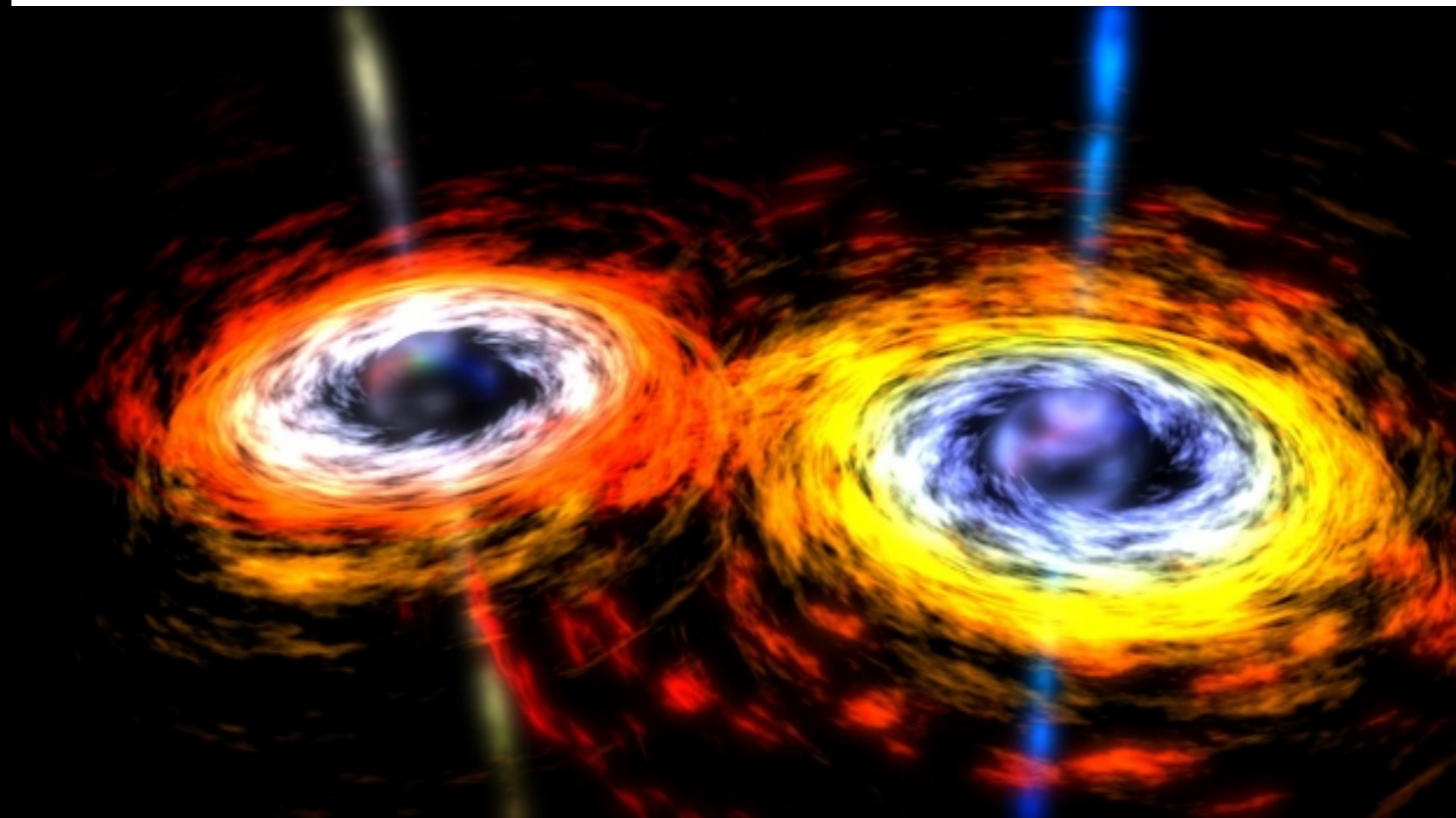
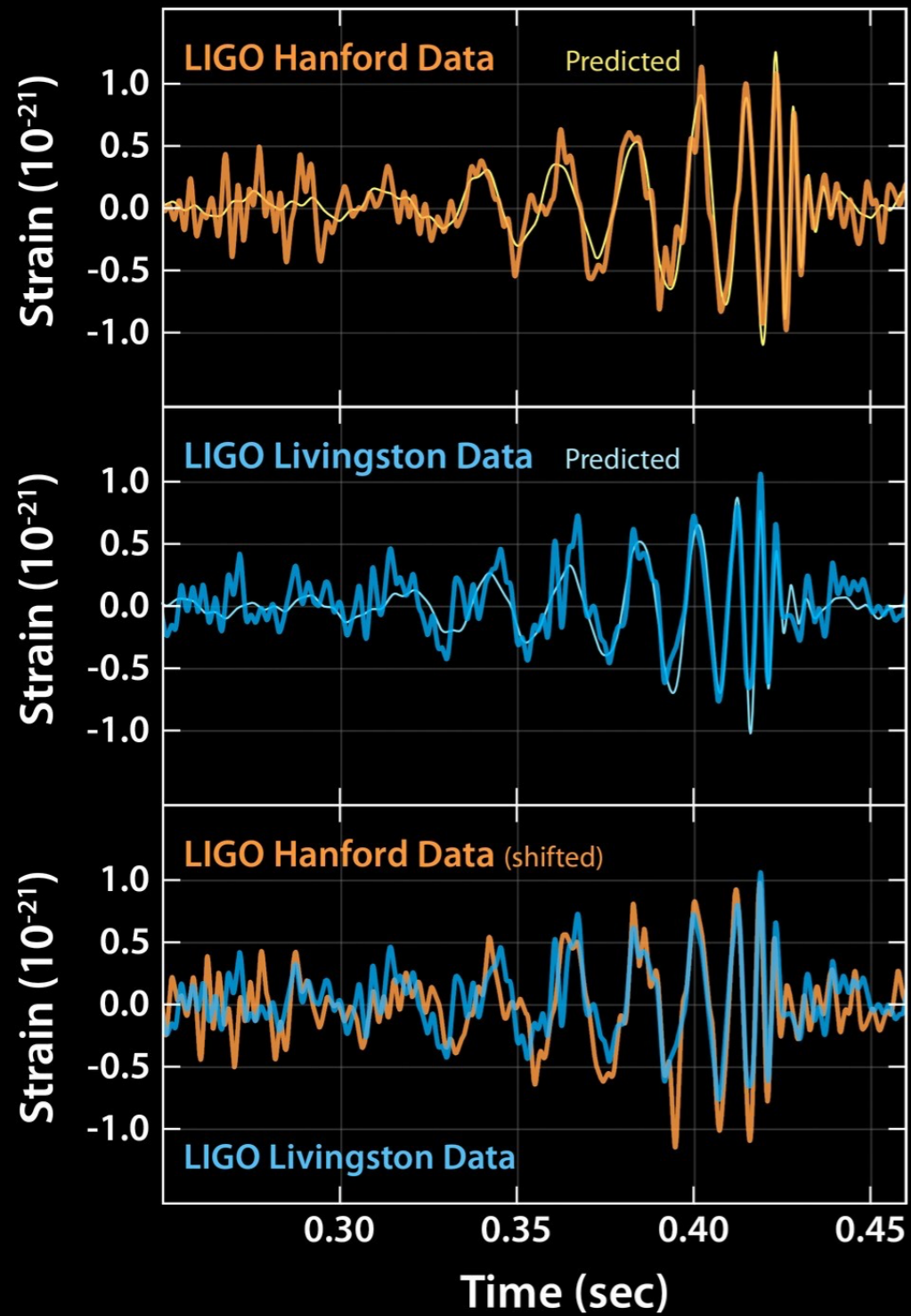
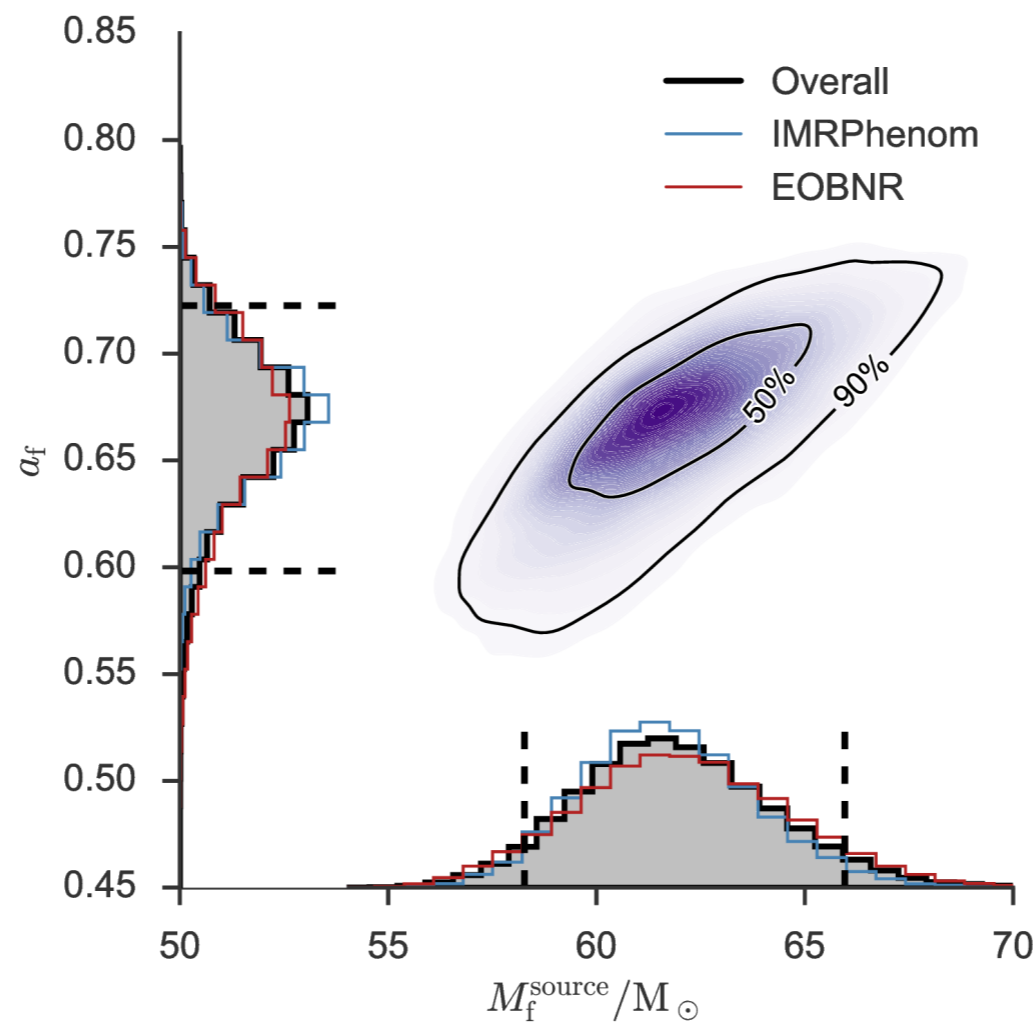


September 14, 2015



Properties of GW150914



Effective inspiral spin parameter χ_{eff}

Dimensionless primary spin magnitude a_1

Dimensionless secondary spin magnitude a_2

Final spin a_f

$$-0.09^{+0.19}_{-0.17}$$

$$0.32^{+0.45}_{-0.28}$$

$$0.57^{+0.40}_{-0.51}$$

$$0.67^{+0.06}_{-0.08}$$

$$-0.03^{+0.14}_{-0.15}$$

$$0.31^{+0.51}_{-0.27}$$

$$0.39^{+0.50}_{-0.34}$$

$$0.67^{+0.06}_{-0.06}$$

$$-0.06^{+0.17 \pm 0.01}_{-0.18 \pm 0.07}$$

$$0.31^{+0.48 \pm 0.04}_{-0.28 \pm 0.01}$$

$$0.46^{+0.48 \pm 0.07}_{-0.42 \pm 0.01}$$

$$0.67^{+0.06 \pm 0.00}_{-0.07 \pm 0.03}$$

New Era

- New telescope
- The violent Universe
 - Black Hole mergers, phase transitions, inflation
- New precision science
 - ~one merger per day — a lot of data per merger
- BSM physics?

