

Lepton Flavor Violation in Exclusive $b \rightarrow s$ Decays

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- 1 Introduction
- 2 LFU violation in $b \rightarrow sl^+\ell^-$
- 3 LFV in $b \rightarrow sl_1l_2$
- 4 Brief discussion of $h \rightarrow \mu\tau$
- 5 Conclusions and Perspectives

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Introduction

- Lepton Flavor Universality (**LFU**) is not a fundamental symmetry of the SM: **accidental** in the gauge sector and **broken by Yukawas**.
- LFU tested in pion and kaon decays – agrees very well with the SM
 \Rightarrow *To be improved by NA62*.
- Renewed interest in LFUV motivated by the recently found *conflict between theory and experiment* in

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})}, \quad \text{and} \quad R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu \mu)}{\mathcal{B}(B^+ \rightarrow K^+ e e)} \Bigg|_{q^2 \in (1,6) \text{ GeV}^2}$$

$$R_{D^*}^{\text{exp}} = 0.323 \pm 0.021$$

$$R_{D^*}^{\text{th}} = 0.252 \pm 0.003^{**} \quad [3.9\sigma]^{**}$$

$$R_D^{\text{exp}} = 0.41 \pm 0.05$$

$$R_D^{\text{th}} = 0.31 \pm 0.02^* \quad [2\sigma]^*$$

$$R_K^{\text{exp}} = 0.745_{-0.074}^{+0.090} \pm 0.036$$

$$R_K^{\text{th}} = 1.003 \pm 0.001 \quad [2.6\sigma]$$

Introduction

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$$[2.6\sigma]$$

- Is there a **model of NP** to explain these anomalies?
- What additional **experimental signatures** should we expect?

In general, $R_K \neq 1 \Leftrightarrow \mathbf{LFUV} \Rightarrow$ Lepton Flavor Violation (**LFV**).

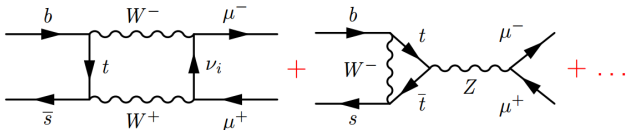
[Glashow et al, 2014.]

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LFU violation

(i) $b \rightarrow s \mu^+ \mu^-$

- FCNC process:



- Form-factors cancel out in the ratio \Rightarrow **Extremely clean prediction.**

$$R_K \equiv \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu \mu)}{\mathcal{B}(B^+ \rightarrow K^+ e e)} \bigg|_{q^2 \in (1,6) \text{ GeV}^2} \stackrel{\text{SM}}{=} 1.003(1) \quad [\text{Hiller, Kruger 2003}]$$

- 2.6 σ deviation** observed by LHCb:

$$R_K^{\text{exp}} = 0.745^{+0.090}_{-0.074}(\text{stat}) \pm 0.036(\text{syst})$$

LFU violation

(i) $b \rightarrow s\mu^+\mu^-$

- **2.6 σ deviation** observed by LHCb:

$$R_K^{\text{exp}} = 0.745_{-0.074}^{+0.090} \pm 0.036$$
$$R_K^{\text{SM}} = 1.003 \pm 0.001$$

- Instead, $\mathcal{B}(B^+ \rightarrow K^+ ee)_{q^2 \in [1,6]}$ agrees with the SM, whereas

$$\mathcal{B}(B^+ \rightarrow K^+ \mu\mu)_{q^2 \in [1,6]}^{\text{exp}} \text{ GeV}^2 = (1.19 \pm 0.07) \times 10^{-7}$$
$$\mathcal{B}(B^+ \rightarrow K^+ \mu\mu)_{q^2 \in [1,6]}^{\text{SM}} \text{ GeV}^2 = (1.75_{-0.29}^{+0.60}) \times 10^{-7}$$

- $\mathcal{B}(B_s \rightarrow \mu^+\mu^-)$ is slightly smaller than the SM:

$$\overline{\mathcal{B}}(B_s \rightarrow \mu\mu)^{\text{LHCb+CMS}} = (2.8_{-0.6}^{+0.7}) \times 10^{-9} \quad \overline{\mathcal{B}}(B_s \rightarrow \mu\mu)^{\text{Atlas}} = (0.9_{-0.8}^{+1.1}) \times 10^{-9}$$
$$\overline{\mathcal{B}}(B_s \rightarrow \mu\mu)^{\text{SM}} = (3.65 \pm 0.23) \times 10^{-9}$$

- Anomalies in $B \rightarrow K^* \mu^+ \mu^-$ angular distributions \Rightarrow yesterday talks.

