



## LPT-Orsay

### Some phenomenological aspects of sterile fermions

- 👉 Motivating sterile neutrinos
- 👉 Theoretical frameworks
- 👉 Direct and indirect searches: LFUV, cLFV, CPV,...  
at high-intensities and colliders



Invisibles 2016, Padova, 12 Septembre 2016

# Beyond the SM: sterile fermions

## 👉 Observational problems (not accounted by the SM):

BAU, DM,  $\nu$  masses & mixings

## 👉 Extending the SM with sterile fermions: singlets under $SU(3)_c \times SU(2)_L \times U(1)_Y$

Interactions with SM fields: through mixings with **active neutrinos**

A priori, **no bound** on the **number** of sterile states, **no limit** on their **mass scale(s)**

Present in several **theoretical models** accounting for  $\nu$  masses and mixings

## ▶ Interest & phenomenological implications - strongly dependent on their mass!

**eV scale**  $\leftrightarrow$  extra neutrinos suggested by **short baseline  $\nu$  oscillation anomalies**

**keV scale**  $\leftrightarrow$  warm dark matter candidates; explain **pulsar velocities (kicks)**; 3.5 keV line..

**MeV - TeV scale**  $\leftrightarrow$  **experimental testability!** (and BAU, DM,  $m_\nu$  generation...)

**Beyond  $10^9$  GeV**  $\leftrightarrow$  **theoretical appeal:** standard seesaw, BAU, GUTs

$m_{\nu_s}$	Motivation	$\nu$ -oscillations	laboratory searches
$\lesssim \text{eV}$	$\nu$ -oscil. anomalies, dark radiation	masses by seesaw, explain anomalies	oscillation anomalies, $\beta$ -decays
keV	DM	no if DM	direct searches? , nuclear decays?
MeV	testability	masses by seesaw	intensity frontier, $0\nu\beta\beta$
GeV	testability, minimality	masses by seesaw	intensity frontier, EW precision data, $0\nu\beta\beta$
TeV	minimality, testability	masses by seesaw	LHC
$\gtrsim 10^9 \text{ GeV}$	grand unification, "naturalness"	masses by seesaw	-



$m_{\nu_s}$	CMB	BBN	DM	Leptogenesis
$\lesssim \text{eV}$	explain $N_{\text{eff}} > 3$	may explain $N_{\text{eff}} > 3$	no	no
keV	act as DM, no effect on $N_{\text{eff}}$	effect on $N_{\text{eff}}$ too small if DM	good candidate	no
MeV	unaffected	constrains $m_{\nu_s} \gtrsim 200 \text{ MeV}$	no	possible (finetuning)
GeV	unaffected	unaffected	no	possible
TeV	unaffected	unaffected	no	possible
$\gtrsim 10^9 \text{ GeV}$	unaffected	unaffected	no	natural

[Adapted from  
Drewes, '13]

👉 **Extending the SM with sterile fermions:** (testable!) theoretical frameworks

▶ Incorporating  $\nu_R$  - low scale seesaws: type I seesaw [ TeV ]  $\rightarrow$  small  $Y^\nu$

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & v Y^{\nu T} \\ v Y^\nu & M_R \end{pmatrix}$$

$$\Rightarrow m_\nu \approx -v^2 Y_\nu^T \frac{1}{M_R} Y_\nu$$

type I seesaw & MFV  $\rightarrow$  "large"  $Y^\nu$

$\nu$ MSM [ GeV ]  $\rightarrow$  tiny  $Y^\nu$

▶ Incorporating  $\nu_R$  and additional sterile fermions: Inverse seesaw (ISS)  $\rightarrow$  sizeable  $Y^\nu$

$$\mathcal{M}_{\text{ISS}} = \begin{pmatrix} 0 & Y_\nu^T v & 0 \\ Y_\nu v & 0 & M_R \\ 0 & M_R^T & \mu_X \end{pmatrix}$$

$$\Rightarrow m_\nu \approx \frac{(Y_\nu v)^2}{M_R^2} \mu_X$$

Linear seesaw (LSS)  $\rightarrow$  sizeable  $Y^\nu$

$$\mathcal{M}_{\text{LSS}} = \begin{pmatrix} 0 & Y_\nu^T v & M_L^T \\ Y_\nu v & 0 & M_R \\ M_L & M_R^T & 0 \end{pmatrix}$$

$$\Rightarrow m_\nu \approx (v Y_\nu) (M_L M_R^{-1})^T + (M_L M_R^{-1}) (v Y_\nu)^T$$

[see, e.g., Mohapatra et al, 1986, Gonzalez-Garcia et al, 1988, Deppisch et al, '04, Asaka et al, '05, Gavela et al, '09, Ibarra, Petcov et al, '10, Abada, Lucente, '14, ...]

👉 **Extending the SM with sterile fermions:** phenomenological consequences

▶ **Modified charged ( $W^\pm$ ) and neutral ( $Z^0$ ) current interactions:**

$$\mathcal{L}_{W^\pm} \sim -\frac{g_w}{\sqrt{2}} W_\mu^- \sum_{\alpha=e,\mu,\tau} \sum_{i=1}^{3+N_S} \mathbf{U}_{\alpha i} \bar{\ell}_\alpha \gamma^\mu P_L \nu_i$$

$$\mathcal{L}_{Z^0} \sim -\frac{g_w}{2 \cos \theta_w} Z_\mu \sum_{i,j=1}^{3+N_S} \bar{\nu}_i \gamma^\mu \left[ P_L (\mathbf{U}^\dagger \mathbf{U})_{ij} - P_R (\mathbf{U}^\dagger \mathbf{U})_{ij}^* \right] \nu_j$$

$\mathbf{U}_{\alpha i}$   $\rightarrow$  modified lepton mixing - now encodes also active-sterile mixings

(for  $N_s = 0$ ,  $\mathbf{U}_{\alpha i} = U_{\text{PMNS}}$ )

▶ If sufficiently light, sterile  $\nu$ s can be **produced as final states**

👉 **Huge impact for numerous observables:** high-intensity and colliders (as well as DM, ..)

But also abundant constraints..

👉 **Illustrate these phenomenological consequences via simple ad-hoc extensions:**

SM +  $N_s$  sterile fermions

👉 **Extending the SM with sterile fermions:** (testable!) simple “ad-hoc models”

First phenomenological studies can be carried for SM +  $\#\nu_s \rightarrow “3 + N_s”$

No hypothesis on mechanism of neutrino mass generation (seesaw, ...)

Physical parameters: masses [3 light (mostly active) +  $N_s$  heavier (mostly sterile) states]

mixing matrix (angles and CPV phases)

$$U_{(3+N_s) \times (3+N_s)} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} & \cdots \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} & \cdots \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} & \cdots \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} & \cdots \\ \vdots & \vdots & \vdots & \vdots & \ddots \end{pmatrix}$$

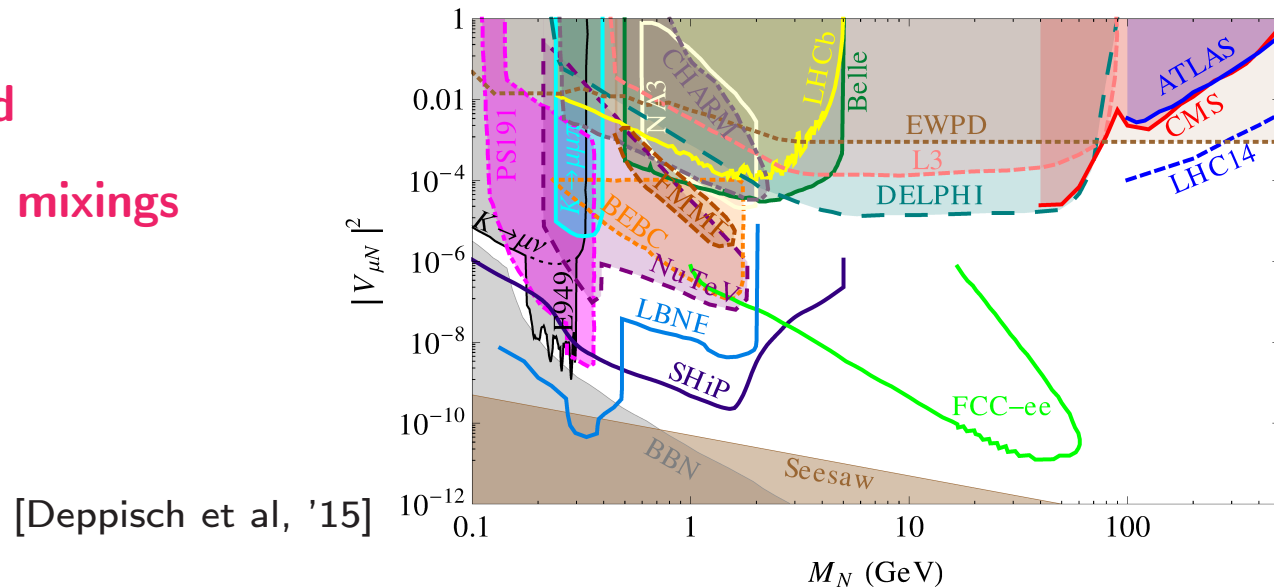
Left-handed lepton mixing  $U_{\alpha 1-3}$  :