New spectroscopy

Black Holes as Nature's Detectors



$$(15 \text{ km}) \times (M / 10 M_{\odot})$$

Range of astrophysical Black Holes:
few M_{\odot} to $10^{10} M_{\odot}$

Sensitive to boson masses 10^{-20} - 10^{-10} eV

Focus on stellar black holes

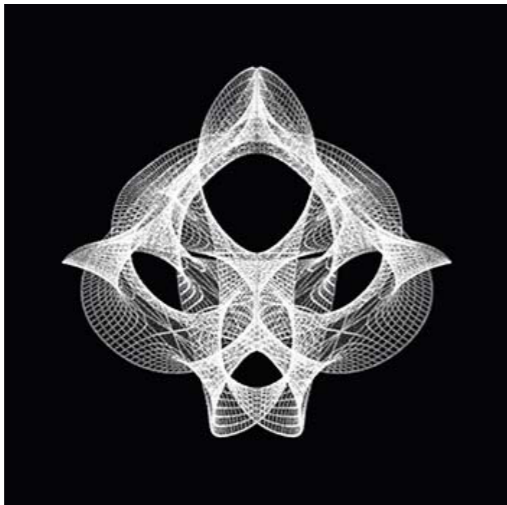
Why is this interesting?

- The Strong CP problem and the QCD axion

$$\mu_a \sim 6 \times 10^{-11} \text{ eV} \frac{10^{17} \text{ GeV}}{f_a} \sim (3 \text{ km})^{-1} \frac{10^{17} \text{ GeV}}{f_a}$$

- The String Axiverse

Arvanitaki, SD, Dubovsky, Kaloper, March-Russell (2009)



- Superradiance probes any boson in the right mass range

BLACK HOLES AND THE QCD AXION AT ADVANCED LIGO

Savas Dimopoulos
Stanford University

with

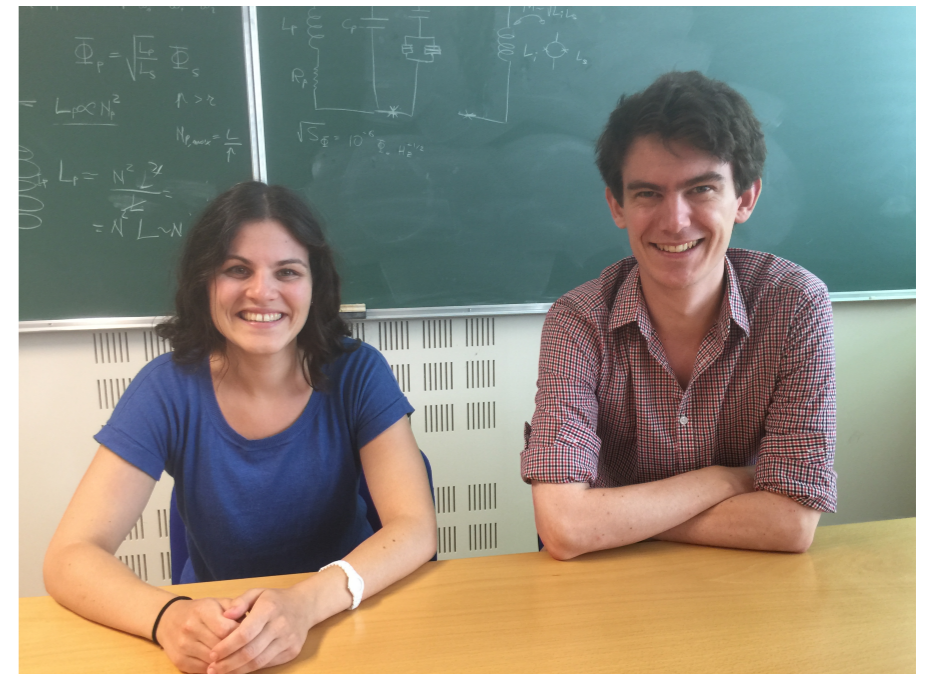
Arvanitaki, Dubovsky, Kaloper, March-Russell (2009)

Baryakhtar, Lasenby, Arvanitaki, Dubovsky (2016)

also based on

Arvanitaki, Dubovsky (2010)

Arvanitaki, Baryakhtar, X. Huang (2014)

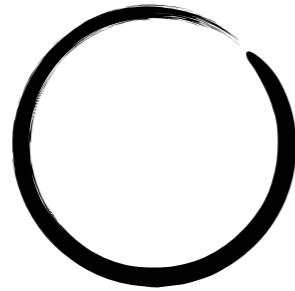


Super-Radiance Cartoon



Super-radiant scattering of a massive object

Super-Radiance Cartoon



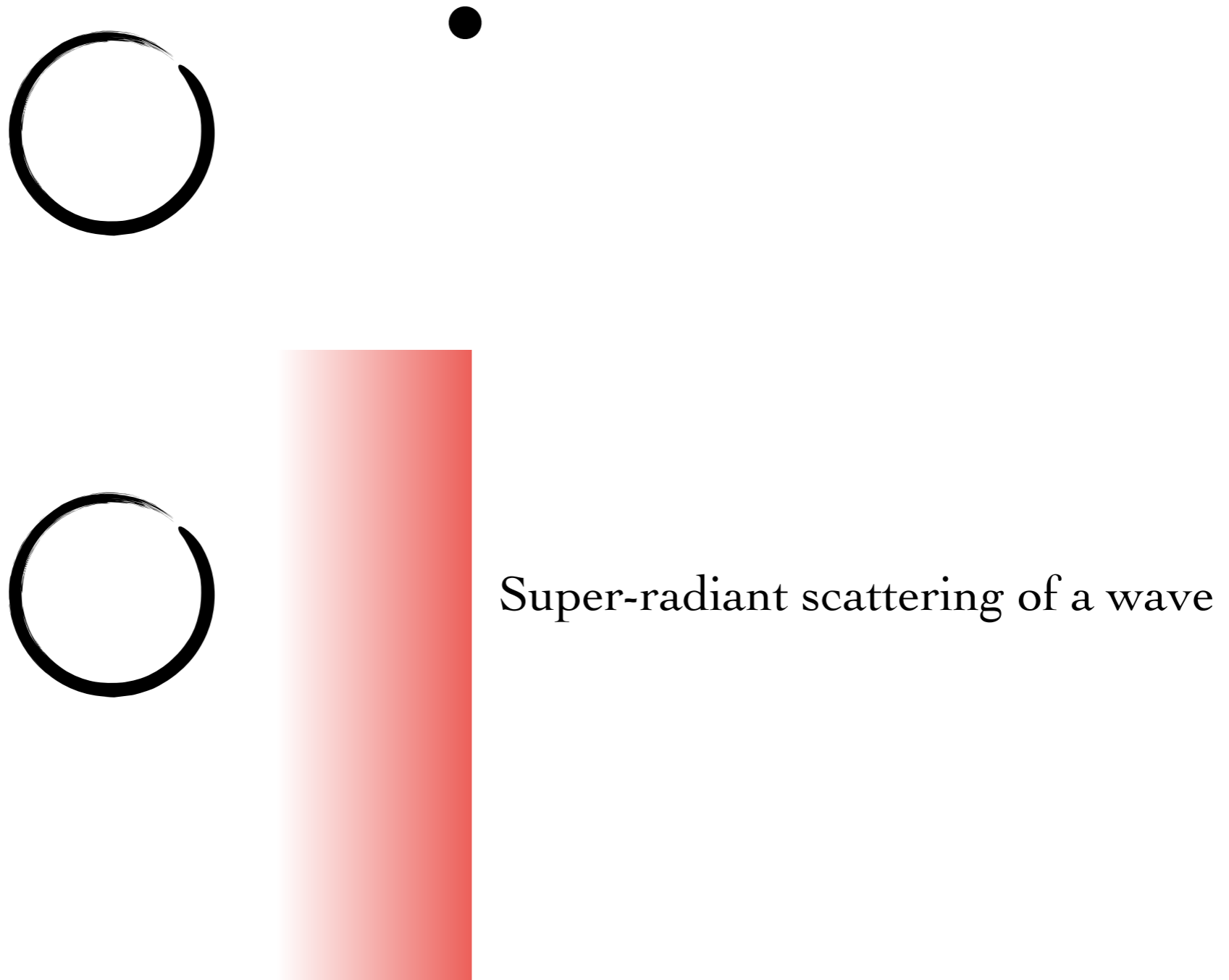
Super-radiant scattering of a massive object

Super-Radiance Cartoon



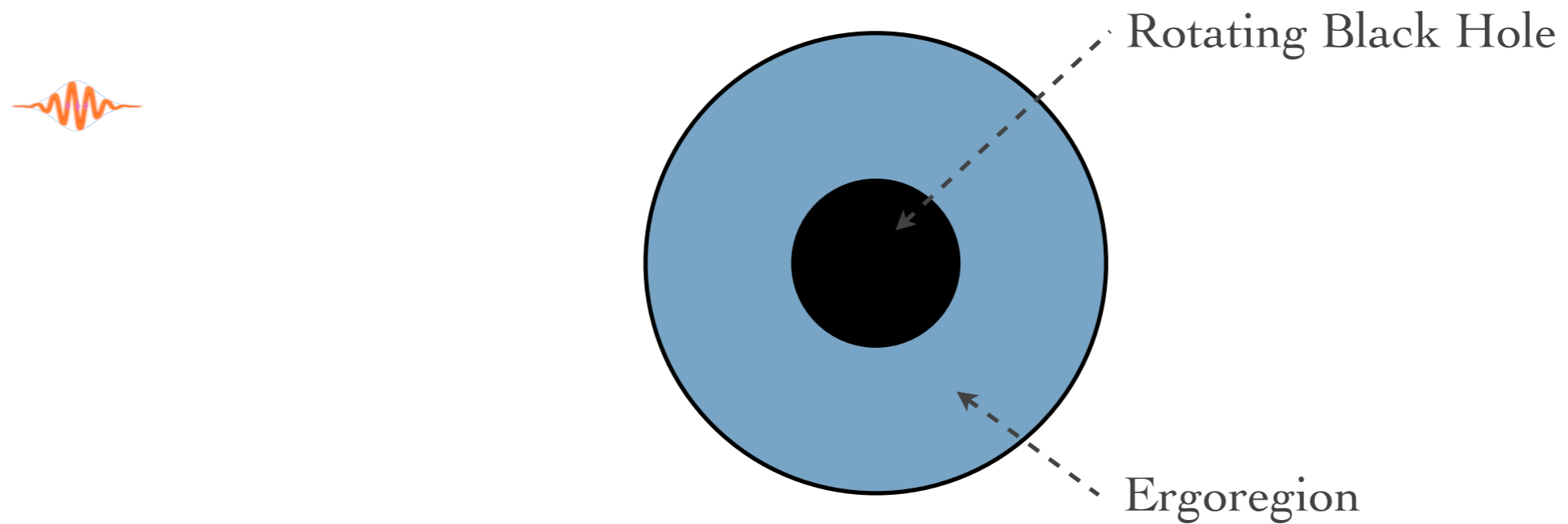
Super-radiant scattering of a wave

Super-Radiance Cartoon



Black Hole Superradiance

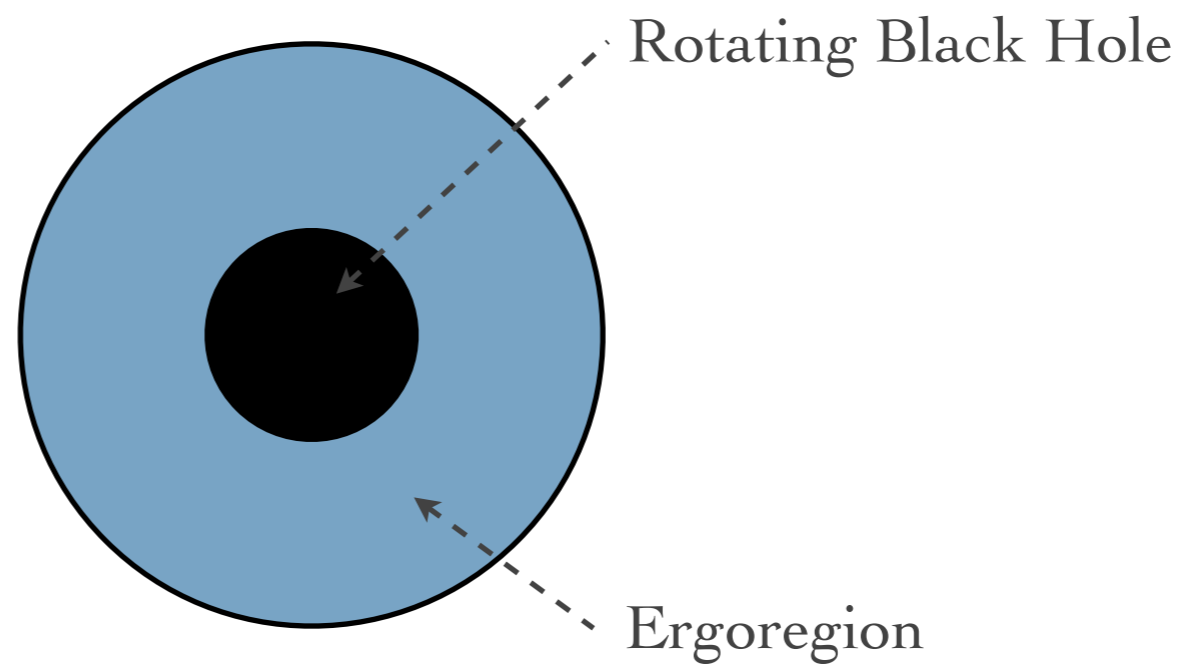
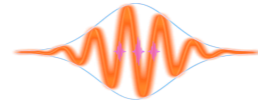
Penrose Process



