

# RECENT RESULTS ON BOTTOMONIUM STUDIES AT BELLE

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# Introduction



Bottomonium system yielded many surprises.

$$R \equiv \frac{\sigma(h_b(nP)\pi^+\pi^-)}{\sigma(\Upsilon(2S)\pi^+\pi^-)} \sim 1$$

for  $h_b(1P)$  and  $h_b(2P)$ .

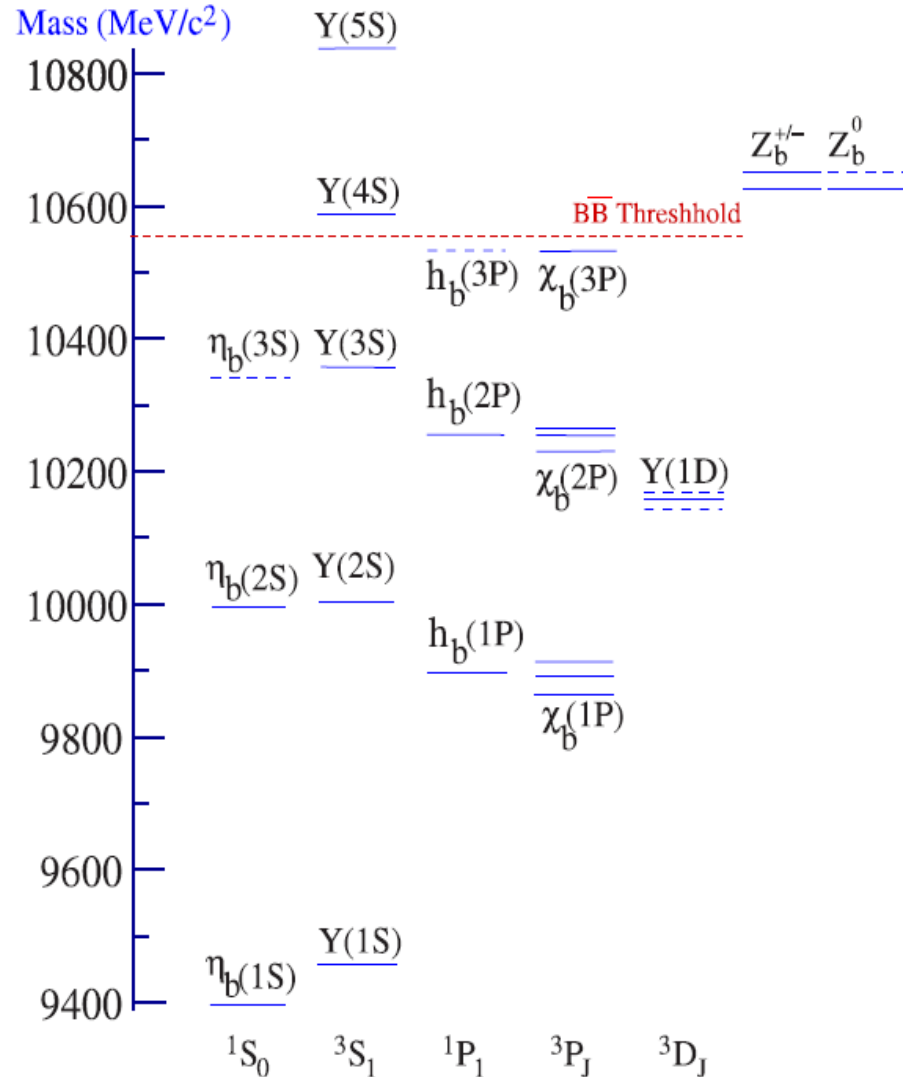
$Y(5S) \rightarrow Y(2S)\pi^+\pi^-$  } similar  
 $Y(5S) \rightarrow h_b(nP)\pi^+\pi^-$  } rates

requires spin flip

- discoveries of  $\eta_b(2S)$  and  $h_b(1P, 2P)$
- exotic bottomonium-like states  $Z_b$

This talk:

- three energy scans
  - $e^+e^- \rightarrow Y(nS)\pi^+\pi^-$
  - $e^+e^- \rightarrow h_b(nP)\pi^+\pi^-$
  - $e^+e^- \rightarrow B^{(*)}B^{(*)}\pi^\pm$
- $\eta$  transition
  - $Y(4S) \rightarrow \eta h_b(1P)$



### Data:

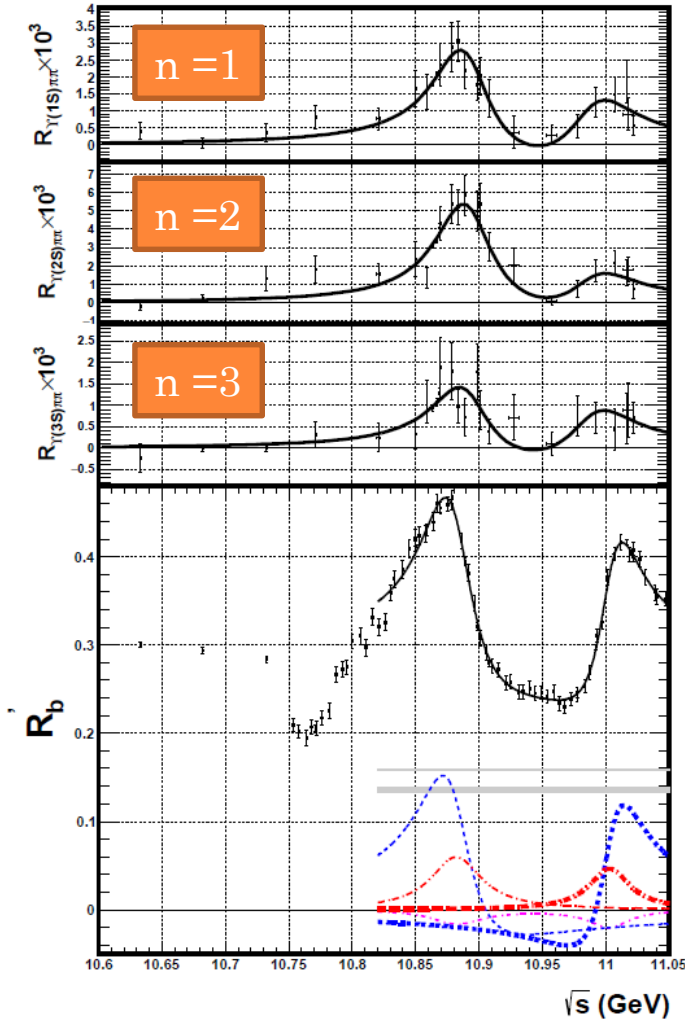
- 10.63 – 11.02 GeV;
- 121.4 fb<sup>-1</sup> at Y(5S) (3 energy points);
- 26 fb<sup>-1</sup> scan (19 energy points for  $e^+e^- \rightarrow Y(nS)\pi^+\pi^-$ ,  
74 energy points for  $e^+e^- \rightarrow b\bar{b}$ ).

### Selection:

- $Y(nS) \rightarrow \mu^+\mu^-$ ;
- $\pi^+\pi^-\mu^+\mu^-$  and no other tracks;
- $M(\pi^+\pi^-\mu^+\mu^-)$  consistent with  $\sqrt{s}$ ;
- $\Delta M = M(\pi^+\pi^-\mu^+\mu^-) - M(\mu^+\mu^-)$  consistent with  $\sqrt{s} - M_{Y(nS)}$ .