Explaining R_K

If the LFUV takes place at scales well above EWSB, then use OPE:

- Operators relevant to $b \rightarrow s \ell \ell$ are

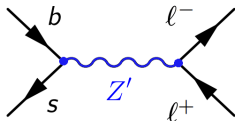
$$\begin{aligned}\mathcal{O}_9^{(\prime)} &= (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\ell} \gamma^\mu \ell), & \mathcal{O}_{10}^{(\prime)} &= (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\ell} \gamma^\mu \gamma^5 \ell), \\ \mathcal{O}_S^{(\prime)} &= (\bar{s} P_{R(L)} b) (\bar{\ell} \ell), & \mathcal{O}_P^{(\prime)} &= (\bar{s} P_{R(L)} b) (\bar{\ell} \gamma^5 \ell), \\ \mathcal{O}_7^{(\prime)} &= (\bar{s} \sigma_{\mu\nu} P_{R(L)} b) F^{\mu\nu} \quad \dots\end{aligned}$$

- To explain $R_K < 1$, one needs effective coefficients $C_9^{(\prime)}$, $C_{10}^{(\prime)}$ different from the SM values.
- Compatible with results based on the global fits of $b \rightarrow s \ell \ell$ data.
[Straub et al. 2014, Descotes-Genon et al. 2015, Hurth et al. 2016]

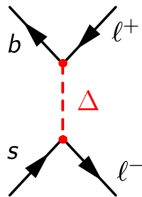
Are there **specific models** capable of generating $C_{9,10}^{(\prime)}$ to explain R_K ?

Representative models:

Z' models



Leptoquark models



Buras et al., Altmannshofer et al.,
Crivellin et al., Celis et al. ...

Hiller et al., Becirevic et al.,
Gripaios et al. ...

- Vector leptoquark models also plausible, but non-renormalizable [problematic, how to compute loops? $B_s - \bar{B}_s$ constraint?]

Barbieri et al., Fajfer et al.

- Interesting feature: **LFV** is in general **expected** .

Explaining R_K : Illustration

Scalar Leptoquark Models

Analysis of the separate modes: data **prefers** to decrease $\mathcal{B}(B^+ \rightarrow K^+ \mu\mu)$.

⇒ Let us focus on NP with couplings **only to muons**

[although couplings to electrons are also possible, cf. Hiller, Schmaltz 2014]

Representation under $SU(3)_c \times SU(2)_L \times U(1)_Y$:

- $(3, 2)_{7/6}$: Increases $B \rightarrow K \mu^+ \mu^-$ $(C_9)_{\mu\mu} = (C_{10})_{\mu\mu}$ $\bar{Q} \Delta^{(7/6)} \ell_R$
- **$(3, 2)_{1/6}$: Decreases $B \rightarrow K \mu^+ \mu^-$ $(C'_9)_{\mu\mu} = -(C'_{10})_{\mu\mu}$ $\bar{L} \tilde{\Delta}^{(1/6)} d_R$**
- $(\bar{3}, 3)_{1/3}$ and $(3, 1)_{4/3} \Rightarrow$ Proton destabilizes

[Kosnik, 2012]

NB. Convention: $Q = T_3 + Y$.

Explaining R_K : Illustration

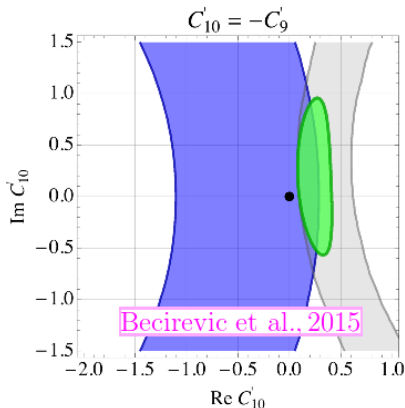
Scalar Leptoquark $(3, 2)_{1/6}$

1st step: Wilson coefficients fit.