Ergoregion: Region where even light has to be rotating

Black Hole Superradiance

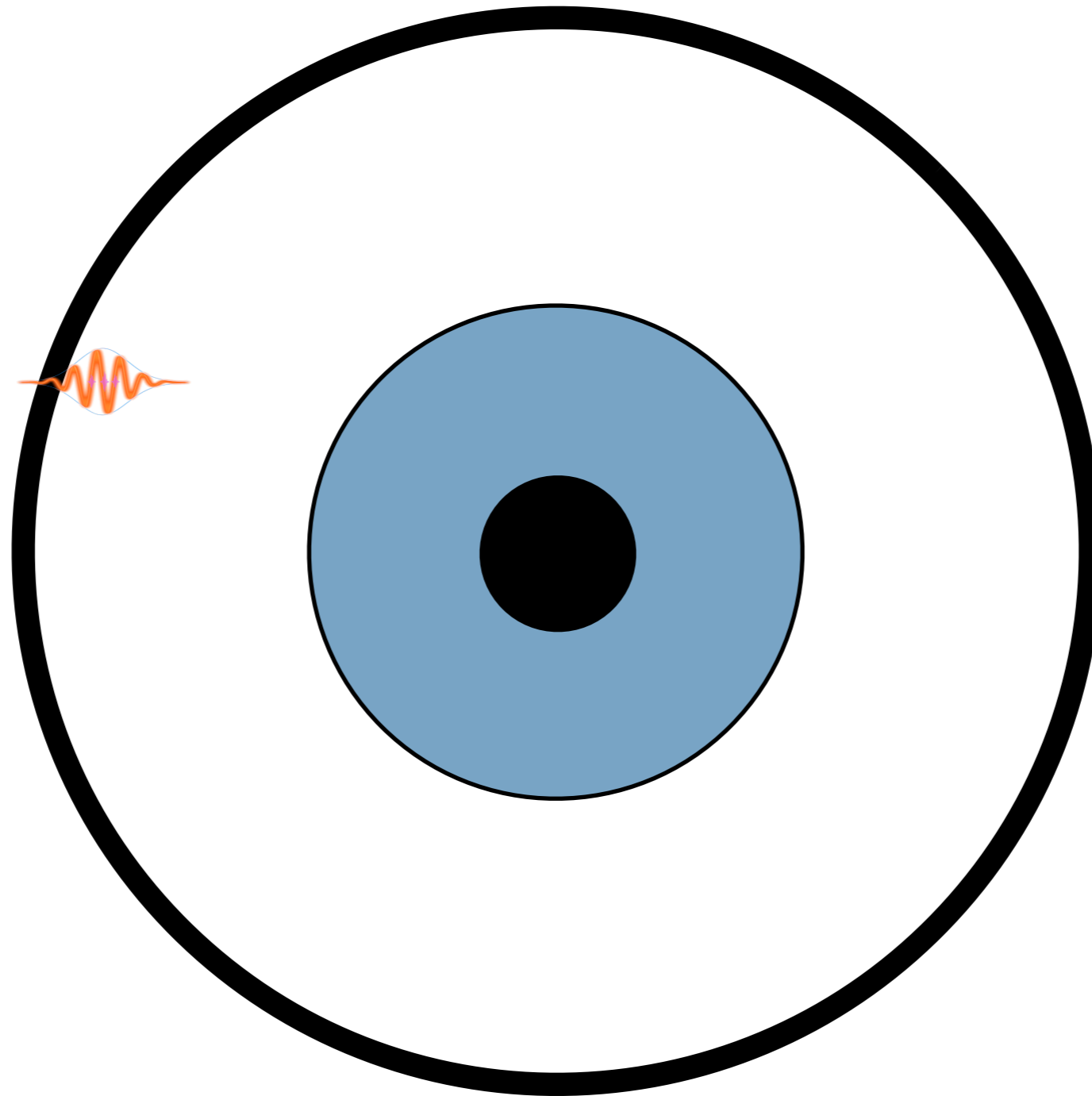
Penrose Process



Extracts angular momentum and mass from a spinning black hole

Black Hole Bomb

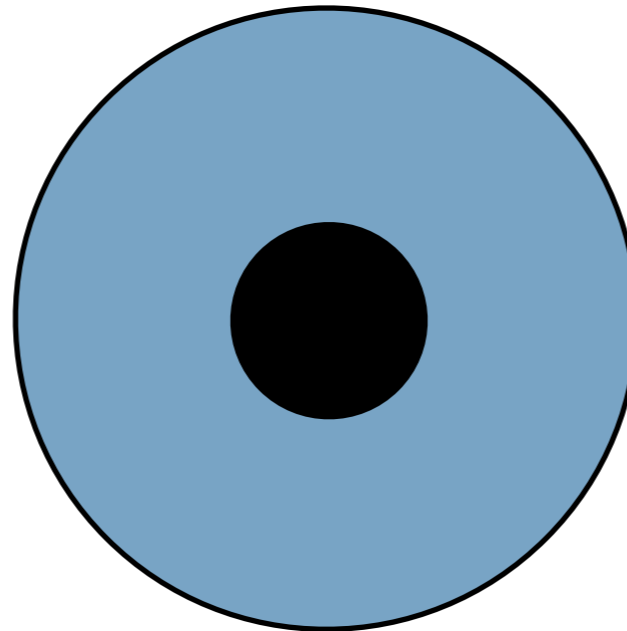
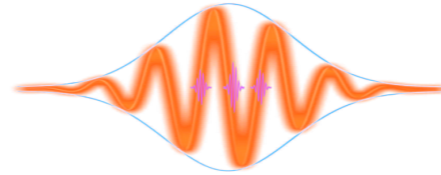
Press & Teukolsky 1972



Photons reflected back and forth from the black hole
and through the ergoregion

Black Hole Bomb

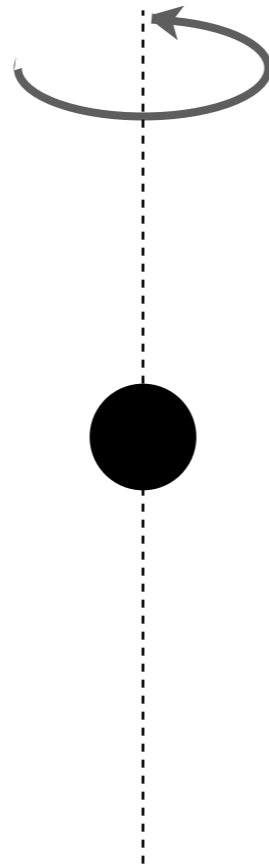
Press & Teukolsky 1972



Photons reflected back and forth from the black hole
and through the ergoregion

Superradiance for a massive boson

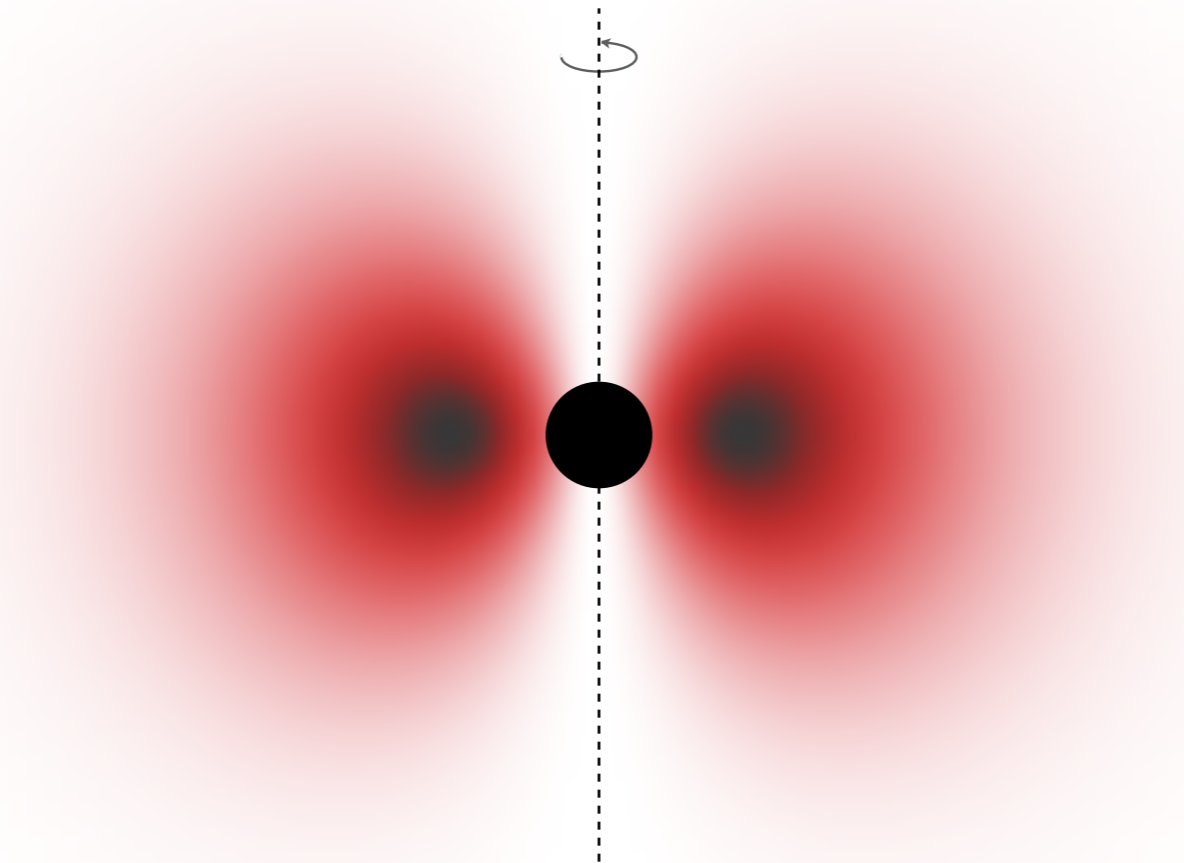
Damour et al; Zouros & Eardley;
Detweiler; Gaina (Early 70s)



Particle Compton Wavelength comparable to the size of the Black Hole

Superradiance for a massive boson

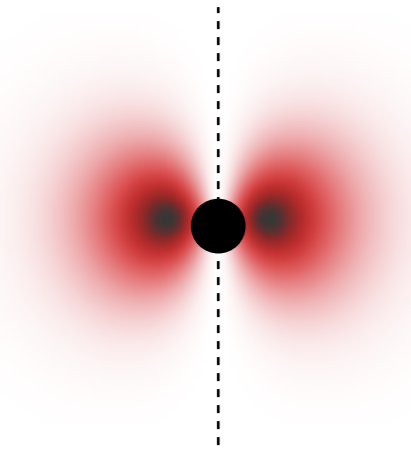
Damour et al; Zouros & Eardley;
Detweiler; Gaina (Early 70s)



Particle Compton Wavelength comparable to the size of the Black Hole

Gravitational Atom in the Sky

The gravitational Hydrogen Atom



Fine-structure constant:

$$\alpha = G_{\text{N}} M_{\text{BH}} \mu_a = R_g \mu_a$$

Principal (n), orbital (l), and
magnetic (m) quantum number for each level

$$E_{\text{binding}} = -\frac{\alpha^2 \mu_a}{2n^2}$$

Main differences from hydrogen atom:

Levels occupied by bosons - occupation number $> 10^{77}$

In-going Boundary Condition at Horizon

Key Points About Superradiance

- For light axions (weak coupling) equation identical to Hydrogen atom
- Boundary conditions different:
 - Regular at the origin \longrightarrow Ingoing (BH is absorber)
 - Hermitian \longrightarrow Non-hermitian

Superradiance Parametrics

Superradiance Condition

$$\omega_{\text{axion}} < m \Omega_+$$

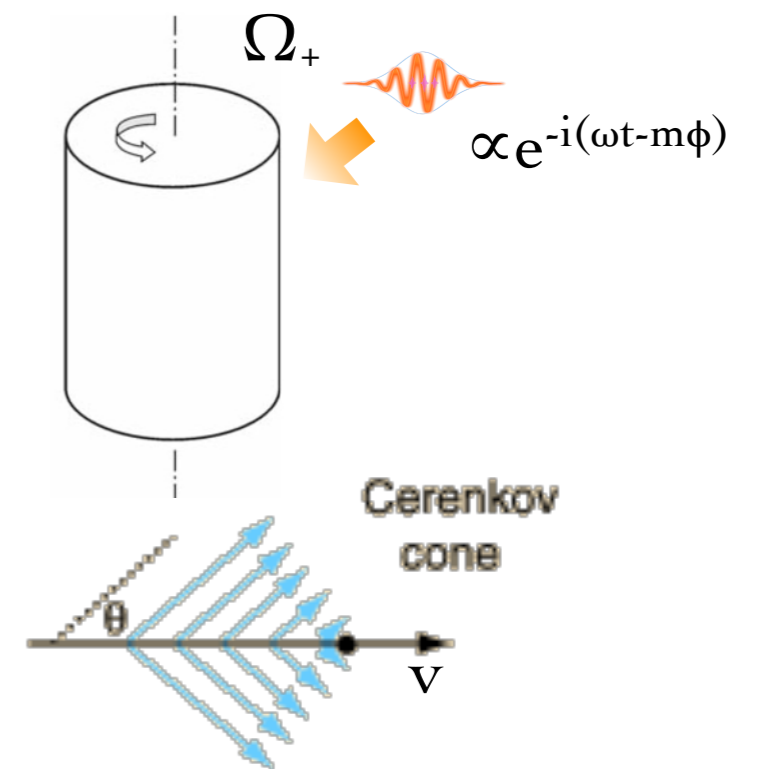
m : magnetic quantum number

Ω_+ : angular velocity of the BH

Universal Phenomenon:

Superluminal rotational motion of a conducting cylinder

Superluminal linear motion - Cherenkov radiation $1/n(\omega) < v$



Condition can be extracted from requiring that $dA_{\text{BH}} > 0$

Superradiance Parametrics

Superradiance Rate

$$\tau_{sr} \sim 0.6 \times 10^7 R_g \text{ for } R_g \mu_a \sim 0.4$$

As short as 100 sec vs $\tau_{\text{accretion}} \sim 10^8$ years

When $R_g \mu_a \gg 1$,

$$\tau_{sr} = 10^7 e^{3.7(\mu_a R_g)} R_g$$

When $R_g \mu_a \ll 1$

$$\tau_{sr} = \left(\frac{24}{a}\right) (\mu_a R_g)^{-9} R_g$$



Evolution of Superradiance for an Axion

Superradiance instability

Self interactions

Evolution of Superradiance for an Axion

Superradiance instability

Self interactions

Gravity wave transitions of axions between levels



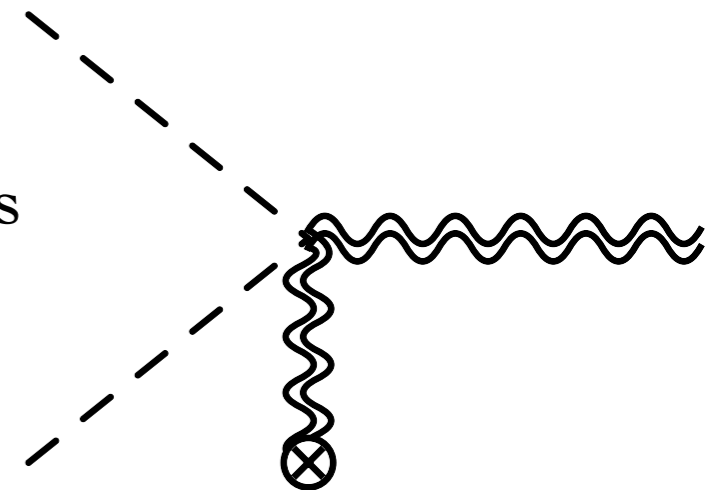
Evolution of Superradiance for an Axion

Superradiance instability

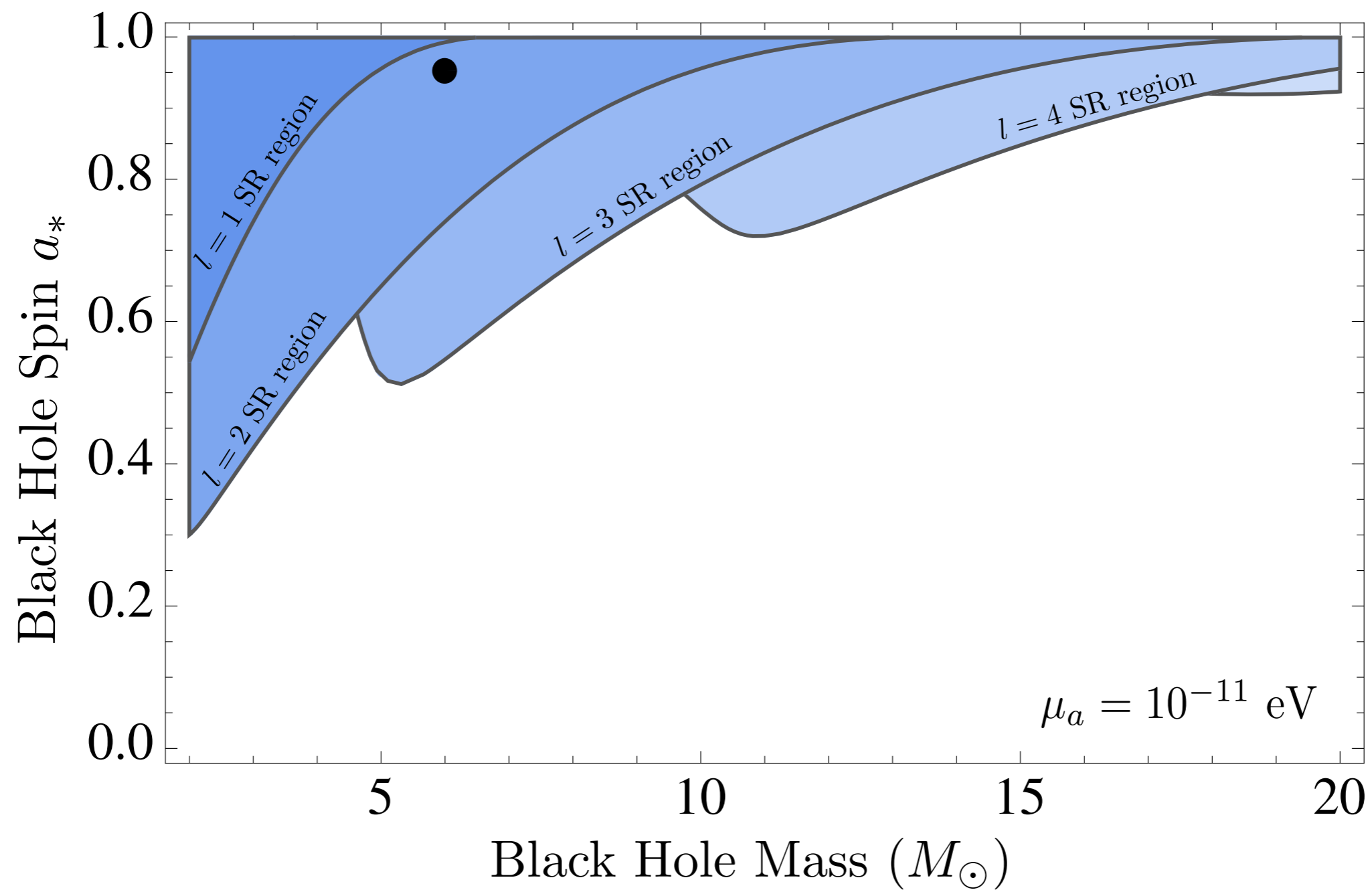
Self interactions

Gravity wave transitions of axions between levels

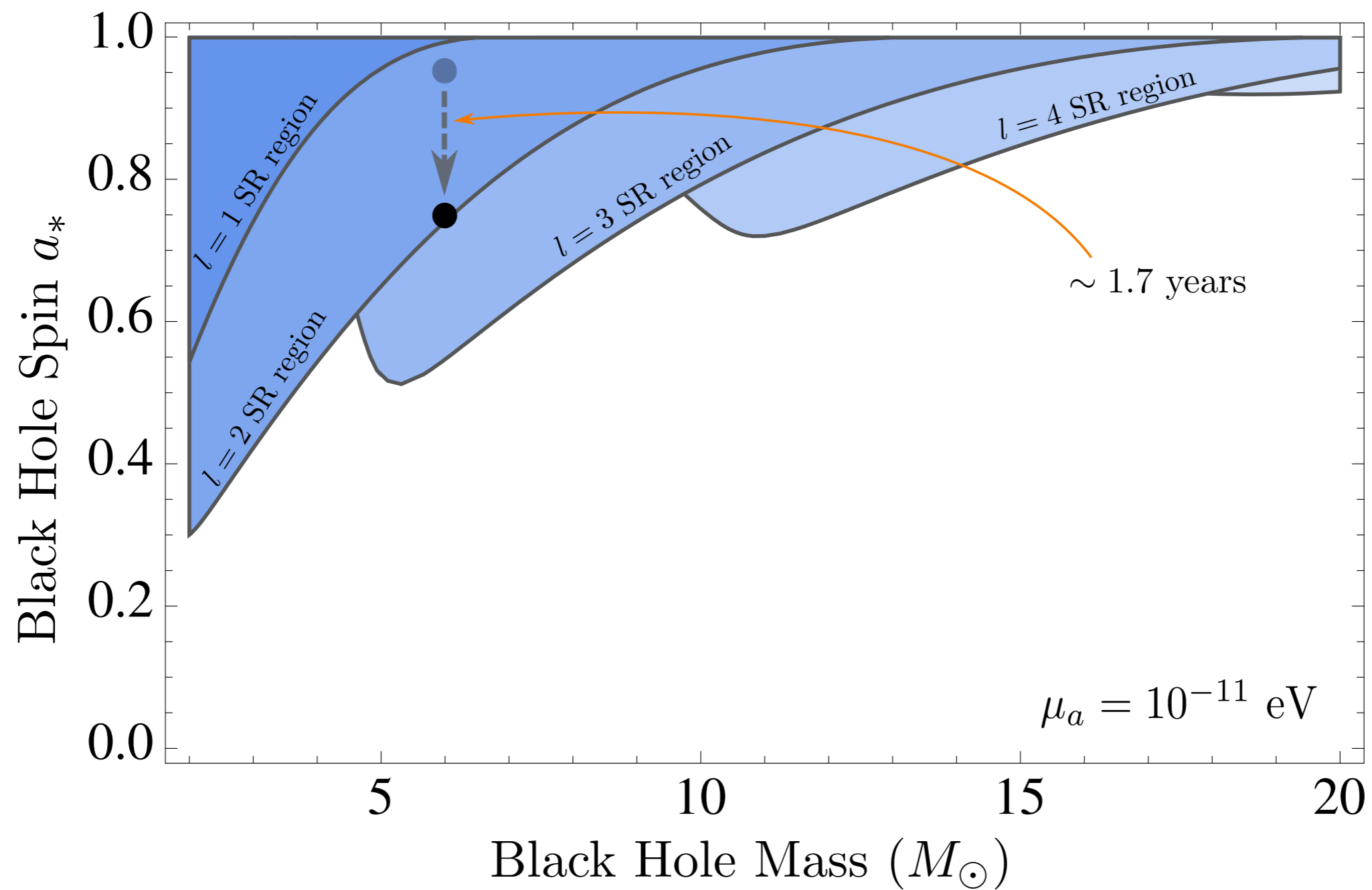
Gravity wave emission through axion annihilations



