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Reviews of Higher Order Modes Effects in LCLS-II Superconducting Linac

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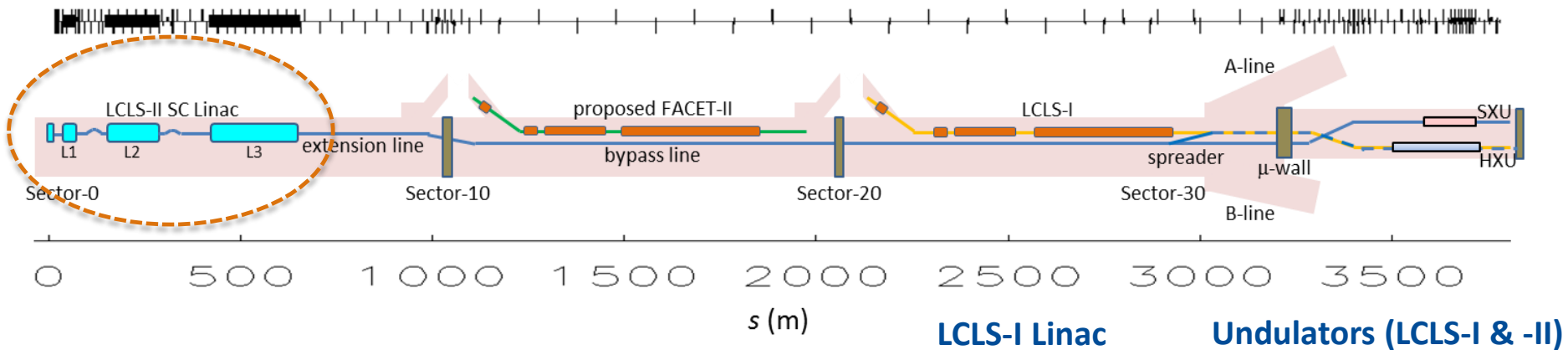
Motivation

- Operation of SC linac in CW regime put stringent tolerances on cryogenic load. Additional heat deposited by HOMs in operating environment of 2K may lead to:
 - Increase in operating cost of the machine.
- Generation of high-brightness x-rays requires preservation of beam quality along the linac.
 - Monopole HOMs may result in a energy spread among bunches as well as within particles in the bunch.
 - Transverse cumulative effects due to transverse HOMs may result in transverse emittance dilution and in worst case beam break-up.
- High peak current and bunches as short as $25\text{ }\mu\text{m}$ results in excitation of broad spectrum($\omega \approx \frac{c}{\sigma}$) of HOMs that extends up to terahertz range.
 - Breaking of cooper-pairs that may lead to transition of superconducting state into normal conducting states.
 - Understanding of wake power distribution in the cryogenic environment
 - Implication of transition effects originating due to change in bunch pattern.

Scope of Work

- Wake power loss in LCLS-II SC linac
- Understanding of power distribution of broad-range propagating HOMs.
 - Diffusion Model.
 - Wake decomposition model
- Consequences of additional HOMs power deposition on the surface of superconducting cavity
 - Cooper pair breaking due to Tera-Hertz propagating HOMs
- Possibility of HOMs trapping and resonance excitation:
 - Monopole modes
 - Additional heating at operating temperature of 2K
 - Dipole modes
 - Transverse emittance dilution due to cumulative effects
- Implication of transition effects :
 - Longitudinal
 - Transverse

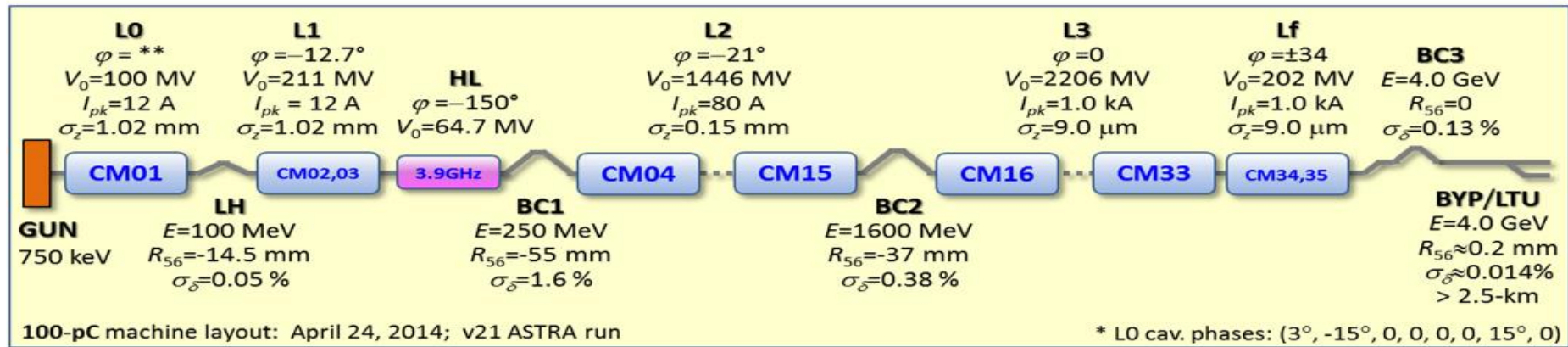
Linac Coherent Light Source-II



- The Linac Coherent Light Source –II (LCLS-II) is a proposed fourth generation x-ray light source facility under construction at SLAC.
- It is based on a new superconducting radio frequency linac that will operate in continuous wave (CW) mode and will deliver a 4GeV electron beam.
- The SCRF linac will employ XFEL/ILC technology and will use 1.3 GHz 9-cell SCRF cavity for beam acceleration.

LCLS-II SCRF Linac Architecture

PRD: LCLSII-2.4-PR-0041



- On the basis of RF parameters and intermediate warm regions, LCLS-II SCRF Linac is mainly segmented into several sections.
- All sections except HL are composed of 9-cell 1.3 GHz accelerating cavity. One cryomodule comprise eight cavities.
- HL section is employed to compensate non-linearity in longitudinal phase space and composed of 3.9 GHz 9-cell cavity.

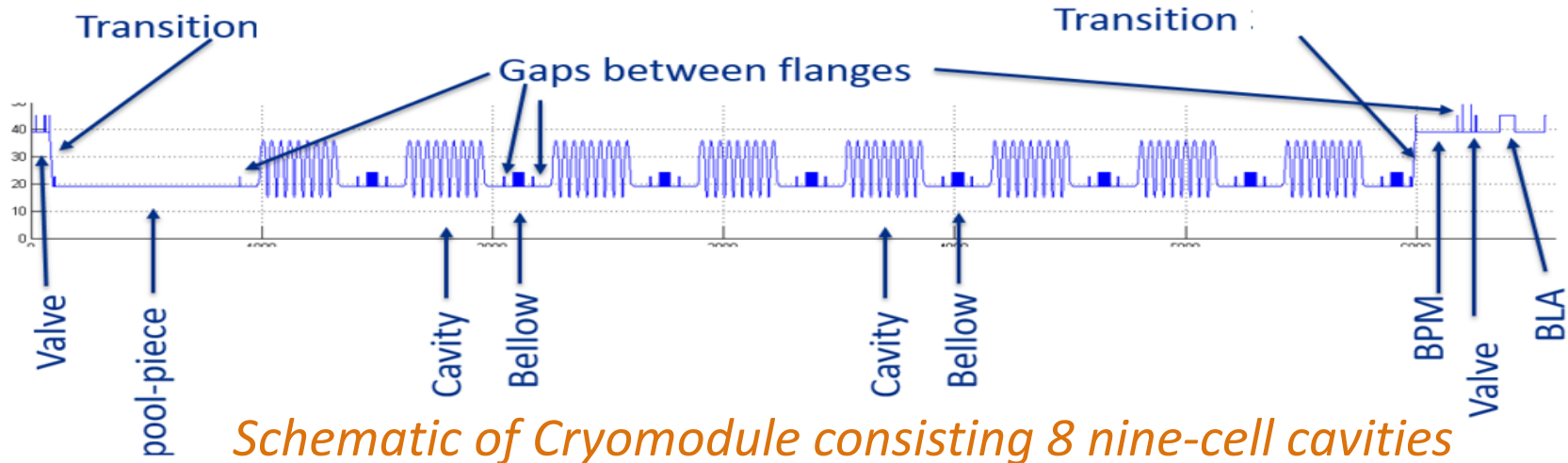
Section	V_0 (MV)	Φ (deg)	Acc.Grad (MV/m)	CMs
L0	100	~ 0	16.3	1
L1	211	-12.7	13.6	2
HL	-64.7	-150	12.5	2
L2	1446	-21.0	15.5	12
L3	2206	0	15.7	18
Lf	202	+/- 34	15.7	2

LCLS-II Linac Baseline Parameters

LCLSII-1.1-PR-0133, LCLS-II Parameters

Parameter	symbol	nominal	range	units
Electron Energy	E_f	4.0	2.0 - 4.14	GeV
Bunch Charge	Q_b	100	10 - 300	pC
Bunch Repetition Rate in Linac	f_b	0.62	0 - 0.93	MHz
Average e^- current in linac	I_{avg}	0.062	0.0 - 0.3	mA
Avg. e^- beam power at linac end	P_{av}	0.25	0 - 1.2	MW
Norm. rms slice emittance at undulator	$\gamma\epsilon_{\perp-s}$	0.45	0.2 - 0.7	μm
Final peak current (at undulator)	I_{pk}	1000	500 - 1500	A
Final slice E-spread (rms, w/heater)	σ_{Es}	500	125 - 1500	keV
RF frequency	f_{RF}	1.3	-	GHz
Avg. CW RF gradient (powered cavities)	E_{acc}	16	-	MV/m
Avg. Cavity Q0	$Q0$	2.7e10	1.5 - 5e10	-
Photon energy range of SXR (SCRF)	E_{phot}	-	0.2 - 1.3	keV
Photon energy range of HXR (SCRF)	E_{phot}	-	1 - 5	keV
Photon energy range of HXR (Cu-RF)	E_{phot}	-	1 - 25	keV

HOMs power generated in LCLS-II Linac



- A cryomodule (CM) in the LCLS-II linac is composed of eight 9-cell SC cavities and quadrupole magnet. A beam line absorber (BLA) is also placed b/w two cryomodules.
- When beam traverses through a CM in linac, its wake energy is radiated into modes that are much above cut-off frequency. They are named as un-trapped radiation.
- Primary source of excitation of un-trapped radiation in the LCLS-II SC linac is irises of 9-cell cavities. Interconnecting bellows and beam pipe transitions also contributes in this process.
- HOM power generated by beam is: $P = Q_b^2 f_{rep} k_{loss}$
- *In LCLS-II, maximum HOMs power is generated for the case $Q_b = 300\text{pC}$ and $f_{rep} = 1\text{MHz}$.*

Steady State Wake Losses

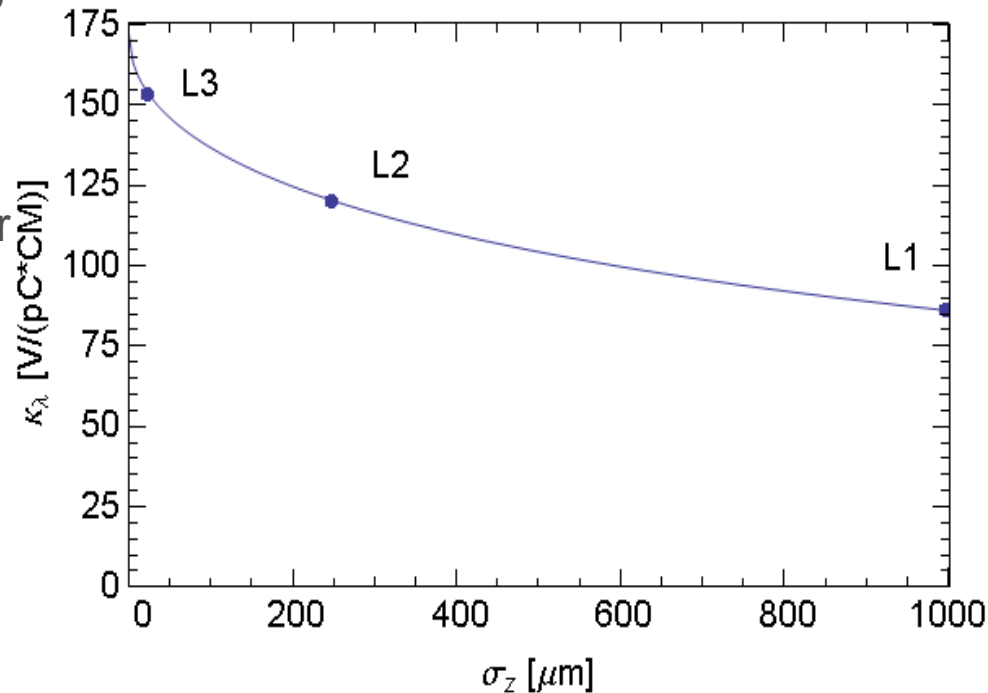
LCLS-II TN-13-04: K. Bane et al

- Loss factor (k_{loss}) is estimated for L1, L2 and L3 sections using :

$$k_{loss} = \frac{1}{2\sigma_z\sqrt{\pi}} \int_0^{\infty} w_{||}^0(s) e^{-(s/\sigma_z)^2/4} ds; \quad w_{||}^0(s) = 344 e^{-\sqrt{s/s_0}};$$

where $s_0 = 1.74$ mm. Longitudinal bunch distribution is considered Gaussian.

- For RMS bunch length of 1 mm, 0.25 mm, and 0.25 μm in L1, L2 and L3, loss factor is 86, 119 and 154 V/pC per cryomodule respectively. Loss factor in HL section is 151.6 V/pC per cryomodule.
- HOM power generated for $Q_b = 300\text{pC}$ and $f_{rep} = 1\text{MHz}$ is 7.7, 10.7 and 13.8 W/CM in L1, L2 and L3 respectively.
- HOM power generated in HL section is 13.6 W/CM.



