{ fb}^{-1}$ ) direct measurement of  $M_W$ .

