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# Measurement of $\sin^2\theta_{\text{eff}}^{\text{lept}}$

Using 2012 8 TeV dataset ( $\sim 19/\text{fb}$ )



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Physics  
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Representing the CMS collaboration

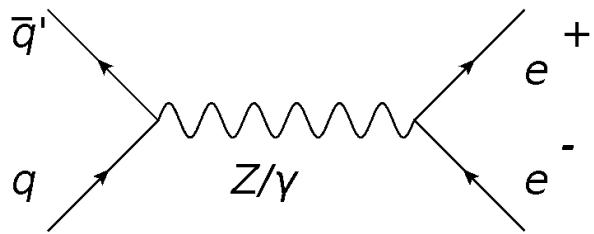
6 Jul 2017, 10:30 15m

Room Volpi (Palazzo del Casinò)

# Dilepton production Hadron colliders



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The axial and vector neutral currents interfere

Weak neutral current strength related to  $\sin^2\theta_{\text{eff}}$

$$\sin^2\theta_W = \sin^2\theta_W^{\text{on-shell}} = 1 - M_W^2 / M_Z^2$$

$$\cdot \sin^2\theta_{\text{eff}}^{\text{lept}} = \text{Re}[\kappa_l(M_Z^2, \sin^2\theta_w)] \sin^2\theta_w \\ \downarrow \approx 1.037$$

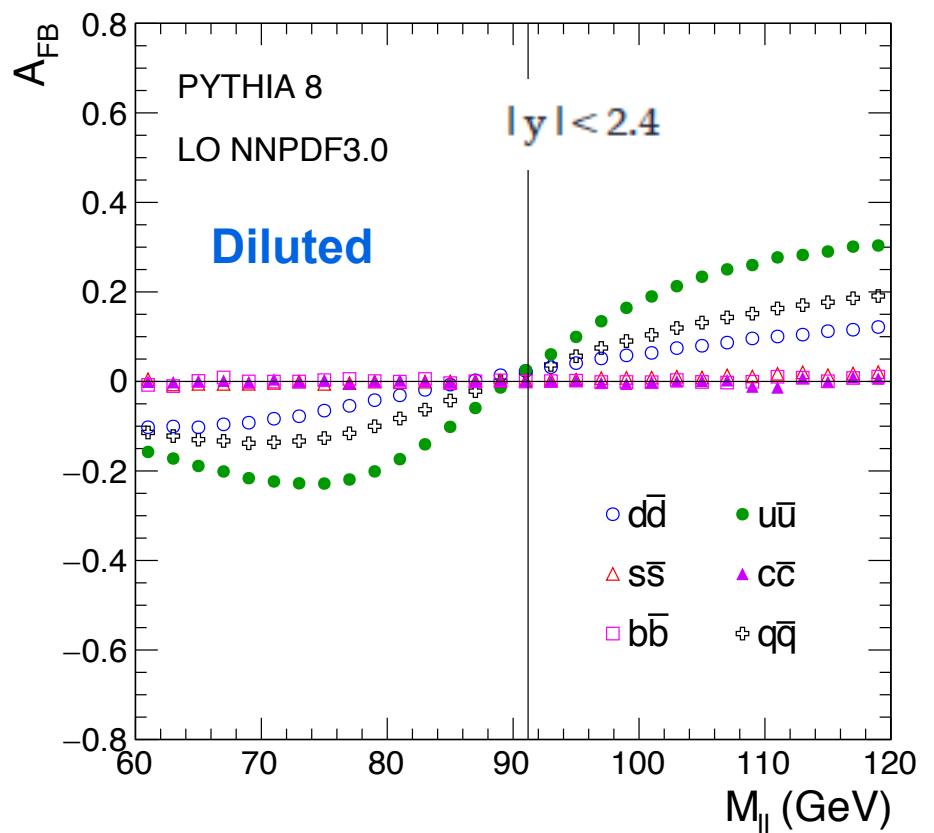
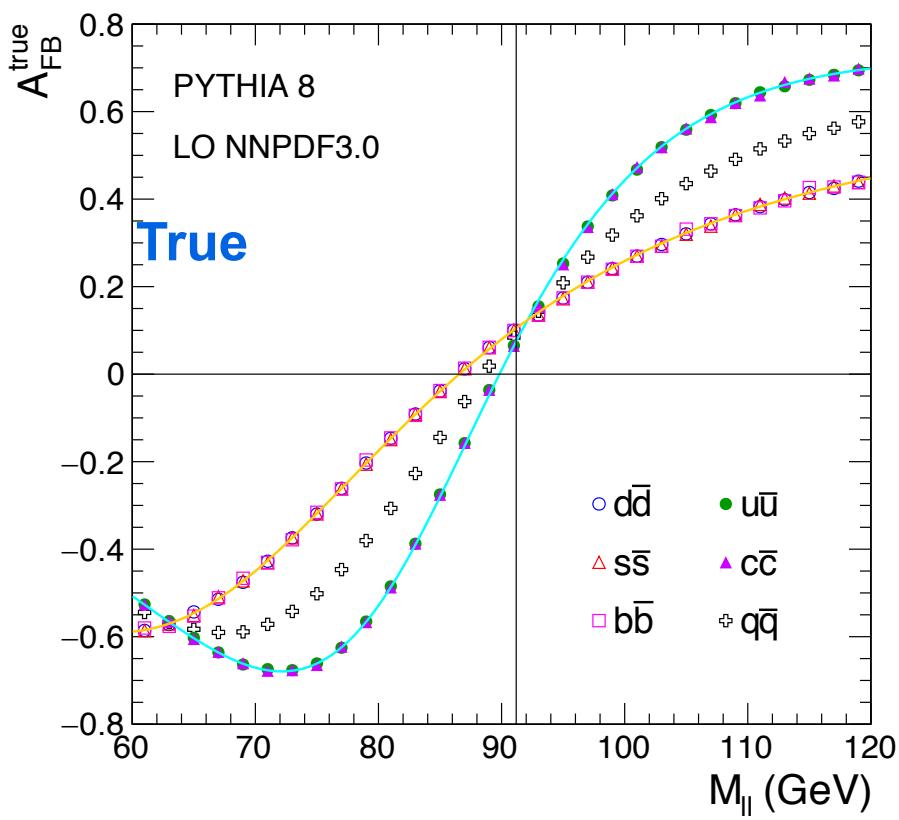
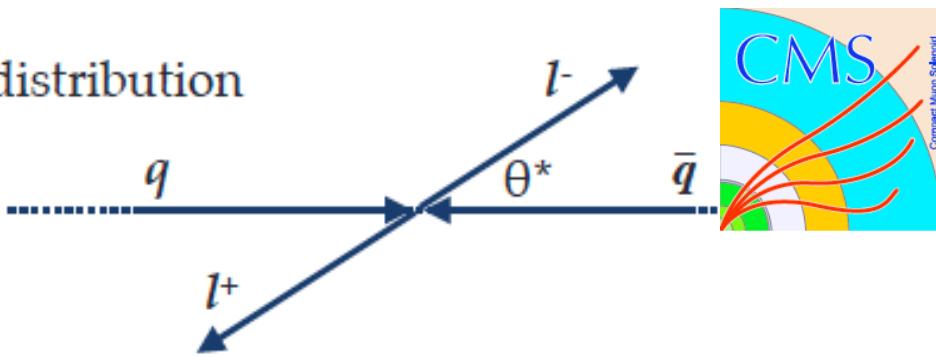
With a known Higgs mass, Standard Model is over constrained.  
A measurement of  $\sin^2\theta_{\text{eff}}$  is equivalent to a measurement of  $M_W$

