

# Implications of Vector Boson Scattering Unitarity in Composite Higgs Models

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arXiv:1705.02787

EPS2017, Venice, July 7, 2017

# Introduction

- Despite its incredible success, the SM is plagued by several problems.
- Composite Higgs (CH) models are among the most promising alternatives,
- dynamically generating the EW scale through a vacuum condensate misaligned with the vacuum that breaks EW symmetry

$$v = f \sin \theta$$

- and at the same time explaining the mass gap between the Higgs and the other composite states → Higgs = Goldstone boson of spontaneous symmetry G/H.

- A striking evidence of strong dynamics is the growing (with  $E^2$ ) behavior of **Goldstone Boson Scattering (GBS)** amplitudes

$$\mathcal{A}(\pi\pi \rightarrow \pi\pi) \sim \frac{s}{f^2} = \frac{s}{v^2} \sin^2 \theta,$$

- controlled by strong effects at high energies, **broad continuum** or **composite resonances**, saturating unitarity - similar to hadron physics.
- **Perturbative unitarity** is a powerful tool to assess the **scale of strong effects** and properties of the composite spectrum.

# Effective Lagrangian

- The **(pseudo-)Goldstone bosons** can be described by the CCWZ construction, at  $d = 2$ ,

$$\mathcal{L}_2 = \frac{1}{2} f^2 \langle x_\mu x^\mu \rangle$$

- Higgs coupling  $hVV$  deviation (mainly)  $\sim \cos \theta$  disturbs EWPO

$$\sin \theta \lesssim 0.2 \quad (\text{EWPO})$$

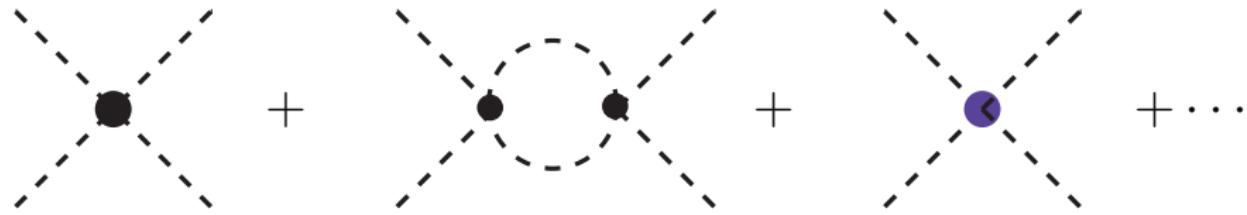
- Different origins of vacuum alignment in effective potential typically implies not so small  $\theta$  (model dependent)
- To analyze perturbative unitarity it is imperative to include higher order terms  $\rightarrow$  together with high dimensional operators. At  $d = 4$ ,

$$\begin{aligned}\mathcal{L}_4 &= L_0 \langle x^\mu x^\nu x_\mu x_\nu \rangle + L_1 \langle x^\mu x_\mu \rangle \langle x^\nu x_\nu \rangle \\ &+ L_2 \langle x^\mu x^\nu \rangle \langle x_\mu x_\nu \rangle + L_3 \langle x^\mu x_\mu x^\nu x_\nu \rangle\end{aligned}$$

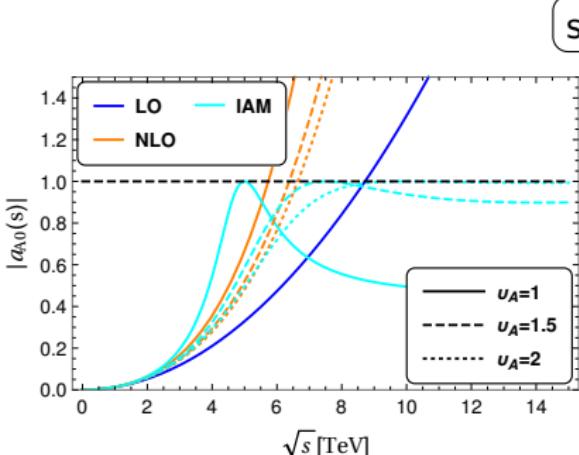
# Unitarity of GBS amplitudes

- Consider  $\pi^a \pi^b \rightarrow \pi^c \pi^d$  scattering amplitude in  $SU(4)/Sp(4)$ . Expand in  $Sp(4)$  channels  $\mathbf{5} \otimes \mathbf{5} = \mathbf{1} \oplus \mathbf{10} \oplus \mathbf{14} \equiv \mathbf{A} \oplus \mathbf{B} \oplus \mathbf{C}$  and partial waves,  $J$
- Focus on  $\mathbf{A}$   $J=0$  channel for this talk
- In this basis, **elastic unitarity** condition read

