

# Top mass effects at NLO

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# Recap & Motivation

- Lot of progress in HEFT approach since first NLO calculation [Dawson, Dittmaier, Spira '98]:
  - NNLO [de Florian, Mazzitelli '13, Grigo, Melnikov, Steinhauser '14]
  - NLO+NNLL [Shao, Li, Li, Wang '13],
  - NNLO+NNLL [de Florian, Mazzitelli '15],  
remaining scale uncertainty 5-6%
- Mass effects beyond LO only partially understood:
  - in NLO real radiation [Maltoni, Vryonidou, Zaro '14]: -10%
  - from  $1/m_t^2$  expansion [Grigo, Hoff, Steinhauser '15]:  
+/-10% at NLO, +/- 5% at NNLO
- PDF +  $\alpha_s$  uncertainties (PDF4LHC15): 3-4% [Javier's talk in Nov.]
- Largest uncertainty from missing mass effects,  
👉 full NLO calculation needed

## Effects from NLO real radiation

- $gg \rightarrow HHg$  and  $qg \rightarrow HHq$  one-loop matrix elements from **GoSam** [Greiner, Heinrich, Jahn, Luisoni, Mastrolia, Ossola, Peraro, Schlenk, von Soden-Fraunhofen, Tramontano]
- Dipole subtraction [Catani, Seymour '97]
- Phase-space integration using parton-level Monte-Carlo
- Checks:
  - $gg \rightarrow Hg$  etc. reproduced and compared to **Sushi** [Harlander, Liebler, Mantler '13]
  - Independence of dipole-cut  $\alpha$  parameter [Nagy '03]
  - Compare with **MG5\_aMC@NLO** result [Maltoni, Vryonidou, Zaro '14]  later in this talk

# Effects from virtual two-loop amplitude

- Generate diagrams with `qgraf` [Nogueira '93] 
- Generate amplitude within extended GoSam framework using `form` [Vermaseren] 
- (Partial) reduction to master integrals with `Reduze` [von Manteuffel, Studerus] 
- Checks:
  - Amplitude generated in second framework 
  - $gg \rightarrow H$  reproduced and compared to `Sushi` 
- Numerical evaluation of (master) integrals with `SecDec` [Borowka, Heinrich, Jahn, Jones, Kerner, Schlenk, TZ]  
 needs more time + validation 

**meanwhile...**

# Approximate top-mass effects at NLO

$$\begin{aligned} \sigma^{NLO}(p) = & \int d\phi_3 \left[ (d\sigma^R(p))_{\epsilon=0} - \left( \sum_{\text{dipoles}} d\sigma^{LO}(p) \otimes dV_{\text{dipole}} \right)_{\epsilon=0} \right] \checkmark \\ & + \int d\phi_2 [d\sigma^V(p) + d\sigma^{LO}(p) \otimes \mathbf{I}]_{\epsilon=0} \\ & + \int_0^1 dx \int d\phi_2 [d\sigma^{LO}(xp) \otimes (\mathbf{P} + \mathbf{K})(x)]_{\epsilon=0} \checkmark \end{aligned}$$