$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$ and $\mathcal{B}(B^+ \rightarrow K^+ \mu \mu)_{\text{high } q^2}$

$\Rightarrow (C'_{10})_{\mu\mu} = -(C'_9)_{\mu\mu} \in (0.19, 0.52)$

$\Rightarrow \mathbf{R_K^{\text{pred}}} = \mathbf{0.88(8)}$.



Model independent prediction: $\mathbf{R_{K^*} = 1.11(8)}$

[RH quark currents imply $R_{K^*} > 1$]

[Hiller, Schmaltz 2014]

Explaining R_K : Illustration

Scalar Leptoquark $(3, 2)_{1/6}$

2nd step: Model dependent interpretation.

$$\mathcal{L}_Y = Y_{ij} \bar{L}_{Li} \tilde{\Delta}^{(1/6)} d_{Rj} + \text{h.c.}$$

$$C'_9 = -C'_{10} \propto \frac{Y_{\mu s} Y_{\mu b}^*}{m_{\tilde{\Delta}}^2}$$

$$Y = \begin{pmatrix} 0 & 0 & 0 \\ 0 & Y_{\mu s} & Y_{\mu b} \\ 0 & & \end{pmatrix}$$

Explaining R_K : Illustration

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$$\mathbb{Y} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & Y_{\mu s} & Y_{\mu b} \\ 0 & Y_{\tau s} & Y_{\tau b} \end{pmatrix}$$

How can we probe the couplings to τ 's?

- $\tau \rightarrow \mu\phi$ is an useful constraint
- **LFV** in $B_{(s)}$ decays.!

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- OPE for LFV:

$$\begin{aligned}
 \mathcal{O}_9^{(\prime)} &= (\bar{s}\gamma_\mu P_{L(R)}b)(\bar{\ell}_1\gamma^\mu\ell_2), & \mathcal{O}_{10}^{(\prime)} &= (\bar{s}\gamma_\mu P_{L(R)}b)(\bar{\ell}_1\gamma^\mu\gamma^5\ell_2), \\
 \mathcal{O}_S^{(\prime)} &= (\bar{s}P_{R(L)}b)(\bar{\ell}_1\ell_2), & \mathcal{O}_P^{(\prime)} &= (\bar{s}P_{R(L)}b)(\bar{\ell}_1\gamma_5\ell_2), \\
 \mathcal{O}_7^{(\prime)} &= (\bar{s}\sigma_{\mu\nu}P_{R(L)}b)F^{\mu\nu} \quad \dots
 \end{aligned}$$

- Let us focus on scenarios with $C_{9,10}^{(\prime)} \neq 0$ (SLQ and Z').
- $C_{S,P}^{(\prime)} \neq 0 \Rightarrow$ We used CMS hint $\mathcal{B}(h \rightarrow \tau\mu) = 0.83(38)\%$ to fix the couplings and obtained that LFV in B decays is too small ($\lesssim 10^{-13}$).

- **Attention:** $i\partial_\mu(\bar{l}_1\gamma^\mu l_2) = (m_2 - m_1)\bar{l}_1l_2 \neq 0$
 \Rightarrow New contributions appear in the LFV modes

$$\mathcal{B}(B_s \rightarrow l_1^- l_2^+) \propto [m_{B_s}^2 - (m_1 + m_2)^2](m_1 - m_2)^2 \cdot |C_9 - C_9'|^2 \\ + [m_{B_s}^2 - (m_1 - m_2)^2](m_1 + m_2)^2 \cdot |C_{10} - C_{10}'|^2$$

- $C_9^{(\prime)} = -C_{10}^{(\prime)} \neq 0 \Rightarrow$ Hierarchy between modes:

$$\mathcal{B}(B_s \rightarrow l_1 l_2) < \mathcal{B}(B \rightarrow K l_1 l_2) < \mathcal{B}(B \rightarrow K^* l_1 l_2)$$

$$\frac{\mathcal{B}(B \rightarrow K^* \mu\tau)}{\mathcal{B}(B \rightarrow K \mu\tau)} \approx 1.8, \quad \frac{\mathcal{B}(B \rightarrow K \mu\tau)}{\mathcal{B}(B_s \rightarrow \mu\tau)} \approx 1.25.$$

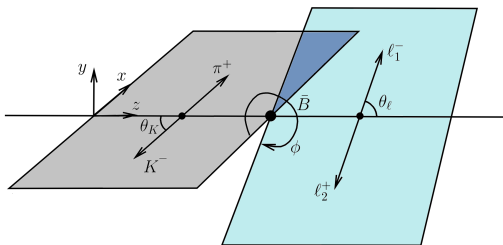
- **Important:** Limits on one exclusive LFV mode can set constraints on the others.

