Theory overview of the tree-level B decays

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$$R_{D(*)} = \frac{B(B \to D^{(*)} \tau \nu_{\tau})}{B(B \to D^{(*)} \ell \nu_{\ell})}$$

➤ In loop-induced modes:
$$P_5^{'}$$
, R_K , R_{K^*} $R_{K^*} = \frac{B(B \to K^{(*)}\mu^+\mu^-)}{B(B \to K^{(*)}e^+e^-)}\Big|_{q^2 \in [q_{\min}^2, q_{\max}^2]}$

$$R_{K(*)} = \frac{B(B \to K^{(*)} \mu^{+} \mu^{-})}{B(B \to K^{(*)} e^{+} e^{-})} \bigg|_{q^{2} \in [q_{\min}^{2}, q_{\max}^{2}]}$$

long standing puzzles

- \triangleright $|V_{cb}|$: tension between inclusive and exclusive determinations
- \triangleright $|V_{ub}|$: tension between inclusive and exclusive determinations

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$$\triangleright$$
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questions to address

- are these tensions related?
- should we invoke LFU violation?

SM: LFU only in Yukawas

➤ In tree-level B decays : R_D, R_{D*}

- \rightarrow violation of τ/μ , τ/e universality
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- \triangleright In loop-induced modes : P_5' , R_K , R_{K^*} \rightarrow violation of μ /e universality

long standing puzzles

 \triangleright $|V_{cb}|$: tension between inclusive and exclusive determinations

this talk

 \triangleright $|V_{ub}|$: tension between inclusive and exclusive determinations

questions to address

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- should we invoke LFU violation?

SM: LFU only in Yukawas

b --> c ℓ v decays

tensions:

- ratios R(D^(*)) deviate from SM predictions (≈3.9σ)
- long standing issue: discrepancy in |V_{cb}| determinations from inclusive and exclusive B modes (≈3.1σ)



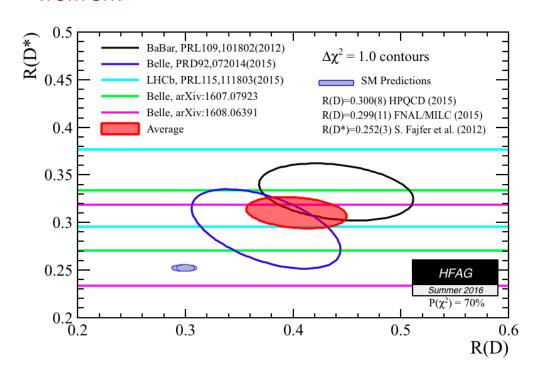
impact on other flavour observables, i.e. ε_{κ}

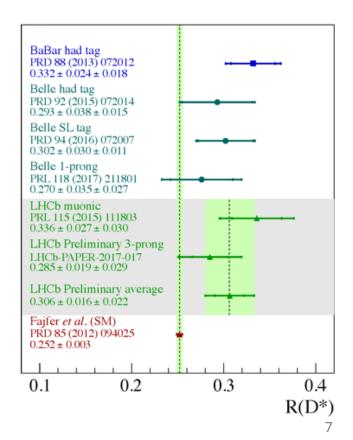
anomalies in semileptonic transitions: is NP hiding under tree-level processes?

$$|\mathcal{R}^{0}(D)|_{SM} = \frac{\mathcal{B}(\bar{B}^{0} \to D^{+}\tau^{-}\bar{\nu}_{\tau})}{\mathcal{B}(\bar{B}^{0} \to D^{+}\ell^{-}\bar{\nu}_{\ell})}\Big|_{SM} = 0.324 \pm 0.022$$

$$\mathcal{R}^{0}(D^{*})\Big|_{SM} = \frac{\mathcal{B}(\bar{B}^{0} \to D^{*+}\tau^{-}\bar{\nu}_{\tau})}{\mathcal{B}(\bar{B}^{0} \to D^{*+}\ell^{-}\bar{\nu}_{\ell})}\Big|_{SM} = 0.250 \pm 0.003$$

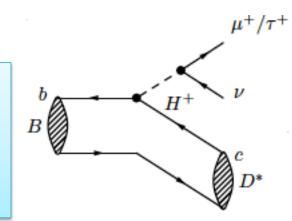
present scenario HFAG quotes 3.9σ deviation from SM



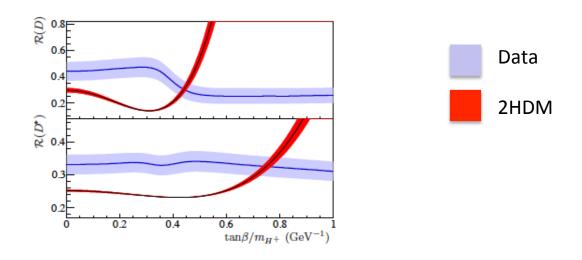


most "natural" explanation: new scalars with couplings to leptons proportional to their mass

- would explain the enhancement of τ modes
- would enhance both semileptonic and purely leptonic modes



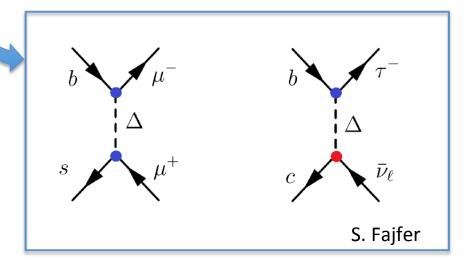
the simplest model (2HDM) excluded (BABAR): no possibility to simultaneously reproduce R(D) and R(D*)



many other explanations put forward....

common solution to the R(K^(*)) tension -> new left-handed effective interaction no effect observed in K, π decays -> NP mainly coupling to 3rd generation of q, ℓ

- ♦ new gauge bosons
- leptoquarks (scalar)
- ♦ leptoquarks (vector) -> may be either gauge bosons or vector mesons