**$\pm 0.00050$  error in  $\sin^2\theta_W$  is equiv. to  $\pm 25$  MeV error in  $M_W$  (indirect)**

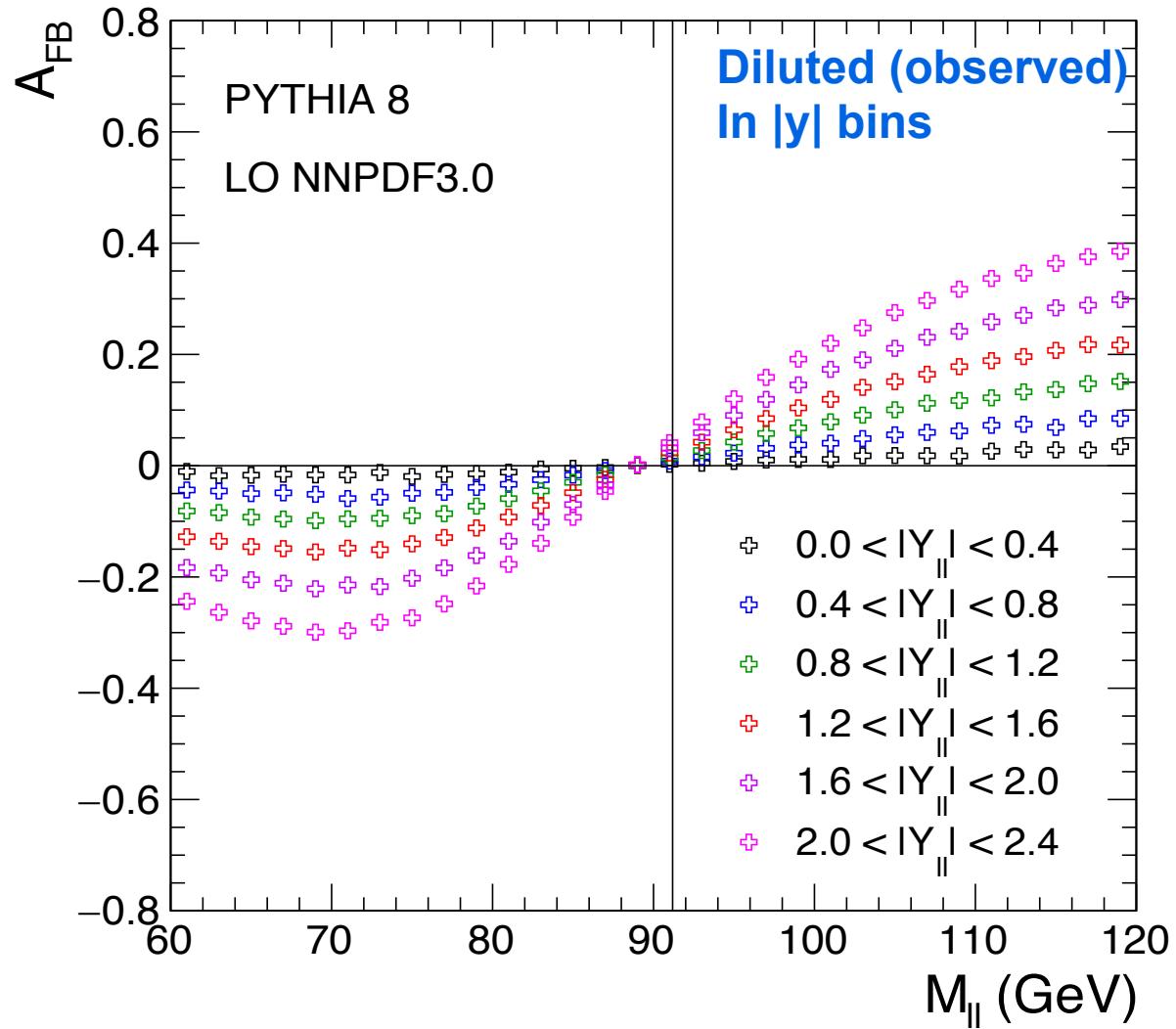
This new CMS measurement has a total error of  $\pm 0.00052$

All errors reported in this talk are quoted to five decimal places.

- Vector and axial couplings result in  $A_{FB}$  of  $\cos\theta^*$  distribution
- $A_{FB}$  near Z peak sensitive to leptonic  $\sin^2\theta_{eff}$
- Mass dependence from  $Z/\gamma^*$  interference
- Observable  $A_{FB}$  in  $pp$  collisions based on  $ll$  boost
- $A_{FB}$  dependence on PDFs:
  1. Fraction of valence u vs. d
  2. Dilution (y dependent) from high x antiquarks



- 6 bins of  $|y|$ : 0.0, 0.4, 0.8, 1.2, 1.6, 2.0, 2.4
- 12 bins of  $m$ : 60, 70, 78, 84, 87, 89, 91, 93, 95, 98, 104, 112, 120



Dilution ( $y$  dependent).  
Therefore bin data in  
rapidity.

Extract  $\sin^2\theta_{\text{eff}}$  by fitting  
the observed  $A_{FB}$  to  
templates generated with  
different values of  $\sin^2\theta_{\text{eff}}$

- Fit  $A_{FB}$  distribution in bins of  $m$  and  $|y|$  with different  $\sin^2\theta_{\text{eff}}$  templates



## A precision measurement using three new techniques:

1: Precise lepton momentum/energy scale (and modeling resolution)

Reduces contribution to  $\Delta \sin^2 \theta_{\text{eff}}$  to  $\pm 0.00008$

A. Bodek et al., "Extracting Muon Momentum Scale Corrections for Hadron Collider Experiments", *Eur. Phys. J.* C72 (2012) 2194,  
doi:10.1140/epjc/s10052-012-2194-8, arXiv:1208.3710.

2: Angular Event weighting method for  $A_{FB}$  analyses:

systematic errors in acceptance & efficiency cancel:  $\Delta \sin^2 \theta_{\text{eff}} \pm 0.00008$

A. Bodek, "A simple event weighting technique for optimizing the measurement of the forward-backward asymmetry of Drell-Yan dilepton pairs at hadron colliders", *Eur. Phys. J.* C67 (2010) 321–334, doi:10.1140/epjc/s10052-010-1287-5,  
arXiv:0911.2850.

3: New PDF constraints using the same Drell Yan Data above and below the Z peak. Reduced contribution to  $\Delta \sin^2 \theta_{\text{eff}}$  from  $\pm 0.00054$  to  $\pm 0.00030$ )<sup>a</sup>

A. Bodek, J. Han, A. Khukhunaishvili, and W. Sakumoto, "Using Drell-Yan forward-backward asymmetry to reduce PDF uncertainties in the measurement of electroweak parameters", *Eur. Phys. J.* C76 (2016), no. 3, 115,  
doi:10.1140/epjc/s10052-016-3958-3, arXiv:1507.02470.

**$\pm 0.00050$  error in  $\sin^2 \theta_W$  is equiv. to  $\pm 25$  MeV error in  $M_W$  (indirect)**



## Precise Lepton Energy/Momentum

New technique used for both  $\mu^+\mu^-$  and  $e^+e^-$  for both data and MC. Used in CDF and CMS for muons and electrons.

**Step I : Remove the correlations between the scale for the two leptons** by getting an initial calibration using Z events and requiring that the mean  $\langle 1/P_T \rangle$  of each lepton in bins of  $\eta$ ,  $\Phi$  and charge be correct.

**Step II: The Z mass used as a reference scale.** The Z mass as a function of  $\eta$ ,  $\Phi$ , (and charge for  $\mu^+\mu^-$ ) of each lepton be correct (done in bins of  $\eta$ ,  $\Phi$  ).

