You can hide but you have to run: direct detection with vector mediators

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LHC



 $pp \rightarrow \chi \chi j$

 $\sqrt{s} = 13 \,\mathrm{TeV}$

Energy scales: LHC >> Direct Detection

Direct Detection



 $\chi \mathcal{N} \rightarrow \chi \mathcal{N}$

 $\langle E_{\rm recoil} \rangle \simeq 2 \frac{m_{\rm DM}^2 M_N}{(m_{\rm DM} + M_N)^2} v^2 \simeq 50 \,\mathrm{keV}$

Xe and $m_{\rm DM} = 100 \,{\rm GeV}$









How are LHC limits translated into the (m_{DM}, σ_{SD}) plane?

LHC bounds have to be evolved down to the direct detection scale

You have to run! (RGE)

$$\mathcal{L} = g_{\chi} A_{\mu} \,\overline{\chi} \gamma^{\mu} \gamma^{5} \chi + g_{q} A_{\mu} \,\overline{q} \gamma^{\mu} \gamma^{5} q$$



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B meson decay: $B \rightarrow D \pi$ $\mathcal{M}_{B \rightarrow D \pi} = \langle D \pi | \mathcal{L}_{SM} | B \rangle$



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RGE effects

• changing size of the effective couplings

 generating new interactions (operator mixing)

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DM-Nucleus scattering:

only through couplings to light SM degrees of freedom

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very sensitive to the details of the interactions

Goodman and Witten, PRD31 (1985)

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or light

DM

Direct detection rates can be orders of magnitude larger than the ones computed without RGE effects

 This was realized for specific interactions in: Kopp, Niro, Schwetz, Zupan, PRD80 (2009), arXiv:0907.3159; Freytsis, Ligeti, PRD83 (2011), arXiv:1012.5317
 Frandsen, Haisch, Kahlhoefer, Mertsch, Schmidt-Hoberg, JCAP1210 (2012), arXiv:1207.3971; Haisch, Kahlhoefer, JCAP1304 (2013), arXiv:1302.4454; Kopp, Michaels, Smirnov, JCAP1404 (2014) arXiv:1401.6457
 Crivellin, Haisch, PRD90 (2014), arXiv:1408.5046

 $\mathcal{L} = \mathcal{L}_{\rm SM} + \mathcal{L}_{\rm DM} + \mathcal{L}_{V} + J^{\mu}_{\rm DM} V_{\mu} + J^{\mu}_{\rm SM} V_{\mu}$

Mediator effects fully accounted for



•
$$p^2 \lesssim m_V^2$$

Contact interaction

•
$$p^2 \simeq m_V^2$$

Resonant production

•
$$p^2 \gtrsim m_V^2$$

EFT badly breaks down

$\mathcal{L} = \mathcal{L}_{\rm SM} + \mathcal{L}_{\rm DM} + \mathcal{L}_{V} + J^{\mu}_{\rm DM} V_{\mu} + J^{\mu}_{\rm SM} V_{\mu}$

Both scalar DM (complex) and fermion DM (Dirac or Majorana)

$$\mathcal{L}_{\rm DM} = \begin{cases} \left| \partial_{\mu} \phi \right|^2 - m_{\phi}^2 \left| \phi \right|^2 & \text{scalar DM} \\ \mathcal{K}_{\chi} \, \overline{\chi} \left(i \partial \!\!\!/ - m_{\chi} \right) \chi & \text{fermion DM} \end{cases}$$

$$\mathcal{K}_{\chi} = \begin{cases} 1 & \text{Dirac} \\ 1/2 & \text{Majorana} \end{cases}$$

 $\mathcal{L} = \mathcal{L}_{\rm SM} + \mathcal{L}_{\rm DM} + \mathcal{L}_{V} + J^{\mu}_{\rm DM} V_{\mu} + J^{\mu}_{\rm SM} V_{\mu}$

Spin-I massive mediator

$$\mathcal{L}_{V} = -\frac{1}{4} V^{\mu\nu} V_{\mu\nu} + \frac{1}{2} m_{V}^{2} V^{\mu} V_{\mu}$$

