

PROBING CHIRALITY OF TOP-HIGGS FCNC COUPLINGS AT LINEAR COLLIDERS

BLAZENKA MELIC

Theoretical Physics Division **ThPhys**^{@IRB}

Rudjer Boskovic Institute, Zagreb

FCNC IN THE TOP-HIGGS COUPLINGS

- search for the **Flavor Changing Neutral Current (FCNC)** processes has been one of the leading tools to test the Standard Model (SM), in an attempt of either discovering or putting stringent limits on the new physics scenarios
- we investigate **rare top-Higgs flavor changing neutral current decays**

$$t \rightarrow cH, t \rightarrow uH$$

$$\text{BR}(t \rightarrow cH)_{\text{SM}} \sim 10^{(-15)}$$

(many orders of magnitude smaller than the value to be measured at the LHC, at 14 TeV)

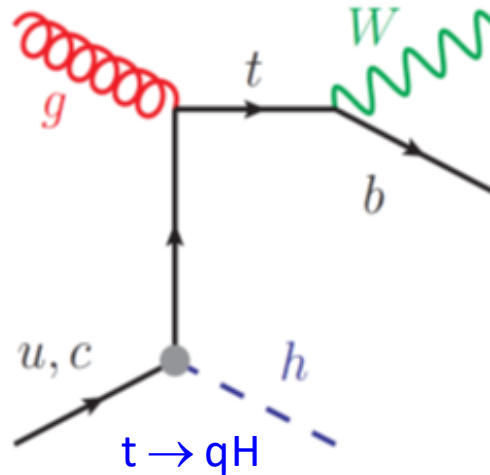
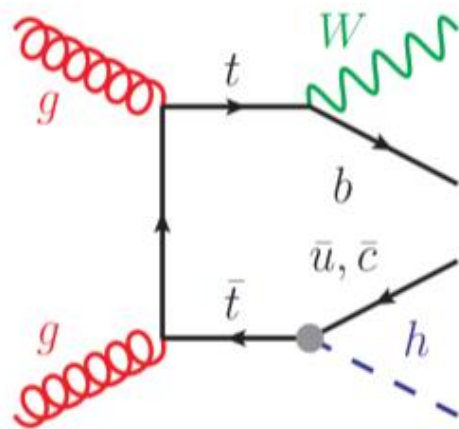
- An affirmative observation of the process $t \rightarrow qH$, well above the SM rate, will be a conclusive indication of a new physics beyond the SM
- tight constraints on $|Y_{qq'}|$ from the flavor oscillations

Technique	Coupling	Constraint
D^0 oscillations	$ Y_{uc} ^2, Y_{cu} ^2$	$< 5.0 \times 10^{-9}$
	$ Y_{uc} Y_{cu} $	$< 7.5 \times 10^{-10}$
B_d^0 oscillations	$ Y_{db} ^2, Y_{bd} ^2$	$< 2.3 \times 10^{-8}$
	$ Y_{db} Y_{bd} $	$< 3.3 \times 10^{-9}$
B_s^0 oscillations	$ Y_{sb} ^2, Y_{bs} ^2$	$< 1.8 \times 10^{-6}$
	$ Y_{sb} Y_{bs} $	$< 2.5 \times 10^{-7}$
K^0 oscillations	$\Re(Y_{ds}^2), \Re(Y_{sd}^2)$	$[-5.9 \dots 5.6] \times 10^{-10}$
	$\Im(Y_{ds}^2), \Im(Y_{sd}^2)$	$[-2.9 \dots 1.6] \times 10^{-12}$
	$\Re(Y_{ds}^* Y_{sd})$	$[-5.6 \dots 5.6] \times 10^{-11}$
	$\Im(Y_{ds}^* Y_{sd})$	$[-1.4 \dots 2.8] \times 10^{-13}$

LHC CONSTRAINTS

CMS $\text{BR}(t \rightarrow cH) < 0.0056 \quad \leftrightarrow \quad \sqrt{|y_{tc}|^2 + |y_{ct}|^2} < 0.14$

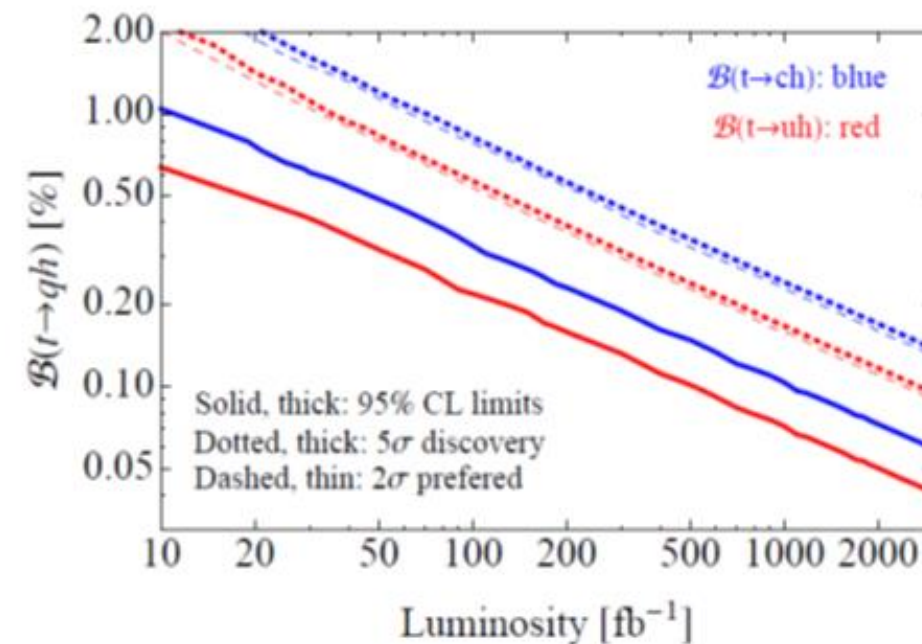
ATLAS $\text{BR}(t \rightarrow cH) < 0.0079 \quad \leftrightarrow \quad \sqrt{|y_{tc}|^2 + |y_{ct}|^2} < 0.17$



