A visualization of the cosmic web, showing a complex network of filaments and nodes of matter in a reddish-orange color scheme. The filaments are interconnected, forming a web-like structure that fills the entire frame. The nodes are denser regions where filaments intersect.

# LARGE SCALE STRUCTURE in the INTERGALACTIC MEDIUM

60 comoving Mpc/h

A horizontal white double-headed arrow spanning the width of the slide, indicating the scale of the visualization.

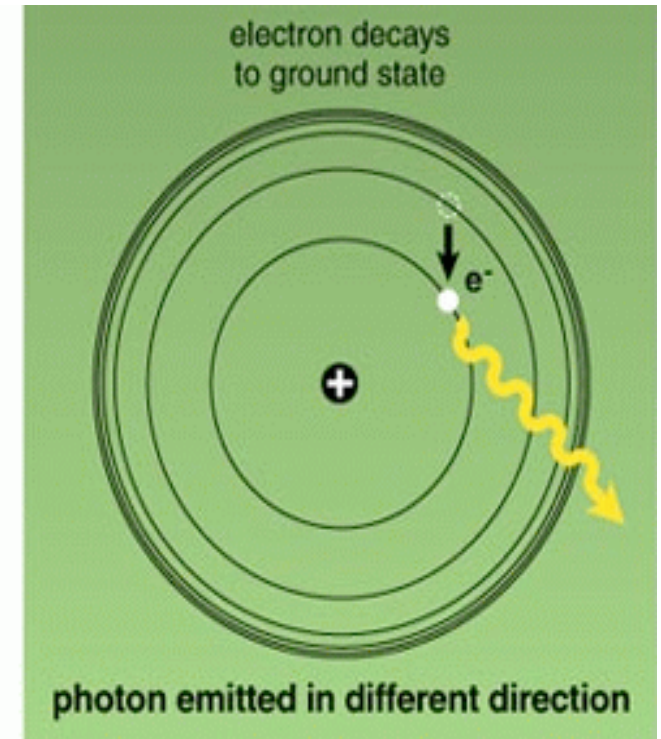
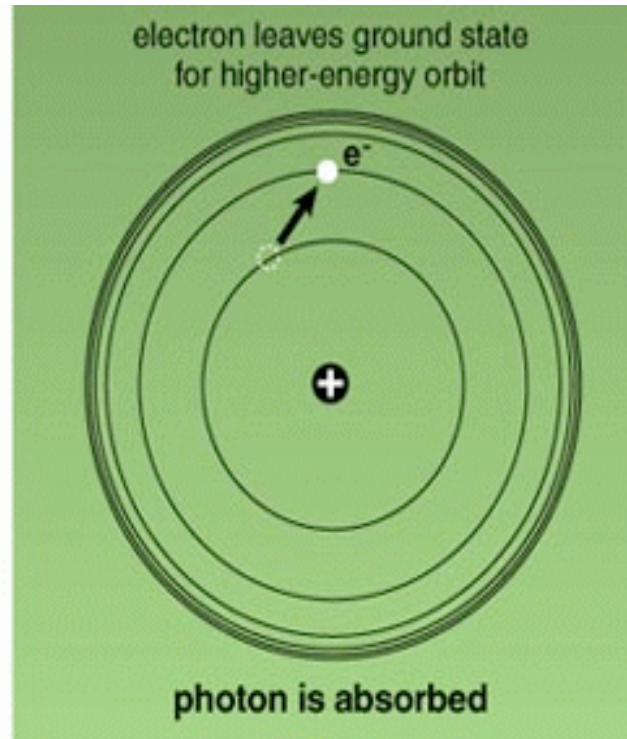
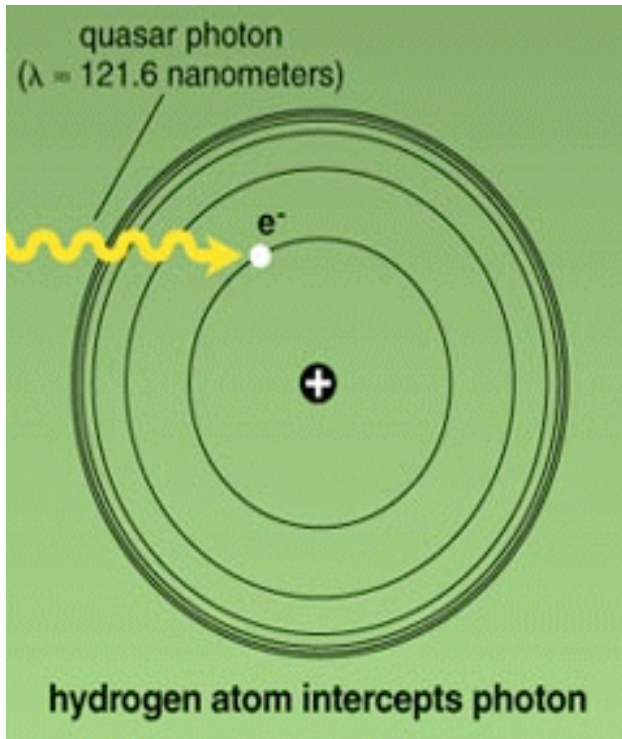
**MATTEO VIEL**

INAF & INFN – Trieste

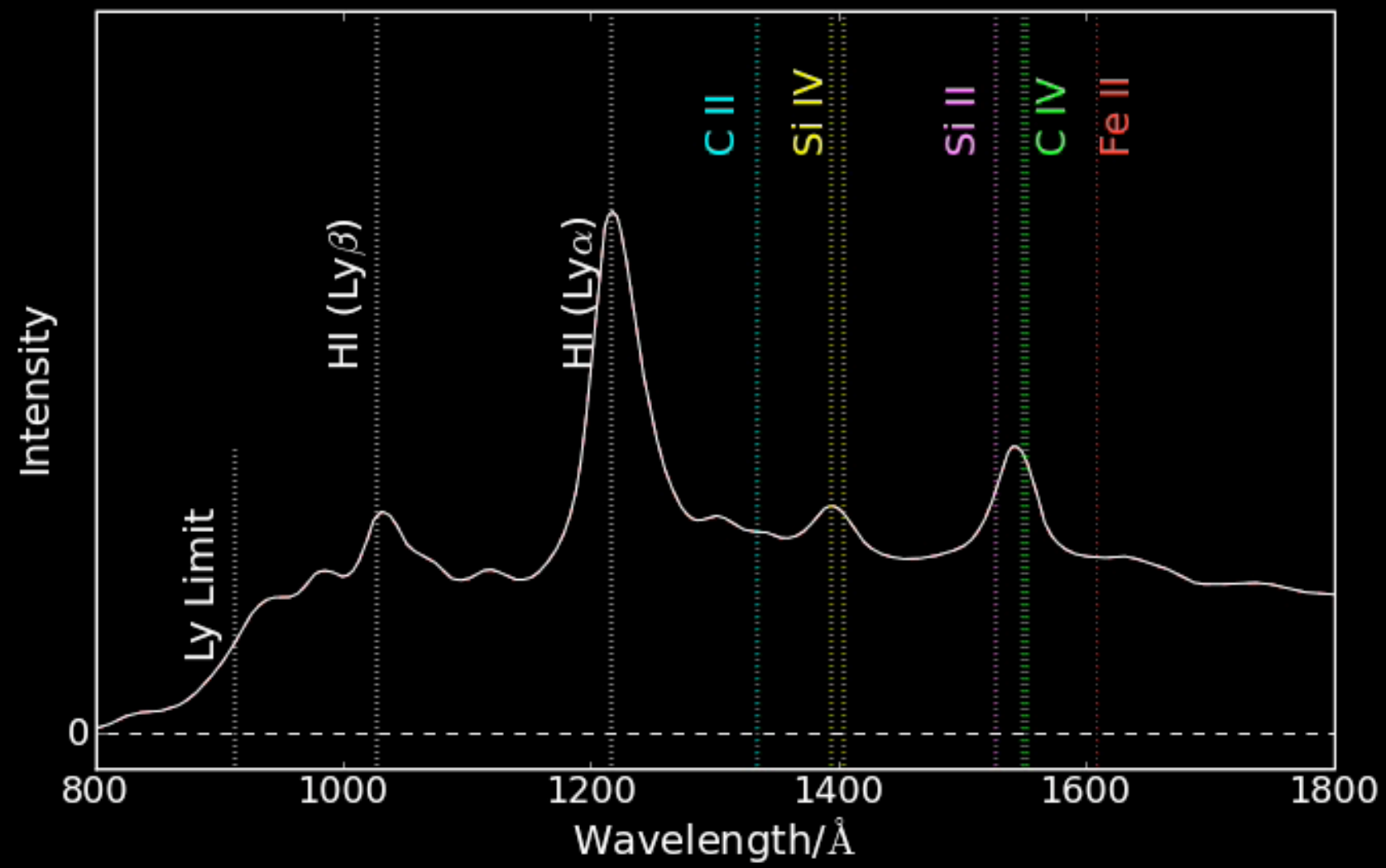
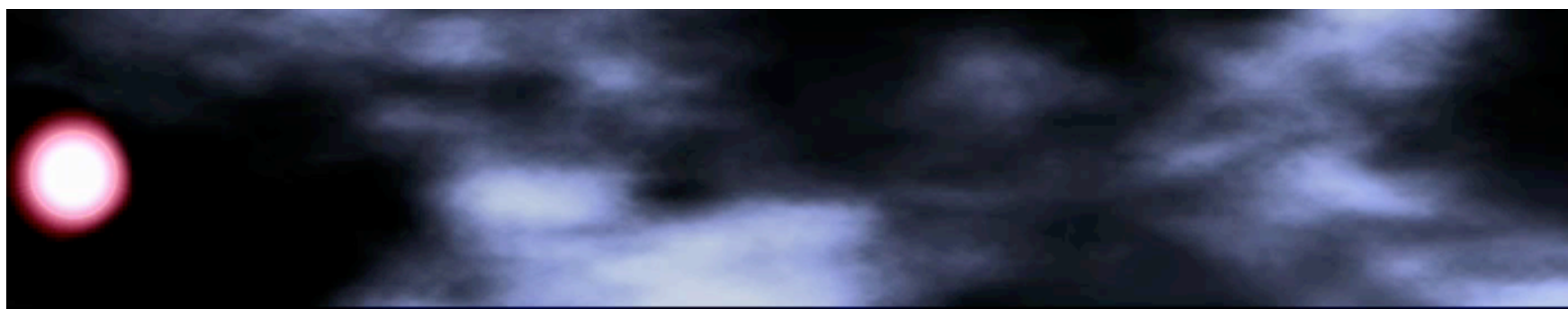
COSMO 09 – CERN