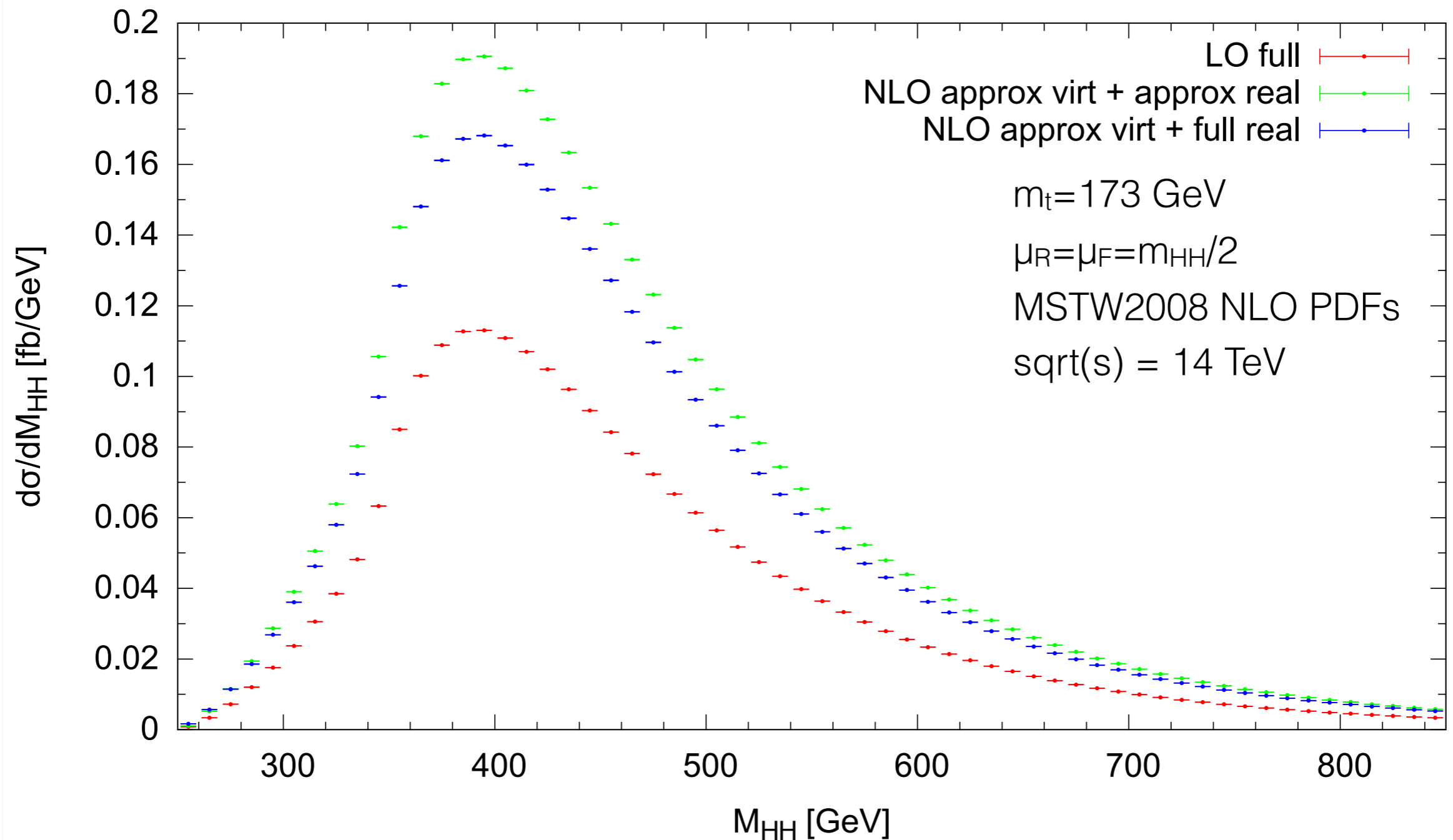
$$\begin{aligned} d\sigma^V + d\sigma^{LO}(\epsilon) \otimes \mathbf{I} & \approx d\sigma_{\text{exp},N}^V \frac{d\sigma^{LO}(\epsilon)}{d\sigma_{\text{exp},N}^{LO}(\epsilon)} + d\sigma^{LO}(\epsilon) \otimes \mathbf{I} \\ & = (d\sigma_{\text{exp},N}^V + d\sigma_{\text{exp},N}^{LO}(\epsilon) \otimes \mathbf{I}) \frac{d\sigma^{LO}(\epsilon)}{d\sigma_{\text{exp},N}^{LO}(\epsilon)} \\ & = (d\sigma_{\text{exp},N}^V + d\sigma_{\text{exp},N}^{LO}(\epsilon) \otimes \mathbf{I}) \frac{d\sigma^{LO}(\epsilon=0)}{d\sigma_{\text{exp},N}^{LO}(\epsilon=0)} + \mathcal{O}(\epsilon) \end{aligned}$$

$$d\sigma_{\text{exp},N} = \sum_{k=0}^N d\sigma^{(k)} \left( \frac{\Lambda}{m_t} \right)^{2k}$$