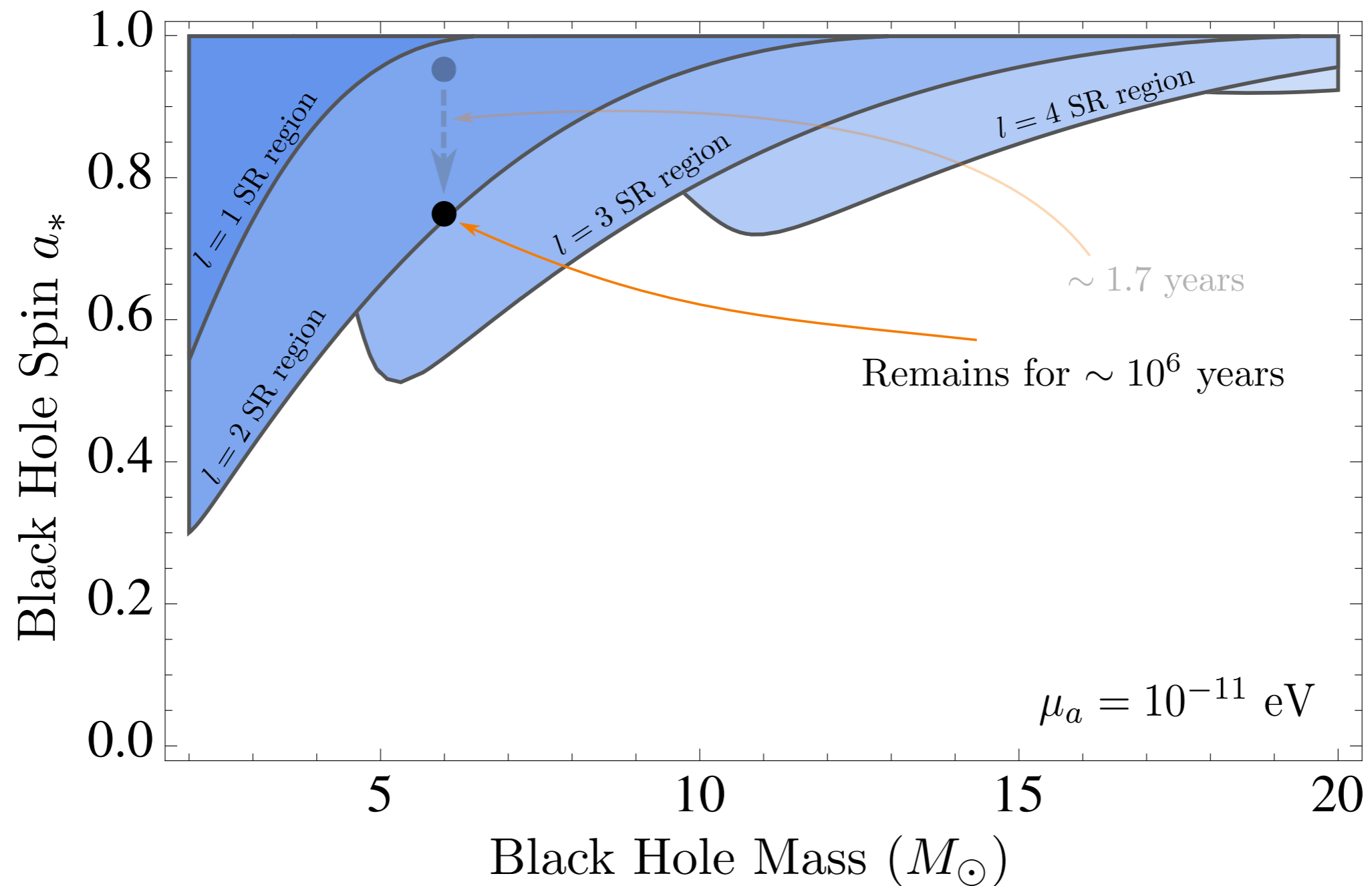
Superradiance Evolution



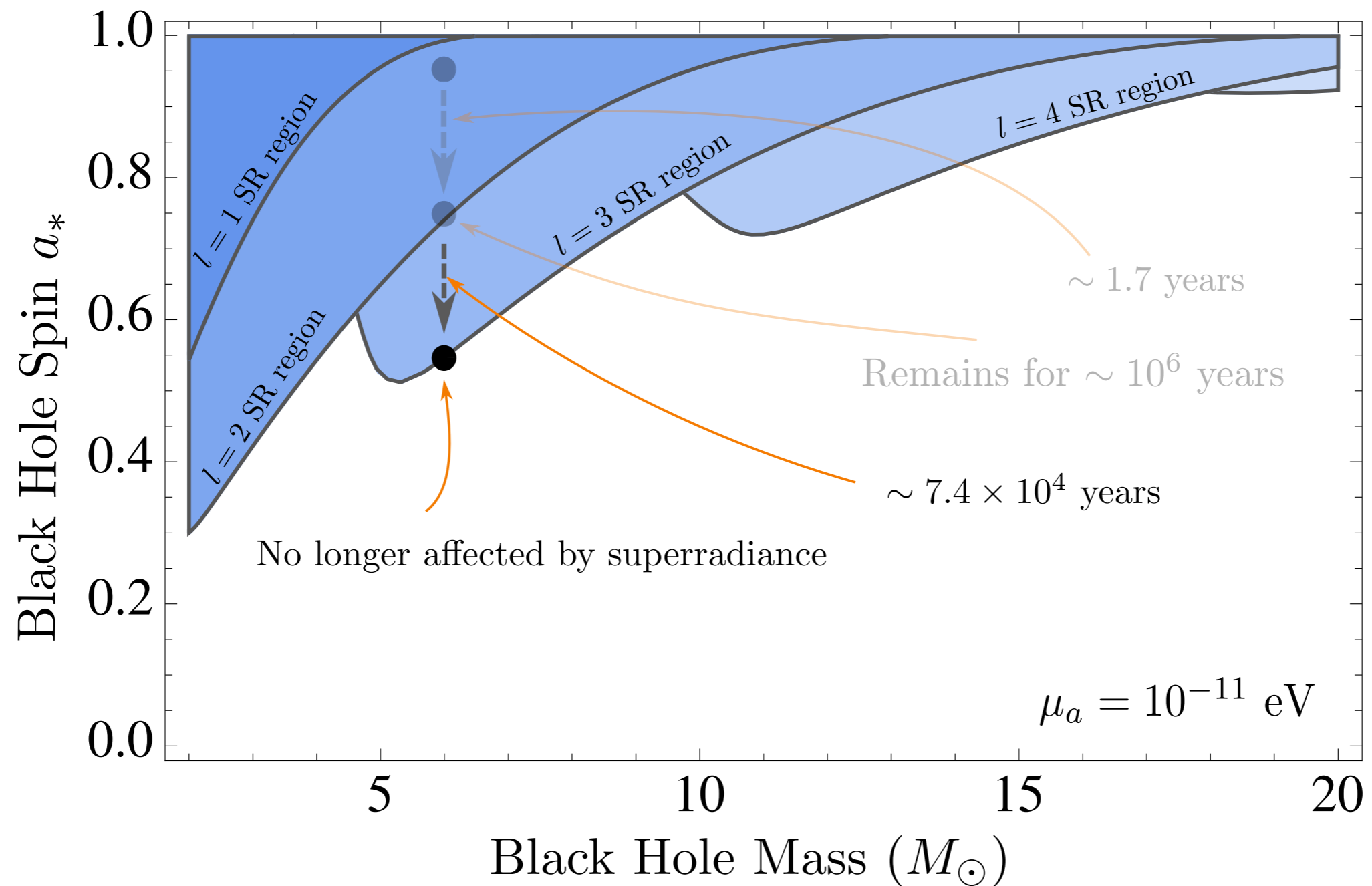
Superradiance Evolution



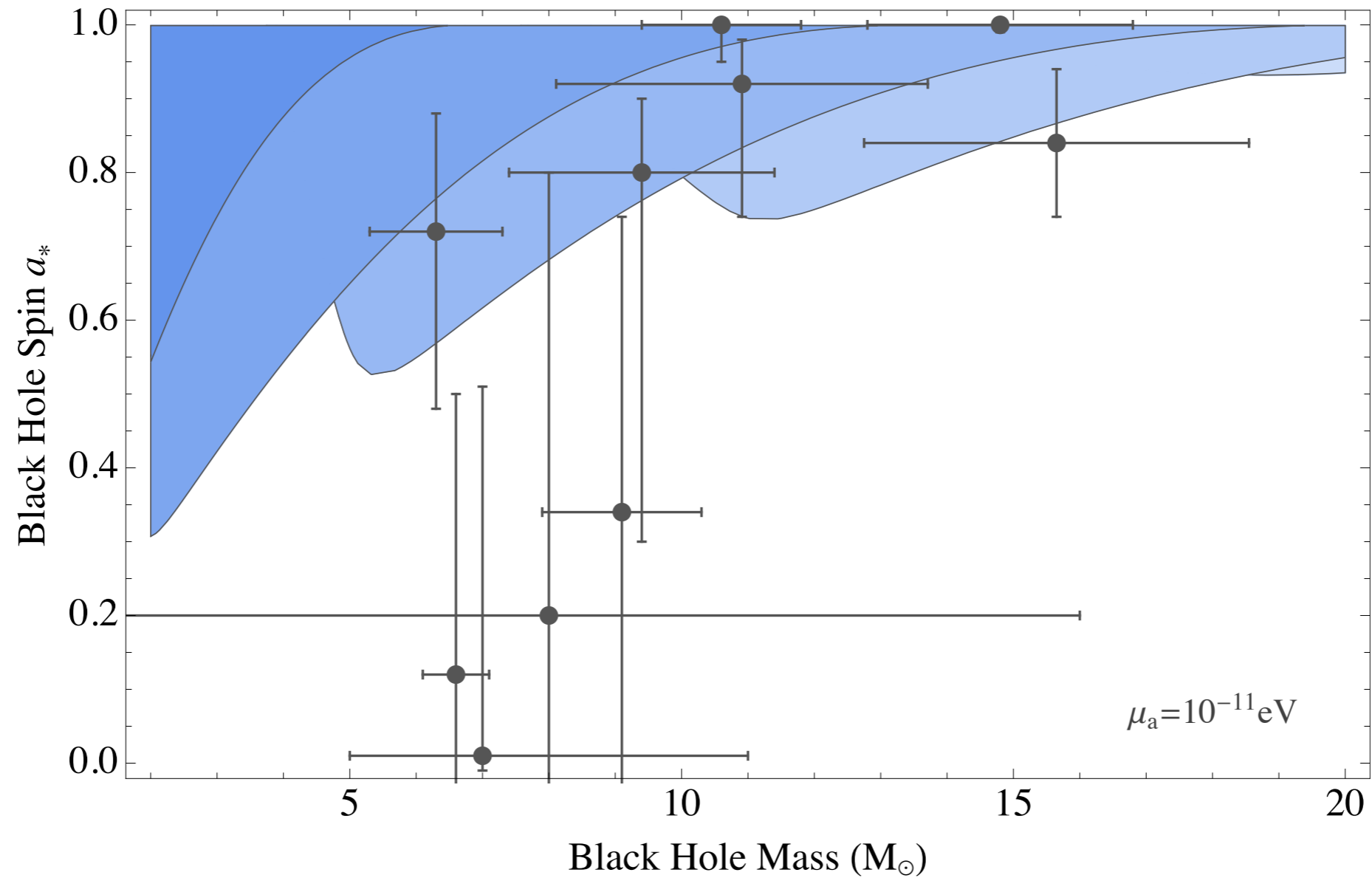
Superradiance Evolution