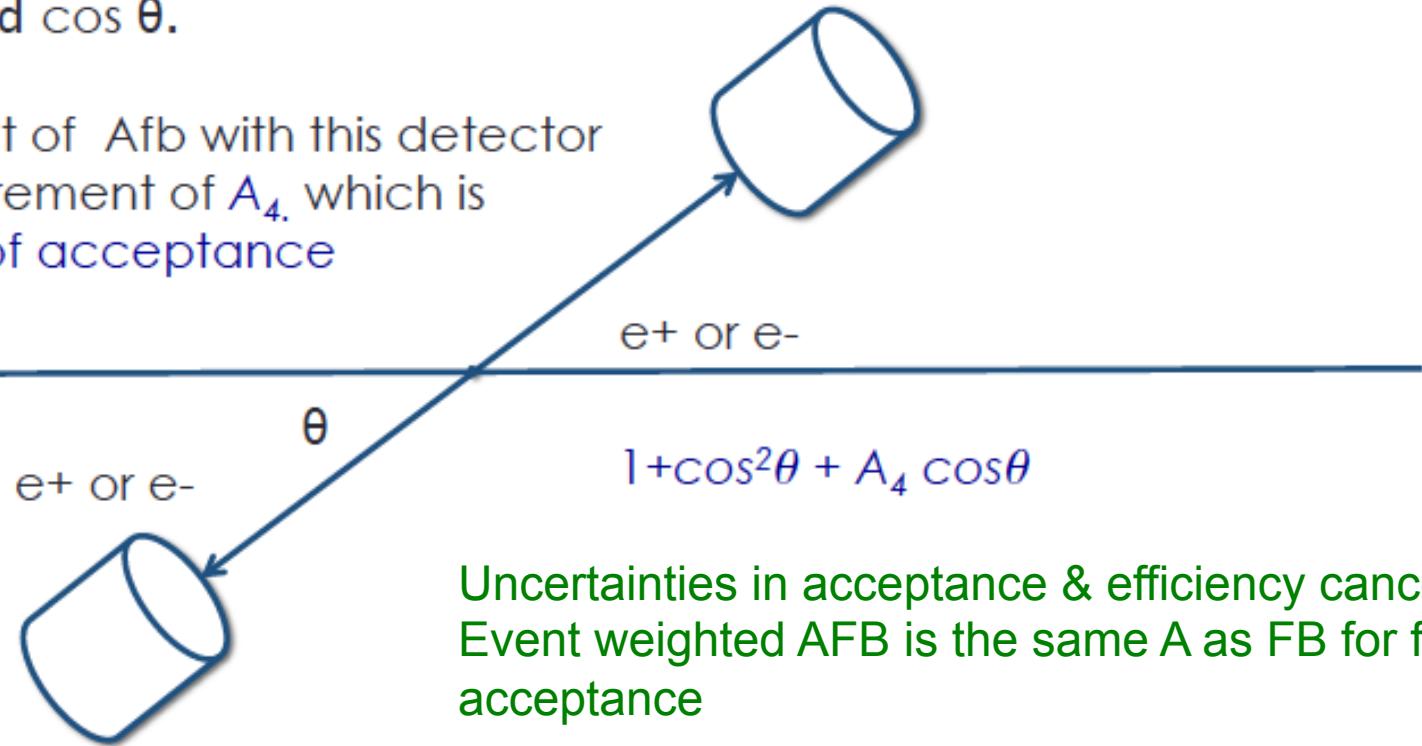
- **Reference scale for muons:** Expected Z mass (post FSR) smeared by resolution (with acceptance cuts). ( J/ $\Psi$  and Y are also used for tuning dE/dx).
- **Reference scale for electrons:** Expected Z mass post FSR with FSR photons clustered to form a dressed electron ) smeared by resolution (with acceptance cuts).
- Usually, both data and MC are misaligned (or mis-calibrated for electrons)  
Corrections must be apply to both data and MC to agree with the Z reference scale.

## Angular event weighting method (used in CMS and CDF)



Imagine a detector with acceptance for only one value of  $\cos \theta$ . Each event has a measured  $\cos \theta$ .

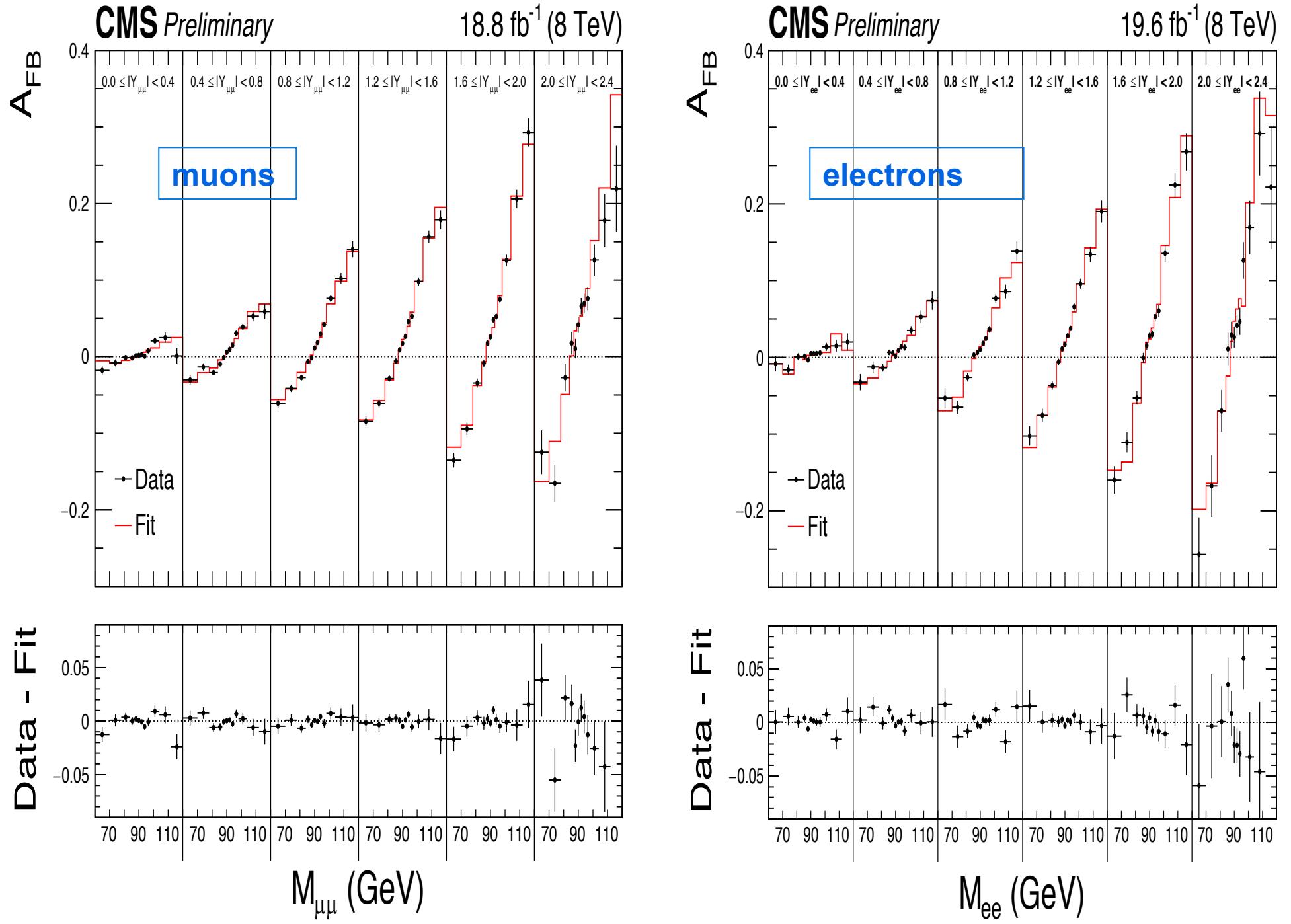
A measurement of  $A_{fb}$  with this detector yields a measurement of  $A_4$ , which is independent of acceptance or efficiency



$\cos \theta = 1$  yields best measurement of  $A_4$ .  $\cos \theta = 0$  yields no measurement of  $A_4$

We can combine measurements of  $A_4$  with different detectors at different values of  $\theta$  by weighting events. Events with  $\cos \theta = 0$  have zero weight. Events with  $\cos \theta = 1$  have maximum weight. → obtain smaller statistical error.