$$\Lambda \in \{ \sqrt{s}, \sqrt{t}, \sqrt{u}, m_h \}$$

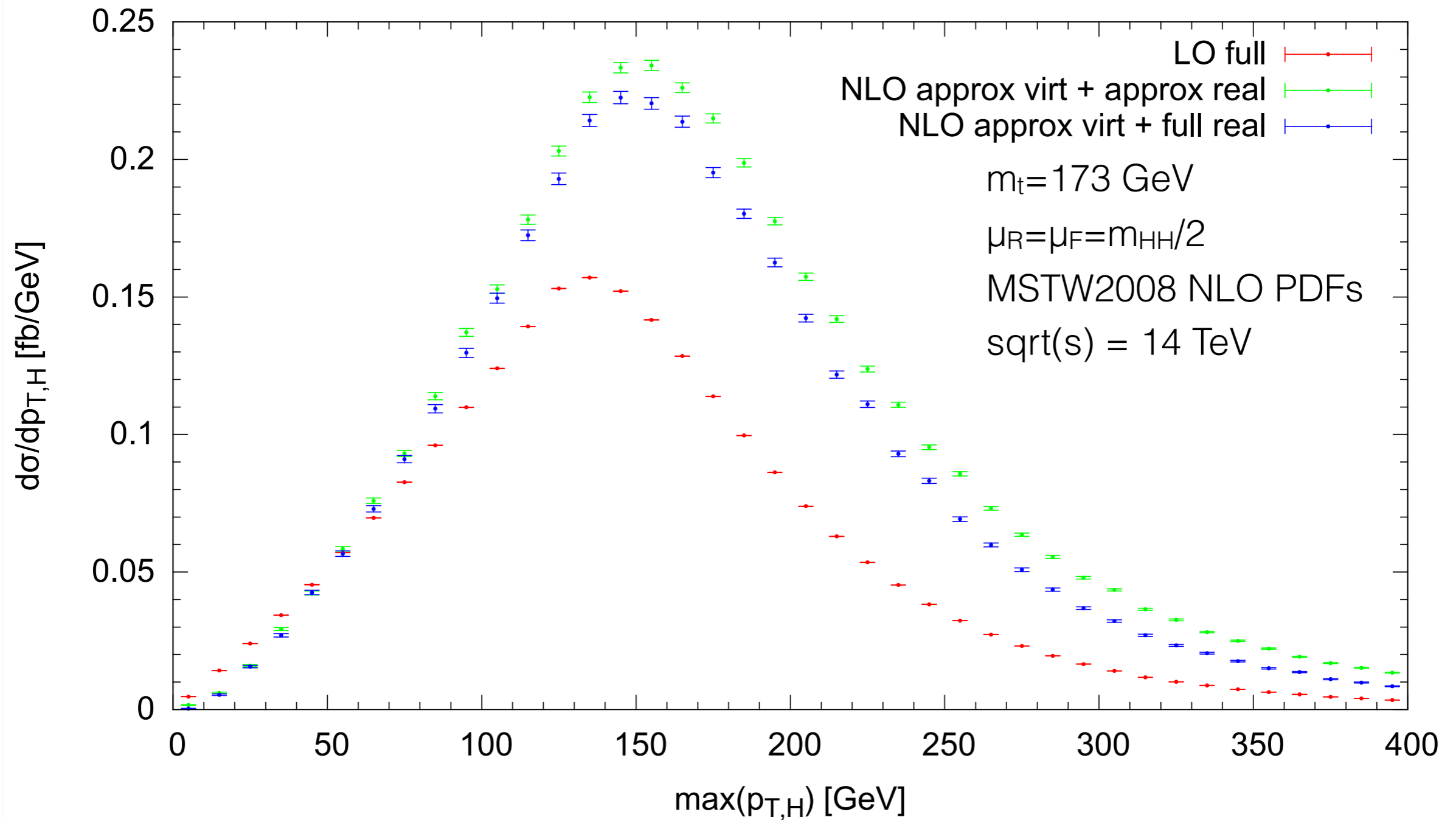
- full real-emission matrix elements and dipoles
- virtual corrections as asymptotic expansion in  $1/m_t^2$  with **q2e/exp** [Harlander, Seidensticker, Seidensticker] + **Reduze** [von Manteuffel, Studerus] + **matad** [Steinhauser]
- not directly comparable with [Grigo, Hoff, Steinhauser], (real radiation treated differently, expansion parameter  $(m_H/m_t)^2$ )