Superradiance Evolution



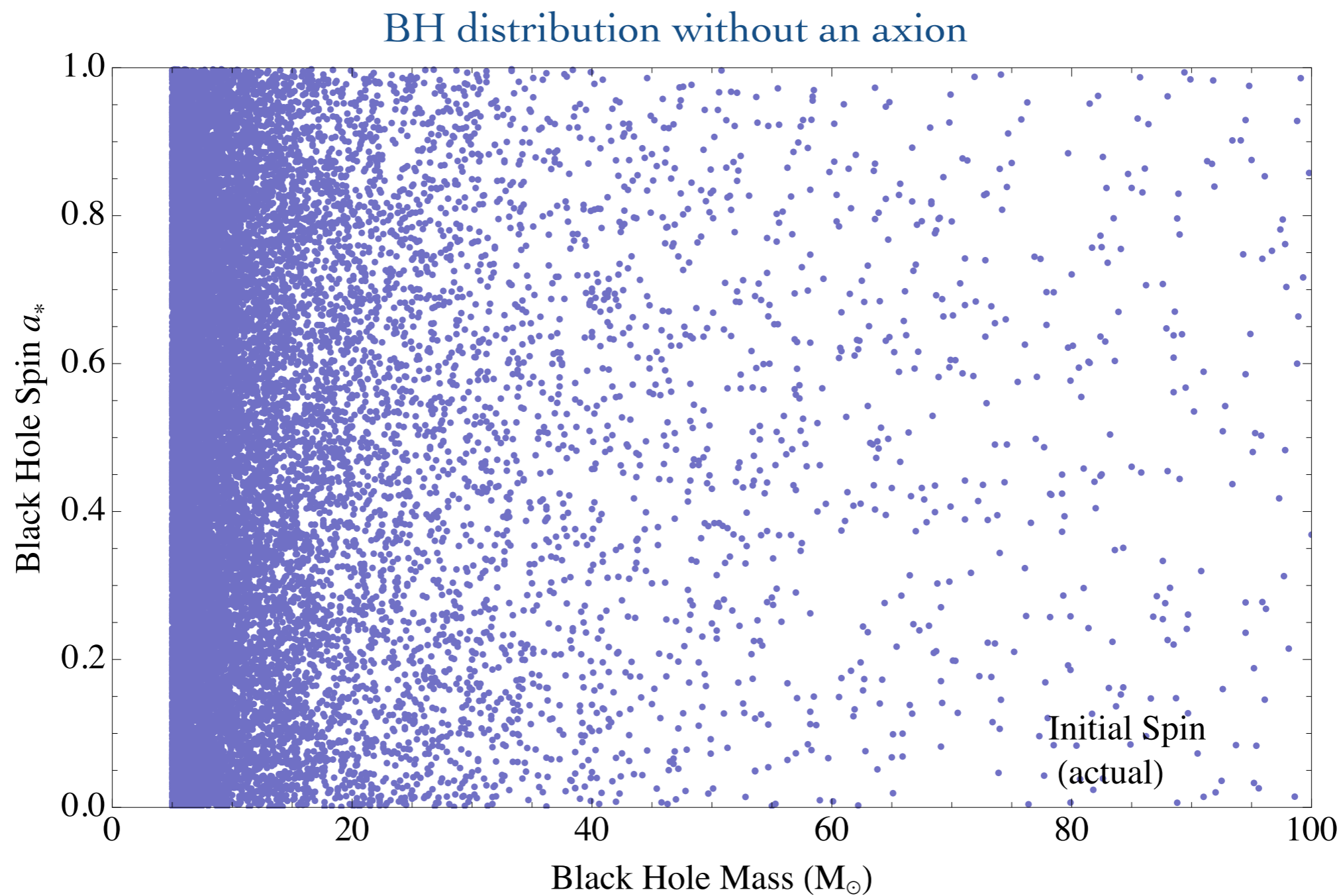
Spin-Down of Astrophysical Black Holes



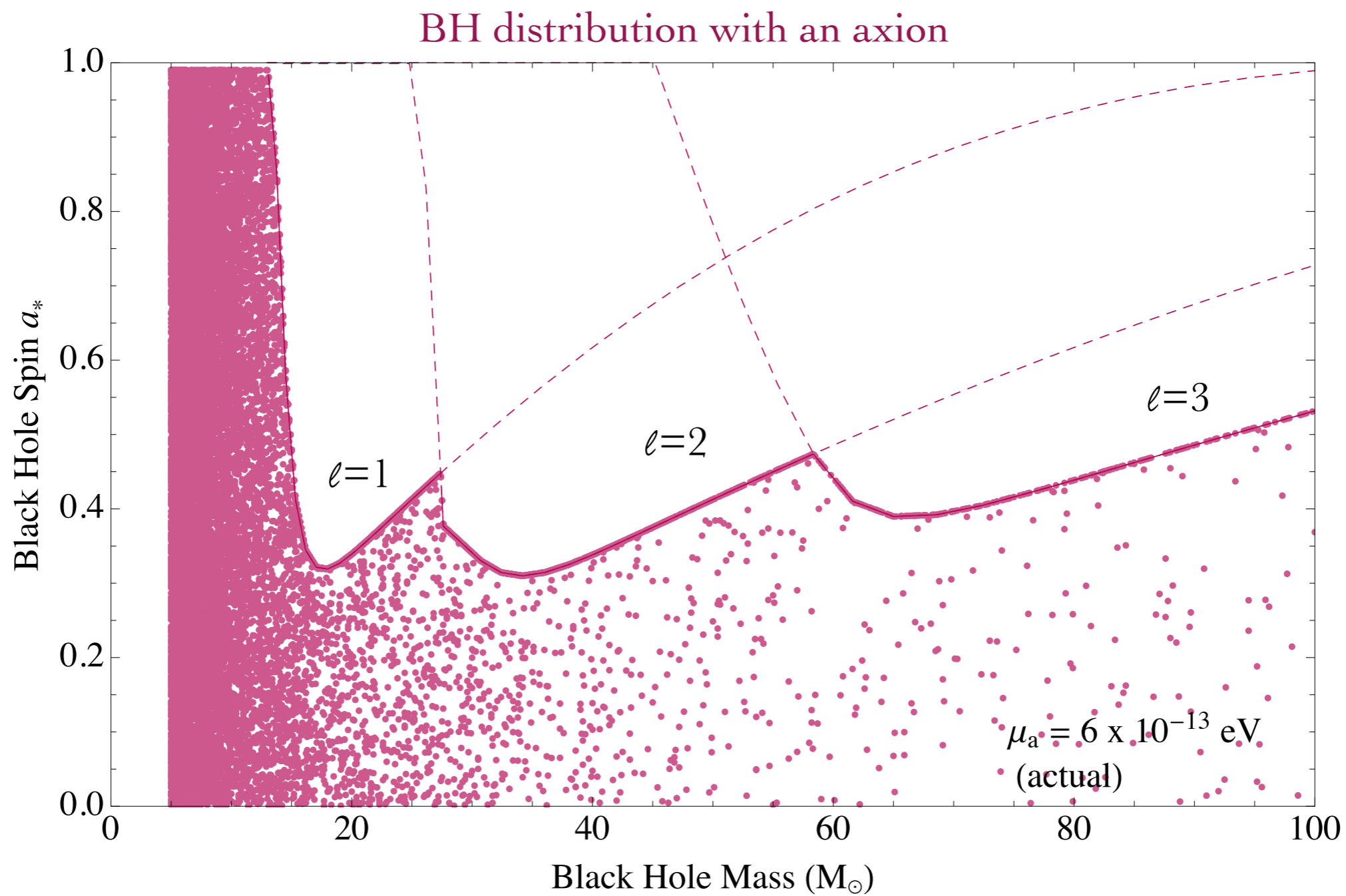
Range of the QCD axion excluded by current measurements