$$A_{fb} (\text{all } \cos \theta) = (3/8) A_4 \rightarrow \text{No acceptance corrections needed.}$$





channel	statistical uncertainty
muon	0.00044
electron	0.00060
combined	0.00036

Combined  $\pm 0.00036$  (stat)

Source	muons	electrons
MC statistics	0.00015	0.00033
Lepton momentum calibration	0.00008	0.00019
Lepton selection efficiency	0.00005	0.00004
Background subtraction	0.00003	0.00005
Pileup modeling	0.00003	0.00002
Total	0.00018	0.00039

Combined  $\pm 0.00018$  (syst)

model variation	Muons	Electrons
Dilepton $p_T$ reweighting	0.00003	0.00003
QCD $\mu_R/F$ scale	0.00011	0.00013
POWHEG MiNLO Z+j vs NLO Z model	0.00009	0.00009
FSR model (PHOTOS vs PYTHIA)	0.00003	0.00005
UE tune	0.00003	0.00004
Electroweak ( $\sin^2 \theta_{\text{eff}}^{\text{lept}} - \sin^2 \theta_{\text{eff}}^{\text{u, d}}$ )	0.00001	0.00001
Total	0.00015	0.00017

Combined  $\pm 0.00016$  (theory)

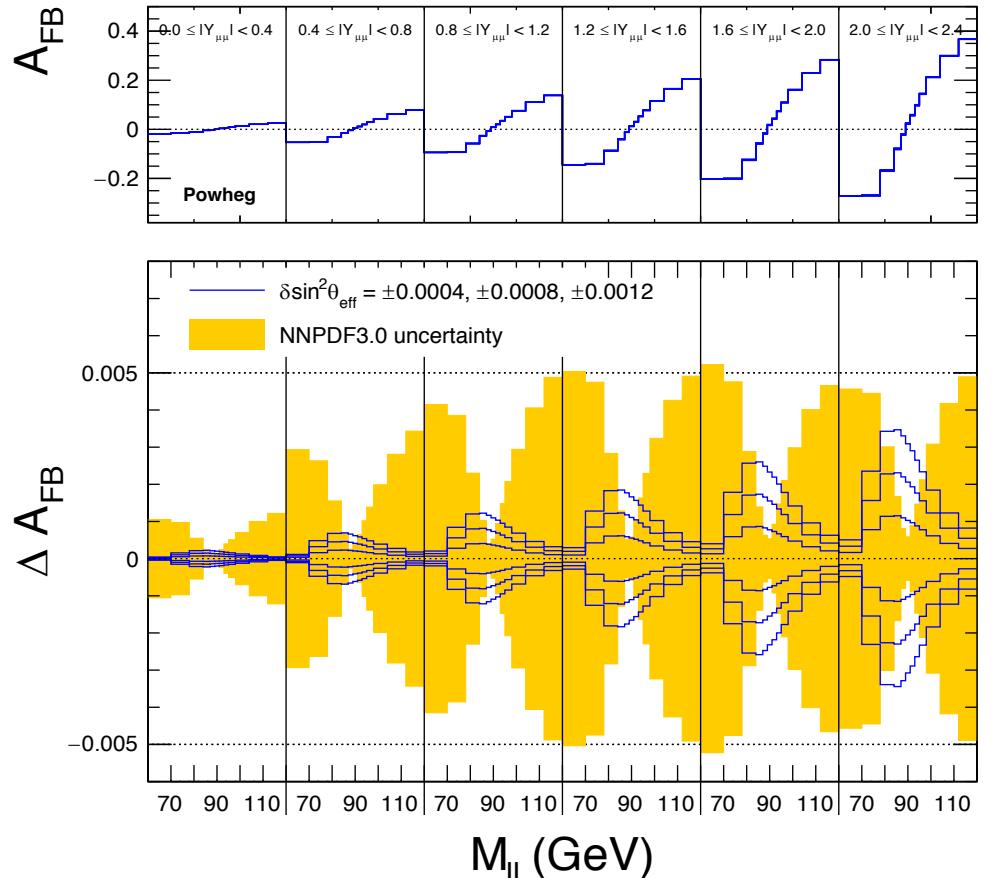
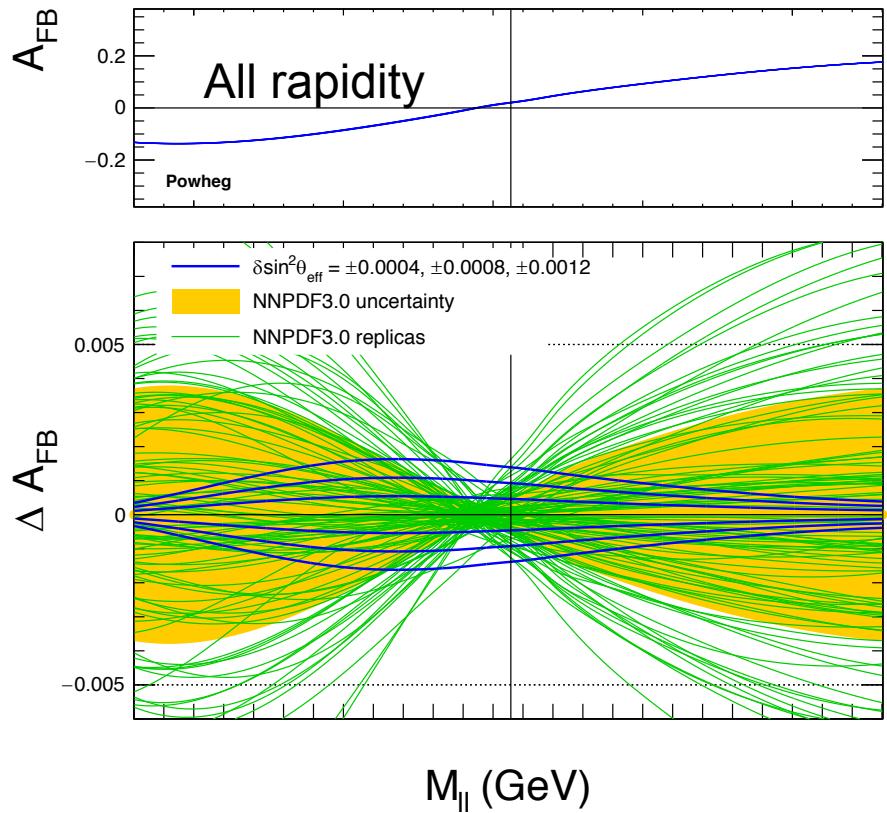
$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = 0.23101 \pm 0.00036(\text{stat}) \pm 0.00018(\text{syst}) \pm 0.00016(\text{theory})$$



Vary  $\sin^2\theta_{\text{eff}}$  for fixed PDF in **GREEN** (left), **PURPLE** (right)