# Mass effects in $M_{HH}$ distribution (I)

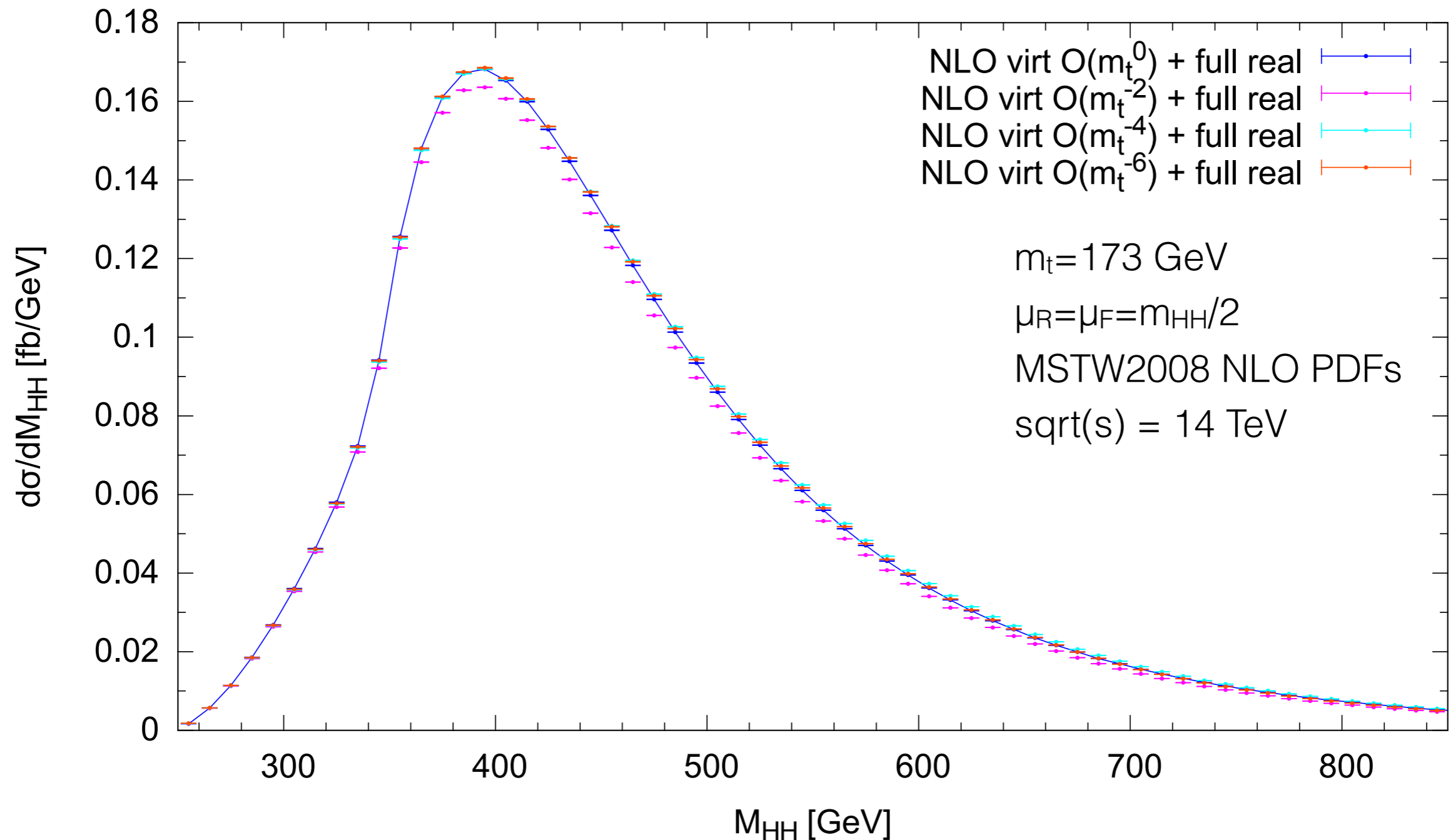


- „approx“  $\hat{=}$  rescaled expansion with  $N=0$
- Known negative mass effects from real radiation