$\tilde{U}_{PMNS}$  (non-unitary)

Active-sterile mixing:  $U_{\alpha i}$

$$\mathbf{U} = U|_{3 \times (3+N_s)}$$

👉 **Heavily constrained  
sterile masses and mixings**



## 👉 Constraints on sterile fermions

👉 **Neutrino oscillation parameters:**  $\tilde{U}_{\text{PMNS}}$  comply with observed mixings

👉 **Electroweak precision tests:** invisible  $Z$  width; leptonic  $Z$  width; Weinberg angle...  
[Del Aguila et al, '08; Atre et al, '09; ...  
Antusch et al, '09-'14; Fernandez-Martinez et al, '16; ...]

👉 **Searches at the LHC:** invisible Higgs decays  $H \rightarrow \nu_L \nu_R$ ; direct searches, ...  
[Dev et al, '12-'15; Bandyopadhyay et al, '12; Cely et al, '14;  
Arganda et al, '14-'15; Deppish et al, '15; ...]

👉 **Peak searches in meson decays:** monochromatic lines in  $\ell^\pm$  spectrum from  $X_M^\pm \rightarrow \ell^\pm \nu_s$   
[Shrock, '80-'81; Atre et al, '09; Kusenko et al, '09; Lello et al, '13]

👉 **Beam dump experiments:**  $\nu_s$  decay products (light mesons,  $\ell^\pm$ ) from  $X_M^\pm$  decays  
[PS191, CHARM, NuTeV, ...]

## 👉 Constraints on sterile fermions (contd.)

👉 **Neutrinoless double beta decays -  $|m_{ee}|$ :** [EXO-200, KamLAND-Zen, GERDA,...]  
[Blenow et al, '10; Lopez-Pavon et al, '13;  
AA et al, '14, ..., Giunti et al]

👉 **Rare meson decays: Lepton Number Violating (LNV)** e.g.  $K^+ \rightarrow \ell^+ \ell^+ \pi^-$

**Lepton Universality Violating (LUV)** e.g.  $R_{X_M}, R(D), R_\tau$   
[CLEO, Belle, BaBar, NA62, LHCb, BES III, ...]  
[Shrock, '81; Atre et al, '09; AA et al, '13-'15, ...]

👉 **Lepton Flavour Violation: 3 body decays among most stringent...**

[Gronau et al, '85; Ilakovac & Pilaftsis, '95 - '14;  
Deppisch et al, '05; Dinh et al, '12; Alonso et al, '12; ...]

👉 **Cosmology:** large scale structures, Lyman- $\alpha$ , BBN, CMB, X-ray, SN1987a, ...

[Smirnov et al, '06; Kusenko, '09; Gelmini, '10;  
Donini et al, '14; Hernández et al, '15-'16; ...]



## ☞ Sterile fermions: contributions to observables

### ➔ Cosmology and astroparticle

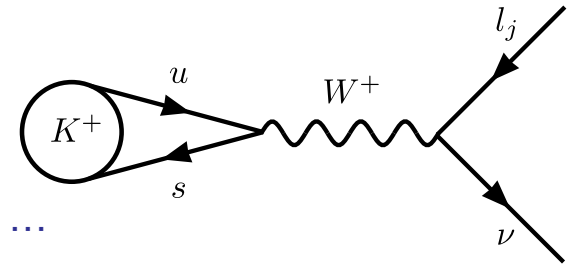
⇒ BAU from leptogenesis (oscillations) [See talk by Hernandez]

⇒ (Warm) dark matter candidates [White paper: Drewes et al, '16, Merle, AA, Lucente, Arcadi, '14, ...]

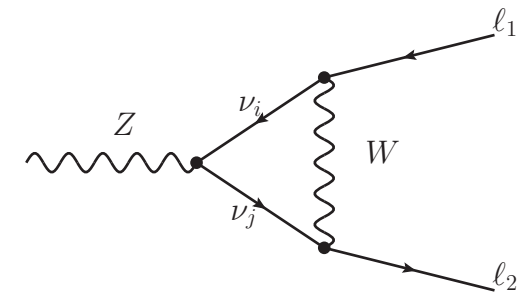
⇒ Astrophysical puzzles: pulsar kicks, ... [e.g. Kusenko, '04 & '09]

### ➔ Particle physics

**Lepton properties:** {  
Electric and magnetic moments  
Neutrinoless double beta decay (LNV)  
Violation of flavour universality (e.g.  $\Delta r_K$ ), ...



**Rare decays:** {  
Lepton number violation  
Violation of lepton flavour  
cLFV  $Z$  decays  
cLFV and invisible  $H$  decays  
Collider signatures, ...



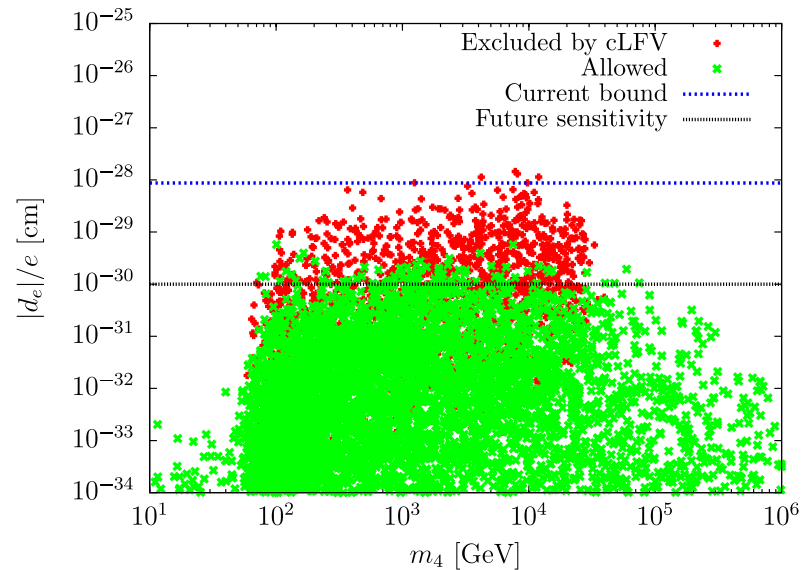
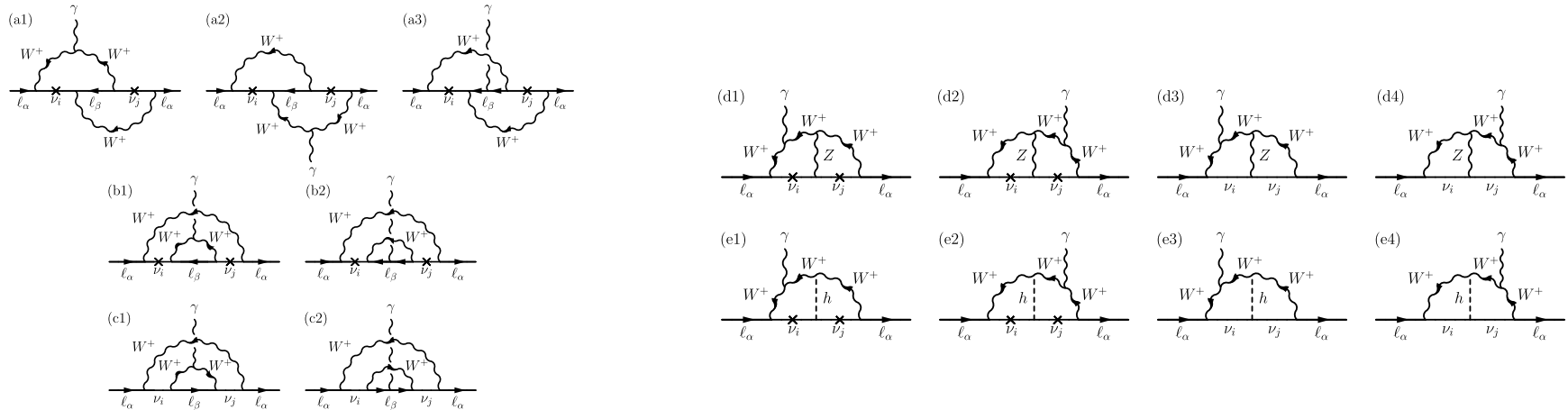
## ☞ Sterile fermions & CPV: contributions to EDMs