**INTRO**

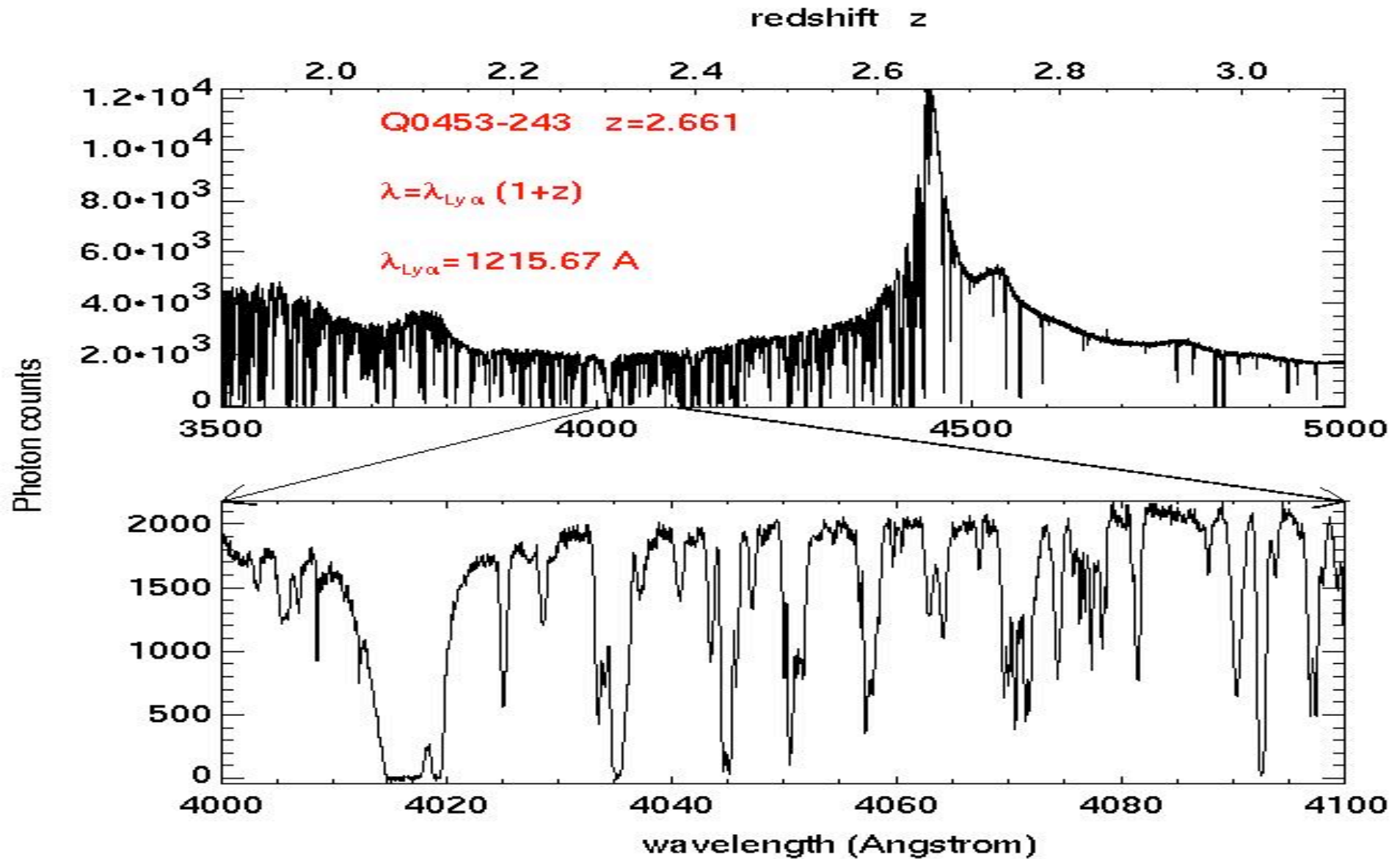
Lyman- $\alpha$  absorption is the main manifestation of the IGM



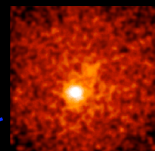
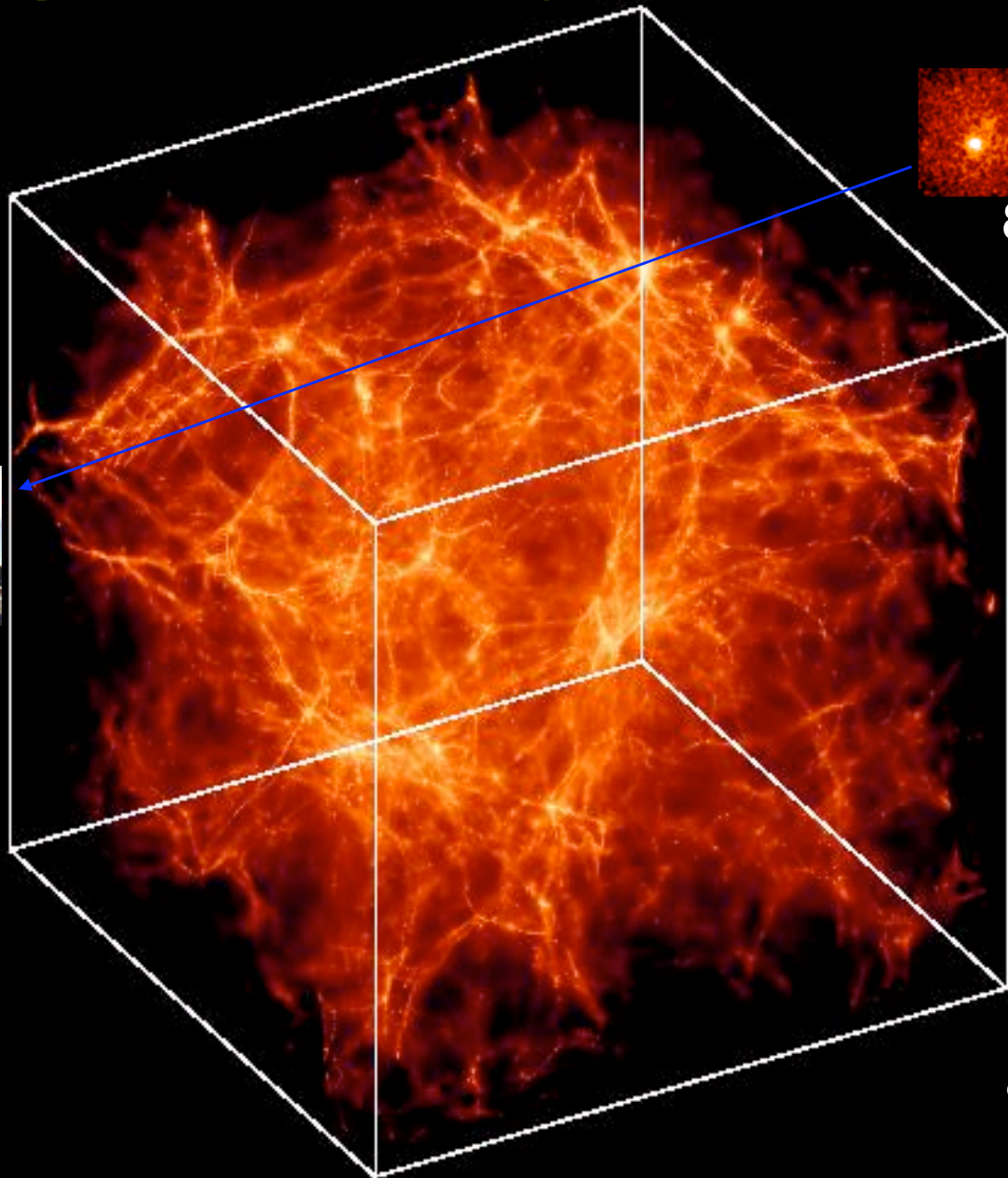
Tiny neutral hydrogen fraction after reionization... But large cross-section



# DATA: high resolution spectrum



# THEORY: GAS in a $\Lambda$ CDM universe



80 % of the baryons at  $z=3$   
are in the Lyman- $\alpha$  forest

Bi & Davidsen (1997), Rauch (1998)

baryons as tracer of the dark  
matter density field

$\delta_{\text{IGM}} \sim \delta_{\text{DM}}$  at scales larger than the  
Jeans length  $\sim 1 \text{ com Mpc}$

$\text{flux} = \exp(-\tau) \sim \exp(-(\delta_{\text{IGM}})^{1.6} T^{-0.7})$

# BRIEF HISTORICAL OVERVIEW of the Lyman- $\alpha$ forest

- Gunn & Peterson (1965): a uniform IGM at redshift 2 is very highly ionized, to avoid very large HI opacity;

'ISOLATED' CLOUDS

PROBES OF THE  
JEANS SCALE

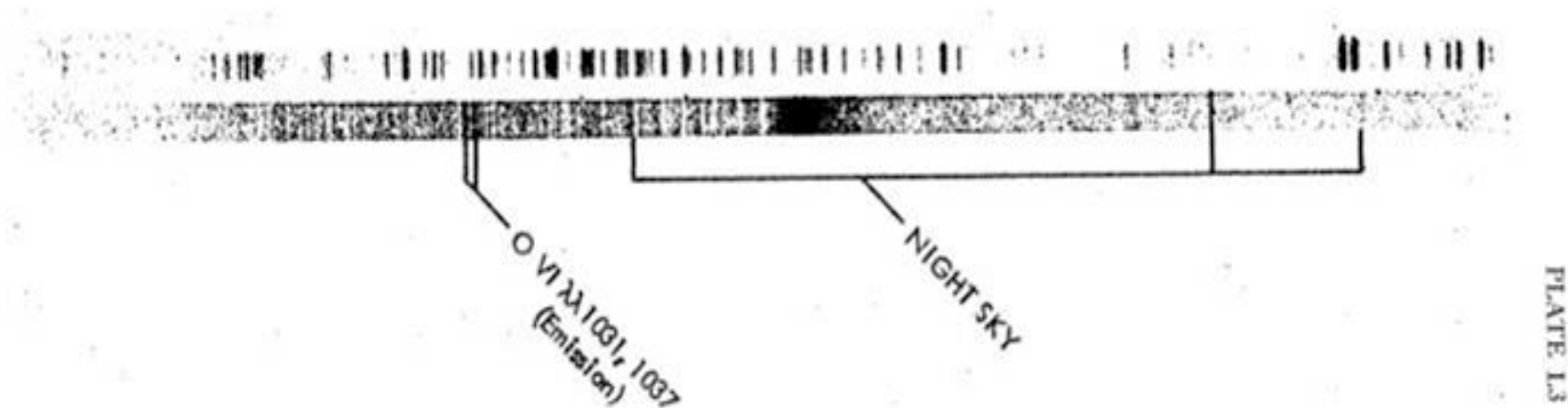


FIG. 1.—A spectrogram illustrating the numerous absorption lines in 4C 05.34. The strong emission line in the center is  $\text{L}\alpha$ . The O VI emission lines and several airglow features are also indicated. The comparison spectrum is He + Ar + Ne.