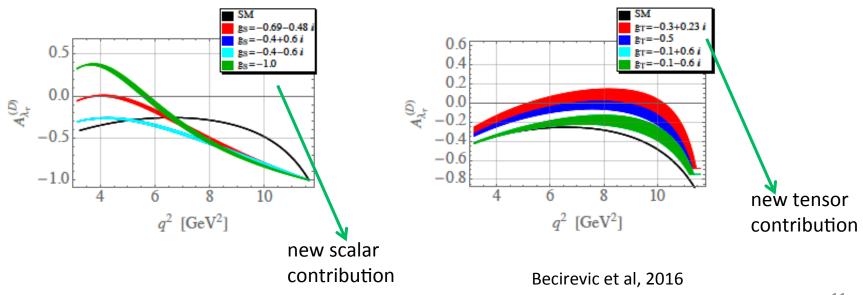
Contribution to charged & neutral currents

- constraints from direct searches of resonances in $\tau^+\tau^-$ inv. mass Faroughy et al. PLB 2017
- constraints from B-Bbar mixing
 not for vector –coloured LQ
 Buttazzo et al 1706.07808

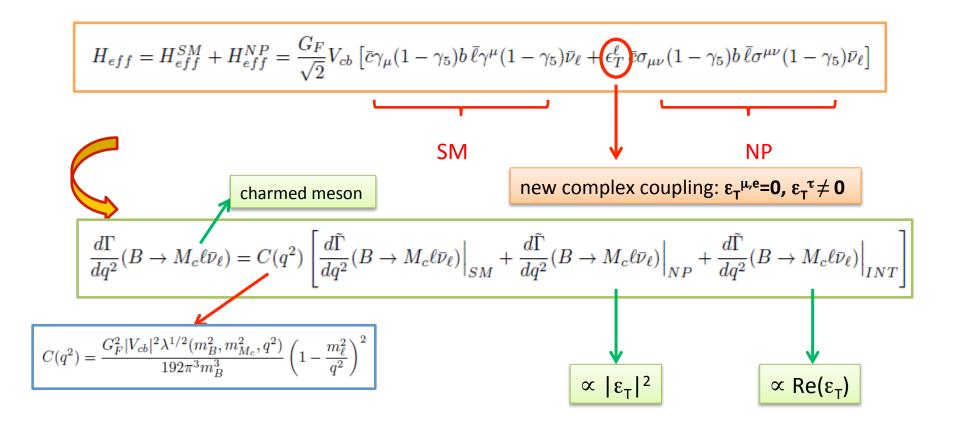
- > NP does not necessarily imply a unique mediator/a unique new structure
- bottom-up approach: no a priori identification of the model consider the new possible structures single out the most sensitive observables

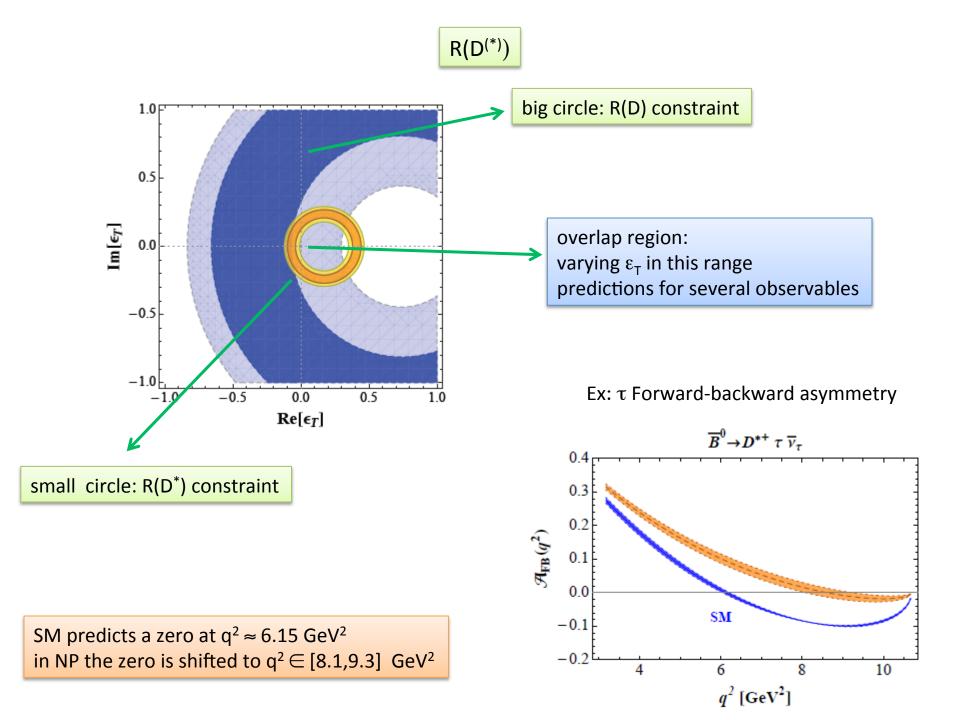
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 τ lepton in the final state: allow to access more form factors sensitive to the lepton mass: lepton polarization asymmetry



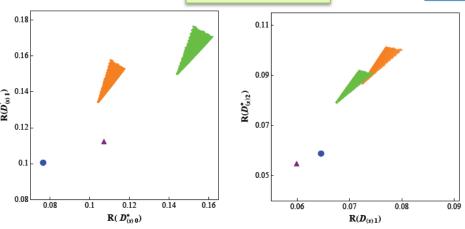
- consider a NP scenario that enhances semileptonic modes but not leptonic ones
- predict the effects in other modes







D**= positive parity excited charmed mesons

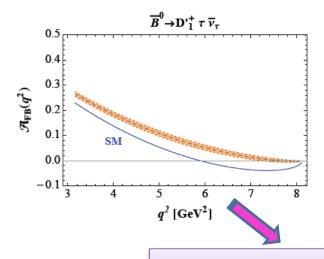


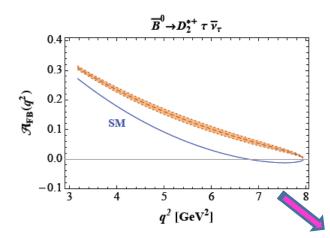
orange = non strange blue circle = SM green = strange triangle = SM



the inclusion of the tensor operator produces an increase in the ratios

forward-backward asymmetries





shift in the position of the zero

the zero disappears

V_{cb}

exclusive determinations from B systematically smaller than inclusive ones

$$|V_{cb}|_{\rm excl} = (39.78 \pm 0.42) \times 10^{-3}$$

C. DeTar, LeptonPhoton2015

$$|V_{cb}|_{\text{incl}} = (42.21 \pm 0.78) \times 10^{-3}$$
.