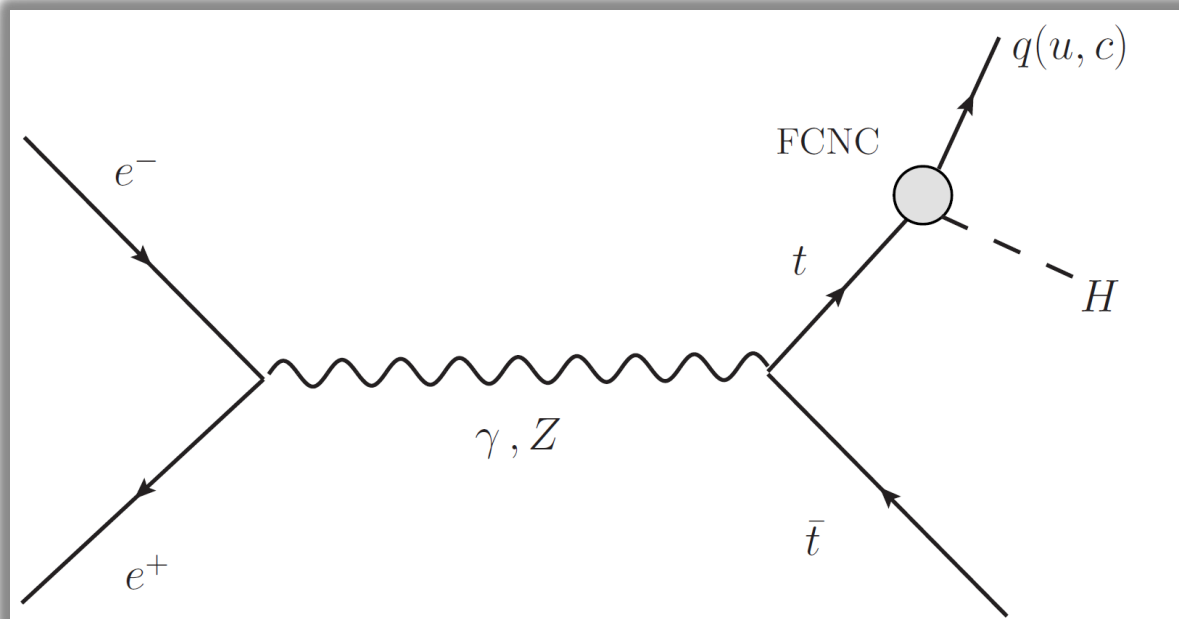
[Greljo, Kamenik, Kopp, 1404.1278]

Discrimination between tuH and tcH coupling at LHC:

(for 5σ discovery, the discrimination is possible at 2σ)



FCNC AT LINEAR COLLIDERS



ILC – International Linear Collider
CLIC – Compact Linear Collider

Operation at: $\sqrt{s} = 350, 500, 1000$ GeV (up 3 TeV CLIC);

our reference point $\sqrt{s} = 500$ GeV

BEAM POLARIZATIONS can be tuned independently:

$\pm 80\%$ for electrons, $\pm 30\%$ for positrons (both longitudinal and transversal)

Excellent opportunities for precision measurements of top-quark and Higgs properties

FCNC AT LINERAR COLLIDERS

The most general FCNC tqH Lagangian:

$$\begin{aligned}\mathcal{L}^{tqH} &= g_{tu}\bar{t}_R u_L H + g_{ut}\bar{u}_R t_L H + g_{tc}\bar{t}_R c_L H + g_{ct}\bar{c}_R t_L H + h.c \\ &= \bar{t}(g_{tq}P_L + g_{qt}^*P_R)qH + \bar{q}(g_{qt}P_L + g_{tq}^*P_R)tH.\end{aligned}$$

$t \rightarrow qH$ normalized to the standard tWb decay:

$$\text{BR}(t \rightarrow qH) = \frac{1}{2\sqrt{2}G_F} \frac{(m_t^2 - m_H^2)^2}{(m_t^2 - m_W^2)^2(m_t^2 + 2m_W^2)} (|g_{tq}|^2 + |g_{qt}|^2) \alpha_{QCD}$$

$$\Gamma_t = \Gamma_t^{SM} + \Gamma_{t \rightarrow qH} \approx \Gamma_t^{SM} + 0.155(|g_{tq}|^2 + |g_{qt}|^2)$$

ANALYSIS

$$e^-(p_1) + e^+(p_2) \rightarrow t(q_1) + \bar{t}(q_2),$$

$$t(q_1) \rightarrow q(p_q) + H, \quad [\bar{t}(q_2) \rightarrow \bar{b}(p_b) + l^+(p_l) + \nu(p_\nu)]$$

$$d\sigma = \frac{1}{2s} \int \frac{ds_1}{2\pi} \frac{1}{((s_1 - m_t^2)^2 + \Gamma_t^2 m_t^2)} \times |\bar{\mathcal{M}}^2|$$

$$\times (2\pi)^4 \delta^4(q_1 + q_2 - p_1 - p_2) \frac{d^3 q_1}{(2\pi^3) 2E_1} \frac{d^3 q_2}{(2\pi^3) 2E_2} \quad [\text{production of } t\bar{t}]$$

