AdS/CFT applied to condensed matter theory

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AdS/CFT - the best thing since sliced bread?

- Bekenstein-Hawking entropy of black holes (1973):

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- Applications to thermalization, quantum information, condensed matter theory

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- We can compute susceptiblity, heat capacity, conductivity etc.