LYNDS (see page L73)

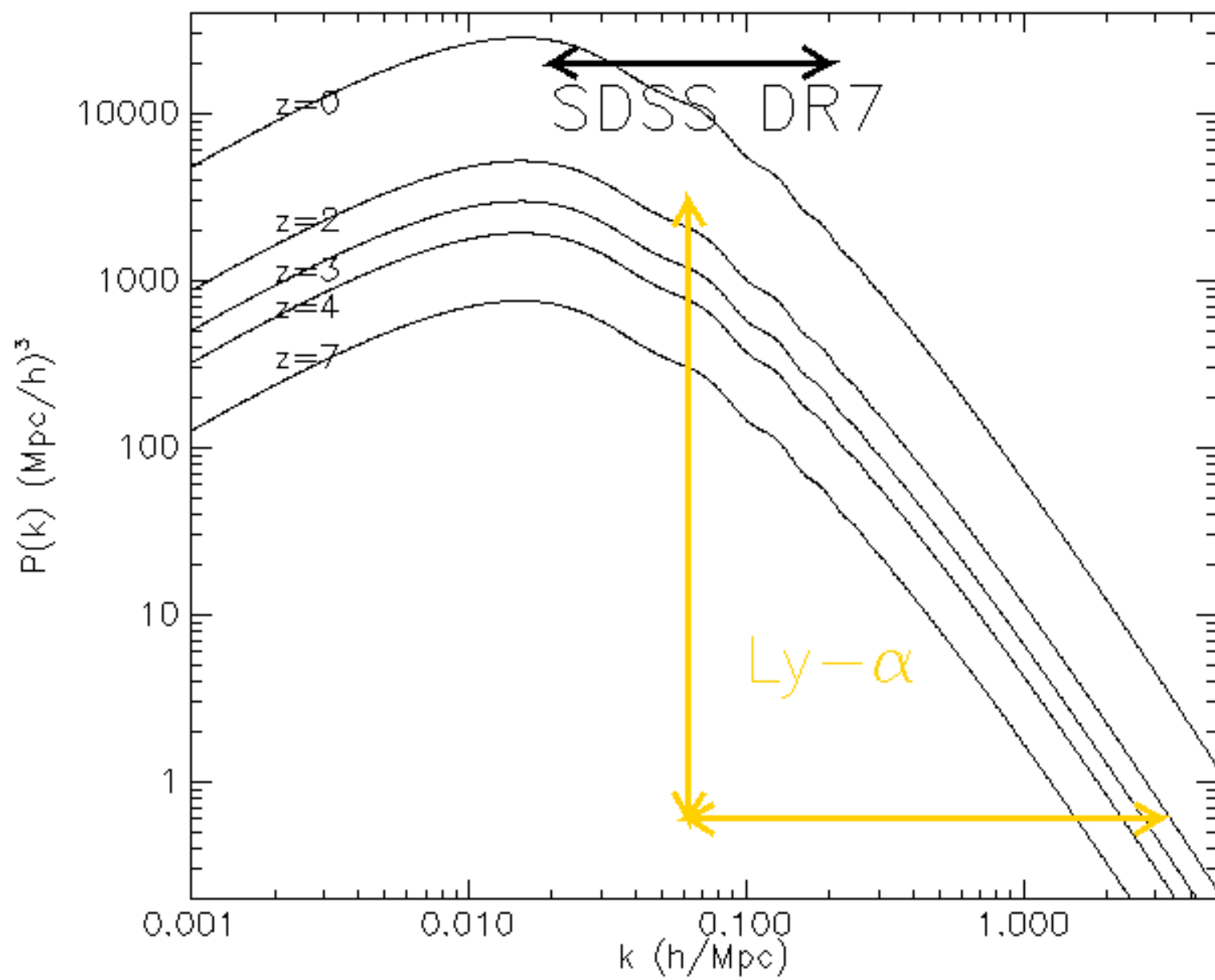
v

NETWORK OF FILAMENTS

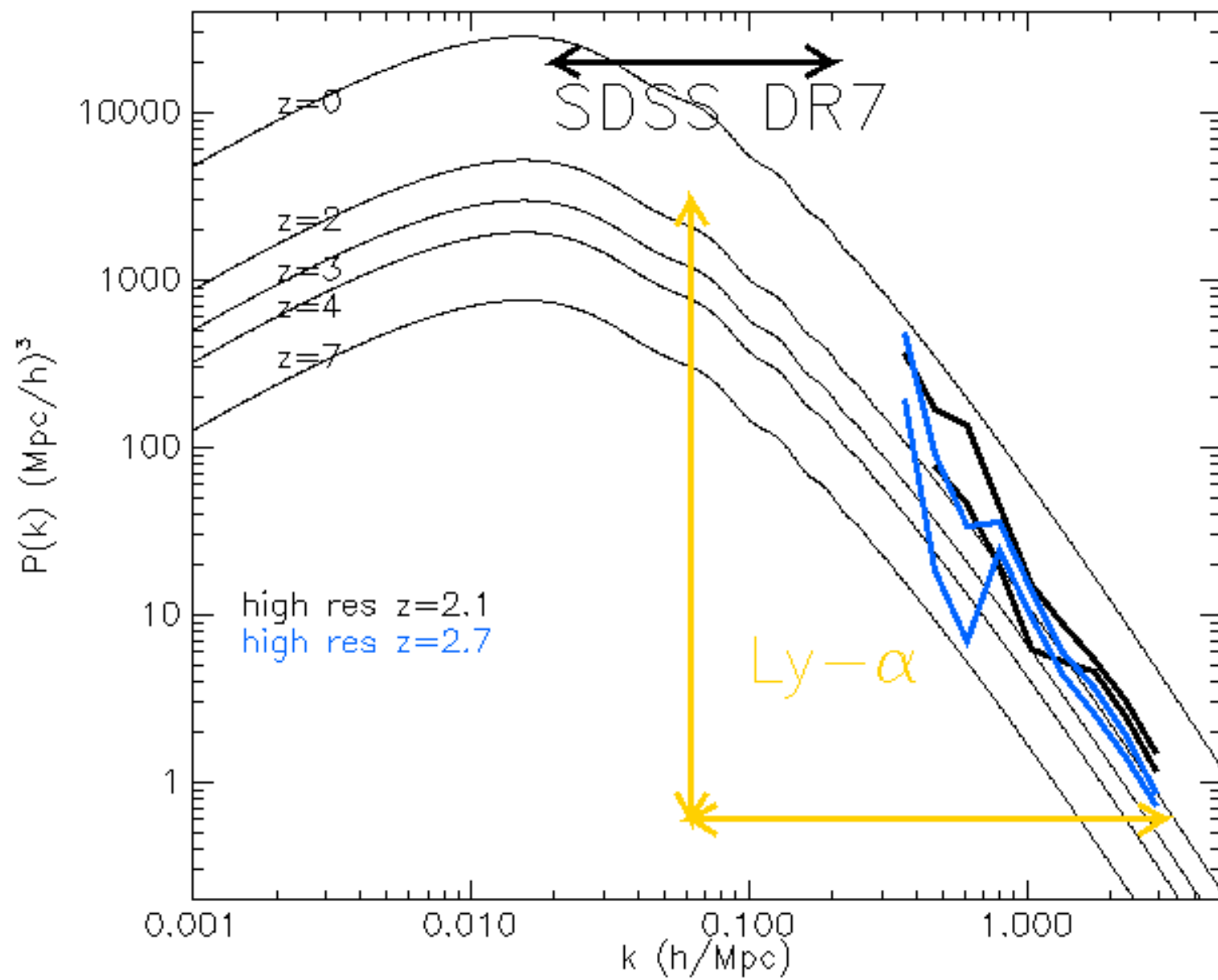
discrete clouds, reproduced most of the observations;

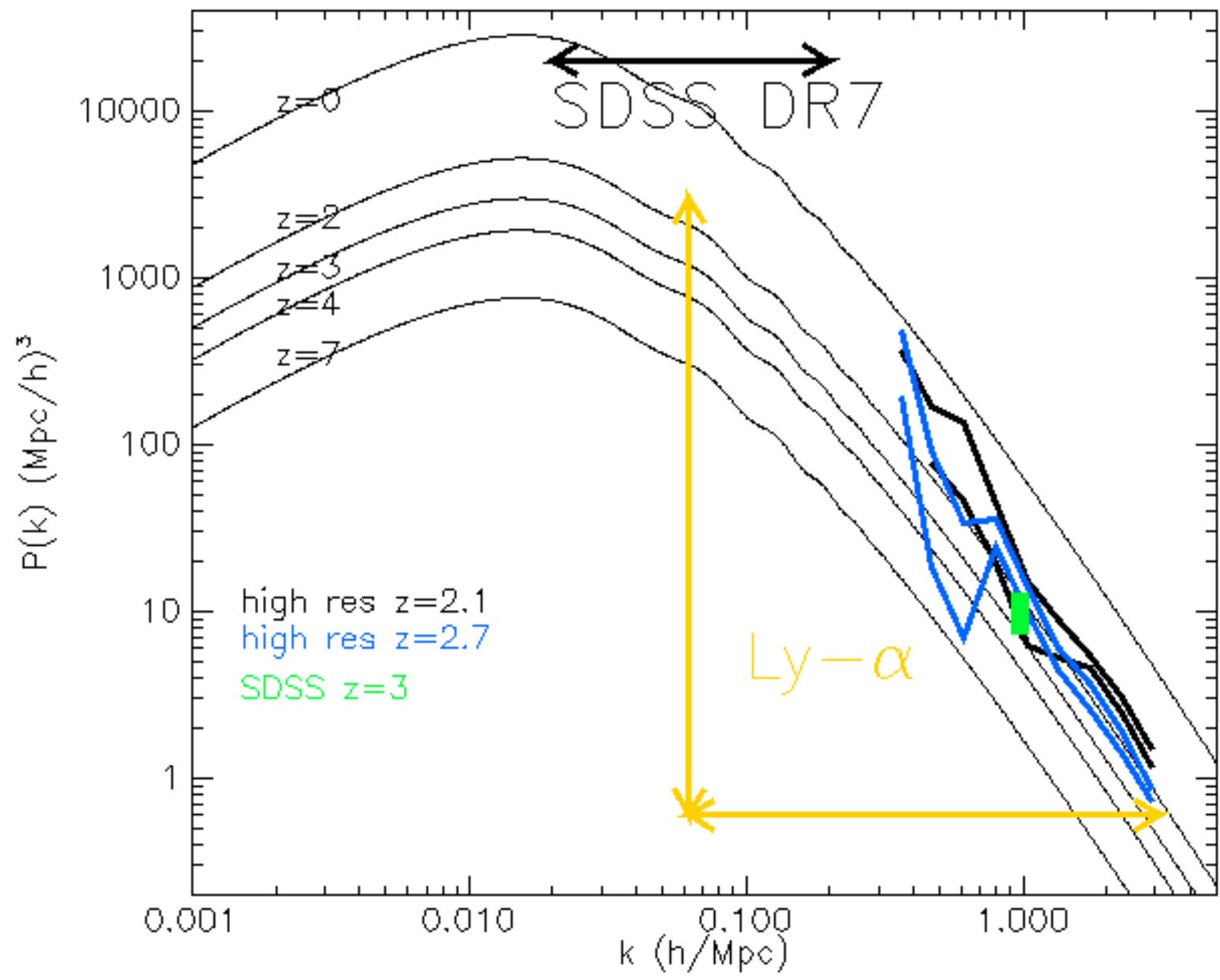
- N-body + Hydro simulations (Cen et al. 1994), semi analytical models (Bi et al., 1993).