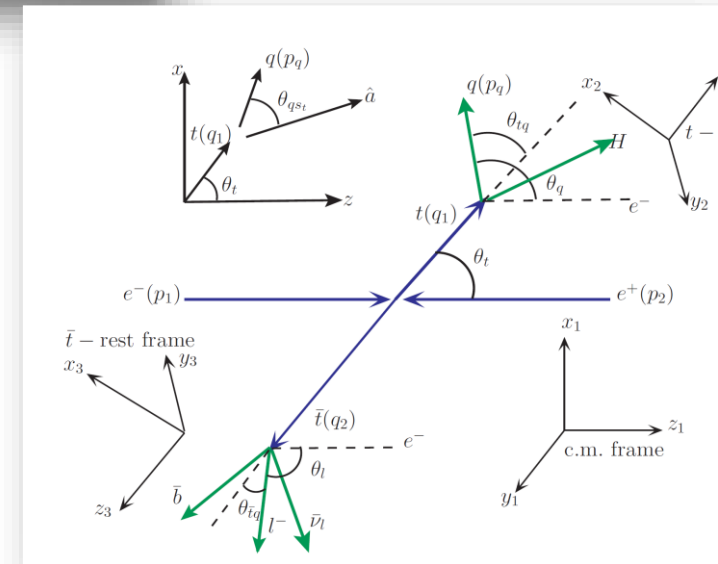
$$\times (2\pi)^4 \delta^4(p_q + p_H - q_1) \frac{d^3 p_q}{(2\pi^3) 2E_q} \frac{d^3 p_H}{(2\pi^3) 2E_H} \quad [\text{decay of } t],$$

Spin of the top λ_t will be considered as well as the beam polarizations :

$$|\bar{\mathcal{M}}^2| = \sum_{L,R} \sum_{(\lambda_t \lambda'_t = \pm)} \mathcal{M}_{\lambda_t}^{L,R} \mathcal{M}_{\lambda'_t}^{*L,R} \rho_{\lambda_t \lambda'_t}^{D^t}$$

PRODUCTION HELICITY MATRIX
for the top quark

DECAY HELICITY MATRIX for the top
(antitop helicities are summed over)



After boosting and integration over some angles like ϕ_q, θ_t

$$\frac{d\sigma}{ds d\cos\theta_q d\phi_t} = \frac{1}{4} \left((1 - P_{e^-}^L)(1 + P_{e^+}^L) |T_{e_L^- e_R^+}|^2 + (1 + P_{e^-}^L)(1 - P_{e^+}^L) |T_{e_R^- e_L^+}|^2 \right) - \frac{1}{2} P_{e^-}^T P_{e^+}^T \text{Re} e^{i(\eta - 2\phi_t)} T_{e_R^- e_L^+}^* T_{e_L^- e_R^+},$$

dependence on the initial beam polarizations $P_{L,T}(e^-) = \pm 0.8$ $P_{L,T}(e^+) = \pm 0.3$

$$|T_{e_L^\mp e_R^\pm}|^2 = (|g_{tq}|^2 + |g_{qt}|^2) (a_0 + a_1 \cos\theta_q + a_2 \cos^2\theta_q) + (|g_{tq}|^2 - |g_{qt}|^2) (b_0 + b_1 \cos\theta_q + b_2 \cos^2\theta_q)$$

The coefficients a_0, a_1, a_2 and b_0, b_1, b_2 differ from each other

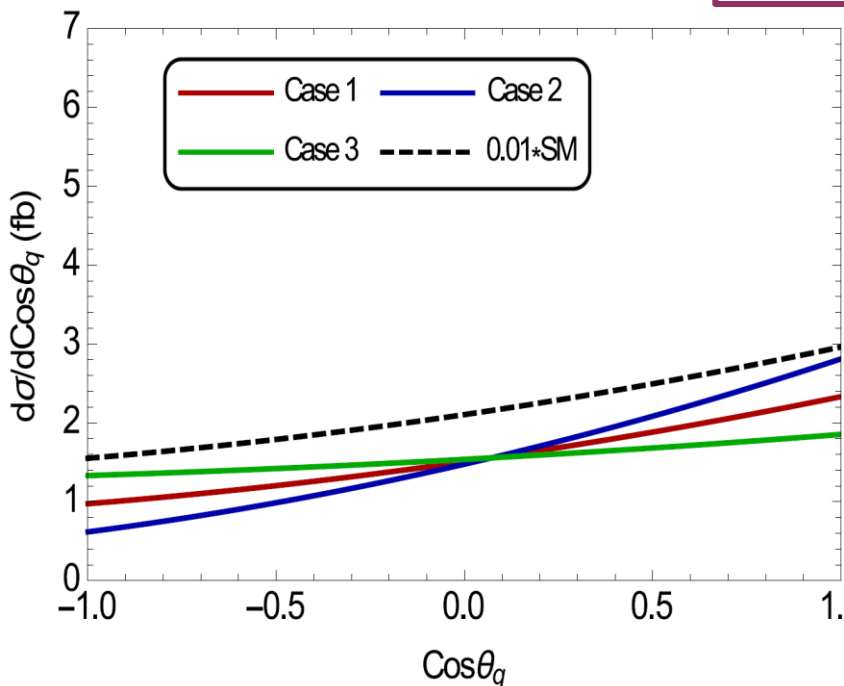
– the couplings $|g_{qt}|^2$ have different angular dependences from $|g_{tq}|^2$