# $e^+e^- \rightarrow Y(nS)\pi^+\pi^-$ & $e^+e^- \rightarrow b\bar{b}$

# II



$$R_{Y(nS)\pi\pi} = \sigma(Y(nS)\pi^+\pi^-) / \sigma_{\mu\mu}^0$$

$$\mathcal{F}'_n(\sqrt{s}) = PHSP(\sqrt{s}) \cdot \{ |A_{5S,n} f_{5S}|^2 + |A_{6S,n} f_{6S}|^2 + 2k_n A_{5S,n} A_{6S,n} \Re[e^{i\delta_n} f_{5S} f_{6S}^*] \}$$

$$f_{nS} = BW(M_{nS}, \Gamma_{nS})$$

$$R_b = \sigma(b\bar{b}) / \sigma_{\mu\mu}^0$$

$$\mathcal{F}(\sqrt{s}) = |A_{ic}|^2 + |A_c + A_{5S} e^{i\phi_{5S}} f_{5S}(\sqrt{s}) + A_{6S} e^{i\phi_{6S}} f_{6S}(\sqrt{s})|^2$$

resonant

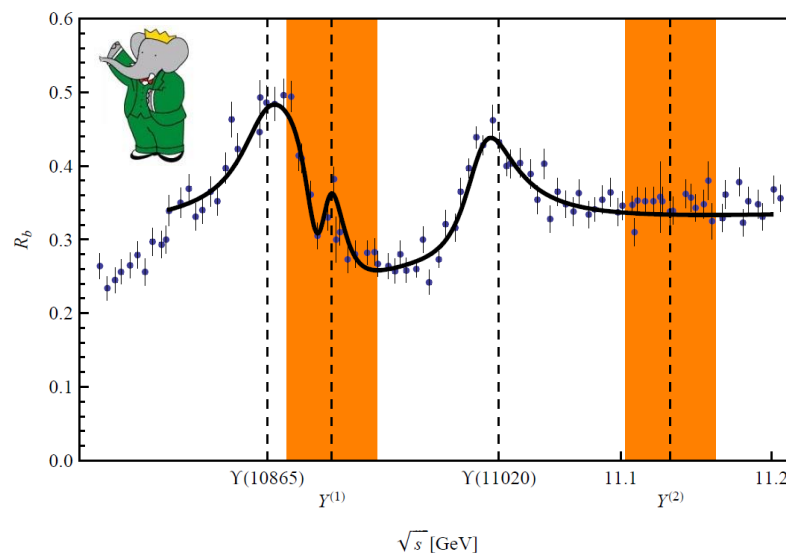
interference of resonances with continuum

interference of two resonances

continuum (coherent & incoherent)

	$M_{5S}$ (MeV/ $c^2$ )	$\Gamma_{5S}$ (MeV)	$M_{6S}$ (MeV/ $c^2$ )	$\Gamma_{6S}$ (MeV)	$\phi_{6S} - \phi_{5S}$ ( $\delta$ ) (rad)	$\chi^2/dof$
$R'_b$	$10881.8^{+1.0}_{-1.1} \pm 1.2$	$48.5^{+1.9}_{-1.8} +^{2.0}_{-2.8}$	$11003.0 \pm 1.1 +^{0.9}_{-1.0}$	$39.3^{+1.7}_{-1.6} +^{1.3}_{-2.4}$	$-1.87^{+0.32}_{-0.51} \pm 0.16$	56/50
$R_{Y(nS)\pi\pi}$	$10891.1 \pm 3.2 +^{0.6}_{-1.7}$	$53.7^{+7.1}_{-5.6} +^{1.3}_{-5.4}$	$10987.5^{+6.4}_{-2.5} +^{9.0}_{-2.1}$	$61^{+9}_{-19} +^2_{-20}$	$-1.0 \pm 0.4 +^{1.4}_{-0.1}$	51/56

- Difference in  $Y(5S)$  and  $Y(6S)$  parameters determined from fits to  $R_{Y(nS)\pi\pi}$  and  $R_b$  may be caused by the complexity of  $R_b$  data (continuum shape, proximity of  $B^{(*)}B^{(*)}$  thresholds & their interaction with resonances).
- Measurements from  $R_{Y(nS)\pi\pi}$  are more reliable.
- No peaking structure near 10.9 GeV suggested in 2010 by A. Ali et al. (*PLB* **684** 28) based on the BaBar measurement of  $R_b$ .



$$e^+e^- \rightarrow h_b(nP)\pi^+\pi^-$$

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$e^+e^- \rightarrow h_b(nP)\pi^+\pi^-$  ( $n = 1, 2$ ) is the next highest statistics channel after  
 $e^+e^- \rightarrow Y(nS)\pi^+\pi^-$

### Data:

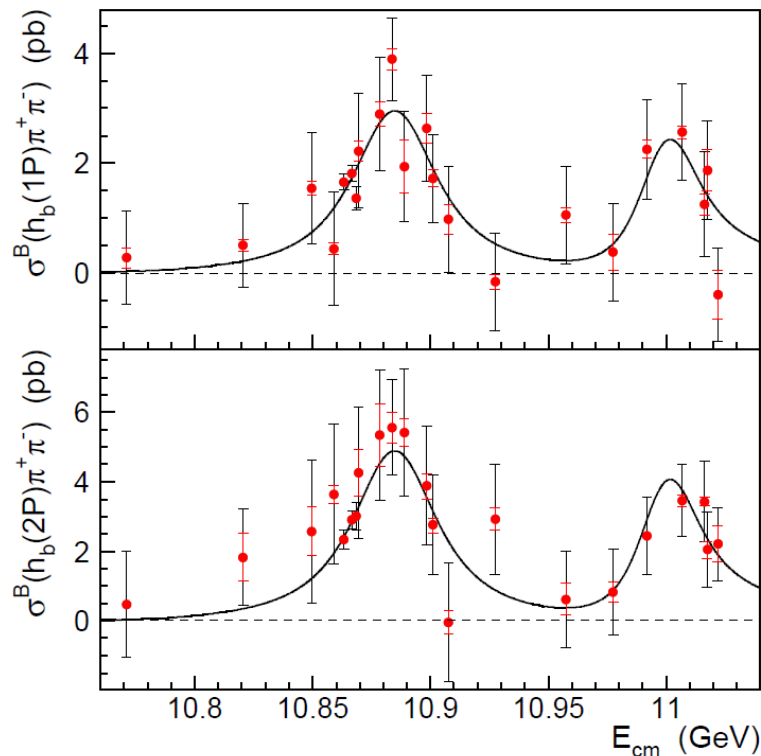
- 10.63 – 11.02 GeV;
- 121.4 fb<sup>-1</sup> at Y(5S) (3 energy points);
- 26 fb<sup>-1</sup> scan (19 energy points).

### Selection:

- consider all  $\pi^+\pi^-$  pairs
- $R_2 < 0.3$ ;
- $10.59 < M_{\text{miss}}(\pi) < 10.67$  GeV ( $Z_b$  region).