A. Alberti et al., PRL 114 (2015) 061802

P. Gambino et al., PRD 94 (2016) 014031

are the tensions in $|V_{cb}|$ and $R(D^{(*)})$ related?

model independent parametrization of NP effects: write a generalized H_{eff}



- additional four-fermion operators (S,P,T)
 - modified W-couplings



imply modified Z couplings if invariance under the SM gauge group is respected model independent parametrization of NP effects: write a generalized $H_{\rm eff}$



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additional four-fermion operators (S,P,T)

if massless leptons are considered



- at zero recoil no interference between SM and NP contributions
- the NP effect is the same in all modes

- include a new tensor operator in H_{eff}
- relax the assumption that it contributes only for τ lepton
- non vanishing m_{ℓ} $\ell=e,\mu,\tau$ and $m_e \neq m_{\mu}$

$$H_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{cb} [\bar{c} \gamma_\mu (1 - \gamma_5) b \bar{\ell} \gamma^\mu (1 - \gamma_5) \bar{\nu}_\ell + \epsilon_T^\ell \bar{c} \sigma_{\mu\nu} (1 - \gamma_5) b \bar{\ell} \sigma^{\mu\nu} (1 - \gamma_5) \bar{\nu}_\ell]$$

new structure-> new coupling

Inclusive B -> $X_c \ell v_\ell$ decay

Heavy Quark Expansion -> $\Gamma(H_Q)$ as series in powers of m_Q^{-1}

$$\frac{d\Gamma}{d\hat{q}^2} = C(q^2) \left[\frac{d\tilde{\Gamma}}{d\hat{q}^2} \bigg|_{\text{SM}} + |\epsilon_T|^2 \frac{d\tilde{\Gamma}}{d\hat{q}^2} \bigg|_{\text{NP}} + \text{Re}(\epsilon_T) \frac{d\tilde{\Gamma}}{d\hat{q}^2} \bigg|_{\text{INT}} \right]$$

$$\hat{q}^2 = \frac{q^2}{m_b^2}$$

each of the three terms expanded in m_b^{-1} α_s corrections included in the SM term

- prediction depends on $|V_{cb}|$ and on the complex parameter ε_T^{ℓ} : three-parameter space $(\text{Re}(\varepsilon_T^{\ell}), |W_{cb}|)$
- non vanishing lepton mass distinguish between e and μ
- result to be compared to experiment

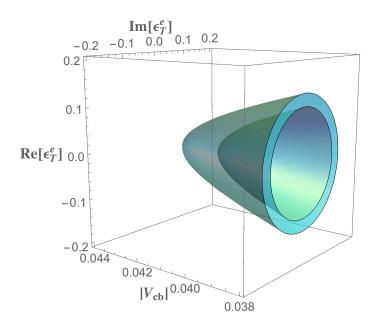
$$\mathcal{B}(B^+ \to X_c e^+ \nu_e) = (10.8 \pm 0.4) \times 10^{-2}$$

PDG

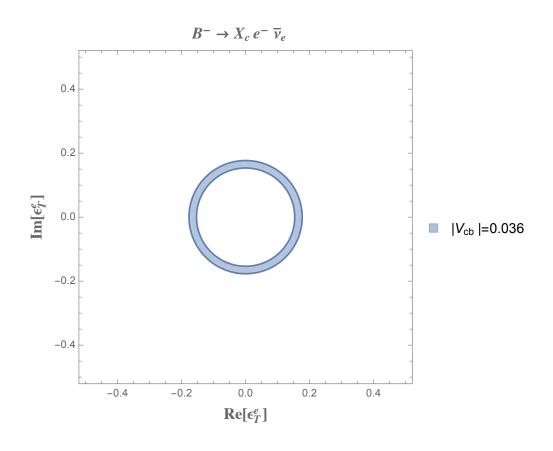
inclusive B -> $X_c \ell v_\ell$ decay: allowed regions

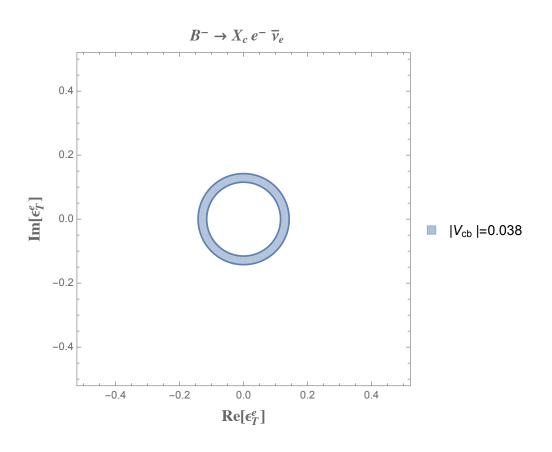
 μ channel

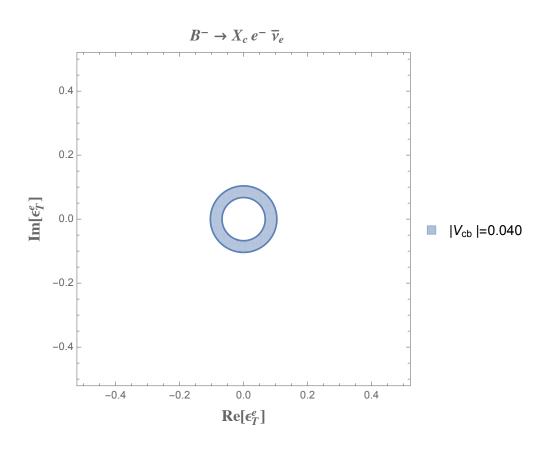
comparison with data at $\, 1 \, \sigma$