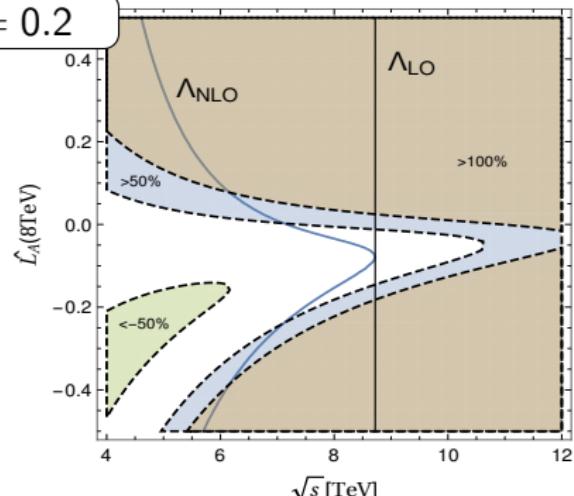
$$\begin{aligned} a_{A0}(s) &= a_{A0}^{(0)}(s) + a_{A0}^{(1)}(s) + \dots & \text{Im } a_J(s) = |a_J(s)|^2 \\ a_{A0}^{(0)}(s) &= \frac{s}{16\pi f^2} & \boxed{\text{Im } a_J^{(1)}(s) = |a_J^{(1)}(s)|^2} \\ a_{A0}^{(1)}(s) &= \frac{s^2}{32\pi f^4} \left[ \frac{1}{16\pi^2} \left( \frac{29}{12} + \frac{46}{18} \log \left( \frac{s}{\mu^2} \right) + 2\pi i \right) + \frac{2}{3} \widehat{L}_A(\mu) \right] \end{aligned}$$



- **Unitarity/Perturbativity test**  $|a(s)| < 1$ .
- LO prediction is conservative. NLO corrections anticipate unitarity violation.
- Unitarity implies an eventual resonance is lighter than  $M_\sigma \lesssim 1.75/\sin\theta$  TeV.
- Lattice results  $M_\sigma = 4.7(2.6)/\sin\theta$  TeV (2 Dirac fermions in fundamental of SU(2), Arthur, Drach, Hansen, Hietanen, Pica, Sannino 16')
- **Inverse Amplitude Method (IAM)** is an Unitarization Model.  
Guidance for how the full non-perturbative amplitude could look like.



$$\sin\theta = 0.2$$



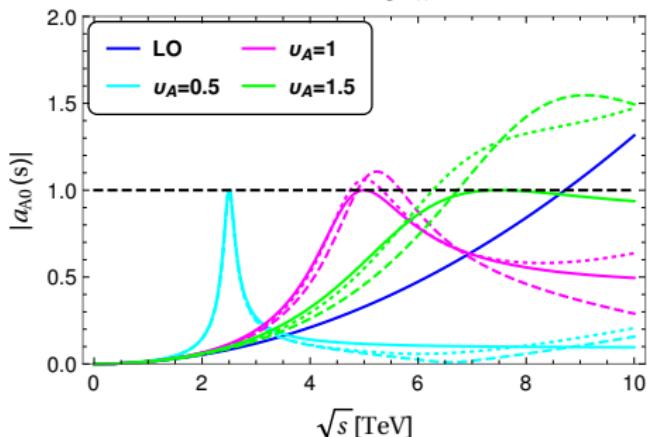
# The $\sigma$ resonance

$$\mathcal{L}_\sigma = \frac{1}{2}\kappa(\sigma)f^2\langle x_\mu x^\mu \rangle + \frac{1}{2}\partial_\mu\sigma\partial^\mu\sigma - \frac{1}{2}M_\sigma^2\sigma^2$$



$$a_{A0}^\sigma(s) = \frac{g_\sigma^2}{32\pi f^2} \left( \frac{5s^2}{m_\sigma^2 - i\Gamma_\sigma m_\sigma - s} - 2m_\sigma^2 + \frac{2m_\sigma^4 \log\left(\frac{s}{m_\sigma^2} + 1\right)}{s} + s \right)$$

$$v_A \equiv \frac{m_\sigma \sin \theta}{\text{TeV}}, \quad \Gamma_\sigma \sim 5 \frac{g_\sigma^2 m_\sigma^3}{32\pi f^2}, \quad \kappa(\sigma) = 1 + \kappa' \sigma/f + \kappa'' \sigma^2/(2f) + \dots$$