Assumption:  $e^+e^- \rightarrow Z_b\pi \rightarrow h_b(nP)\pi\pi$  (based on Y(5S) decays)

- Cross sections of  $e^+e^- \rightarrow h_b(nP)\pi^+\pi^-$  and  $e^+e^- \rightarrow Y(nS)\pi^+\pi^-$  look very similar and give consistent resonance parameters with no continuum contribution.
- **Charmonium:** difference between  $e^+e^- \rightarrow h_c\pi^+\pi^-$  and  $e^+e^- \rightarrow J/\psi\pi^+\pi^-$  shapes is much more pronounced (possible new peaks and non-res contribution).



$$N_1 |BW(M_5, \Gamma_5) + A_2 \exp\{iP_2\} BW(M_6, \Gamma_6)|$$

$$N_1 = (2.1 \pm 0.4) 10^3$$

$$N_2 = (3.2 \pm 0.7) 10^3$$

$$M_5 = 10\,887 \pm 3 \text{ MeV}$$

$$\Gamma_5 = 36 \pm 6 \text{ MeV}$$

$$M_6 = 11\,001 \pm 4 \text{ MeV}$$

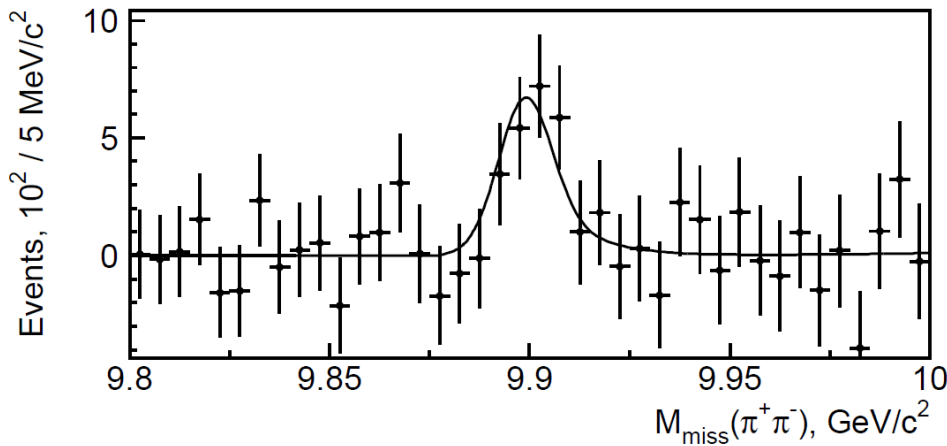
$$\Gamma_6 = 29 \pm 11 \text{ MeV}$$

$$A_2 = 0.85 \pm 0.14$$

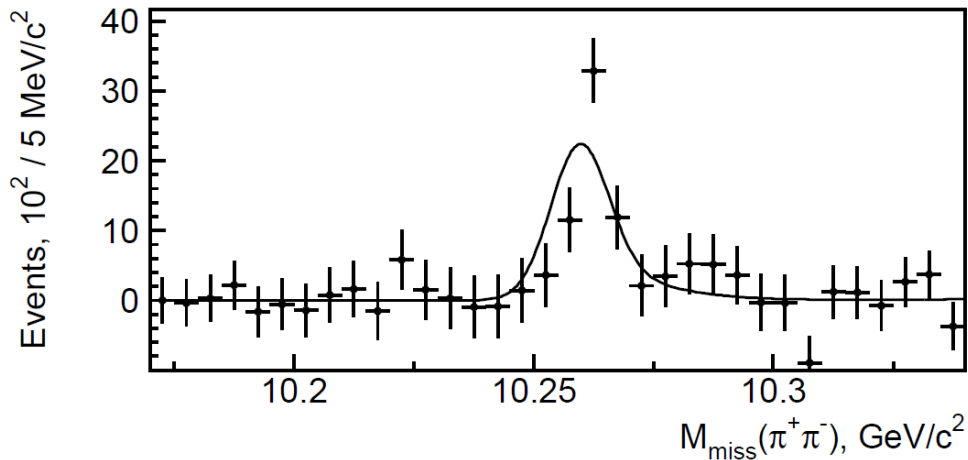
$$P_2 = (0.14 \pm 0.31) \pi$$

$Y(6S) \rightarrow h_b(nP)\pi^+\pi^-$  $M_{\text{miss}}(\pi^+\pi^-)$  fit

5 energy points



first evidence ( $3.6 \sigma$ ) for  
 $Y(6S) \rightarrow h_b(1P)\pi^+\pi^-$



first observation ( $5.4 \sigma$ ) of  
 $Y(6S) \rightarrow h_b(2P)\pi^+\pi^-$

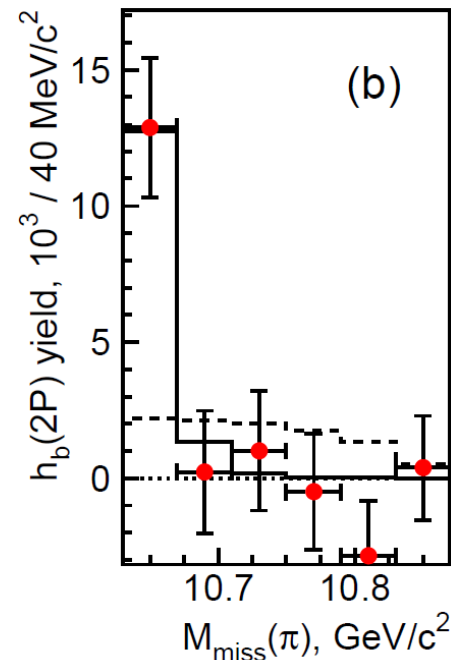
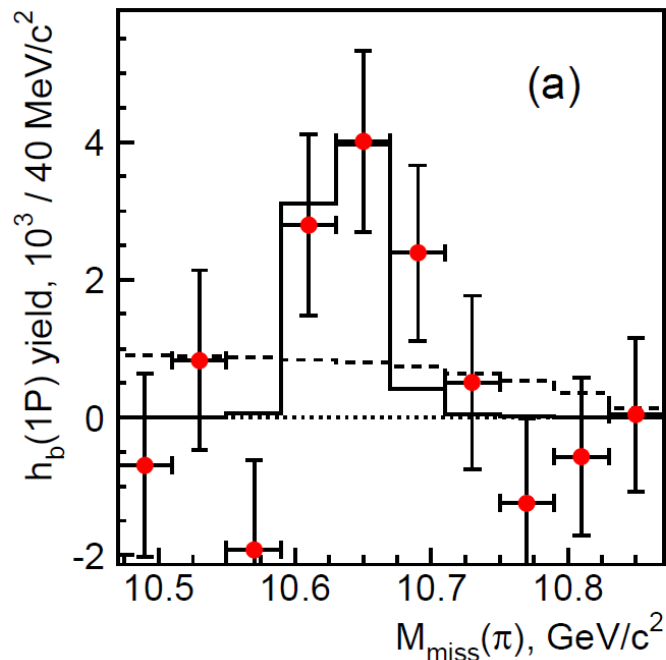


$Y(6S) \rightarrow h_b(nP)\pi^+\pi^-$ 

$M_{\text{miss}}(\pi)$  data do not follow phase space distribution, but populate  $Z_b$  mass region.