COSMOLOGICAL  
PROBES









# Outline

- What data we got
- How we used them
- What we achieved

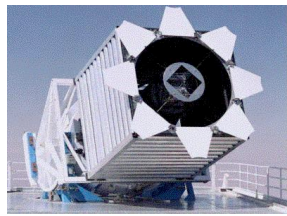
The data sets

Theoretical framework

Results

Why Lyman- $\alpha$  ? Small scales  
high redshift  
Most of the baryonic mass is in this form  
Quasars sample 75% of the age of the universe

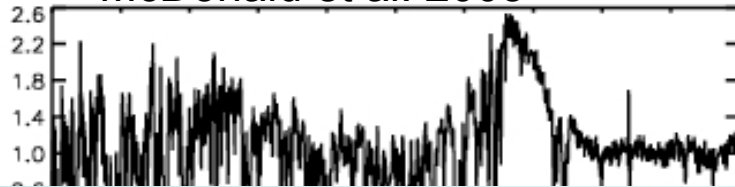
# The data sets



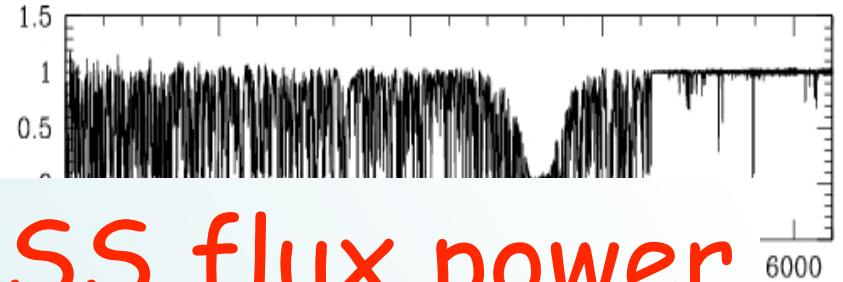
# SDSS vs LUQAS



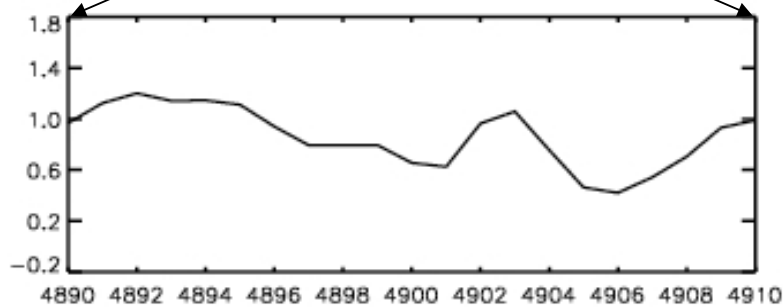
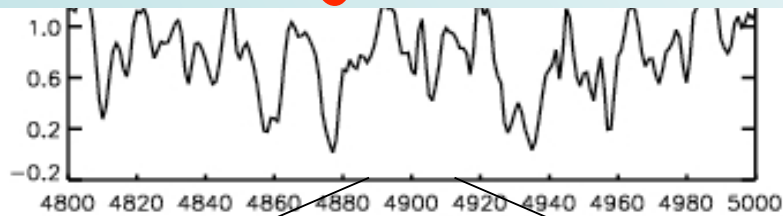
McDonald et al. 2005



Kim, MV et al. 2004

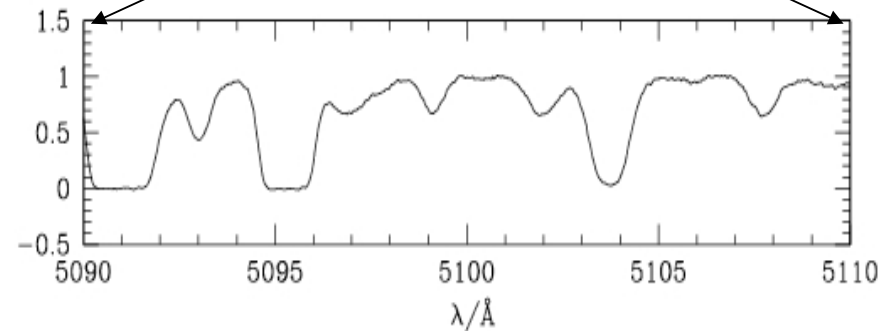
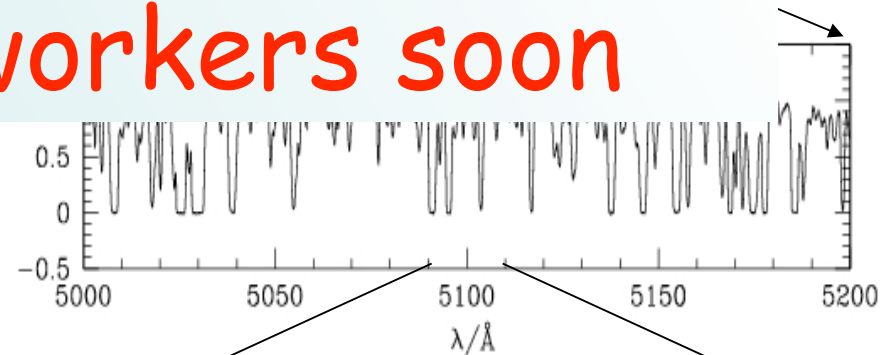


New Release of SDSS flux power  
Abazajian and co-workers soon



SDSS

3035 LOW RESOLUTION LOW S/N



LUQAS

30 HIGH RESOLUTION HIGH S/N

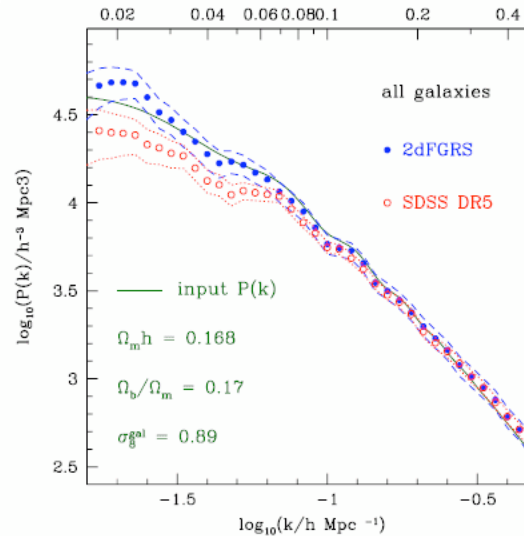
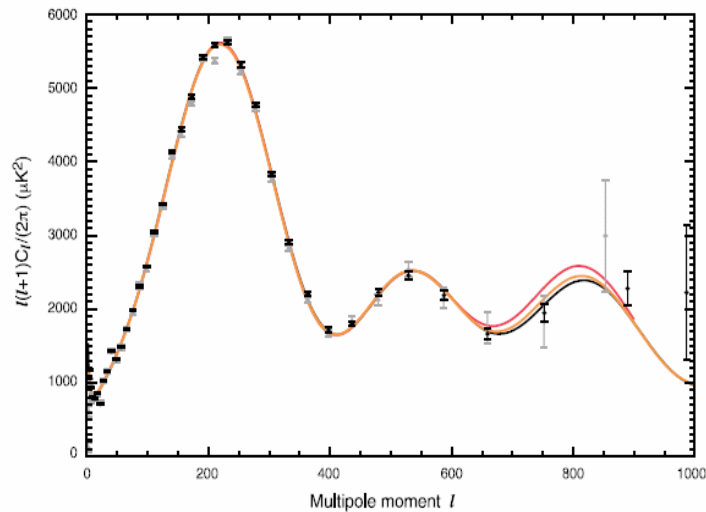
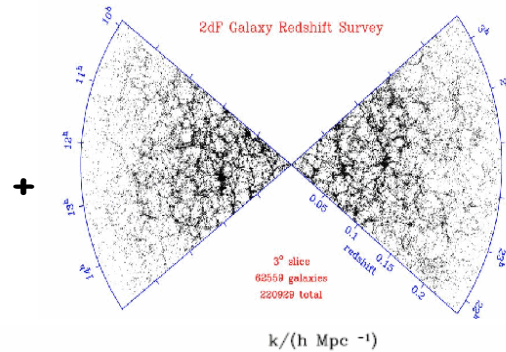
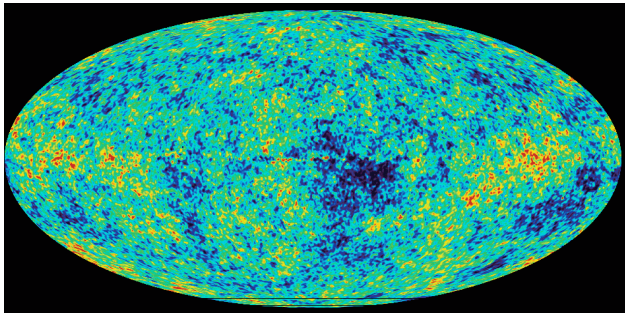
vs

# The interpretation: full grid of sims - I

SDSS power analysed by forward modelling motivated by the huge amount of data with small statistical errors

CMB: Spergel et al. (05)

Galaxy  $P(k)$ : Sanchez & Cole (07)



Cosmological parameters

+ e.g. bias

# The interpretation: full grid of sims - II

McDonald et al. 05

We vary 34 parameters, 3 of which are fixed for our primary result but varied for consistency checks. We give a summary before defining each in detail. In parentheses we give the actual number of parameters for each type:

Parameters  $\Delta_L^2(k_p, z_p)$ ,  $n_{\text{eff}}(k_p, z_p)$ , and  $\alpha_{\text{eff}}(k_p, z_p)$  (3).—Standard linear power spectrum amplitude, slope, and curvature on the scale of the Ly $\alpha$  forest, assuming a typical  $\Lambda$ CDM-like universe. Parameter  $\alpha_{\text{eff}}(k_p, z_p)$  is fixed to  $-0.23$  for the main result.

Parameters  $g'$  and  $s'$  (2).—Modifiers of the evolution of the amplitude and slope with redshift, to test for deviations from the expectation for  $\Lambda$ CDM. Fixed for main result.

Parameters  $\bar{F}(z_p)$  and  $\nu_F$  (2).—Mean transmitted flux normalization and redshift evolution.

Parameters  $T_{i=1 \dots 3}$  and  $\tilde{\gamma}_{i=1 \dots 3}$  (6).—Temperature-density relation parameters, including redshift evolution.

Parameter  $x_{\text{rei}}$  (1).—Degree of Jeans smoothing, related to the redshift and temperature of reionization.

Parameters  $f_{\text{Si III}}$  and  $\nu_{\text{Si III}}$  (2).—Normalization and redshift evolution of the Si III–Ly $\alpha$  cross-correlation term.

Parameters  $\epsilon_{n,i=1 \dots 11}$  (11).—Freedom in the noise amplitude in the data in each SDSS redshift bin.

Parameter  $\alpha_R$  (1).—Freedom in the resolution for the SDSS data.

Parameter  $A_{\text{damp}}$  (1).—Normalization of the power contributed by high-density systems.

Parameters  $a_{\text{NOSN}}$  and  $a_{\text{NOMETAL}}$  (2).—Admixture of corrections from the NOSN and NOMETAL hydrodynamic simulations.

Parameters  $A_{\text{UV}}$  and  $\nu_{\text{UV}}$  (2).—Normalization and redshift evolution of the correction for fluctuations in the ionizing background.

Parameter  $x_{\text{extrap}}$  (1).—Freedom in the extrapolation of our small simulation results to low  $k$ .