- In this presentation we address worst cases i.e. L3 section and HL section.

HOM power spectrum(1)

- In order to understand distribution of power among the modes, HOM power spectrum calculated.

$$\frac{dP}{d\omega} = Q_b^2 f_{rep} Z_{\parallel}(\omega) e^{-\left(\frac{\omega\sigma_z}{c}\right)^2}; \quad Z_{\parallel} \text{ is longitudinal wake impedance}$$

$$Z_{\parallel} = \frac{1}{\pi c} \operatorname{Re} \left(\int_0^{\infty} w_{\parallel}^0(s) e^{-\frac{i\omega s}{c}} ds \right); \quad w_{\parallel}^0 \text{ is longitudinal wake function of a point like charge.}$$

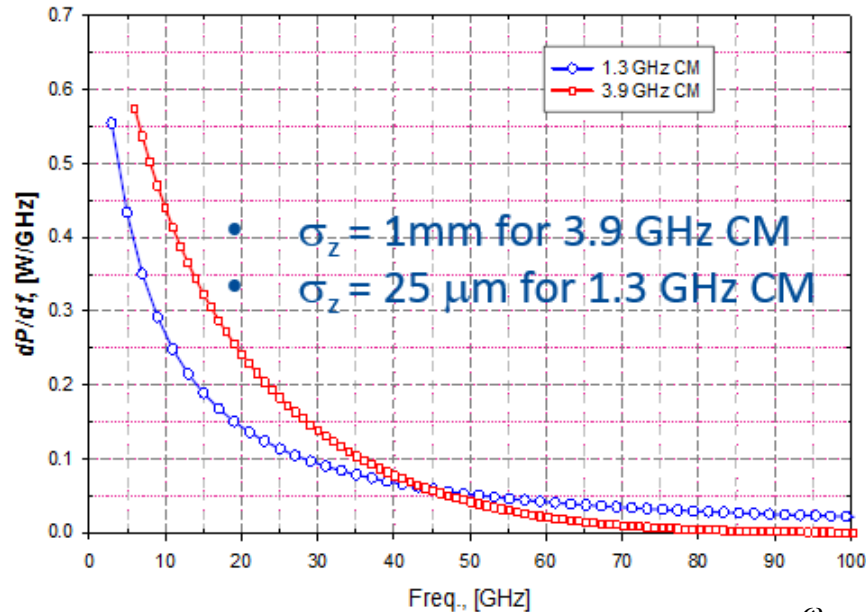
- Wake potential is given as: $W_{\parallel}^0(s) = \frac{1}{Q_b} \int_{-\infty}^s w_{\parallel}^0(s-s') q(s') ds'; \quad q(s) = \frac{1}{\sigma_z \sqrt{2\pi}} e^{-\frac{s^2}{2\sigma_z^2}};$
- Analytically estimated wake potential is fitted to wake potential computed numerically (ECHO) by adjusting wake function.
- Wake function for 1.3 GHz CM : $w_{\parallel}^0(s) = 344 e^{-\sqrt{\frac{s}{s_0}}}; \quad s_0 = 1.73 \text{ mm}$
- Wake function for 3.9 GHz CM :

$$w_{\parallel}^0(s) = -H(s) \left(A e^{-\sqrt{\frac{s}{s_0}}} + 0.9 \frac{\cos(5830 s^{0.83})}{\sqrt{s} + 195s} + B \delta(s) \right); \quad s_0 = 8.4 * 10^{-4}, A = 784, B = 1098$$

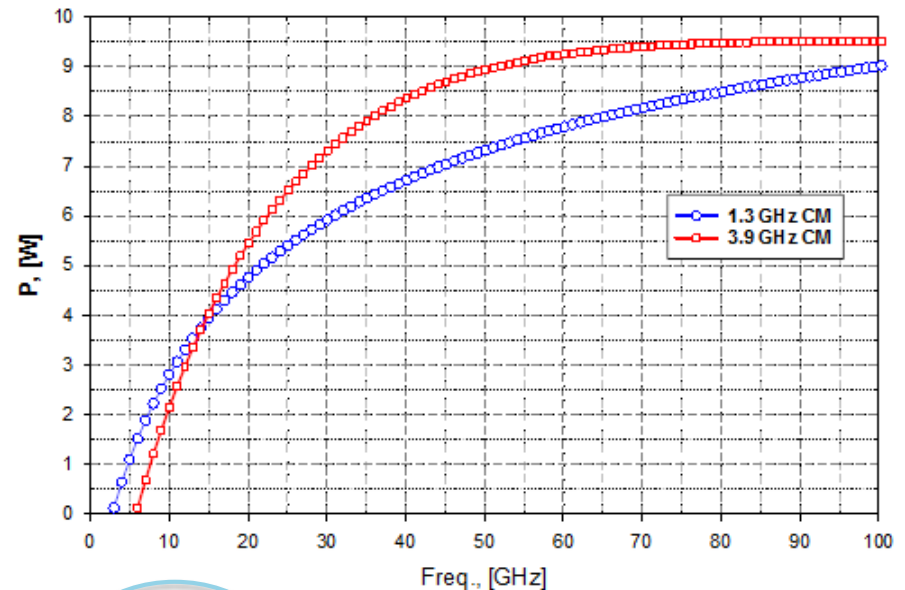
* I. Zagorodnov, T. Weiland, "Wake Fields Generated by the LOLA-IV Structure and the 3rd Harmonic Section in TTF-II", TESLA Report 2004-1

HOMs power spectrum(2)

Differential Power



Integrated Power



$$P_{total} = \int_0^{\omega_c} \frac{dP}{d\omega} d\omega + \int_{\omega_c}^{\omega} \frac{dP}{d\omega} d\omega$$

Propagating/un-trapped HOM power

- HOMs power comprised in propagating/un-trapped modes is 12.8 W/CM and 9.5 W/CM for 1.3 GHz cryomodule in L3 section and 3.9 GHz cryomodule respectively.
- In order to estimate total cryogenic heat load, a good understanding of power distribution of propagating modes is required.

Distribution of Un-trapped radiation

$$P_{total} = \int_0^{\omega_c} \frac{dP}{d\omega} d\omega + \int_{\omega_c}^{\omega} \frac{dP}{d\omega} d\omega$$

- Power below cut off frequency is extracted by HOMs coupler
- HOMs above cut-off propagates along the linac make several reflection on the surface of beamline elements.
- Numerical estimation of propagating HOMs power (spectrum ranging up to tera-Hertz) is unfeasible.
- A diffusion model is prepared to understand power distribution of propagating HOMs in LCLS-II linac.
- Model is based on assumption that HOMs above cut-off frequency can be treated as photons gas uniformly distributed in a cryomodule..
- It is also assumed that total wake power generated in a cryomodule is dissipated inside cryomodule.
 - Assumption is valid in long cryostrring arrangement.

Diffusion Model

- Power absorption is proportional to impedance of element.

$$I_i^{abs}(\omega) \sim n_i S_i \frac{dP(\omega)}{d\omega} \text{Re}(Z_i(\omega)) d\omega$$

- S_i : Surface area of i^{th} element, i is type of element such as cavity, bellows, beam pipe etc; n : no of elements, ω : angular frequency, $dP(\omega)/d\omega$: HOM spectral power, $\text{Re}(Z_i(\omega))$: real part of surface impedance.

- Power absorbed by i^{th} type element is

$$P_i = \int_0^{\infty} \frac{dP}{d\omega} \frac{I_i^{abs}(\omega)}{\sum I_i^{abs}(\omega)} d\omega$$

- *Total Power losses in a cryomodule is $P_{cryo} = 12.8 \text{ W}$ for L3 section and 9.5 W for HL section .*

Surface Impedance of Elements

- *BCS surface resistance is* : $Z_{BCS} = \frac{A}{T} * f^2 \exp(\frac{-\Delta}{kT})$
 - Assuming surface impedances of cavity operating at 1.3 GHz at 2K is 5 nΩ

$$Z_{cav}(\omega) = Z_{cav}(1.3GHz) * \frac{f^2}{1.3^2}$$

- Surface impedance of steel is computed using:

- $$Z_{Bellow}^{SS}(\omega) = \text{Re}\left(\frac{1+i}{\sqrt{2}}\sqrt{\frac{\omega\mu_0}{\kappa}}\right)$$

- κ is electrical conductivity. We used $\kappa = 1E+06$ 1/ Ωm for stainless steel.

- Copper exhibits anomalous effects at 4K at higher frequencies.

- $$Z_{Bellow}^{Cu} = \text{Re}\left(A.\omega^{2/3}.(1+i\sqrt{3})\right)$$

- $A = 3.3E-10$ (W sec^{2/3}).

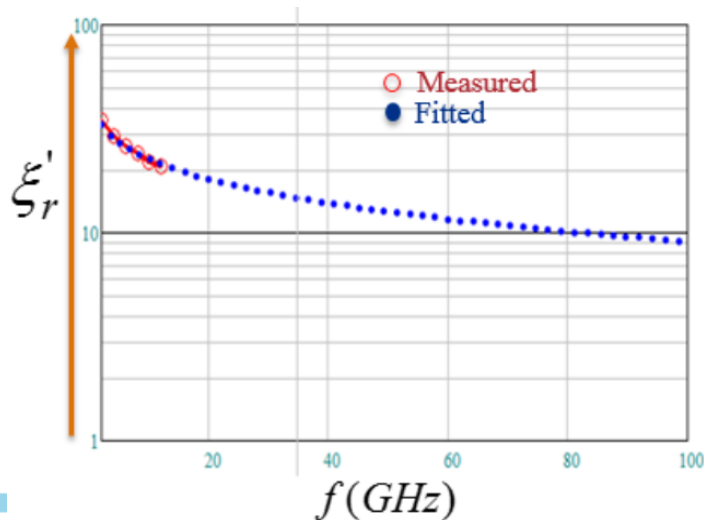
Surface Impedance of Absorber

- Attenuation coefficient (α) in lossy medium is:

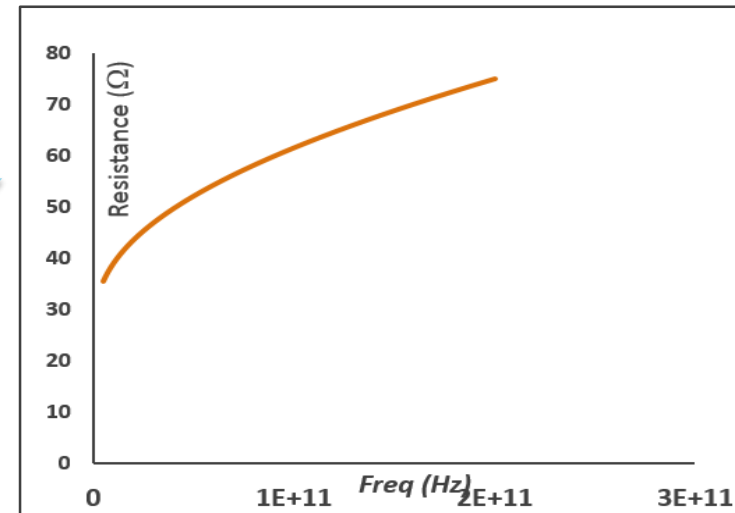
$$\alpha(\omega) = \frac{\omega}{c\sqrt{2}} \sqrt{(\xi_r' \mu_r')} \cdot \sqrt{(\sqrt{1 + \tan^2 \delta_d}) - 1};$$

$$\tan \delta_d = \frac{\xi_r''}{\xi_r'}; \delta_s = \frac{1}{\alpha}; \quad \kappa = \xi_r'' \xi_0 \omega; \quad Z_{Absorber} = \frac{1}{\kappa \delta_s}$$

- where ξ_r' , ξ_r'' are real and imaginary part of relative electrical permittivity and μ_r' is relative permeability.
- STL-150D aluminum nitride ceramic is chosen for absorber material. Loss tangent for this material is >0.4 and $\xi_r' < 30$.



