

Recent results on (semi)leptonic B decays from Belle

Saskia Falke

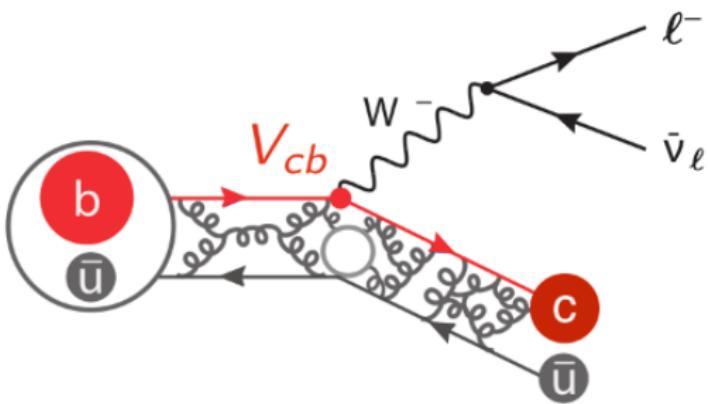
saskia.falke@lapp.in2p3.fr

On behalf of the Belle collaboration

EPS-HEP in Venise, July 6th, 2017

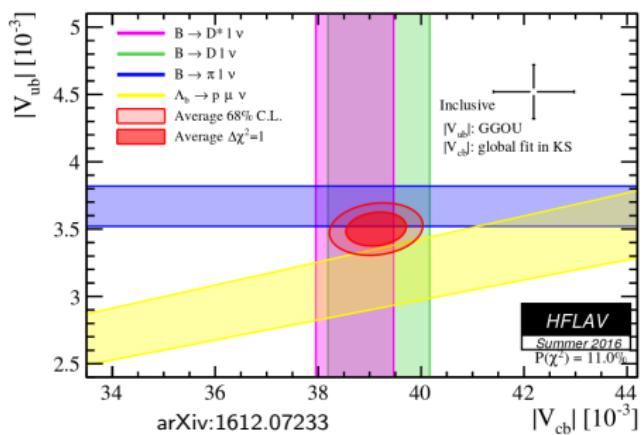


- Decays with leptons precisely predicted in the Standard Model
- They have high branching fractions
- Leptonic and hadronic currents factorise

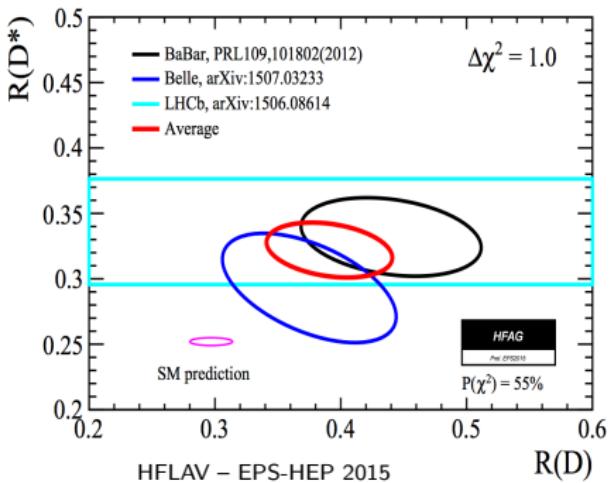


Introduction

- Several tensions seen in B physics that can be tested using (semi)leptonic decays



$$\mathcal{R}(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$$



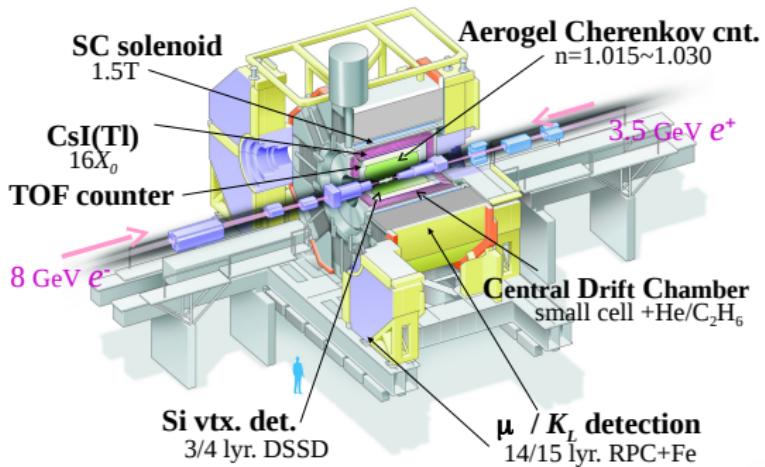
Tension: inclusive and exclusive

World average at 4σ from SM

Outline

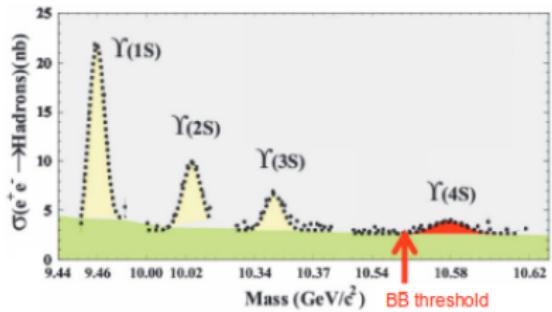
- ① Measurement of $|V_{cb}|$ and form factors from $B \rightarrow D^* \ell \nu$
- ② Recent measurement of $\mathcal{R}(D^{(*)})$
- ③ Measurement $B \rightarrow \eta(') \ell \nu$
- ④ Search for purely leptonic $B \rightarrow \mu \nu$ decays

Belle Detector



- 1999 to 2010 in Tsukuba, Japan
- At KEKB: asymmetric e^+e^- collider

- $\sqrt{s} = 10.58 \text{ GeV} = m(\Upsilon(4S))$
- $\mathcal{B}(\Upsilon(4S) \rightarrow B\bar{B}) \sim 100\%$
- Int. luminosity on $\Upsilon(4S)$: 711 fb^{-1}
- 772 Mio. $B\bar{B}$ pairs



Results from $B \rightarrow D^{(*)}\ell\nu$ decays



- Semileptonic $B \rightarrow D^{(*)}\ell\nu$ ($\ell = e, \mu$) allow for measurement of $|V_{cb}|$
- Measure hadronic form factor parameters
- Decays with τ leptons are sensitive to New Physics coupling 3rd generation
- Test lepton flavour universality

Systematics on $|V_{cb}|$, efficiencies, form factors, etc. cancel

$$\mathcal{R}(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)}$$

SM prediction

$$\mathcal{R}(D^*) = 0.252 \pm 0.003$$

$$\mathcal{R}(D) = 0.300 \pm 0.008$$

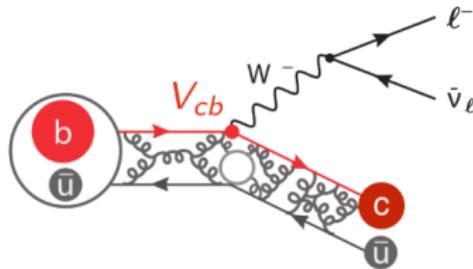
Heechang Na et al.

Svetlana Fajfer et al.