Tens of thousands of models  
Monte Carlo Markov Chains

- Cosmology

- Cosmology

- Mean flux

-  $T = T_0 (1 + \delta)^{\gamma - 1}$

- Reionization

- Metals

- Noise

- Resolution

- Damped Systems

- Physics

- UV background

- Small scales

# The interpretation: flux derivatives - III

Independent analysis of SDSS power

The flux power spectrum is a smooth function of  $k$  and  $z$

Flux power

$$P_F(k, z; \mathbf{p}) = \underbrace{P_F(k, z; \mathbf{p}^0)}_{\text{Best fit}} + \sum_{i=1, N} \left. \frac{\partial P_F(k, z; p_i)}{\partial p_i} \right|_{\mathbf{p} = \mathbf{p}^0} (p_i - p_i^0)$$

$\mathbf{p}$ : astrophysical and cosmological parameters

but even resolution and/or box size effects if you want to save CPU time

# RESULTS

POWER SPECTRUM AND NEUTRINOS



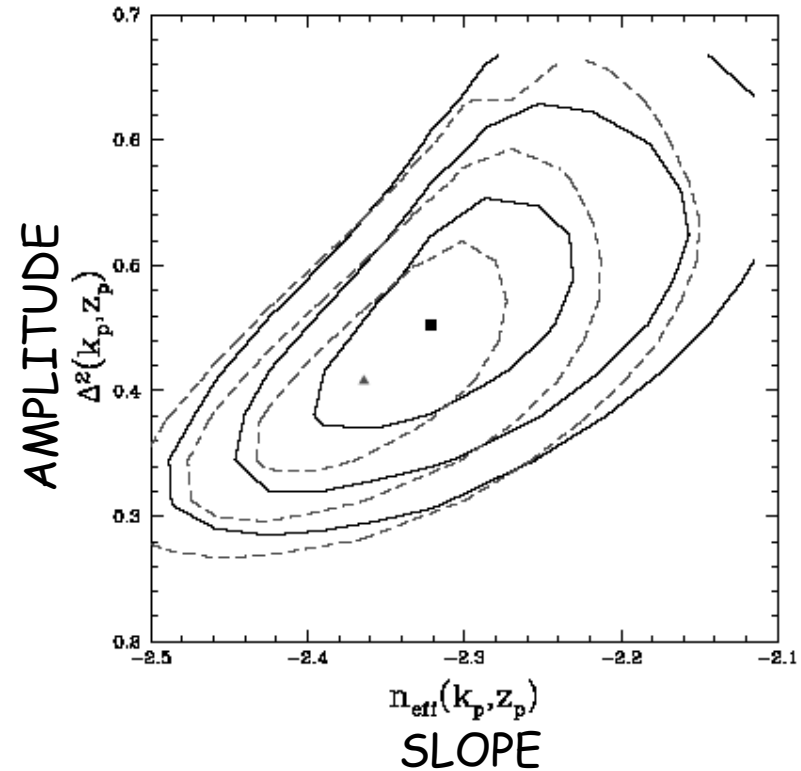
## Results Lyman- $\alpha$ only with full grid: amplitude and slope

$$\Delta_L^2(k, z) \simeq \left[ \frac{D(z)}{D(z_p)} \right]^2 \Delta_L^2(k_p, z_p) \times \left[ \frac{k}{k_*(z)} \right]^{3+n_{\text{eff}}(k_p, z_p) + (1/2)\alpha_{\text{eff}}(k_p, z_p) \ln[k/k_*(z)]}$$

$\chi^2$  likelihood code distributed with *COSMOMC*

McDonald et al. 05

Croft et al. 98,02	40% uncertainty
Croft et al. 02	28% uncertainty
Viel et al. 04	29% uncertainty
McDonald et al. 05	14% uncertainty

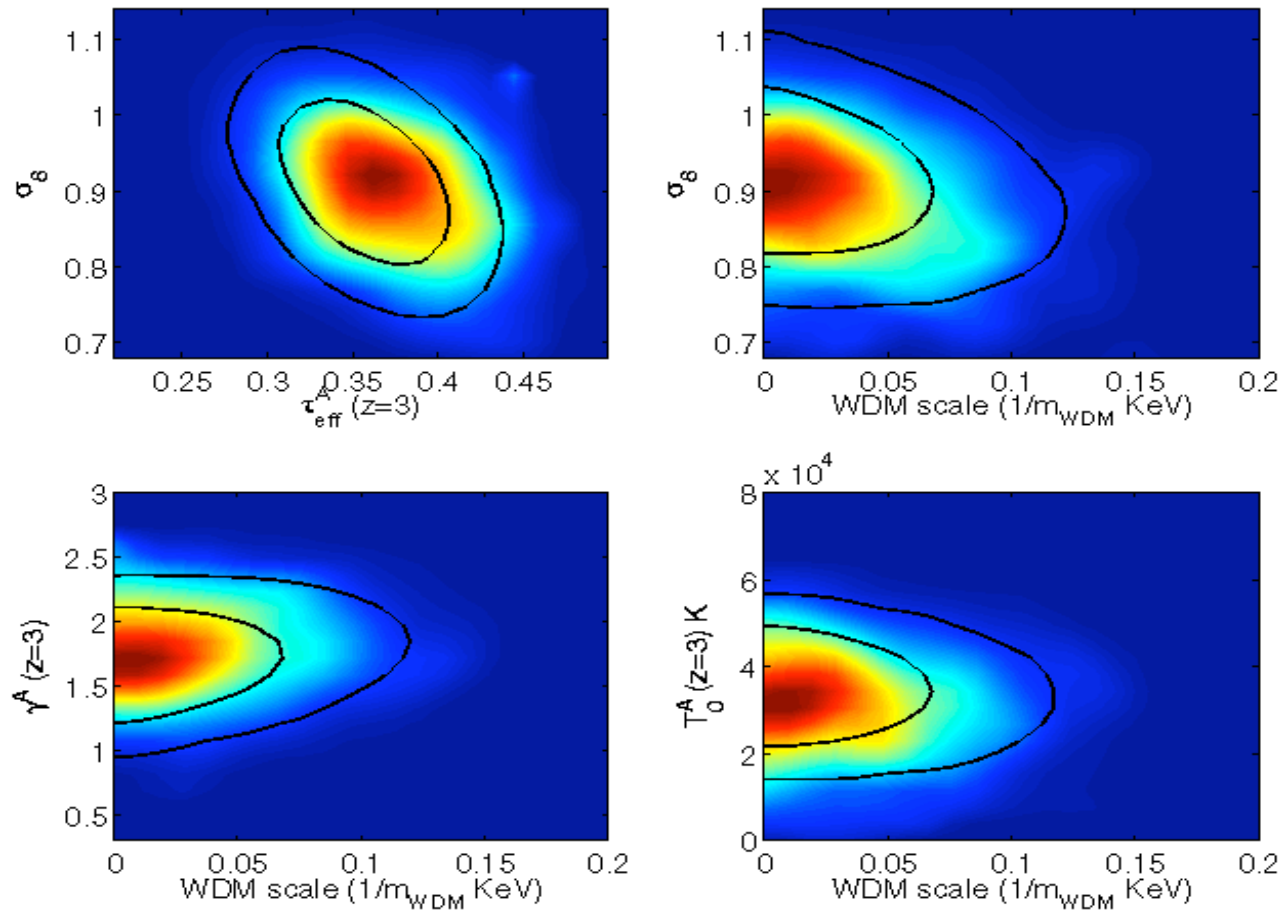


Redshift  $z=3$  and  $k=0.009$  s/km corresponding to 7 comoving Mpc/h

# Results Lyman- $\alpha$ only with flux derivatives: correlations

Fitting SDSS data with  
GADGET-2  
this is SDSS Ly- $\alpha$   
only !!

FLUX DERIVATIVES



SDSS data only

$$\sigma_8 = 0.91 \pm 0.07$$
$$n = 0.97 \pm 0.04$$

# Summary (highlights) of results

1. Competitive constraints in terms of cosmological parameters (in particular shape and curvature of the power spectrum)

Lesgourgues, MV, Haehnelt, Massey (2007) JCAP 11 008

2. Tightest constraints to date on neutrino masses and running of the spectral index

Seljak, Slosar, McDonald JCAP (2006) 10 014

3. Tightest constraints to date on the coldness of cold dark matter

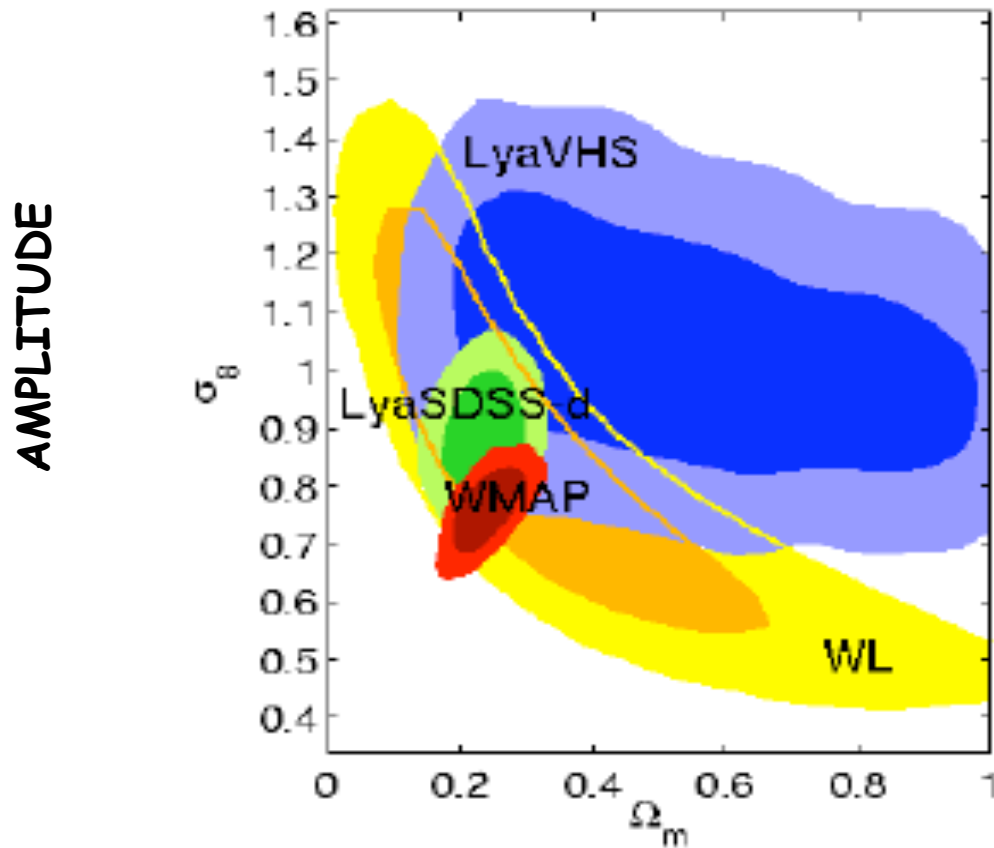
MV et al., Phys.Rev.Lett. 100 (2008) 041304

# Lyman- $\alpha$ forest + Weak Lensing + WMAP 3yrs

VHS-LUQAS: high res Ly- $\alpha$  from (Viel, Haehnelt, Springel 2004)

SDSS-d: re-analysis of low res data SDSS (Viel & Haehnelt 2006)

WL: COSMOS-3D survey Weak Lensing (Massey et al. 2007) 1.64 sq degree  
public available weak lensing COSMOMC module



