

Unitarity Triangle analysis in the Standard Model and beyond from UTfit



Marcella Bona (and/or Luca Silvestrini)

QMUL The QMUL logo consists of the letters "QMUL" in a blue serif font, followed by a blue icon of a crown or castle tower.

on behalf of the UTfit Collaboration

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47th EPS-HEP Conference,
Venice, Italy

Unitarity Triangle analysis in the SM

● SM UT analysis:

- provide the best determination of CKM parameters
- test the consistency of the SM (“*direct*” vs “*indirect*” determinations)
- provide predictions (from data..) for SM observables
- charm mixing averages

.. and beyond

● NP UT analysis:

- model-independent analysis
- provides limit on the allowed deviations from the SM
- obtain the NP scale

the method and the inputs:

$$f(\bar{\rho}, \bar{\eta}, X | c_1, \dots, c_m) \sim \prod_{j=1,m} f_j(\mathcal{C} | \bar{\rho}, \bar{\eta}, X) * \prod_{i=1,N} f_i(x_i) f_0(\bar{\rho}, \bar{\eta})$$

Bayes Theorem

$X \equiv x_1, \dots, x_n = m_t, B_K, F_B, \dots$

$\mathcal{C} \equiv c_1, \dots, c_m = \epsilon, \Delta m_d / \Delta m_s, A_{CP}(J/\psi K_S), \dots$

$(b \rightarrow u)/(b \rightarrow c)$

$\bar{\rho}^2 + \bar{\eta}^2$

$\bar{\Lambda}, \lambda_1, F(1), \dots$

Standard Model +
OPE/HQET/
Lattice QCD

ϵ_K

$\bar{\eta}[(1 - \bar{\rho}) + P]$

B_K

Δm_d

$(1 - \bar{\rho})^2 + \bar{\eta}^2$

$f_B^2 B_B$

to go

$\Delta m_d / \Delta m_s$

$(1 - \bar{\rho})^2 + \bar{\eta}^2$

ξ

from quarks
to hadrons

$A_{CP}(J/\psi K_S)$

$\sin 2\beta$

M. Bona *et al.* (UTfit Collaboration)
JHEP 0507:028,2005 hep-ph/0501199
M. Bona *et al.* (UTfit Collaboration)
JHEP 0603:080,2006 hep-ph/0509219

V_{cb} and V_{ub}

New HFAG (HFLAV) @CKM16

$$|V_{cb}| \text{ (excl)} = (38.88 \pm 0.60) 10^{-3}$$

$$|V_{cb}| \text{ (incl)} = (42.19 \pm 0.78) 10^{-3}$$

New HFAG @CKM16

$\sim 3.3\sigma$ discrepancy

New HFAG @CKM16

$$|V_{ub}| \text{ (excl)} = (3.65 \pm 0.14) 10^{-3}$$

$$|V_{ub}| \text{ (incl)} = (4.50 \pm 0.20) 10^{-3}$$

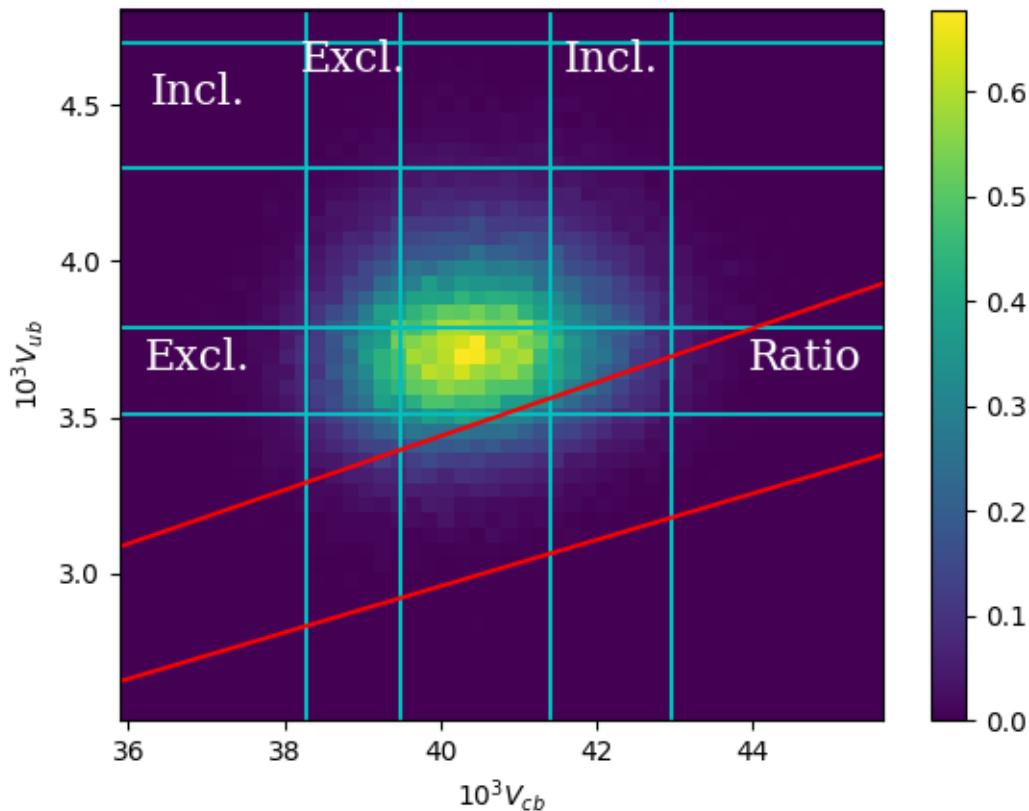
New HFAG @CKM16

$\sim 3.4\sigma$ discrepancy

$$|V_{ub} / V_{cb}| \text{ (LHCb)} = (8.0 \pm 0.6) 10^{-2}$$

Updated value

updated for LHCP17



V_{cb} and V_{ub}

2D average inspired by D'Agostini skeptical procedure (hep-ex/9910036) with $\sigma=1$. Very similar results obtained from a 2D a la PDG procedure.