LFV in $b \rightarrow sl_1 l_2$

Clarifying the Angular Conventions in $\bar{B} \rightarrow \bar{K}^* \ell \ell$

[Becirevic et al. 1602.0081]

- Most theory papers do not provide the full angular conventions for $\bar{B} \rightarrow \bar{K}^* \ell \ell$ [ambiguity in the definition of ϕ].
- We adopt the conventions of [Gratex et al., 2015] \equiv LHCb and find full agreement for $I_i(q^2)$.



K^* rest frame:

$$p_K^\mu = (E_K, \hat{\mathbf{p}}_{\mathbf{K}} |p_K|), \quad p_\pi^\mu = (E_\pi, -\hat{\mathbf{p}}_{\mathbf{K}} |p_K|),$$

with $\hat{\mathbf{p}}_{\mathbf{K}} = (-\sin \theta_K, 0, -\cos \theta_K)$.

Dilepton rest frame:

$$p_1^\mu = (E_\alpha, \hat{\mathbf{p}}_\ell |p_\ell|), \quad p_2^\mu = (E_\beta, -\hat{\mathbf{p}}_\ell |p_\ell|),$$

with $\hat{\mathbf{p}}_\ell = (\sin \theta_\ell \cos \phi, -\sin \theta_\ell \sin \phi, \cos \theta_\ell)$.

LFV in $b \rightarrow sl_1 l_2$

Helicity Formalism for $m_1 \neq m_2$

- LFC case ($m_1 = m_2$) - $A_{\parallel, \perp, 0}^{L,R}$ and $A_{S,P}$:

$$\bar{\ell} \gamma_5 \ell = \frac{q^\mu (\bar{\ell} \gamma_\mu \gamma_5 \ell)}{2m_\ell} \Rightarrow C_{P^{(\prime)}} \text{ can be absorbed in } A_t.$$

$$q^\mu (\bar{\ell} \gamma_\mu \ell) = 0 \Rightarrow C_{S^{(\prime)}} \text{ require a residual HA } A_S.$$

- LFV case ($m_1 \neq m_2$) - $A_{\parallel, \perp, 0, t}^{L,R}$:

$$\bar{\ell}_1 \gamma_5 \ell_2 = \frac{q^\mu (\bar{\ell}_1 \gamma_\mu \gamma_5 \ell_2)}{m_1 + m_2}, \quad \bar{\ell}_1 \ell_2 = \frac{q^\mu (\bar{\ell}_1 \gamma_\mu \ell_2)}{m_1 - m_2} \Rightarrow \text{New HA's } A_t^{L,R}$$

LFV in $b \rightarrow sl_1 l_2$

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Going from LFC to LFV:

$$A_t = \lim_{m_1 \rightarrow m_2} (A_t^L - A_t^R), \quad A_S = \lim_{m_1 \rightarrow m_2} \left[\frac{m_1 - m_2}{\sqrt{q^2}} (A_t^L + A_t^R) \right]$$

NB. The singularity in $m_1 = m_2$ cancels out in $I_i(q^2)$.

LFV in $b \rightarrow s\mu\tau$

Scalar Leptoquark $(3, 2)_{1/6}$

Maximally allowed value lies just below the BaBar limit:
 $B(B^+ \rightarrow K^+ \mu\tau) \leq 4.8 \times 10^{-5}$ [90% CL].

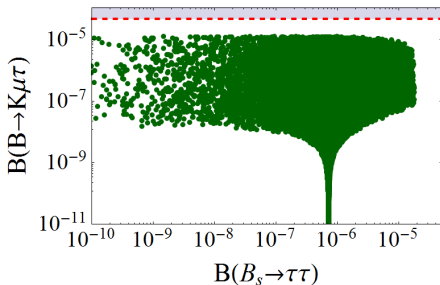
[Becirevic et al., to appear]

Can LHCb do better ?