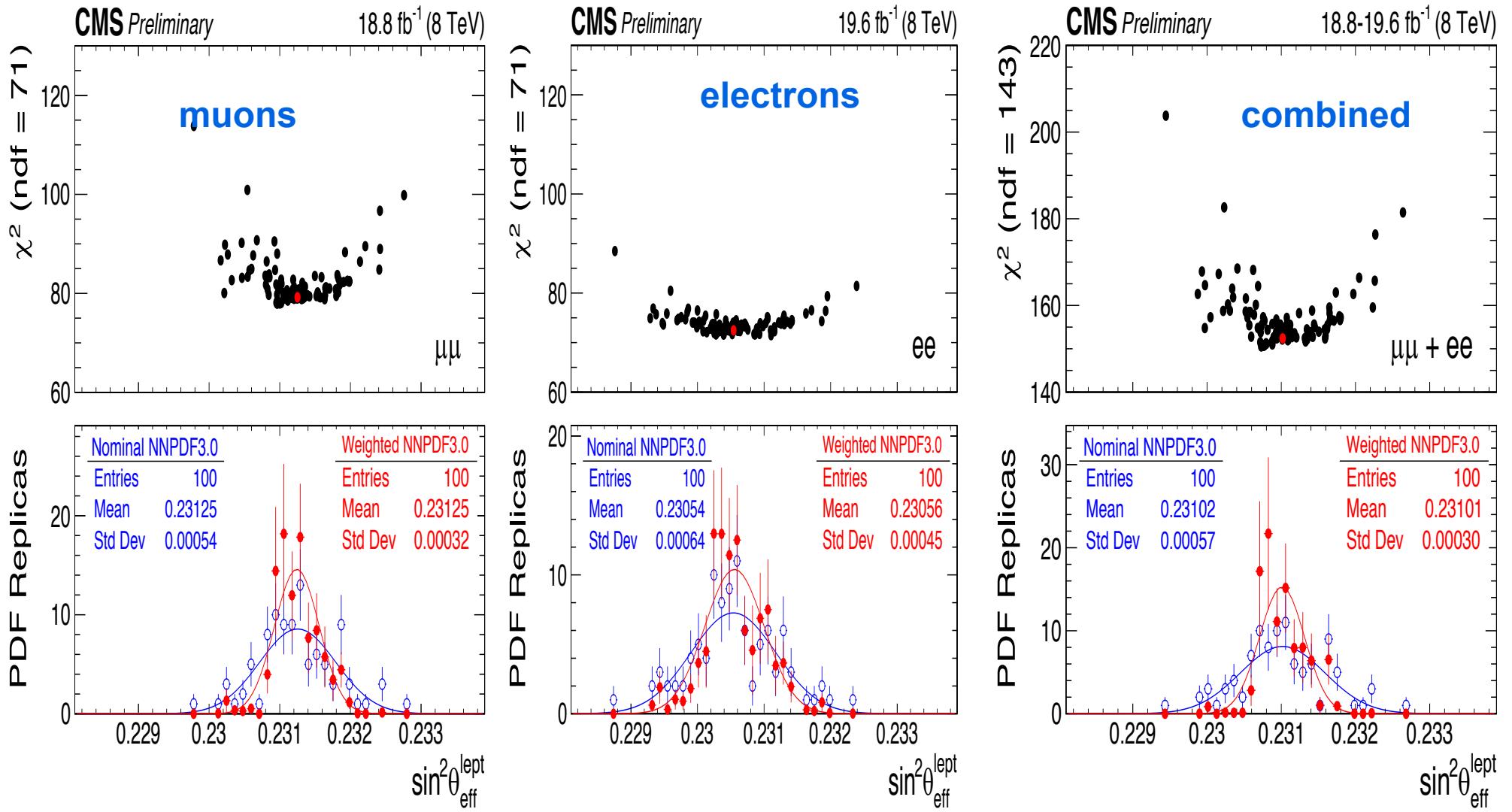
Vary 100 NNPDF replicas for fixed  $\sin^2\theta_{\text{eff}}$  in **ORANGE**

- Observed  $A_{\text{FB}}$  is very sensitive to PDFs
- Large in low and high masses, small near the peak (+ specific dependence on  $Y$ )



- Perform  $\sin^2\theta_{\text{eff}}$  fit for each PDF replica  
(by default we use NNPDF3.0)
- Weight each replica by

$$w_i = \frac{e^{-\frac{\chi^2}{2}}}{\frac{1}{N} \sum_{i=1}^N e^{-\frac{\chi^2}{2}}}$$

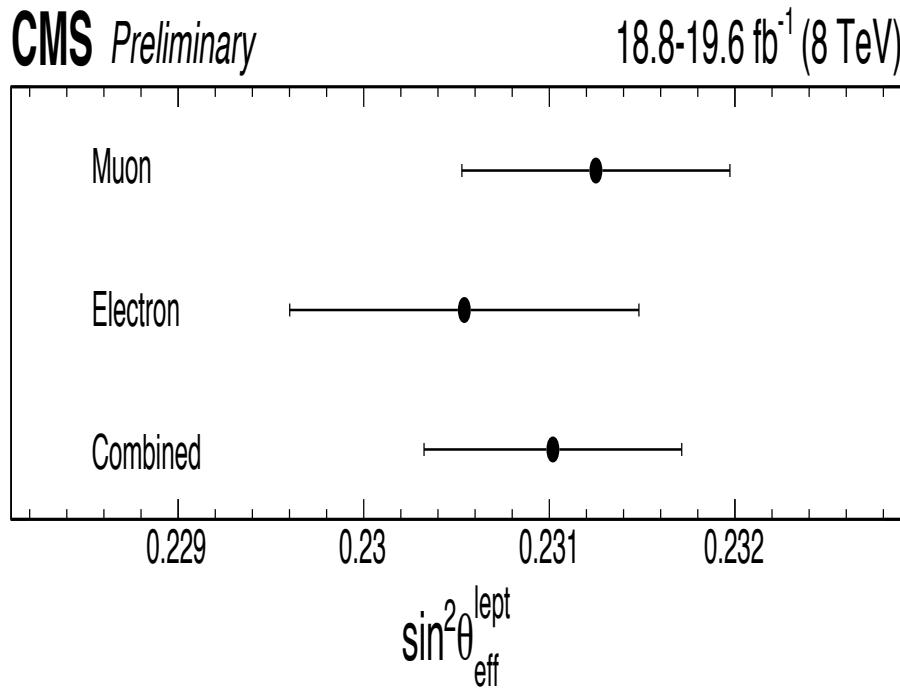


Channel	without constraining PDFs	with constraining PDFs
Muon	$0.23125 \pm 0.00054$	$0.23125 \pm 0.00032$
Electron	$0.23054 \pm 0.00064$	$0.23056 \pm 0.00045$
Combined	$0.23102 \pm 0.00057$	$0.23101 \pm 0.00030$

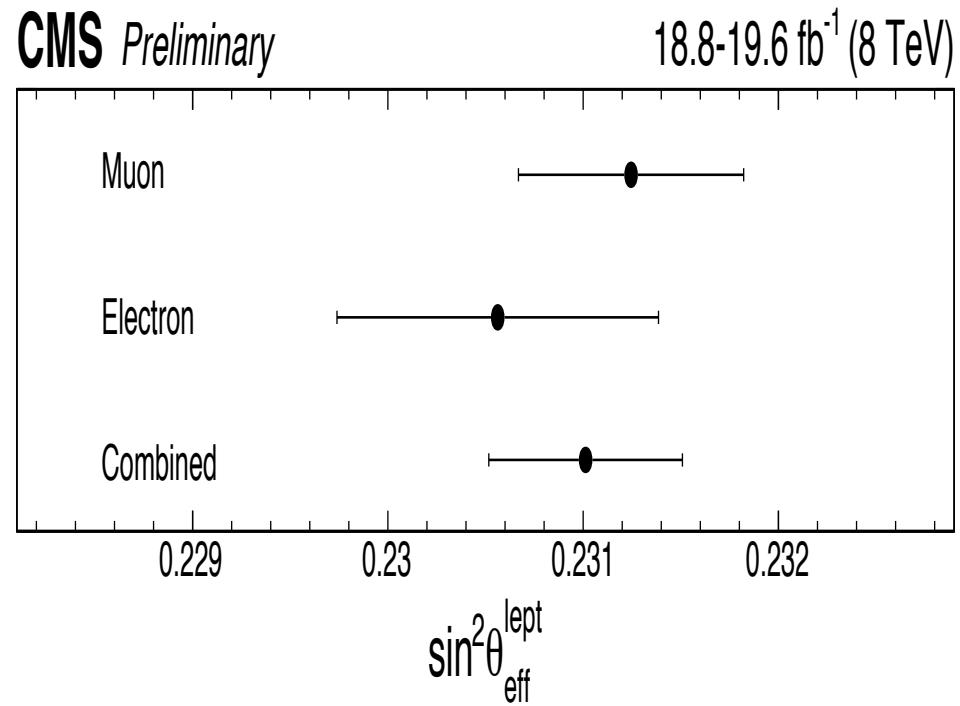
With larger statistical samples and new analysis techniques (including **precise lepton scale calibration**, **angular event weighting** and **additional PDF constraints**) the errors are significantly reduced.