$$|V_{cb}| = (40.5 \pm 1.1) 10^{-3}$$

uncertainty $\sim 2.4\%$

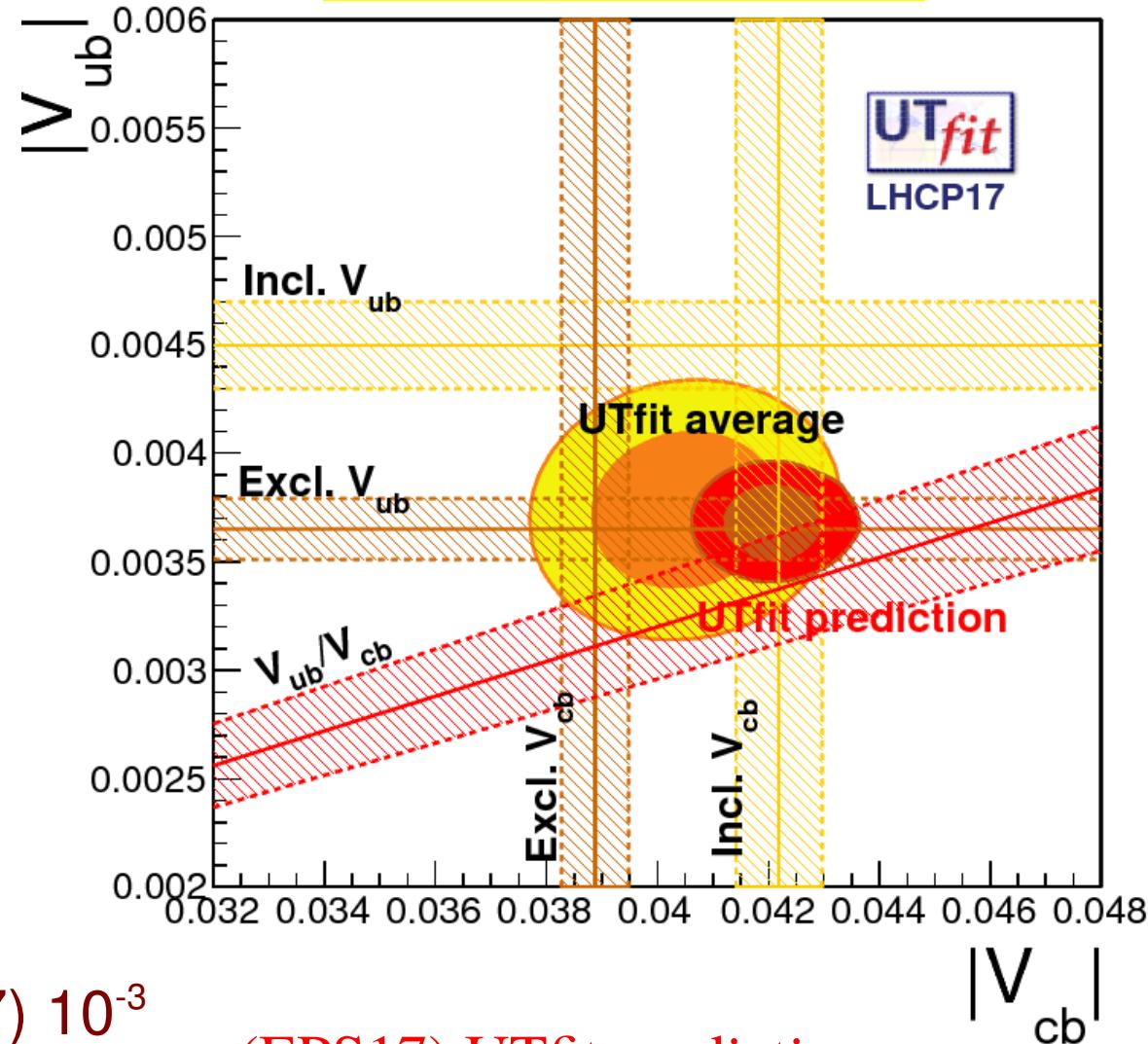
$$|V_{ub}| = (3.74 \pm 0.23) 10^{-3}$$

uncertainty $\sim 5.6\%$

$$|V_{cb}| = (42.7 \pm 0.7) 10^{-3}$$

$$|V_{ub}| = (3.61 \pm 0.12) 10^{-3}$$

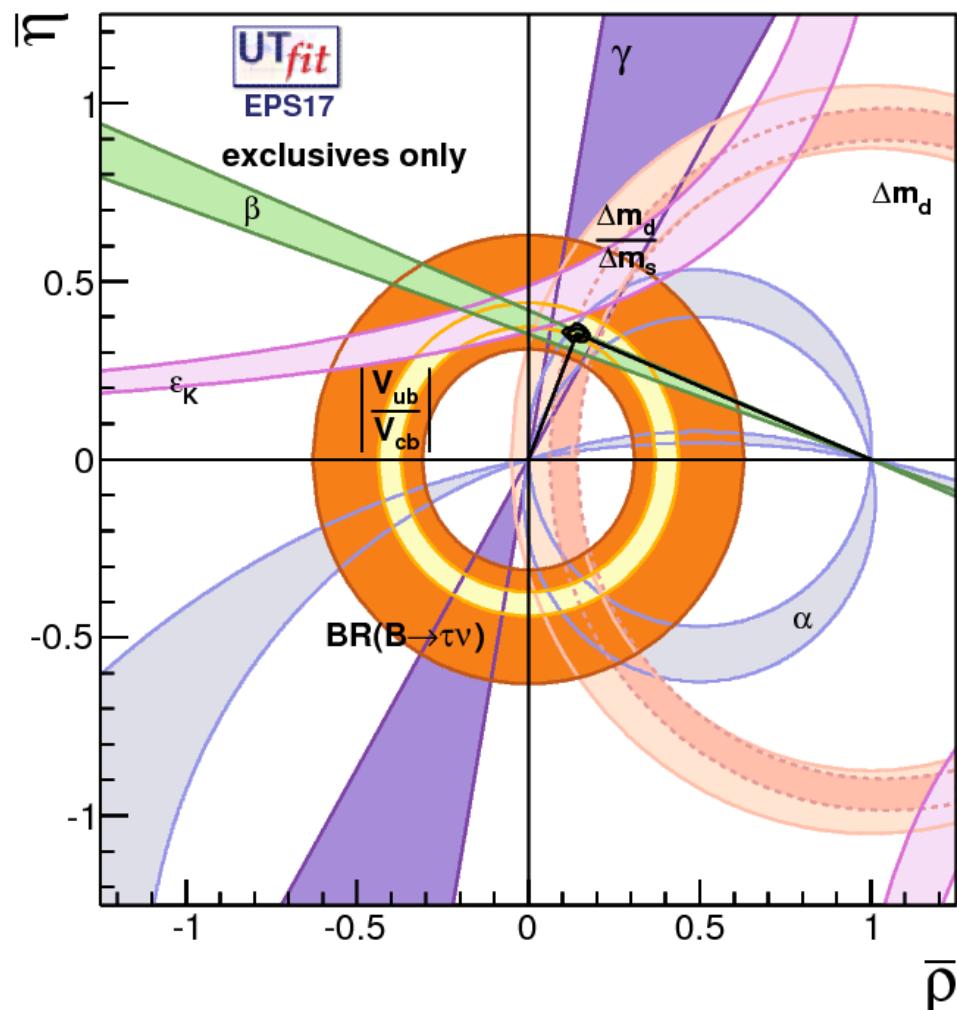
updated for LHCP17



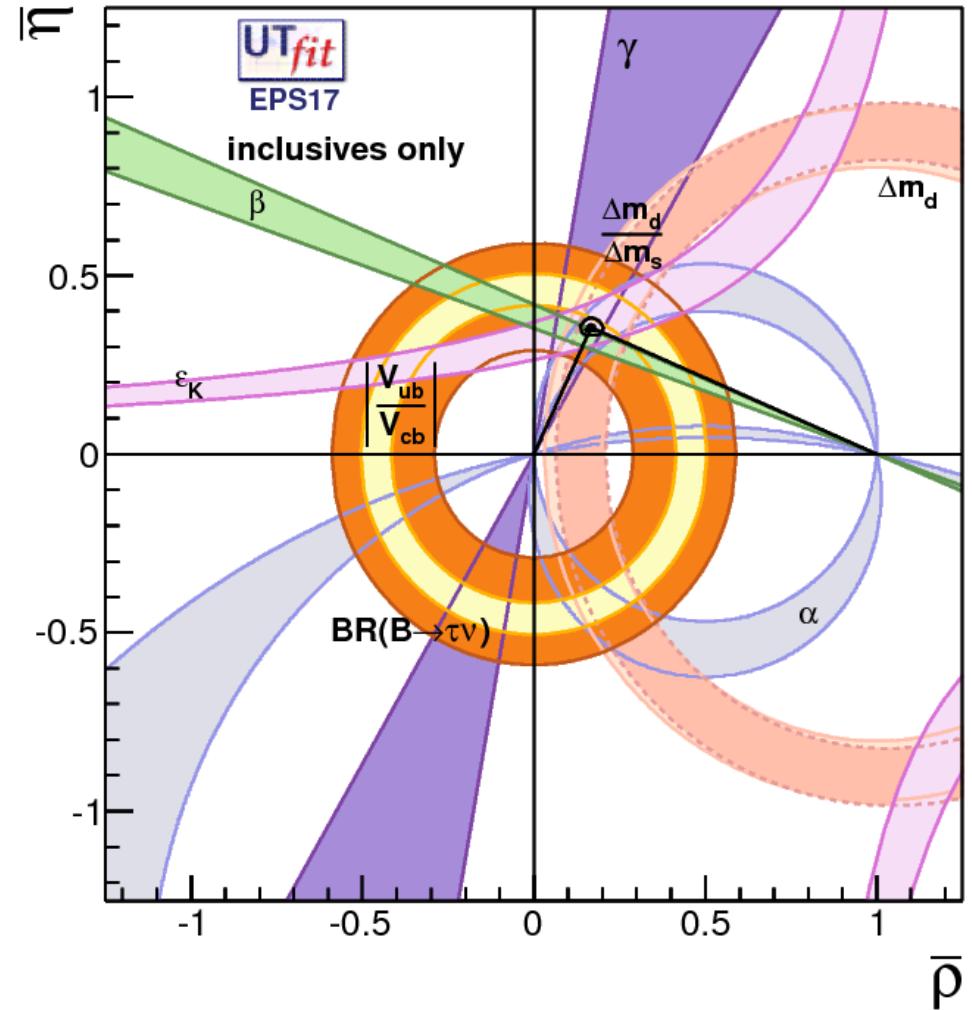
(EPS17) UTfit predictions

exclusives vs inclusives

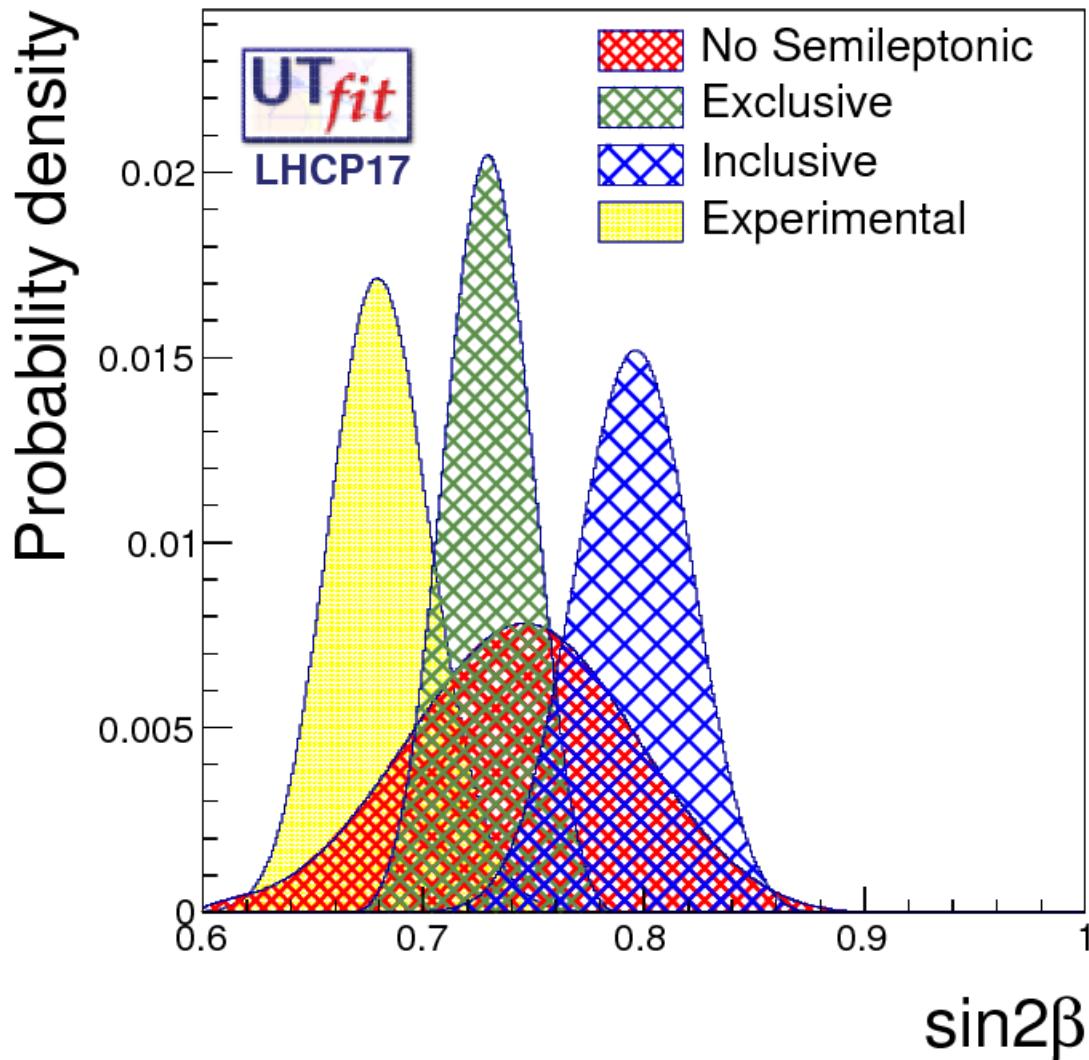
only exclusive values



only inclusive values



exclusives vs inclusives



EPS17: updated input value

$J/\psi K^0$ average 0.680 ± 0.019 (B-factories + LHCb)
adding -0.01 ± 0.01 as data-driven theory uncertainty

predictions from
the EPS17 fit:

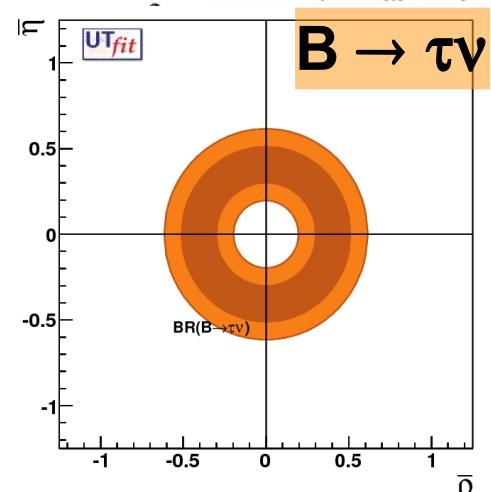
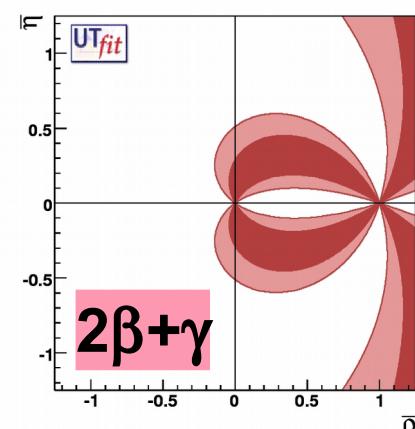
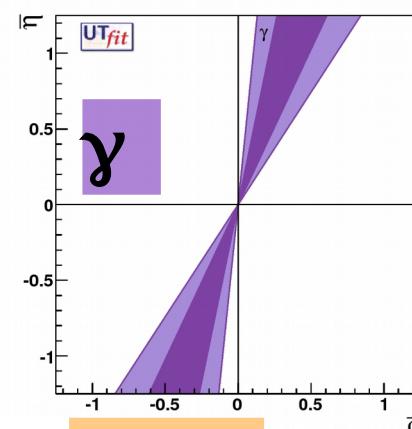
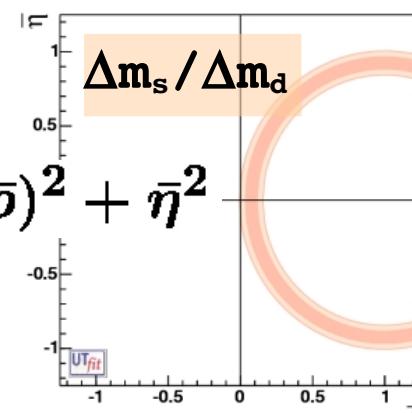
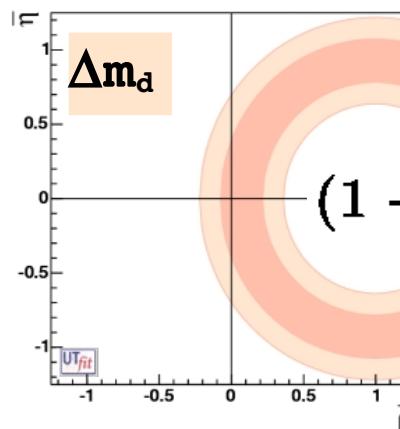
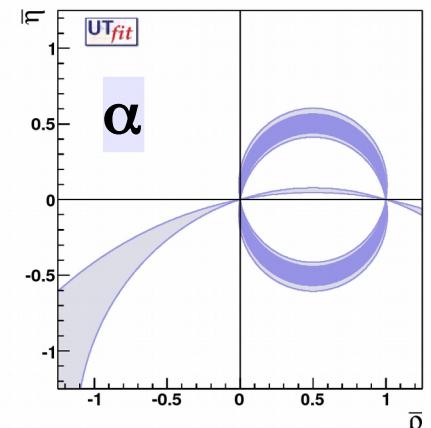
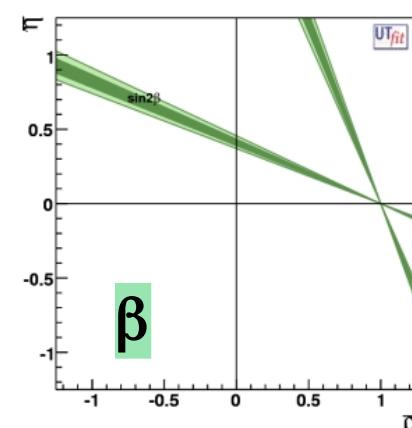
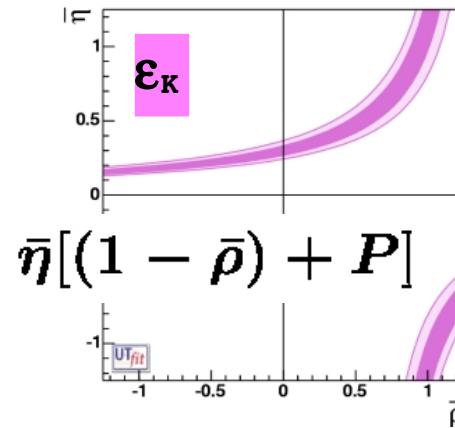
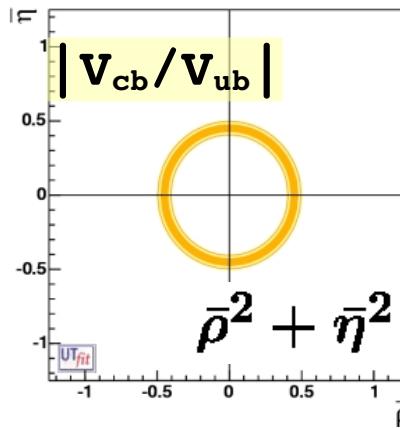
$$\sin 2\beta_{\text{UTfit}} = 0.729 \pm 0.017$$

$$\sin 2\beta_{\text{UTfit}} = 0.793 \pm 0.026$$

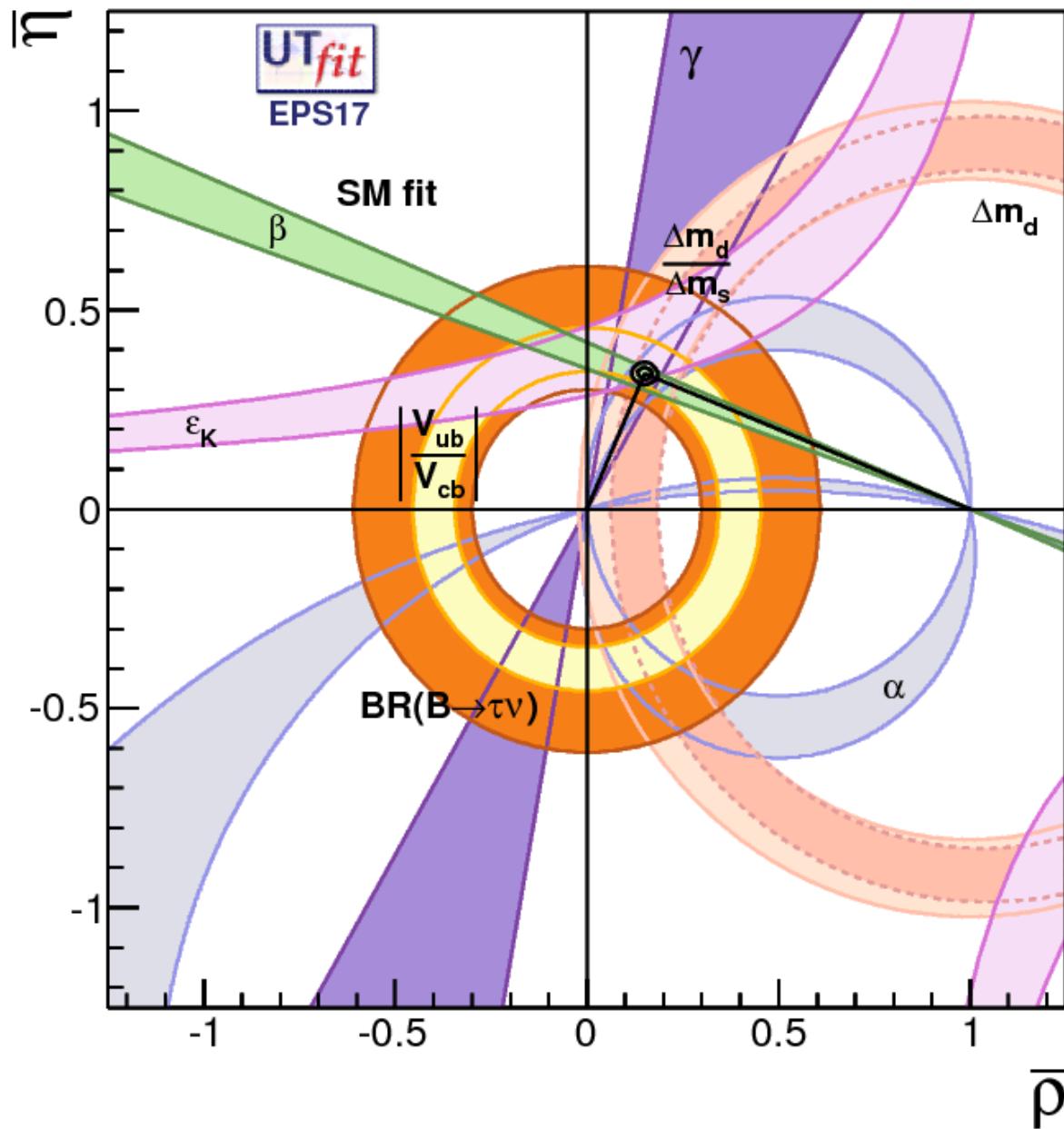
$$\sin 2\beta_{\text{exp}} = 0.670 \pm 0.022$$

$$\sin 2\beta_{\text{UTfit}} = 0.740 \pm 0.032$$

Unitarity Triangle analysis in the SM:



Unitarity Triangle analysis in the SM:



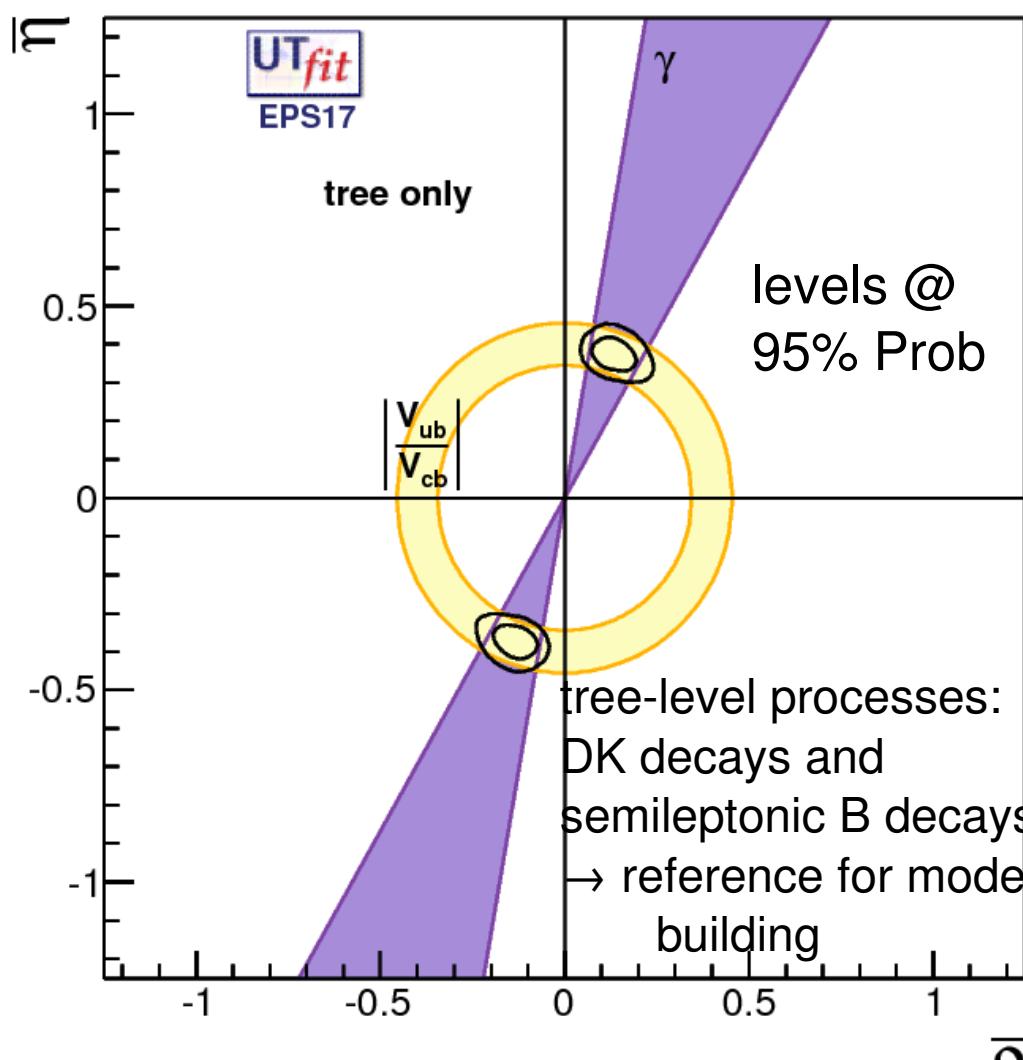
levels @
95% Prob

~9%

$$\begin{aligned}\bar{\rho} &= 0.151 \pm 0.014 \\ \bar{\eta} &= 0.342 \pm 0.013\end{aligned}$$