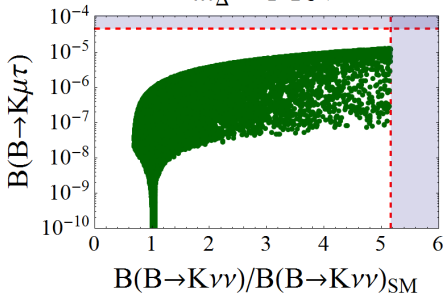
Even weak limits on $B \rightarrow K\mu\tau$ can be useful to constraint $Y_{\tau s}$, $Y_{\tau b}$ and $B \rightarrow K\nu\nu$ (Belle-2).

$$\mathbb{Y} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & Y_{\mu s} & Y_{\mu b} \\ 0 & Y_{\tau s} & Y_{\tau b} \end{pmatrix}$$

$m_\Delta = 1 \text{ TeV}$



$m_\Delta = 1 \text{ TeV}$



Explaining R_K : Another Possibility

Z' Models

Z' bosons are usually associated with a new Abelian symmetry $U(1)'$.

A few examples:

- Gauged $L_\mu - L_\tau$ symmetry [Crivellin, D'Ambrosio, Heeck, 1501.00993]
- Gauged $B - L$ charges [Crivellin, D'Ambrosio, Heeck, 1503.03477]

Here, we will consider a **bottom-up approach**:

$\Rightarrow Z'$ couplings are only **fixed by data**.

[Crivellin et al. 2015, Becirevic et al. 2016]

$$\mathcal{L}_{Z'} \supset g_{\ell_i \ell_j}^L \bar{\ell}_i \gamma^\mu P_L \ell_j Z'_\mu + g_{sb}^L \bar{s} \gamma^\mu P_L b Z'_\mu + (L \rightarrow R)$$

Assumptions: gauge invariance (e.g., $g_{\ell_i \ell_j}^L = g_{\nu_i, \nu_j}^L$) and no couplings to electrons.

- Scenario I: $g_{sb}^L, g_{\mu\mu}^L \neq 0$ $(C_9)_{\mu\mu} = -(C_{10})_{\mu\mu} \propto g_{sb}^L g_{\mu\mu}^L$.
- Scenario II: $g_{sb}^R, g_{\mu\mu}^L \neq 0$ $(C'_9)_{\mu\mu} = -(C'_{10})_{\mu\mu} \propto g_{sb}^R g_{\mu\mu}^L$.

$$\mathcal{L}_{Z'} \supset g_{\ell_i \ell_j}^L \bar{\ell}_i \gamma^\mu P_L \ell_j Z'_\mu + g_{sb}^L \bar{s} \gamma^\mu P_L b Z'_\mu + (L \rightarrow R)$$

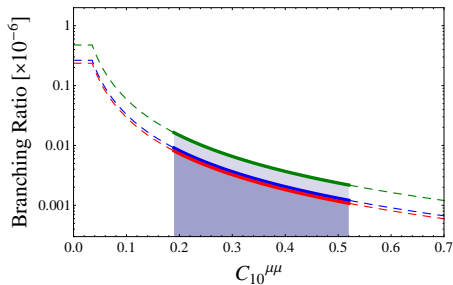
Most relevant constraints:

$B_s - \bar{B}_s$ mixing	\iff	$ g_{sb}^{L(R)} /m_{Z'} \leq 1.6 \times 10^{-3} \text{ TeV}^{-1}$
$\tau \rightarrow \mu \bar{\nu}_\mu \nu_\tau$	\iff	$(g_{\mu\mu}^L, g_{\mu\tau}^L, g_{\mu\tau}^R)/m_{Z'}$
$\tau \rightarrow 3\mu$	\iff	$(g_{\mu\tau}^L, g_{\mu\tau}^R)/m_{Z'}$

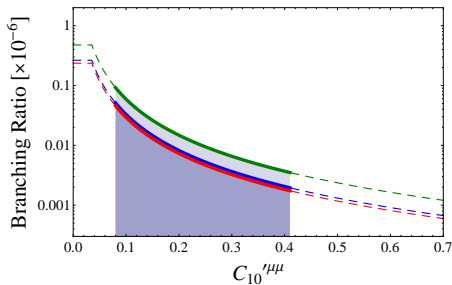
Maximal branching ratios \Rightarrow Possibly within the reach of LHCb and Belle-2.