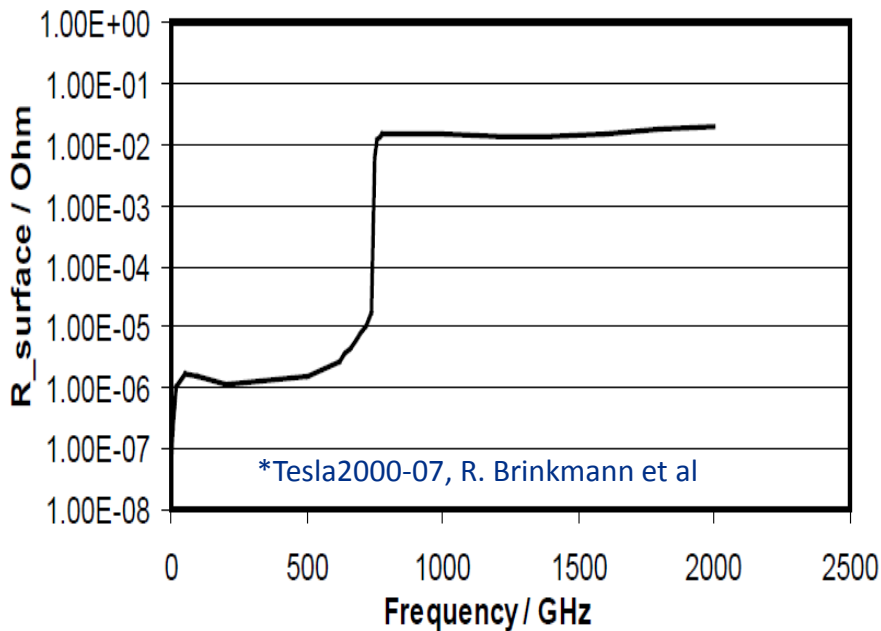
Absorber Impedance



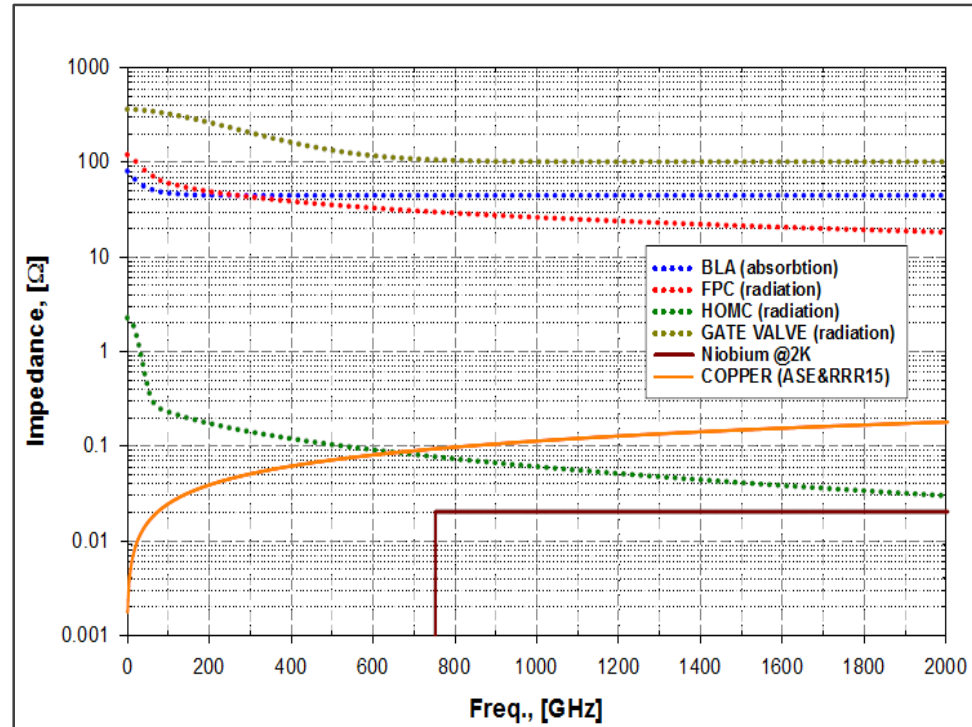
Variation in Surface Impedance with Frequency

Cavity Impedance

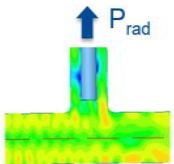
Surface Resistance of Nb @ 2K vs. Frequency



Impedance of other Elements



- Surface impedance of cavity is much smaller at frequency < 750 GHz.
- A fraction of power is also radiated out through coupler port and gate valves. Their contributions are included and corresponding impedances are used in model for power loss distribution.



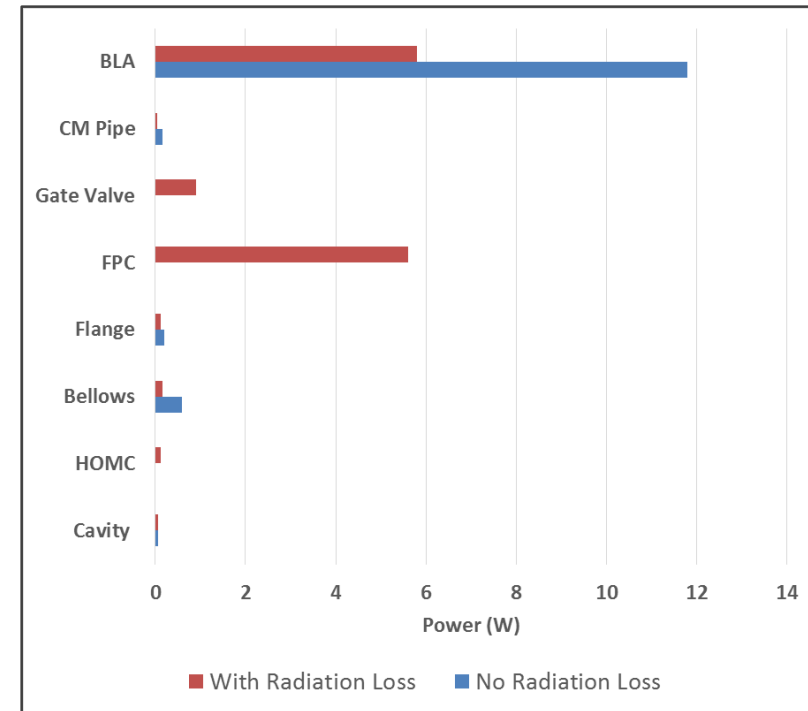
Distribution of Untrapped radiation in 1.3 GHz CM

- ❑ 2 K : Cavities, Bellows, Flanges, Gate Valve, Cryomodule Beam pipes
- ❑ 70 K: Absorbers,

	P_{Cavity}	P_{HOMC}	P_{FPC}	P_{Bellows}	P_{Flange}	P_{BLA}	P_{GV}	$P_{\text{CM pipe}}$
n	8	16	8	9	22	1	2	1
	0.07	0.13	5.6	0.16	0.2	5.8	0.9	0.05

- Power dissipation at 2K (inside the cavity) is negligible.
- If no radiation loss to the coupler ports and HOMs are considered, most of HOM power is deposited to the absorber at 70 K.
- Power is uniformly distributed between fundamental power coupler (FPC) and absorber if radiation losses were included.
- Most of power going to coupler is absorbed outside the operating environment.

Distribution of power losses (Watt) in Cryomodule



Distribution of unstrapped radiation in 3.9 GHz section

Baseline layout of 3rd Harmonic section.

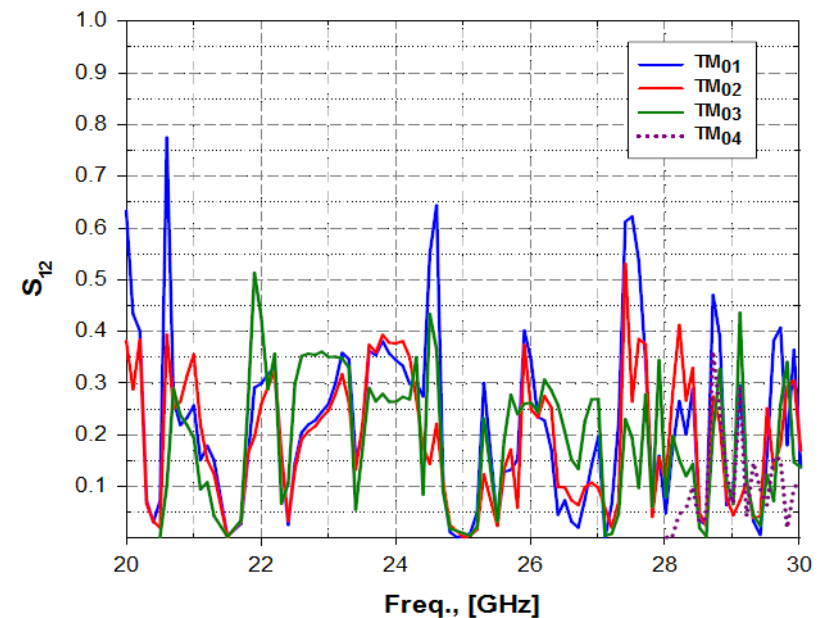
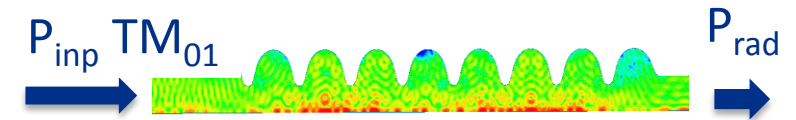
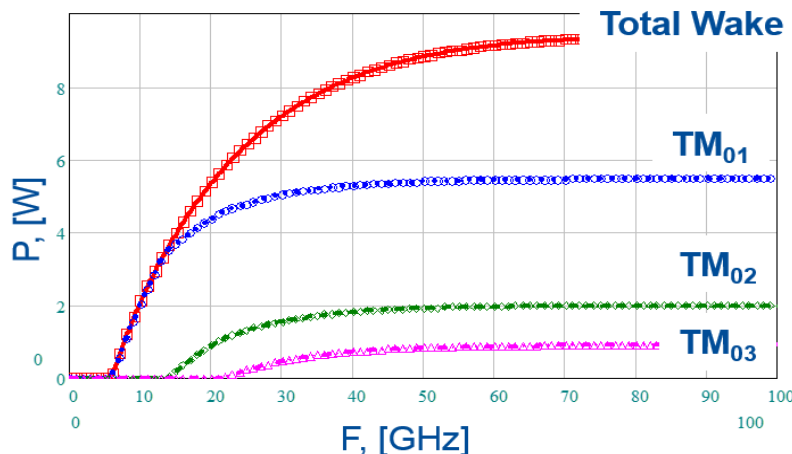


- Third harmonic section consists of two 3.9 GHz cryomodules.
- Each cryomodule consists of eight 9-cell 3.9GHz cavities.
- Wake power loss per cryomodule is 13.6 W. Contribution of untrapped radiation is 9.4 W.
- Un-trapped radiation will leak out from cryomodule ends.
 - Diffusion model based on assumption that total HOMs power dissipated in CM provide overestimation.
- Distribution of un-trapped radiation is estimated using two approach
 - Modified diffusion model that assumed total wake power will be lost in the section.
 - S-matrix based wake decomposition model.

Wake decomposition model(1):

- Model is based on the fact that wake fields can be decomposed into propagating modes.
 - Assumed only monopole modes are excited by beam.
- Wake power at a given frequency is expressed as:

$$\frac{dP_{wake}(\omega)}{d\omega} = \sum_{n=1}^N \frac{P_{TM_{0n}}}{N}$$
 - where N is no of propagating modes.
- Most of the total wake power in 3.9 GHz CM is contained in first few modes.



Transformation of 20 GHz TM_{01} mode passing through 3.9 GHz Cavity

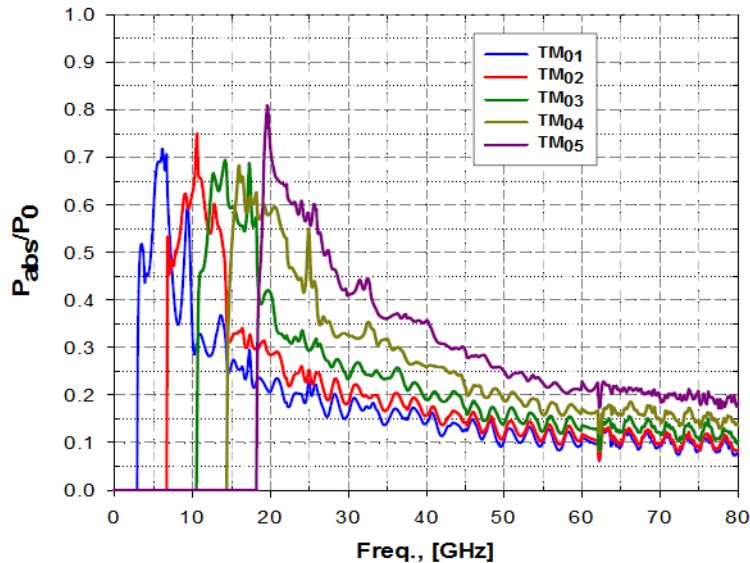
Wake Decomposition Model(2): Single Pass Absorption

- Fraction of power absorbed by a element in a single pass of un-trapped radiation is

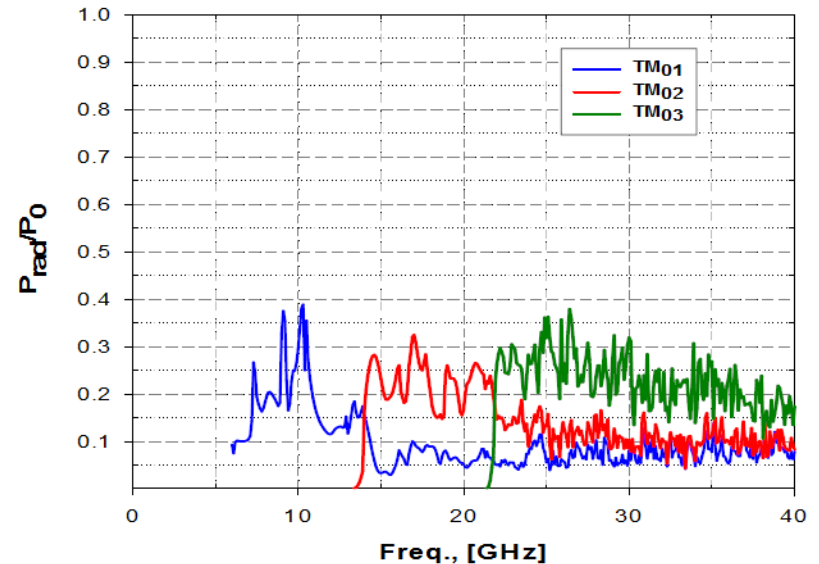
$$P_{abs} \approx \sum_{n=1}^N \int_{\omega}^{\infty} \frac{dP}{d\omega} (1 - S_{12}^2 - S_{11}^2) d\omega$$

- Single pass losses are computed numerically using HFSS for all elements in Cryomodules.