~4%

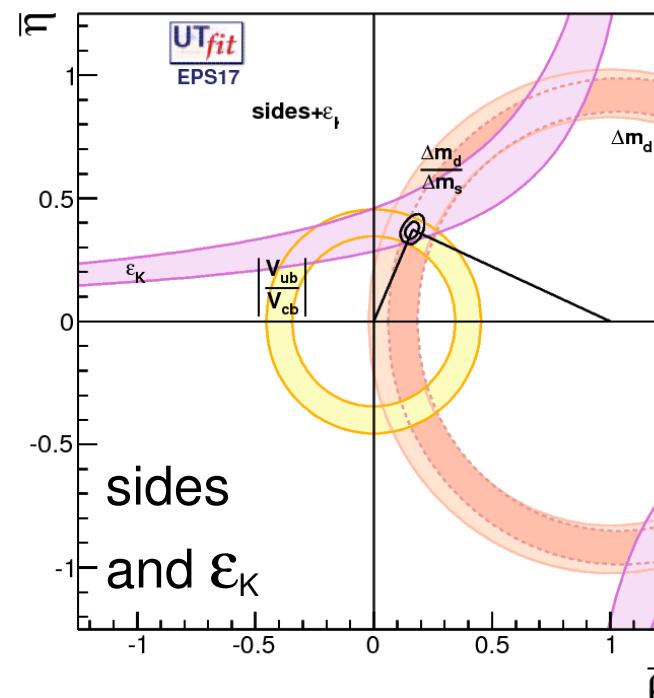
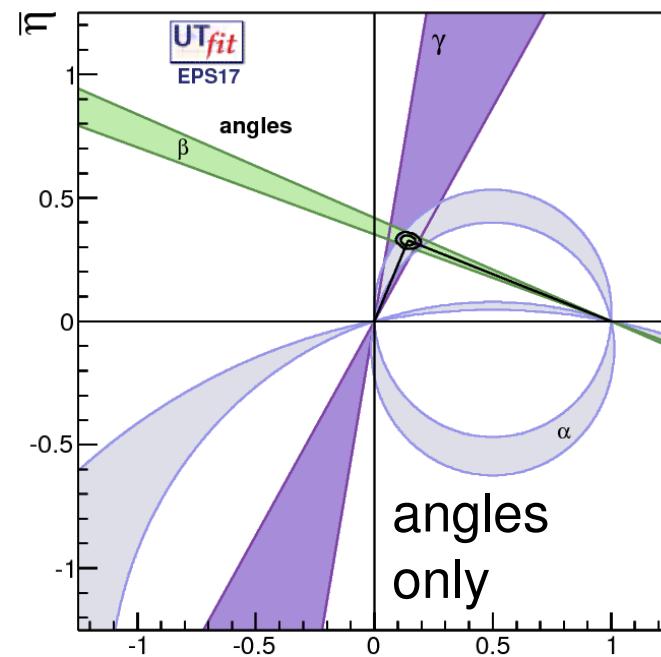
Unitarity Triangle analysis in the SM:



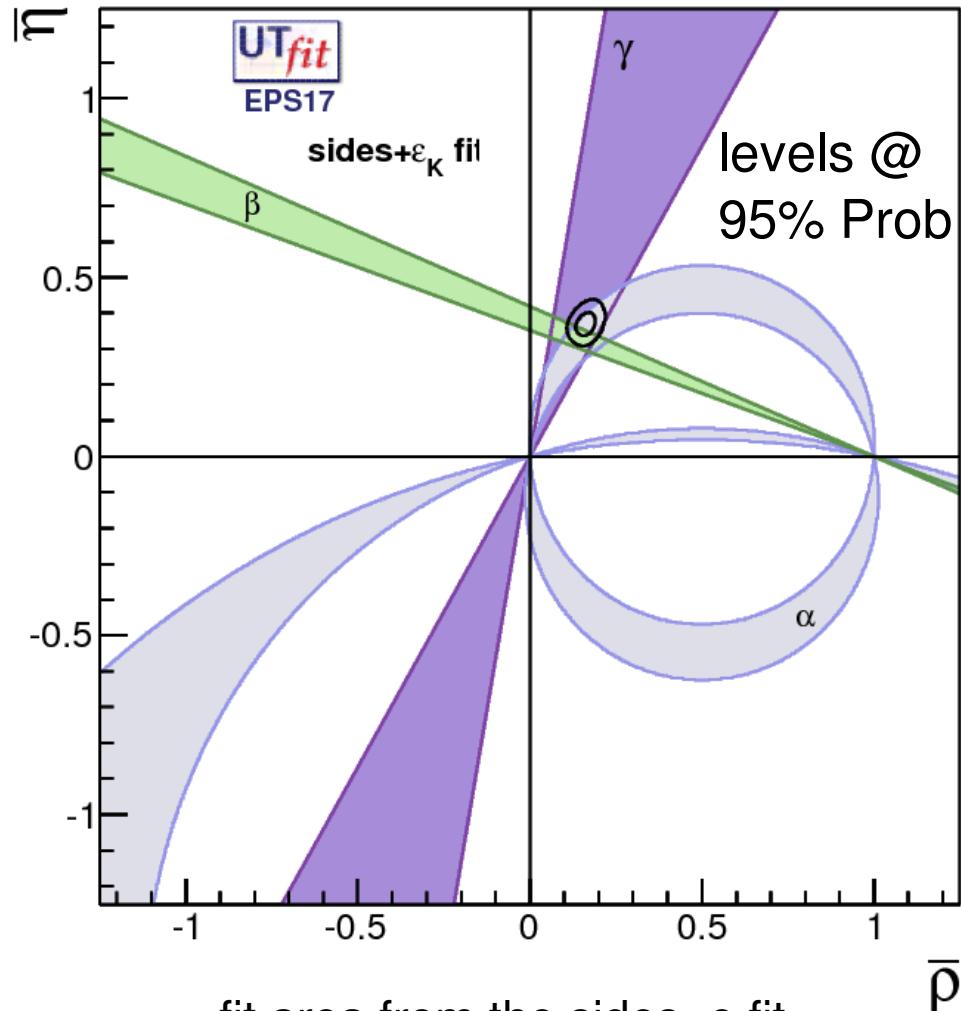
$$\bar{\rho} = 0.137 \pm 0.040$$

$$\bar{\eta} = 0.374 \pm 0.029$$

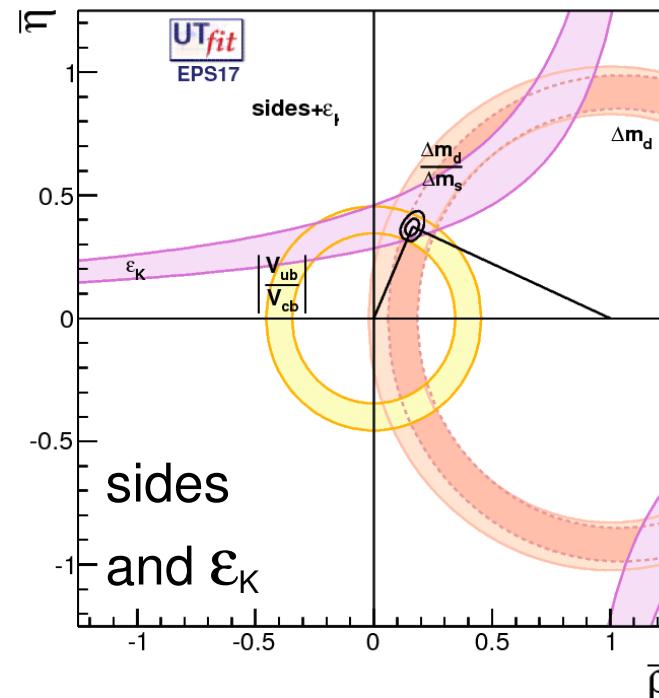
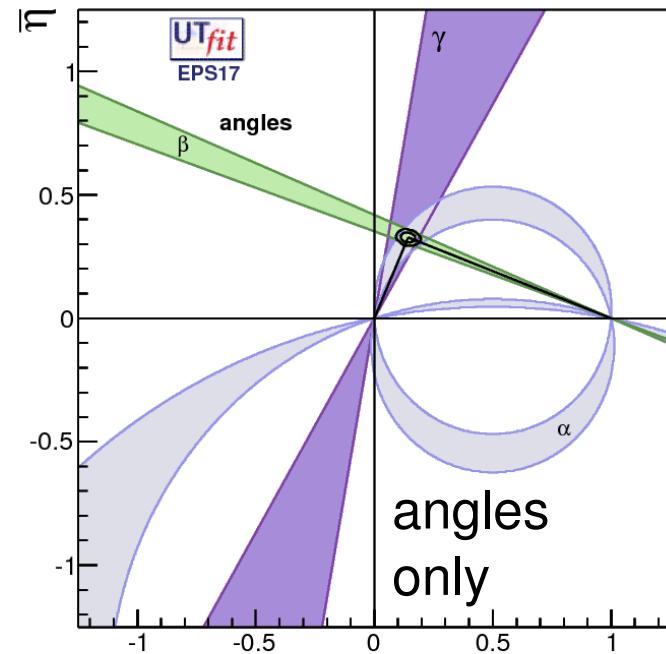
$\sim 29\%$
 $\sim 8\%$



Unitarity Triangle analysis in the SM:



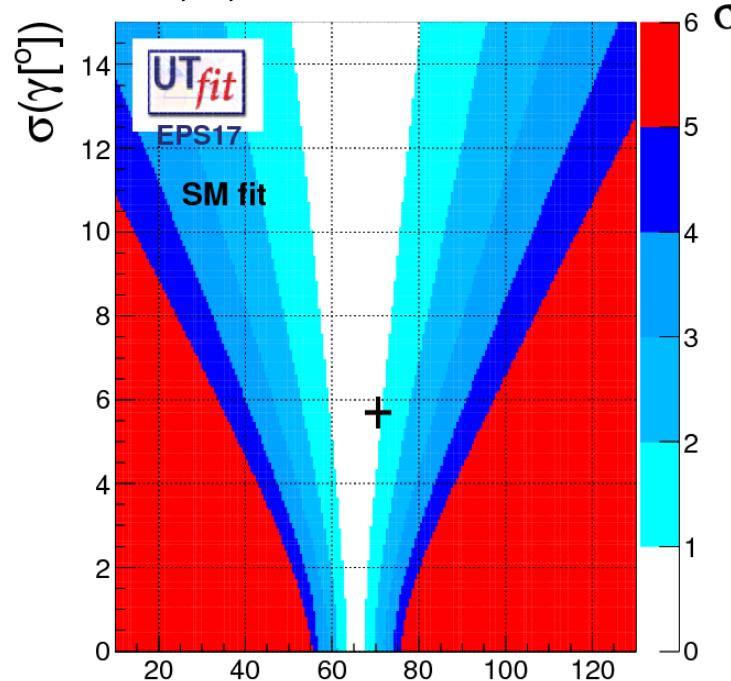
fit area from the sides+e fit
compared to the areas of the
three angle constraints



compatibility plots

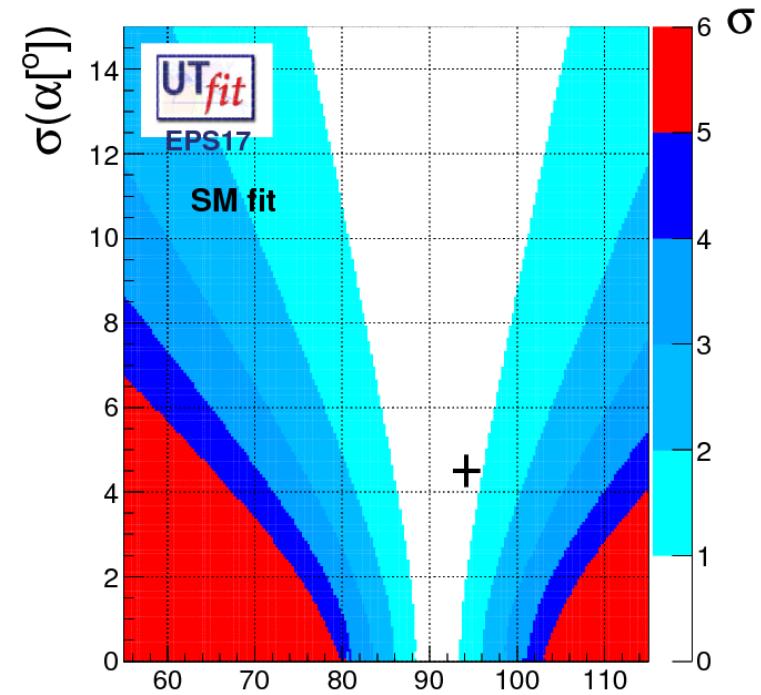
A way to “measure” the agreement of a single measurement with the indirect determination from the fit using all the other inputs: test for the SM description of the flavour physics

Color code: agreement between the predicted values and the measurements at better than 1, 2, ... σ



$$\begin{aligned}\gamma_{\text{exp}} &= (70.5 \pm 5.7)^\circ & \gamma[\circ] \\ \gamma_{\text{UTfit}} &= (65.6 \pm 2.2)^\circ\end{aligned}$$

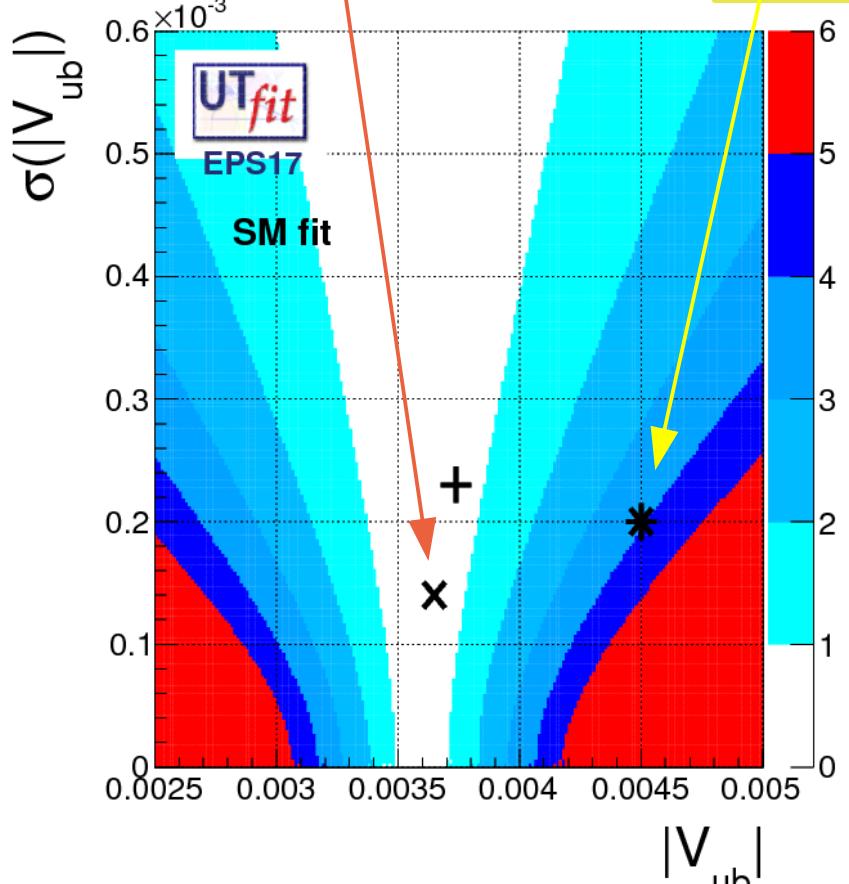
The cross has the coordinates $(x,y)=(\text{central value}, \text{error})$ of the direct measurement



$$\begin{aligned}\alpha_{\text{exp}} &= (94.2 \pm 4.5)^\circ & \alpha[\circ] \\ \alpha_{\text{UTfit}} &= (91.0 \pm 2.5)^\circ\end{aligned}$$

tensions? not really.. still that V_{ub} inclusive

$$V_{ub} \text{ (excl)} = (3.65 \pm 0.14) \cdot 10^{-3}$$



$$V_{ub\text{exp}} = (3.74 \pm 0.23) \cdot 10^{-3}$$

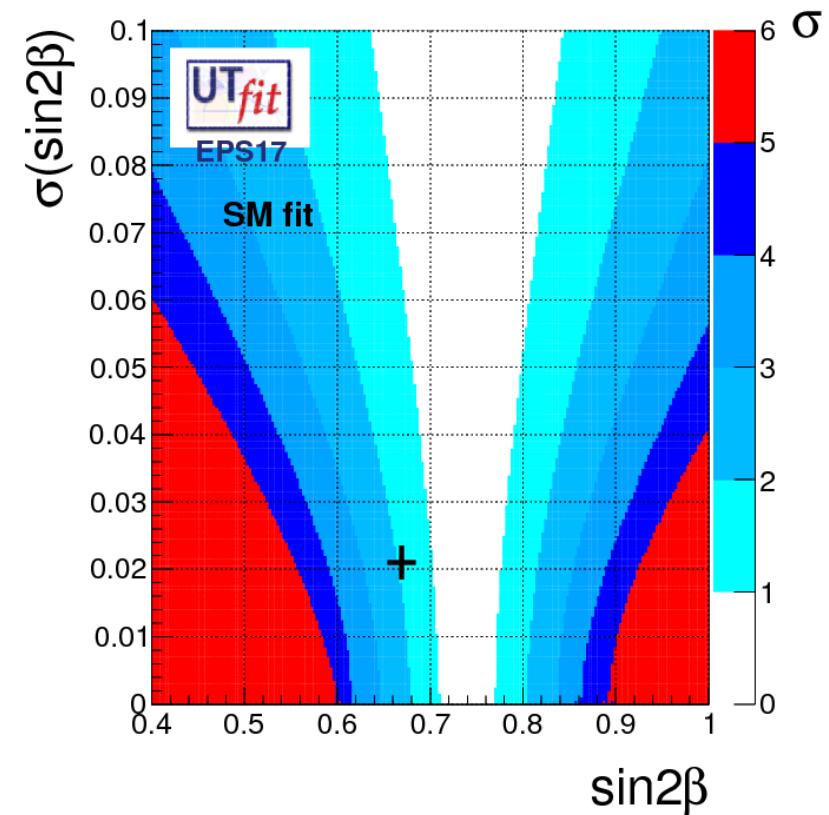
$$V_{ub\text{UTfit}} = (3.61 \pm 0.12) \cdot 10^{-3}$$

$$V_{ub} \text{ (incl)} = (4.50 \pm 0.20) \cdot 10^{-3}$$

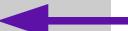
$\sim 1.8\sigma$

$$\sin 2\beta_{\text{exp}} = 0.670 \pm 0.022$$

$$\sin 2\beta_{\text{UTfit}} = 0.740 \pm 0.032$$



Unitarity Triangle analysis in the SM:

Observables	Measurement	Prediction	Pull (# σ)
$\sin 2\beta$	0.670 ± 0.022	0.740 ± 0.032	~ 1.8
γ	70.5 ± 5.7	65.6 ± 2.2	< 1
α	94.2 ± 4.5	91.0 ± 2.5	< 1
$ V_{ub} \cdot 10^3$	3.74 ± 0.23	3.61 ± 0.12	< 1
$ V_{ub} \cdot 10^3$ (incl)	4.50 ± 0.20	-	~ 3.8 
$ V_{ub} \cdot 10^3$ (excl)	3.65 ± 0.14	-	< 1
$ V_{cb} \cdot 10^3$	40.5 ± 1.1	42.7 ± 0.7	~ 1.7
$\text{BR}(B \rightarrow \tau\nu)[10^{-4}]$	1.06 ± 0.19	0.79 ± 0.06	~ 1.3
$A_{SL}^d \cdot 10^3$	-2.1 ± 1.7	-0.289 ± 0.027	~ 1
$A_{SL}^s \cdot 10^3$	-0.6 ± 2.8	0.013 ± 0.001	< 1

obtained excluding
the given constraint
from the fit

Mixing in the charm sector

Fit to data with parameters: x , y , $|q/p|$, $R_{k\pi}$, $\delta_{k\pi}$, $\delta_{k\pi\pi}$

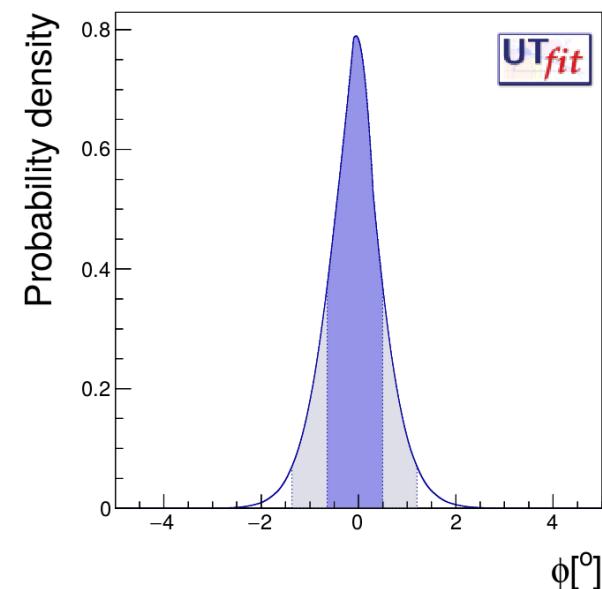
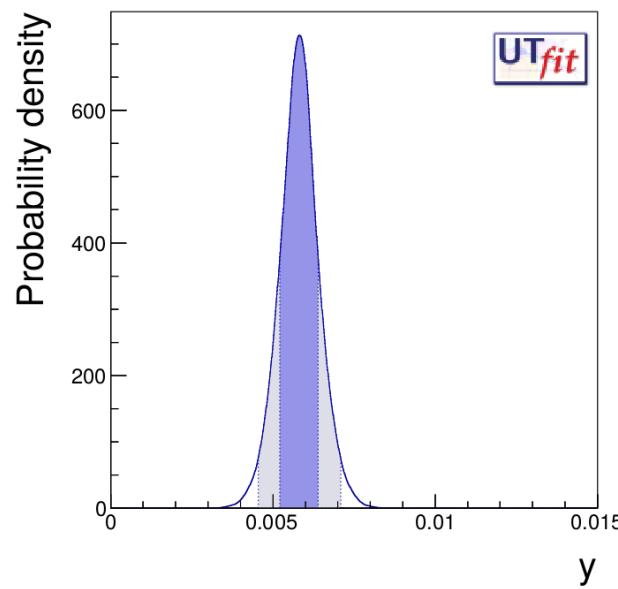
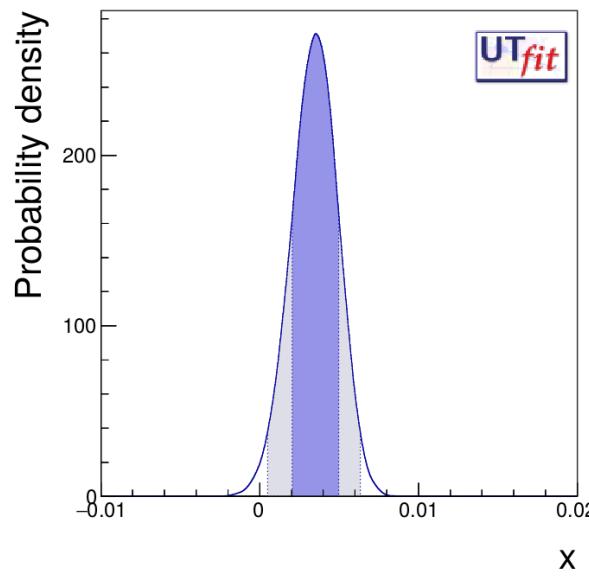
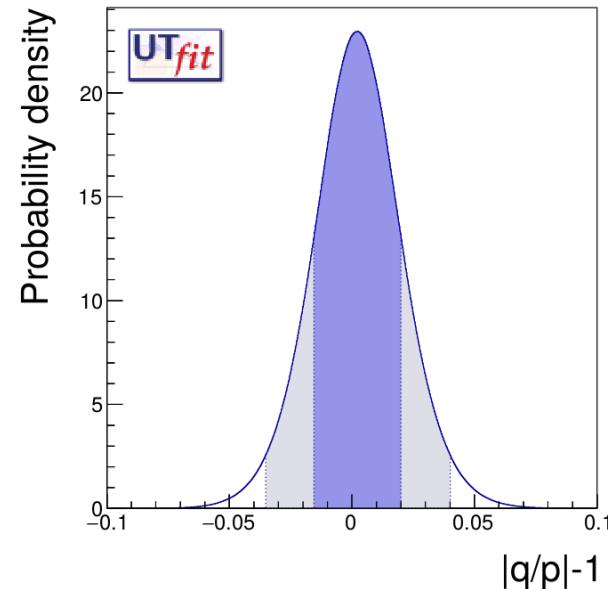
Summer17 UTfit average:

$$x = (3.5 \pm 1.5) 10^{-3}$$

$$y = (5.8 \pm 0.6) 10^{-3}$$

$$|q/p|-1 = (0.2 \pm 1.8) 10^{-2}$$

$$\phi = \arg(q/p) = (-0.08 \pm 0.57)^\circ$$



Mixing in the charm sector

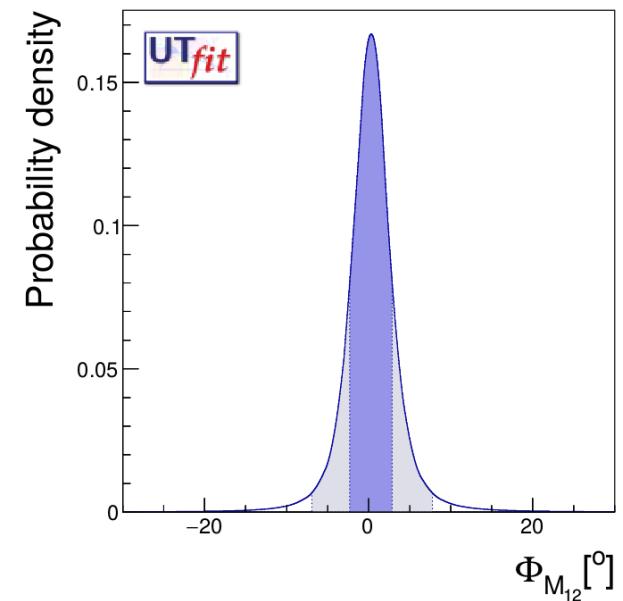
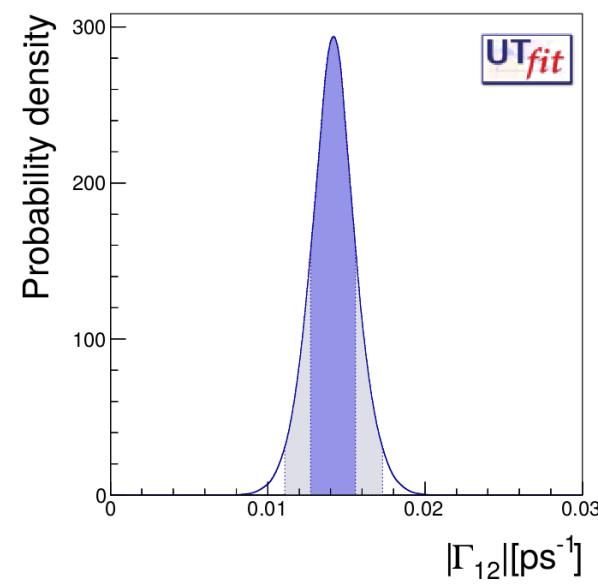
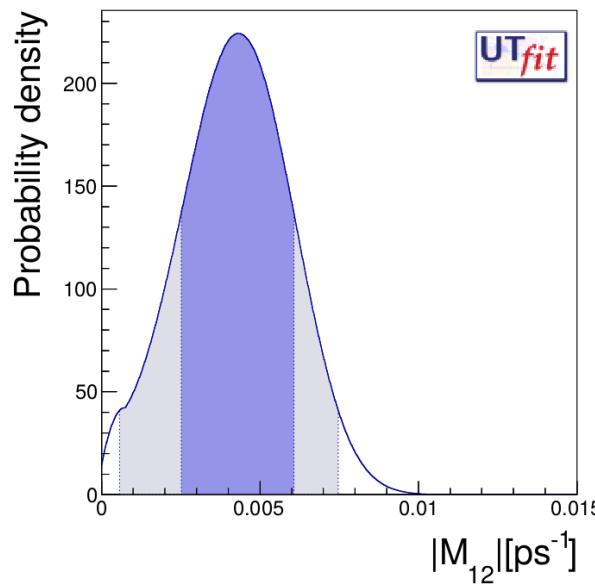
Fit to data with parameters: x , y , $|q/p|$, $R_{k\pi}$, $\delta_{k\pi}$, $\delta_{k\pi\pi}$

The corresponding results on fundamental parameters are

$$|M_{12}| = (4.3 \pm 1.8)/\text{fs},$$

$$|\Gamma_{12}| = (14.2 \pm 1.4)/\text{fs}$$

$$\Phi_{12} = (0.3 \pm 2.6)^\circ$$



UT analysis including new physics

fit simultaneously for the CKM and the NP parameters (generalized UT fit)

- add most general loop NP to all sectors
- use all available experimental info
- find out NP contributions to $\Delta F=2$ transitions

B_d and B_s mixing amplitudes
(2+2 real parameters):

$$A_q = C_{B_q} e^{2i\phi_{B_q}} A_q^{SM} e^{2i\phi_q^{SM}} = \left(1 + \frac{A_q^{NP}}{A_q^{SM}} e^{2i(\phi_q^{NP} - \phi_q^{SM})} \right) A_q^{SM} e^{2i\phi_q^{SM}}$$

$$\Delta m_{q/K} = C_{B_q/\Delta m_K} (\Delta m_{q/K})^{SM}$$

$$A_{CP}^{B_d \rightarrow J/\psi K_s} = \sin 2(\beta + \Phi_{B_d})$$

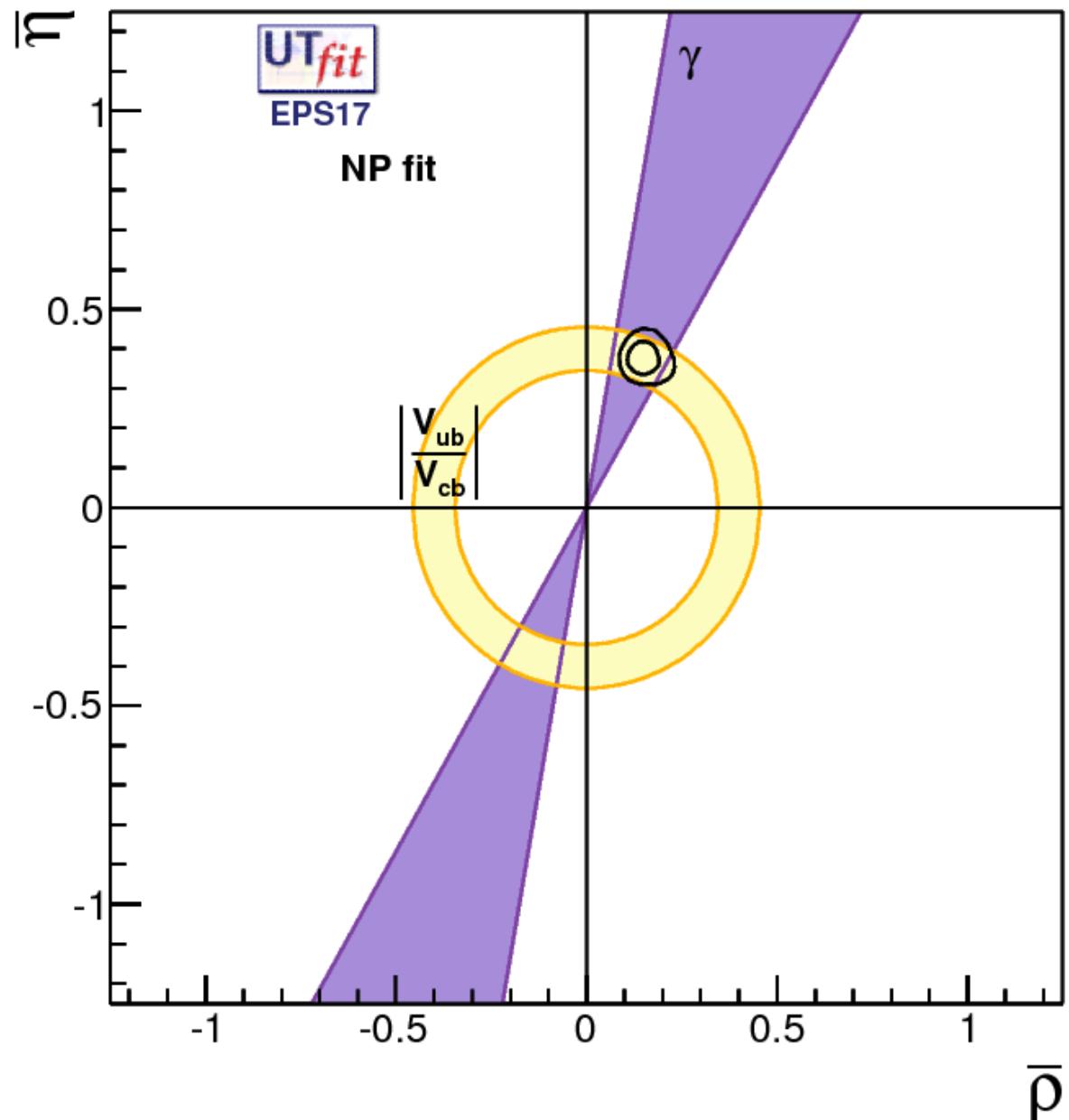
$$A_{SL}^q = \text{Im} \left(\Gamma_{12}^q / A_q \right)$$