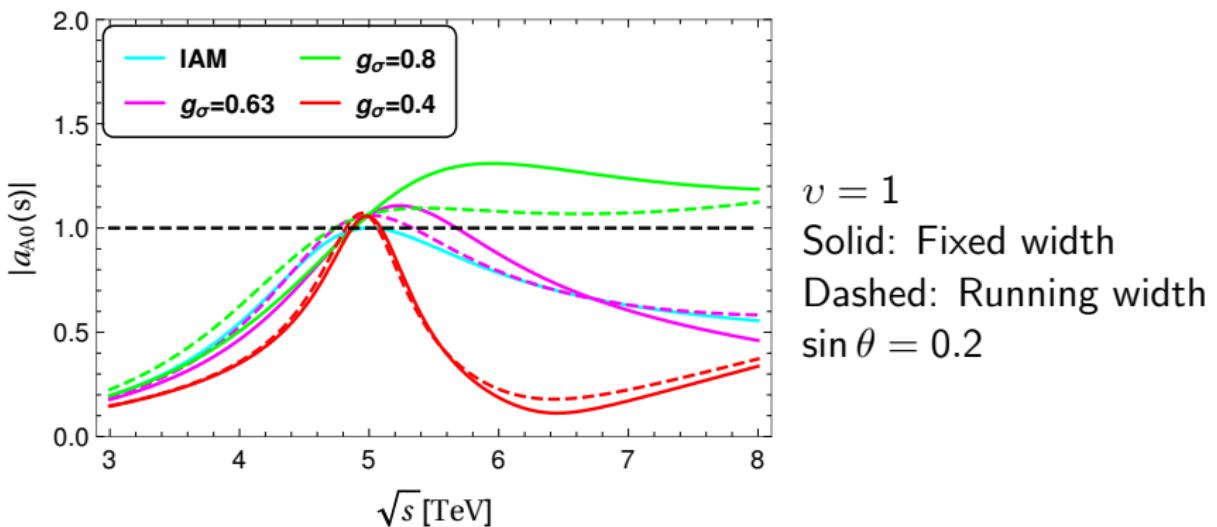
$$g_\sigma \equiv \kappa'/2 \sim \sqrt{2/5} \sim 0.63$$

Dashed: Fixed width

Dotted: Running width

Solid: IAM

$$\sin \theta = 0.2$$

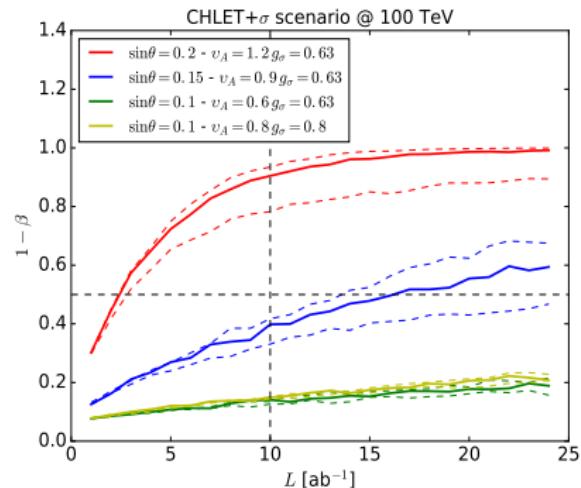
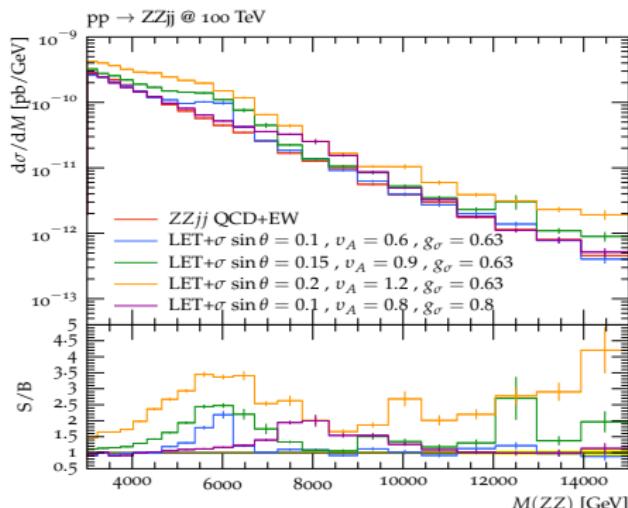