- ▶ Majorana (and Dirac) phases  $\Rightarrow$  lepton EDMs:

$$d_e = -\frac{g_2^4 e m_e}{4(4\pi)^2 m_W^2} \sum_{\beta} \sum_{i,j} \left[ J_{ije\beta}^M I_M(x_i, x_j) + J_{ije\beta}^D I_D(x_i, x_j) \right],$$

$$J_{ij\alpha\beta}^M \equiv \text{Im} (U_{\alpha j} U_{\beta j} U_{\beta i}^* U_{\alpha i}^*), \quad J_{ij\alpha\beta}^D \equiv \text{Im} (U_{\alpha j} U_{\beta j}^* U_{\beta i} U_{\alpha i}^*)$$

- ▶ Many new (2-loop) contributions!



- ▶ Non-vanishing contributions: at least two sterile  $\nu$

- ▶  $|d_e|/e \geq 10^{-30}$  cm for  $m_{\nu_{4,5}} \sim [100 \text{ GeV}, 100 \text{ TeV}]$

Within ACME reach

[AA and Toma, '15]

## ☞ Sterile fermions: lepton number violation

### ▶ Lepton number violation: $0\nu 2\beta$ decays

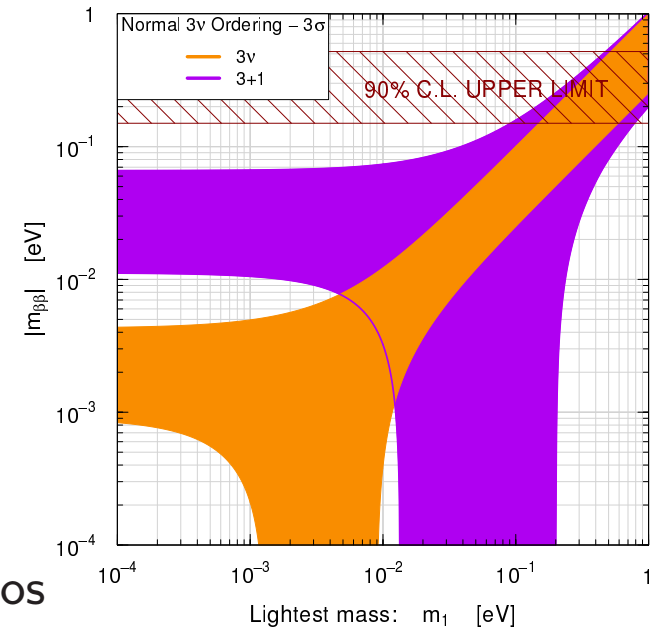
▶  $\nu_s$  can strongly impact predictions for  $|m_{ee}|$

⇒ augmented ranges for effective mass (*IH and NH*)

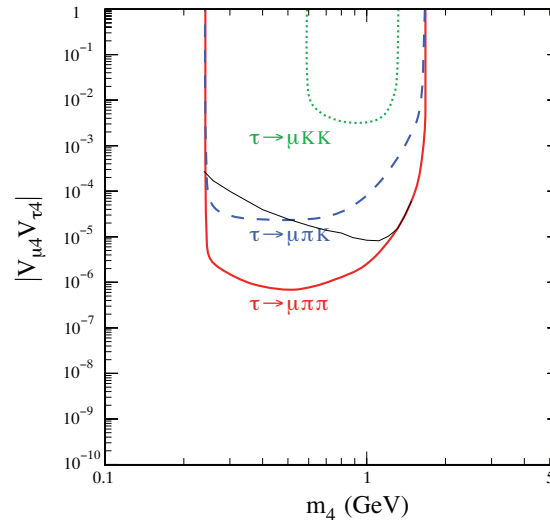
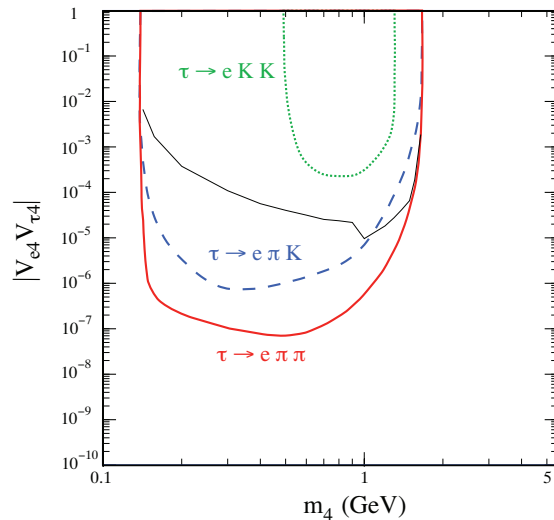
▶ Observation of  $0\nu 2\beta$  signal in future experiments

does not imply **Inverted Ordering** for light neutrinos

[AA, De Romeri and Teixeira, '14; Lopez-Pavon et al. '13, Girardi, Meroni, Petcov, '13,...; Giunti et al, '15 ←]