$$2 \times 10^{-11} > \mu_a > 6 \times 10^{-13} \text{ eV}$$

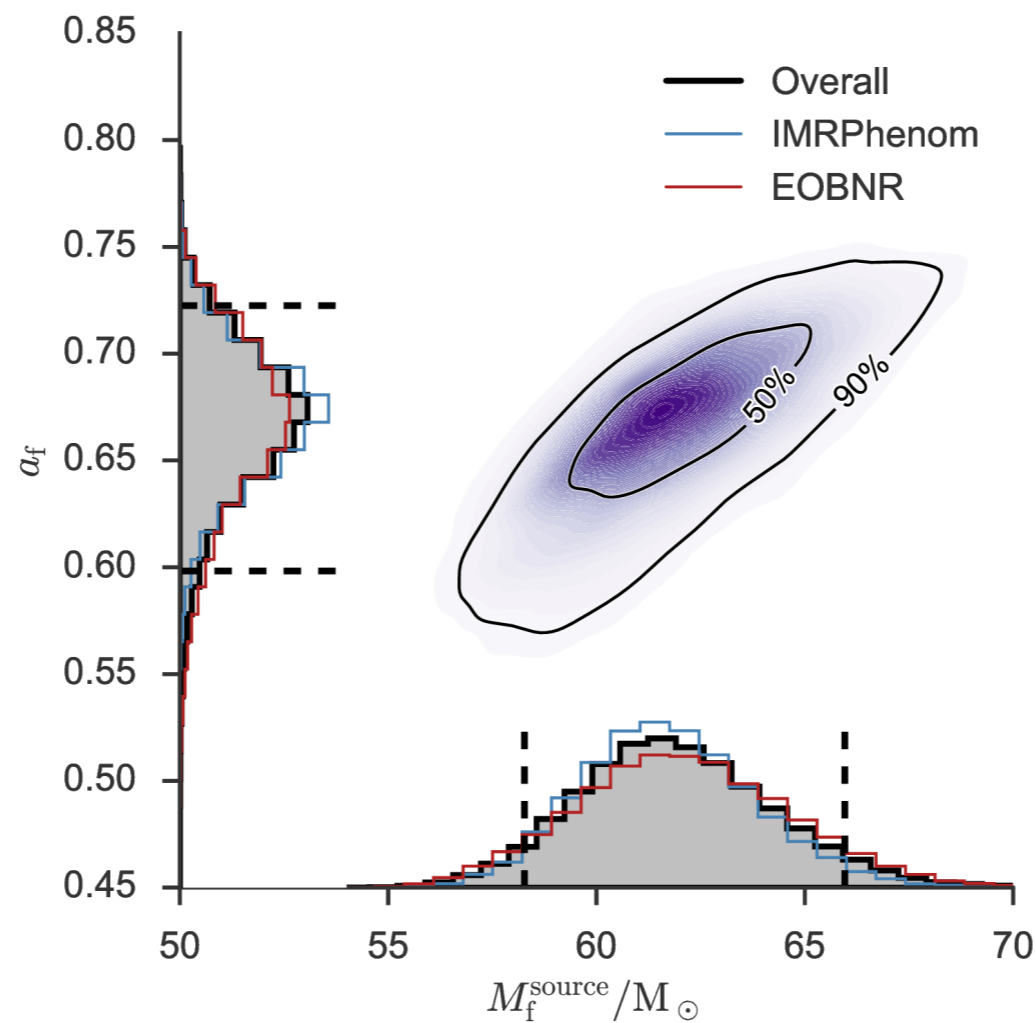
Black Hole Spins at aLIGO



Black Hole Spins at aLIGO



Properties of GW150914



Effective inspiral spin parameter χ_{eff}

Dimensionless primary spin magnitude a_1

Dimensionless secondary spin magnitude a_2

Final spin a_f

$$-0.09^{+0.19}_{-0.17}$$

$$0.32^{+0.45}_{-0.28}$$

$$0.57^{+0.40}_{-0.51}$$

$$0.67^{+0.06}_{-0.08}$$

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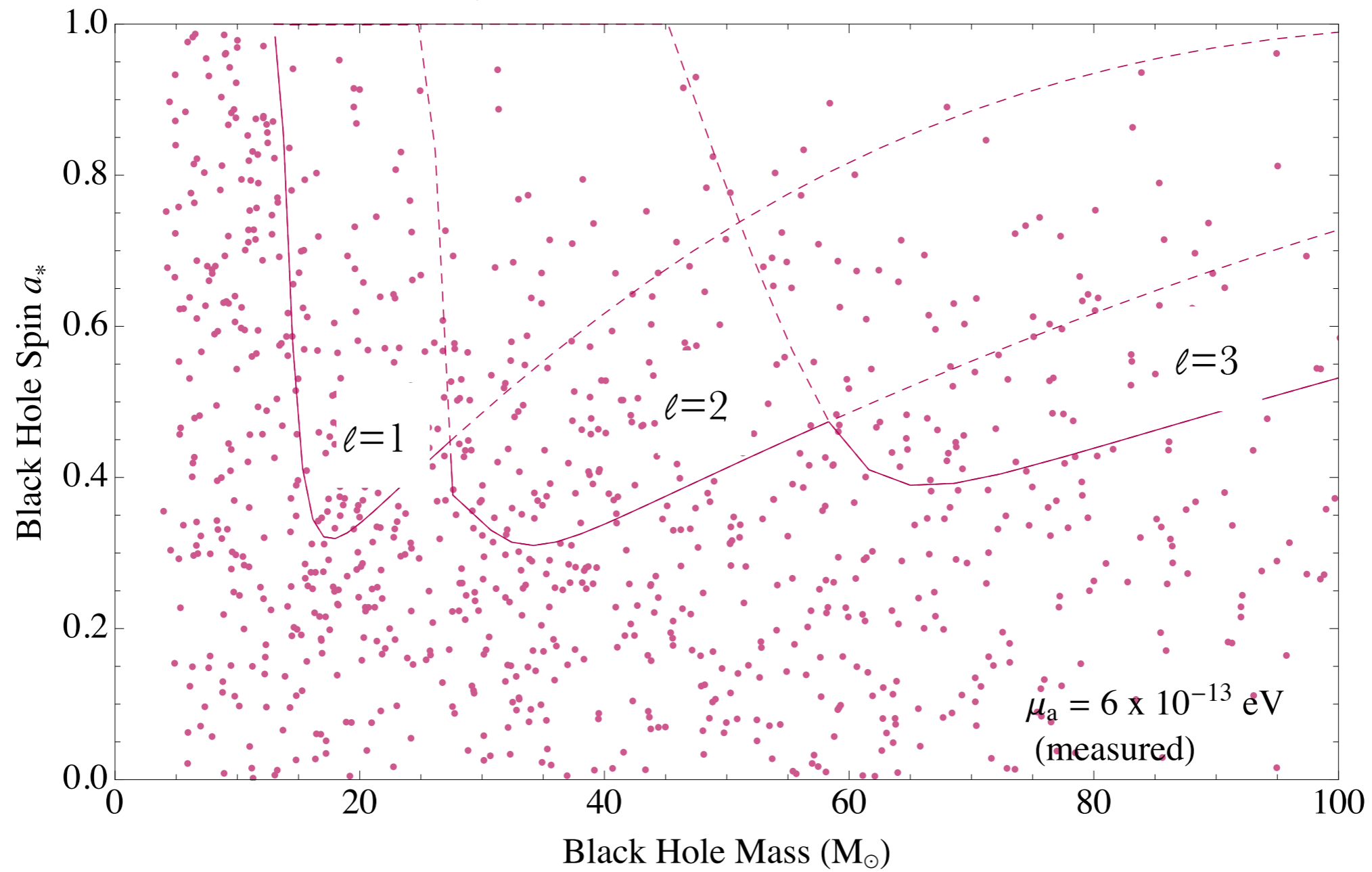
$$0.46^{+0.48 \pm 0.07}_{-0.42 \pm 0.01}$$

$$0.67^{+0.06 \pm 0.00}_{-0.07 \pm 0.03}$$

Black Hole Spins at aLIGO

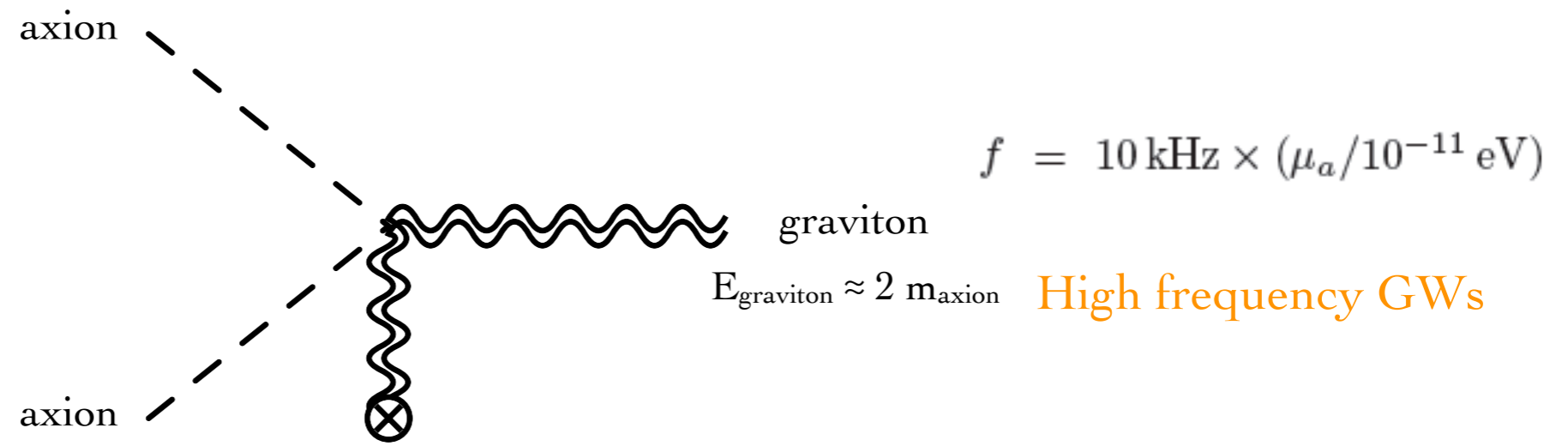
BH distribution with an axion
including errors

$$\sigma_M/M \sim 0.1; \quad \sigma_{a_*} \sim 0.25$$



Super-Radiance Signatures

GW annihilations



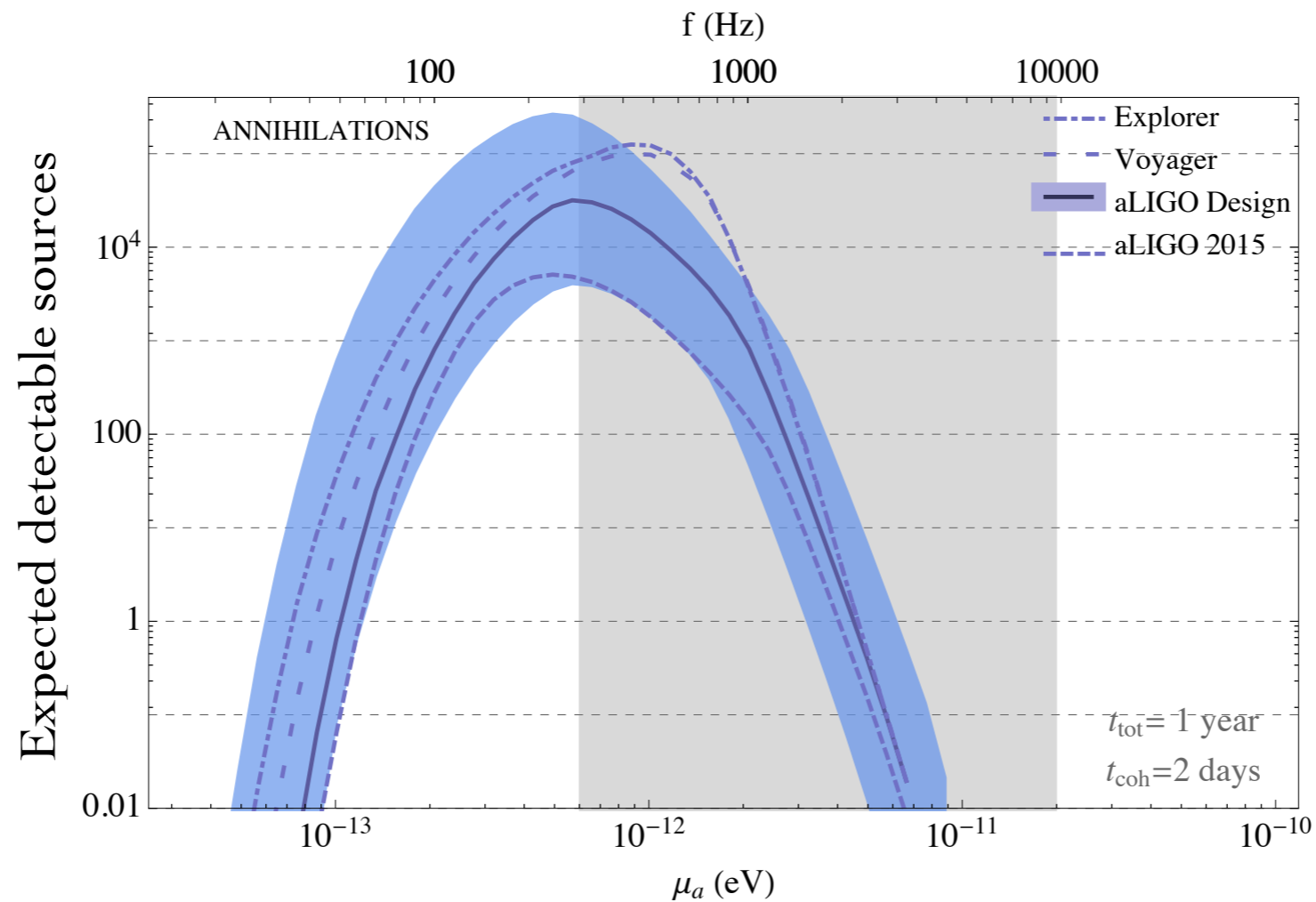
- Signal enhanced by the square of the occupation number of the state

$$h_{\text{peak}} \simeq 10^{-22} \left(\frac{1 \text{ kpc}}{r} \right) \left(\frac{\alpha/\ell}{0.5} \right)^{\frac{p}{2}} \frac{\alpha^{-\frac{1}{2}}}{\ell} \left(\frac{M}{10M_{\odot}} \right)$$

- Signal **duration** determined by the annihilation rate (can last thousands of years)

Expected Events from Annihilations

- Large uncertainties coming from tails of BH mass distribution



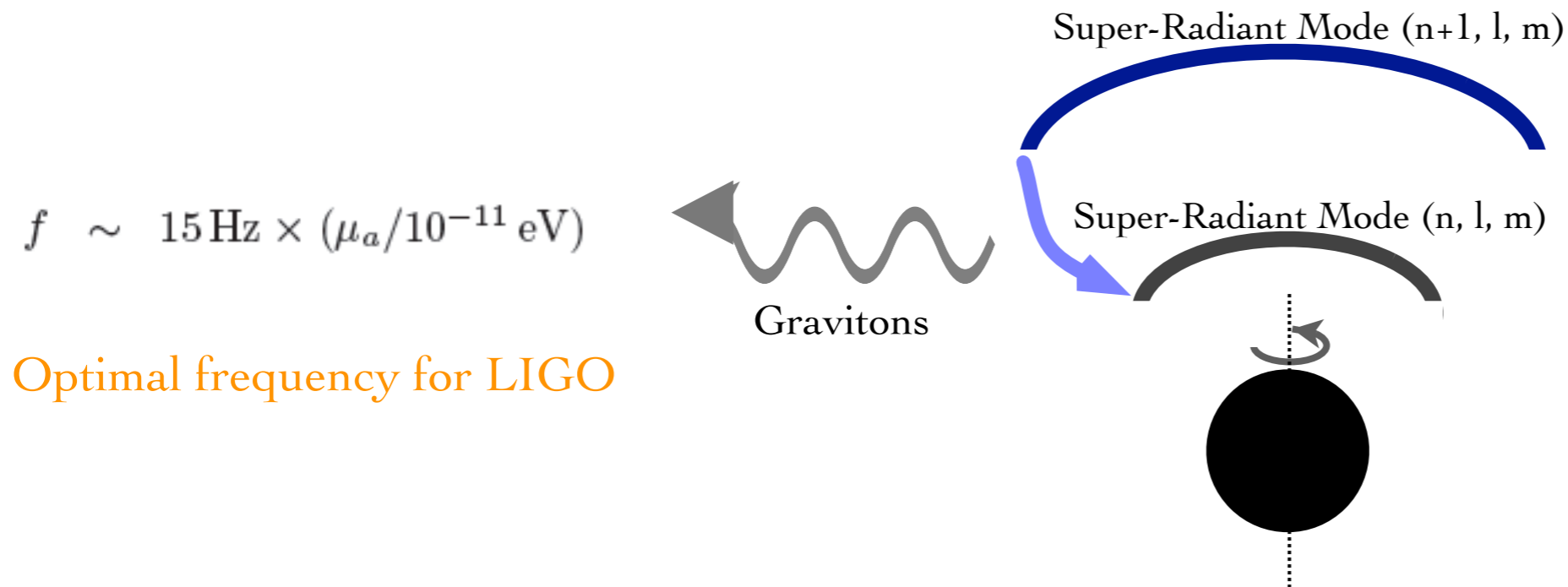
Pessimistic: flat spin distribution and 0.1 BH/century