Unitarity and perturbativity give further information about effective Lagrangian beyond pure dimensional analysis:

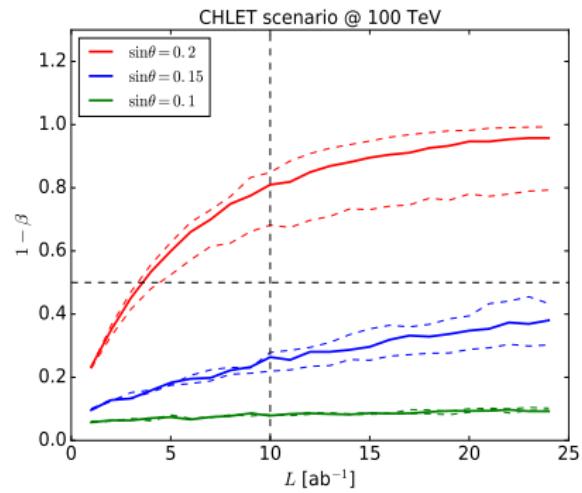
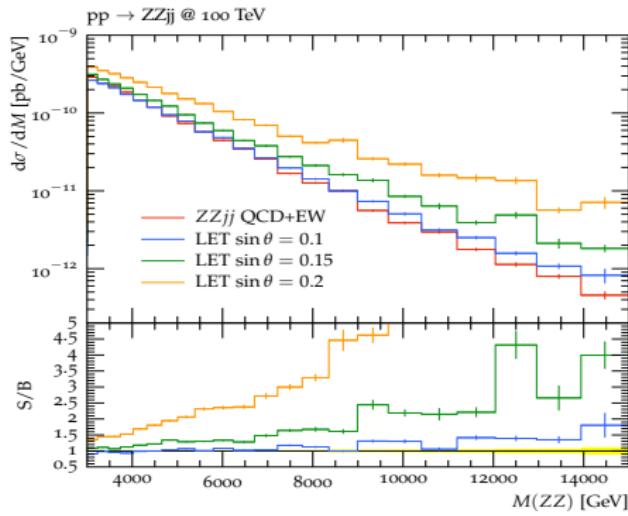
$$g_\sigma \lesssim 0.8 \text{ and } M_\sigma \lesssim \frac{1.2}{\sin \theta} \text{ TeV}$$

# Strong VBS in $pp \rightarrow jjZZ \rightarrow jj4\ell$

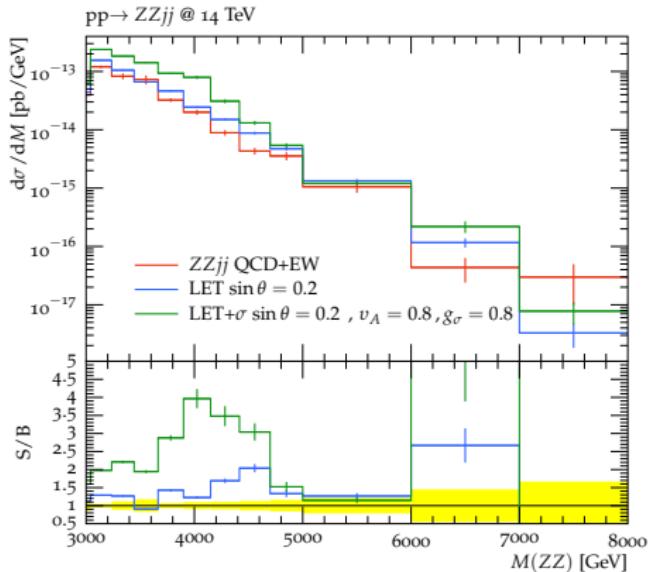
- **Scalar  $\sigma$  resonance at 100 TeV**
- Models implemented via FEYNRULES in UFO format and events generated with SHERPA generator.
- Typical VBS kinematical cuts applied.
- Mixing  $h - \sigma$  very small  $\alpha \sim \frac{2m_h^2}{m_\sigma^2}$ , suppressed gluon fusion.