Jernej F. Kamenik, Federico Mescia
Fermilab Lattice, MILC Collaborations

Form factor parameters measured from $B \rightarrow D^{(*)}\ell\nu$ decays used as input for prediction

Precise determination of the CKM matrix element $|V_{cb}|$ with $\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}_\ell$ decays with hadronic tagging at Belle

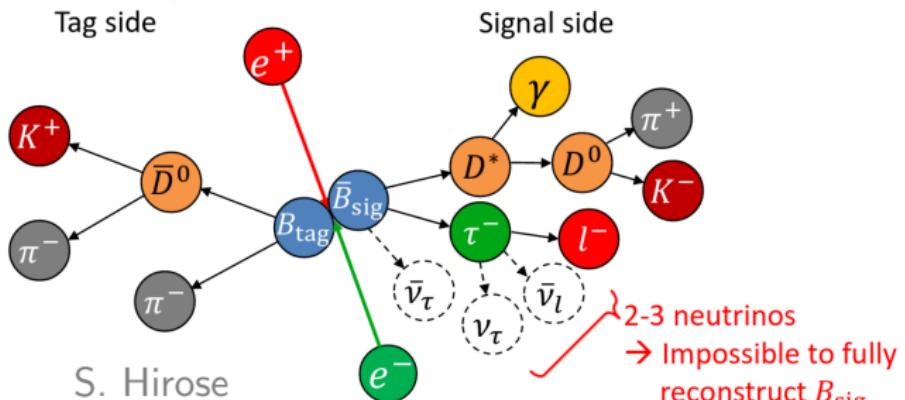


BELLE-CONF-1612
arXiv:1702.01521 [hep-ex] 14 Feb 2017

Hadronic B meson tagging

Analysis performed with hadronic tagging (fully reconstructed B_{tag}):

- reduce non- B background
- know kinematics of signal B



B_{tag} reconstructed in
1104 different
hadronic decay modes

Efficiency: $\sim 10^{-3}$

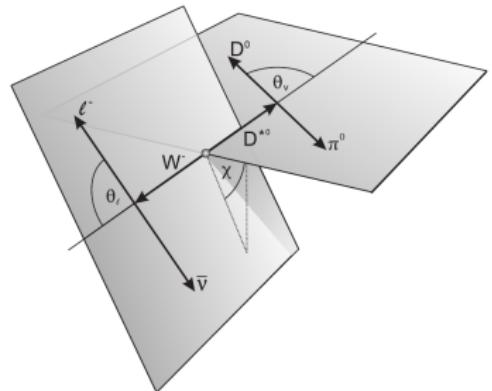
- Performed using neural network
- Efficiency correction in MC using reference channel

Goal of the analysis

$$\frac{d^4\Gamma(B \rightarrow D^*\ell\nu)}{dw d\cos\theta_\nu d\cos\theta_\ell d\chi} = f(|V_{cb}|^2, \underbrace{\rho_{D^*}^2, R_1, R_2}_{\text{form factor parameters}})$$

Kinematic variables:

- $w = \frac{m_B^2 - m_{D^*}^2 - \cancel{q}^2}{m_B m_{D^*}}$
- $\cos\theta_\nu, \cos\theta_\ell, \chi$: decay angles

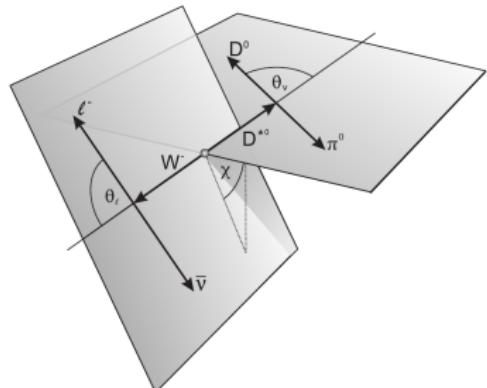


Goal of the analysis

$$\frac{d^4\Gamma(B \rightarrow D^*\ell\nu)}{dw \, d\cos\theta_\nu \, d\cos\theta_\ell \, d\chi} = f(|V_{cb}|^2, \underbrace{\rho_{D^*}^2, R_1, R_2}_{\text{form factor parameters}})$$

Kinematic variables:

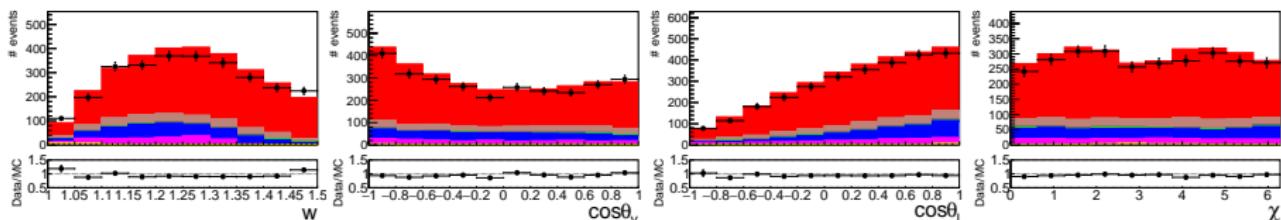
- $w = \frac{m_B^2 - m_{D^*}^2 - q^2}{m_B m_{D^*}}$
- $\cos\theta_\nu, \cos\theta_\ell, \chi$: decay angles



Reconstruction of kinematic distributions

- Signal B reconstructed in $B \rightarrow D^*\ell\nu$
- Use 1-dimensional projections of differential decay rates

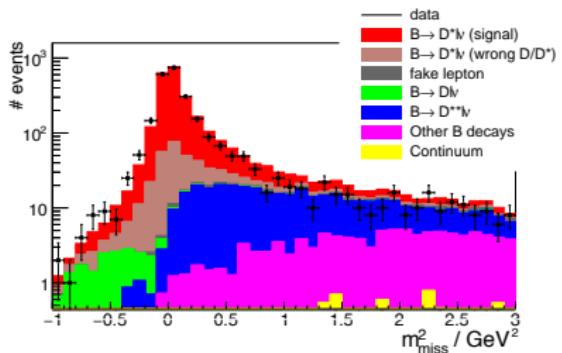
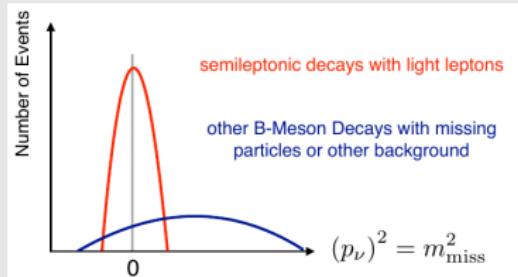
	data
red	$B \rightarrow D^*\ell\nu$ (signal)
brown	$B \rightarrow D^*\ell\nu$ (wrong D/D*)
grey	fake lepton
green	$B \rightarrow D^*\nu$
blue	$B \rightarrow D^+\ell\nu$
magenta	Other B decays
yellow	Continuum



Signal extraction

- Single non-reconstructed particle in event: neutrino from signal decay

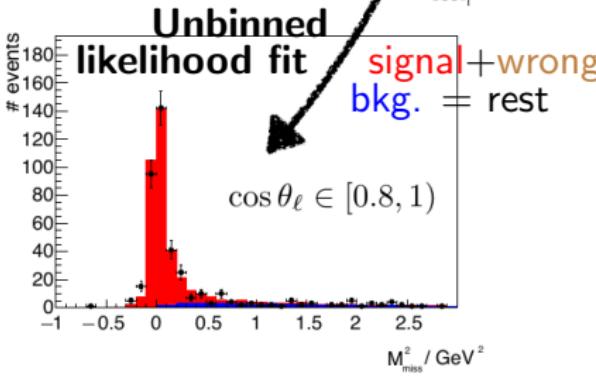
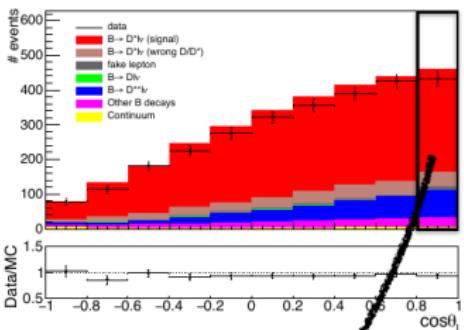
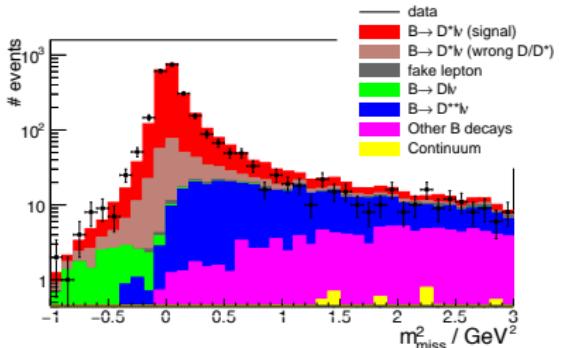
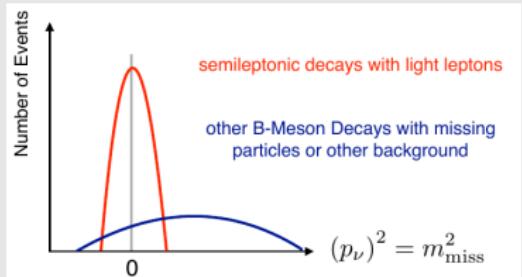
$$m_{miss}^2 = (p_{\Upsilon(4S)} - p_{tag} - p_{D^*} - p_\ell)^2$$