 **possibility to test chirality of the FCNC tqH couplings !**

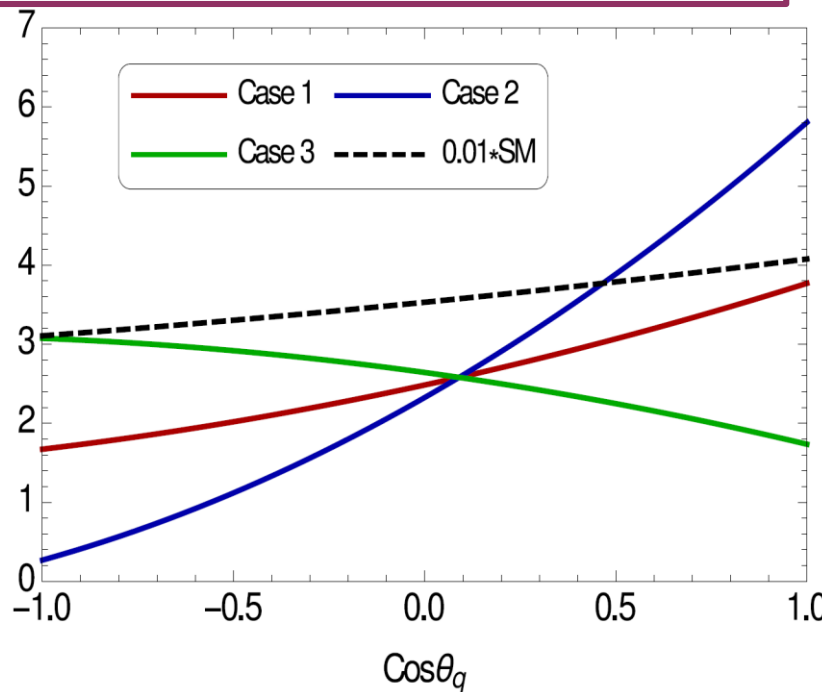
POLAR ANGLE DISTRIBUTION

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta_q} \text{ vs } \cos\theta_q$$

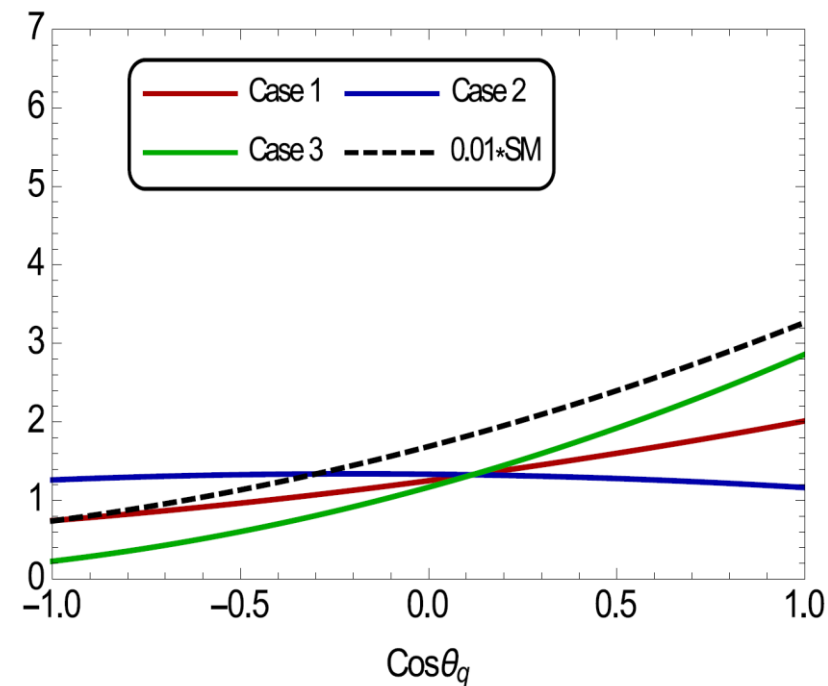
- Case 1 : $\sqrt{|g_{tq}|^2 + |g_{qt}|^2} = 0.16$ present LHC bound
- Case 2 : $\sqrt{|g_{tq}|^2 + |g_{qt}|^2} = 0.16$, with $|g_{qt}|^2 = 0$
- Case 3 : $\sqrt{|g_{tq}|^2 + |g_{qt}|^2} = 0.16$, with $|g_{tq}|^2 = 0$



$P_L(e^-) = 0 \quad P_L(e^+) = 0$



$P_L(e^-) = -0.8 \quad P_L(e^+) = +0.3 \quad \text{LR}$



$P_L(e^-) = +0.8 \quad P_L(e^+) = -0.3 \quad \text{RL}$

Clear dependence on the initial beam polarizations in differentiating among the chiral couplings !

FULL NUMERICAL ANALYSIS

$$e^-(p_1, \lambda_{e-}) + e^+(p_2, \lambda_{e+}) \rightarrow t(q_1, s_t) + \bar{t}(q_2, s_{\bar{t}})$$

$$t(q_1, s_t) \rightarrow q(p_q) + H(\rightarrow b\bar{b})$$

$$\bar{t}(q_2, s_{\bar{t}}) \rightarrow b(p_b) + l(p_l) + \nu(p_\nu)$$

❖ **background** for the process is the $t\bar{t}$ production, with one top decaying hadronically and the other to lepton, neutrino and a b-quark

❖ **applying cuts** in the search for

– an isolated lepton; q-quark from the top decay; b-tagged jet; reconstructed Higgs decay from two b-jets

$$\frac{d\sigma}{d\cos\theta_f d\cos\theta_{\bar{f}}} = \frac{\sigma}{4} (1 + \kappa_f B_t \cos\theta_f + \kappa_{\bar{f}} B_{\bar{t}} \cos\theta_{\bar{f}} - \kappa_f \kappa_{\bar{f}} C \cos\theta_f \cos\theta_{\bar{f}})$$

κ_f top spin analysing power factors of the top decaying products f :