Beam Line Absorber



Fundamental Power Coupler



Component	BLA	FPC	Gate Valve	HOMC	Bellows (Cu-plated)	End Pipe (2.5 m, SS)	End Pipe (ø32 mm, rad.)
1-pass loss, [%]	42	23	2.7	1.6	0.2	11	41

Wake Decomposition Model (3): Power loss in Cryomodule



- Power radiated at each side of CM
- $PCM_{rad} \approx \frac{P_0}{16} \sum_{i=1}^8 \left(1 - (SP_{FPC} + 2 \times SP_{HOM} + SP_{BELLOWS})\right)^i = 1.5W$
 - SP is a single pass power loss in the FPC, HOMC and bellows.
- Power absorbed in a CM is:
 - $PCM_{loss} = P_{wake} - 2 \times PCM_{rad} = 6.4 W$.
- Power absorbed at BLA2 is:
 - $P_{BLA2} \approx (PCM_{rad} - P_{GV2}) \times 0.42 = 0.6 W$
 - where P_{GV2} is power absorbed at Gate valve.
- **Power loss at BLA2 is small and we could remove this.**
- New proposed layout of HL section:



Un-trapped Radiation Distribution in Third Harmonic Section



Components	#	Surface Area, [mm ²]	Power Deposition, [W]	
			Wake Decomposition	Diffusion
BLA	2	1.4e4	3.6	11.5
End Pipe (SS)	1	6.2e5	0.12	0.6
End Pipe (Rad)	2	804	1.1	-
Bellows (Cu&SS)	18	3.7e4	0.12	0.12
Gate Valve	4	2.0e2	0.4	1.1
Spool Pipe (Cu)	1	1.0e5	0.01	0.01
HOMC	32	3.1e2	1.6	0.6
FPC	16	7.1e2	12.0	5.0
Total Wake Power			18.9	18.9

- Wake decomposition model predicts a small fraction of power loss to BLA.
- Most of power is intercepted before it reaches to BLA.
- ~1W power is leaked out from section.
- Analysis allows to get rid of BLA2.

Implications of un-trapped radiation : Cooper Pair Breaking

- Additional HOM power deposited on surface of superconducting cavity will result in an increase in wall losses
 - Increase in Surface temperature (small ~ mK)
 - Increase in fraction of unpaired electrons.
- Cooper pairs are basis of superconducting state. In nominal conditions, number of Cooper pairs in penetration depth $\delta \sim 100 \text{ nm}$ are:

$$N_{Cooper} \cong \frac{\Delta E}{E_f} n_e S_{cav} \delta$$

where $\Delta E = 1.55 \times 10^{-3}$ is band gap of niobium, Fermi energy, $E_f = 5.35 \text{ V}$, surface area of cavity $S_{cav} = 0.8 \text{ m}^2$. n_e is density of normal conducting electrons $= 2.3 \times 10^{30}$. It yields $N_{cooper} = 2.3 \times 10^{19}$

- Interaction of photons with Cooper pair at frequency above Cooper pair breaking threshold frequency, $f_{cbp} = 750 \text{ GHz}$ results in breaking of Cooper pairs.

Cooper Pair Breaking(2)

- First few cavities at the beginning of sections will experience largest cooper pair breaking due to transient wakes.
- Maximum radiated wake power is deposited in L3 section.
- No. of photons with $f \geq 750 \text{ GHz}$ interacting with cavity is:

$$N_{ph} = \frac{1}{8} \frac{r_{cpb} U_{wake}}{hf_{cbp}}$$

where $r_{cbp}=0.33$ is fraction of HOMs power above $f \geq 750 \text{ GHz}$, $U_{wake}=30 \mu\text{J}$ is transient wake energy and h is plank constant. It yields 5.4×10^{15} .

- $N_{Cooper} \gg N_{ph}$
- No of cooper pair breaking is negligible even for the case when maximum wake power is deposited to the surface of SC cavities in LCLS-II linac.
- Cooper pair recombination time is $\sim 0.4 \text{ ps}$. Equilibrium state is achieved during the time next bunch ($1 \mu\text{s}$ later) traverses through the cavity and therefore no cumulative effects are present.

Implications of Cooper pair breaking is minimum in LCLS-II SC linac

HOMs trapping and Resonance Excitation

- HOMs Heating
- Emittance Dilution

HOMs Modes below 12 GHz are considered.

Resonance Excitation and Trapping: HOMs Heating:

- Total power dissipated at surface of the cavity due to HOMs excited by beam harmonics is given as:

$$P_c = \sum_p \sum_n \frac{\omega_p^4}{(\omega_n^2 - \omega_p^2)^2 + \left(\frac{\omega_n \omega_p}{(Q_L)_p} \right)^2} \frac{I_n^2}{4} \left(\frac{R}{Q} \right)_p \left(\frac{1}{Q_0} \right)_p$$

I_n and ω_n : amplitude and frequency of beam harmonic.

ω_p : Angular frequency of p^{th} mode.

Q_L : Loaded quality factor for p^{th} mode.

Q_0 : Cavity quality factor for p^{th} mode.

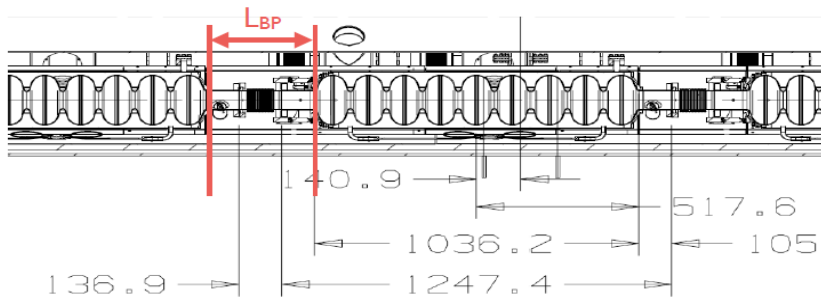
- Power dissipated if the p^{th} mode is close to frequency of beam harmonic:

$$P_c = \frac{1}{1 + 4Q_L^2 \left(\frac{\Delta f}{f_p} \right)^2} \frac{I_n^2}{4} \left(\frac{R}{Q} \right)_p \left(\frac{Q_L^2}{Q_0} \right)_p$$

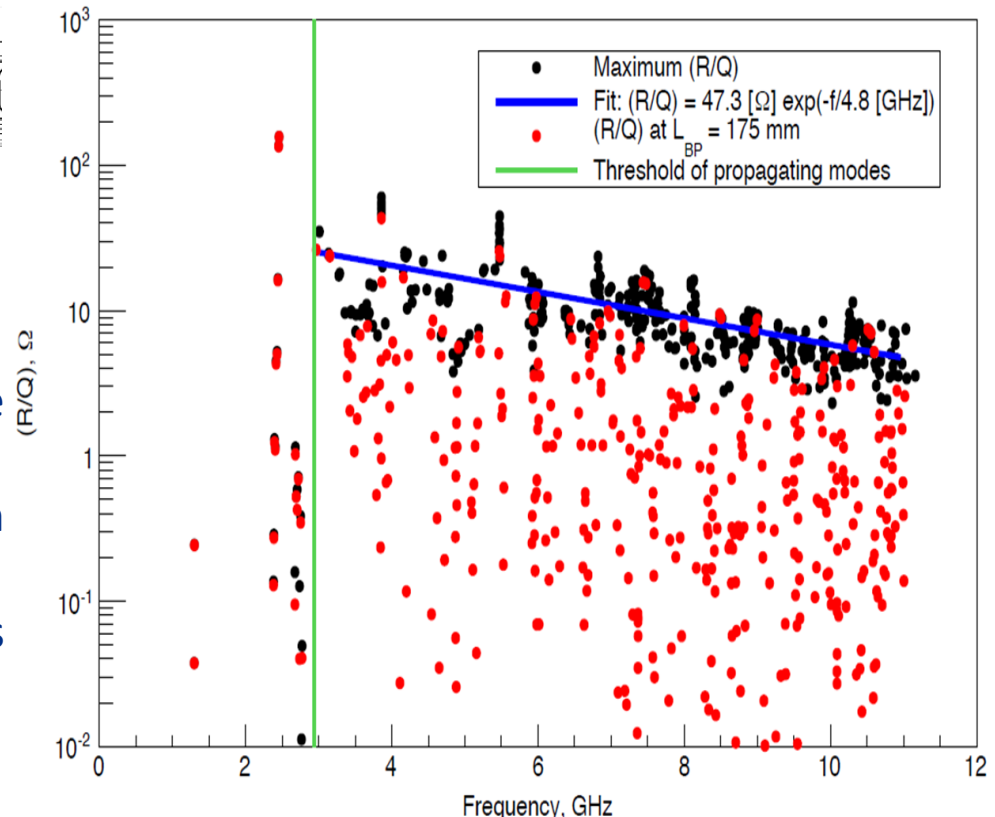
- In order to estimate maximum power loss due to HOMs we use following approach:
 - Maximum (R/Q) is computed by creating mode trapping conditions.
 - A random RMS frequency spread of 1MHz in HOMs is introduced from cavity to cavity.

Maximum (R/Q) Estimation:

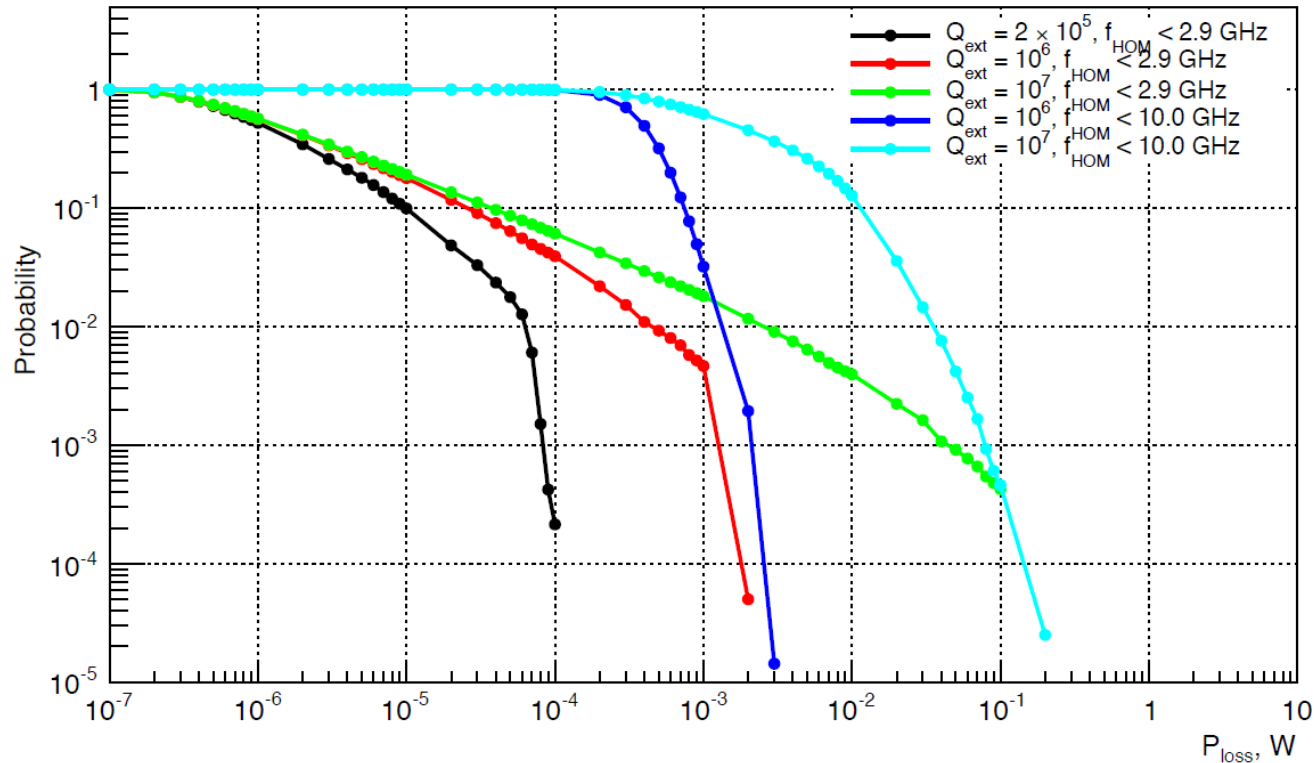
- Propagating HOMs may form standing wave in a periodic arrangement of cavities and get trapped.
- In order to find trapped modes, length of beam pipe connecting neighboring cavities is varied.



- Monopole modes up to 11 GHz are computed for 1.3 GHz 9-cell cavity
- A linear fit is obtained for maximum (R/Q) for respective modes.
- Those values are used for power loss estimation.