Hypotheses:

- Both  $Z_b(10610)$  &  $Z_b(10650)$  ( ——— )
- Phase space ( - - - - ) excluded at level  $3.6 \sigma$  ( $h_b(1P)$ ) and  $4.5 \sigma$  ( $h_b(2P)$ )
- Single  $Z_b(10610)$  excluded at level  $3.3 \sigma$  ( $h_b(1P)$ )
- Single  $Z_b(10650)$  cannot be excluded at significant level



$$e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}\pi^\pm$$

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- $Z_b(10610)$  &  $Z_b(10650)$  contain at least four quarks (including  $b\bar{b}$ ).
- One of the models: loosely bound  $B^{(*)}\bar{B}^*$  systems.
- Decay rates of  $Z_b \rightarrow B^{(*)}\bar{B}^*$  are expected to be significant.
- Evidence for  $Y(5S) \rightarrow B\bar{B}^*\pi$  was reported by Belle ( $23.6 \text{ fb}^{-1}$ ).

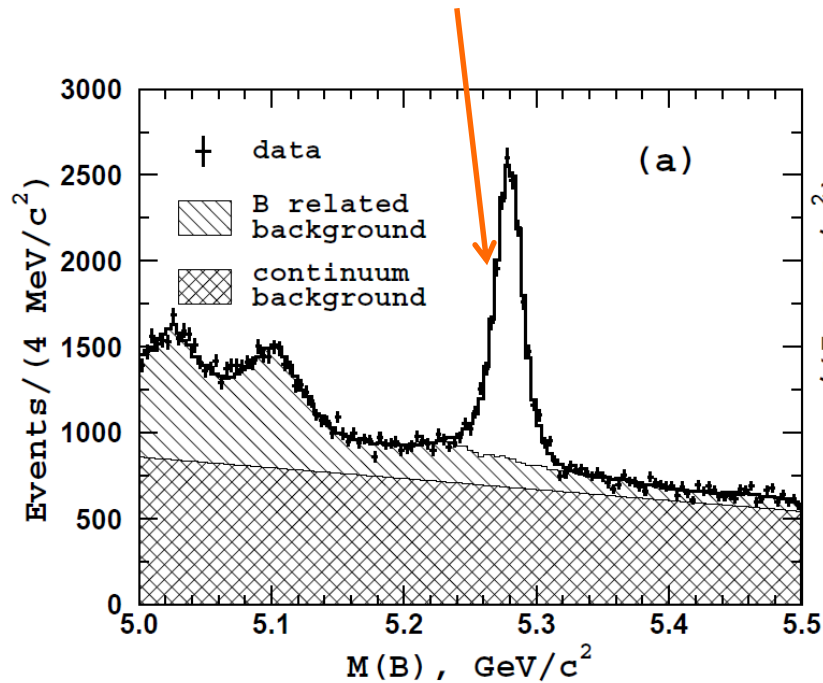
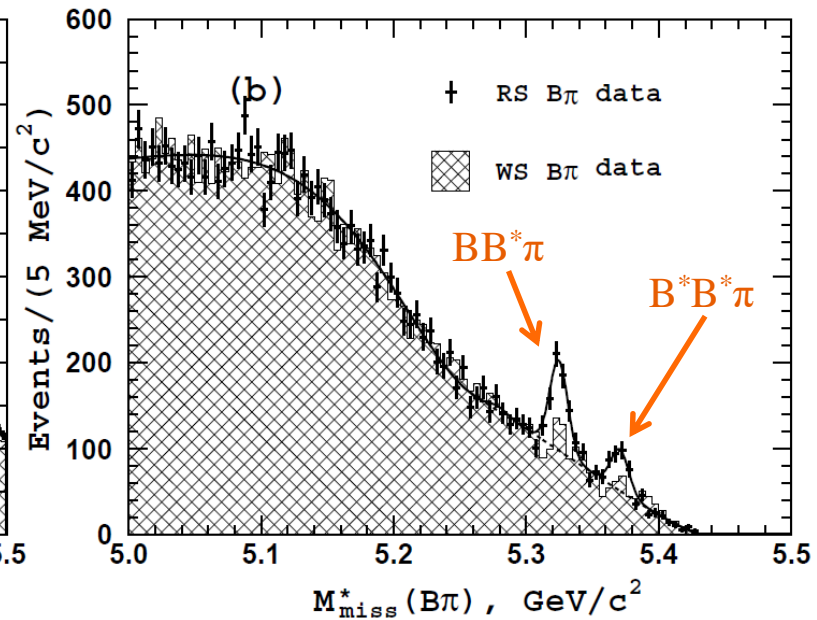
### Data:

- $121.4 \text{ fb}^{-1}$  at  $Y(5S)$  resonance;

### Selection:

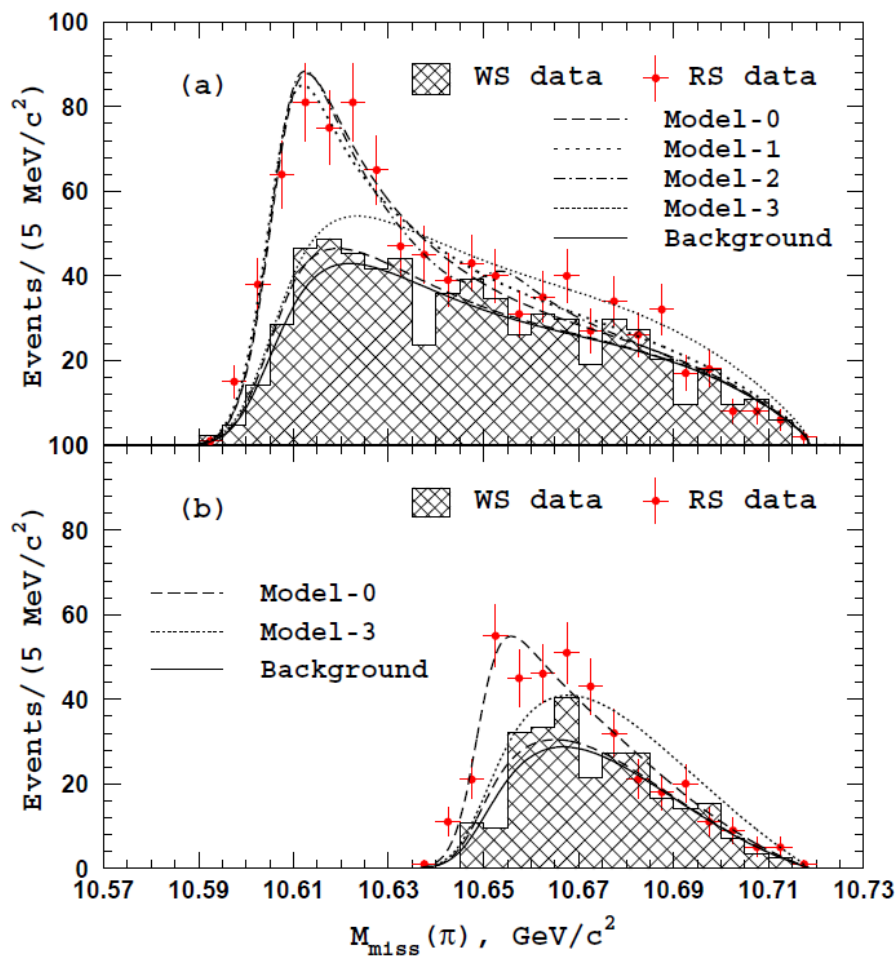
- one B meson from 16 decay modes ( $J/\psi K^{(*)}$  &  $D^{(*)}\pi$ );
- $\cos\theta_{\text{thrust}} < 0.8$ ;
- momentum  $P(B) < 1.35 \text{ GeV}$ ;
- invariant mass consistent with B meson.