Scenario	I (LH)	II (RH)
$\mathcal{B}(B \rightarrow K^* \mu\tau) \leq$	1.6×10^{-8}	9.3×10^{-8}
$\mathcal{B}(B \rightarrow K \mu\tau) \leq$	0.9×10^{-8}	5.2×10^{-8}
$\mathcal{B}(B_s \rightarrow \mu\tau) \leq$	0.8×10^{-8}	4.6×10^{-8}

Scenario I



Scenario II



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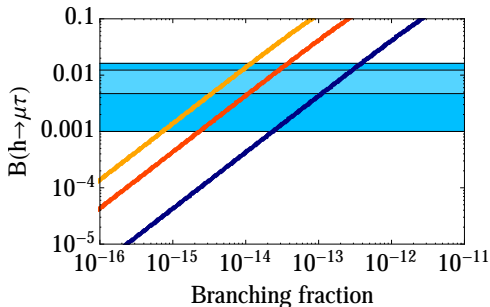
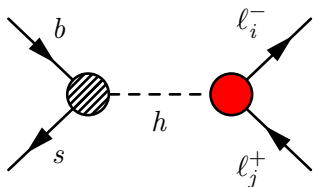
Brief discussion of $h \rightarrow \mu\tau$

- CMS observed $\mathcal{B}(h \rightarrow \tau\mu) = 0.846_{-0.37}^{+0.39}\%$ [2.2σ]. What are the implications for B physics if this result is confirmed?

Brief discussion of $h \rightarrow \mu\tau$

- CMS observed $\mathcal{B}(h \rightarrow \tau\mu) = 0.846_{-0.37}^{+0.39}\%$ [2.2 σ]. What are the implications for B physics if this result is confirmed?

$$\mathcal{L}_{\text{eff}} = -y_{ij}\bar{\ell}_L^i\bar{\ell}_R^j h + \text{h.c.} \quad \Leftrightarrow \quad 0.8 \times 10^{-3} < \sqrt{|y_{\mu\tau}|^2 + |y_{\tau\mu}|^2} < 3.6 \times 10^{-3}$$



Largest BR is $\mathcal{B}(B_s \rightarrow \mu\tau) < 4 \times 10^{-13} \Rightarrow$ **Too small!**

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Conclusions and Perspectives

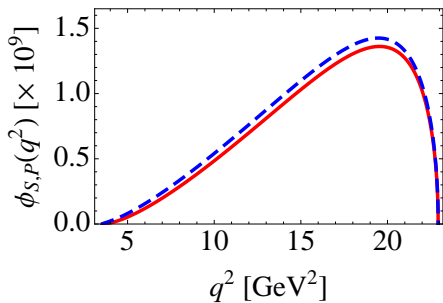
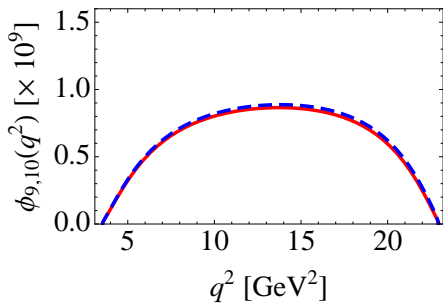
- Interesting **hints of LFU violation** in R_K and $R_{D^{(*)}}$ – **Higgs Flavor Era** around the corner?
- Important cross-checks: R_{K^*} , R_ϕ , $\mathcal{B}(B_s \rightarrow D_s \tau \bar{\nu})/\mathcal{B}(B_s \rightarrow D_s \ell \bar{\nu})$ etc [theoretically and experimentally clean].
- **LFV is expected** in most models aiming to explain R_K . We give predictions in models with generic Z' states ($\sim 10^{-7}$) and SLQ ($\sim 10^{-5}$).
- **Take-home message:** even not so stringent experimental limits on exclusive B LFV decay modes can be useful to constrain models of NP.

Thank you!

Back-up

More on B LFV

$$\begin{aligned} \mathcal{B}(B_s \rightarrow \ell_1^- \ell_2^+)^{theo} &= \frac{\tau_{B_s}}{64\pi^3} \frac{\alpha^2 G_F^2}{m_{B_s}^3} f_{B_s}^2 |V_{tb} V_{ts}^*|^2 \lambda^{1/2}(m_{B_s}, m_1, m_2) \\ &\times \left\{ [m_{B_s}^2 - (m_1 + m_2)^2] \cdot \left| (C_9 - C'_9)(m_1 - m_2) + (C_S - C'_S) \frac{m_{B_s}^2}{m_b + m_s} \right|^2 \right. \\ &\quad \left. + [m_{B_s}^2 - (m_1 - m_2)^2] \cdot \left| (C_{10} - C'_{10})(m_1 + m_2) + (C_P - C'_P) \frac{m_{B_s}^2}{m_b + m_s} \right|^2 \right\} \end{aligned}$$