**MATTER DENSITY**

**SPECTRAL INDEX**

# Lyman- $\alpha$ forest + Weak Lensing + WMAP 3yrs

Lesgourgues, MV, Haehnelt, Massey, 2007, JCAP, 8, 11

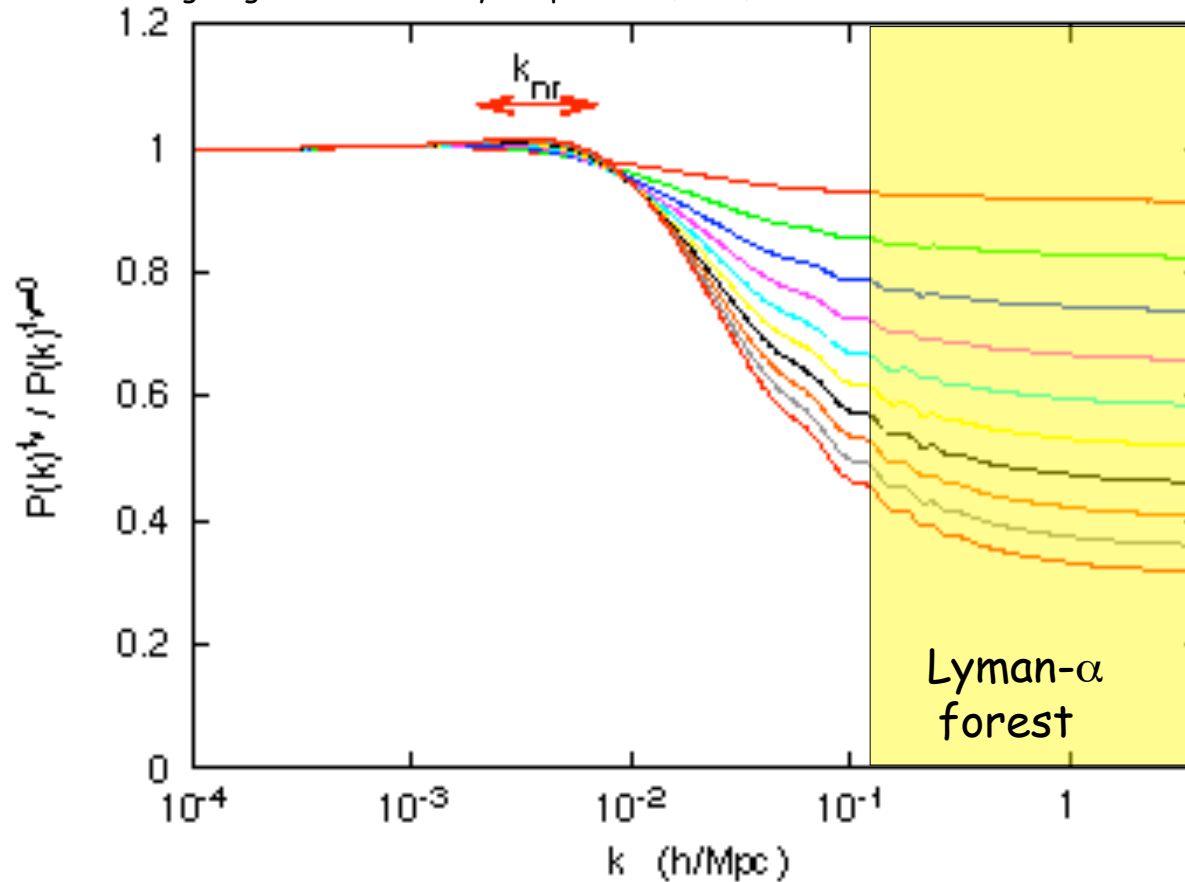
	WL+WMAP3+Ly $\alpha$ VHS	WL+WMAP3+Ly $\alpha$ SDSS-d
$\sigma_8$	$0.822 \pm 0.032$	$0.800 \pm 0.023$
$n_s$	$0.960 \pm 0.016$	$0.971 \pm 0.011$
$\Omega_{0m}$	$0.282 \pm 0.026$	$0.247 \pm 0.016$
$h$	$0.700 \pm 0.022$	$0.730 \pm 0.016$
$\tau$	$0.094 \pm 0.028$	$0.109 \pm 0.026$

$|dn/d\ln k| < 0.021$

# Active neutrinos - I

$$k_{nr} \simeq 0.018 \Omega_m^{1/2} \left( \frac{m}{1 \text{ eV}} \right)^{1/2} h \text{ Mpc}^{-1}$$

Lesgourgues & Pastor Phys.Rept. 2006, 429, 307



$$\Sigma m_\nu = 0.138 \text{ eV}$$

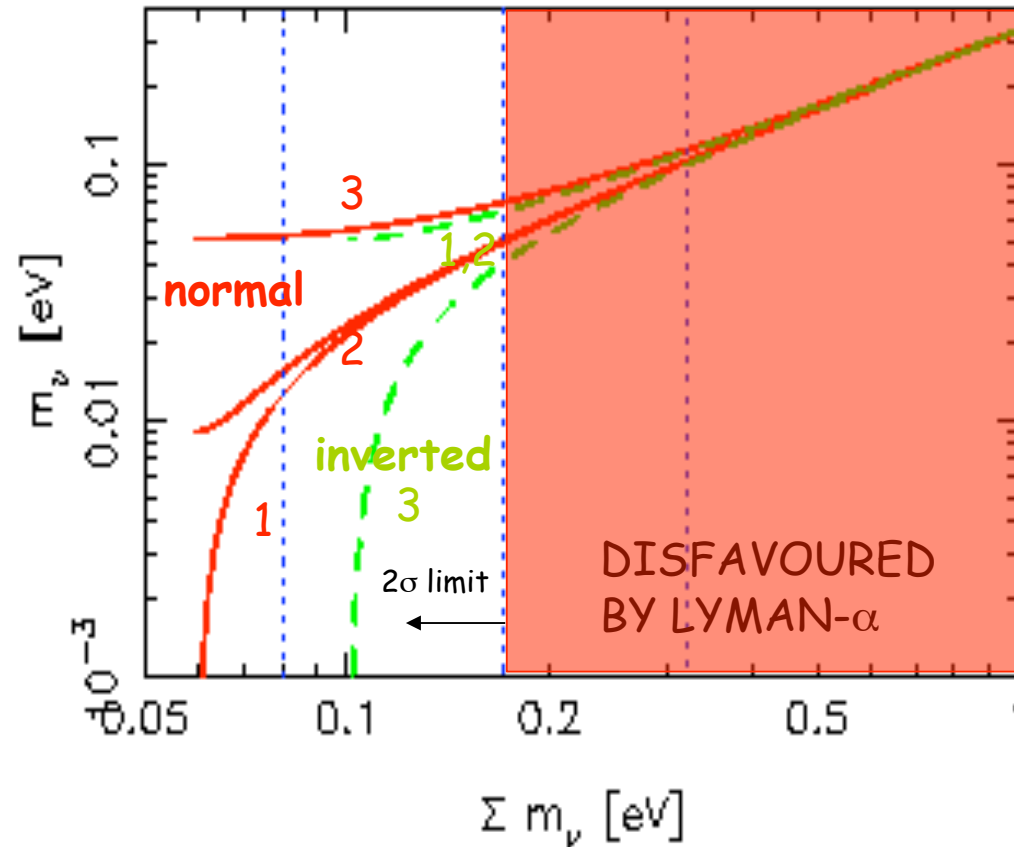
$$\Sigma m_\nu = 1.38 \text{ eV}$$

$$v_{th} \equiv \frac{\langle p \rangle}{m} \simeq \frac{3T_\nu}{m} = \frac{3T_\nu^0}{m} \left( \frac{a_0}{a} \right) \simeq 150(1+z) \left( \frac{1 \text{ eV}}{m} \right) \text{ km s}^{-1}$$

$$k_{FS}(t) = \left( \frac{4\pi G \bar{\rho}(t) a^2(t)}{v_{th}^2(t)} \right)^{1/2}, \quad \lambda_{FS}(t) = 2\pi \frac{a(t)}{k_{FS}(t)} = 2\pi \sqrt{\frac{2}{3}} \frac{v_{th}(t)}{H(t)}$$

# Active neutrinos - II

Seljak, Slosar, McDonald, 2006, JCAP, 0610, 014



Tight constraints because data are marginally compatible

$\Sigma m_\nu$  (eV) < 0.17 (95 %C.L.), < **0.19 eV** (Fogli et al. 08)  
 $r$  < 0.22 (95 % C.L.)  
 running =  $-0.015 \pm 0.012$   
 $N_{\text{eff}} = 5.2$  (3.2 without Ly  $\alpha$ )  
**CMB + SN + SDSS gal+ SDSS Ly- $\alpha$**

Goobar et al. 06 get upper limits 2-3 times larger.....  
 for forecasting see Gratton, Lewis, Efstathiou 2007

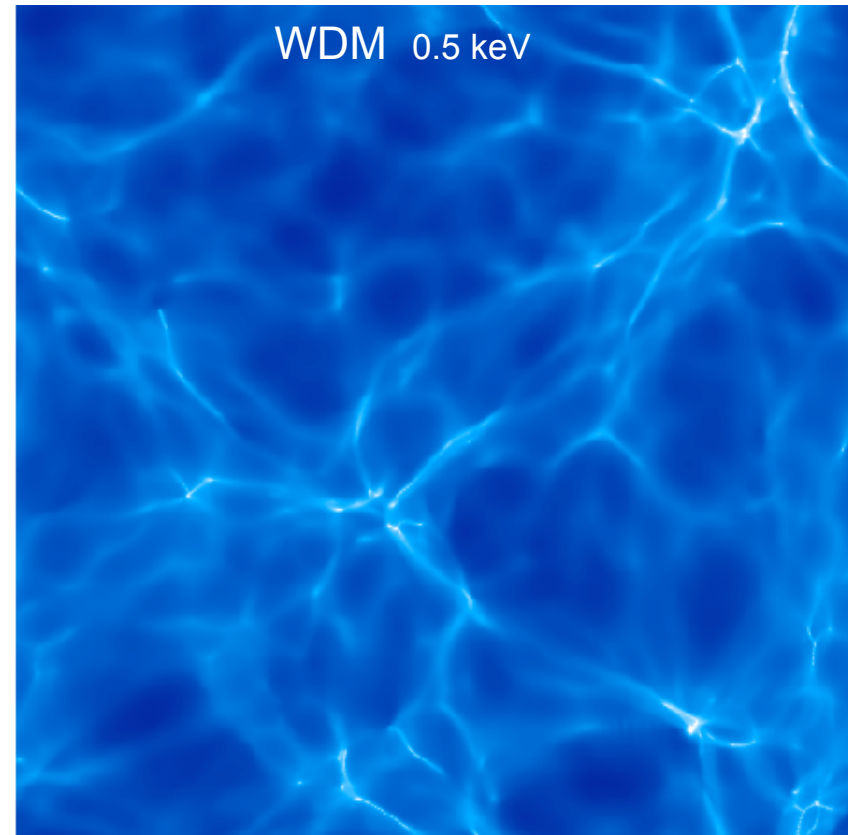
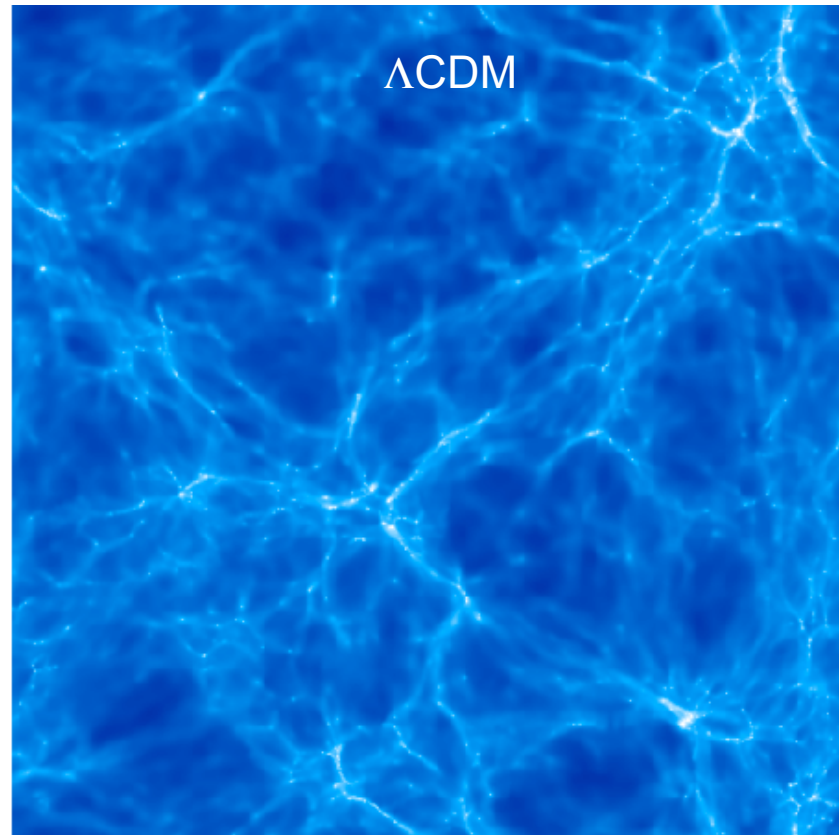
# RESULTS