## B meson reconstruction

 $B^+$  and  $B^0$  combination with  $\pi^{(+)}$   
form **Right** (Wrong) Sign data

After selecting  $B\bar{B}^*\pi$  and  $B^*\bar{B}^*\pi$  events we perform  $M_{\text{miss}}(\pi)$  fit.

- Simultaneous fit of RS and WS samples.
- WS data are used to estimate background.
- $Z_b$  parameters are fixed from  $Y(5S) \rightarrow Y(nS)\pi^+\pi^-$  and  $Y(5S) \rightarrow h_b(nP)\pi^+\pi^-$  decays.



**Model 0:** single  $Z_b$  amplitude

**Model 1:** + non-res component

(no significant improvement compared to Model 0)

**Model 2:** + another  $Z_b$  amplitude

(no significant improvement compared to Model 0)

**Model 3:** pure non-res amplitude

(fit is significantly worse)

Born cross sections are  $\sigma(e^+e^- \rightarrow [B\bar{B}^* + \text{c.c.}]^\pm \pi^\mp) = (17.4 \pm 1.6 \pm 1.9)$  pb  
 $\sigma(e^+e^- \rightarrow [B^*\bar{B}^*]^\pm \pi^\mp) = (8.75 \pm 1.15 \pm 1.04)$  pb  
 $\sigma(e^+e^- \rightarrow [B\bar{B}]^\pm \pi^\mp) < 2.9$  pb

Channel	Fraction, %	
	$Z_b(10610)$	$Z_b(10650)$
$\Upsilon(1S)\pi^+$	$0.54^{+0.16+0.11}_{-0.13-0.08}$	$0.17^{+0.07+0.03}_{-0.06-0.02}$
$\Upsilon(2S)\pi^+$	$3.62^{+0.76+0.79}_{-0.59-0.53}$	$1.39^{+0.48+0.34}_{-0.38-0.23}$
$\Upsilon(3S)\pi^+$	$2.15^{+0.55+0.60}_{-0.42-0.43}$	$1.63^{+0.53+0.39}_{-0.42-0.28}$
$h_b(1P)\pi^+$	$3.45^{+0.87+0.86}_{-0.71-0.63}$	$8.41^{+2.43+1.49}_{-2.12-1.06}$
$h_b(2P)\pi^+$	$4.67^{+1.24+1.18}_{-1.00-0.89}$	$14.7^{+3.2+2.8}_{-2.8-2.3}$
$B^+\bar{B}^{*0} + \bar{B}^0B^{*+}$	$85.6^{+1.5+1.5}_{-2.0-2.1}$	—
$B^{*+}\bar{B}^{*0}$	—	$73.7^{+3.4+2.7}_{-4.4-3.5}$

$\rightarrow Z_b$  decays are dominated by  $B^{(*)}\bar{B}^*$  channels

# $Y(4S) \rightarrow \eta h_b(1P)$

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- QCD multipole expansion (low  $m, n$ ):  $Y(nS) \rightarrow Y(mS)(gg) \xrightarrow{E1E1} \pi\pi$
- Above BB threshold spin-flip processes are not suppressed due to presence of exotic bottomonium.  $\xrightarrow{E1M2} \eta$  suppressed due to spin flip
- Branching of  $Y(4S) \rightarrow \eta h_b(1P)$  is predicted to be  $10^{-3}$  (*PRL 105 162001*).

## Data:

- $711 \text{ fb}^{-1}$  at  $Y(4S)$  resonance.

## Selection:

- $R_2 < 0.3$ ;
- $\eta \rightarrow \gamma\gamma$ ;
- $\cos\theta_{\text{hel}} < 0.9$ ;
- $\pi^0$  veto.

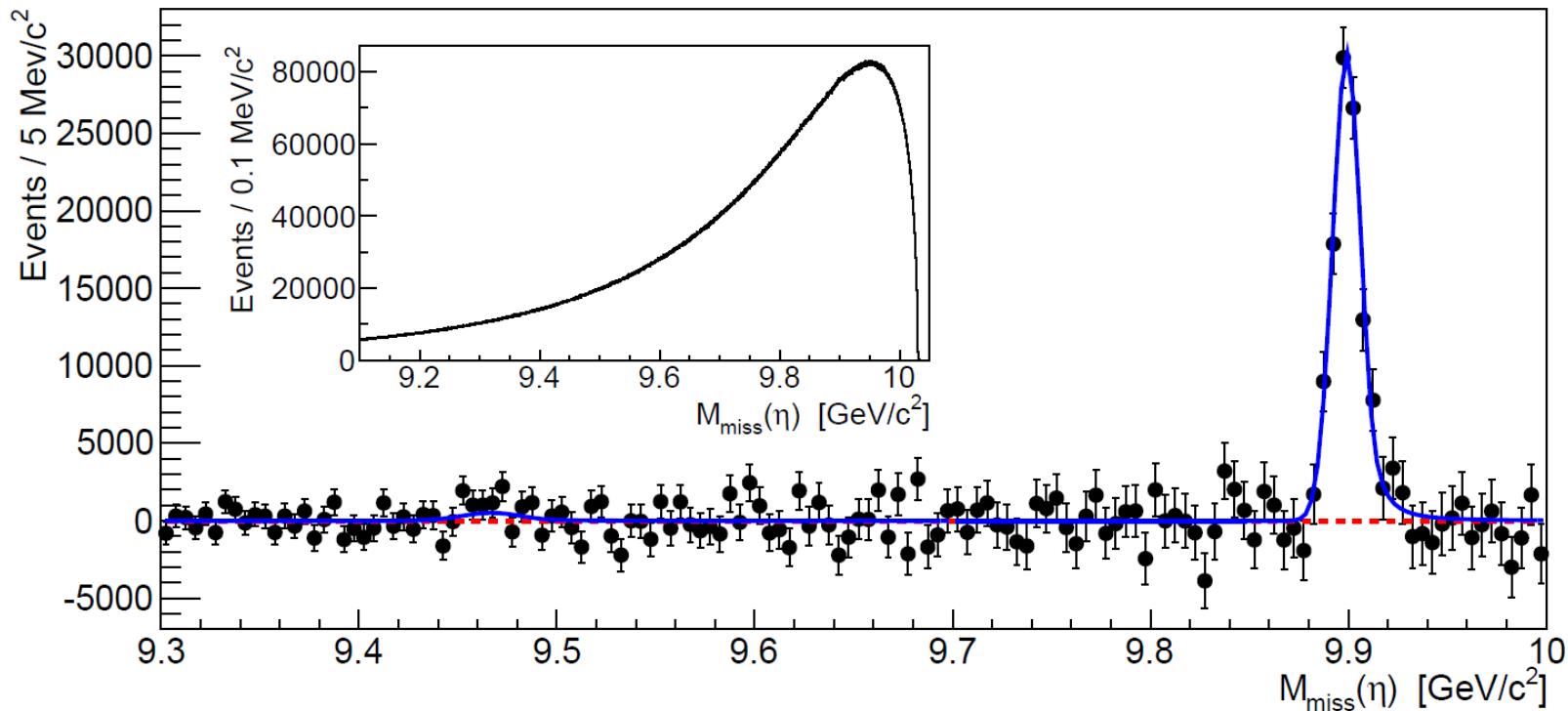
$$M_{h_b(1P)} = (9899.3 \pm 0.4 \pm 1.0) \text{ MeV}$$

$$\mathcal{B}[\Upsilon(4S) \rightarrow \eta h_b(1P)] = (2.18 \pm 0.11 \pm 0.18) \times 10^{-3}$$

$$\mathcal{B}[\Upsilon(4S) \rightarrow \eta \Upsilon(1S)] < 2.7 \times 10^{-4} \quad 90\% \text{ CL (agreement with BaBar)}$$