$$\varepsilon_K = C_\varepsilon \varepsilon_K^{SM}$$

$$A_{CP}^{B_s \rightarrow J/\psi \phi} \sim \sin 2(-\beta_s + \Phi_{B_s})$$

$$\Delta \Gamma^q / \Delta m_q = \text{Re} \left(\Gamma_{12}^q / A_q \right)$$

NP analysis results



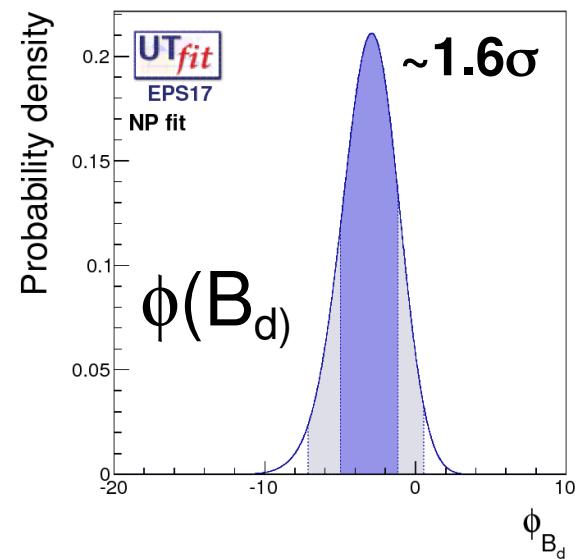
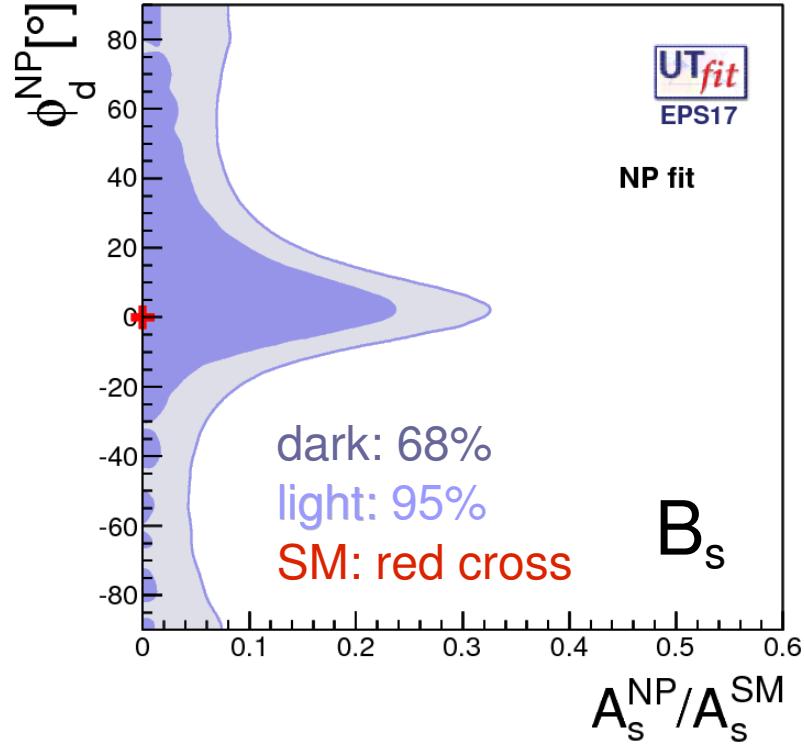
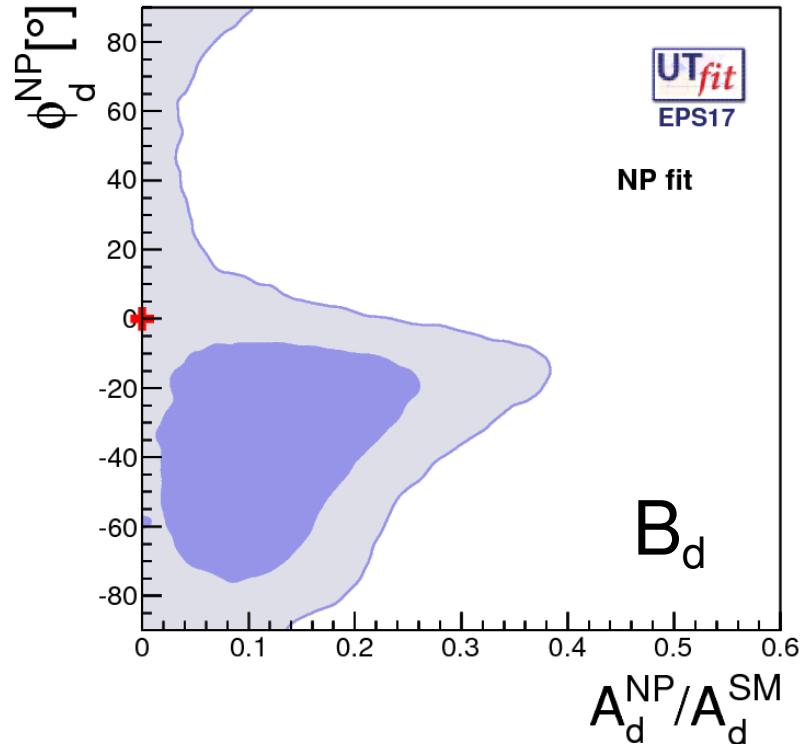
NP parameter results

$$A_q = C_{B_q} e^{2i\phi_{B_q}} A_q^{SM} e^{2i\phi_q^{SM}}$$

$C_{B_d} = 1.08 \pm 0.13$
 $\phi_{B_d} = (-3.0 \pm 1.9)^\circ$

$C_{B_s} = 1.12 \pm 0.10$
 $\phi_{B_s} = (0.4 \pm 0.9)^\circ$

$$A_q = \left(1 + \frac{A_q^{NP}}{A_q^{SM}} e^{2i(\phi_q^{NP} - \phi_q^{SM})} \right) A_q^{SM} e^{2i\phi_q^{SM}}$$



Ratio of NP/SM amplitudes is:
 $< 20\% @ 68\%$
 $(40\% @ 95\%)$
in B_d mixing
 $< 25\% @ 68\%$
 $(30\% @ 95\%)$
in B_s mixing

testing the new-physics scale



At the high scale

new physics enters according to its specific features

At the low scale

use OPE to write the most general effective Hamiltonian.
the operators have different chiralities than the SM
NP effects are in the Wilson Coefficients C

$$C_i(\Lambda) = \frac{F_i}{L_i} \frac{1}{\Lambda^2}$$

F_i: function of the NP flavour couplings

L_i: loop factor (in NP models with no tree-level FCNC)

Λ: NP scale (typical mass of new particles mediating ΔF=2 transitions)

$$\mathcal{H}_{\text{eff}}^{\Delta B=2} = \sum_{i=1}^5 C_i Q_i^{bq} + \sum_{i=1}^3 \tilde{C}_i \tilde{Q}_i^{bq}$$

$$Q_1^{q_i q_j} = \bar{q}_{jL}^\alpha \gamma_\mu q_{iL}^\alpha \bar{q}_{jL}^\beta \gamma^\mu q_{iL}^\beta ,$$

$$Q_2^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jR}^\beta q_{iL}^\beta ,$$

$$Q_3^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jR}^\beta q_{iL}^\alpha ,$$

$$Q_4^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jL}^\beta q_{iR}^\beta ,$$

$$Q_5^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jL}^\beta q_{iR}^\alpha .$$

M. Bona *et al.* (UTfit)
JHEP 0803:049,2008
arXiv:0707.0636

testing the TeV scale

The dependence of C on Λ changes depending on the flavour structure.

We can consider different flavour scenarios:

- **Generic:** $C(\Lambda) = \alpha/\Lambda^2$ $F_i \sim 1$, arbitrary phase
- **NMFV:** $C(\Lambda) = \alpha \times |F_{\text{SM}}|/\Lambda^2$ $F_i \sim |F_{\text{SM}}|$, arbitrary phase
- **MFV:** $C(\Lambda) = \alpha \times |F_{\text{SM}}|/\Lambda^2$ $F_1 \sim |F_{\text{SM}}|$, $F_{i \neq 1} \sim 0$, SM phase

$\alpha (L_i)$ is the coupling among NP and SM

- $\alpha \sim 1$ for strongly coupled NP
- $\alpha \sim \alpha_w (\alpha_s)$ in case of loop coupling through weak (strong) interactions

If no NP effect is seen
lower bound on NP scale Λ
if NP is seen
upper bound on NP scale Λ

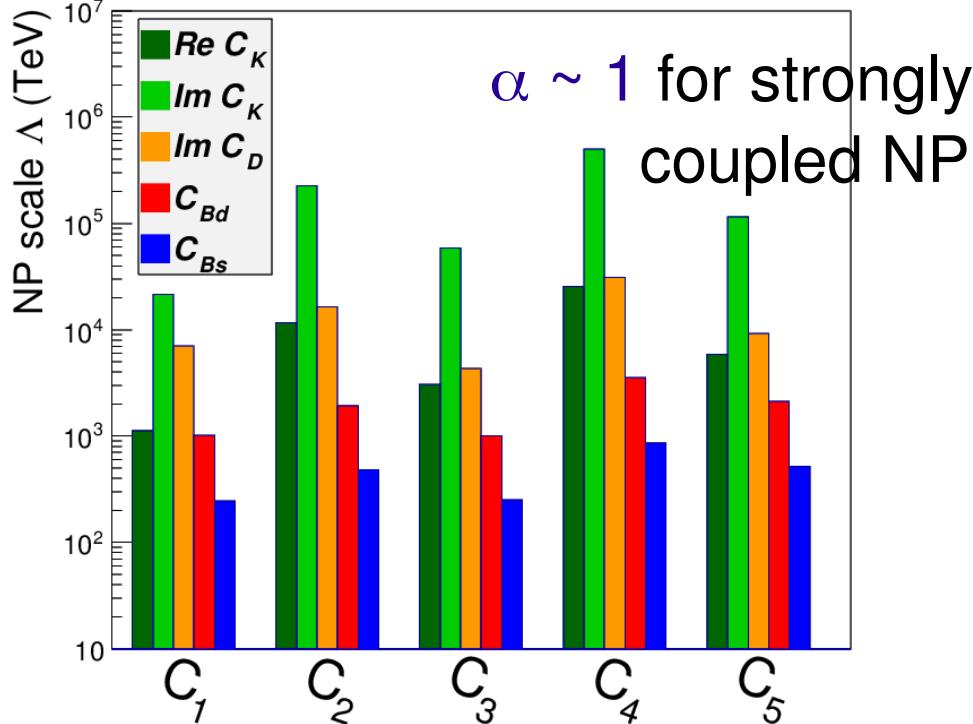
F is the flavour coupling and so

F_{SM} is the combination of CKM factors for the considered process

$$C_i(\Lambda) = F_i \frac{L_i}{\Lambda^2}$$

results from the Wilson coefficients

Generic: $C(\Lambda) = \alpha/\Lambda^2$,
 $F_i \sim 1$, arbitrary phase

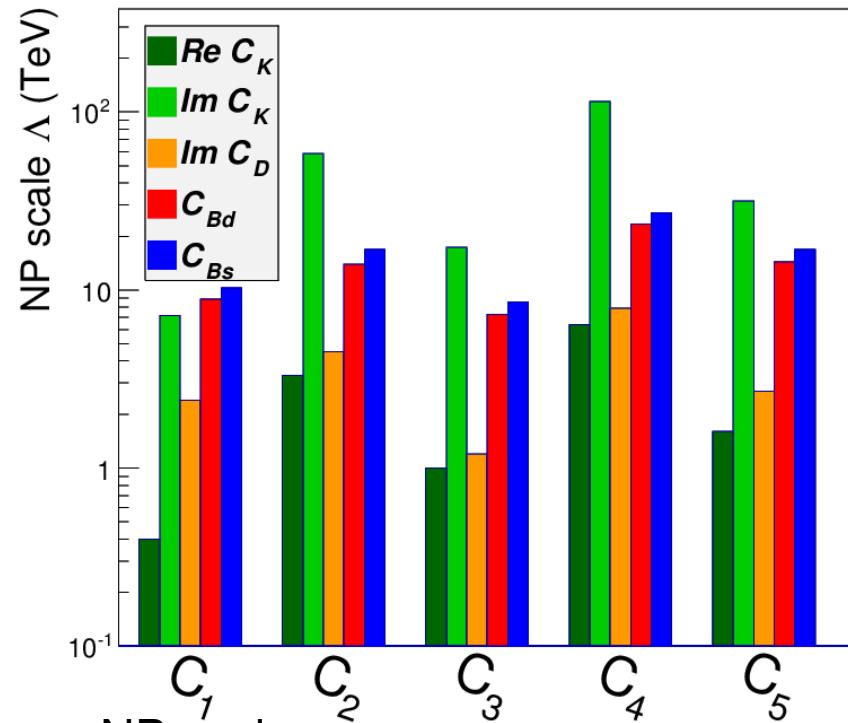


$\Lambda > 5.0 \cdot 10^5 \text{ TeV}$

$\alpha \sim \alpha_w$ in case of loop coupling
through **weak** interactions

$\Lambda > 1.5 \cdot 10^4 \text{ TeV}$

NMFV: $C(\Lambda) = \alpha \times |F_{SM}|/\Lambda^2$,
 $F_i \sim |F_{SM}|$, arbitrary phase



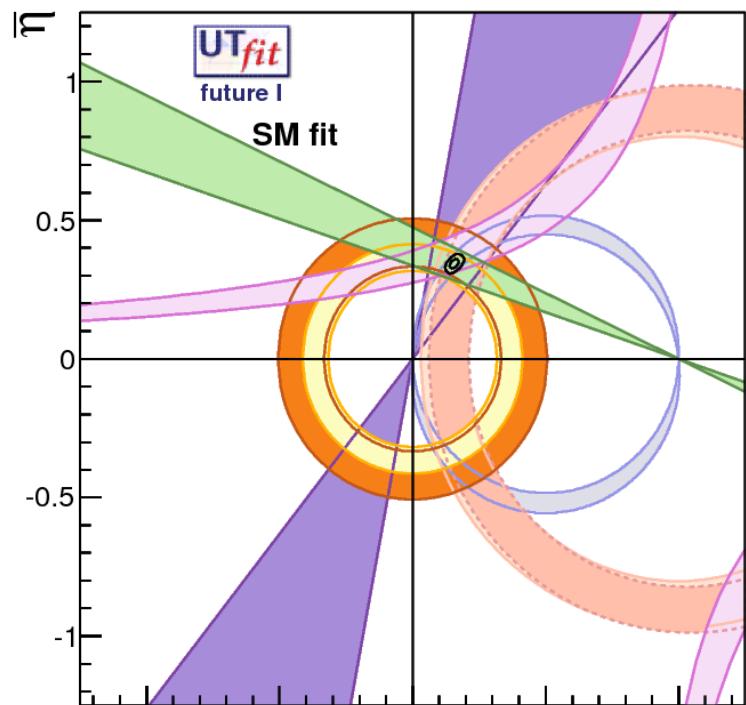
$\Lambda > 114 \text{ TeV}$

$\alpha \sim \alpha_w$ in case of loop coupling
through **weak** interactions

$\Lambda > 3.4 \text{ TeV}$

for lower bound for loop-mediated contributions,
simply multiply by α_s (~ 0.1) or by α_w (~ 0.03).

Look at the near future



$$\begin{aligned}\bar{\rho} &= \pm 0.015 \\ \bar{\eta} &= \pm 0.015\end{aligned}$$

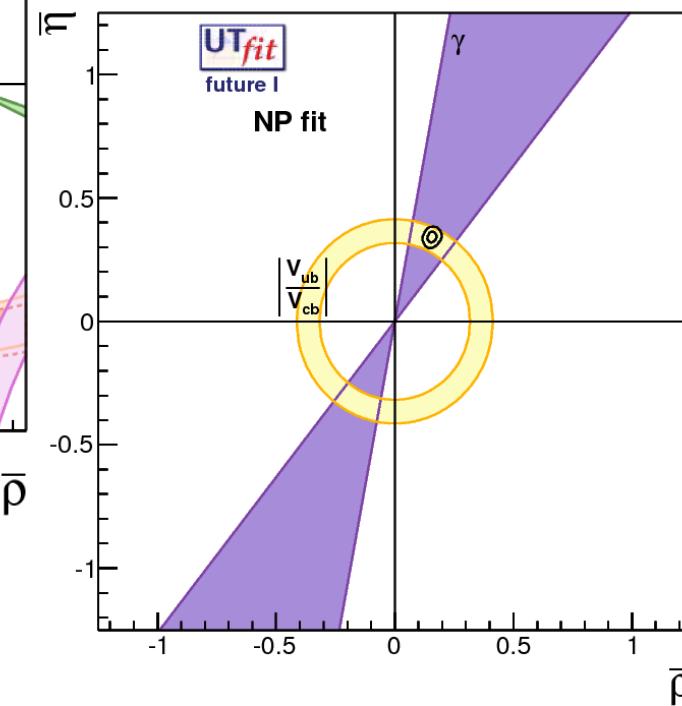
$$\begin{aligned}\bar{\rho} &= 0.154 \pm 0.015 \\ \bar{\eta} &= 0.346 \pm 0.013\end{aligned}$$

current sensitivity

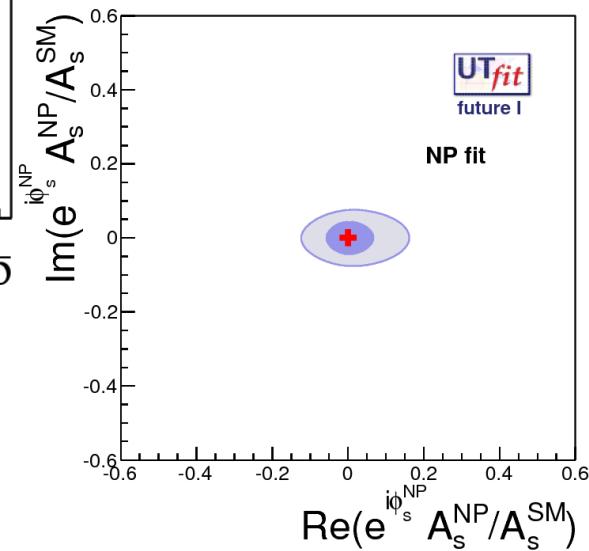
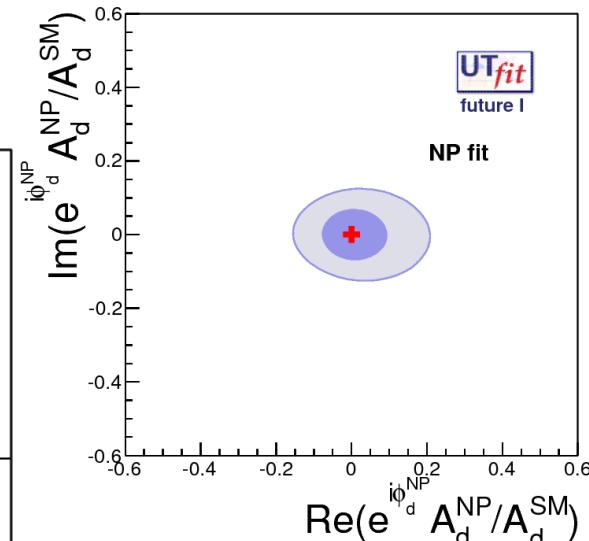
$$\begin{aligned}\bar{\rho} &= 0.150 \pm 0.027 \\ \bar{\eta} &= 0.363 \pm 0.025\end{aligned}$$

future I scenario:
errors from
Belle II at 5/ab
+ **LHCb at 10/fb**

preliminary



$$\begin{aligned}\bar{\rho} &= \pm 0.016 \\ \bar{\eta} &= \pm 0.019\end{aligned}$$



conclusions

- SM analysis displays very good overall consistency
- Still open discussion on semileptonic inclusive vs exclusive
- UTA provides determination of NP contributions to $\Delta F=2$ amplitudes. It currently leaves space for NP at the level of 25-40%
- So the scale analysis points to high scales for the generic scenario and at the limit of LHC reach for weak coupling. Indirect searches are complementary to direct searches.
- Even if we don't see relevant deviations in the down sector, the up sector is still very much open..