 $\mathcal{L} = \mathcal{L}_{\mathrm{SM}} + \mathcal{L}_{\mathrm{DM}} + \mathcal{L}_{V} + J^{\mu}_{\mathrm{DM}} V_{\mu} + J^{\mu}_{\mathrm{SM}} V_{\mu}$

Mediator coupled to spin-1 DM currents

DM

 $J_{\rm DM}^{\mu} = \begin{cases} c_{\phi} \phi^{\dagger} \overleftrightarrow{\partial}_{\mu} \phi \\ \mathcal{K}_{\nu} \left(c_{\nu V} \,\overline{\chi} \gamma^{\mu} \chi + c_{\chi A} \,\overline{\chi} \gamma^{\mu} \gamma^{5} \chi \right) \end{cases}$ scalar DM fermion DM

$\mathcal{L} = \mathcal{L}_{\mathrm{SM}} + \mathcal{L}_{\mathrm{DM}} + \mathcal{L}_{V} + J^{\mu}_{\mathrm{DM}} V_{\mu} + J^{\mu}_{\mathrm{SM}} V_{\mu}$

Mediator coupled to spin-I currents of SM fermions

15 independent $SU(2)_L \times U(1)_Y$ gauge invariant couplings to SM fermions



 $J_{\rm SM}^{\mu} = \sum_{i=1}^{3} \left[c_q^{(i)} \ \overline{q_L^i} \gamma^{\mu} q_L^i + c_u^{(i)} \ \overline{u_R^i} \gamma^{\mu} u_R^i + c_d^{(i)} \ \overline{d_R^i} \gamma^{\mu} d_R^i + c_l^{(i)} \ \overline{l_L^i} \gamma^{\mu} l_L^i + c_e^{(i)} \ \overline{e_R^i} \gamma^{\mu} e_R^i \right]$

 $\mathcal{L} = \mathcal{L}_{\rm SM} + \mathcal{L}_{\rm DM} + \mathcal{L}_{V} + J^{\mu}_{\rm DM} V_{\mu} + J^{\mu}_{\rm SM} V_{\mu}$

Apply EFT techniques:

- evaluate direct detection rates
- compare LHC with direct detection for this broad class of models







STEP II: Connecting Energy Scales

$$\frac{d c}{d \ln \mu} = \gamma_{\rm SM_{\chi}} c$$



Crivellin, FD, Procura, Phys.Rev.Lett.112 (2014), arXiv:1402.1173 FD, Procura, JHEP1504 (2015), arXiv:1411.3342



Cirelli, Del Nobile, Panci, JCAP1310 (2013), arXiv:1307.5955

runDM: code for RGE

Inclusion of RGE effects automatic

INPUT:

Effective couplings at an arbitrary energy scale

FD, Kavanagh, Panci, arXiv:1605.04917

runDM vI.0 - examples

With runDMC, It's Tricky. With runDM, it's not.

runDM is a tool for calculating the running of the couplings of Dark Matter (DM) to the Standard Model (SM) in simplified models with vector mediators. By specifying the mass of the mediator and the couplings of the mediator to SM fields at high energy, the code can be used to calculate the couplings at low energy, taking into account the mixing of all dimension-6 operators. The code can also be used to extract the operator coefficients relevant for direct detection, namely low energy couplings to up, down and strange quarks and to protons and neutrons. See the manual and arXiv:1605.04917 for more details.

Initialisation

Let's start by loading in the runDM code.

In[1]:= Get[NotebookDirectory[] <> "runDM.m"];

First, let's specify the couplings at high energy. This will be a 1-D array with 16 elements, defined in Eq. 4 of the manual. runDM comes with a number of pre-defined benchmarks, which can be accessed using setBenchmark.