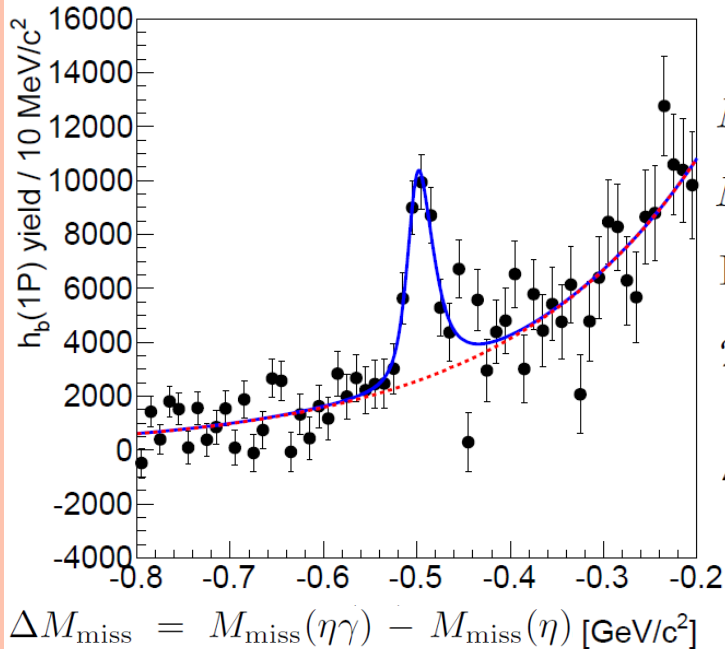
$$1P \text{ hyperfine splitting } \Delta M_{\text{HF}}(1P) = m(h_b(1P)) - m^{\text{sa}}(\chi_{bJ}(1P))$$

$$\Delta M_{\text{HF}}(1P) = (+0.6 \pm 0.4 \pm 1.0) \text{ MeV} \quad (\text{no sizeable spin-spin interactions})$$



strongest known transition of  $\Upsilon(4S)$  to lower bottomonium

## Y(4S) → η h<sub>b</sub>(1P) → η γ η<sub>b</sub>(1S)



$$M_{\eta_b(1S)} - M_{h_b(1P)} = (-498.6 \pm 1.7 \pm 1.2) \text{ MeV}$$

$$M_{\eta_b(1S)} = M_{h_b(1P)} + \Delta M_{\text{miss}} = (9400.7 \pm 1.7 \pm 1.6) \text{ MeV}$$

$$\Gamma_{\eta_b(1S)} = (8_{-5}^{+6} \pm 5) \text{ MeV}$$

$$\mathcal{B}[h_b(1P) \rightarrow \gamma \eta_b(1S)] = \frac{N_{\eta_b(1S)} \epsilon_{\eta h_b(1P)}}{N_{h_b(1P)} \epsilon_{\eta \gamma \eta_b(1S)}} = (56 \pm 8 \pm 4)\%$$

$$\Delta M_{\text{HF}}(1S) = (59.6 \pm 1.7 \pm 1.6) \text{ MeV}$$

### M(η<sub>b</sub>(1S))

- in agreement with Y(5S) → π<sup>+</sup>π<sup>-</sup>h<sub>b</sub>(1P) → π<sup>+</sup>π<sup>-</sup>γ η<sub>b</sub>(1S):
  - (9402.4 ± 1.5 ± 1.8) MeV (*PRL* **109**, 232002);
- in discrepancy with Y(2S,3S) → γ η<sub>b</sub>(1S):
  - (9388.9 <sup>+3.1</sup><sub>-2.3</sub> ± 2.7) MeV (*PRL* **101** 071801),
  - (9390.8 ± 3.2) MeV (*PRL* **103** 161801),
  - (9391.8 ± 6.6 ± 2.0) MeV (*PRD* **81** 031104).

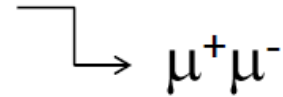


- $ee \rightarrow Y(nS)\pi\pi$  ( $n = 1, 2, 3$ ) &  $ee \rightarrow bb$ 
  - We have measured the cross sections  $e^+e^- \rightarrow Y(nS)\pi^+\pi^-$  ( $n = 1, 2, 3$ ) and  $e^+e^- \rightarrow bb$  in the region  $\sqrt{s} = 10.8 - 11.05$  GeV to determine masses and widths for  $Y(5S)$  and  $Y(6S)$ .
  - $R_{Y(nS)\pi\pi}$  is dominated by the two resonances with no continuum.
  - $R_b$  fit is not reliable enough.
  - No peaking structure is seen at 10.9 GeV.
- $ee \rightarrow h_b(nP)\pi\pi$ 
  - We have measured the  $e^+e^- \rightarrow h_b(nP)\pi^+\pi^-$  cross section and determined the parameters of  $Y(10860)$  and  $Y(11020)$ .
  - First evidence for  $Y(6S) \rightarrow h_b(1P)\pi^+\pi^-$ .
  - First observation of  $Y(6S) \rightarrow h_b(2P)\pi^+\pi^-$ .
  - These transitions proceed either through one or two  $Z_b$ 's.
- $ee \rightarrow B^{(*)}\bar{B}^{(*)}\pi$ 
  - First observations of  $e^+e^- \rightarrow B\bar{B}^*\pi$  and  $e^+e^- \rightarrow B^*\bar{B}\pi$  and cross sections measurement.
  - Upper limit on  $e^+e^- \rightarrow B\bar{B}\pi$ .
  - These processes are dominated by  $e^+e^- \rightarrow Z_b\pi$ .
- $Y(4S) \rightarrow \eta h_b(1P)$ 
  - First observation of  $Y(4S) \rightarrow \eta h_b(1P)$  and branching measurement.
  - New measurement of  $h_b(1P)$  mass and calculation of 1P hyperfine splitting.
  - Branching measurement of  $h_b(1P) \rightarrow \gamma \eta_b(1S)$ .
  - New measurement of the  $\eta_b(1S)$  width and  $h_b(1P) - \eta_b(1S)$  mass difference and calculation of  $\eta_b(1S)$  mass and 1S hyperfine splitting.