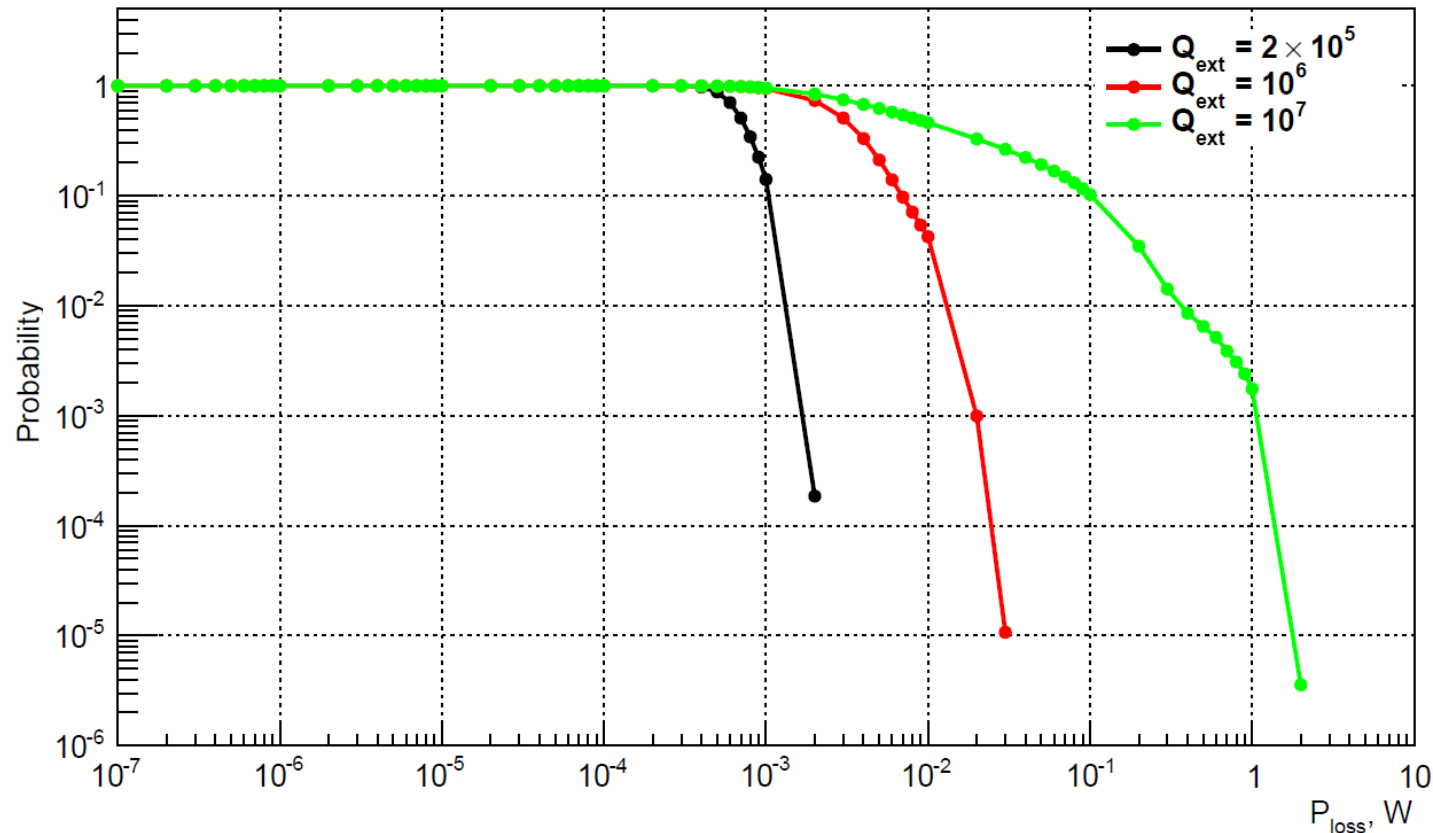


Power losses on surface of 1.3 GHz Cavity



- Study is performed for 10^5 . RMS frequency spread of 1MHz is applied cavity to cavity.
- Results is presented in terms of complimentary cumulative distribution function.
- Median losses (50 % probability) for frequency up to 10 GHz is $\sim 1\text{mW}$ for the case of $Q_{\text{ext}}=10^7$.

Power Losses on surface of 3.9 GHz Cavity

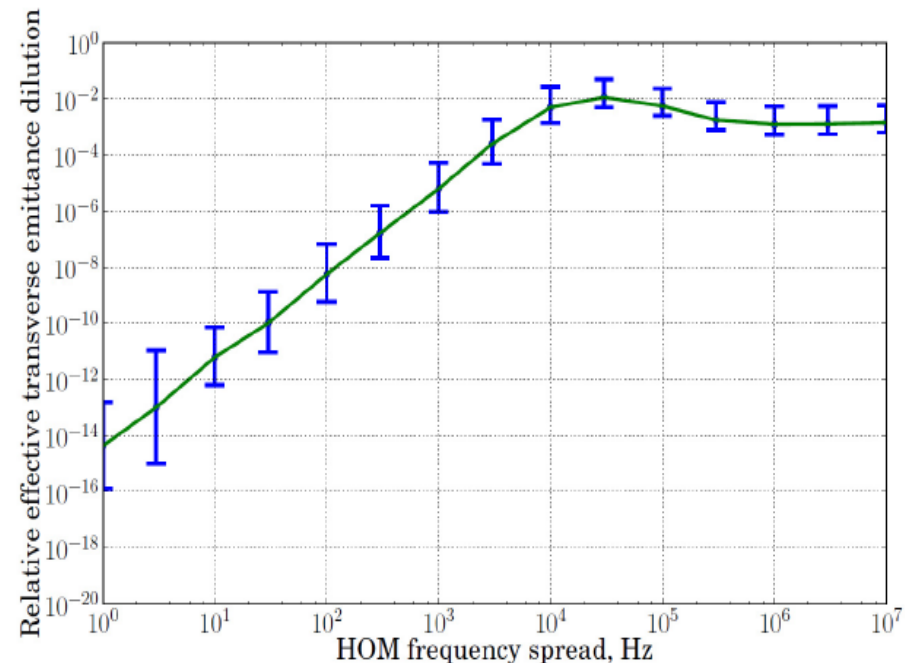


- Similar approach is used to estimate power losses in 3.9 GHz cavity.
- Median losses (50 % probability) for frequency up to 10 GHz is ~ 10 mW for the case of $Q_{\text{ext}} = 10^7$.

Dipole Modes Excitation: Cumulative Effects

- A bunch passing through the cavity with an offset excites the dipole modes in cavity.
- Dipole modes result in a transverse kick to the following bunches. Offset bunches further excites dipole.
- Similar approach is used and study is performed to analyze maximum emittance dilution.
- Maximum (R/Q) for dipole modes are computed by creating trapped mode conditions.
- Cavity RMS misalignment of 0.5 mm is applied.
- An RMS frequency spread of 1MHz in HOMs is introduced from cavity to cavity.
- *NO significant Impact in framework of LCLS-II SC Linac*

Emittance Dilution in L3 section



Transition Effects:

- Sudden interruption in bunch pattern will result a phase shift between HOMs fields and bunch arrival.
 - Implication on
 - Longitudinal dynamics
 - Transverse dynamics

Switching from one undulator section to another and time to time beam delivery to diagnostic section will disturb regular bunch pattern in LCLS-II linac and therefore will result in the transition effects

Transition Effect: Longitudinal

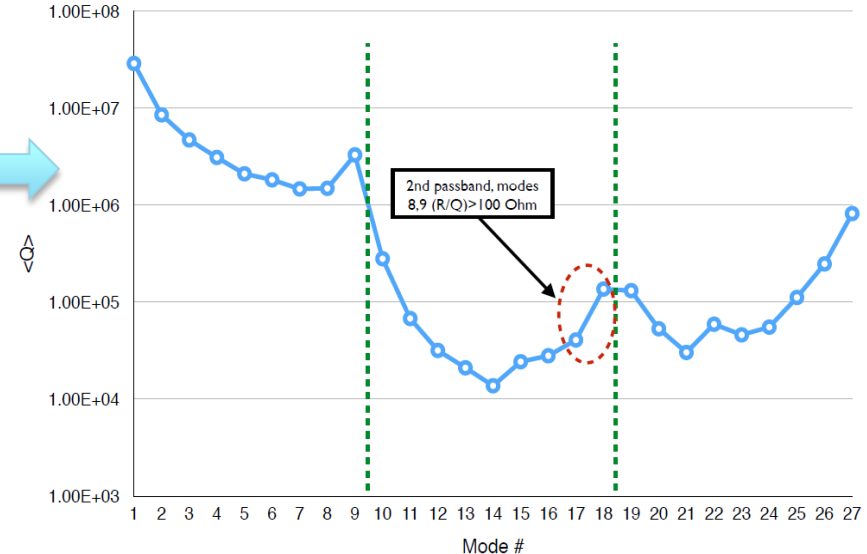
- Voltage corresponds to i^{th} mode in a cavity is given as:

$$V_{cav,i}(t=0) = \frac{1}{2} \left(\frac{R}{Q} \right)_i \omega_i Q_b$$

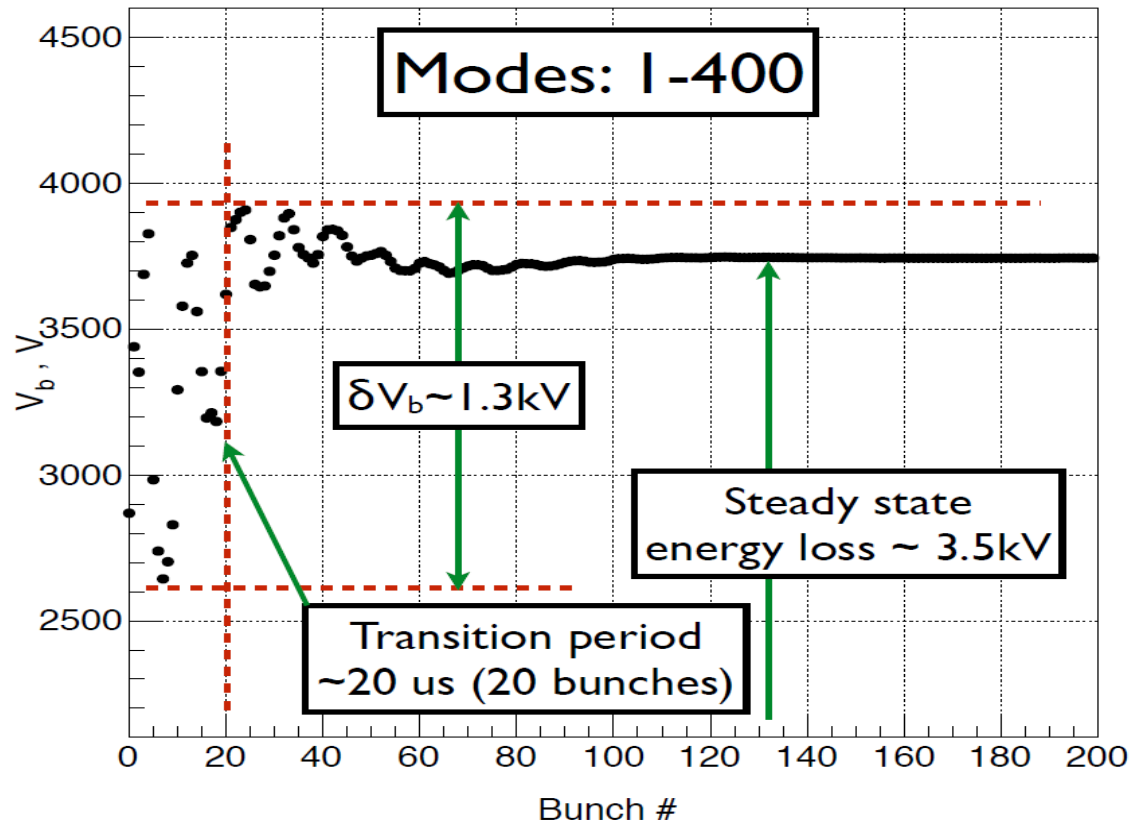
- N^{th} bunch passing through the cavity see voltage:

$$V_{b,i}\left(t = \frac{N}{f_b}\right) = V_{cav,i}(t=0) \left(\frac{1}{2} + \sum_{n=1}^N \cos\left(\frac{\omega_i n}{f_b}\right) \exp\left(-\frac{\omega_i n}{2Q_{ex,i} f_b}\right) \right)$$

- Total voltage seen by N^{th} bunch can be obtained by summing over all excited modes.
- 400 modes are used in studies.
- Quality factors for first three monopole passbands were measured at Fermilab.
- Rest of modes we use $Q_{ex,i}=10^5$



Transition Effects on Longitudinal Beam Dynamics



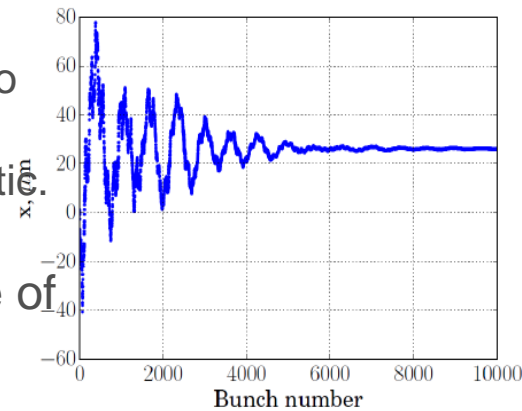
- Energy variations among the 200 bunches at the end of L3 section are computed for first 400 modes in 1.3 GHz cavity.
- Maximum bunch to bunch energy variation is 1.3 keV.
- Steady state energy loss is 3.5 keV.
- Laser Heater introduces RMS energy spread of 20 keV.

Bunch to bunch energy spread is within specification

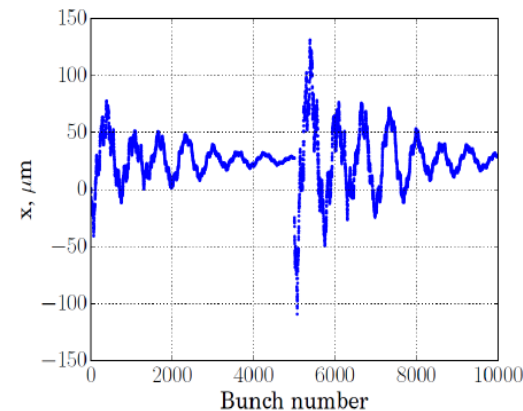
Transition Effects on Transverse dynamics

- RF deflector operates at 325 MHz.
- Beam phase is shifted by
 - 180° at 325 MHz during switching to undulator section.
 - 360° at 325 MHz for beam diagnostics.
- A steady state is achieved with residual beam centroid shift in case of
 - No beam phase shift
 - Beam phase shift interval is longer (5ms).
- Fast periodic beam phase shift results in
 - Beam centroid oscillation with large amplitude due to correlation in transition effects from each shift.
- A beam centroid shift of 200 μm for periodic beam phase shift with 1kHz rate satisfies LCLS-II specification.