# LET no-resonant enhancement at 100 TeV: Conservative scenario, unitarity violation highly suppressed for $\sin \theta < 0.2$



## $\sigma$ resonance at the LHC



- $\sigma \sim 2.9 \times 10^{-4}$  ab very small.
- Other VBS channels imperative for this search.
- Gluon fusion contribution could help.

# Conclusion

- Perturbative unitarity gives valuable information about spectrum and couplings of composite sector in CH models. Beyond simple dimensional analysis.
- Scalar sector:  $\sigma$  resonance,  $g_\sigma \lesssim 0.8$  and  $M_\sigma \lesssim 1.2/\sin\theta$  TeV or *continuum* (vector sector not discussed in this talk, but present in the paper).
- A 100 TeV collider is more appropriate to observe strong effects of CH models in VBS,
- but LHC may be able in a very optimistic case, usually not considered. More study necessary.

- Vacuum  $\Sigma_0 = \cos \theta \Sigma_B + \sin \theta \Sigma_H$ .
- Minimization  $\cos \theta_{min} = \frac{2C_m}{y_t' C_t}$ , for  $y_t' C_t > 2|C_m|$ .
- Generators

$$\begin{aligned} V^a \cdot \Sigma_0 + \Sigma_0 \cdot V^{aT} &= 0, & S^a \cdot \Sigma_B + \Sigma_B \cdot S^{aT} &= 0, \\ Y^a \cdot \Sigma_0 - \Sigma_0 \cdot Y^{aT} &= 0. & X^a \cdot \Sigma_B - \Sigma_B \cdot X^{aT} &= 0, \end{aligned}$$

$$U = \exp \left[ \frac{i\sqrt{2}}{f} \sum_{a=1}^5 \pi^a Y^a \right],$$

$$\begin{aligned} \omega_\mu &= U^\dagger D_\mu U, \\ D_\mu &= \partial_\mu - ig W_\mu^i S^i - ig' B_\mu S^6, \\ x_\mu &= 2\text{Tr}[Y_a \omega_\mu] Y^a, \\ s_\mu &= 2\text{Tr}[V_a \omega_\mu] V^a. \end{aligned}$$

# Hidden Local Symmetry (HLS)

- Enhance the symmetry group  $SU(4)_0 \times SU(4)_1$ , and embed the SM gauge bosons in  $SU(4)_0$  and the heavy resonances in  $SU(4)_1$ .  $SU(4)_i \rightarrow Sp(4)_i$ .  
 $Sp(4)_0 \times Sp(4)_1 \rightarrow Sp(4)$  by a sigma field  $K$

$$U_0 = \exp \left[ \frac{i\sqrt{2}}{f_0} \sum_{a=1}^5 (\pi_0^a Y^a) \right], \quad U_1 = \exp \left[ \frac{i\sqrt{2}}{f_1} \sum_{a=1}^5 (\pi_1^a Y^a) \right]. \quad (1)$$

$$\begin{aligned} D_\mu U_0 &= (\partial_\mu - ig W_\mu^i S^i - ig' B_\mu S^6) U_0, \\ D_\mu U_1 &= (\partial_\mu - i\tilde{g} V_\mu^a V^a - i\tilde{g} A_\mu^b Y^b) U_1. \end{aligned} \quad (2)$$

$$\begin{aligned} K &= \exp [ik^a V^a / f_K], \\ D_\mu K &= \partial_\mu K - iv_{0\mu} K + iKv_{1\mu} \end{aligned} \quad (3)$$

$$\mathcal{F}_\mu = \mathcal{V}_\mu + \mathcal{A}_\mu = \sum_{a=1}^{d_H} \mathcal{V}_\mu^a V_a + \sum_{a=1}^{d_G - d_H} \mathcal{A}_\mu^a Y_a,$$

$$\begin{aligned} \mathcal{L}_v &= -\frac{1}{2\tilde{g}^2} \langle \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu} \rangle + \frac{1}{2} f_0^2 \langle x_{0\mu} x_0^\mu \rangle + \frac{1}{2} f_1^2 \langle x_{1\mu} x_1^\mu \rangle \\ &\quad + r f_1^2 \langle x_{0\mu} K x_1^\mu K^\dagger \rangle + \frac{1}{2} f_K^2 \langle D^\mu K D_\mu K^\dagger \rangle. \end{aligned}$$