# Mass effects in $p_T$ distribution (I)



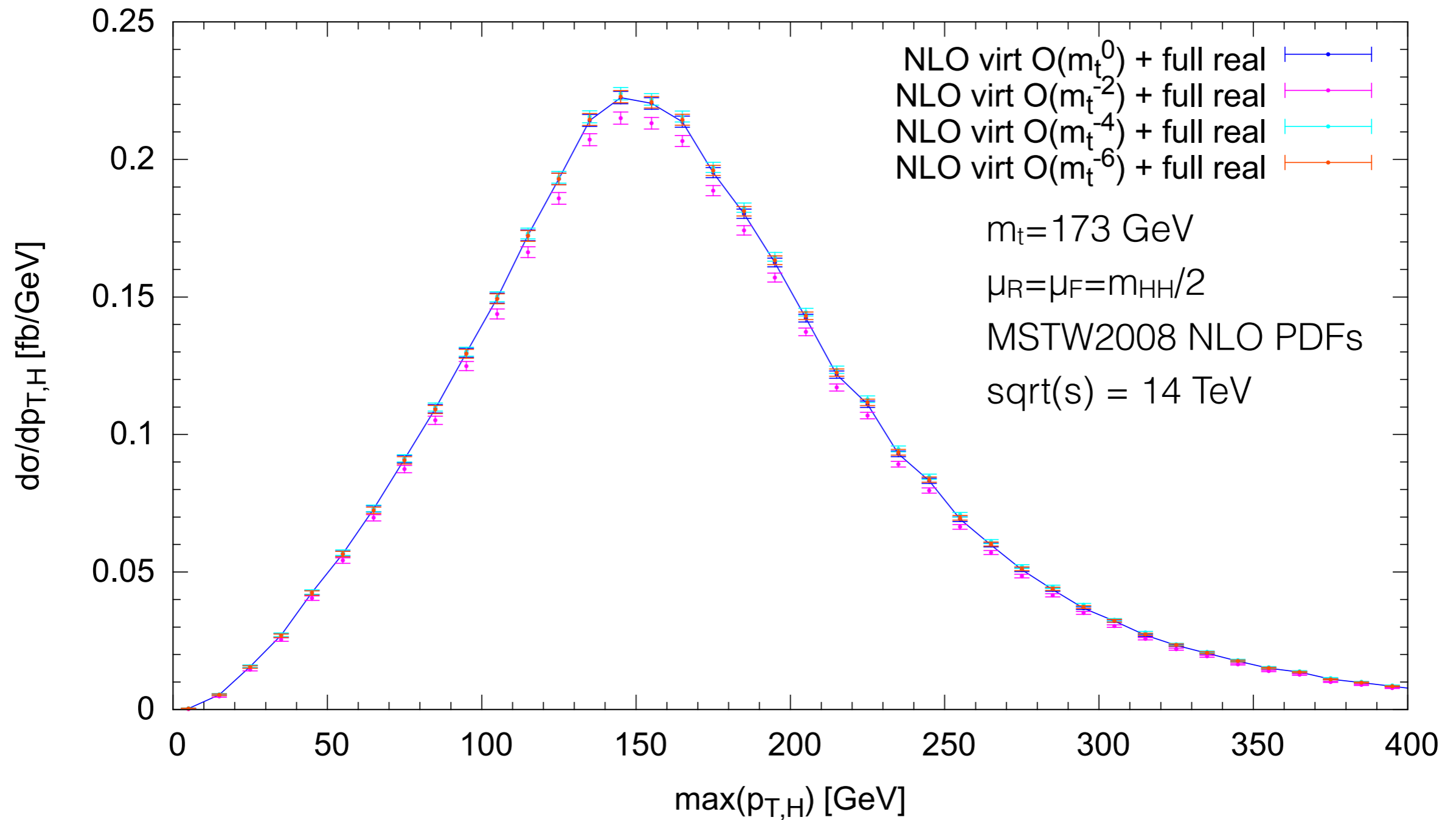
# Mass effects in $M_{HH}$ distribution (II)



- Slight tendency that -10% effect persists, **but:** spoiled cancellations? threshold effects?



# Mass effects in $p_T$ distribution (II)



# Preliminary results for cross-check

- full real-emission matrix elements
- virtual corrections in HEFT ( $\hat{=}$  expansion with  $N=0$ )
- $m_t=172.5$  GeV,  $\mu_0=m_{HH}$ ,  $\mu_R=\mu_F \in [\mu_0/2, 2\mu_0]$
- PDF4LHC15\_nlo\_30\_pdfas PDFs with (without)  $\alpha_s$  variation

	$gg \rightarrow HH$ total cross section [fb]			
	$m_H = 124.5$ GeV	$m_H = 125.0$ GeV	$m_H = 125.09$ GeV	$m_H = 125.5$ GeV
$\sqrt{s} = 7$ TeV	5.047	$5.011^{+19\%}_{-16\%} \pm 4.5\% (\pm 4.2\%)$	5.004	4.975
$\sqrt{s} = 8$ TeV	7.343	$7.292^{+18\%}_{-15\%} \pm 4.2\% (\pm 3.8\%)$	7.283	7.241
$\sqrt{s} = 13$ TeV	25.13	$24.97^{+15\%}_{-14\%} \pm 3.2\% (\pm 2.8\%)$	24.94	24.80
$\sqrt{s} = 14$ TeV	29.85	$29.66^{+18\%}_{-15\%} \pm 3.1\% (\pm 2.6\%)$	29.62	29.47

- compare to MG5\_aMC@NLO results (for  $m_H = 125$  GeV):

	$\sqrt{s} = 8$ TeV NLO	$\sqrt{s} = 13$ TeV NLO
$HH$ (NLO_approx)	$7.28^{+18\%}_{-15\%} \pm 0.7\%$	$24.9^{+15\%}_{-13\%} \pm 0.5\%$

(borrowed from Eleni's talk on Nov. 19)

# Conclusions

- Reproduced -10% mass effects from NLO real radiation
- Setup for full NLO calculation ready
- Results with full top-mass dependence within close reach