Signal extraction

- Single non-reconstructed particle in event: neutrino from signal decay

$$m_{miss}^2 = (p_{\gamma(4S)} - p_{tag} - p_{D^*} - p_\ell)^2$$



Results of $|V_{cb}|^2$ and FF parameter fit

Parameter	Measurement	World average
$ V_{cb} \cdot 10^3$	37.4 ± 1.2	39.2 ± 0.7
$\rho_{D^*}^2$	1.04 ± 0.13	1.20 ± 0.03
R_1	1.38 ± 0.07	1.40 ± 0.03
R_2	0.86 ± 0.10	0.85 ± 0.02

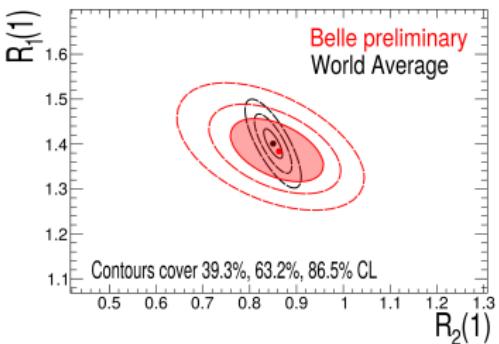
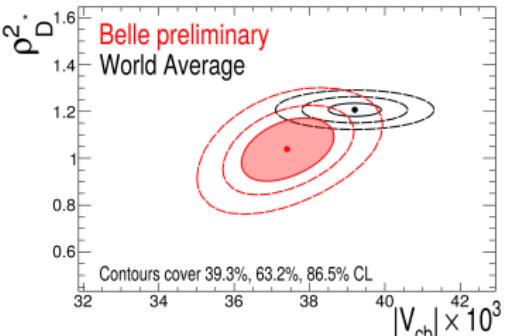
CLN parametrisation

- Measured values can be used to calculate SM prediction of $\mathcal{R}(D^*)$
- Use additional FF R_0 from sum rules [arXiv:1203.2653]

Prediction:

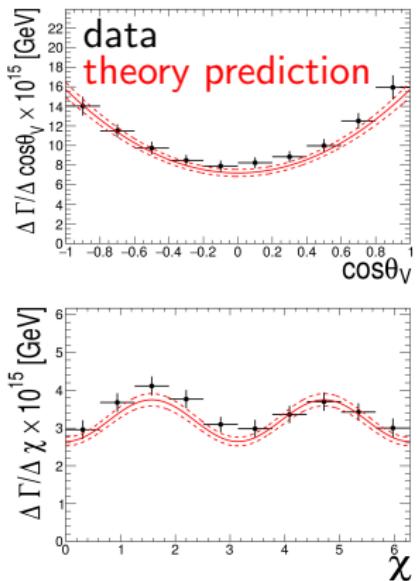
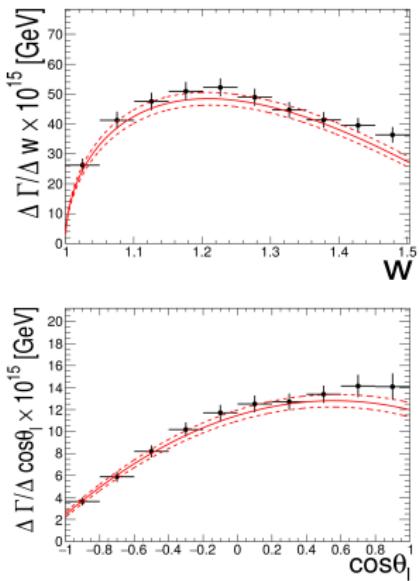
$$\mathcal{R}(D^*)_{\text{SM}} = 0.242 \pm 0.005$$

- Possibility to test compatibility with NP such as right-handed currents once calculations for FF available



Unfolding of the kinematic distributions

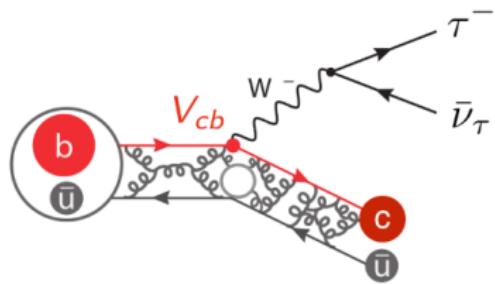
- Unfolded spectra provided: corrected for migration and acceptance
- Difference between inclusive and exclusive depends on parametrisation
- Work ongoing to extract $|V_{cb}|$ using BGL parametrisation



Follow up papers:
arXiv:1703.05330 (04/17)
arXiv:1703.06124 (04/17)
arXiv:1703.08170 (06/17)

→ Talk by Stefan Schacht
(<https://indico.cern.ch/event/466934/contributions/2586301/>)

Measurement of the branching ratio of $\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$
relative to $\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}_\ell$ decays with a semileptonic
tagging method



Phys.Rev. D94 (2016) no.7, 072007 – Published 27 October 2016
arXiv:1607.07923 [hep-ex] 13 Dec 2016

Analysis strategy

- Analysis restricted to neutral $B^0\bar{B}^0$ pairs (due to high background)

Reconstruction

Semileptonic tag ($\epsilon \sim 10^{-2}$): $B_{tag} \rightarrow D^*\ell\nu$ (1 neutrino)

Signal: $B_{sig} \rightarrow D^*\tau\nu$ $\tau \rightarrow \ell\nu_\ell\nu_\tau$ (3 neutrino)

Normalisation: $B_{sig} \rightarrow D^*\ell\nu$ (1 neutrino)

Analysis strategy

- Analysis restricted to neutral $B^0\bar{B}^0$ pairs (due to high background)

Reconstruction

Semileptonic tag ($\epsilon \sim 10^{-2}$): $B_{tag} \rightarrow D^*\ell\nu$ (1 neutrino)

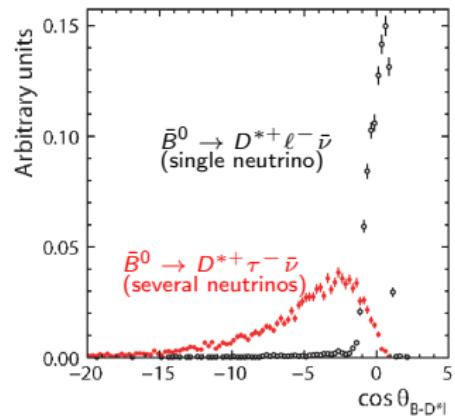
Signal: $B_{sig} \rightarrow D^*\tau\nu$ $\tau \rightarrow \ell\nu_\ell\nu_\tau$ (3 neutrino)

Normalisation: $B_{sig} \rightarrow D^*\ell\nu$ (1 neutrino)

Separation of signal mode and normalisation mode

Angle betw. B and $D^*\ell$ -system in $\Upsilon(4S)$ frame:

$$\cos \theta_{B-D^*\ell} = \frac{2E_{beam}E_{D^*\ell} - m_B^2 - M_{D^*\ell}^2}{2|\vec{p}_B||\vec{p}_{D^*\ell}|}$$