SM:

$$\kappa_{\bar{f}} = \kappa_l = 1$$

$t \rightarrow qH$:

$$\kappa_f = \kappa_q = \frac{|g_{qt}|^2 - |g_{tq}|^2}{|g_{qt}|^2 + |g_{tq}|^2}$$

for $|g_{qt}|^2 \simeq |g_{tq}|^2$
spin information is lost

TOP SPIN OBSERVABLES

(TOP DECAY PRODUCTS OF CONTAIN INFO ABOUT THE TOP SPIN)

$$\frac{d\sigma}{d\cos\theta_f d\cos\theta_{\bar{f}}} = \frac{\sigma}{4} (1 + \kappa_f B_t \cos\theta_f + \kappa_{\bar{f}} B_{\bar{t}} \cos\theta_{\bar{f}} - \kappa_f \kappa_{\bar{f}} C \cos\theta_f \cos\theta_{\bar{f}})$$

$$\langle \mathcal{O}_2 \rangle = B_t$$

$$\langle \mathcal{O}_3 \rangle = C$$

$$\begin{aligned} \mathcal{O}_1 &= S_t \cdot S_{\bar{t}} \\ \mathcal{O}_2 &= S_t \cdot \hat{a}, \quad \mathcal{O}_{\bar{2}} = S_{\bar{t}} \cdot \hat{b} \\ \mathcal{O}_3 &= 4(S_t \cdot \hat{a})(S_{\bar{t}} \cdot \hat{b}) \\ \mathcal{O}_4 &= 4((S_t \cdot \hat{p})(S_{\bar{t}} \cdot \hat{q}_1) + (S_t \cdot \hat{q}_1)(S_{\bar{t}} \cdot \hat{p})) \end{aligned}$$

OPENING ANGLE DISTRIBUTION

between directions of two spin analysers
(final particles in the top decays):

$$\frac{d\sigma}{d\cos\phi_{f\bar{f}}} = \frac{\sigma}{2} (1 - \kappa_f D \cos\phi_{f\bar{f}})$$

$$\langle \mathcal{O}_1 \rangle = D$$

QUANTIZATION AXES:

$$\hat{a} = -\hat{b} = \hat{q}_1$$

helicity basis (top dir.)

$$\hat{a} = \hat{b} = \hat{p}$$

beamline basis

$$\hat{a} = \hat{b} = \hat{d}_x$$

**max basis –
OFF-DIAGONAL**

(specific for each model X)

$$\hat{a} = \hat{b} = \hat{e}_x$$

minimal basis

(specific for each model X)

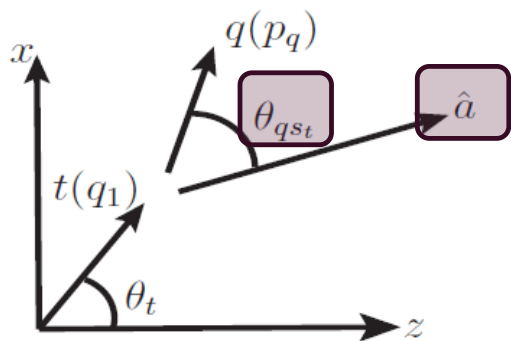
OFF-DIAGONAL = max correlations

– almost 100% at ILC/Tevatron

[Mahlon and Parke, hep-ph/9512264
Bernreuther et al., hep-ph/0403035]

$$\hat{d}_{SM} = \hat{d}_{SM}^{\max} = \frac{-\hat{p} + (1 - \gamma)z \hat{q}_1}{\sqrt{1 - (1 - \gamma^2)z^2}}$$