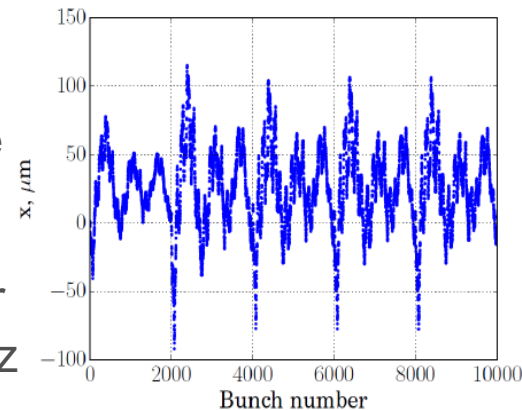
Transverse beam centroid of bunches



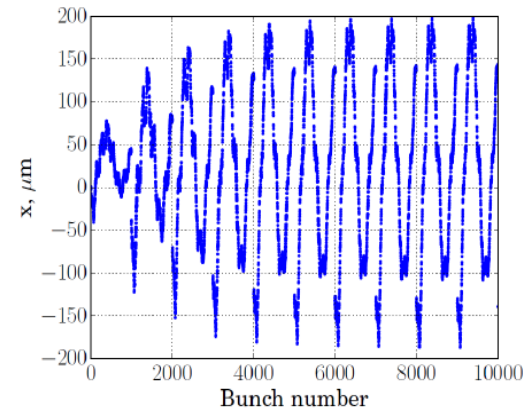
(a) HOM phase shift is off.



(b) Sudden HOM phase shift by 180° .



(c) Periodic 500 Hz HOM phase shift by 180° .



(d) Periodic 1 kHz HOM phase shift by 180° .

Beam centroid shift as large as 5 mm can be corrected using steering correctors:

LCLSII-TN-14-03, A.Saini et al, Studies of Misalignment Tolerances for SC Linac of LCLS-II.

Summary

- Bunch with total charge of 300pC and RMS length of 25 μm will result in HOM power losses of 13.8 W and 13.4 W per cryomodule in L3 and HL sections respectively.
 - HOMs losses are included in cryogenic budget and LCLS-II cryomodules are capable to deal with those losses.
- Distribution of un-trapped radiation power is analyzed using two approaches
 - Diffusion model and Wake decomposing model.
 - HOMs power deposited to cavity is negligible.
 - A significant HOMs power is radiated out through coupler ports.
- Implications of resonance excitation were studied for worst cases
 - HOMs power dissipation in cavity is below 10 mW even for $Q_{\text{ext}}=10^7$.
 - Maximum emittance dilution is below 10 % in L3 section
- Transition effects have been addressed.
 - A steady state energy loss is 3.5 keV
 - Maximum beam centroid shift for periodic beam phase shift at the rate of 1kHz is 200 μm .

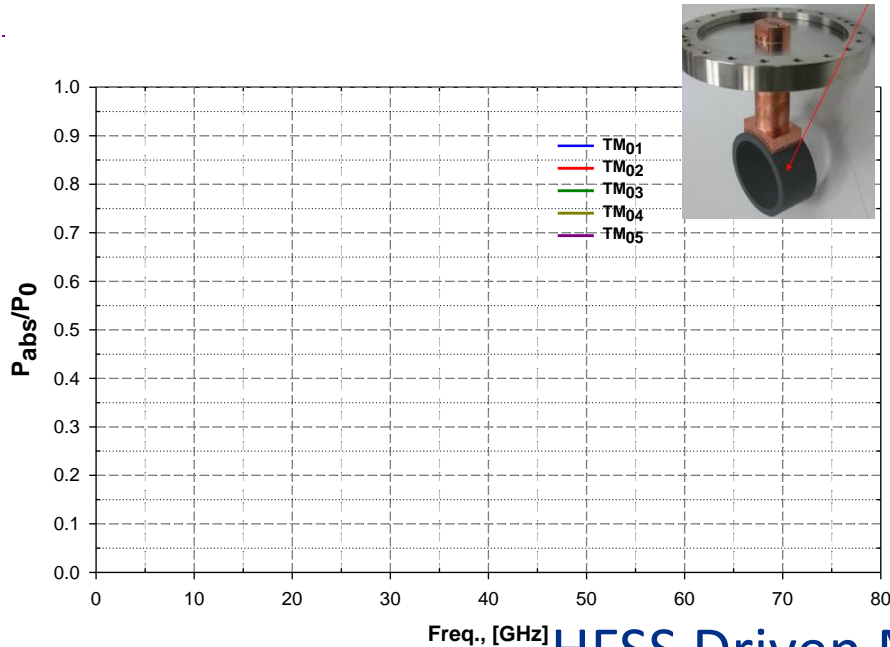
Acknowledgement

A. Lunin, A. Sukhanov, N. Solyak, V. Yakovlev and entire
LCLS-II SRF Team

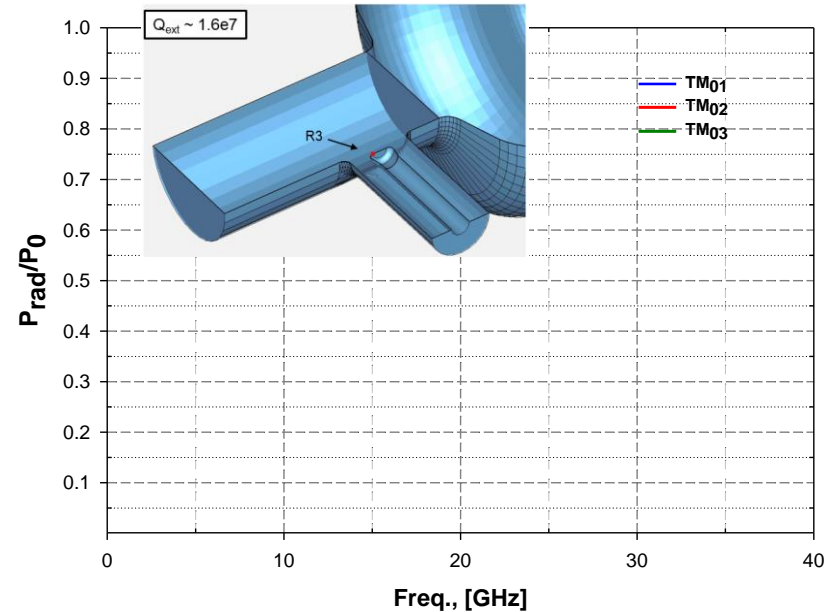
Back-up Slides

Wake transmission (single pass) through beam line components

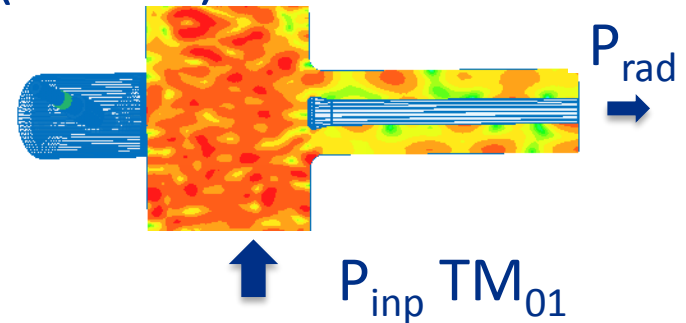
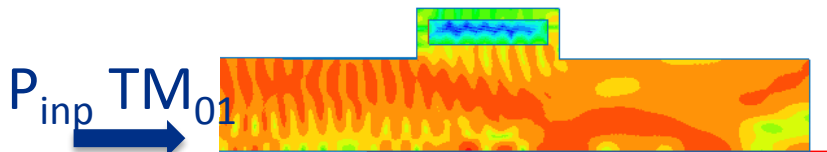
BLA wake loss is $\sim 42\%$



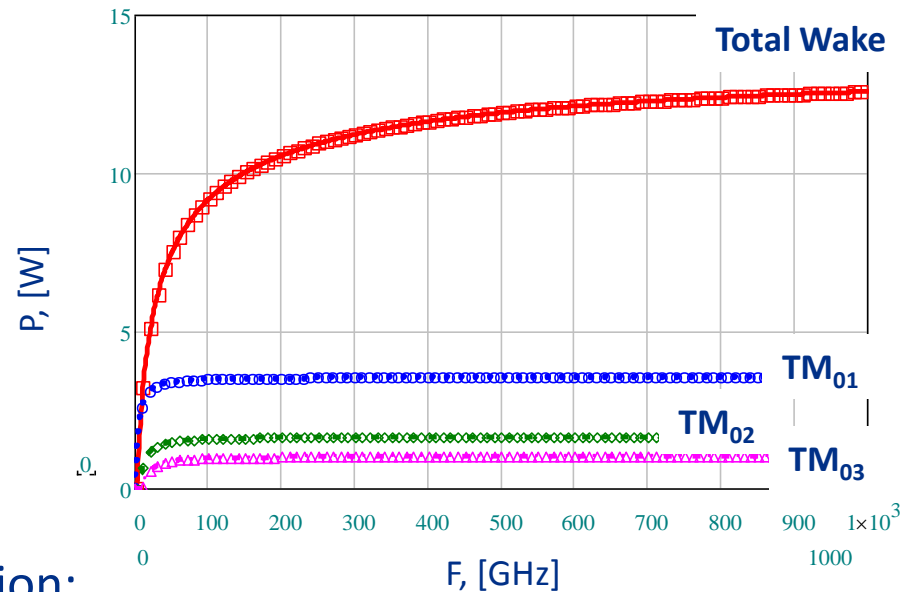
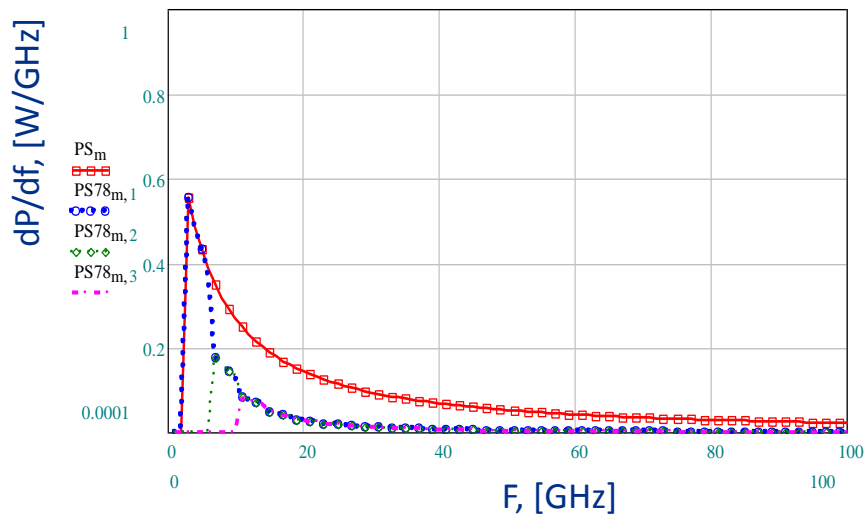
FPC wake loss is $\sim 9\%$



HFSS Driven Modal (20 GHz)



Wake Power Deposition (Transition Model)



Wake Monopole TM-modes Decomposition:

$$P(f) = \sum_{n=1}^{N(fc_n)} \frac{P_{TM_{0n}}}{N(fc_n)}, \text{ where } N(fc_n) \text{ is number of } TM_{0n} \text{ modes below the cut off frequency}$$

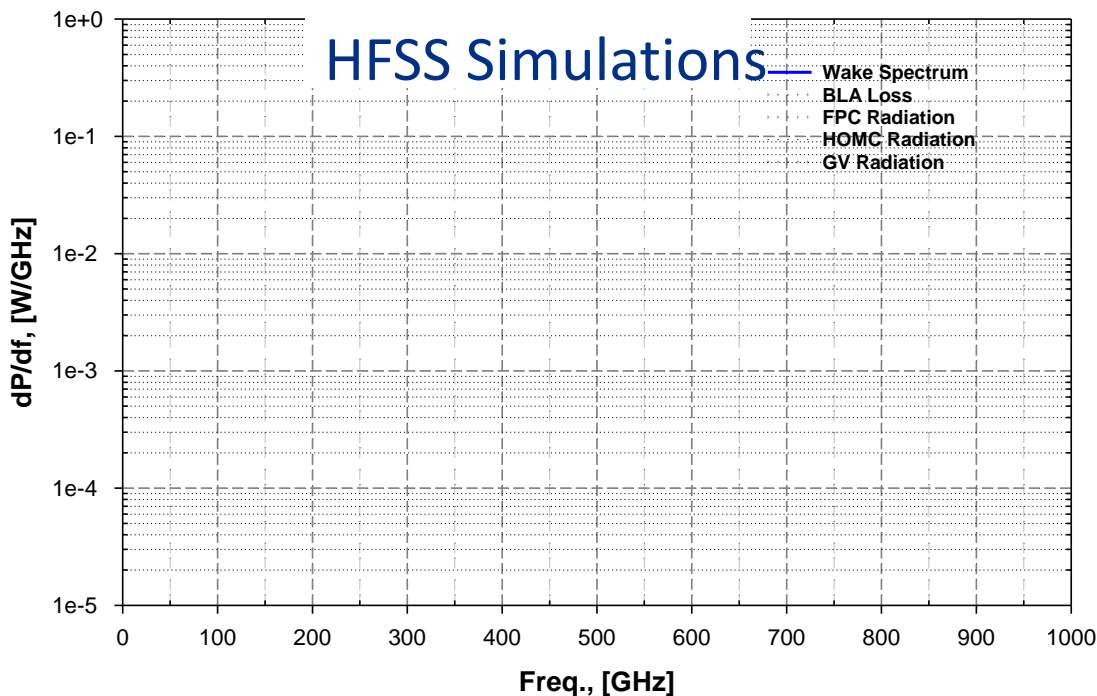
Transition model approaches wake power deposition by a direct calculation of monopole modes transitions through beam line components (BLA, FPC, HOMC, Gate Valves):

$$P \approx \sum_{n=1}^N \int_{fc}^{\infty} \frac{dP_{TM_{0n}}}{df} (1 - S_{12}^2) df$$