## WARM DARK MATTER

Or if you prefer.. How cold is cold dark matter?



# Lyman- $\alpha$ and Warm Dark Matter - I



30 comoving Mpc/h  $z=3$

In general

$$k_{FS} \sim 5 \left( T_V/T_X \right) (m_X/1\text{keV}) \text{ Mpc}^{-1}$$

A blue circle is drawn around the term  $(T_V/T_X)$  in the equation, with a blue arrow pointing from it down towards the text below.

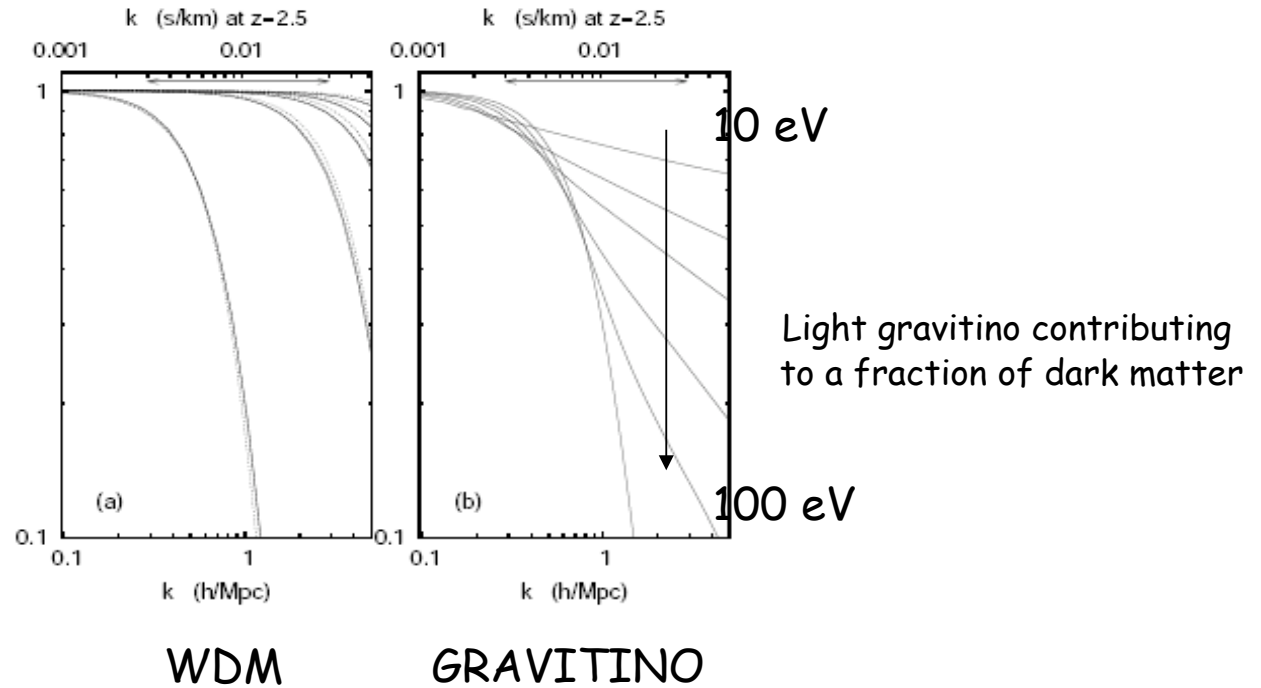
Set by relativistic degrees of freedom at decoupling

See Colombi, Dodelson, Widrow, 1996  
Colin, Avila-Reese, Valenzuela 2000  
Bode, Ostriker, Turok 2001  
Abazajian, Fuller, Patel 2001  
Abazajian 2006  
Abazajian & Koushiappas 2006  
Wang & White 2007  
Colin, Avila-Reese, Valenzuela 2008

# Lyman- $\alpha$ and Warm Dark Matter - II

$$[P(k)_{\text{WDM}}/P(k)_{\text{CDM}}]^{1/2}$$

$$\frac{T_x}{T_\nu} = \frac{10.75^{1/3}}{g(T_D)^{1/3}}$$



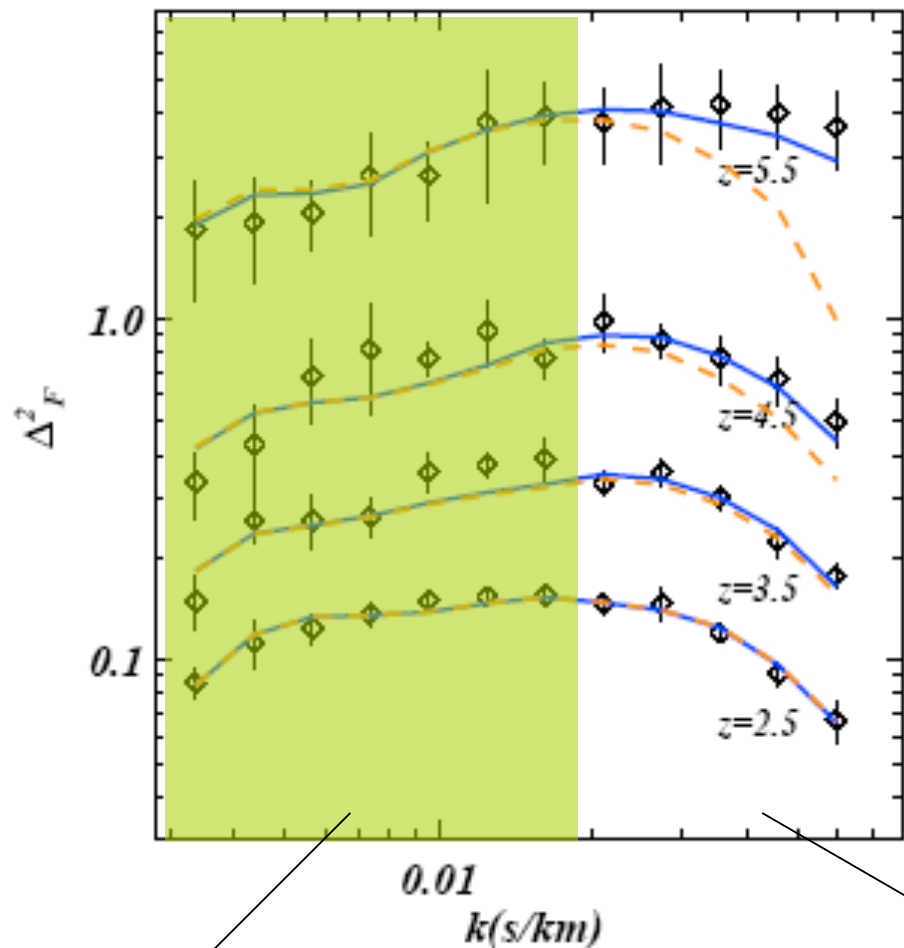
$m_{\text{gravitino}} < 16 \text{ eV}$  ( $2 \sigma$  C.L.)  
 (or any particle with  
 $g(T_D) \sim 90-100$ )  
 From high res. Lyman- $\alpha$  data

If the gravitino is the LSP then the susy breaking scale is limited from above

$$\Lambda_{\text{susy}} < 260 \text{ TeV}$$

# Lyman- $\alpha$ and Warm Dark Matter - III

MV et al., Phys.Rev.Lett. 100 (2008) 041304



SDSS + HIRES data

(SDSS still very constraining!)

Tightest constraints on mass of  
WDM particles to date:

$m_{\text{WDM}} > 4 \text{ keV}$  (early decoupled  
thermal relics)