- Assumes single neutrino
- Outside range $[-1, 1]$ for signal decay

Signal extraction

- 2-dimensional extended binned likelihood fit to E_{ECL} and O_{NB}

E_{ECL}

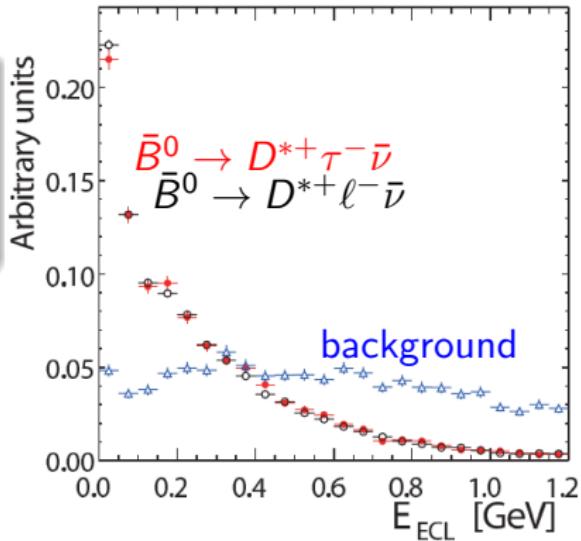
Cluster energy not associated to event

- around zero for correct reconstruction
- flat for background

O_{NB} : Neural network classifier

Signal likelihood using:

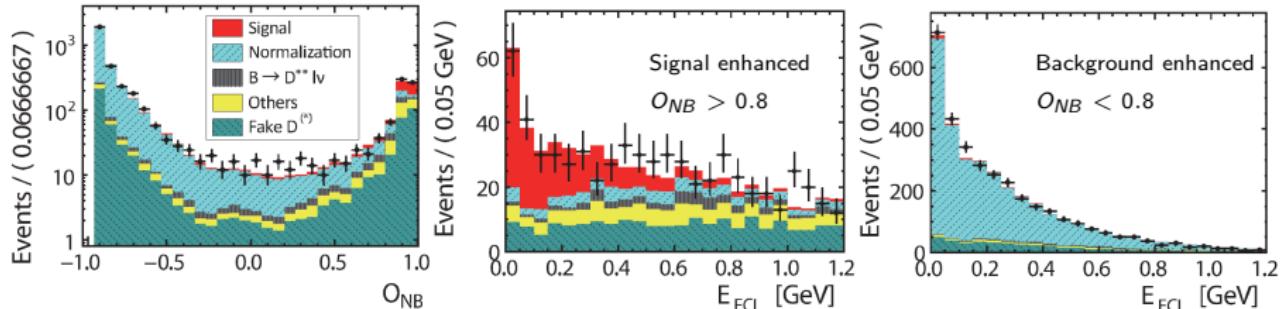
- $\cos \theta_{B-D^* \ell \nu}^{sig}$
- $m_{miss}^2 = (2E_{beam} - \sum_i E_i)^2 - |\sum_i \vec{p}_i|^2$
- $E_{vis} = \sum_i E_i$



Efficiency: $\frac{\epsilon_{norm}}{\epsilon_{sig}} = 1.289 \pm 0.015$

Results

Fit to data:



$$\mathcal{R}(D^*) = \frac{1}{2\mathcal{B}(\tau \rightarrow \ell\nu_\ell\nu_\tau)} \cdot \underbrace{\frac{\epsilon_{norm}}{\epsilon_{sig}}}_{\text{determined from MC}} \cdot \underbrace{\frac{N_{sig}}{N_{norm}}}_{\text{from fit}}$$

Result

$$\mathcal{R}(D^*) = 0.302 \pm 0.030 \pm 0.011 \quad (\text{agreement with SM: } 1.6\sigma)$$

- Good agreement with previous Belle measurements

New Physics interpretation

- Compatibility with New Physics tested in model independent way

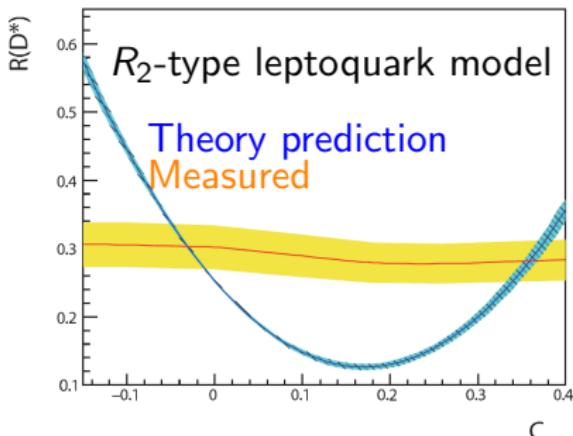
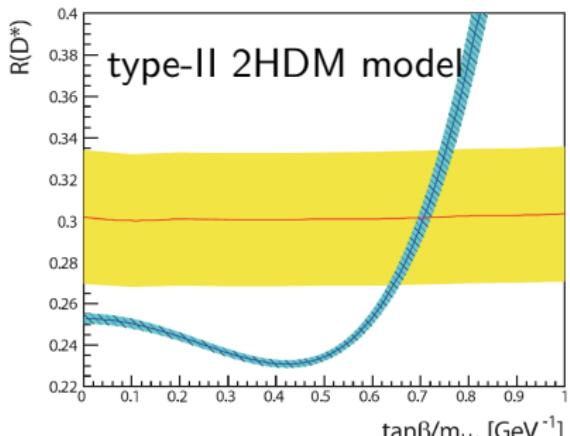
$$H_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{cb} \left[\mathcal{O}_{SM} + \sum_{\text{all}} C_X \mathcal{O}_X \right]$$

\mathcal{O}_X : all possible 4-fermion operator

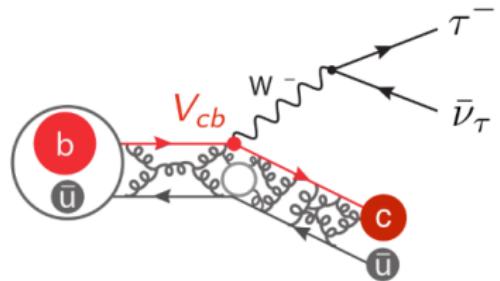
C_X : Wilson coefficients

- Analysis repeated using MC for each of 6 \mathcal{O}_X added one-by-one to constrain Wilson Coefficients

Examples of model interpretations:



Measurement of the τ lepton polarization and $\mathcal{R}(D^*)$ in the decay $\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau$



Phys. Rev. Lett. 118, 211801 Published 26 May 2017
arXiv:1612.00529 [hep-ex]

Measurement of τ lepton polarisation in $B \rightarrow D^* \tau \nu$



$$P_\tau(D^*) = \frac{\Gamma^+(D^*) - \Gamma^-(D^*)}{\Gamma^+(D^*) + \Gamma^-(D^*)}$$

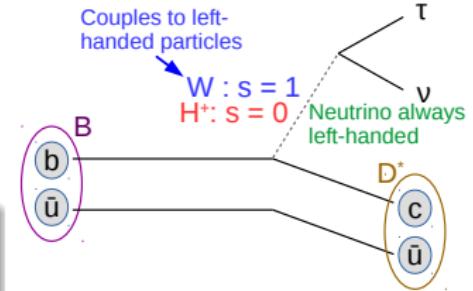
$\Gamma^\pm(D^*)$: $B \rightarrow D^* \tau \nu$ decay rate for τ helicity = $\pm \frac{1}{2}$

SM prediction

$$P_\tau(D^*) = -0.497 \pm 0.013$$

Tanaka & Watanabe (Phys. Rev. D 87, 034028, 2013)