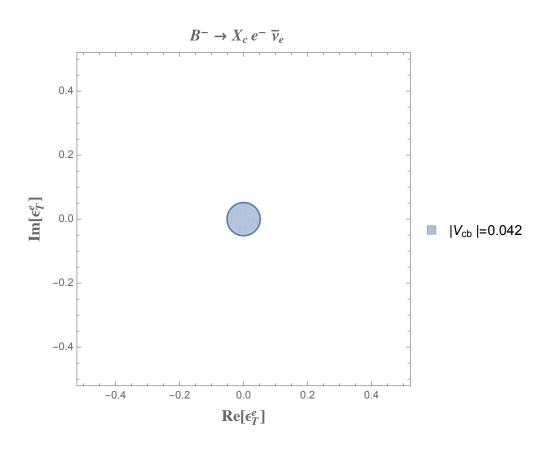


e channel

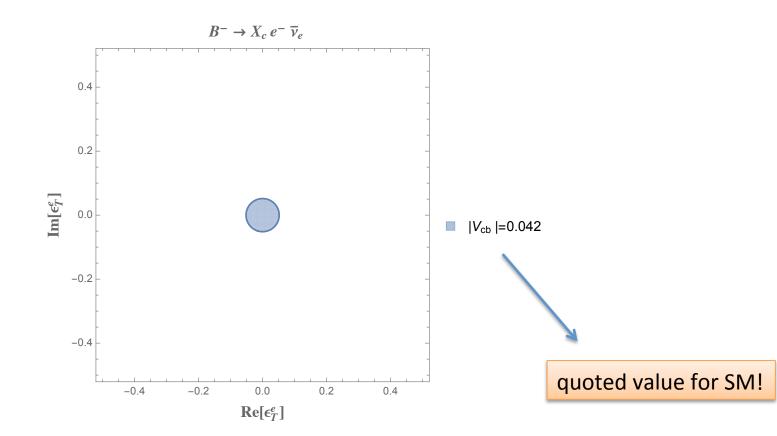




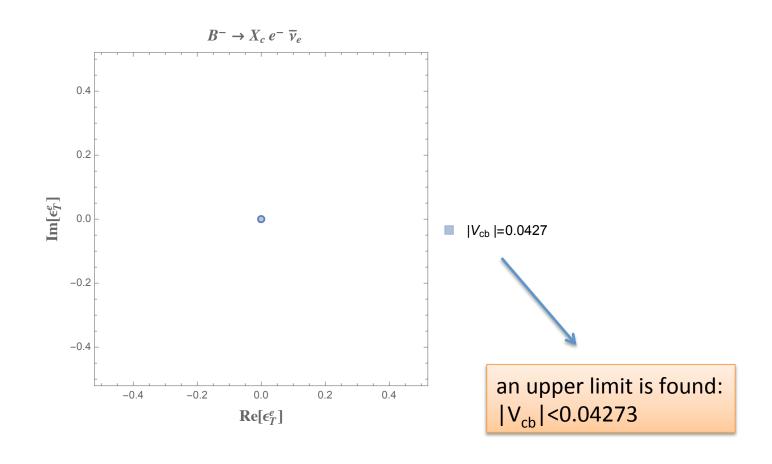




inclusive B -> $X_c \ell v_\ell$ decay: allowed regions



inclusive B -> $X_c \ell v_\ell$ decay: allowed regions



Exclusive B -> $D^{(*)} \ell v_{\ell}$ decay

$$\frac{d\Gamma}{dq^2}(B \to M_c \ell \bar{\nu}_\ell) = \frac{d\Gamma}{dq^2} \bigg|_{\rm SM} + \frac{d\Gamma}{dq^2} \bigg|_{\rm NP} + \frac{d\Gamma}{dq^2} \bigg|_{\rm INT}$$

- B ->D and B->D*
- two sets of form factors: one for each structure in H_{eff}
- experimental data specific for e and μ available

$$B \rightarrow D \ell v_{\ell}$$

$$\langle D(p')|\bar{c}\gamma_{\mu}b|B(p)\rangle = F_{1}(q^{2})(p+p')_{\mu} + \frac{m_{B}^{2} - m_{D}^{2}}{q^{2}} \left[F_{0}(q^{2}) - F_{1}(q^{2})\right] q_{\mu}$$

$$\langle D(p')|\bar{c}\sigma_{\mu\nu}(1-\gamma_{5})b|B(p)\rangle = F_{T}(q^{2}) \underbrace{F_{T}(q^{2})}_{m_{B}+m_{D}} \epsilon_{\mu\nu\alpha\beta}p'^{\alpha}p^{\beta} + i\underbrace{G_{T}(q^{2})}_{m_{B}+m_{D}} (p_{\mu}p'_{\nu} - p_{\nu}p'_{\mu})$$

HQ relations: all form factors in terms of the Isgur Wise

- m_h^{-1} and α_s corrections known for F_1 and F_0
- leading order relations for F_{T} and G_{T}