# Backup

# Selection of $\sigma(e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-)$



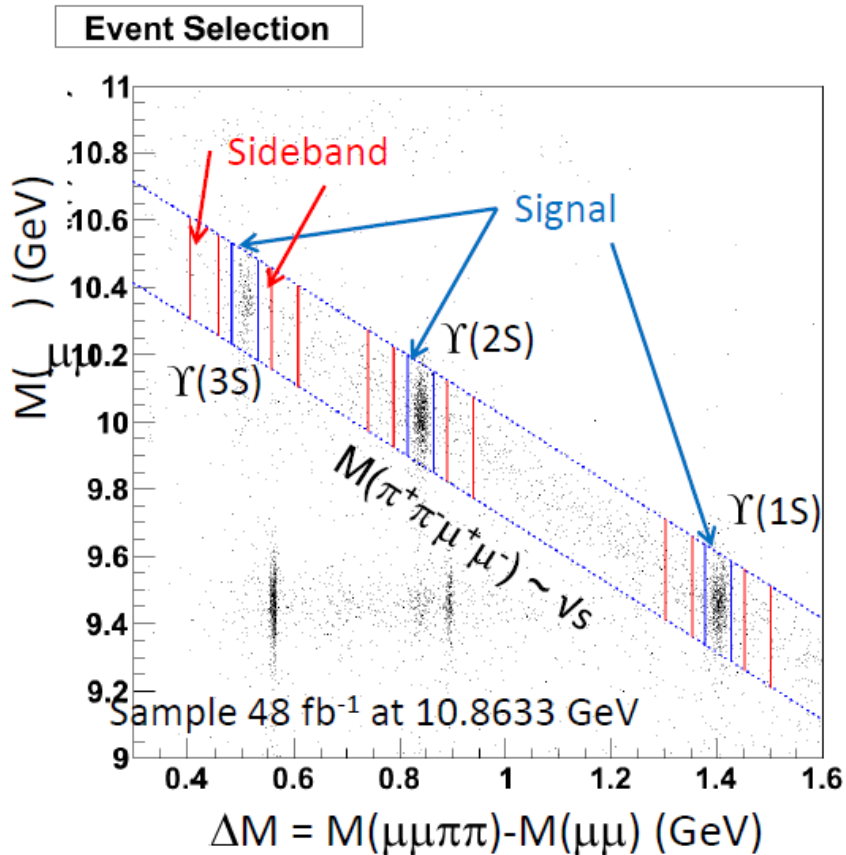
Similar event selection to  
PRD 82, 091106(R) 2010

- $\pi^+\pi^-\mu^+\mu^-$  & no other tracks
- $M(\pi^+\pi^-\mu^+\mu^-)$  consistent with  $\sqrt{s}$
- $\Delta M = M(\pi^+\pi^-\mu^+\mu^-) - M(\mu^+\mu^-)$  consistent with  $\sqrt{s} - M_{\Upsilon(nS)}$

Data :  $e^+e^- \rightarrow \Upsilon(nS)[\mu^+\mu^-]\pi^+\pi^-$

- 10.63-11.02 GeV
- 22  $\sim 1 \text{ fb}^{-1}$  scan points
- 121  $\text{fb}^{-1}$  on-resonance at  $\Upsilon(10860)$

More detail in BN1307



# Method



Consider all  $\pi^+\pi^-$  pairs, fit  $M_{\text{miss}}(\pi^+\pi^-)$  spectrum.

Use energy calibration by Yuan-Pao Yang and Dan Santel.

# Selection

Same as in  $h_b$ ,  $\eta_b$  papers.

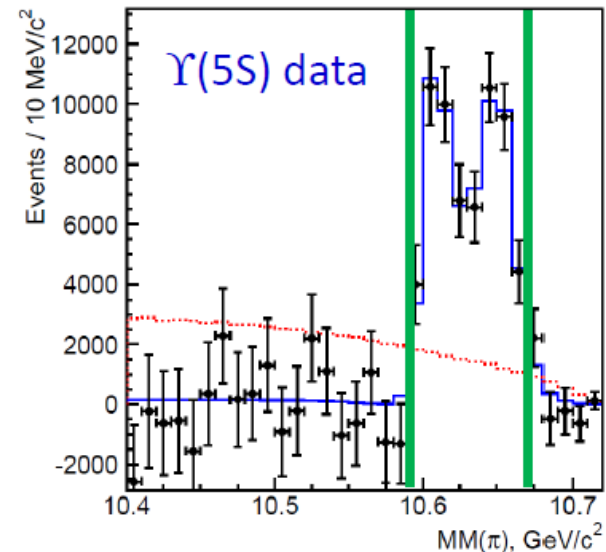
HadronB skim

$dr < 0.3\text{cm}$ ,  $dz < 2\text{cm}$

$L(\pi/K) > 0.1$ ,  $L(\pi/p) > 0.1$ , e veto:  $P_e < 0.9$

$R2 < 0.3$

$Z_b$  mass window:  $10.59 < M_{\text{miss}}(\pi) < 10.67 \text{ GeV}$



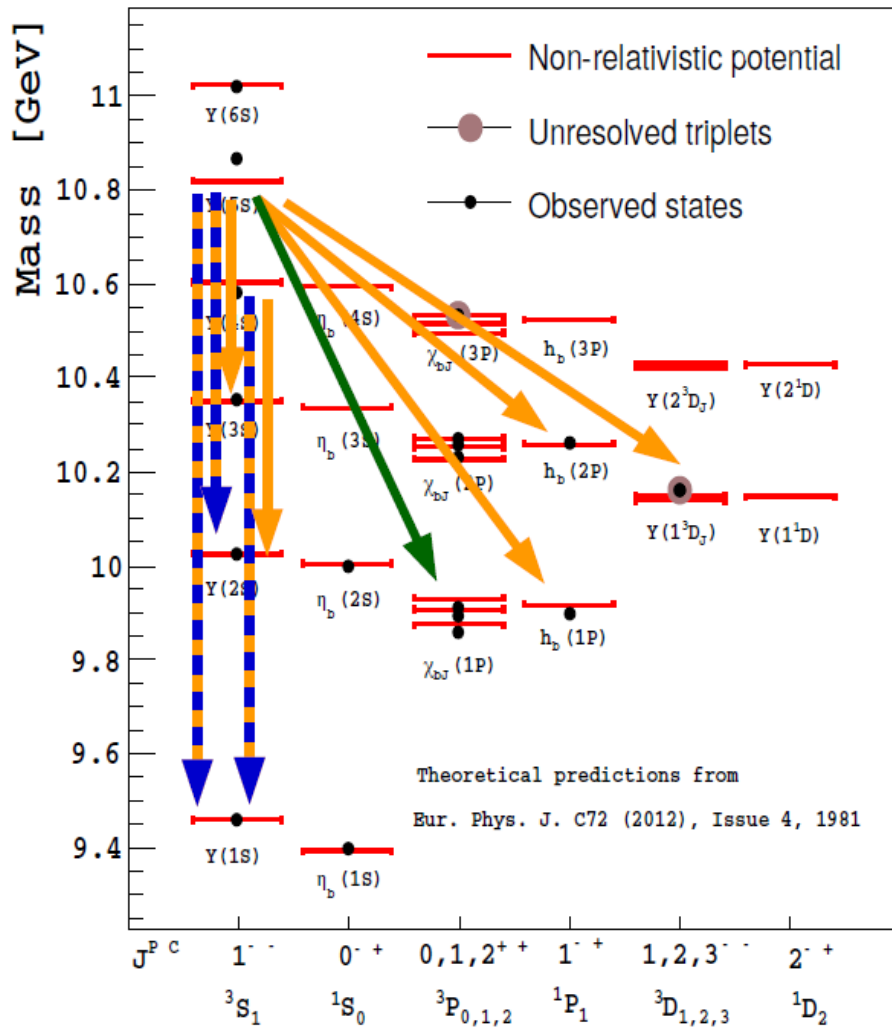
B candidates are reconstructed in the following decay modes:



$B^- \rightarrow D^0 \pi^-$	$D^0 \rightarrow K^- \pi^+; K^- \pi^+ \pi^0; K^- \pi^- \pi^+ \pi^+$
$D^{*0} \pi^-$	$D^{*0} \rightarrow D^0 \pi^0$ $\hookrightarrow D^0 \rightarrow K^- \pi^+; K^- \pi^- \pi^+ \pi^+$
$J/\psi K^-$	$J/\psi \rightarrow \mu^+ \mu^-; e^+ e^-$
$\bar{B}^0 \rightarrow D^+ \pi^-$	$D^+ \rightarrow K^+ \pi^- \pi^-$
$D^{*+} \pi^-$	$D^{*+} \rightarrow D^0 \pi^+$ $\hookrightarrow D^0 \rightarrow K^- \pi^+; K^- \pi^+ \pi^0; K^- \pi^- \pi^+ \pi^+$ $D^{*+} \rightarrow D^+ \pi^0$ $\hookrightarrow D^+ \rightarrow K^+ \pi^- \pi^-$
$J/\psi K_S^0$	$J/\psi \rightarrow \mu^+ \mu^-; e^+ e^-$ $K_S^0 \rightarrow \pi^+ \pi^-$
$J/\psi \bar{K}^{*0}$	$J/\psi \rightarrow \mu^+ \mu^-; e^+ e^-$ $\bar{K}^{*0} \rightarrow K^- \pi^+$

16 decay modes in total

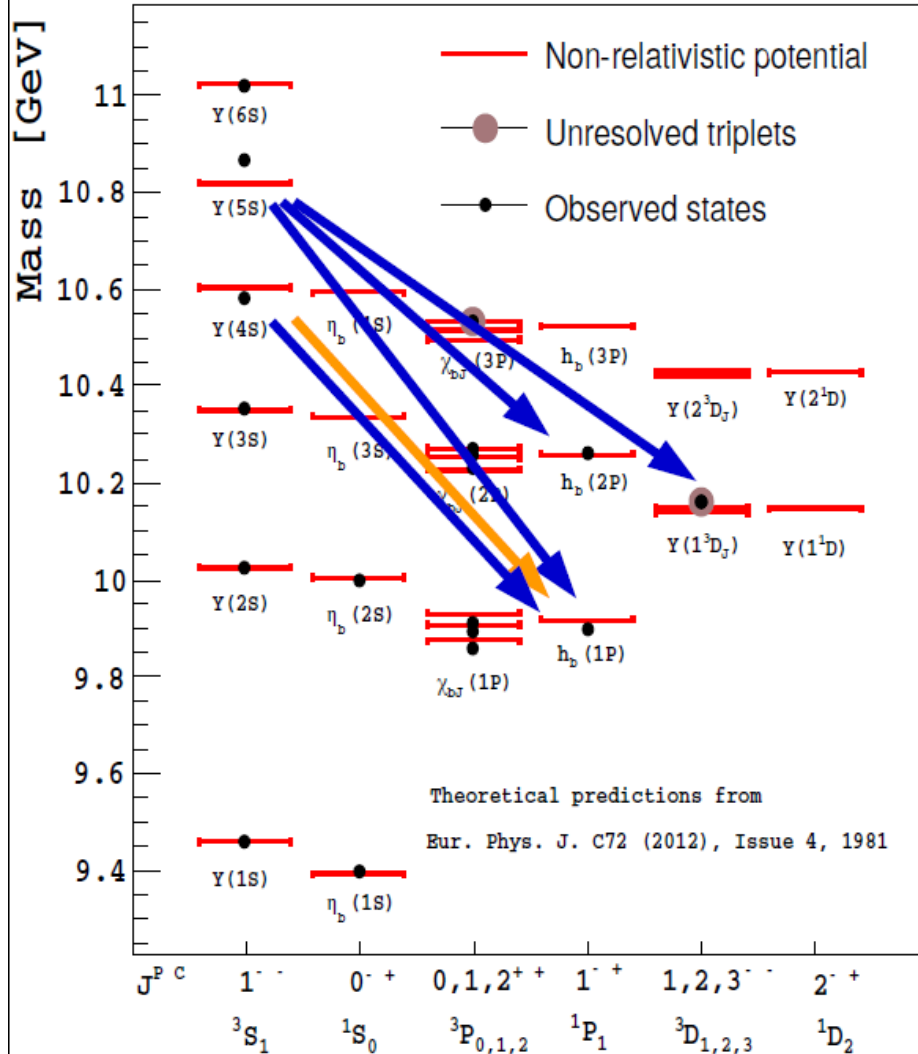
# Y(4,5S) hadronic transitions



What we have measured from Y(4,5S):

- Y(5S)  $\rightarrow$   $\eta/\pi\pi$  Y(1S)
- Y(5S)  $\rightarrow$   $\eta/\pi\pi$  Y(2S)
- Y(5S)  $\rightarrow$   $\pi\pi$  Y(3S)
- Y(5S)  $\rightarrow$   $\pi\pi$  hb(1P)
- Y(5S)  $\rightarrow$   $\pi\pi$  hb(2P)
- Y(5S)  $\rightarrow$   $\eta/\pi\pi$  Y( $^3D$ )
- Y(5S)  $\rightarrow$   $\omega$   $\chi_b$ (1P)
  
- Y(4S)  $\rightarrow$   $\eta/\pi\pi$  Y(1S)
- Y(4S)  $\rightarrow$   $\pi\pi$  Y(2S)

# Y(4,5S) Missing hadronic transitions



What we are missing:

Y(5S)  $\rightarrow$   $\eta$  hb(1P)

Y(5S)  $\rightarrow$   $\eta$  hb(2P)

Y(5S)  $\rightarrow$   $\eta$  Y(1D)

Y(4S)  $\rightarrow$   $\pi\pi$  hb(1P)

Y(4S)  $\rightarrow$   $\eta$  hb(1P)

Y(4S)  $\rightarrow$   $\eta$  hb(1P)

Guo, PRL 105

Predicted as large as  $10^{-3}$  (2010) 162001

Y(5S)  $\rightarrow$   $\eta$  hb(1P)

Y(5S)  $\rightarrow$   $\eta$  hb(2P)

No predictions

# $\eta \rightarrow \gamma\gamma$ reconstruction



## Event reconstruction

Inclusive  $\eta \rightarrow \gamma\gamma$  reconstruction  
Fit of  $MM(\eta)$

## Selection Criteria

### Good photon quality

- shower containment
- $E > 50$  MeV

$\cos(\text{helicity angle}) < 0.9$

$\pi^0$  veto

$|M(\gamma\gamma) - M(\eta)| < 0.026$  GeV

Kinematic fit with mass constraint

## Continuum suppression

$R2 < 0.3$