### ▶ Lepton number violation in meson decays



$$\tau^- \rightarrow l^+ \pi^- \pi^- (K^- K^-)$$

$$\tau^- \rightarrow l^+ \pi^- K^-$$

$$D_{(s)}^- \rightarrow l^- l'^- \pi^+ (K^+)$$

$$B^- \rightarrow l^- l'^- \pi^+ (K^+, D^+)$$

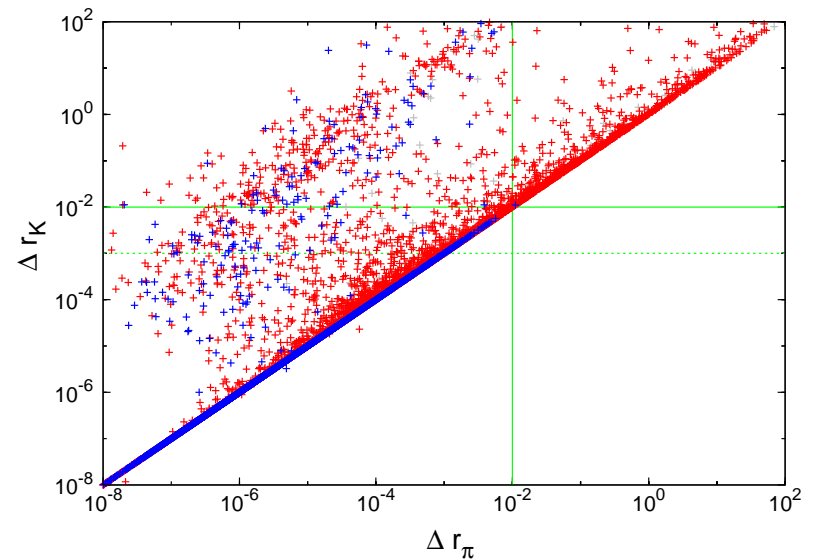
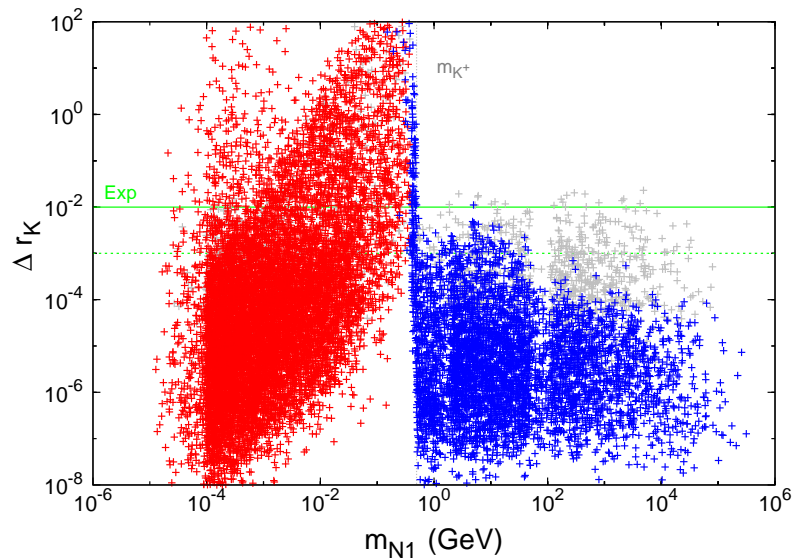
[Belle, BaBar, LHCb - NA62, ...]

[Atre et al, '09]

☞ Sterile fermions: violation of lepton flavour universality

Lepton Universality Violation in  $K$  and  $\pi$  decays: tree level effect

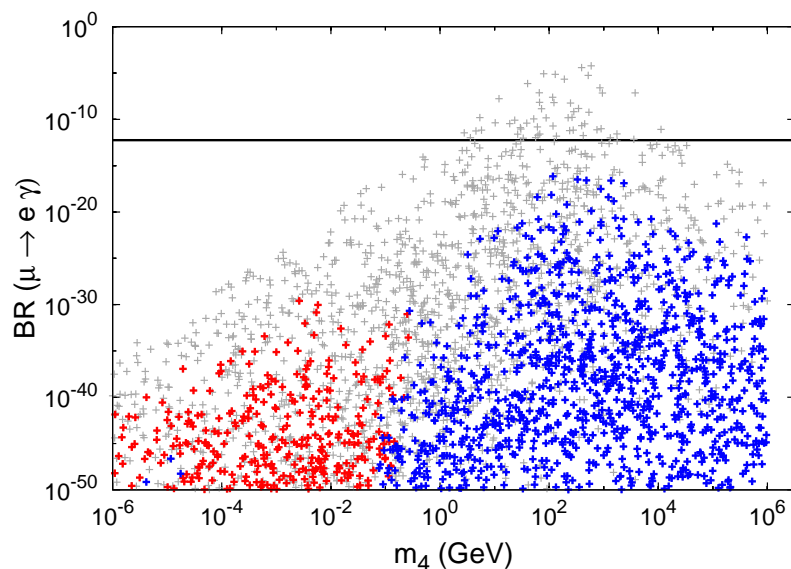
$$R_K = \frac{\Gamma(K \rightarrow e\nu)}{\Gamma(K \rightarrow \mu\nu)} \quad \text{comparison with SM th predictions} \quad \Delta r_K = \frac{R_K^{\text{exp}}}{R_K^{\text{SM}}} - 1$$



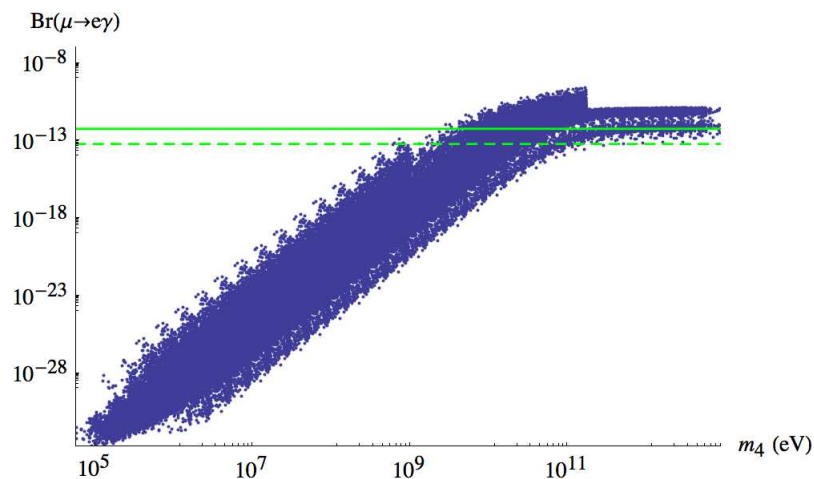
[“ISS (3,3)”: AA, Teixeira, Vicente and Weiland, '11-'13]

- ▶ Sterile neutrino contributions:  $\Delta r_{K,\pi} \gtrsim \mathcal{O}(10^{-2})$
- ▶  $\Delta r_{K,\pi} \sim \mathcal{O}(1) \Rightarrow$  one of the strongest constraints in SM +  $\nu_s$  models!

☞ Sterile fermions: cLFV in radiative decays  $l_i \rightarrow l_j \gamma$  and 3-body decays  $l_i \rightarrow 3l_j$



“3+1” toy model, [AA, De Romeri and Teixeira, '15]



“(2,2) ISS realisation” [AA and Lucente, '14]

► Consider  $\mu \rightarrow e \gamma$ :

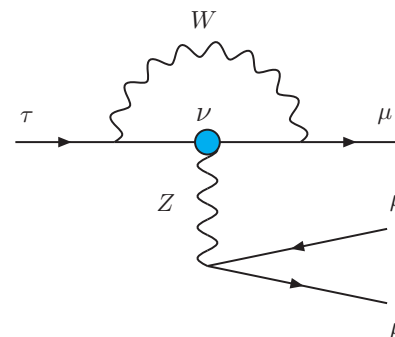
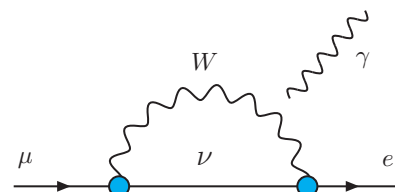
for  $m_s \gtrsim 10 - 100$  GeV sizeable  $\nu_s$  contributions

... but precluded by invisible  $Z$  width

And by other cLFV observables!