Realistic: 30% above spin of 0.8 and 0.4 BH/century

Optimistic: 90% above spin of 0.9 and 0.9 BH/century

Super-Radiance Signatures

GW transitions



- Signal enhanced by the occupation numbers of excited and ground states

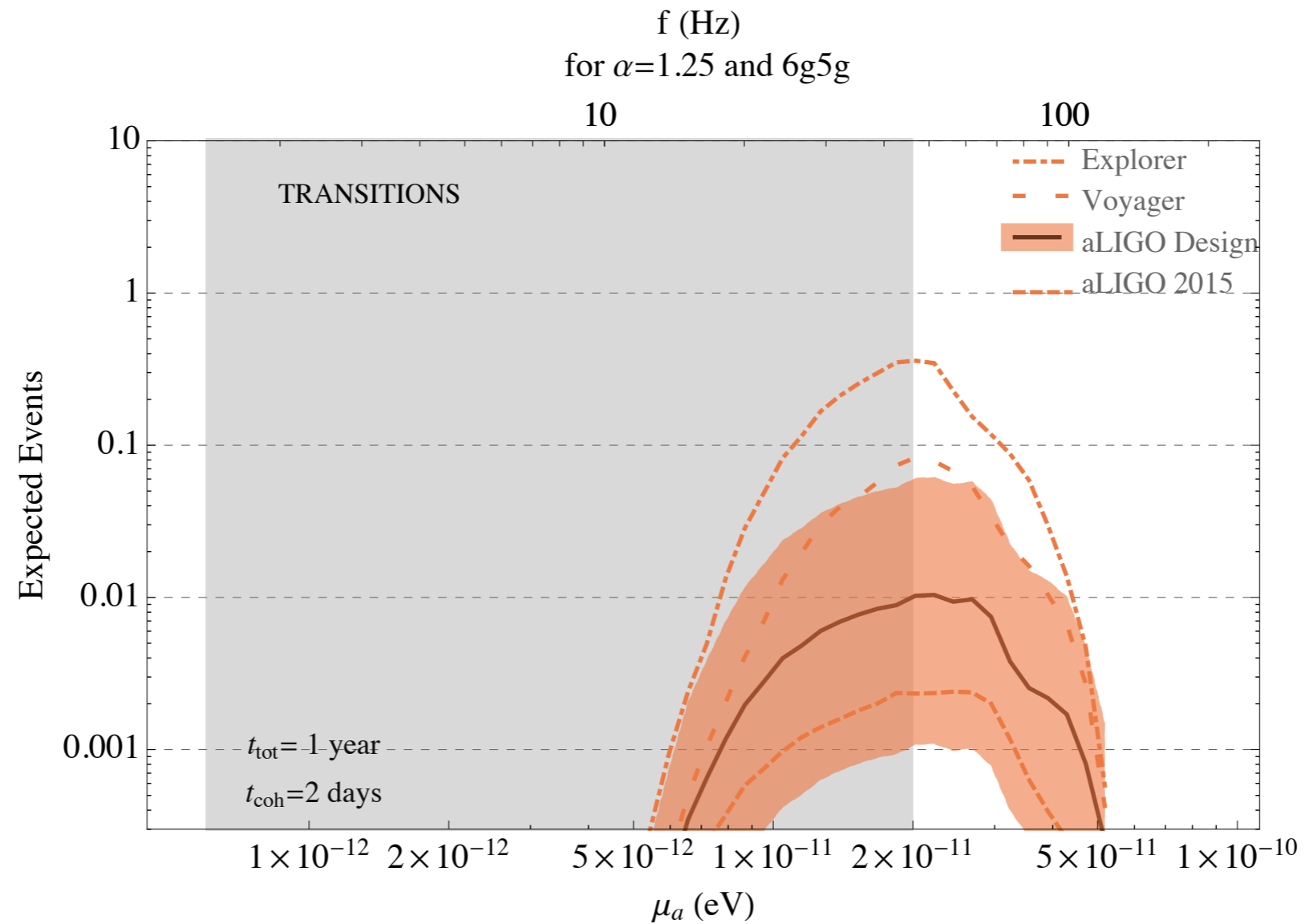
- Signal **strength** determined by the occupation number of the excited state

$$h \sim 3 \times 10^{-25} \text{ for a BH 10 kpc away}$$

- Signal **duration** determined by the superradiance rate (1-100 years duration)

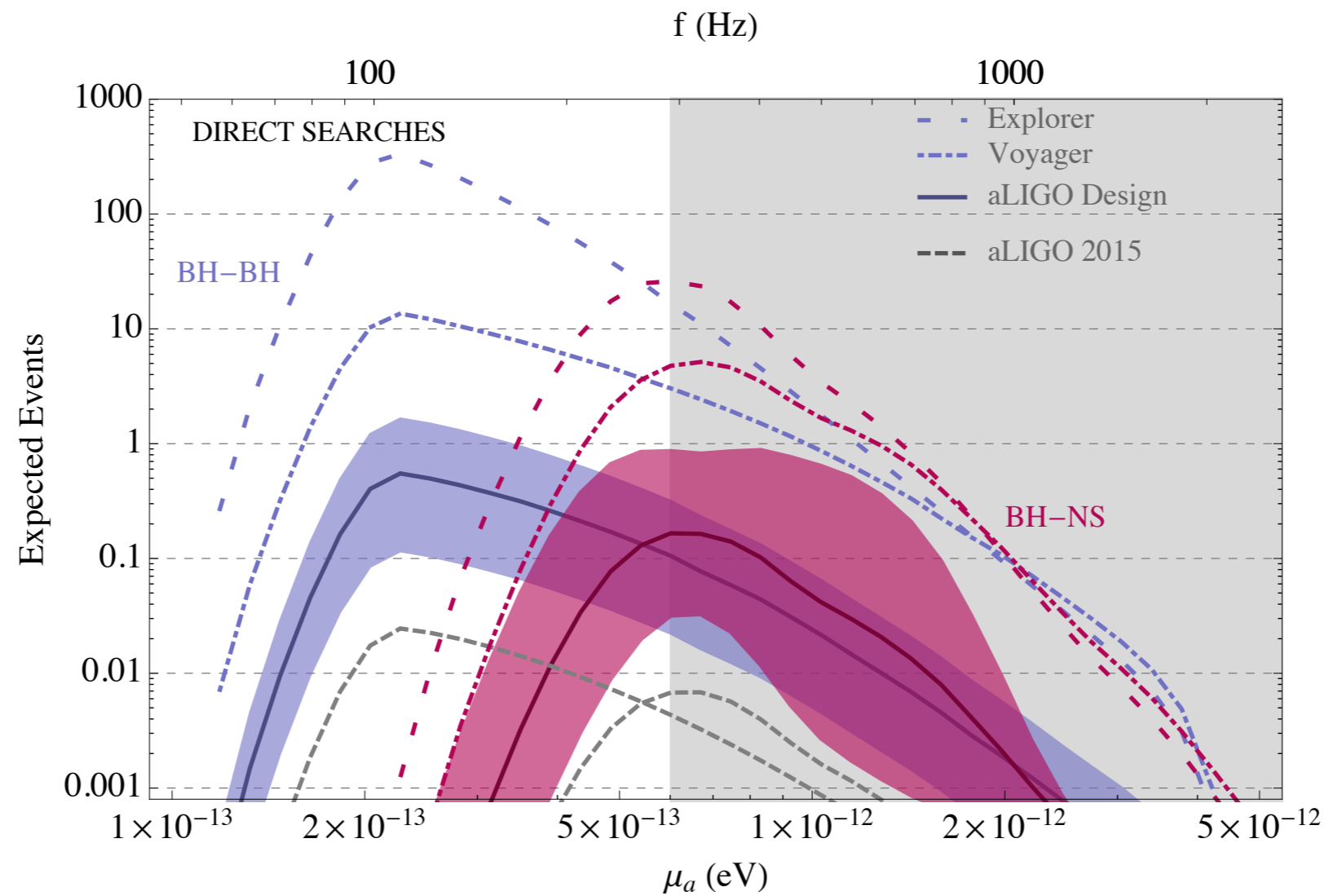
Transition Events Estimates

- Lower number of observable sources due to signal duration



Real-Time Superradiance

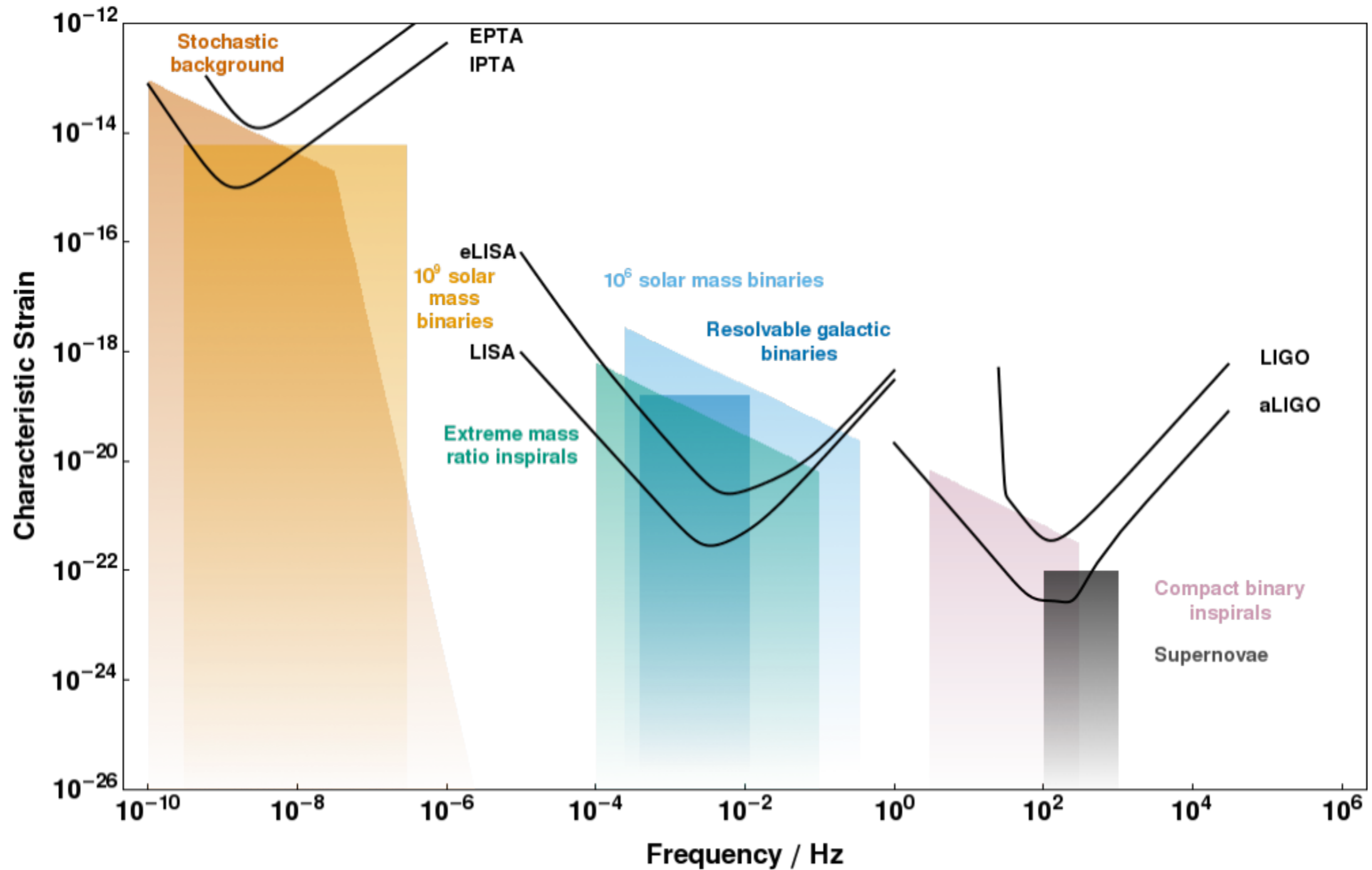
Black Holes produced from mergers are point sources candidates



Superradiance Prospects

- Probes axions between 10^{-20} and 10^{-10} eV independent of DM abundance
- Spin-mass distribution measured from mergers may reveal the presence of an axion
- Blind searches at aLIGO for annihilations most promising for lighter axions
- Merger events allow to follow SR in real time

Just The Beginning



Super Radiance Effect: Increased Progress Towards International Peace

TROUGH GROUP PRACTICE OF THE TRANSCENDENTAL
MEDITATION AND TM-SIDHI PROGRAM