Wake Power Deposition (Diffusion Model)

TM-mode Loss in the Circular Pipe:

$$dP_n(\omega) = P_0(1 - e^{-2\alpha_n l}) \quad \alpha_n(\omega) = \frac{(\omega)}{Z_0 r} \left(\sqrt{1 - \left(\frac{\omega c_n}{\omega} \right)^2} \right)^{-1}$$



$$dP(\omega) = \sum_{n=1}^{N(\omega c_n)} dP_n(\omega)$$

$$2\pi r l_n = S_n$$

where, S_n is the area of lossy (radiating) surface and l_n is the length of a beam pipe with an equivalent impedance $Z(\omega)$

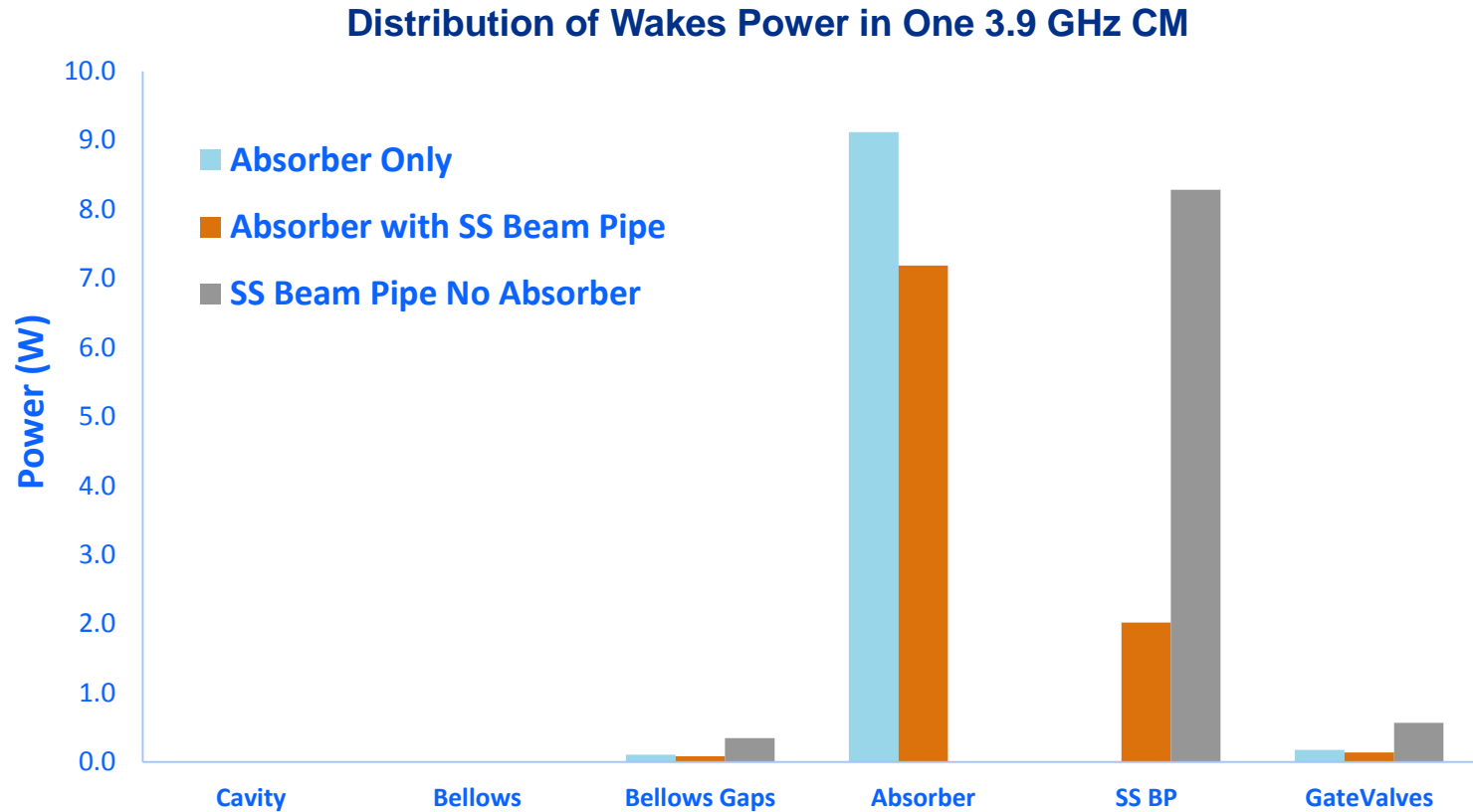
We can derive the equivalent surface impedance $Z(\omega)$ for beam line components

Wake Power Deposition in the 1.3 GHz Cryomodule (Diffusion Model)

Components	#	Surface Area, [mm ²]	Power Deposition, [W/CM]	
			Cu Bellows	SS Bellows
BLA	1	1.4e4	5.8	5.1
Cavity (Nb)	8	9e5	0.07	0.04
Flanges (SS)	18	2.4e3	0.13	0.12
Bellows (Cu&SS)	9	6.4e4	0.16	1.7
Gate Valve	2	2.0e2	0.9	0.8
Spool Pipe (Cu)	1	2.2e5	0.05	0.04
HOMC	16	1.3e3	0.13	0.12
FPC	8	1.3e3	5.6	4.9
Total Wake Power			12.8	12.8

1. Non-plated SS bellows intercept < 2 W/CM of wakefield power
2. About 43% of wake power is radiated to FPC & HOMC couplers!

Power Losses Distribution in One 3.9 GHz Cryomodule



Total Power Deposition: 9.5 W

Wake Power Deposition (Diffusion Model)

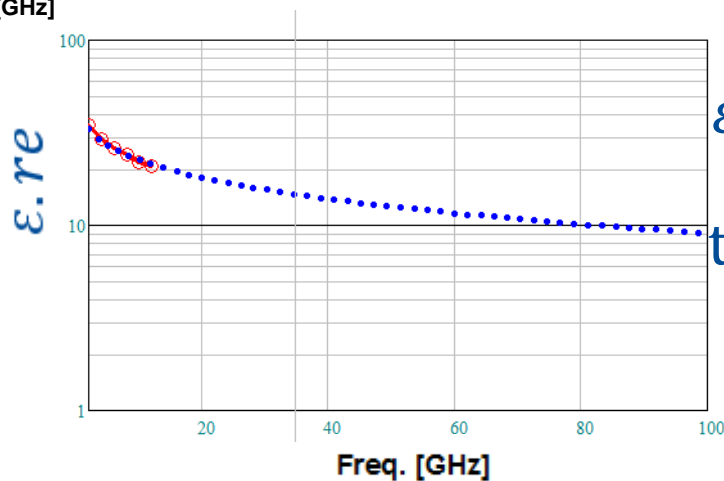
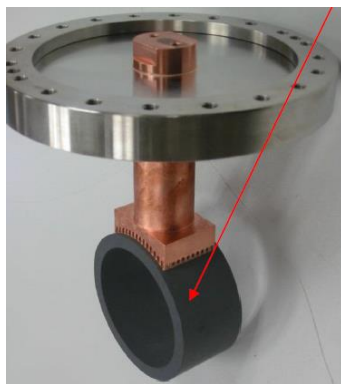
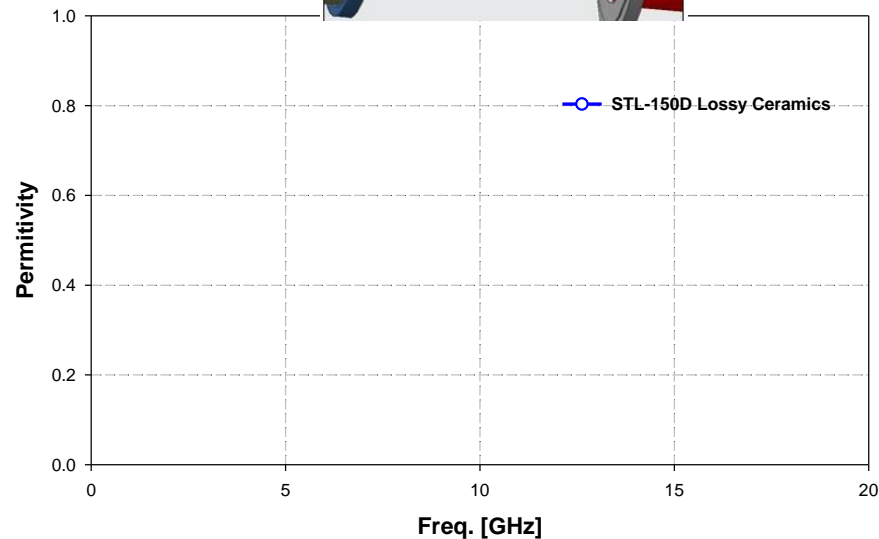
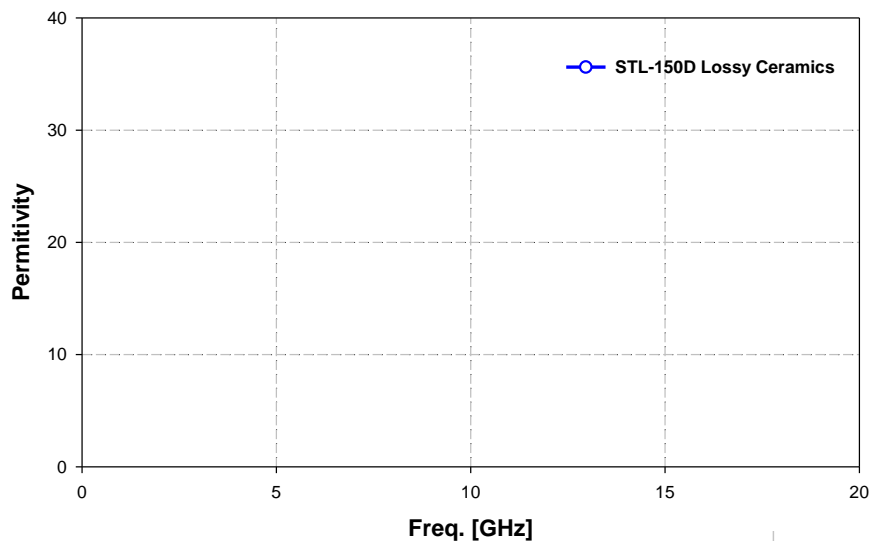
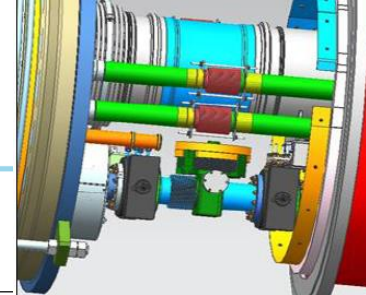
Wake Loss in the 3rd harmonic section

Components in 2 CM's	Power Deposition, [W]			
	A (baseline)		B	C
	w/o HOM&PC	with HOM&PC	with HOM&PC	with HOM&PC
BLA (1 or 2)	16.2 (per 2)	13.5	10.5	14.5
SS end-pipe 2.5m (1)	1.65	1.4	2.2	0.07
Bellows (17)	0.36	0.3	0.4	0.27
Gate Valve (4)	0.6	0.45	0.7	0.5
Spool Pipe (2)	0.02	0.02	0.03	0.02
HOMC (32)	0	0.5	0.75	0.5
FPC (16)	0	2.7	4.1	2.8
Total power	18.8			

Beam Line Absorber properties

Sienna Technologies AlN STL-150D

$\epsilon < 30$ @ $\tan \delta > 0.4$ for $5 \text{ GHz} < f < 12 \text{ GHz}$



$$\epsilon.re(f) \approx 73e^{-0.66f^{0.25}}$$

$$\tan(\Delta) = 0.4 = \text{const}$$

Model for HOMs Trapping and Resonance Excitation in LCLS-II SC linac(2)

- Power losses at cavity surface and Bellows are estimated for each mode.
- Total mode losses is computed as: $\frac{1}{Q_L} = \frac{1}{Q_0} + \frac{1}{Q_b} + \frac{1}{Q_h}$;

Q_0, Q_b, Q_h , are quality factor associated with power losses to cavity surface, bellows and HOM & power coupler. Q_h used in this analysis is $2 \times 10^5, 10^6, 10^7$

- Magnetic field induced on the surface of cavity by nth component of beam spectrum is given is sum of all excited modes:

$$- \quad H_n = \sum_p H_{pn}(z); \quad H_{pn} = \frac{-i\omega_p^2}{\omega_n^2 - \omega_p^2 - i\frac{\omega_n\omega_p}{(Q_L)_p}} \frac{I_n}{2} \sqrt{\frac{(R/Q)_p}{\omega_p W_p}} H_p^{Sim}$$

$$- \quad P_{(0,h,b)} = \sum_p \sum_n \frac{\omega_p^4}{(\omega_n^2 - \omega_p^2)^2 + \left(\frac{\omega_n\omega_p}{(Q_L)_p}\right)^2} \frac{I_n^2}{4} \left(\frac{R}{Q}\right) \left(\frac{1}{(Q_{(0,h,b)})}\right)$$

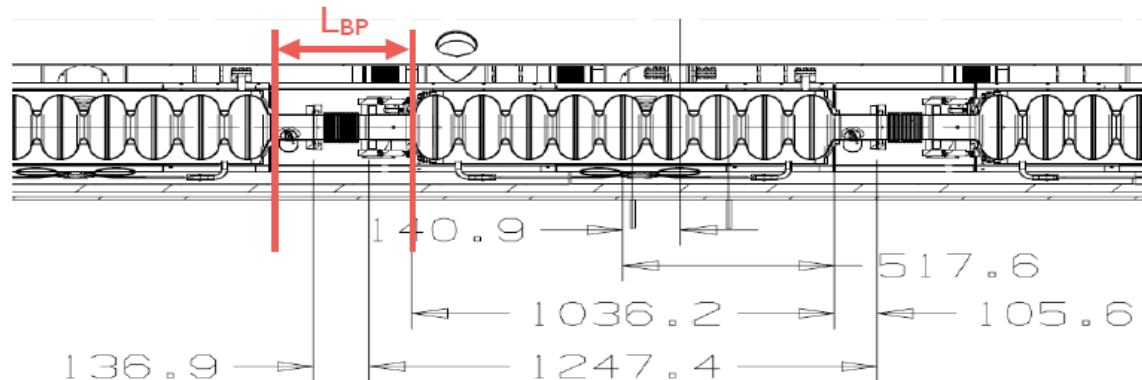
H_p^{Sim} : is simulated magnetic field for pth mode.