Back up slides



www.utfit.org

C. Alpigiani, A. Bevan, M.B., M. Ciuchini,
D. Derkach, E. Franco, V. Lubicz, G. Martinelli,
F. Parodi, M. Pierini, C. Schiavi, L. Silvestrini,
A. Stocchi, V. Sordini, C. Tarantino and V. Vagnoni

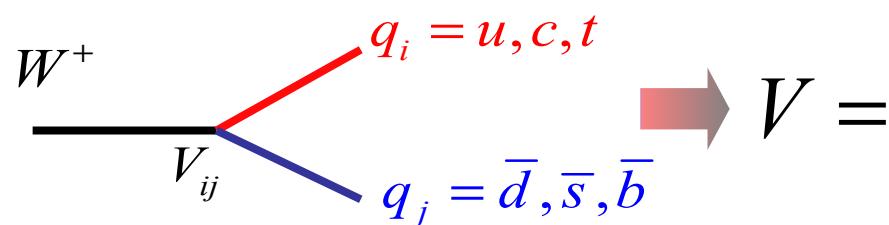
Other UT analyses exist, by:

CKMfitter (<http://ckmfitter.in2p3.fr/>),

Laiho&Lunghi&Van de Water (<http://latticeaverages.org/>)

Lunghi&Soni (1010.6069)

CKM matrix and its parameters



$$\text{Relative magnitudes} \quad \begin{matrix} d & s & b \\ u & \begin{pmatrix} \text{blue square} & \text{small blue square} & \cdot \\ \cdot & \text{blue square} & \cdot \\ \cdot & \cdot & \text{blue square} \end{pmatrix} & \\ c & \begin{pmatrix} \text{blue square} & \cdot & \cdot \\ \cdot & \text{blue square} & \cdot \\ \cdot & \cdot & \text{blue square} \end{pmatrix} & \\ t & \begin{pmatrix} \cdot & \cdot & \text{blue square} \end{pmatrix} & \end{matrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$\begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix}$$

where here we use
the Buras correction
to the Wolfenstein
parametrisation

$$\bar{\rho} + i\bar{\eta} \equiv -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}$$

$$\begin{aligned} \bar{\rho} &= \rho (1 - \lambda^2/2) \\ \bar{\eta} &= \eta (1 - \lambda^2/2) \end{aligned}$$

$$A = 0.831 \pm 0.013, \quad \lambda = 0.22510 \pm 0.00064$$

$\sin 2\alpha (\phi_2)$ from charmless B decays: $\pi\pi$, $\rho\rho$, $\pi\rho$

$\pi^0\pi^0$ from Belle at CKM14
to be updated soon (?)

$$\text{BR}(\pi^0\pi^0) = (1.17 \pm 0.13) 10^{-6}$$

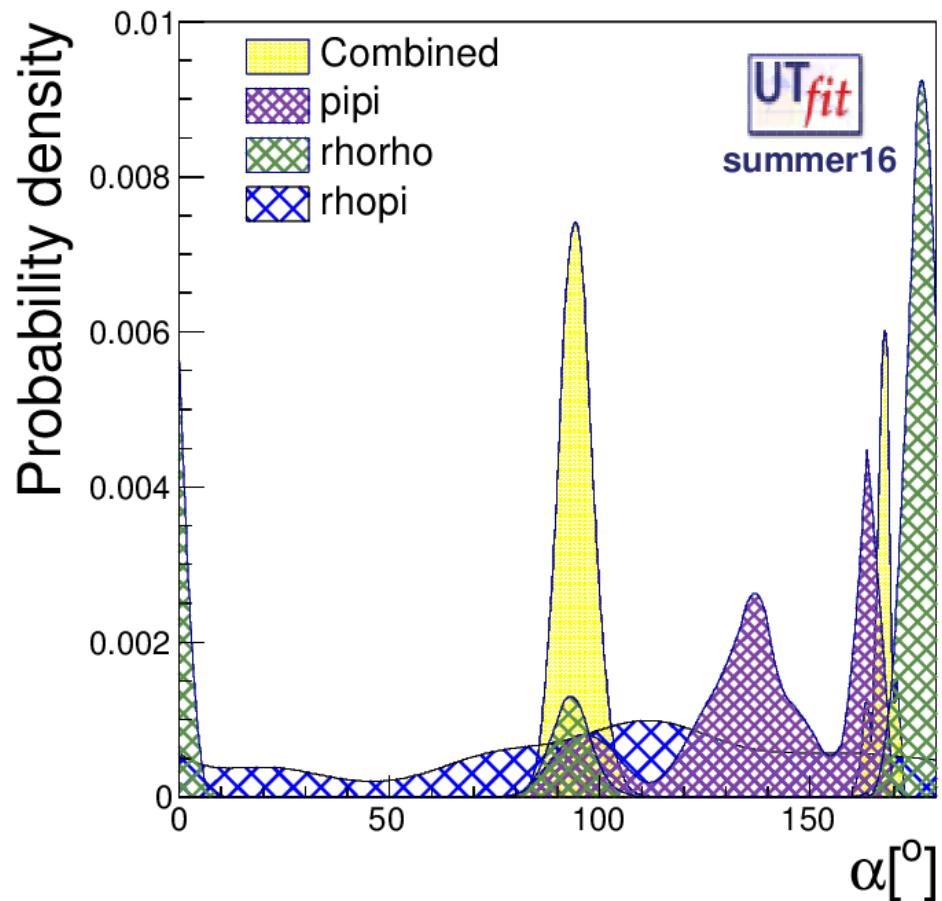
HFAG 2014

a *à la PDG* average would give
an inflated uncertainty of 0.41

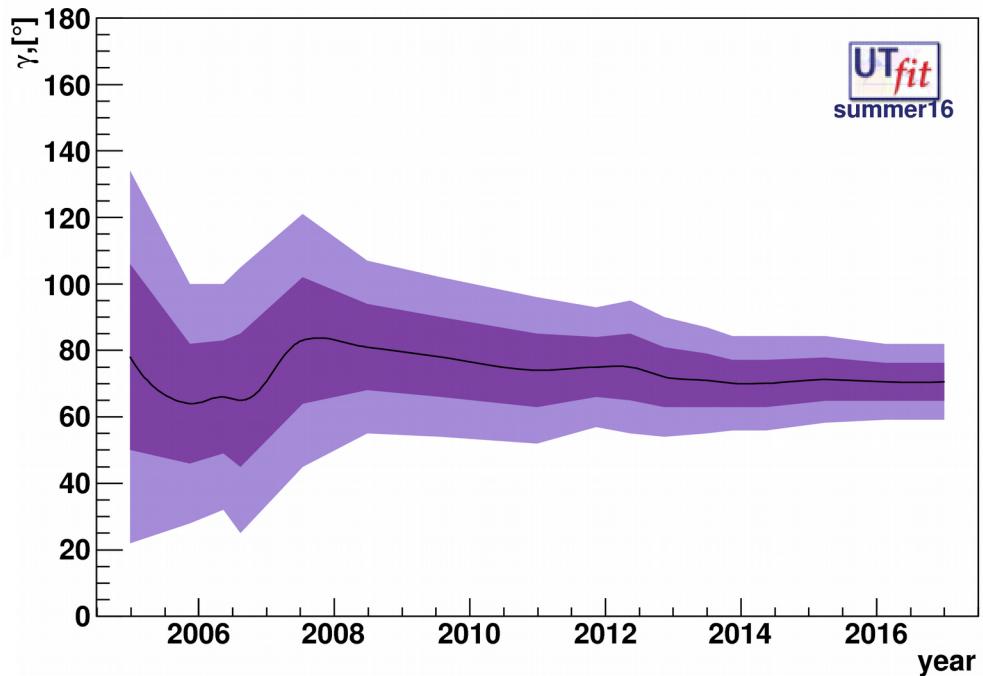
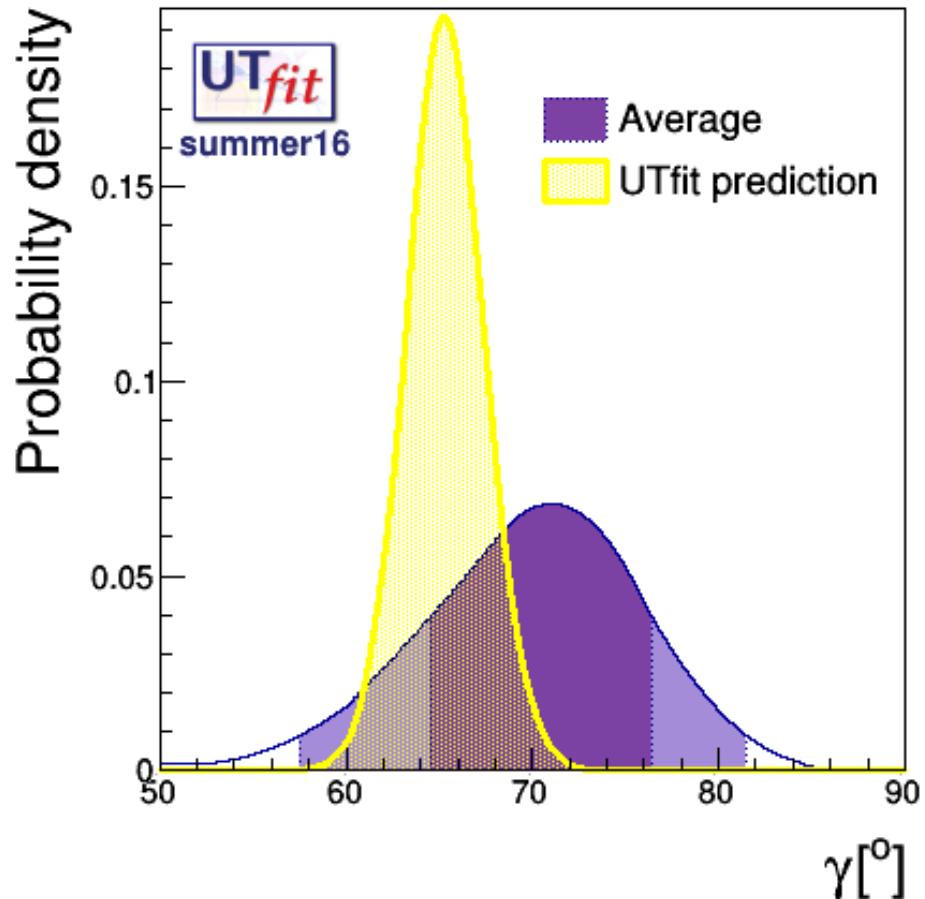
$\rho^+\rho^-$ average updated including
Belle arXiv:1510.01245

$\rho^0\rho^0$ average updated including
LHCb arXiv:1503.07770

α from $\pi\pi$, $\rho\rho$, $\pi\rho$ decays:
combined: $(94.2 \pm 4.5)^\circ$
UTfit prediction: $(90.6 \pm 2.5)^\circ$



γ and DK trees



After a decade of analyses and almost 50 papers published, the world average uncertainty has decreased by a factor 3

combined: $(70.5 \pm 5.7)^\circ$

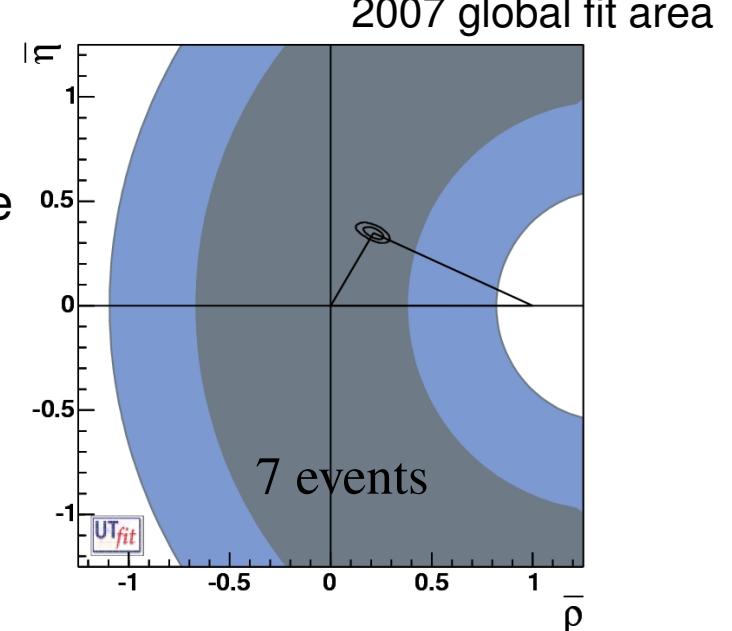
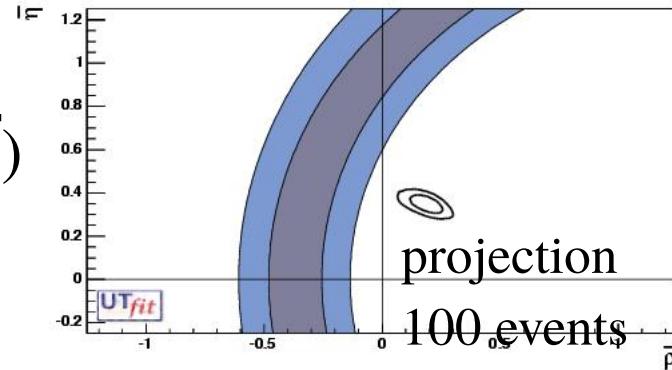
UTfit prediction: $(65.5 \pm 2.1)^\circ$

some old plots coming back to fashion:

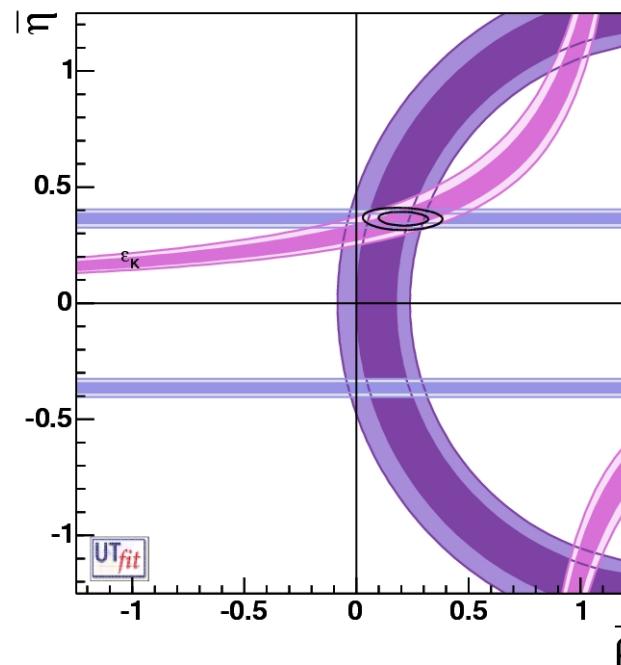
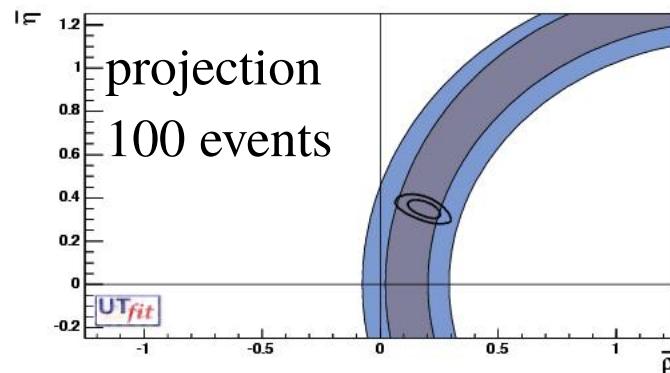
As NA62 and KOTO are approaching data taking:

$\text{BR}(K^+ \rightarrow \pi^+ \bar{\nu}\bar{\nu})$

E949 central value



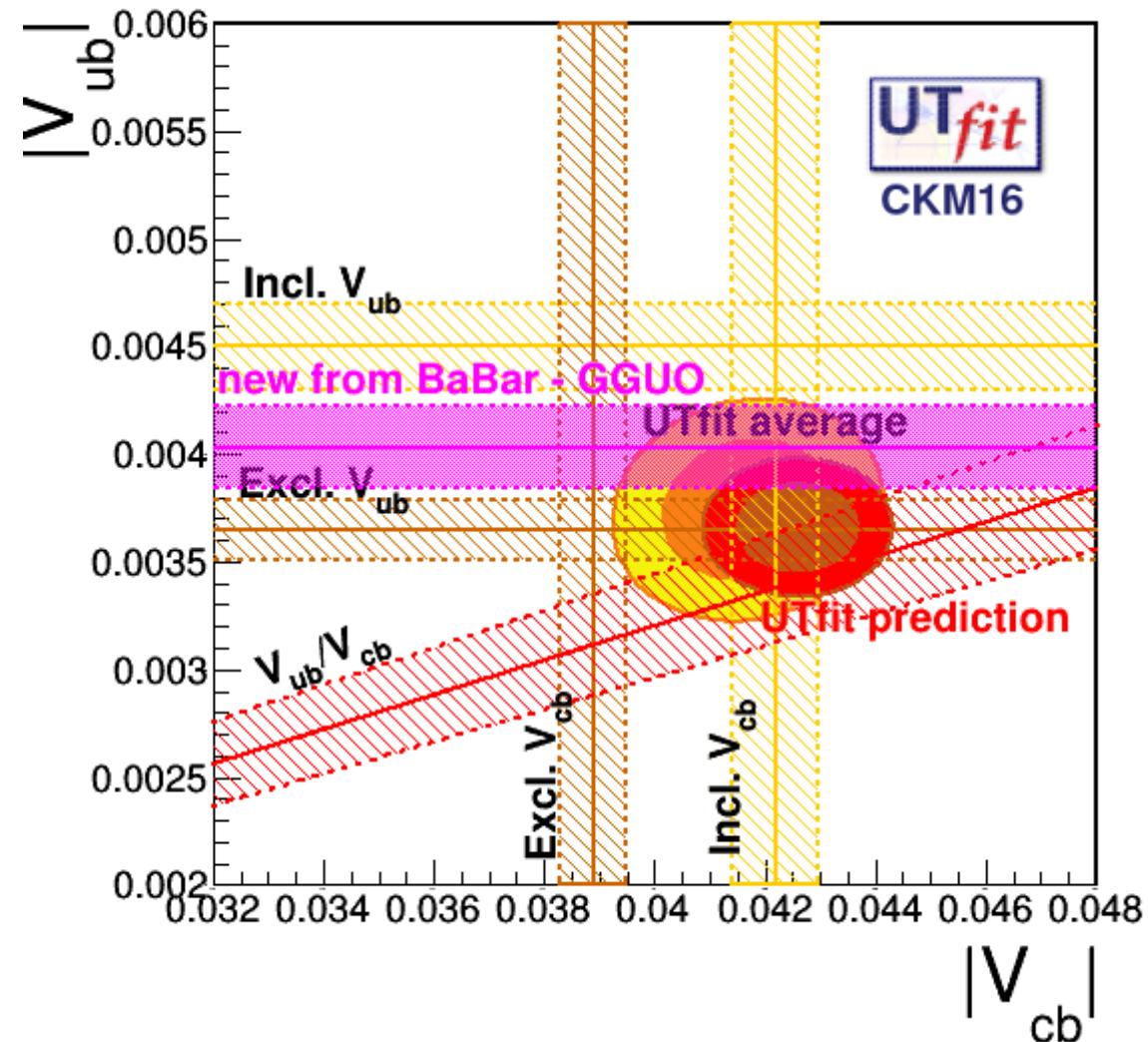
SM central value



including
 $\text{BR}(K^0 \rightarrow \pi^0 \bar{\nu}\bar{\nu})$
SM central value

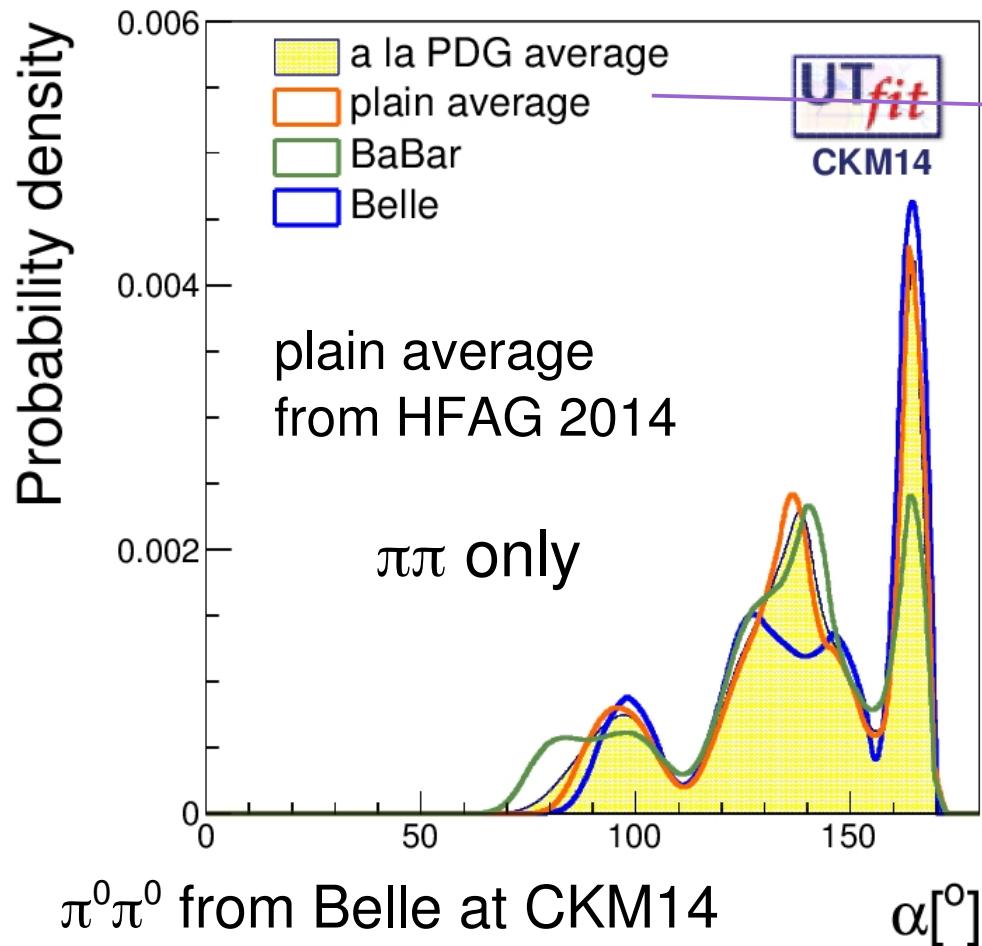
V_{cb} and V_{ub}

some new extra results @CKM16:
a lay(wo)man's visualisation..



new BaBar result
for inclusive V_{ub}
@Kowalewski
on Tue in WG2

$\sin 2\alpha (\phi_2)$ from charmless B decays: pp, ($\rho\rho$, $\pi\rho$)

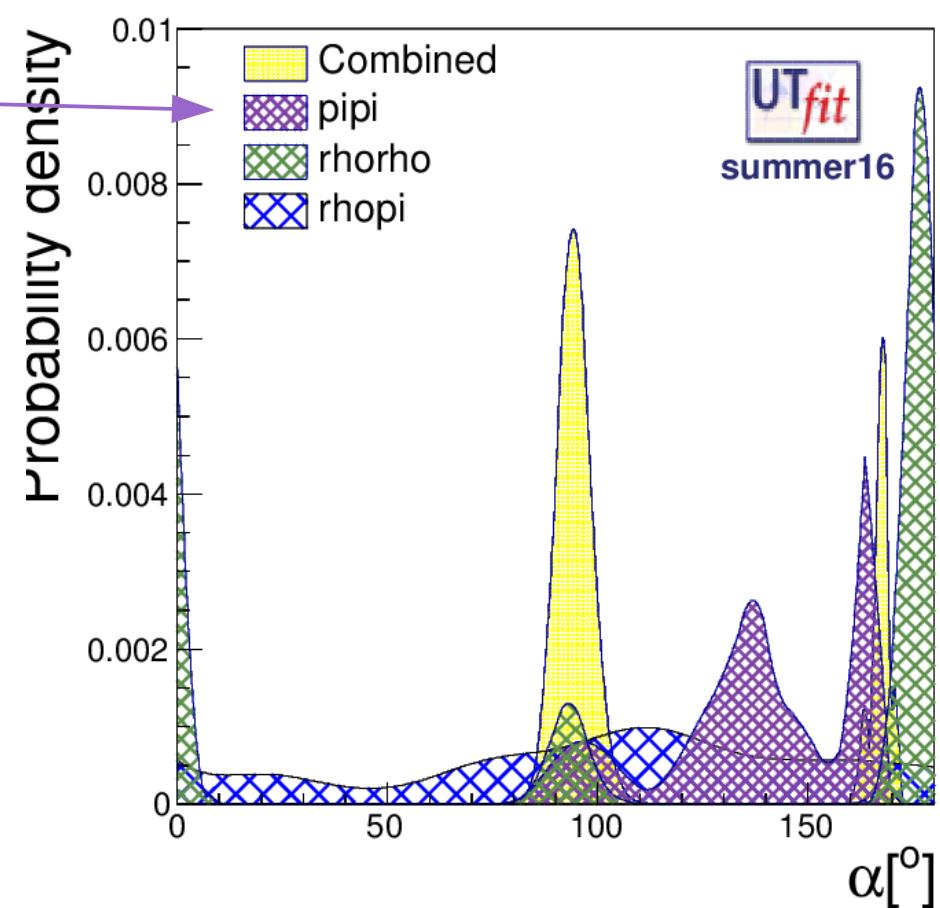


$\pi^0\pi^0$ from Belle at CKM14

to be updated soon (?)

$$\text{BR}(\pi^0\pi^0) = (1.17 \pm 0.13) 10^{-6}$$

compared with a *à la PDG* average
giving an inflated uncertainty of 0.41



α from $\pi\pi$, $\rho\rho$, $\pi\rho$ decays:
combined: $(94.2 \pm 4.5) {}^\circ$

Unitarity Triangle analysis in the SM:

summer 2016

obtained excluding
the given constraint
from the fit

Observables	Measurement	Prediction	Pull (# σ)
B_K	0.740 ± 0.029	0.81 ± 0.07	< 1
f_{Bs}	0.226 ± 0.005	0.220 ± 0.007	< 1
f_{Bs}/f_{Bd}	1.203 ± 0.013	1.210 ± 0.030	< 1
B_{Bs}/B_{Bd}	1.032 ± 0.036	1.07 ± 0.05	< 1
B_{Bs}	1.35 ± 0.08	1.30 ± 0.07	< 1

in general: average the $N_f=2+1+1$ and $N_f=2+1$ FLAG averages,
through eq.(28) in arXiv:1403.4504

for B_K , f_{Bs} , f_{Bs}/f_{Bd} :

FLAG $N_f=2+1+1$ (single result) and $N_f=2+1$ average

for B_{Bs} , B_{Bs}/B_{Bd} :

update w.r.t. the $N_f=2+1$ FLAG average (no $N_f=2+1+1$ results yet)
updating the FNAL/MILC result to FNAL/MILC 2016 (1602.03560)

new-physics-specific constraints

$$A_{\text{SL}}^s \equiv \frac{\Gamma(\bar{B}_s \rightarrow \ell^+ X) - \Gamma(B_s \rightarrow \ell^- X)}{\Gamma(\bar{B}_s \rightarrow \ell^+ X) + \Gamma(B_s \rightarrow \ell^- X)} = \text{Im} \left(\frac{\Gamma_{12}^s}{A_s^{\text{full}}} \right)$$

semileptonic asymmetries in B^0 and B_s : sensitive to NP effects in both size and phase. Currently using a 2D average done by LHCb in 1605.09768 (pre-ICHEP16 value).

BaBar, Belle,
D0 + LHCb

same-side dilepton charge asymmetry:

D0 arXiv:1106.6308

admixture of B_s and B_d so sensitive to NP effects in both.

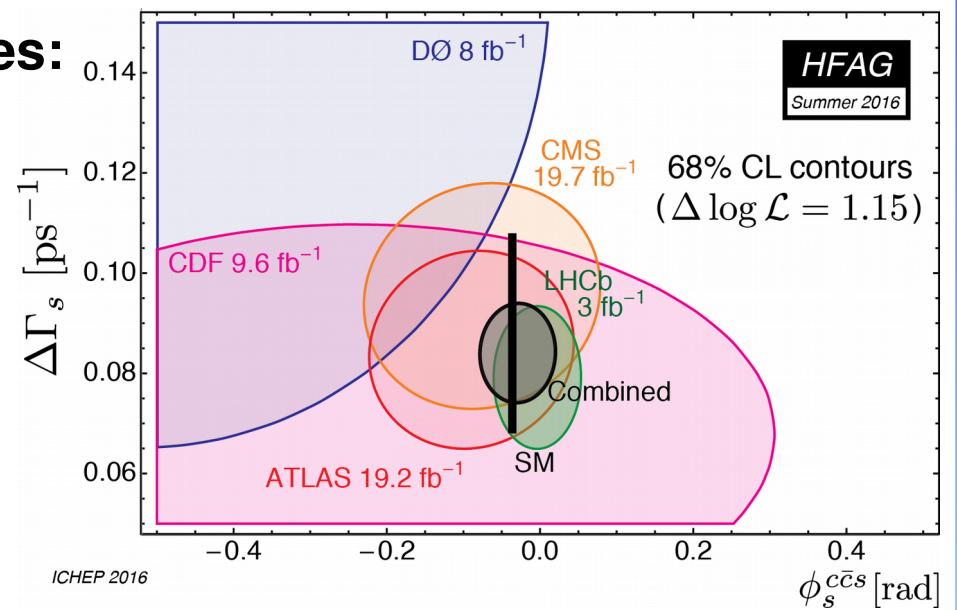
$$A_{\text{SL}}^{\mu\mu} \times 10^3 = -7.9 \pm 2.0$$

$$A_{\text{SL}}^{\mu\mu} = \frac{f_d \chi_{d0} A_{\text{SL}}^d + f_s \chi_{s0} A_{\text{SL}}^s}{f_d \chi_{d0} + f_s \chi_{s0}}$$

lifetime τ^{FS} in flavour-specific final states: average lifetime is a function to the width and the width difference

$$\tau^{\text{FS}}(B_s) = 1.511 \pm 0.014 \text{ ps}$$

HFAG
Summer 2016



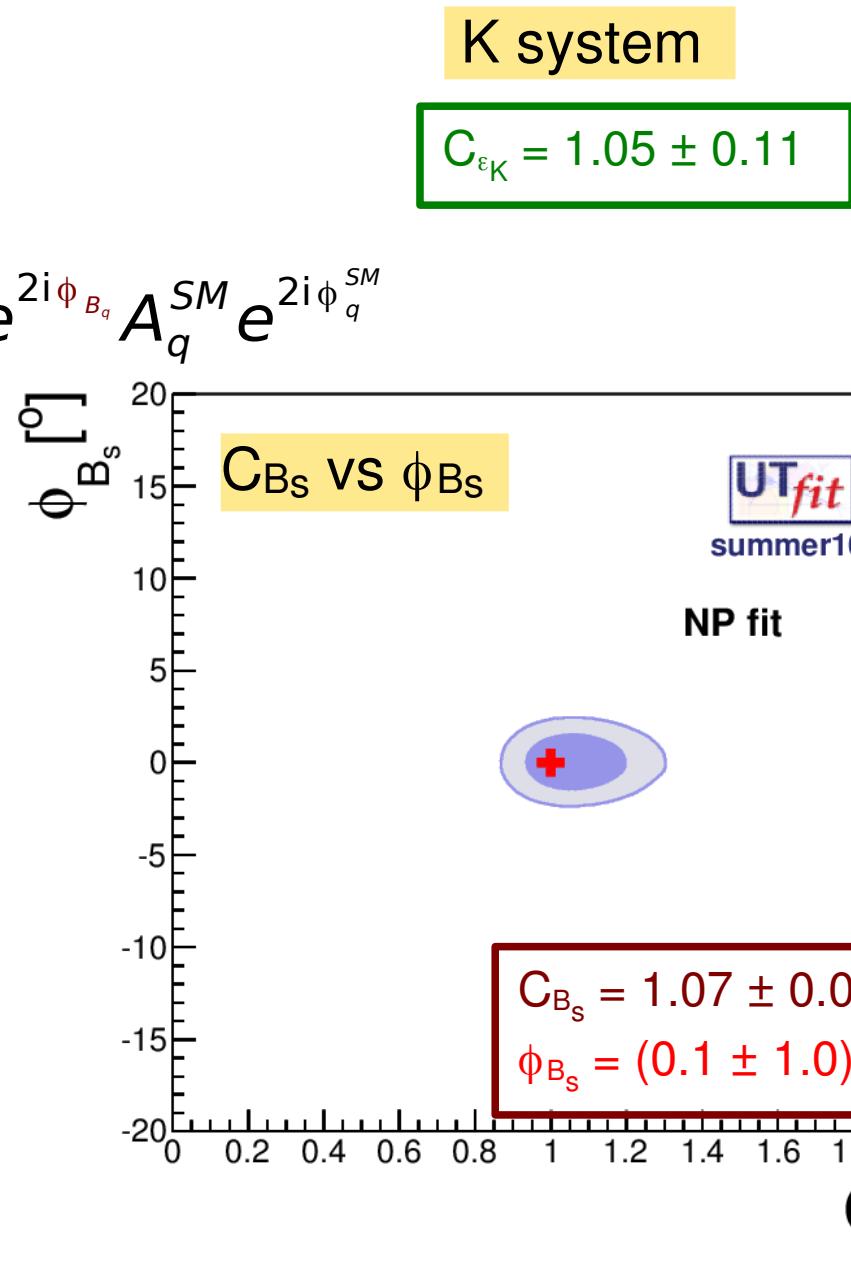
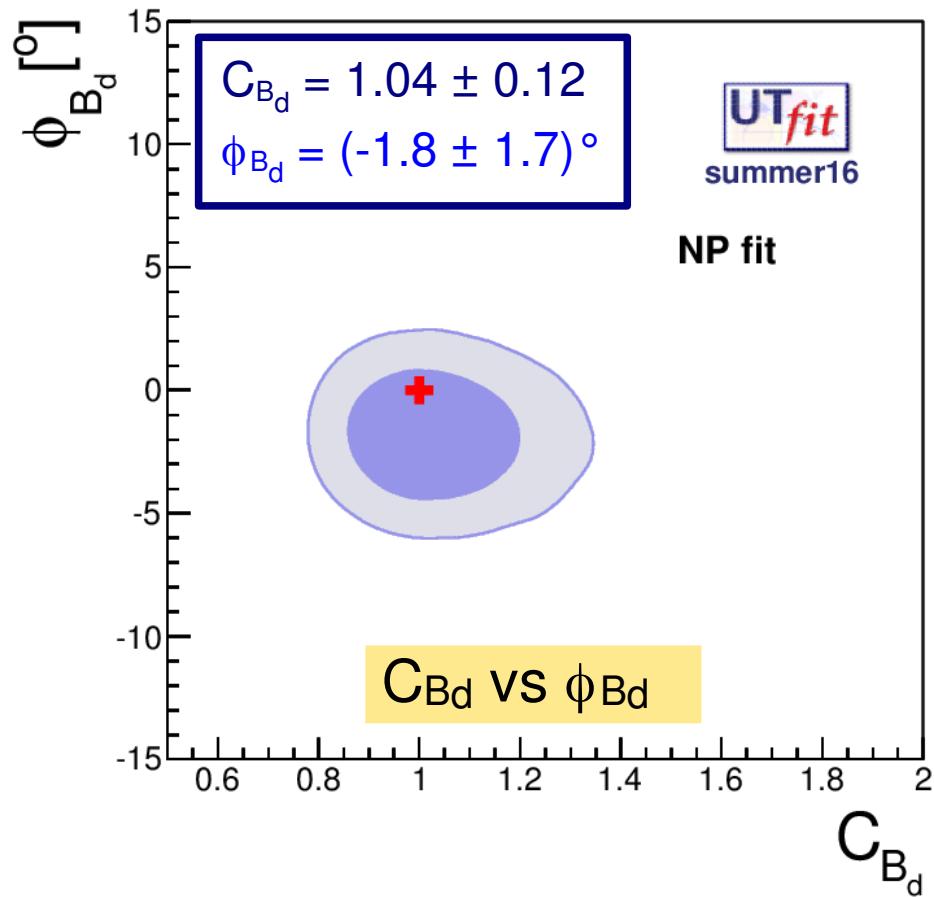
$\phi_s = 2\beta_s$ vs $\Delta\Gamma_s$ from $B_s \rightarrow J/\psi \phi$
angular analysis as a function of proper time and b-tagging