- F₁ and F₀ from lattice
- HQ relations to derive F_T and G_T from F_1 , F_0

J.A. Bailey et al.,

PRD 89 (2014) 114504

I. Caprini, L. Lellouch, M. Neubert,

M. Neubert,

Phys. Rep. 245 (1994) 259

NPB 530 (1998) 153

Compare to experiment:

$$\begin{split} \mathcal{B}(B^- \to D^0 \mu^- \bar{\nu}_\mu) &= (2.25 \pm 0.04 \pm 0.17) \times 10^{-2} \\ \\ \mathcal{B}(B^- \to D^0 e^- \bar{\nu}_e) &= (2.38 \pm 0.04 \pm 0.15) \times 10^{-2}. \end{split}$$

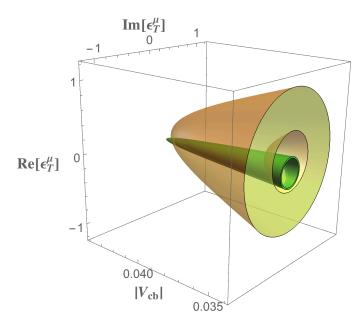
$$\mathcal{B}(B^- \to D^0 e^- \bar{\nu}_e) = (2.38 \pm 0.04 \pm 0.15) \times 10^{-2}$$
.

BABAR Collab., PRD 79 (2009) 012002

Theory prediction depends on $|V_{ch}|$ and on the complex parameter ε_T

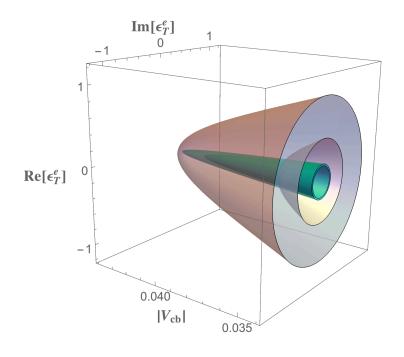
$$(\mathrm{Re}(\epsilon_T^{\ell}),\mathrm{Im}(\epsilon_T^{\ell}),|V_{cb}|)$$

$B \rightarrow D \ell v_{\ell} + B \rightarrow X_{c} \ell v_{\ell}$: allowed regions



 μ channel

inner regions: inclusive outer regions: exclusive



e channel

role of the lepton mass:

the symmetry axes of the two regions do not coincide in the case of μ , they are almost coincident for e

$$B \rightarrow D^* \ell \nu_{\ell}$$

procedure adopted by BaBar

$$q^2 = m_B^2 + m_{D^{(*)}}^2 - 2m_B m_{D^{(*)}} w.$$

BABAR, PRD79, 012002 (2009)

$$\frac{d\Gamma}{dw}(B \to D^*\ell\bar{\nu}_\ell) = \frac{G_F^2|V_{cb}|^2 m_B^5}{48\pi^3} (1 - r^*)^2 r^{*3} W_{D^*}(w) h_{A_1}^2(w) \sqrt{w^2 - 1} (w + 1)^2$$

$$\left\{ \left[1 + (1 - R_2(w)) \frac{w - 1}{1 - r^*} \right]^2 + 2 \left[\frac{1 - 2wr^* + r^{*2}}{(1 - r^*)^2} \right] \left[1 + R_1(w)^2 \frac{w - 1}{w + 1} \right] \right\}$$

$$R_2(w) \triangleq R_1(1) + 0.11(w - 1) - 0.06(w - 1)^2 R_1(w) = R_1(1) - 0.12(w - 1) + 0.05(w - 1)^2$$

$$h_{A_1}(w) = h_{A_1}(1)[1 - 8\hat{\rho}^2 z + (53\hat{\rho}^2 - 15)z^2 - (231\hat{\rho}^2 - 91)z^3]$$

Parameters	De sample	$D\mu$ sample	Combined result
ρ_D^2	$1.22 \pm 0.05 \pm 0.10$	$1.10 \pm 0.07 \pm 0.10$	$1.16 \pm 0.04 \pm 0.08$
$ ho_D^2 ho_{D^*}$	$1.34 \pm 0.05 \pm 0.09$	$1.33 \pm 0.06 \pm 0.09$	$1.33 \pm 0.04 \pm 0.09$
R_1	$1.59 \pm 0.09 \pm 0.15$	$1.53 \pm 0.10 \pm 0.17$	$1.56 \pm 0.07 \pm 0.15$
R_2	$0.67 \pm 0.07 \pm 0.10$	$0.68 \pm 0.08 \pm 0.10$	$0.66 \pm 0.05 \pm 0.09$
$\mathcal{B}(D^0\ell\bar{\nu})(\%)$	$2.38 \pm 0.04 \pm 0.15$	$2.25 \pm 0.04 \pm 0.17$	$2.32 \pm 0.03 \pm 0.13$
$\mathcal{B}(D^{*0}\ell\bar{\nu})(\%)$	$5.50 \pm 0.05 \pm 0.23$	$5.34 \pm 0.06 \pm 0.37$	$5.48 \pm 0.04 \pm 0.22$
χ^2 /n.d.f. (probability)	416/468 (0.96)	488/464 (0.21)	2.0/6 (0.92)

$$h_{A_1}^e(1)|V_{cb}| = (35.94 \pm 1.65) \times 10^{-3}.$$

$$h_{A_1}^{\mu}(1)|V_{cb}| = (35.63 \pm 1.96) \times 10^{-3}$$

$$B \rightarrow D^* \ell \nu_{\ell}$$

compare experiment to theory when w->1:

$$\begin{split} &\frac{d\Gamma^{\text{th}}}{dw}(B^{-}\to D^{*0}\ell^{-}\bar{\nu}_{\ell})|_{w\to 1} \\ &= \frac{G_{R}^{2}(V_{cb}|^{2})n_{D^{*}}^{2}}{16\sqrt{2}\pi^{3}}\sqrt{w-1}\left[1-\frac{m_{\ell}^{2}}{(m_{B}-m_{D^{*}})^{2}}\right]^{2} \\ &\times \{(m_{B}+m_{D^{*}})^{2}[2(m_{B}-m_{D^{*}})^{2}+m_{\ell}^{2}]A_{1}(1)^{2} \\ &+ [\epsilon_{T}]^{2}4[(m_{B}-m_{D^{*}})^{2}+2m_{\ell}^{2}][m_{B}\tilde{T}_{1}(1)+m_{D^{*}}\tilde{T}_{2}(1)]^{2} \\ &-12\text{Re}(\epsilon_{T})(m_{B}^{2}-m_{D^{*}}^{2})m_{\ell}A_{1}(1)[m_{B}\tilde{T}_{1}(1)+m_{D^{*}}\tilde{T}_{2}(1)]\} \end{split}$$