# GBS amplitudes

- $\pi\pi \rightarrow \pi\pi$  scattering amplitudes expanded in partial wave amplitudes

$$\mathcal{A}(s, t) = 32\pi \sum_{J=0}^{\infty} a_J(s)(2J+1)P_J(\cos \theta)$$

- In order to force elasticity (at least below new heavy states appear), decompose amplitude in conserved quantum number
- **Template: SU(4)/Sp(4), FMCHM**, decompose in multiplets of Sp(4) (very good symmetry at high energy)

$$\mathbf{5} \otimes \mathbf{5} = \mathbf{1} \oplus \mathbf{10} \oplus \mathbf{14} \equiv \mathbf{A} \oplus \mathbf{B} \oplus \mathbf{C}$$

# Inverse Amplitude Method

- Phenomenological approach to describe the physics beyond unitarity violation, successful in describing lightest mesonic resonances in pion-pion and pion-kaon scattering up to 1.2 GeV

$$a_{IJ}^{IAM}(s) = \frac{a_{IJ}^{(0)}(s)}{1 - \frac{a_{IJ}^{(1)}(s)}{a_{IJ}^{(0)}(s)}}$$

- Use with caution, not a QFT!
- Generate poles interpreted as dynamically generated resonances in each channel, e.g.

$$M_A^2 = \frac{2f^2}{\frac{1}{16\pi^2} \left(\frac{29}{12}\right) + \frac{2}{3} \widehat{L}_A(M_A)}, \quad \Gamma_A = \frac{M_A^3}{16\pi f^2}$$

- Normalized mass:  $v_I \equiv \frac{M_I \sin \theta}{\text{TeV}}$ ,  $I = A, B, C$ .

# $pp \rightarrow ZZjj$ analysis

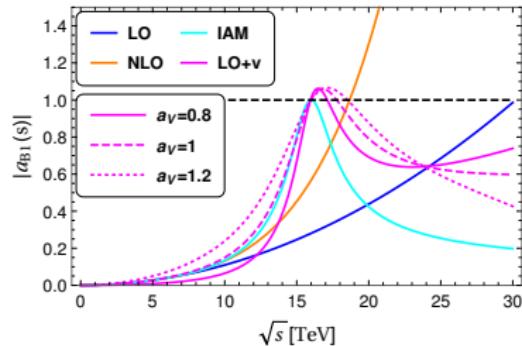
Cuts:

cut	100 TeV	14 TeV
2 jets	$p_T > 30 \text{ GeV}$ , $ \eta  > 3.5$ , $\eta_1 \cdot \eta_2 < 0$	$p_{T,j} > 30 \text{ GeV}$ , $ \eta_j  > 3.$ , $\eta_{j1} \cdot \eta_{j2} < 0$
ZZ invariant mass	$m_{ZZ} > 3 \text{ TeV}$	$m_{ZZ} > 3 \text{ TeV}$
di-jet invariant mass	$m_{jj} > 1 \text{ TeV}$	$m_{jj} > 1 \text{ TeV}$
Zs centrality	$ \eta_{Z_i}  < 2.$	$ \eta_{Z_i}  < 2.$
Zs momentum	$p_{T,Z_i} > 1 \text{ TeV}$	$p_{T,Z_i} > 0.5 \text{ TeV}$

Probability distribution:

$$\mathcal{P}(k; \lambda, \epsilon) = \frac{1}{2\epsilon} \int_{1-\epsilon}^{1+\epsilon} dx e^{-x\lambda} \frac{(x\lambda)^k}{k!}$$

# Vector Analysis



$$g_V = -\frac{M_V}{2f} a_V = -\frac{M_V^2(1-r^2)}{\sqrt{2}\tilde{g}f^2},$$

$$\mathcal{A}(s, t, u) = -g_V^2 \left( \frac{s-u}{t-M_V^2} + \frac{s-t}{u-M_V^2} + \frac{3s}{M_V^2} \right)$$