[2]:= chigh = setBenchmark["UniversalAxial"];
Print["Axial-vector coupling to all SM fermions: " <> ToString[chigh]];

chigh = setBenchmark["LeptonsVector"];
Print["Vector coupling to all SM leptons: " <> ToString[chigh]];

Axial-vector coupling to all SM fermions: {-1., 1., 1., -1., 1., -1., 1., 1., -1., 1., -1., 1., 1., -1., 1., 0.} Vector coupling to all SM leptons: {0., 0., 0., 1., 1., 0., 0., 0., 1., 1., 0., 0., 0., 1., 1., 0.}

Alternatively, you can specify each coupling individually. You can use initCouplings[] to generate an empty array of couplings and then go ahead. But any array of 16 elements will do.

```
In[7]:= chigh = initCouplings[];
chigh[[3]] = 1.0;
chigh[[7]] = -1.0;
Print["User-defined couplings: " <> ToString[chigh]];
User-defined couplings: {0, 0, 1., 0, 0, 0, -1., 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

Mathematica and Python versions available at: https://github.com/bradkav/runDM/

runDM: code for RGE

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FD, Kavanagh, Panci, arXiv:1605.04917

OUTPUT I:

RG evolved couplings at a second arbitrary energy scale (useful for future ID studies)

runCouplings: running between arbitrary scales

From these high energy couplings (defined at some energy E_1), you can obtain the couplings at a different energy scale E_2 by using runCouplings[c, E_1, E_2].

The input coupling vector c should always be the list of high energy couplings to fully gauge-invariant operators above the EW scale (see Eq. 4 of the manual) - *even if* E_1 *is below* m_Z . The output is either a list of coefficients for the same operators - if E_2 is above m_Z – or the list of coefficients for the low energy operators below the EW scale (Eq. 6 of the manual) - if E_2 is below m_Z . Don't worry, runDM takes care of the relative values of E_1 and E_2 .

runDM-examples.nb

```
In[11]:=
    (*Run from 1 TeV to 10 GeV*)
    E<sub>1</sub> = 1000; E<sub>2</sub> = 10;
    clow = runCouplings[chigh, E<sub>1</sub>, E<sub>2</sub>]
Out[12]= {0.00747328, 0.496264, -0.492527, -0.00373596,
```

```
\begin{array}{l} -0.00373619, -0.0112106, -0.0112106, -0.0112106, \\ 1.36429 \times 10^{-6}, 0.4999999, -0.4999999, -1.36429 \times 10^{-6}, \\ -1.12974 \times 10^{-6}, -1.36429 \times 10^{-6}, -1.36429 \times 10^{-6}, -1.36129 \times 10^{-6} \end{array}
```

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runDM: code for RGE

Inclusion of RGE effects automatic

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FD, Kavanagh, Panci, arXiv:1605.04917

OUTPUT II:

RG evolved couplings for direct detection DDCouplingsQuarks: calculating low-energy DM-quark couplings

If we're only interested in direct detection experiments, we can use the function DDCouplingsQuarks[c, E_1] to extract the couplings to light quarks. In this case, the code evolves the couplings from energy E_1 , down to the nuclear energy scale ~ 1 GeV. The output is an array with 5 elements, the vector and axial-vector couplings to light quarks: $c_q = (c_V^{(u)}, c_V^{(d)}, c_A^{(u)}, c_A^{(d)}, c_A^{(s)})$. Let's calculate them and print them out.

₩ runDM-examples.nb