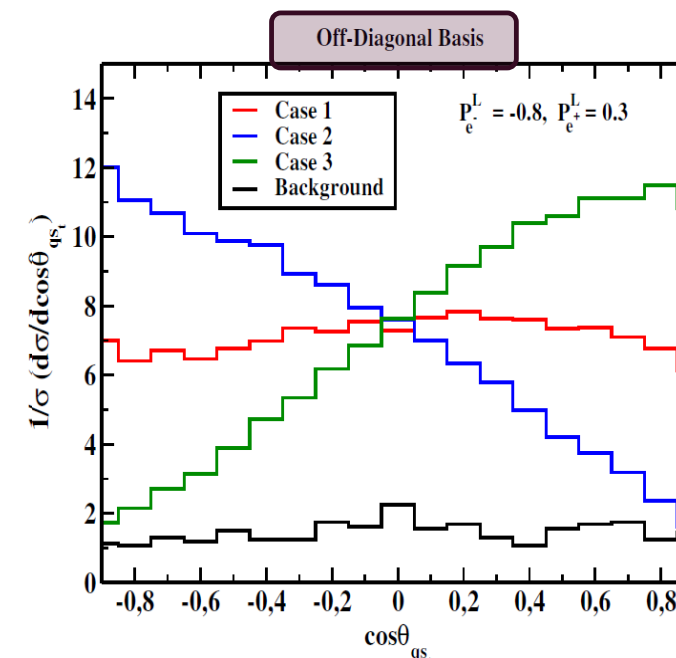
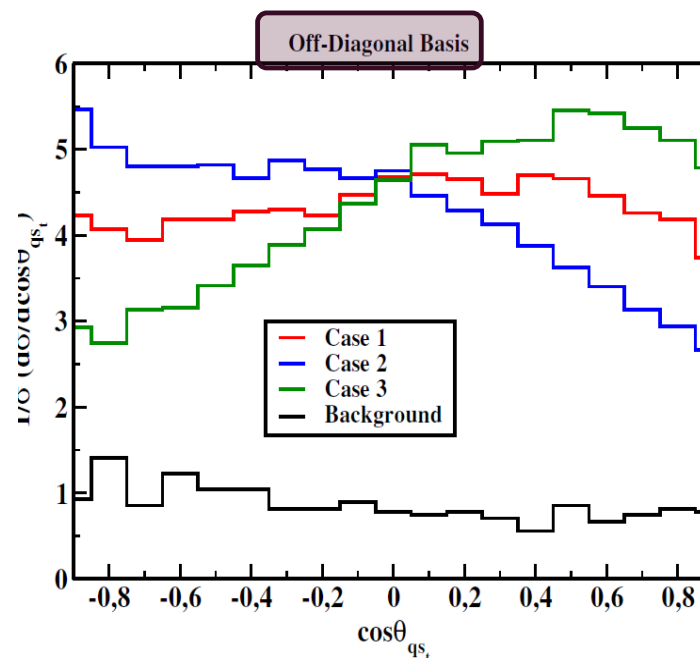
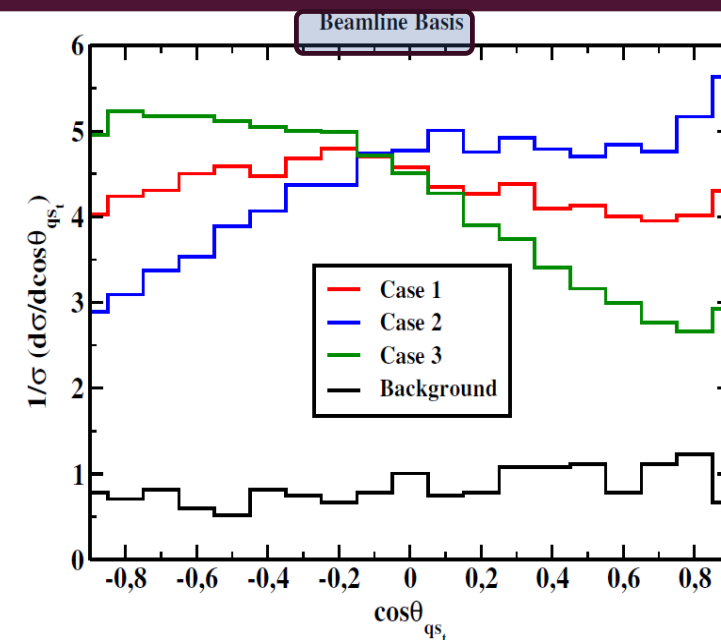
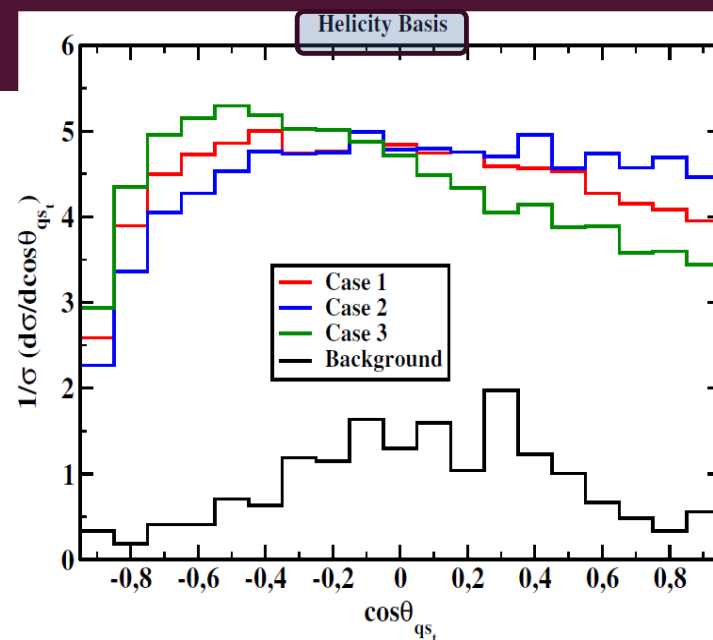
TOP SPIN



$$\mathbf{B}_t = \langle \mathbf{O}_2 \rangle = \langle \mathbf{S}_t \cdot \hat{\mathbf{a}} \rangle$$

- ❖ Clear distinction between chiral couplings
- ❖ Clear enhancement of the effect by using initial beam polarizations

$$\begin{aligned} & - \sqrt{|g_{qt}|^2 + |g_{tq}|^2} = 0.16 \\ & - \sqrt{|g_{tq}|^2} = 0.16, \sqrt{|g_{qt}|^2} = 0 \\ & - \sqrt{|g_{tq}|^2} = 0, \sqrt{|g_{qt}|^2} = 0.16 \end{aligned}$$



TOP-ANTITOP SPIN CORRELATIONS

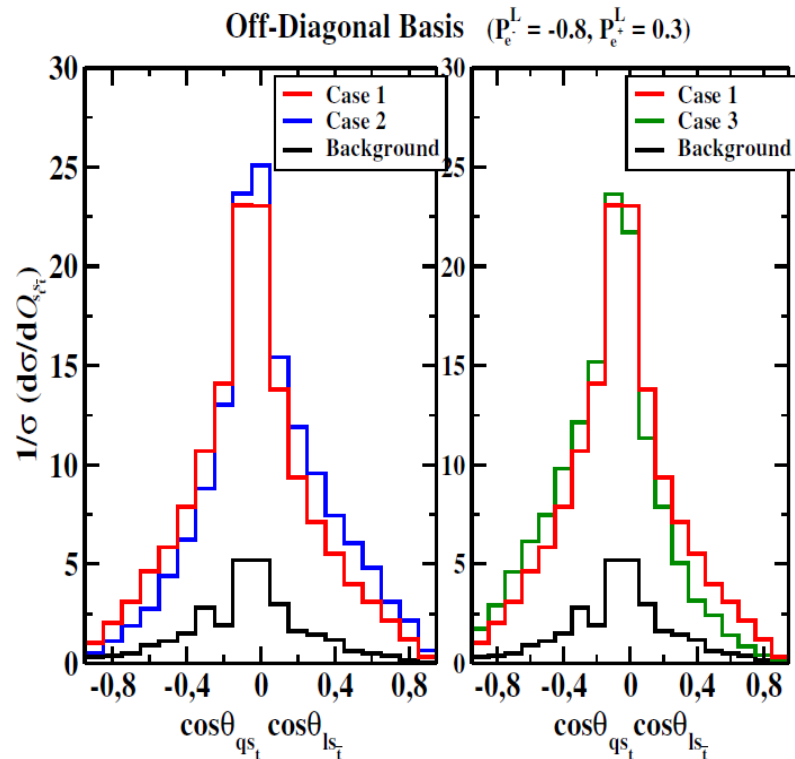
OPENING ANGLE DISTRIBUTION

$$\mathcal{O}_{s_t, s_{\bar{t}}} = \cos \theta_f \cos \theta_{\bar{f}} \text{ distribution:}$$