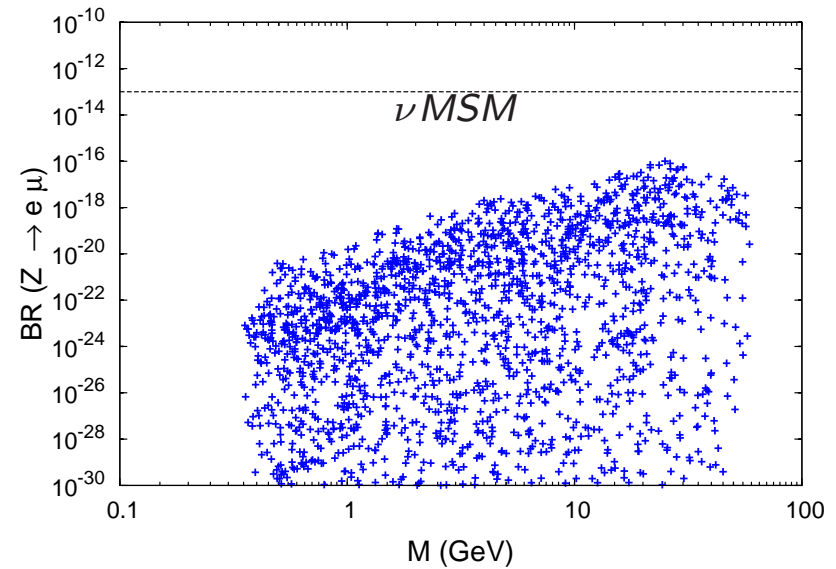
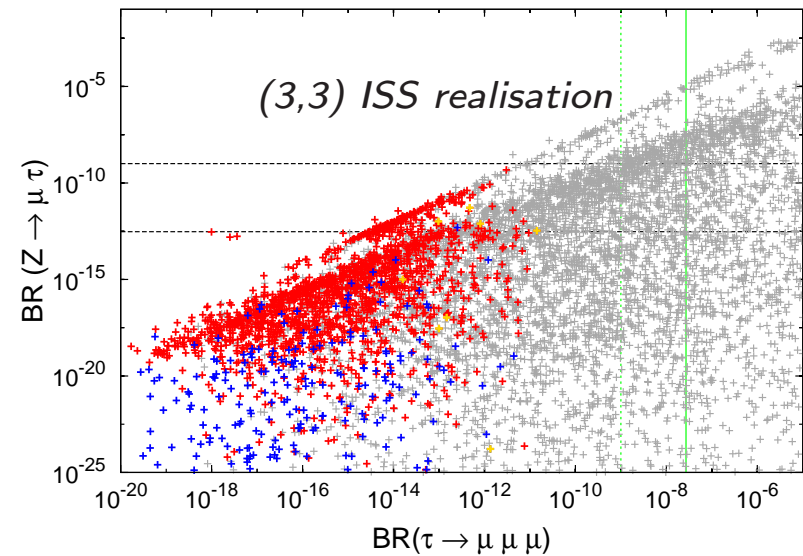
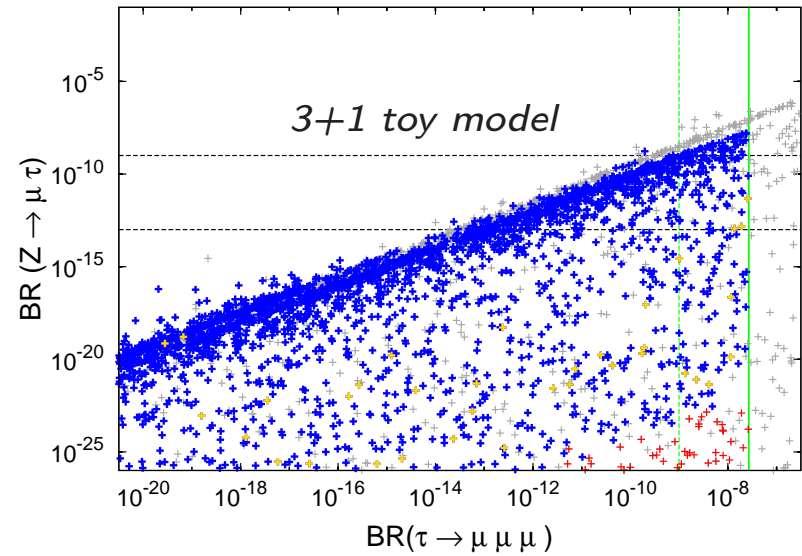
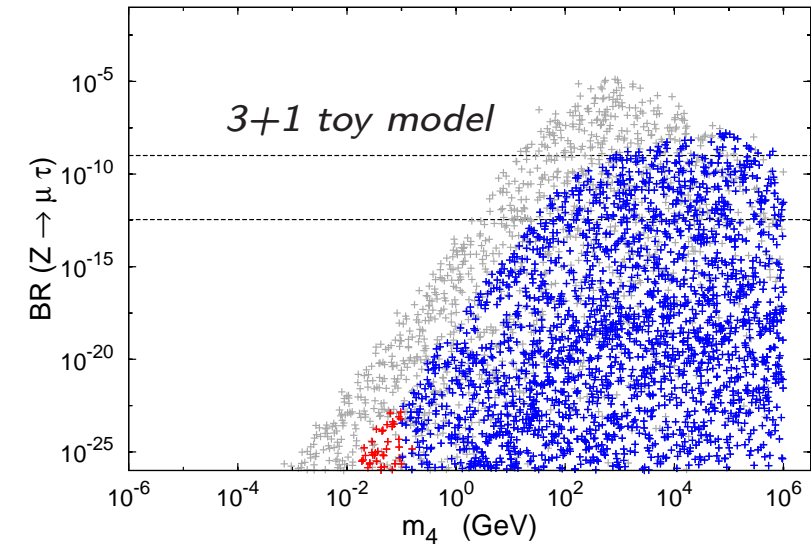
► Particularly constraining:  $\text{BR}(\mu \rightarrow 3e)$ ,  $\text{CR}(\mu - e, N)$

Dominated by  $Z$  penguin contributions for  $m_s \gtrsim M_Z$



# ☞ Sterile fermions: cLFV at high- and low-energies

[AA, De Romeri, Monteil, Orloff, Teixeira, '15]



► **Complementarity probes** of  $\nu_s$  cLFV at **low- and high energies!** (and in LNV...)

►  $Z \rightarrow \mu \tau$  at FCC-ee: allows to **probe  $\mu - \tau$  cLFV** beyond **SuperBelle reach**

[see also De Romeri et al, '16]

## ☞ Sterile fermions: cLFV in muonic atoms

- ▶ **Muonic atoms:** 1s bound state formed when  $\mu^-$  stopped in target

Interesting laboratory to study cLFV!  $\mu - e$  conversion

- ▶ **Muonic atom decay:**  $\mu^- e^- \rightarrow e^- e^-$

[Koike et al, '10]

Initial  $\mu^-$  and  $e^-$ : 1s state bound in Coulomb field of the **muonic atom's nucleus**

- ▶ **Experimental status:** New observable!

Hopefully included in Physics programmes of **COMET & Mu2e** (?)

- ▶ **Coulomb interaction** increases overlap between

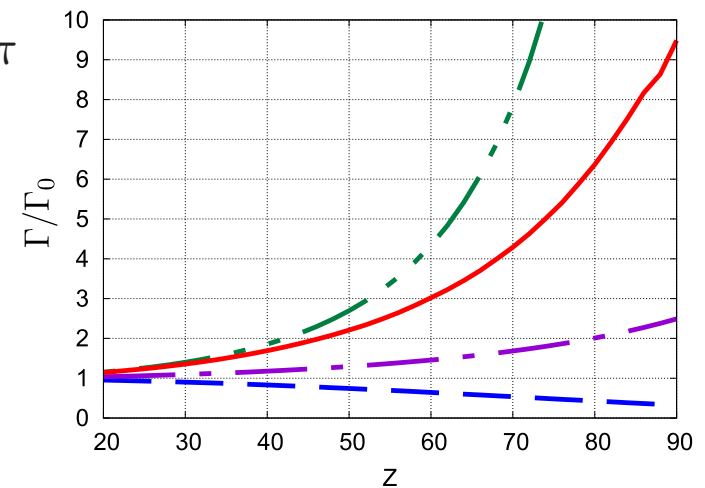
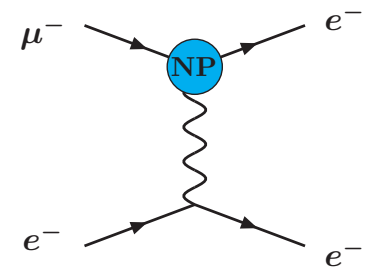
$\Psi_{\mu^-}$  and  $\Psi_{e^-}$  wave functions

$$\Gamma(\mu^- e^- \rightarrow e^- e^-, N) \propto \sigma_{\mu e \rightarrow ee} v_{\text{rel}} [(Z-1) \alpha m_e]^3 / \pi$$

- ▶ **Rate strongly enhanced** in large  $Z$  atoms

$$\Gamma/\Gamma_0 \gtrsim 10 \times (Z-1)^3 \quad [\text{Uesaka et al, '15-'16}]$$

Consider experimental setups for **Pb, U** !?