```
In[13]:= (*Run from 10 TeV to 1 GeV*)
E_{1} = 10000;
cq = DDCouplingsQuarks[chigh, E_{1}];
clabels = \{"c_{v}(u)", "c_{v}(d)", "c_{A}(u)", "c_{A}(d)", "c_{A}(s)"\};
Grid[Transpose[{clabels, cq}]]
c_{v}(u) = 0.0145847
c_{v}(d) = 0.492712
Out[16]= c_{A}(u) = 8.56843 \times 10^{-6}
c_{A}(s) = -8.56843 \times 10^{-6}
```

Mathematica and Python versions available at: https://github.com/bradkav/runDM/

RGE Handbook

Interested in the RGE-induced currents with light quarks



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Results I: quarks vector

Flavor universal couplings to quark vector currents

$$\mathcal{L}_{\rm EFT} = -\frac{1}{m_V^2} J_{\rm DM\,\mu} \sum_{i=1}^3 \left[\overline{u^i} \gamma^\mu u^i + \overline{d^i} \gamma^\mu d^i \right]$$

Results I: quarks vector

 $\mathcal{L}_{\rm EFT} = -\frac{1}{m_V^2} J_{\rm DM\,\mu} \sum_{i=1}^{0} \left[\overline{u^i} \gamma^{\mu} u^i + \overline{d^i} \gamma^{\mu} d^i \right]$

Flavor universal couplings to quark vector currents



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RGE: O(1%) correction to EFT couplings

Very strong bounds, meaningful results also for loop-induced rates

Flavor universal couplings to quark axial currents

$$\mathcal{L}_{\rm EFT} = -\frac{1}{m_V^2} J_{\rm DM\,\mu} \sum_{i=1}^3 \left[\overline{u^i} \gamma^\mu \gamma^5 u^i + \overline{d^i} \gamma^\mu \gamma^5 d^i \right]$$

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Flavor universal couplings

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Results III: other cases



Comparison with LHC

LHC limits on mediator mass translated into limits on direct detection cross section



LUX, arXiv:1602.03489 and PICO-2L, arXiv:1601.03729 ATLAS, arXiv:1604.07773 (mono-jet) and arXiv:1604.01306 (mono-photon)

Impact of the running

$$\sigma_{\rm SD}^{N} = \frac{3\mu_N^2}{\pi} \frac{\left(c_{\chi A} \mathcal{C}_A^{(N)}\right)^2}{m_V^4}$$

$$\mathcal{C}_A^{(N)} \simeq g_q \left[\sum_{q=u,d,s} \Delta_q^{(N)}\right] + g_q \frac{3\alpha_t}{2\pi} \left(\Delta_d^{(N)} + \Delta_s^{(N)} - \Delta_u^{(N)}\right) \ln(m_V/m_Z)$$
Tree-level
Loop-induced

Mono-jet Searches



LUX, arXiv:1602.03489 and PICO-2L, arXiv:1601.03729 ATLAS, arXiv:1604.07773 (mono-jet) and arXiv:1604.01306 (mono-photon)

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How well can be constrained by collider and direct detection?

 $\overline{\chi}\gamma^{\mu}\chi \ \overline{q}\gamma_{\mu}q$

 $\overline{\chi}\gamma^{\mu}\gamma^{5}\chi \ \overline{q}\gamma_{\mu}\gamma^{5}q$

 $\overline{\chi}\gamma^{\mu}\chi \ \overline{q}\gamma_{\mu}\gamma^{5}q$

 $\overline{\chi}\gamma^{\mu}\gamma^{5}\chi \ \overline{q}\gamma_{\mu}q$

How well can be constrained by collider and direct detection?

 $\overline{\chi}\gamma^{\mu}\chi \ \overline{q}\gamma_{\mu}q$

~ same as the others

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~ same as the others

How well can be constrained by collider and direct detection?

Standard Lore

 $\overline{\chi}\gamma^{\mu}\chi \ \overline{q}\gamma_{\mu}q$

~ same as the others Spin-Independent (SI), no suppression

 $\overline{\chi}\gamma^{\mu}\gamma^{5}\chi \ \overline{q}\gamma_{\mu}\gamma^{5}q$

~ same as the others Spin-Dependent (SD), no suppression

 $\overline{\chi}\gamma^{\mu}\chi\ \overline{q}\gamma_{\mu}\gamma^{5}q$

~ same as the others SD with v

 $\overline{\chi}\gamma^{\mu}\gamma^{5}\chi \ \overline{q}\gamma_{\mu}q$

~ same as the others SI with v

How well can be constrained by collider and direct detection?

Standard Lore

 $\overline{\chi}\gamma^{\mu}\chi \ \overline{q}\gamma_{\mu}q$

~ same as the others Spin-Independent (SI), no suppression

 $\overline{\chi}\gamma^{\mu}\gamma^{5}\chi \ \overline{q}\gamma_{\mu}\gamma^{5}q$

~ same as the others Spin-Dependent (SD), no suppression (large corrections)

 $\overline{\chi}\gamma^{\mu}\chi \ \overline{q}\gamma_{\mu}\gamma^{5}q$

~ same as the others Spin-Independent (SI) at one-loop But if you run... (and you have to run!)

Direct detection rates and comparison with LHC: not always straightforward



Still need to quantify RGE effects for other simplified models

Direct detection rates and comparison with LHC: not always straightforward