### PDF nominal



### With PDF re-weighting constraints



Channel	without constraining PDF	with constraining PDFs
Muon	$0.23125 \pm 0.00048 \pm 0.00054$	$0.23125 \pm 0.00048 \pm 0.00032$
Electron	$0.23054 \pm 0.00069 \pm 0.00064$	$0.23056 \pm 0.00069 \pm 0.00054$
Combined	$0.23102 \pm 0.00040 \pm 0.00057$	$0.23101 \pm 0.00040 \pm 0.00030$

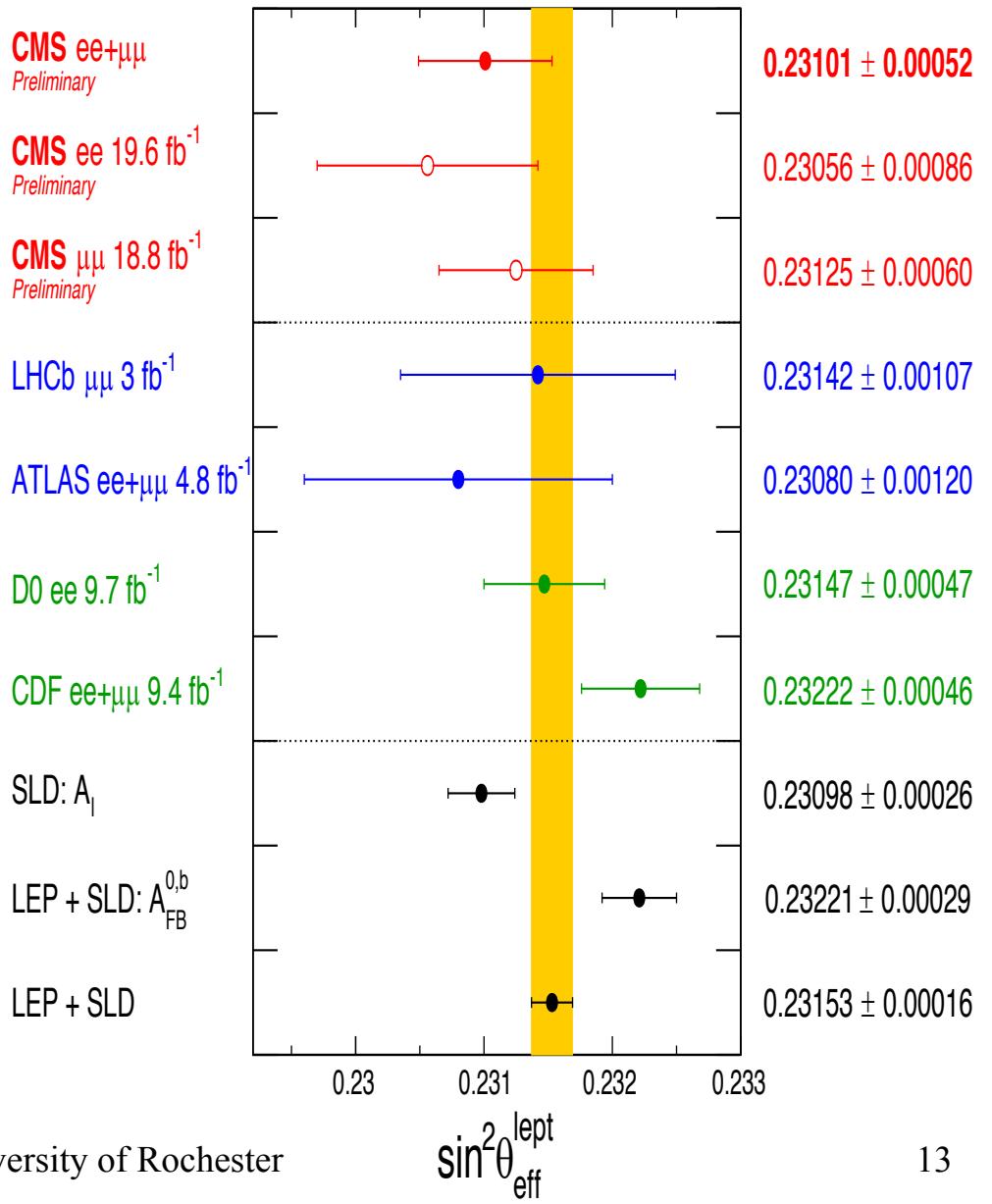
$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = 0.23101 \pm 0.00036(\text{stat}) \pm 0.00018(\text{syst}) \pm 0.00016(\text{theory}) \pm 0.00030(\text{pdf})$$

$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = 0.23101 \pm 0.00052.$$

## Results



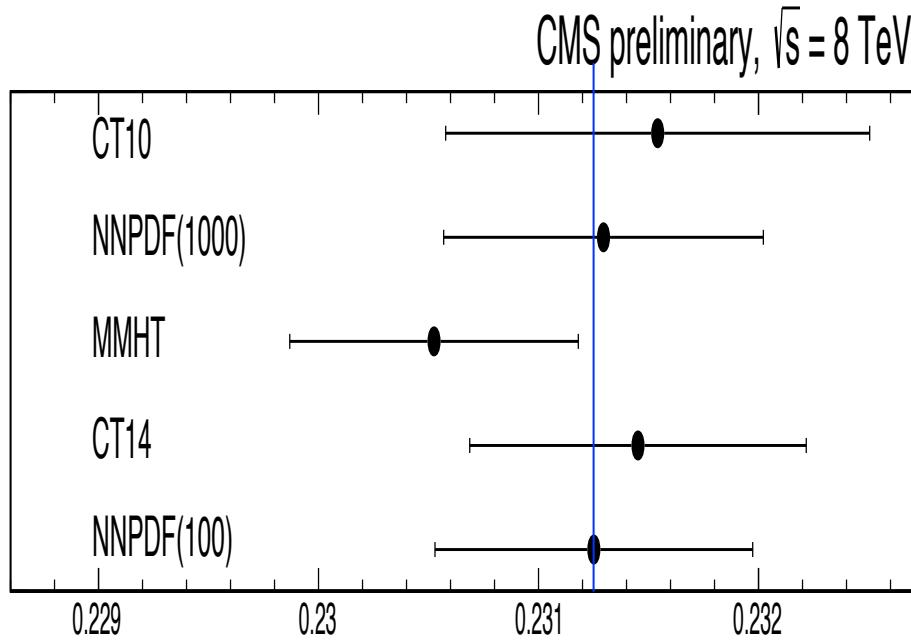
- Measured  $\sin^2 \theta_{\text{eff}}$  8 TeV  $\mu\mu$  and ee
- Statistical uncertainty dominates
- Followed by PDF (reduced with reweighting by ~50%)
- Experimental uncertainties small
  - MC statistics (dominates)
  - lepton calibration
  - lepton selection efficiencies
  - background estimate
  - pileup
- Modeling errors dominated by QCD