τ polarisation sensitive to NP



Measurement of τ lepton polarisation in $B \rightarrow D^* \tau \nu$



$$P_\tau(D^*) = \frac{\Gamma^+(D^*) - \Gamma^-(D^*)}{\Gamma^+(D^*) + \Gamma^-(D^*)}$$

$\Gamma^\pm(D^*)$: $B \rightarrow D^* \tau \nu$ decay rate for τ helicity $= \pm \frac{1}{2}$

SM prediction

$$P_\tau(D^*) = -0.497 \pm 0.013$$

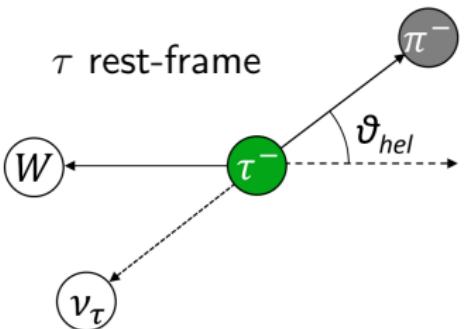
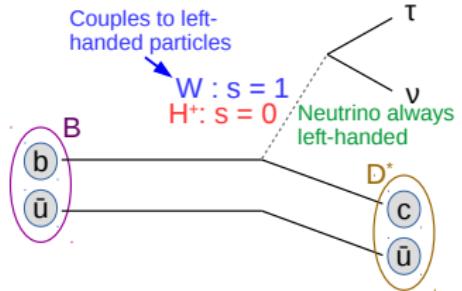
Tanaka & Watanabe (Phys. Rev. D 87, 034028, 2013)

Measurement from two-body hadronic τ decays (hadronic tagging)

$$\frac{d\Gamma(D^*)}{d \cos \vartheta_{hel}} = \frac{\Gamma(D^*)}{2} [1 + \alpha P_\tau(D^*) \cos \vartheta_{hel}]$$

- α : sensitivity from τ decay mode ($\alpha \sim 0$ from leptonic τ decays)
- $\tau \rightarrow \pi \nu_\tau$ ($\alpha = 1$)
- $\tau \rightarrow \rho \nu_\tau$ ($\alpha = 0.45$)

τ polarisation sensitive to NP



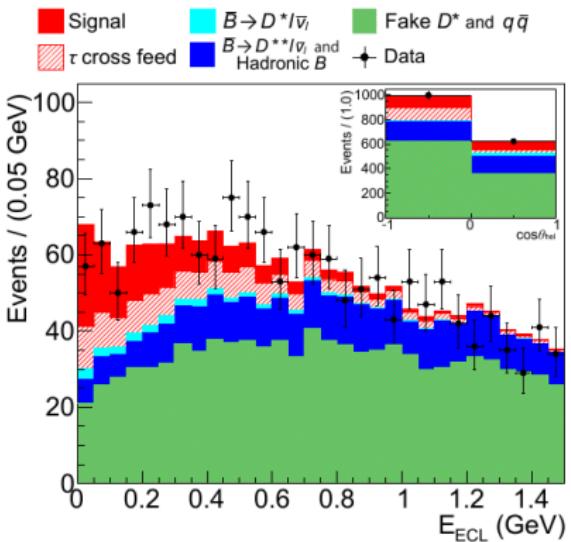
Signal extraction

- Divide signal into forward ($\cos \vartheta_{hel} > 0$) and backward ($\cos \vartheta_{hel} < 0$) to calculate polarisation

$$P_\tau(D^*) = \frac{2(N_{sig}^F - N_{sig}^B)}{\alpha(N_{sig}^F + N_{sig}^B)}$$

8 categories

$$(B^\pm, \bar{B}^0) \otimes (\pi\nu_\tau, \rho\nu_\tau) \otimes (\text{frwd}, \text{bkwd})$$



- Likelihood fit in 2 steps:
 - to normalisation sample for $B \rightarrow D^* \ell \nu$ yield (using M_{miss}^2)
 - simultaneous fit to 8 signal samples (using E_{ECL})

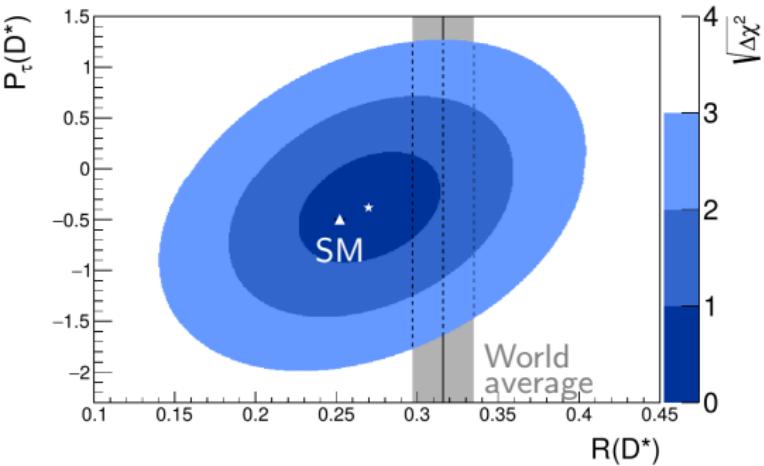
Results

- $\mathcal{R}(D^*)$ can be calculated as before from extracted yields
- Polarisation from forward/backward asymmetry

$$\begin{aligned}\frac{\epsilon_{norm}}{\epsilon_{sig}} &= 0.97 \pm 0.02 \quad (B^\pm, \tau \rightarrow \pi\nu) \\ &= 1.21 \pm 0.03 \quad (B^0, \tau \rightarrow \rho\nu) \\ &= 3.42 \pm 0.07 \quad (B^\pm, \tau \rightarrow \rho\nu) \\ &= 3.83 \pm 0.12 \quad (B^0, \tau \rightarrow \rho\nu)\end{aligned}$$

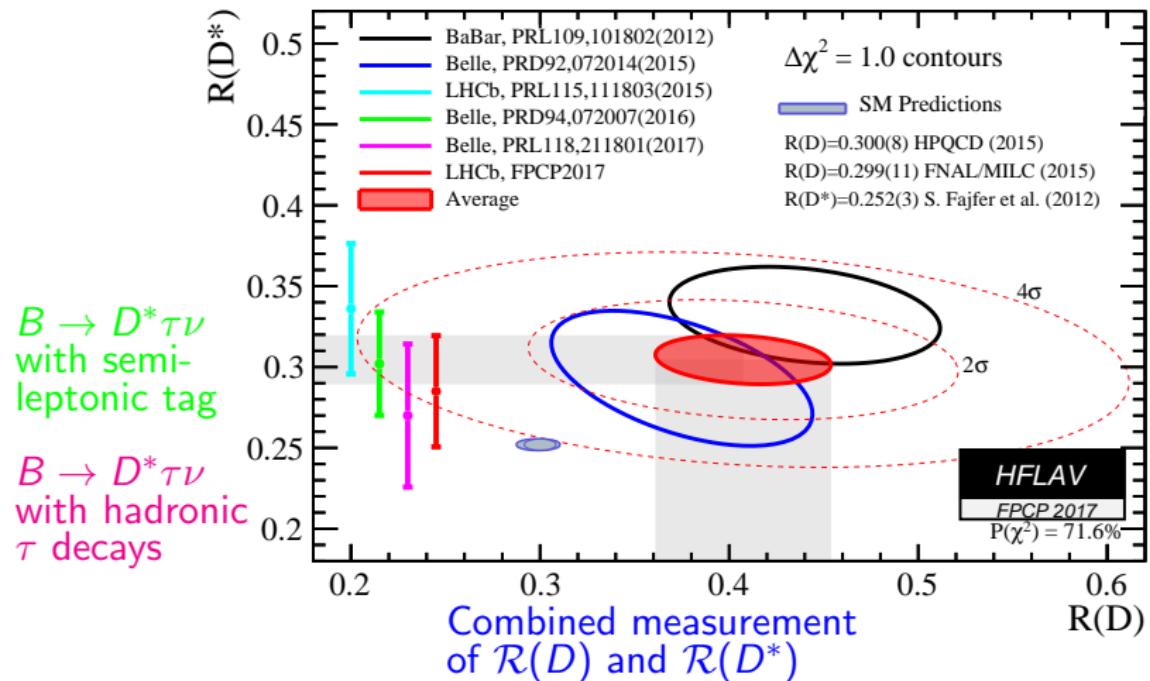
Result

$$\begin{aligned}\mathcal{R}(D^*) &= 0.270 \pm 0.035^{+0.028}_{-0.025} \\ P_\tau(D^*) &= -0.38 \pm 0.51^{+0.21}_{-0.16}\end{aligned}$$