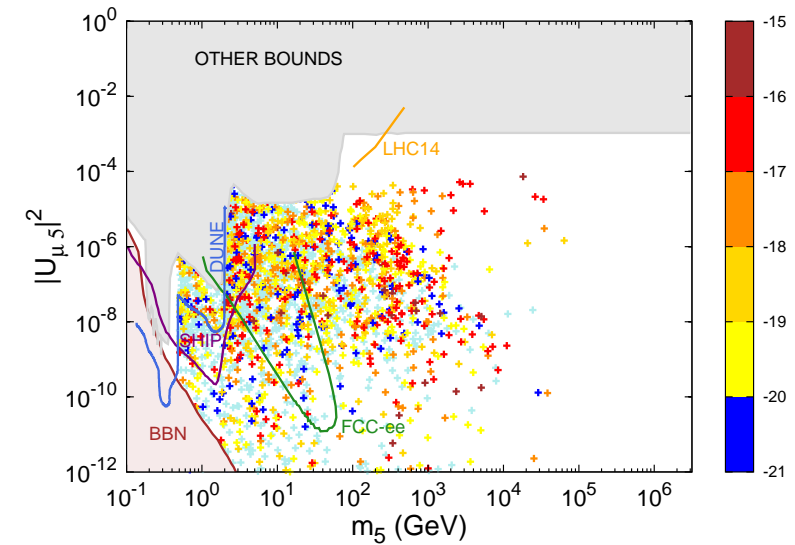
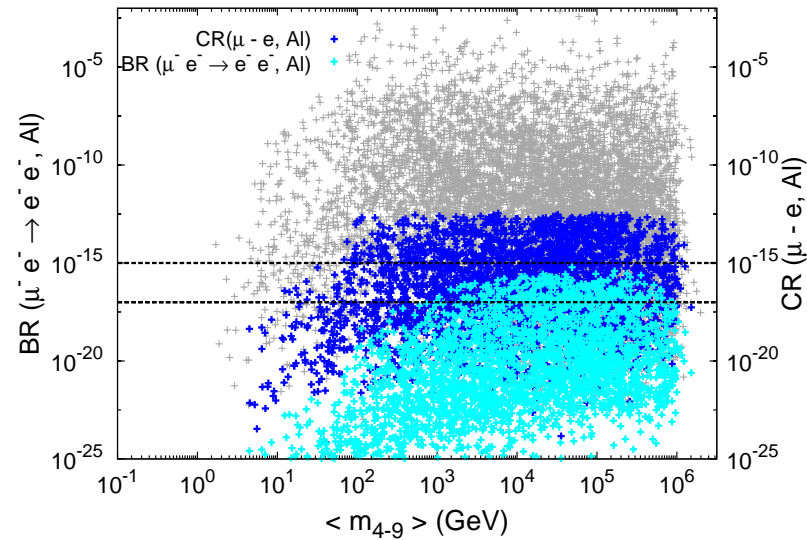
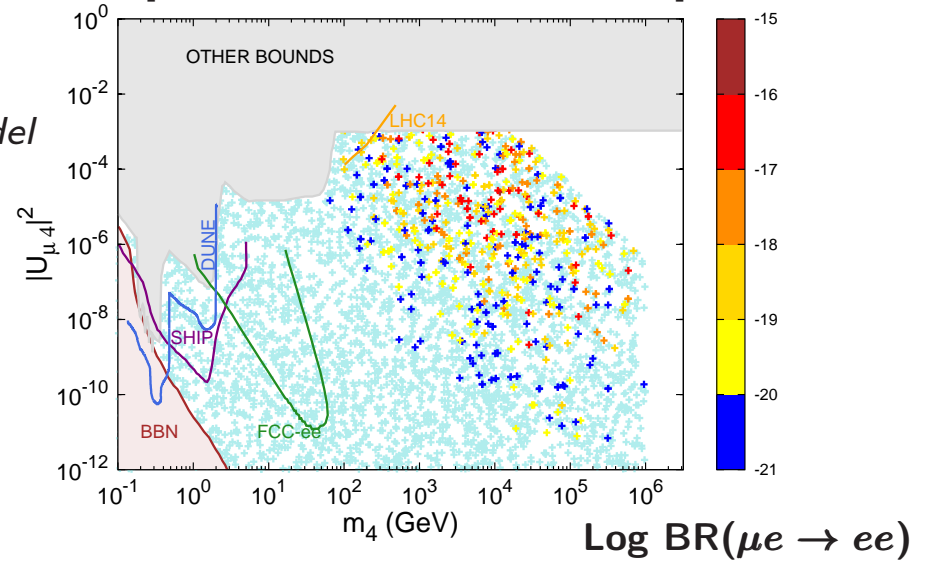
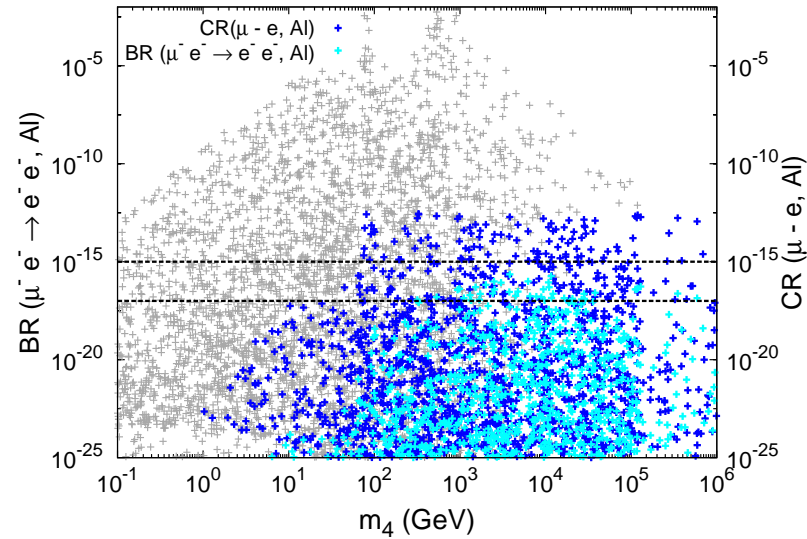


**☞ Sterile fermions: cLFV muonic atom decays**

[AA, De Romeri, Teixeira, '15]

*3+1 toy model*

*(3,3) ISS*



- ▶ Sizeable values for  $BR(\mu^- e^- \rightarrow e^- e^-)$  - potentially within experimental reach!
- ▶ For Aluminium,  $CR(\mu - e)$  appears to have stronger experimental potential .. consider “heavy” targets to probe  $BR(\mu^- e^- \rightarrow e^- e^-)$



## ☞ Sterile fermions: searches at the LHC and beyond

- ▶ Searches for  $\nu_s$  by ATLAS and CMS

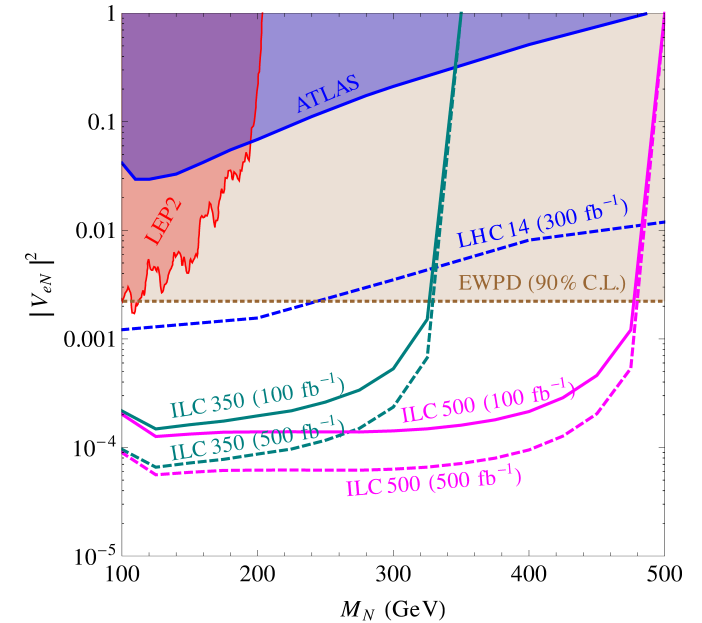
“smoking-gun” (LNV) channel:

$$pp \rightarrow W^* \rightarrow N \ell^\pm \rightarrow \ell^\pm + \ell^\pm + 2 \text{jets}$$

- ▶ Promising prospects for FCC-ee, ILC, CEPC...