I_n and ω_n : amplitude and frequency of beam harmonic.
 W_p : is energy stored in cavity.

- HOMs frequency vary cavity to cavity by RMS value of 1MHz
- Idealized beam current spectrum is used for this studies.

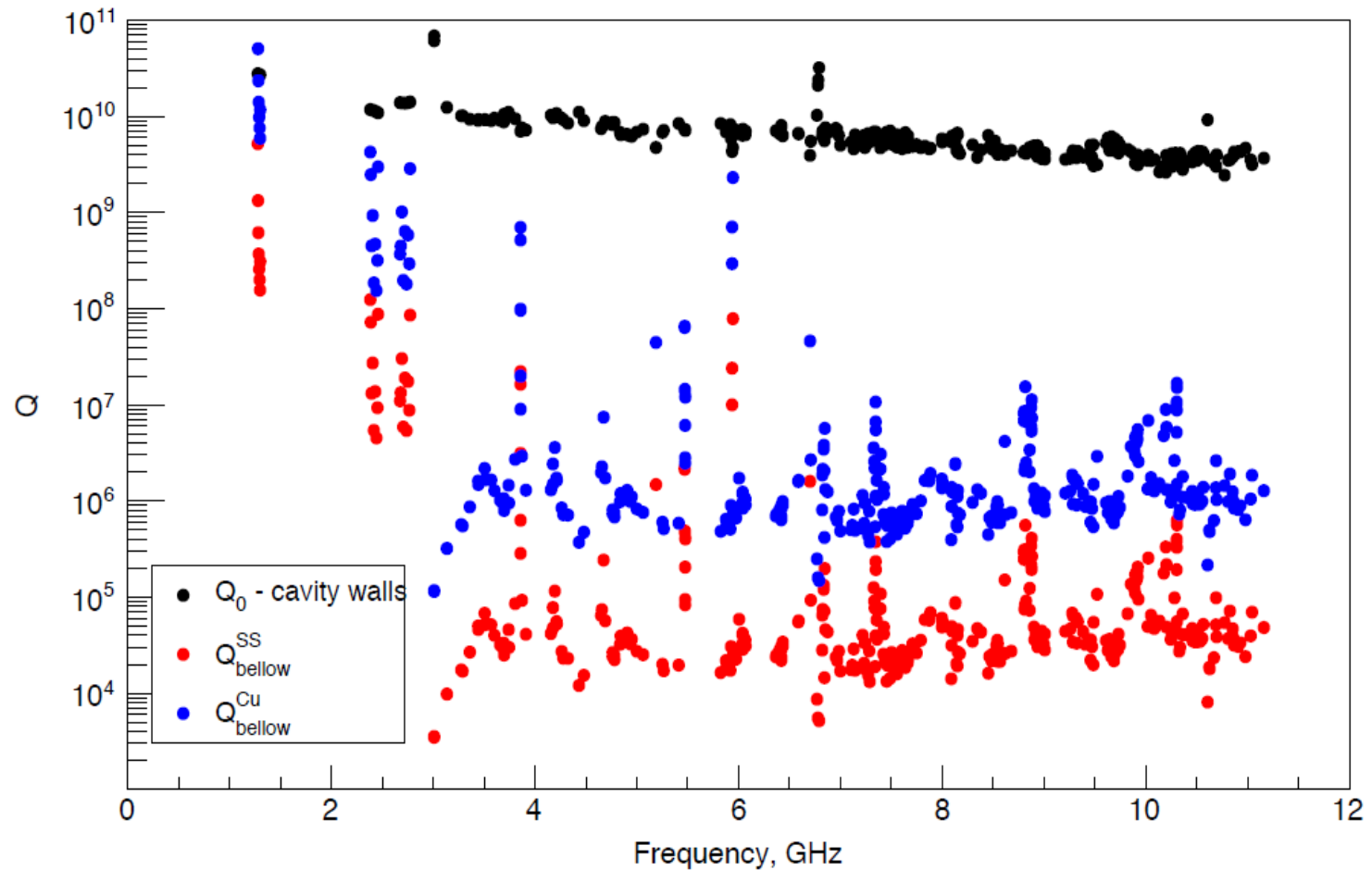
Maxodel for HOMs Trapping and Resonance Excitation in LCLS-II SC linac(1)

- RF Simulation is performed using SuperLANS to compute (R/Q) and fields corresponding to particular mode.
 - Monopole modes up to 11 GHz are computed for 1.3 GHz 9-cell cavity
 - Cut-off frequency of monopole modes is 2.94 GHz



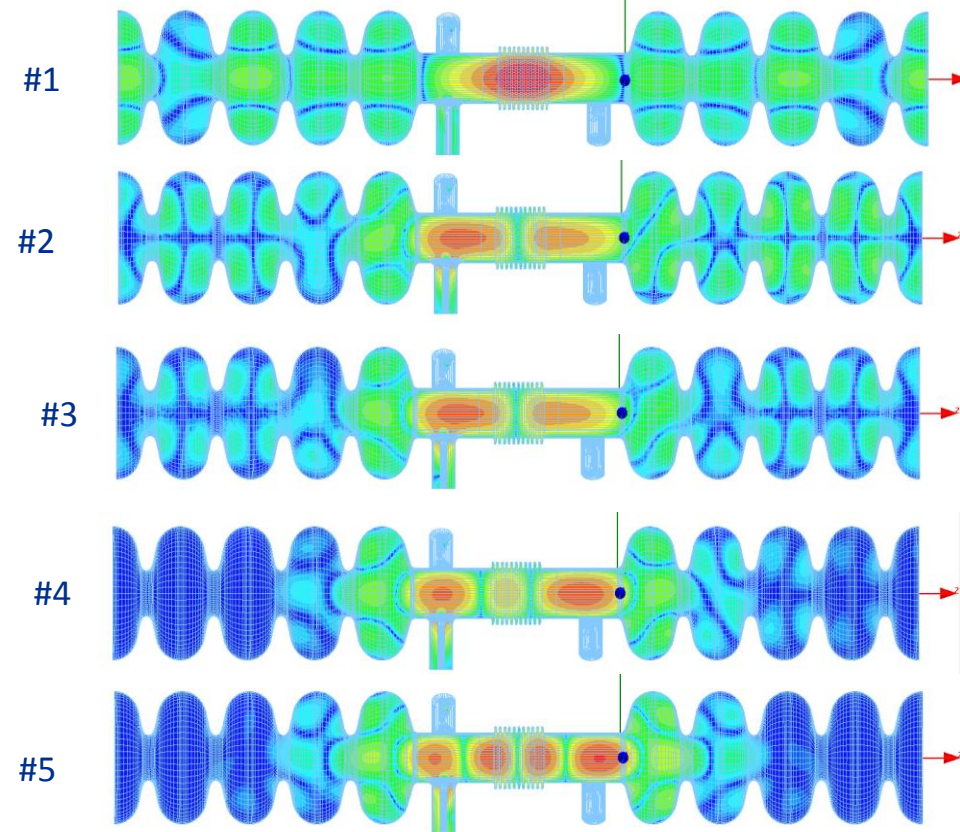
- Propagating HOMs may form standing wave in a periodic arrangement of cavities and get trapped.
- In order to find trapped modes, length of beam pipe connecting neighbouring cavities is varied.
- In order to find worst case, maximum (R/Q) is used to estimate power losses.

Quality factor of cavity and bellows for modes ~11GHz



Resonant Losses in bellows due to Monopole HOMs

Trapped Monopole HOMs in bellows (3D)



Arun Saini | Reviews of HOMs Effects in LCLS-II SC Linac

#	Freq. [GHz]	R/Q, [Ω]*	Q_{ext}	Resonant P_{loss} [mW]
1	2.737	1.5	3.2e4	4.8e-3
2	2.9682	1.6	1.8e4	2.9e-3
3	2.9683	1.5	1.7e4	2.6e-3
4	3.044	1.2	2.0e4	2.4e-4
5	3.169	2.7	8.0e3	2.2e-4

- In a worse case one can estimate $R/Q < 10 \Omega$ and $Q_{\text{ext}} < 1e5$, then the max possible coherent RF losses are:

$$P_{\text{max}} = R/Q * Q * I \approx 10 * 1e5 * 1e-7 \approx 0.1 \text{ W}$$

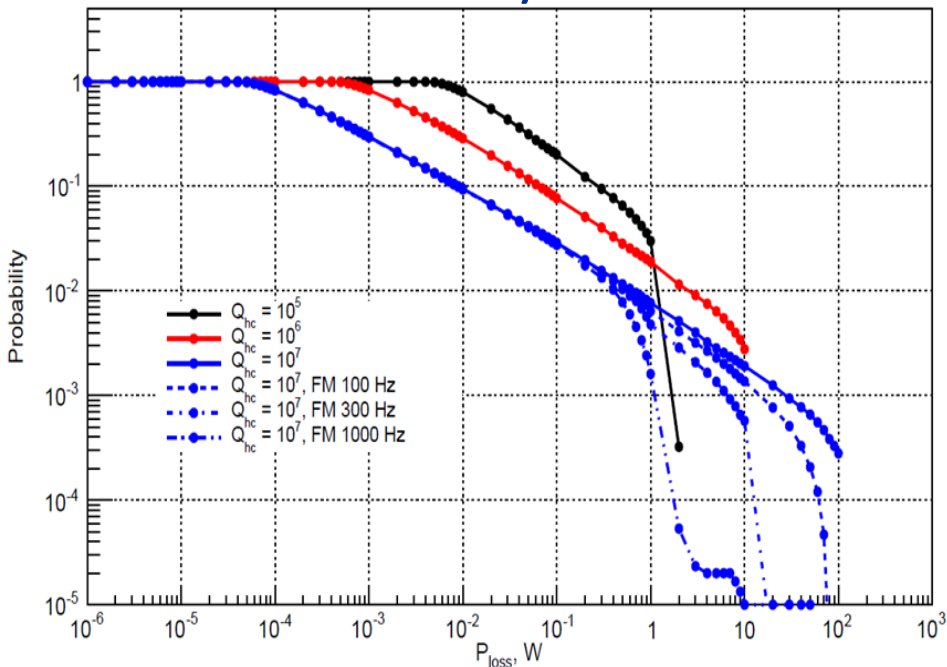
- Losses from operating mode (16MV/m)

$$P_{\text{bellow_SS}} = \omega * W / Q_{\text{bellow_SS}} \approx 0.2 \text{ W}$$

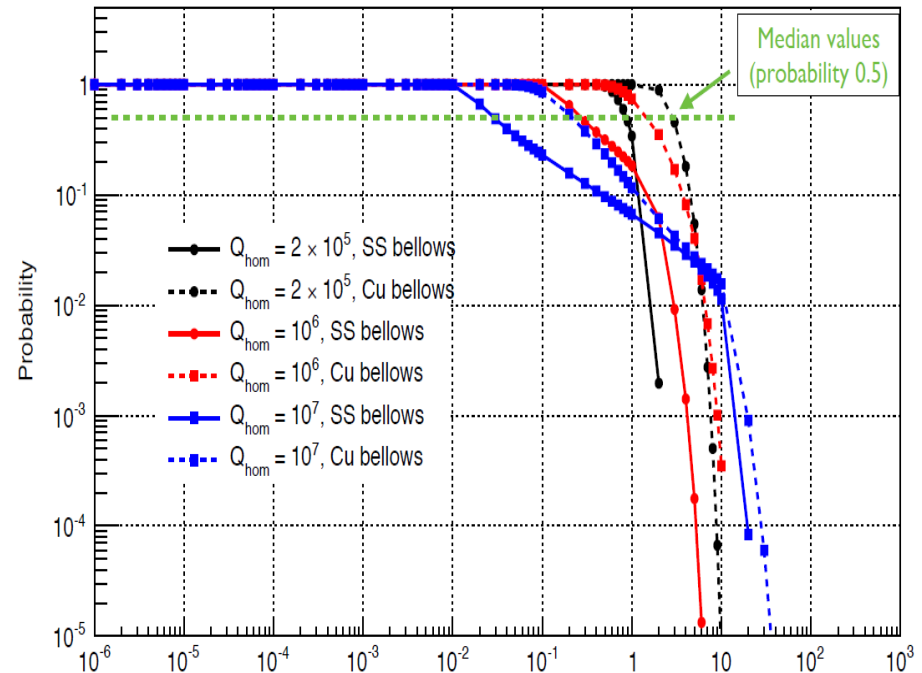
$$P_{\text{bellow_Cu}} = \omega * W / Q_{\text{bellow_Cu}} \approx 0.002 \text{ W}$$

Maximum RF power in HOM coupler

1.3 GHz Cavity



3.9 GHz Cavity



- Median $P < 5\text{W}$
- Only Non-propagating modes ($f < 2.9\text{ GHz}$)
- Random variation of HOM frequencies with 1 MHz R.M.S.