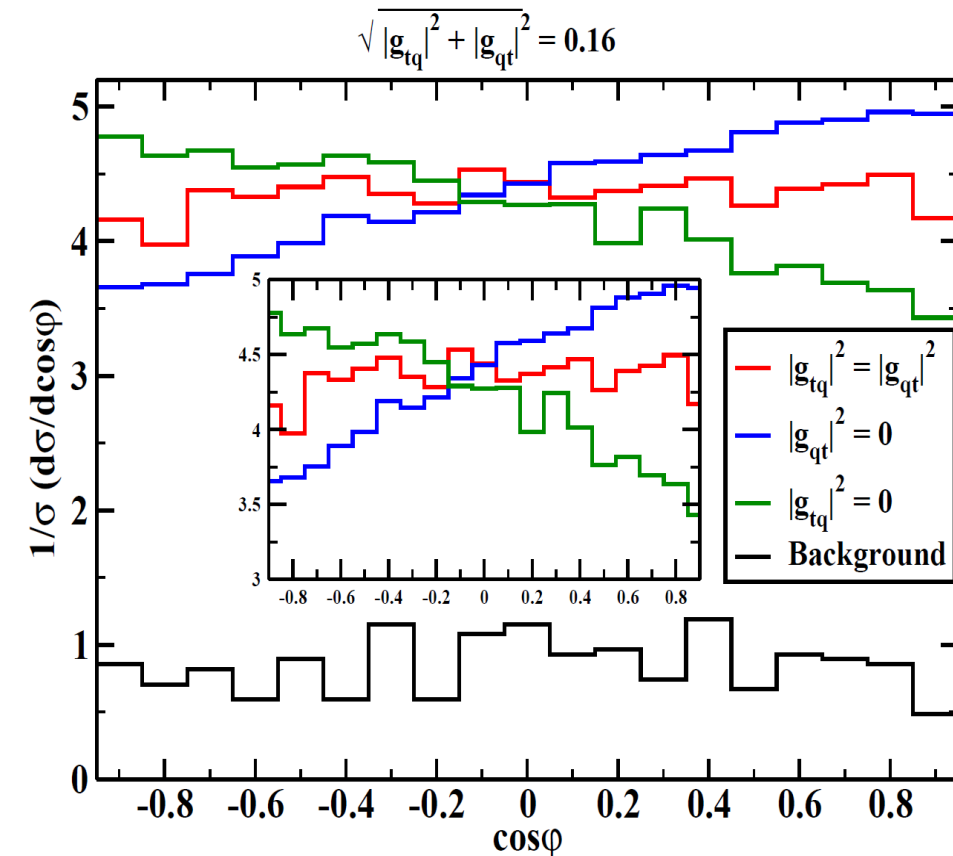
$$\sim \langle \mathbf{O}_3 \rangle = \langle 4(\mathbf{S}_t \cdot \hat{\mathbf{a}})(\mathbf{S}_{\bar{t}} \cdot \hat{\mathbf{b}}) \rangle$$

$$\frac{d\sigma}{d\cos\phi_{f\bar{f}}} = \frac{\sigma}{2} (1 - \kappa_f D \cos\phi_{f\bar{f}})$$

$$D = \langle \mathbf{O}_1 \rangle = \langle \mathbf{S}_t \cdot \mathbf{S}_{\bar{t}} \rangle$$



- $\sqrt{|g_{qt}|^2 + |g_{tq}|^2} = 0.16$
- $\sqrt{|g_{tq}|^2} = 0.16, \sqrt{|g_{qt}|^2} = 0$
- $\sqrt{|g_{tq}|^2} = 0, \sqrt{|g_{qt}|^2} = 0.16$



One can see asymmetry when compared Case2 and Case3
- possibilty to distinguish chiral couplings

BR AND DISCOVERY AT LINEAR COLLIDERS

Most stringent upper bounds at 95 % C.L. $t\bar{t} \rightarrow Wb + qH \rightarrow \ell\nu b + \gamma\gamma q$