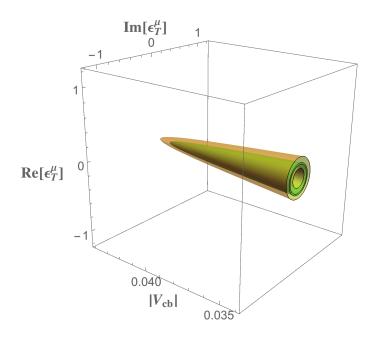


- A₁(1) known from lattice
- the others from HQ relations

theory prediction depends on $|V_{cb}|$ and on the complex parameter ε_T^{ℓ}

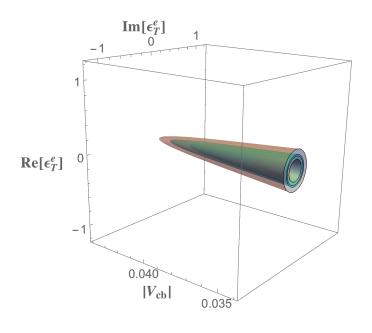
$$(\operatorname{Re}(\epsilon_T^\ell),\operatorname{Im}(\epsilon_T^\ell),|V_{cb}|)$$

B -> D* $\ell \nu_{\ell}$ + B -> $X_c \ell \nu_{\ell}$: allowed regions



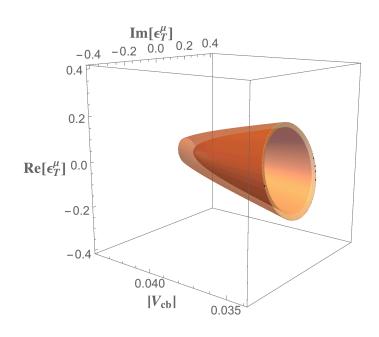
 μ channel

inner regions: inclusive mode outer regions: exclusive mode



e channel

B -> D ℓv_{ℓ} +B -> D* ℓv_{ℓ} + B -> $X_{c} \ell v_{\ell}$: allowed regions

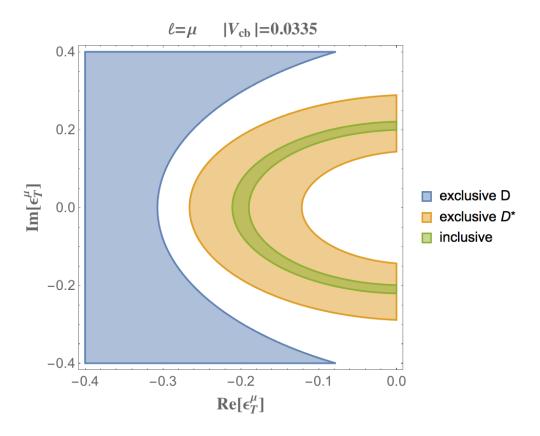


 μ channel

e channel

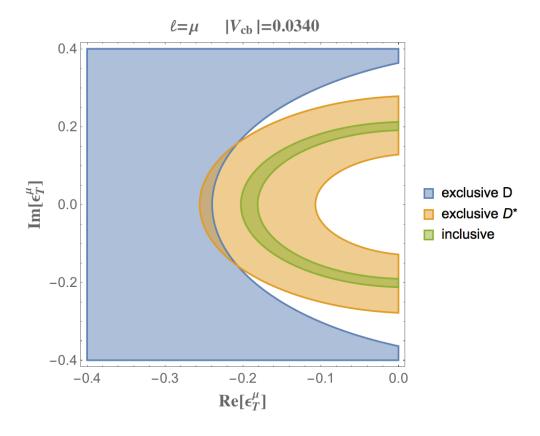
projections in the (Re ε_{T} , Im ε_{T}) plane

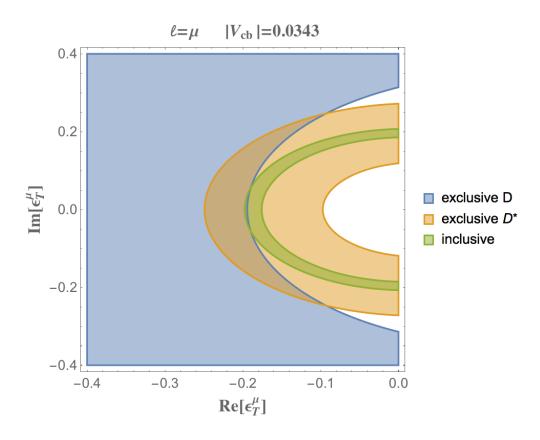
μ channel



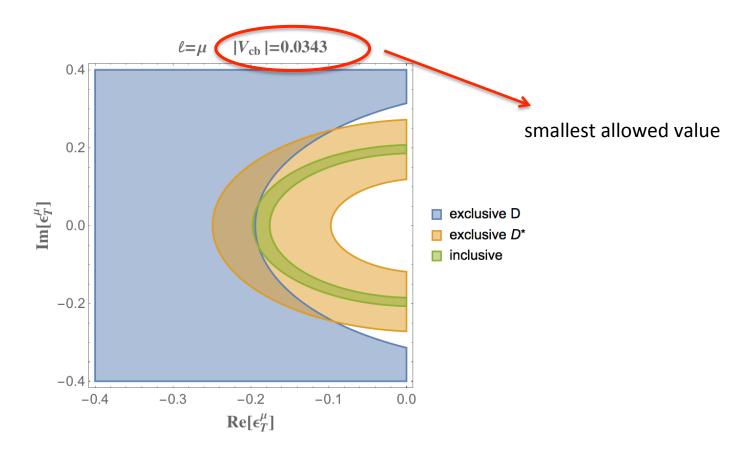
projections in the (Re ε_{T} , Im ε_{T}) plane