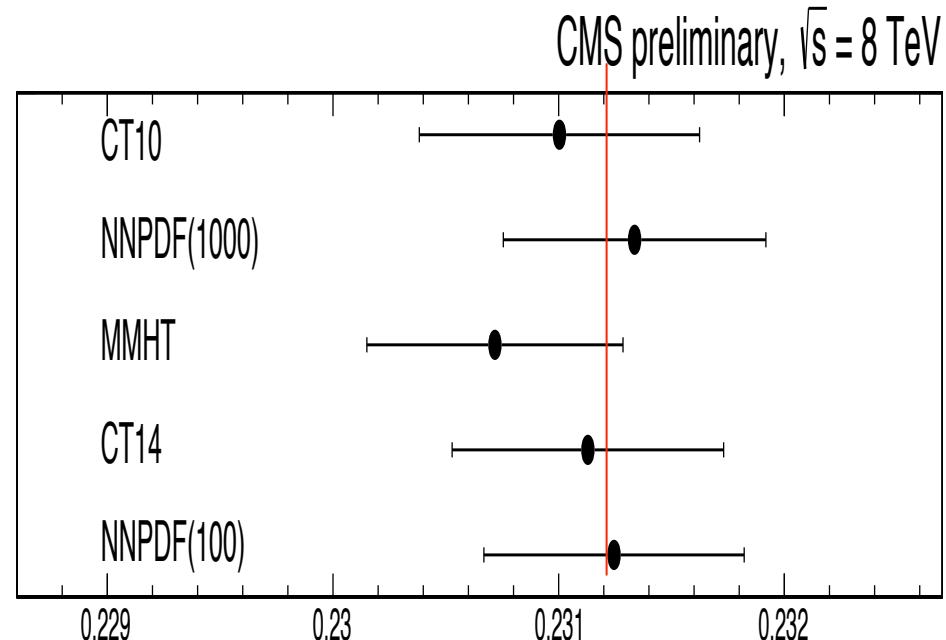
# Additional Slides

## PDF nominal



$$\sin^2 \theta_{\text{eff}}^{\text{lept}}$$

## With PDF re-weighting constraints

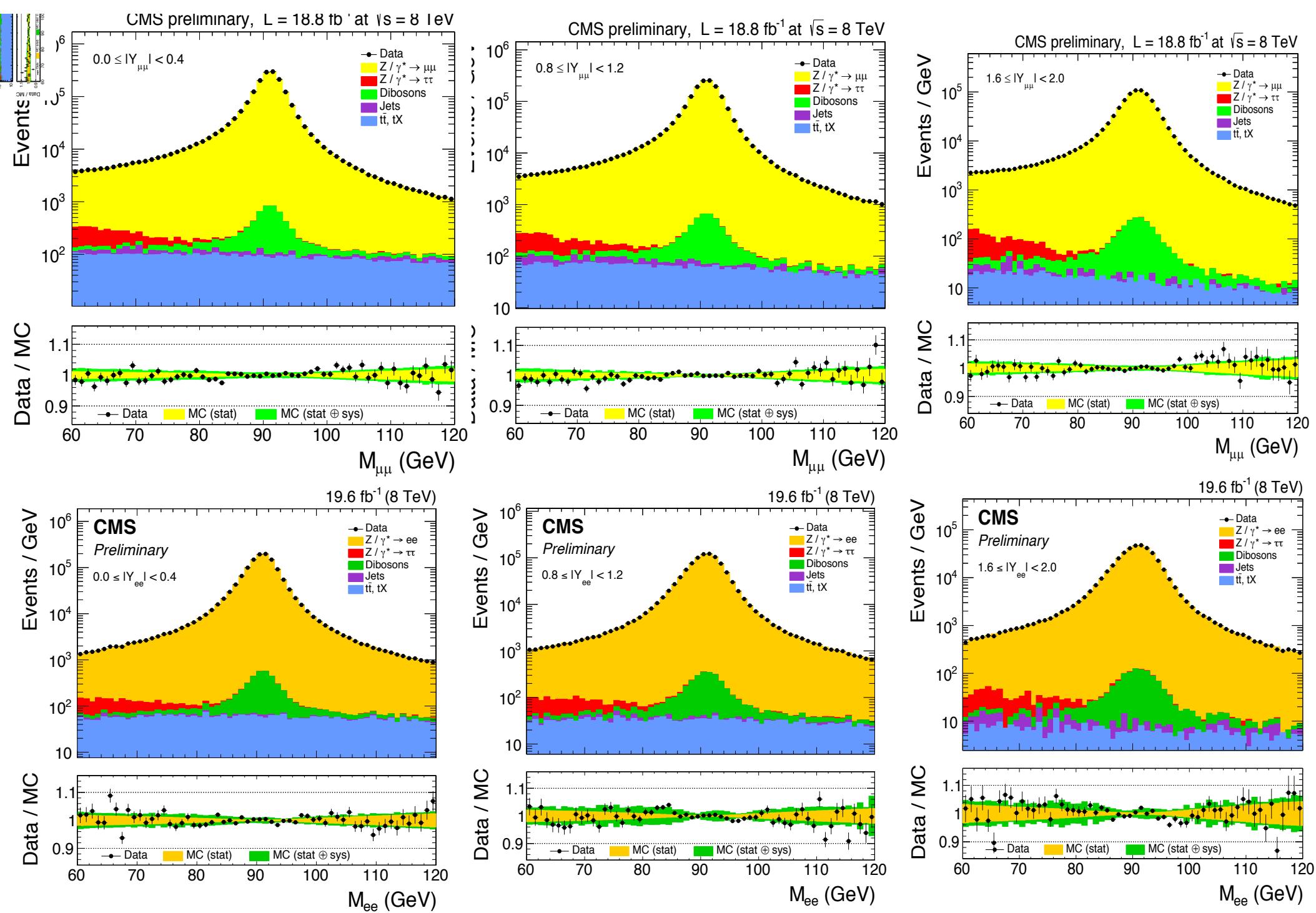


$$\sin^2 \theta_{\text{eff}}^{\text{lept}}$$

**PDF reweighting constraints reduce PDF error by factor of 2**

**With constraints from PDF reweighting the extracted values for different PDF are closer to each other**

Figure 8: Extracted values of  $\sin^2 \theta_{\text{eff}}^{\text{lept}}$  from the dimuon data for different PDF sets with nominal (left) and  $\chi^2$  reweighted (right) PDF replicas. The error bars include the statistical, experimental and the PDF uncertainties.