[Banerjee et al, 1503.05491]

- ▶ Further searches carried for **LFV** final states and/or other exotic channels

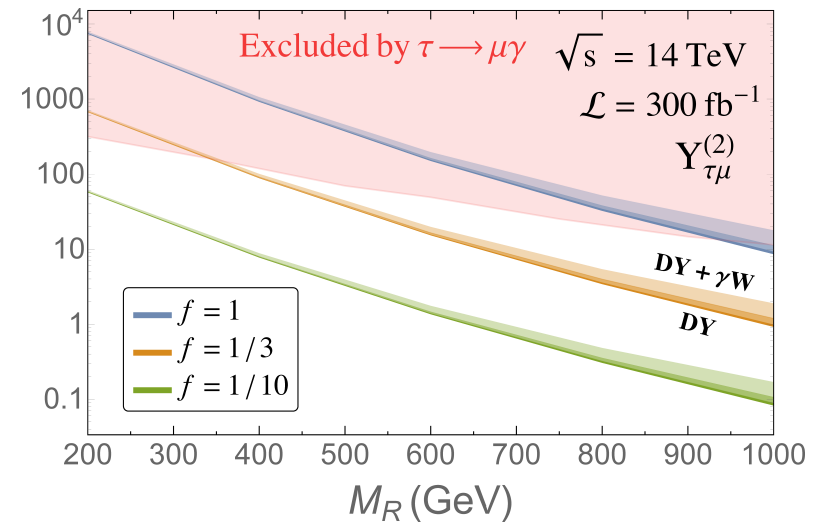


## ▶ cLFV exotic events at the LHC

- ▶ Searches for heavy  $N$  at the LHC

$$qq' \rightarrow \tau \mu + 2 \text{jets} \quad (\text{no missing } E^T!)$$

- ▶ After cuts, **significant number of events!**



## ▶ Resonant mono-Higgs production at FCC-ee

$$N \rightarrow H \nu \rightsquigarrow \text{sizeable deviations from SM mono-Higgs}$$

- ▶ Sensitive probe of  $\nu_s$  at high-energies!

[Antusch et al, '15]

[Arganda et al, 1508.05074]

## ☞ Sterile fermions: further appeal

- ▶ GeV sterile neutrinos → (testable) BAU from leptogenesis via oscillations

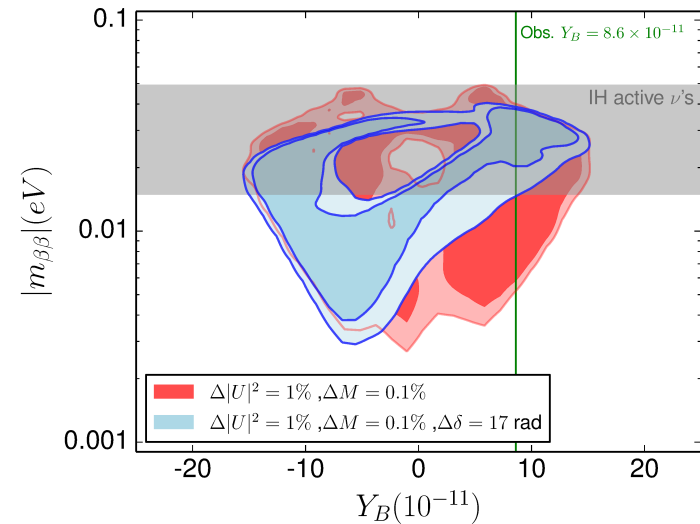
Synergy with (LNV) low-energy observables:

$0\nu 2\beta$  decays

Spectrum & mixings (SHiP),

determination of  $\delta_{CP}$  (DUNE, HyperK)

[Hernandez et al, '16]

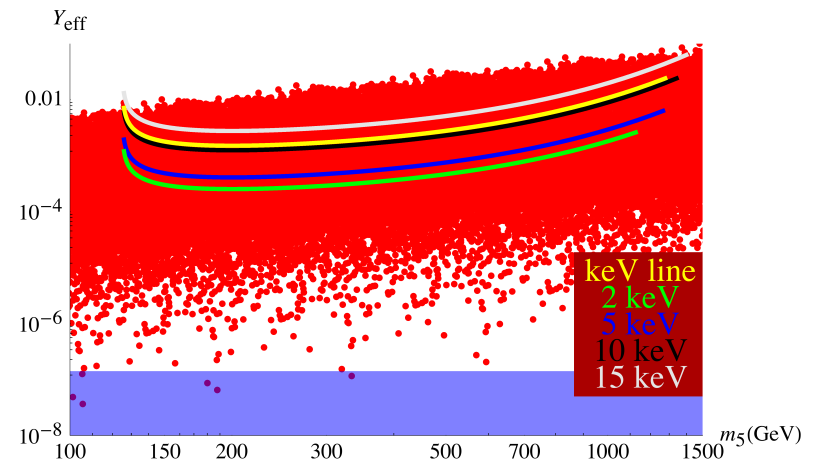


- ▶ Sterile neutrinos → viable warm dark matter candidates [for a review, see Drewes et al, '16]

⇒ impact on structure formation;

signal from  $\gamma$ -rays (3.5 keV line), ...

“(2,3) ISS” [AA, Arcadi and Lucente, '14]



## 👉 Conclusions

- ▶ **SM + Sterile fermions** constitute the “most minimal BSM” ...  
...**embedded** in several well motivated frameworks
- ▶ **Sterile neutrinos** contribute to a vast array of observables: CPV, LNV, LFUV, cLFV, ...  
... at high and low energy
- ▶ **Sterile neutrinos**: key rôle in cosmology as well
- ▶ **Sterile neutrinos** **testable at the three frontiers**: high intensity, high energy and cosmology  
and in LNV neutrinoless double beta decays

Could the NP be "SM + sterile fermions"?

**Additional observables**

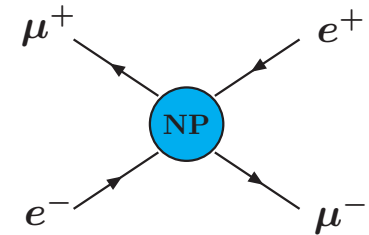
# cLFV in “muonic” atoms: Muonium

► **Muonium:** hydrogen-like **Coulomb bound state** ( $e^- \mu^+$ ); free of hadronic interactions!

► **Mu –  $\overline{\text{Mu}}$  conversion**

Spontaneous conversion of a ( $e^- \mu^+$ ) into ( $e^+ \mu^-$ )

Reflects a **double lepton number violation**:  $\Delta L_e = \Delta L_\mu = 2$



► **Experimental status:**  $P(\text{Mu} - \overline{\text{Mu}}) < 8.3 \times 10^{-11}$  [Willmann et al, 1999]

$$\mathcal{L}_{\text{eff}}^{\text{Mu} - \overline{\text{Mu}}} \sim G_{\text{MM}} [\bar{\mu} \gamma^\alpha (1 - \gamma_5) e] [\bar{e} \gamma_\alpha (1 - \gamma_5) \mu] \iff |\text{Re}(G_{\text{MM}})| < 0.003 \times G_F$$

Future prospects at **FNAL** ?