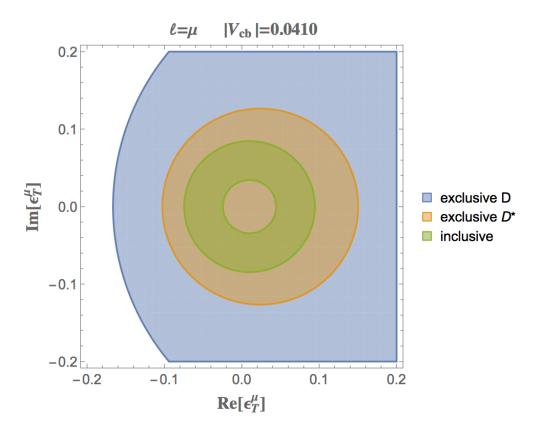
μ channel

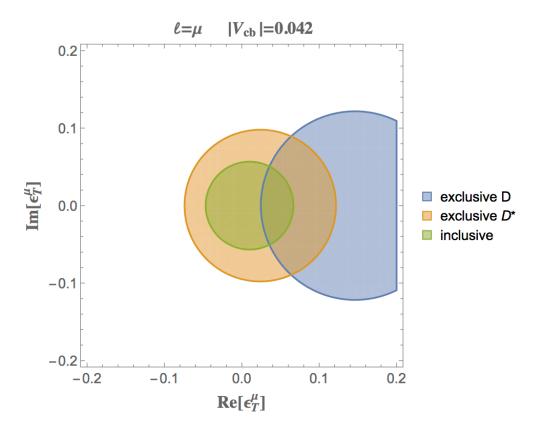


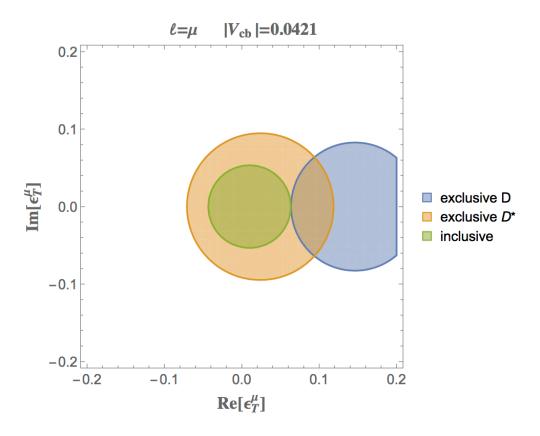


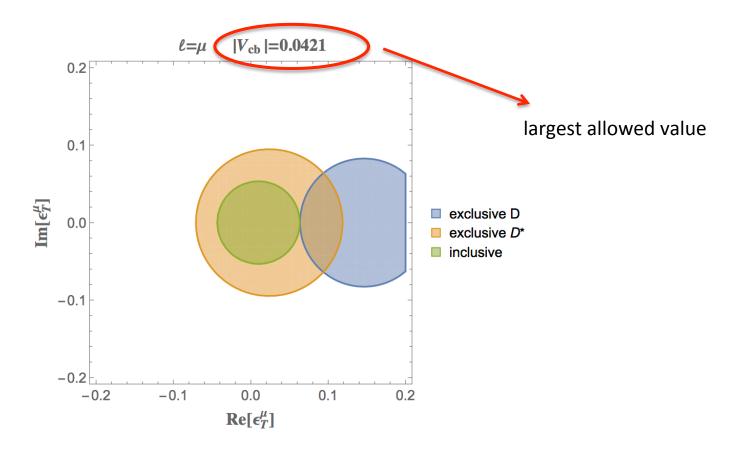
projections in the (Re ε_T , Im ε_T) plane