NP parameter results

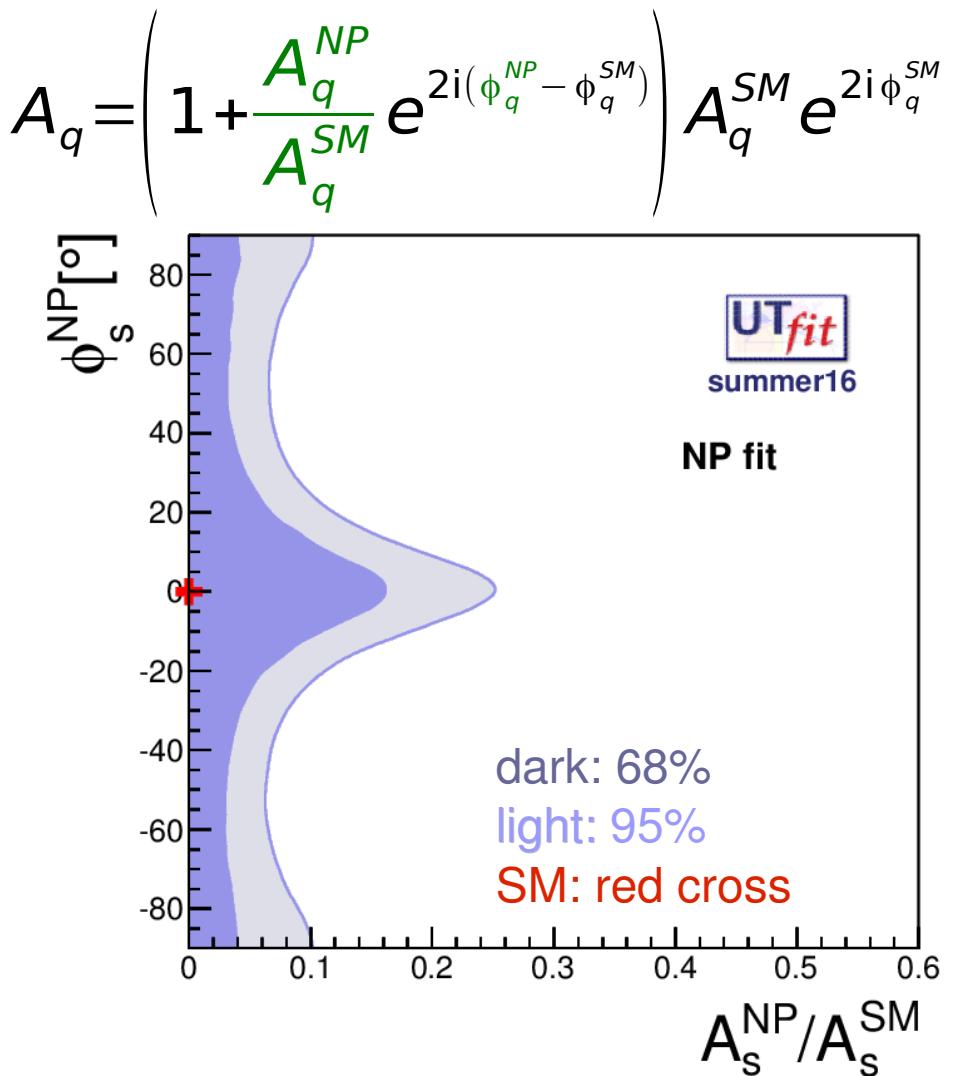
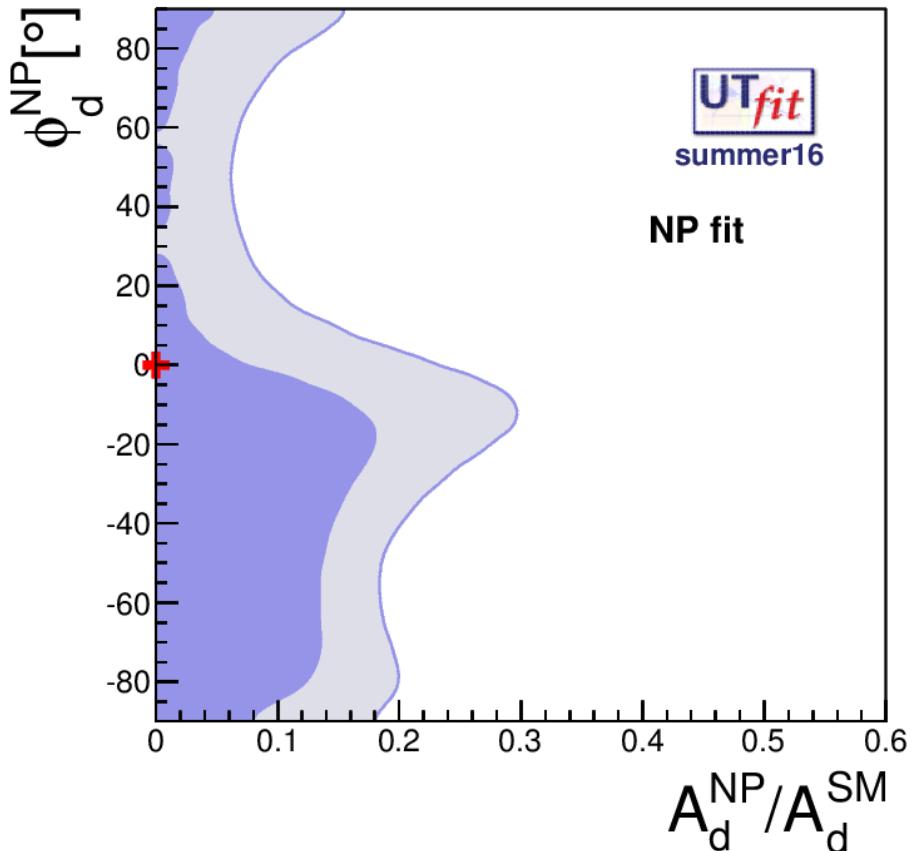
dark: 68%

light: 95%

SM: red cross



NP parameter results



The ratio of NP/SM amplitudes is:

- < 15% @68% prob. (30% @95%) in B_d mixing
- < 15% @68% prob. (25% @95%) in B_s mixing

see also Lunghi & Soni, Buras et al., Ligeti et al.

testing the new-physics scale



At the high scale

new physics enters according to its specific features

At the low scale

use OPE to write the most general effective Hamiltonian.

the operators have different chiralities than the SM

NP effects are in the Wilson Coefficients C

NP effects are enhanced

- up to a factor 10 by the values of the matrix elements especially for transitions among quarks of different chiralities
- up to a factor 8 by RGE

$$\mathcal{H}_{\text{eff}}^{\Delta B=2} = \sum_{i=1}^5 C_i Q_i^{bq} + \sum_{i=1}^3 \tilde{C}_i \tilde{Q}_i^{bq}$$

$$Q_1^{q_i q_j} = \bar{q}_{jL}^\alpha \gamma_\mu q_{iL}^\alpha \bar{q}_{jL}^\beta \gamma^\mu q_{iL}^\beta ,$$

$$Q_2^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jR}^\beta q_{iL}^\beta ,$$

$$Q_3^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jR}^\beta q_{iL}^\alpha ,$$

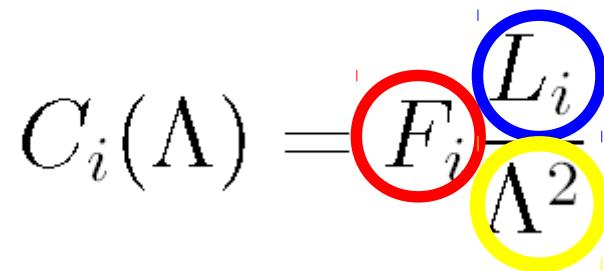
$$Q_4^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\alpha \bar{q}_{jL}^\beta q_{iR}^\beta ,$$

$$Q_5^{q_i q_j} = \bar{q}_{jR}^\alpha q_{iL}^\beta \bar{q}_{jL}^\beta q_{iR}^\alpha .$$

M. Bona et al. (UTfit)
JHEP 0803:049,2008
arXiv:0707.0636

effective BSM Hamiltonian for $\Delta F=2$ transitions

The Wilson coefficients C_i have in general the form

$$C_i(\Lambda) = \frac{F_i}{\Lambda^2} L_i$$


Putting bounds on the Wilson coefficients give insights into the NP scale in different NP scenarios that enter through F_i and L_i

F_i : function of the NP flavour couplings

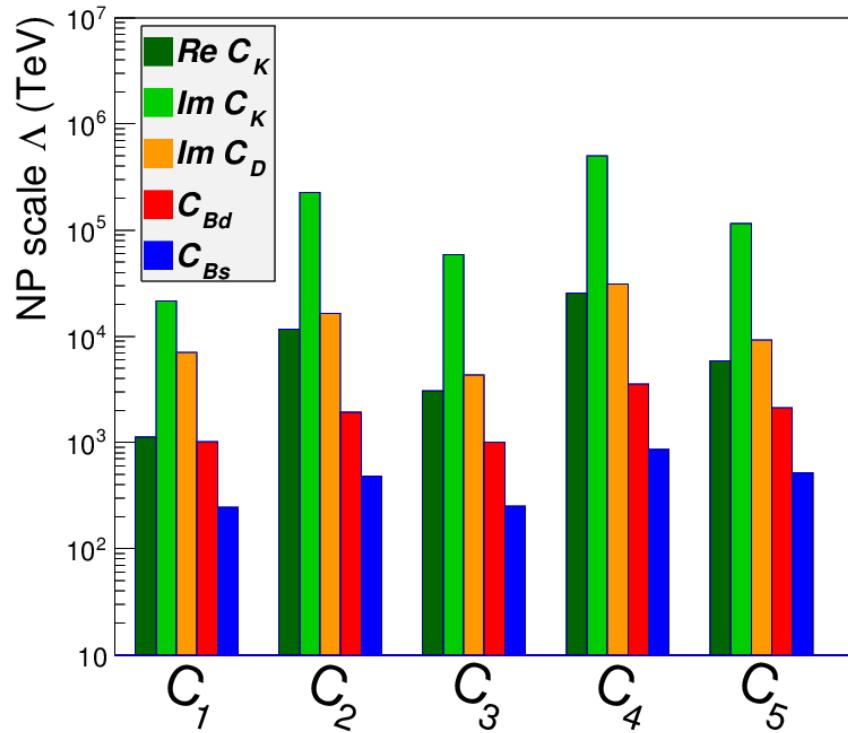
L_i : loop factor (in NP models with no tree-level FCNC)

Λ : NP scale (typical mass of new particles mediating $\Delta F=2$ transitions)

results from the Wilson coefficients

Generic: $C(\Lambda) = \alpha/\Lambda^2$, $F_i \sim 1$, arbitrary phase

$\alpha \sim 1$ for strongly coupled NP



Lower bounds on NP scale
(in TeV at 95% prob.)

Non-perturbative NP
 $\Lambda > 5.0 \times 10^5$ TeV

To obtain the lower bound for loop-mediated contributions, one simply multiplies the bounds by $\alpha_s (\sim 0.1)$ or by $\alpha_w (\sim 0.03)$.

$\alpha \sim \alpha_w$ in case of loop coupling through weak interactions

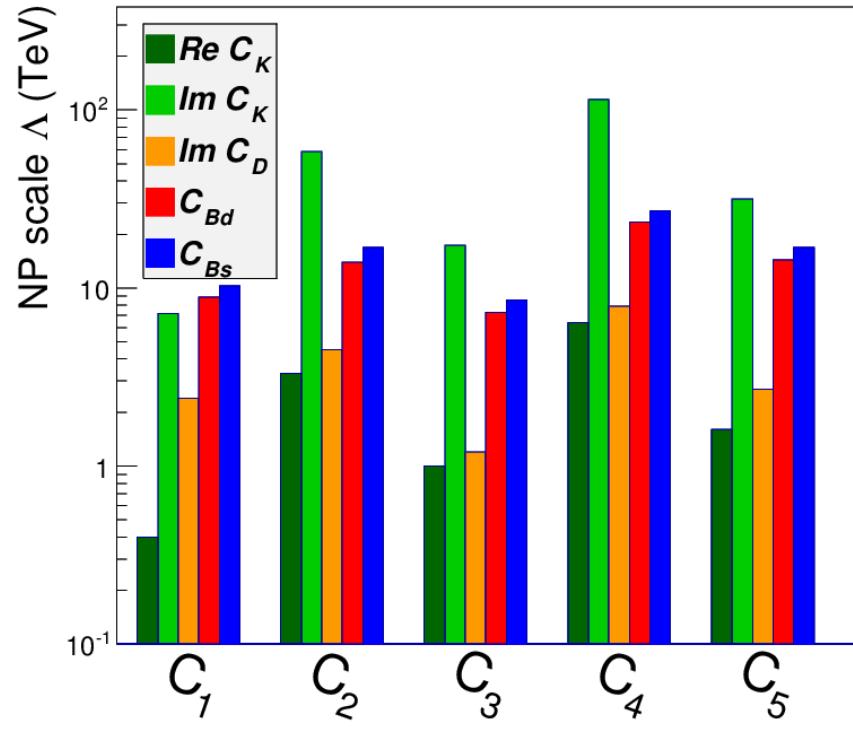
NP in α_w loops
 $\Lambda > 1.5 \times 10^4$ TeV

Best bound from ε_K
dominated by CKM error
CPV in charm mixing follows,
exp error dominant
Best CP conserving from Δm_K ,
dominated by long distance
 B_d and B_s behind,
errors from both CKM
and B-parameters

results from the Wilson coefficients

NMFV: $C(\Lambda) = \alpha \times |F_{\text{SM}}|/\Lambda^2$, $F_i \sim |F_{\text{SM}}|$, arbitrary phase

$\alpha \sim 1$ for strongly coupled NP



Lower bounds on NP scale
(in TeV at 95% prob.)

Non-perturbative NP
 $\Lambda > 114$ TeV

To obtain the lower bound for loop-mediated contributions, one simply multiplies the bounds by $\alpha_s (\sim 0.1)$ or by $\alpha_w (\sim 0.03)$.

$\alpha \sim \alpha_w$ in case of loop coupling through weak interactions

NP in α_w loops
 $\Lambda > 3.4$ TeV

If new chiral structures present,
 ϵ_K still leading
 $B_{(s)}$ mixing provides very stringent
constraints, especially if no new
chiral structures are present
Constraining power of the various
sectors depends on unknown
NP flavour structure.