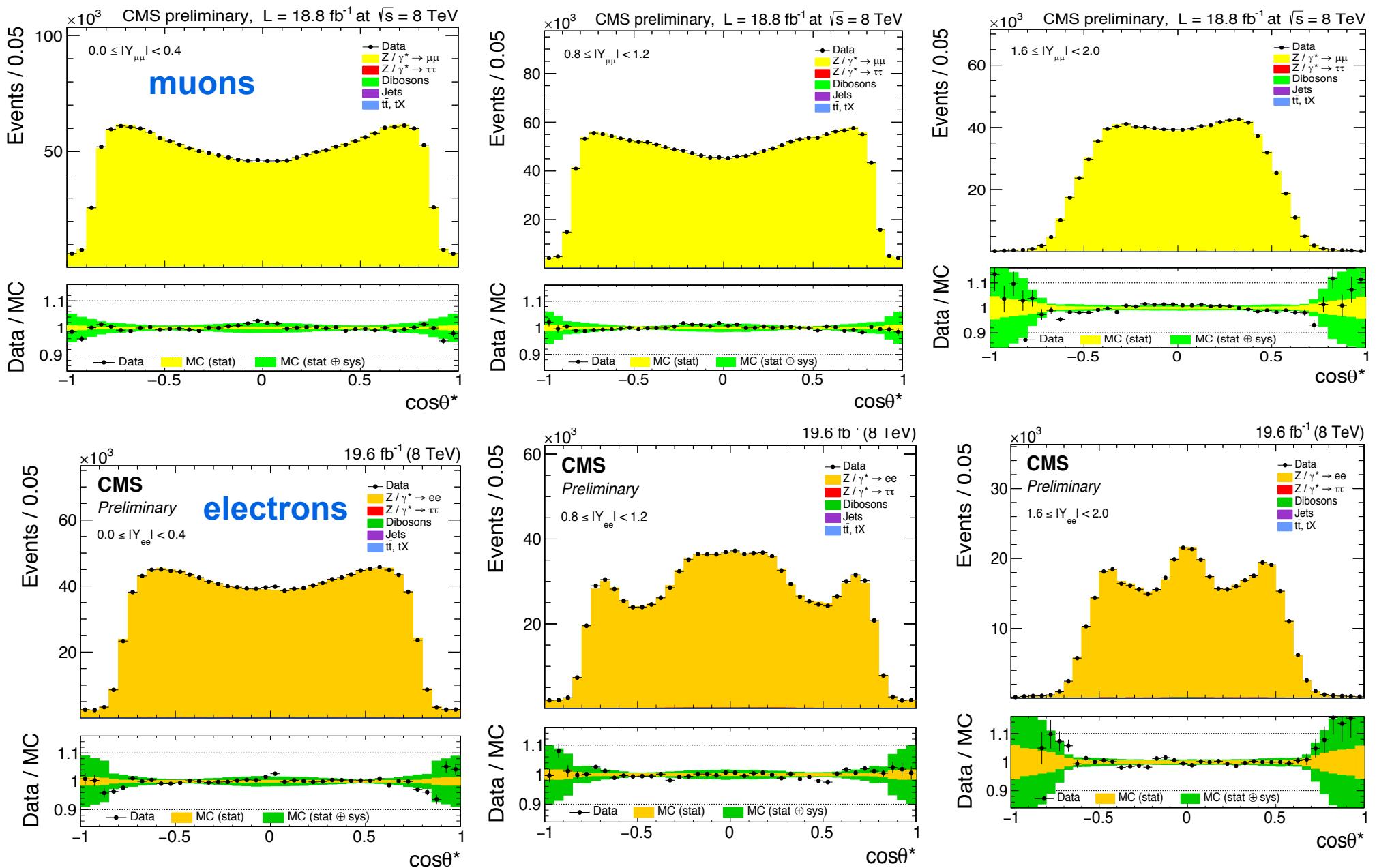


Figure 3: The muon (top) and electron (bottom)  $\cos\theta^*$  distributions in three representative rapidity bins:  $|Y_{ll}| < 0.4$  (left),  $0.8 < |Y_{ll}| < 1.2$  (middle), and  $1.6 < |Y_{ll}| < 2.0$  (right).

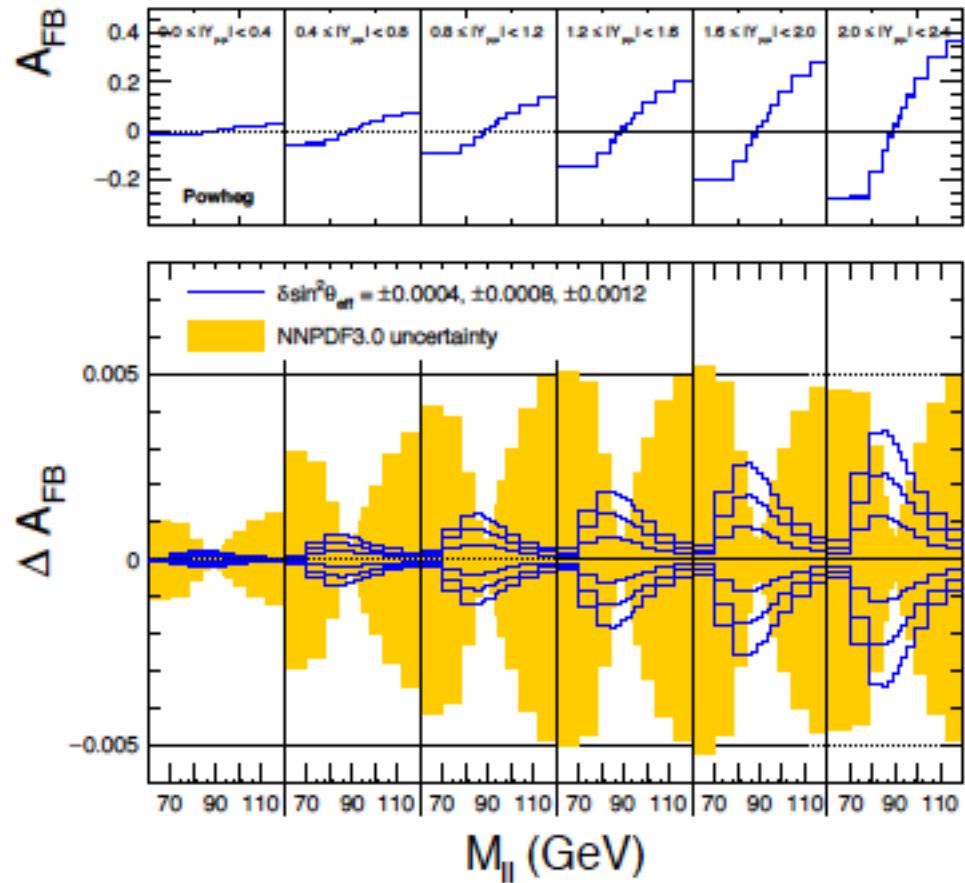
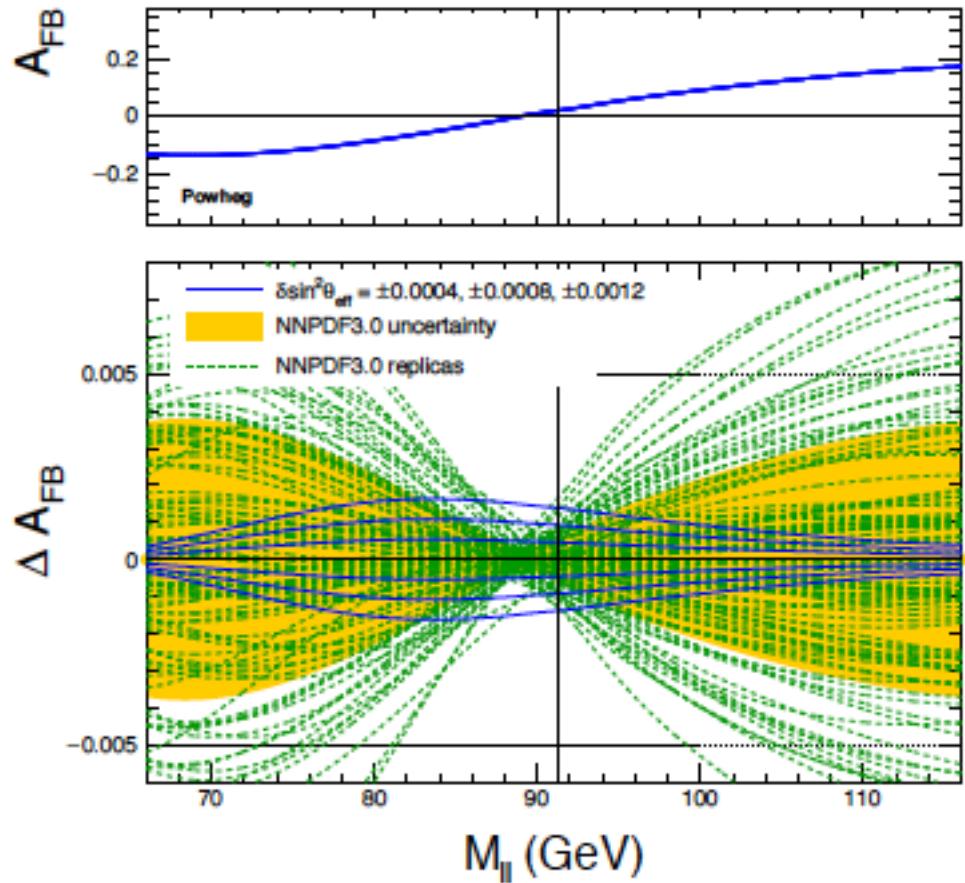


Figure 5: Distribution of  $A_{FB}$  as a function of mass integrated over rapidity (left) and in six rapidity bins (right) for  $\sin^2 \theta_{\text{eff}}^{\text{lept}} = 0.23120$ . The solid lines in the bottom panel correspond to six variations of  $\sin^2 \theta_{\text{eff}}^{\text{lept}}$  around the central value:  $\pm 0.00040$ ,  $\pm 0.00080$  and  $\pm 0.00120$ . The dashed lines correspond to  $A_{FB}$  predictions for 100 NNPDF3.0 replicas. The shaded band illustrates the standard deviation over the NNPDF3.0 replicas.