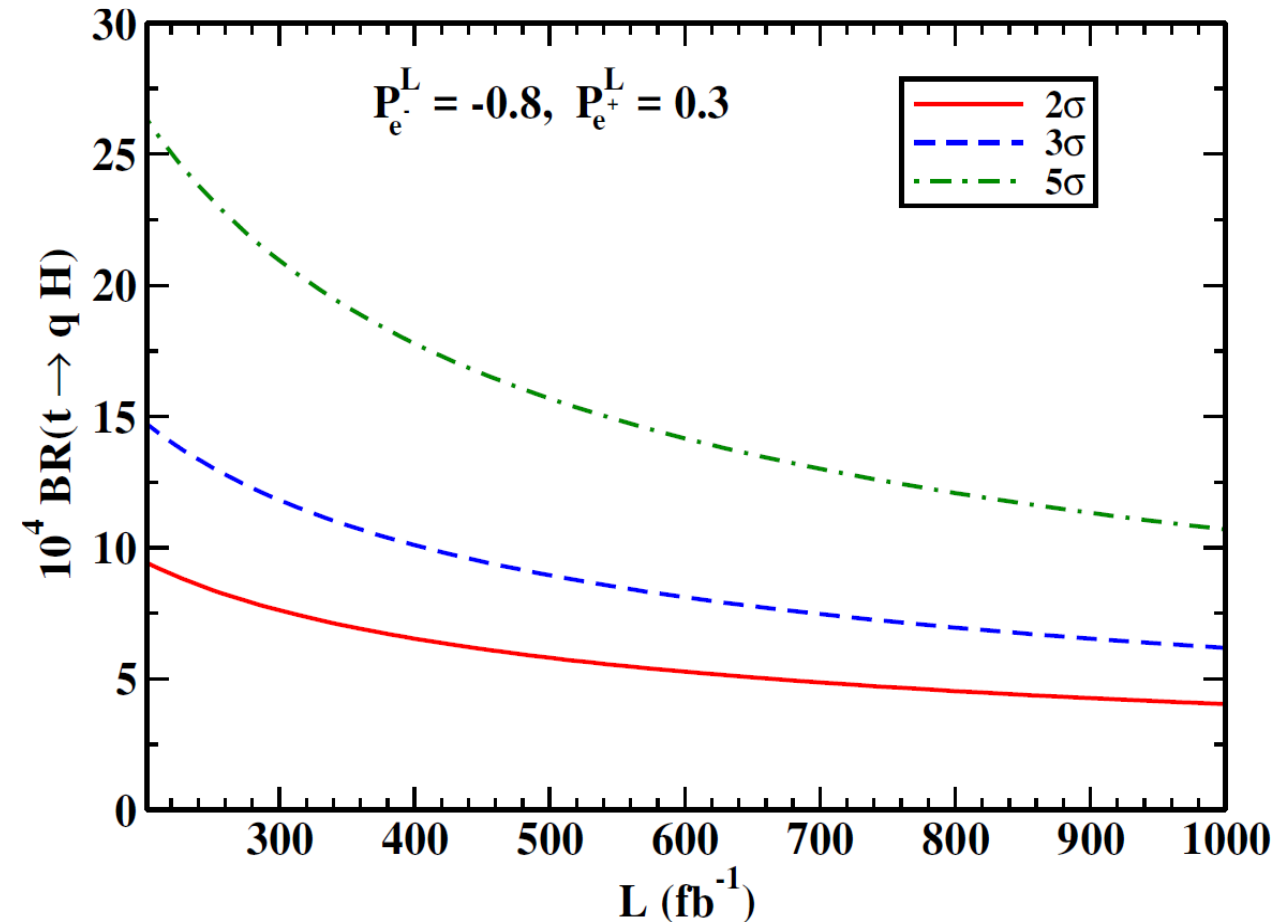
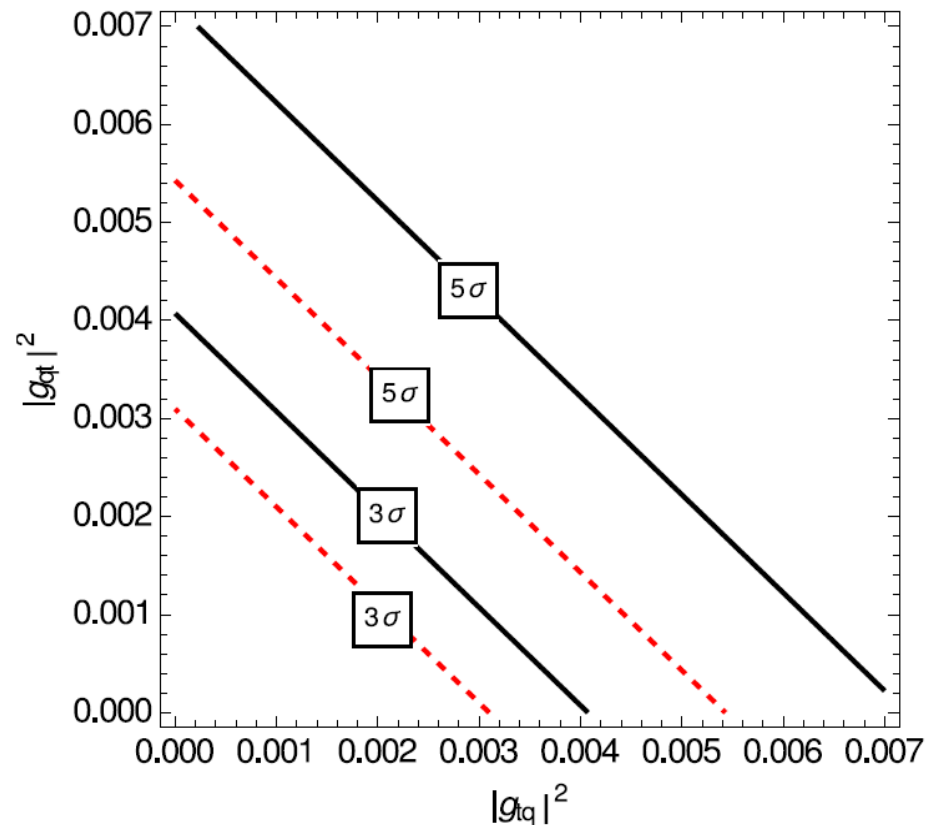
@ 7 TeV: $t \rightarrow qH < 0.79\%$ (ATLAS, JHEP 1406 (2014) 008)

future @ 14 TeV: $t \rightarrow qH < 0.05\%$ at 3000 fb⁻¹ (ATL-PHYS-PUB-2013-012)

— unpolarized beams

----- polarized beams

$P_L(e^-) = -0.8$ $P_L(e^+) = +0.3$



CONCLUSIONS

- ❖ Nature of the FCNC top-Higgs couplings can be probed by using complementary machines, the LHC and the linear colliders
- ❖ At LHC one can distinguish among $|g_{ct}|$ and $|g_{ut}|$ FCNC couplings
- ❖ At linear colliders one can distinguish among different chiral FCNC couplings $|g_{qt}|$ and $|g_{tq}|$ by use of
 - the initial beam polarizations (longitudinal (and possibly transversal))
 - the top-spin polarization observablesand by exploring various angular asymmetries
- ❖ bound obtained at linear colliders could be about a factor of 2 better than the one obtained at LHC

$$\sqrt{|g_{qt}|^2 + |g_{tq}|^2} < 0.05 - 0.07$$