- Consistent with SM and previous measurements!
- Error can be reduced in Belle II

New status of $\mathcal{R}(D^*)$



Excess still 4σ : central value moved towards SM;

on $\mathcal{R}(D^*)$, discrepancy increased from 3.0σ to 3.4σ

Measurement of the decays $B \rightarrow \eta \ell \nu_\ell$ and $B \rightarrow \eta' \ell \nu_\ell$ in fully reconstructed events at Belle

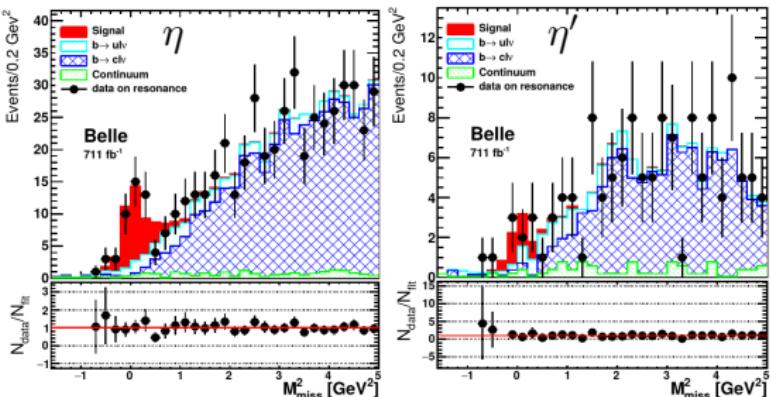
arXiv:1703.10216 – 29 March 2017
submitted to PRD(RC)

Overview and result

Important to know decay composition for signal model in inclusive $|V_{ub}|$ measurements → test tension between inclusive and exclusive

Reconstruction & signal extraction:

- Hadronic tagging to reduce background
- η : $\eta \rightarrow \gamma\gamma$ and $\eta \rightarrow \pi^+\pi^-\pi^0$
- η' : $\eta' \rightarrow \eta\pi^+\pi^-$ with $\eta \rightarrow \gamma\gamma$



Binned likelihood fit on M_{miss}^2 with 4 components

Results

$$\mathcal{B}(B \rightarrow \eta \ell \nu_\ell) = (4.2 \pm 1.1 \pm 0.3) \cdot 10^{-5}$$

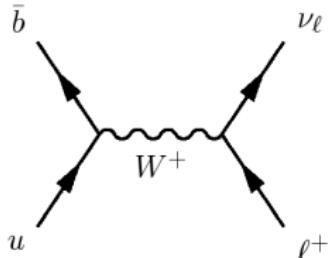
$$\mathcal{B}(B \rightarrow \eta' \ell \nu_\ell) < 0.72 \cdot 10^{-4} \text{ at 90% C.L.}$$

- Compatible with results from CLEO and BaBar
- Limited by stat. → significant improvement with Belle II

Search for $B \rightarrow \mu\nu$ decays at the Belle experiment

July 2017,
PRL journal publication in preparation

- $\mathcal{B}(B \rightarrow \mu\nu)$ precisely predicted in the SM
- May increase significantly within NP models
- Limit (HFLAV, Nov 2016): $< 10 \cdot 10^{-7}$ (90% C.L.)



- New result from Belle: first measurement leading to branching fraction (not upper limit)

SM prediction

$$\mathcal{B}(B \rightarrow \mu\nu) = (3.80 \pm 0.31) \cdot 10^{-7}$$

Input from:

Na et al., arXiv:1212.0586
Particle Data Group, Chin. Phys. C 40, no. 10, 100001 (2016)
Belle Collaboration, Phys. Rev. D 88, 032005 (2016)
Fermilab Lattice and MILC Coll., Phys. Rev. D 92, 014024 (2015)

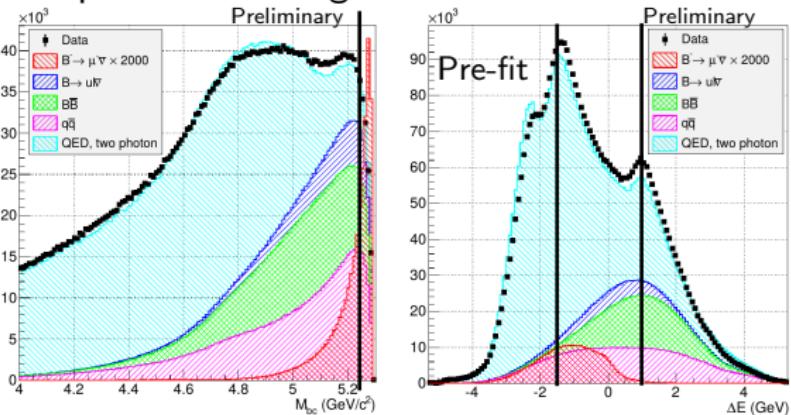
Selection & signal extraction



Untagged: all reco. particles except muon belong to 2nd B

$$M_{bc} = \sqrt{E_{\text{beam}}^2 - \left(\sum_i \vec{p}_i^* \right)^2}$$

$$\Delta E = E_B - E_{\text{beam}}$$



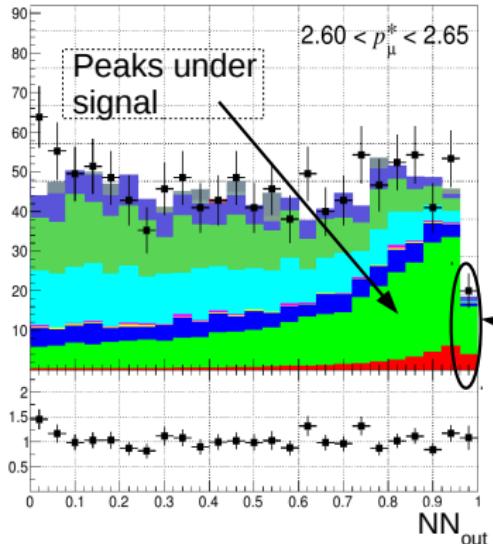
Signal selection

- Angle between \vec{p}_μ and thrust axis used to reduce jet-like continuum
- B rest-frame: $E_\mu = \frac{m_B}{2}$ (boosted in CMS: p_μ^*)
- p_μ^* side-bands used for validation
- Neural network trained for separation of signal from background

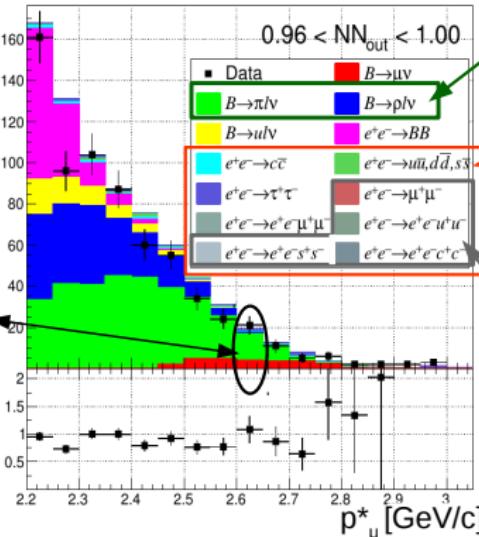
Result

2-dim. binned likelihood fit in p_μ^* and neural network output

Preliminary



Peaks under signal



Detailed study with FF variation

Validated with data below $B\bar{B}$ threshold

Fixed in fit

Signal efficiency: 38%

- Cancellation of systematics in ratio $R = \frac{N_{B \rightarrow \mu\nu}}{N_{B \rightarrow \pi\ell\nu}}$ (efficiency from $R_{\text{fit}}/R_{\text{MC}}$)

Preliminary results

$$\mathcal{B}(B \rightarrow \mu\nu) = (6.46 \pm 2.22 \pm 1.55) \cdot 10^{-7}$$

$$\mathcal{B}(B \rightarrow \mu\nu) \in [2.9, 10.7] \times 10^{-7} \text{ at 90\% C.L.}$$

Consistent with SM!