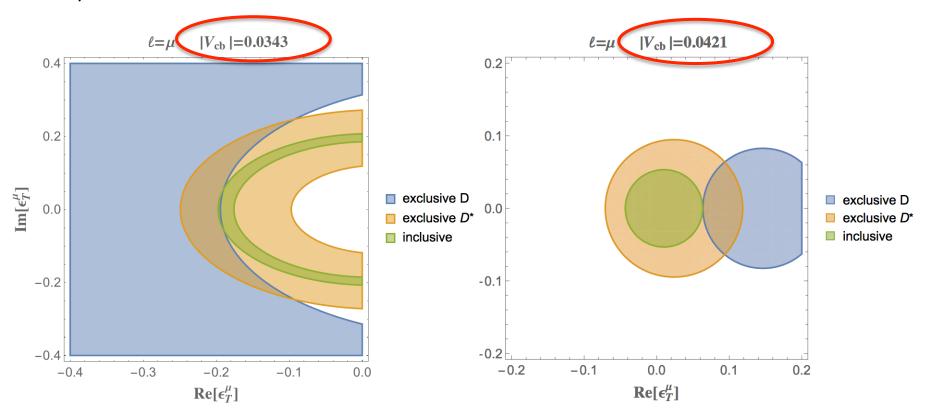






projections in the (Re ε_T , Im ε_T) plane

μ channel

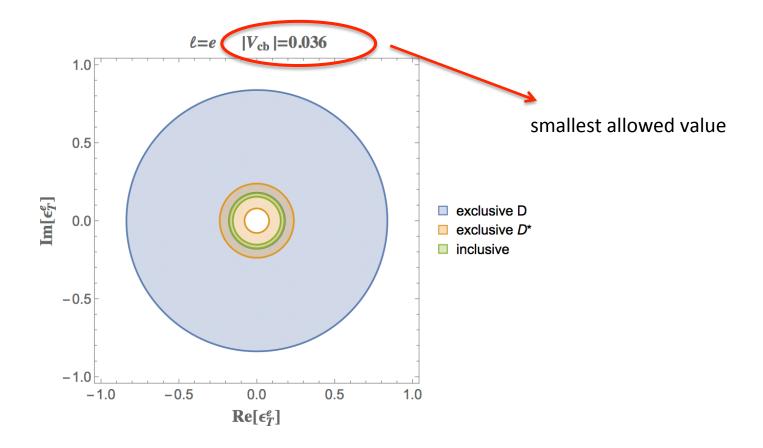


selected range

 $|V_{cb}| \in [0.0343, 0.0421]$

projections in the (Re ε_T , Im ε_T) plane

e channel



the largest value found from inclusive does not change

selected range

$$|V_{cb}| \in [0.036, 0.0427]$$

V_{cb} range from both modes

 μ channel

e channel

$$|V_{cb}| \in [0.0343, 0.0421]$$





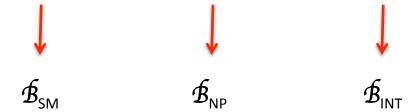
all constraints can be fulfilled in

$$|V_{cb}| \in [0.036, 0.042]$$

role of the NP contributions

$$B \rightarrow X_c \ell v_\ell$$

$$\frac{d\Gamma}{d\hat{q}^2} = C(q^2) \left[\frac{d\tilde{\Gamma}}{d\hat{q}^2} \bigg|_{\text{SM}} + |\epsilon_T|^2 \frac{d\tilde{\Gamma}}{d\hat{q}^2} \bigg|_{\text{NP}} + \text{Re}(\epsilon_T) \frac{d\tilde{\Gamma}}{d\hat{q}^2} \bigg|_{\text{INT}} \right]$$

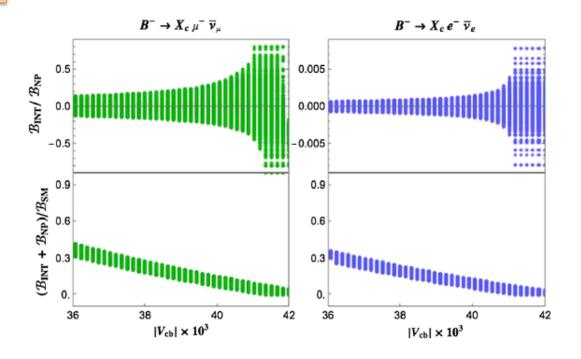




compute varying Re(ϵ_T), Im(ϵ_T) and $|V_{cb}|$ only in the *allowed* region

role of the NP contributions

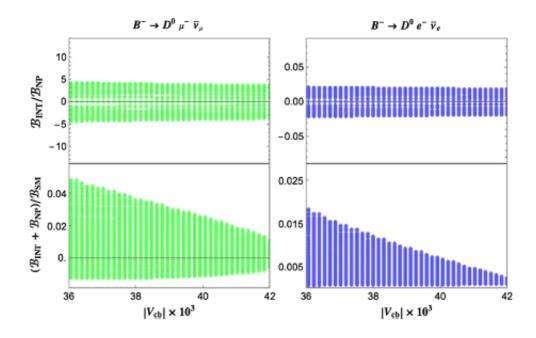
$$B \rightarrow X_c \ell \nu_{\ell}$$



- interference term can be sizable for μ
- the total NP contribution (NP+INT) is negligible for both e and μ when $|V_{cb}|$ is large

role of the NP contributions

$$B \rightarrow D \ell v_{\ell}$$



- interference term can be sizable for μ
- the total NP contribution (NP+INT) has a larger impact in the inclusive mode



the role of NP is different in different channels! a NP H_{eff} might be at the origin of the $|V_{cb}|$ anomaly

$$\frac{d\Gamma(\bar{B} \to D^* l \bar{\nu}_l)}{dw \, d\cos\theta_v \, d\cos\theta_l \, d\chi}$$

Boyd-Grinstein-Lebed (BGL) form factor parametrization instead of Caprini-Lellouch-Neubert (CLN)

differences:

CLN relies on HQET relations (4 parameter fit of the differential rate)

BGL based on unitarity, analiticity (as CLN)

BGL includes single particle (B_c*) contributions (8 parameter fit)

BGL more conservative, data at low recoil better reproduced

→ |V_{cb}| from the fit with BGL closer to the inclusive determination (with a larger uncertainty)

warning: only new Belle data considered

A few words about V_{ub}

- Inclusive determination from B-> X_u I v -> OPE : the same parameters! requires shape function (moments related to the OPE parameters)
- Exclusive: from B-> π I ν , Λ_b -> p I ν : requires FF
- Exclusive leptonic: from B -> $\tau \nu$: requires f_B

Inclusive vs exclusive:

recent lattice calculation of B-> π FF point to larger values of $|V_{ub}|_{excl}$ discrepancy still at 3 σ level

If LFU violation exists in b -> c we should probably see it also in b->u

universal breaking pattern?

Challenging the lepton flavour universality opens new perspectives in NP searches

What is needed

• separate measurements for \emph{e} and μ inclusive and exclusive B modes

 V_{cb}

• new modes, e.g. measurements of B_s and Λ_b semileptonic decays

 V_{cb} R(D^(*))

• modes where the tensor operator does not contribute, i.e. $B_c -> \tau v_{\tau}$

 V_{cb} $R(D^{(*)})$

new observables where effects are expected, e.g. D_i**
 (are F-B asymmetries accessible?)

 V_{cb} $R(D^{(*)})$

Same breaking pattern in b->u transitions?

 V_{ub}

A lot of surprises from three-level processes

The journey in search of phenomena beyond SM continues....