$$C_{9'}^{\ell\ell'} = -C_{10'}^{\ell\ell'} = \frac{\pi v^2}{2\lambda_t \alpha_{\text{em}}} \frac{Y_{s\ell} Y_{b\ell'}^*}{m_\Delta^2},$$

$$\frac{d\Gamma}{dq^2}(B \rightarrow K\nu\bar{\nu}) = \frac{|N|^2}{384\pi^3 m_B^3} |f_+(q^2)|^2 \lambda^{3/2}(m_B^2, m_K^2, q^2) \\ \times \left\{ 3|C_L^{\text{SM}}|^2 + \frac{(Y \cdot Y^\dagger)_{ss} (Y \cdot Y^\dagger)_{bb}}{16N^2 m_\Delta^4} + \frac{2\text{Re}[C_L^{\text{SM}} (Y \cdot Y^\dagger)_{sb}]}{4Nm_\Delta^2} \right\},$$

where $N = \frac{G_F V_{tb} V_{ts}^* \alpha}{\sqrt{2}\pi}$ and $C_L^{\text{SM}} = -6.38(6)$.

Similar scenarios are considered: $C_9^{\mu\mu} \neq 0$ and $C_9^{\mu\mu} = -C_{10}^{\mu\mu} \neq 0$; but the rates are ten times larger. Why?

- 2σ discrepancy in $\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})$?

$$\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})_{\text{SM}} = 17.29(3)\%$$

$$\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})_{\text{exp}} = 17.33(5)\% \quad \text{[Average]}$$

$$\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})_{\text{exp}} = 17.41(4)\% \quad \text{[Fit]}$$

PDG and HFAG fits amplify the 1.6σ discrepancy of

$$\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})/\mathcal{B}(\tau \rightarrow e\nu\bar{\nu})$$

measured by BaBar \Rightarrow The average should be used instead.

- Main source of **disagreement**: $B_s - \bar{B}_s$ mixing

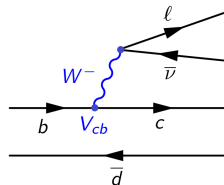
If $b \rightarrow s\mu\mu$ data is analyzed with only $C_{9,10}$, then $g_{sb}^R = 0 \Rightarrow$ **No fine-tuning** in $B_s - \bar{B}_s$.

LFU violation

(ii) $b \rightarrow c\tau\bar{\nu}$

- Tree-level process in the SM:

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)}\ell\bar{\nu})}, \quad \ell = e, \mu.$$



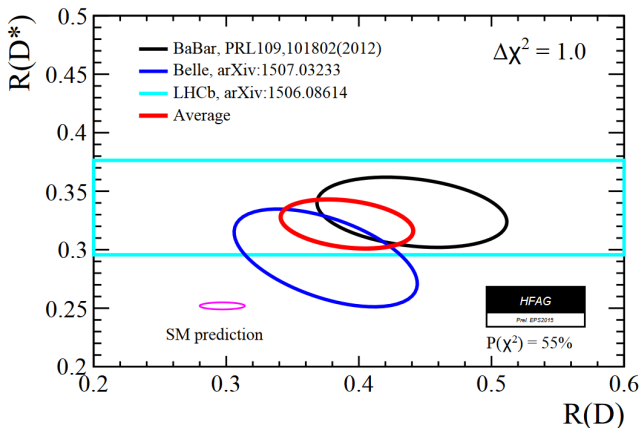
- Non-perturbative QCD \iff form-factors (Lattice QCD)

$$\text{e.g. for } B \rightarrow D, \quad \langle D | \bar{c} \gamma_\mu b | B \rangle \propto f_{0,+}(q^2)$$

- Situation less clear for $B \rightarrow D^* \Rightarrow$ (more FFs, less LQCD results)
[One form factor is unknown from LQCD (error associated?)]

LFU violation

(ii) $b \rightarrow c\tau\bar{\nu}$



- **3.9 σ combined** deviation from the SM [theory error under control?]
- **2 σ** deviation if **only** R_D is considered.