Significance: 2.4σ

Will improve with Belle II...

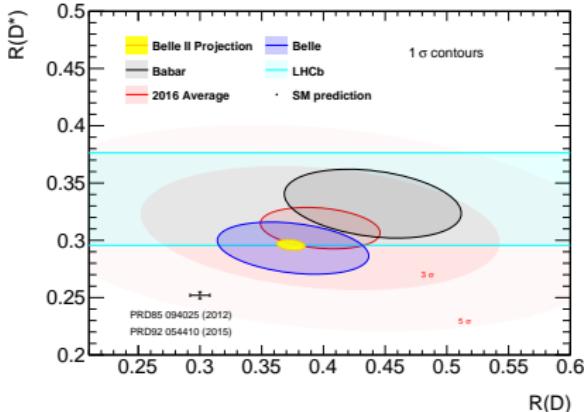
Conclusion

- $|V_{cb}|$ and FF parameters from $B \rightarrow D^* \ell \nu$: agree with world average
- Unfolded differential decay rates: can be used to test different models
- Three measurements of $\mathcal{R}(D^{(*)})$, yielding compatible results
- First measurement of τ polarisation: agrees with the SM prediction
- First measurement of $B \rightarrow \eta^{(\prime)} \ell \nu_\ell$ by Belle
- First measurement of $B \rightarrow \mu \nu$ leading to a branching fraction

Prospects for Belle II:

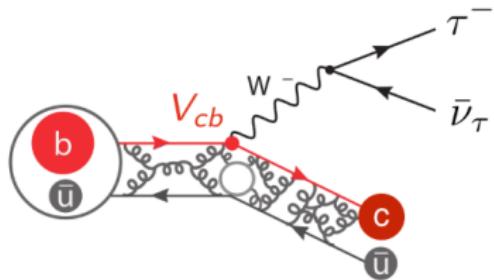
Observable	Belle / LHCb Measurements	Today	Belle II 5/ab	Belle II 50/ab
$R(D)$	0.403 ± 0.040 ± 0.024	12%	5.6%	3.2%
$R(D^*)$	0.310 ± 0.015 ± 0.008	5.4%	3.9%	2.2%

For confirmed central value, would be possible to measure 9σ deviation from SM!



Backup

Measurement of the branching ratio of $\bar{B} \rightarrow D^{(*)}\tau^-\bar{\nu}_\tau$ relative to $\bar{B} \rightarrow D^{(*)}\ell^-\bar{\nu}_\ell$ decays with hadronic tagging at Belle

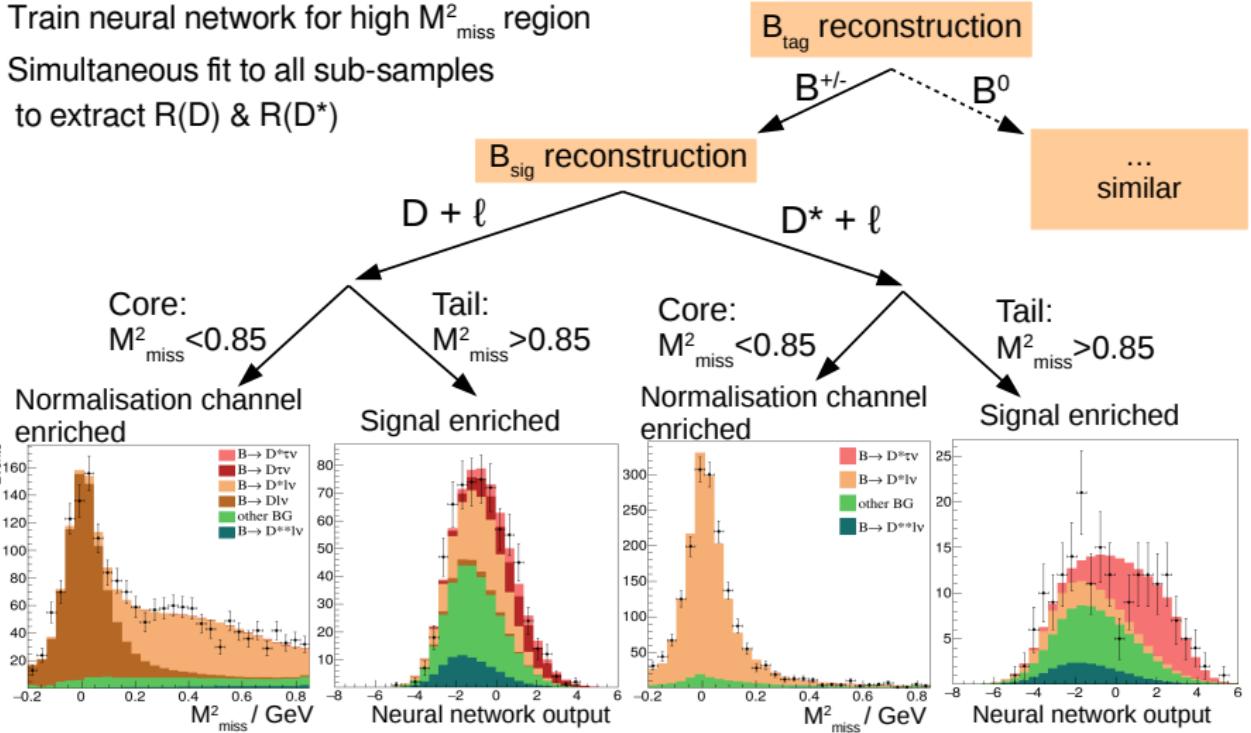


Phys. Rev. D 92, 072014 Published 26 October 2015
arXiv:1507.03233 [hep-ex] 12 July 2015

Simultaneous fit of $\mathcal{R}(D)$ and $\mathcal{R}(D^*)$



- τ lepton reconstructed in $\tau \rightarrow \ell \nu_\ell \bar{\nu}_\tau$
- Same reco. final state for signal and normalisation: use M_{miss}^2 to separate them
- Train neural network for high M_{miss}^2 region
- Simultaneous fit to all sub-samples to extract $R(D)$ & $R(D^*)$



Results and New Physics interpretation



Result

$$\mathcal{R}(D) = 0.375 \pm 0.064 \pm 0.026$$

$$\mathcal{R}(D^*) = 0.293 \pm 0.038 \pm 0.015$$

Agreement with SM: 1.8σ

Test of type II 2HDM model:

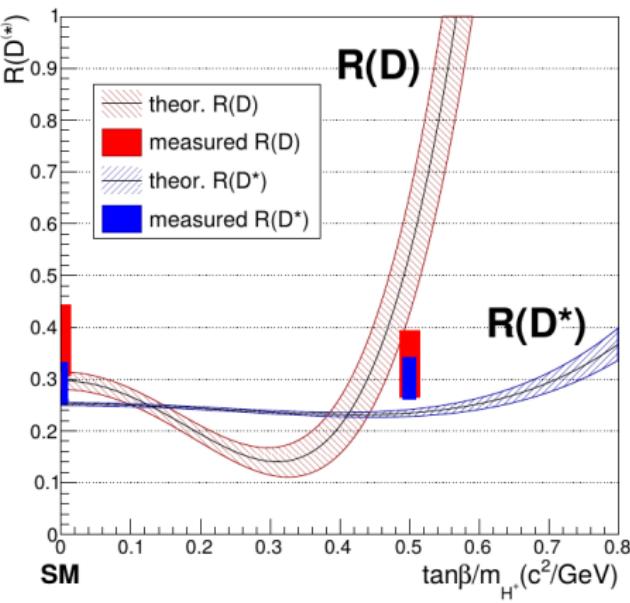
- Acceptances & efficiencies depend model assumptions: fit repeated with MC generated with $\frac{\tan\beta}{m_{H^+}} = 0.5 \text{ GeV}^{-1}$