► **cLFV Mu decay:**  $\text{Mu} \rightarrow e^+ e^-$

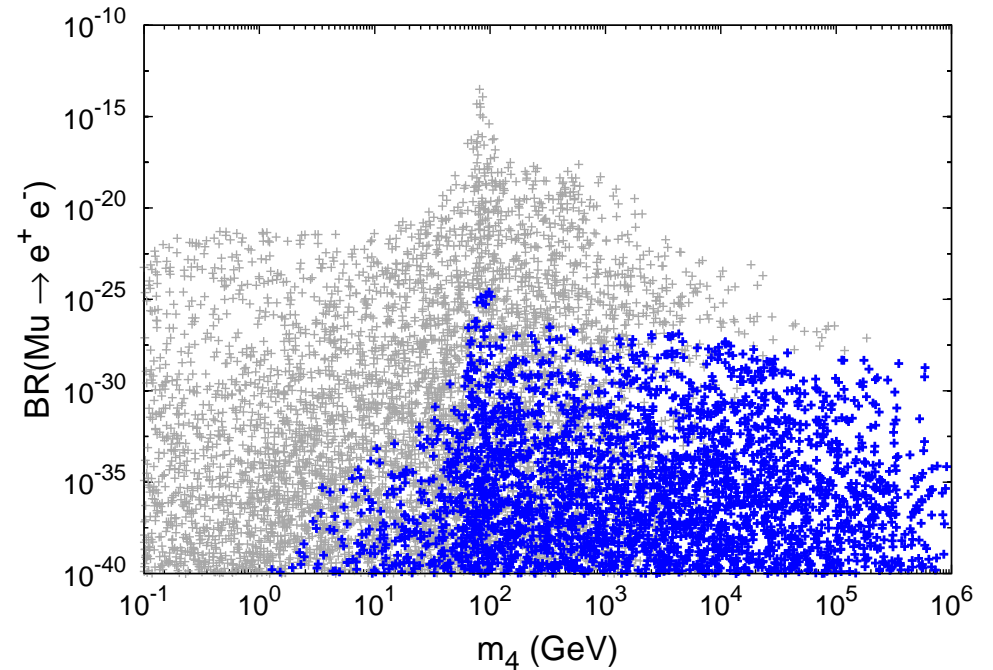
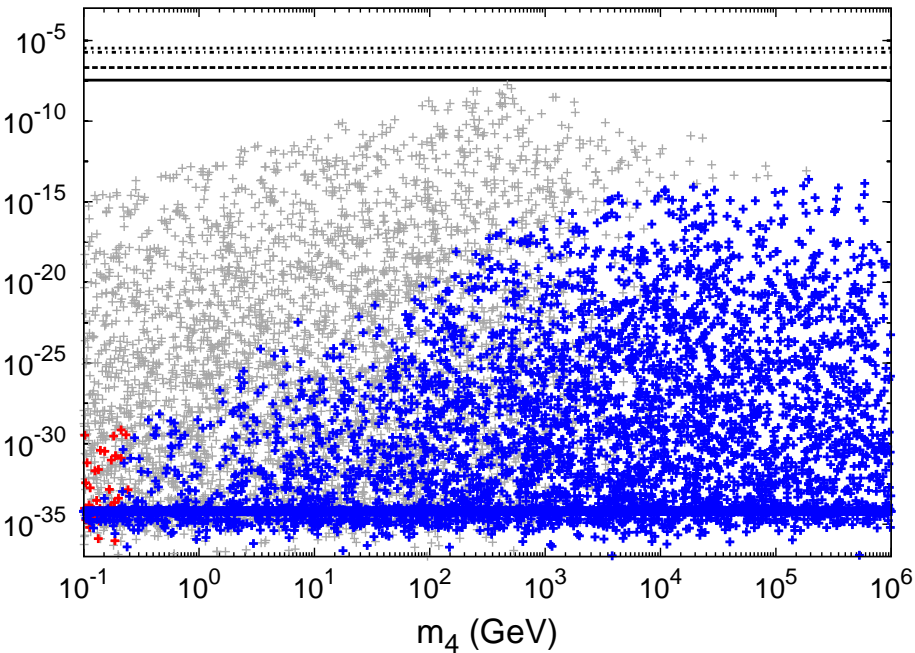
clear signal compared to SM decay  $\text{Mu} \rightarrow e^+ e^- \bar{\nu}_\mu \nu_e$  (no missing energy)

► **Experimental status:** no clear roadmap (nor bounds)...

Hopefully included in Physics programme of **COMET** & **Mu2e** (?)

# Muonium and sterile neutrinos

- ▶ cLFV Muonium processes:  $\text{Mu} - \overline{\text{Mu}}$  oscillation and  $\text{Mu} \rightarrow e^+e^-$  decay

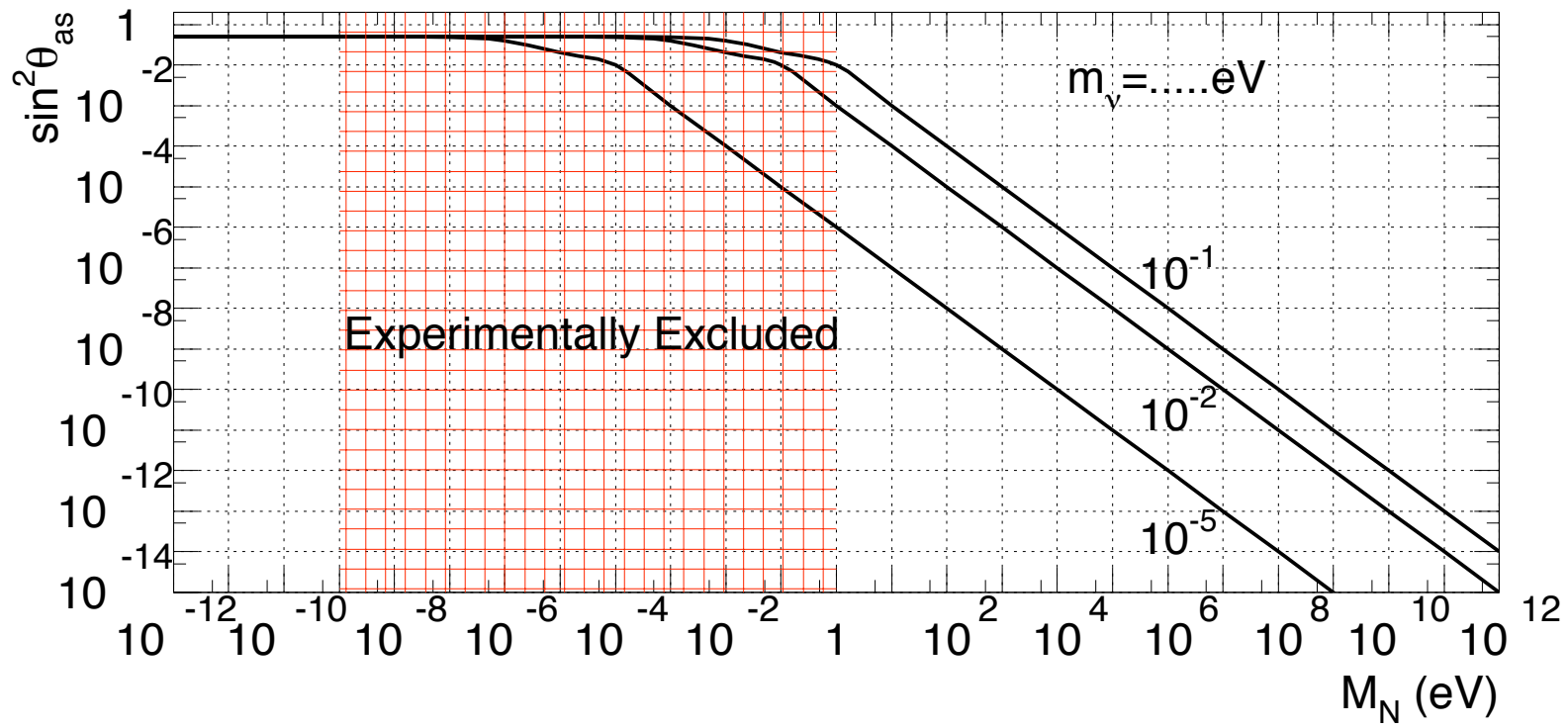


*"3+1" toy model [AA, De Romeri and Teixeira, '15]*

- ▶ Large values of  $G_{\text{MM}}$  precluded due to conflict with  $\text{CR}(\mu - e, \text{Au})$  and  $\text{BR}(\mu \rightarrow 3e)$

Within reach of **next generation of experiments?** (e.g. FNAL)

- ▶ Maximally expected values  $\text{Mu} \rightarrow e^+e^- \sim \mathcal{O}(10^{-25})$  Within experimental reach ?



[de Gouvea et al, '09]