Results:

$$\mathcal{R}(D) = 0.329 \pm 0.060 \pm 0.022$$

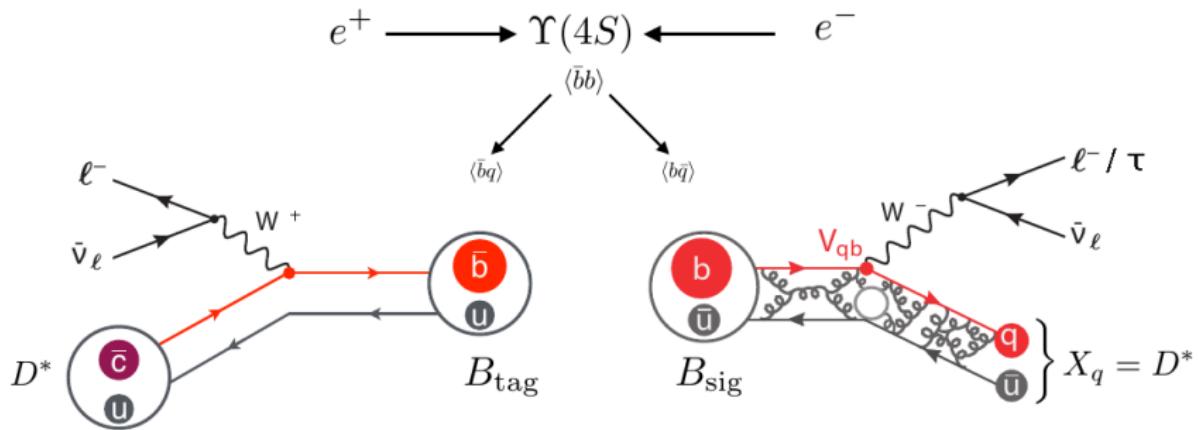
$$\mathcal{R}(D^*) = 0.301 \pm 0.039 \pm 0.015$$

$$\mathcal{R}(D^*) = \frac{1}{2\mathcal{B}(\tau \rightarrow \ell\nu_\ell\nu_\tau)} \cdot \underbrace{\frac{\epsilon_{norm}}{\epsilon_{sig}}}_{\text{determined from MC}} \cdot \underbrace{\frac{N_{sig}}{N_{norm}}}_{\text{from fit}}$$



Semileptonic B meson tagging

- Reconstruct tagging B meson in $B \rightarrow D^* \ell \nu$
- Measurement statistically independent to those with hadronic tagging



$|V_{cb}|$ and FF's from $B \rightarrow D^* \ell \nu$

Systematic uncertainties:

Error Source	$\Delta\mathcal{B}$ [%]
Tagging Calibration	3.6
$N_{B\bar{B}}$	1.4
f_{+0}	1.1
PDF shapes	0.9
$\mathcal{B}(D \rightarrow K\pi(\pi)(\pi))$	0.4
$\mathcal{B}(D^* \rightarrow D\pi)$	0.2
$\mathcal{B}(\bar{B} \rightarrow D^{**}\ell\bar{\nu}_\ell)$	0.2
e PID	0.2
μ PID	0.1
π_{slow} Eff.	0.1
$\mathcal{B}(\bar{B} \rightarrow D\ell\bar{\nu}_\ell)$	< 0.1
$B \rightarrow D^{(*,**)}\ell\bar{\nu}_\ell$ FFs	< 0.1
Lepton Fakerates	< 0.1
K PID	< 0.1
Total	4.2

Combined $\mathcal{R}(D)$ and $\mathcal{R}(D^*)$



Systematic uncertainties:

	$R(D) [\%]$	$R(D^*) [\%]$	Correlation
$D^{(*)\ell\nu}$ shapes	4.2	1.5	0.04
D^{**} composition	1.3	3.0	-0.63
Fake D yield	0.5	0.3	0.13
Fake ℓ yield	0.5	0.6	-0.66
D_s yield	0.1	0.1	-0.85
Rest yield	0.1	0.0	-0.70
Efficiency ratio f^{D^+}	2.5	0.7	-0.98
Efficiency ratio f^{D^0}	1.8	0.4	0.86
Efficiency ratio $f_{\text{eff}}^{D^{*+}}$	1.3	2.5	-0.99
Efficiency ratio $f_{\text{eff}}^{D^{*0}}$	0.7	1.1	0.94
CF double ratio g^+	2.2	2.0	-1.00
CF double ratio g^0	1.7	1.0	-1.00
Efficiency ratio f_{wc}	0.0	0.0	0.84
M_{miss}^2 shape	0.6	1.0	0.00
o'_{NB} shape	3.2	0.8	0.00
Lepton PID efficiency	0.5	0.5	1.00
Total	7.1	5.2	-0.32

Systematic uncertainties:

Sources	$\mathcal{R}(D^*) [\%]$		
	$\ell^{\text{sig}} = e, \mu$	$\ell^{\text{sig}} = e$	$\ell^{\text{sig}} = \mu$
MC size for each PDF shape	2.2 +1.1 -0.0	2.5 +2.1 -0.0	3.9 +2.8 -0.0
PDF shape of the normalization in $\cos \theta_{B-D^*\ell}$	+1.0 -1.7	+0.7 -1.3	+2.2 -3.3
PDF shape and yields of fake $D^{(*)}$	1.4	1.6	1.6
PDF shape and yields of $B \rightarrow X_c D^*$	1.1	1.2	1.1
Reconstruction efficiency ratio $\varepsilon_{\text{norm}}/\varepsilon_{\text{sig}}$	1.2	1.5	1.9
Modeling of semileptonic decay	0.2	0.2	0.3
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.2	0.2	0.2
Total systematic uncertainty	+3.4 -3.5	+4.1 -3.7	+5.9 -5.8

Systematic uncertainties:

Source	rel. uncertainty on $\mathcal{R}(D^*)$	uncertainty on $P_\tau(D^*)$
Hadronic B decay composition	+7.7% -6.9%	+0.13 -0.10
MC stat. for PDF construction	+4.0% -2.8%	+0.15 -0.11
Semileptonic B decays	$\pm 3.5\%$	± 0.05
Fake D^* background	$\pm 3.4\%$	0.02
Other	$\pm 2.2\%$	± 0.03

Allowed regions for Wilson coefficients

Models or operators	Parameters	Allowed regions (68% C.L.)
\mathcal{O}_{S_1}	C_{S_1}	$[-4.25, -3.09], [+0.44, +1.57]$
\mathcal{O}_{S_2}	C_{S_2}	$[-1.56, -0.43], [+3.12, +4.28]$
\mathcal{O}_{V_1}	C_{V_1}	$[-2.15, -2.03], [+0.05, +0.15]$
\mathcal{O}_{V_2}	C_{V_2}	$[-0.17, 0.00], [+1.83, +1.96]$
\mathcal{O}_T	C_T	$[-0.06, -0.01], [+0.34, +0.39]$
R_2 -type leptoquark	$C_T (= +C_{S_2}/7.8)$	$[-0.05, -0.01], [+0.34, +0.38]$
S_1 -type leptoquark	$C_T (= -C_{S_2}/7.8)$	$[-0.07, -0.01], [+0.22, +0.28]$