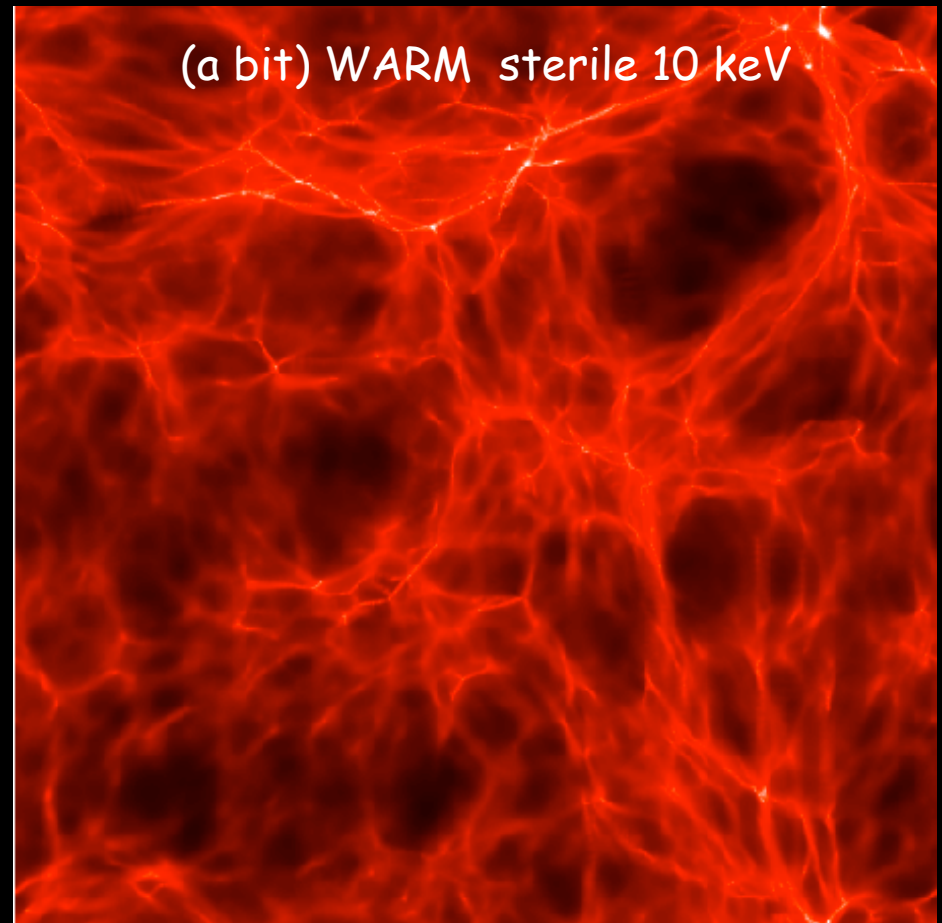
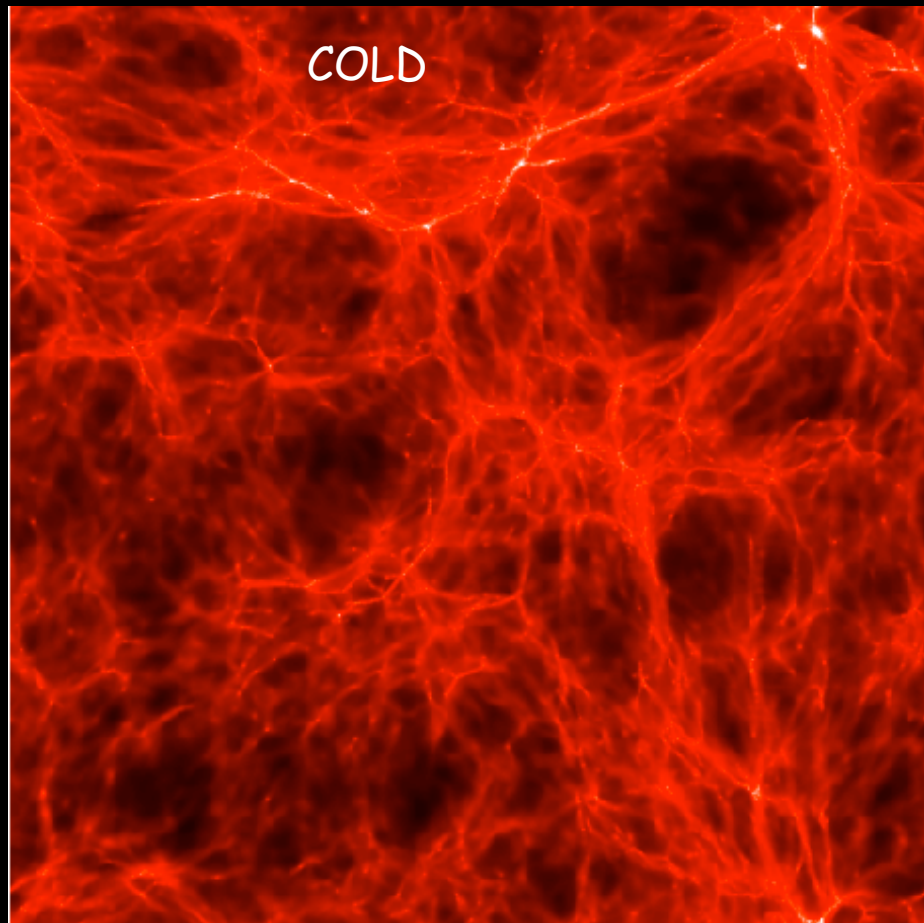
$m_{\text{sterile}} > 28 \text{ keV}$  (standard Dodelson-  
Widrow mechanism)

SDSS range

Completely new small scale regime

Little room for standard warm dark matter scenarios.....

... the cosmic web is likely to be quite "cold"



# RESULTS

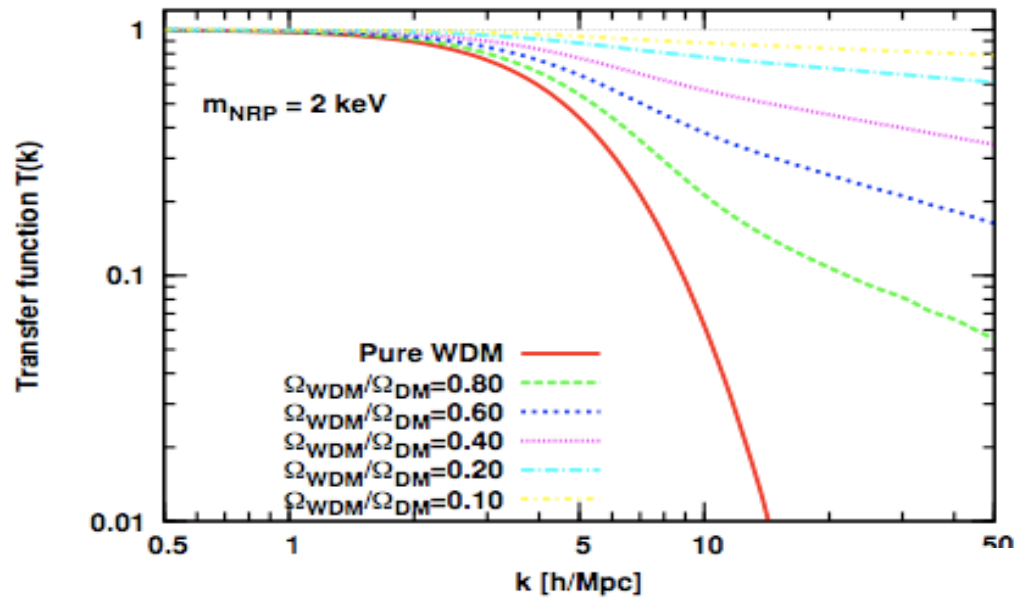
## NEW WARM DARK MATTER MODEL

**(sterile neutrino)**

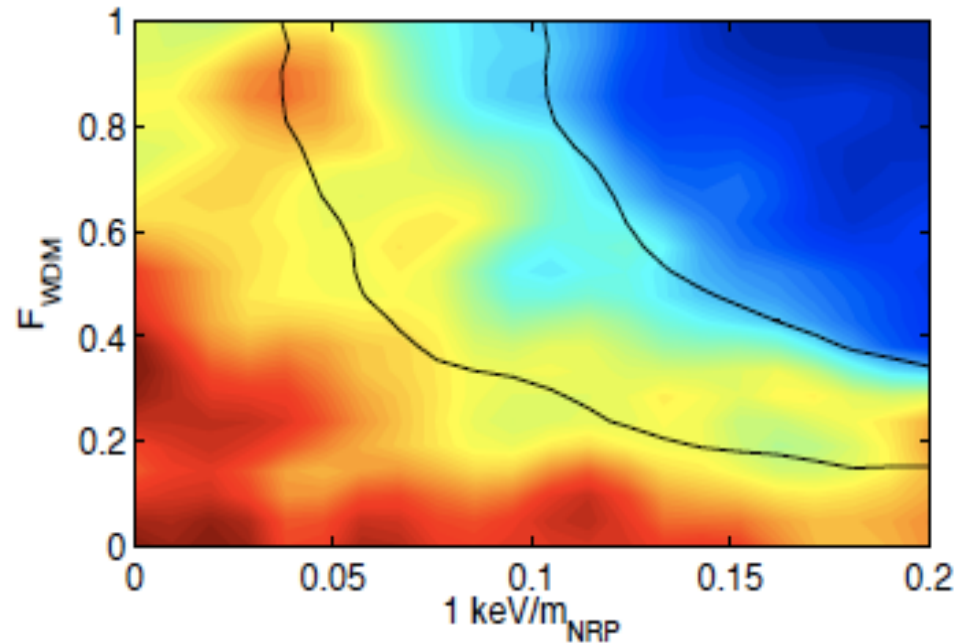
Mixed Cold and Warm models: Boyarsky, Lesgourgues, Ruchayskiy,  
Viel, 2009, JCAP, 05, 012

Shi & Fuller 1999 model:  
Boyarsky, Lesgourgues, Ruchayskiy, Viel, 2009, Phys.Rev.Lett, 102, 201304

# Lyman- $\alpha$ and Cold+Warm Dark Matter - I

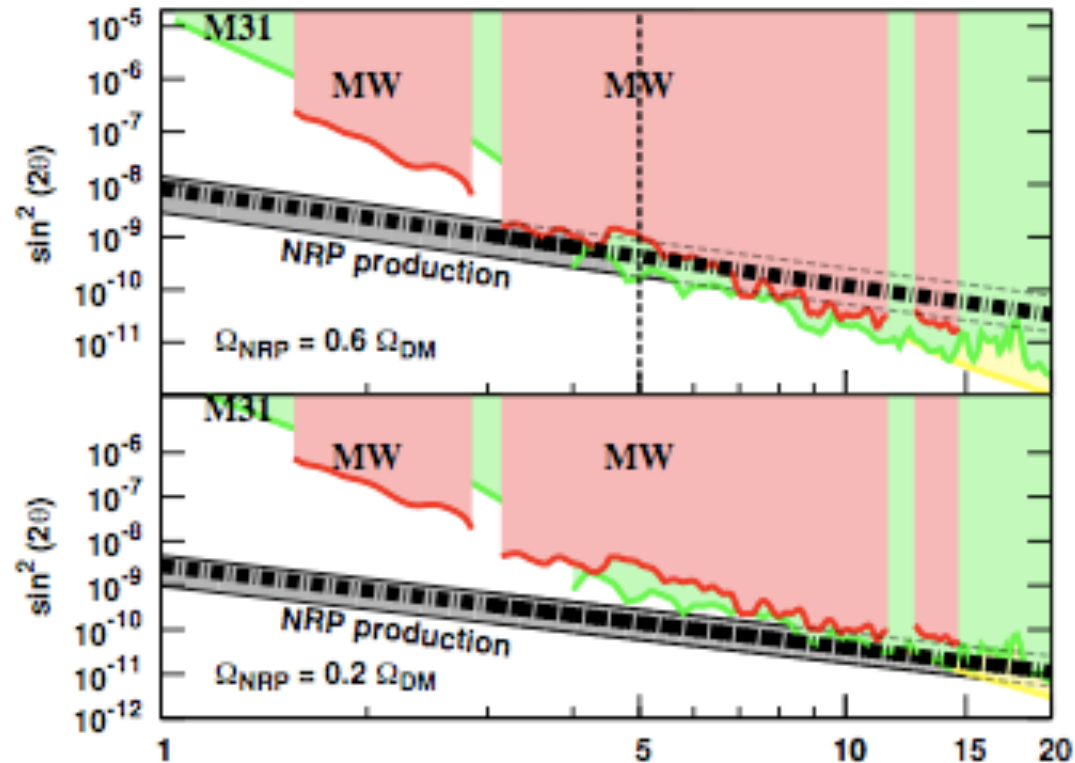


SDSS+WMAP5



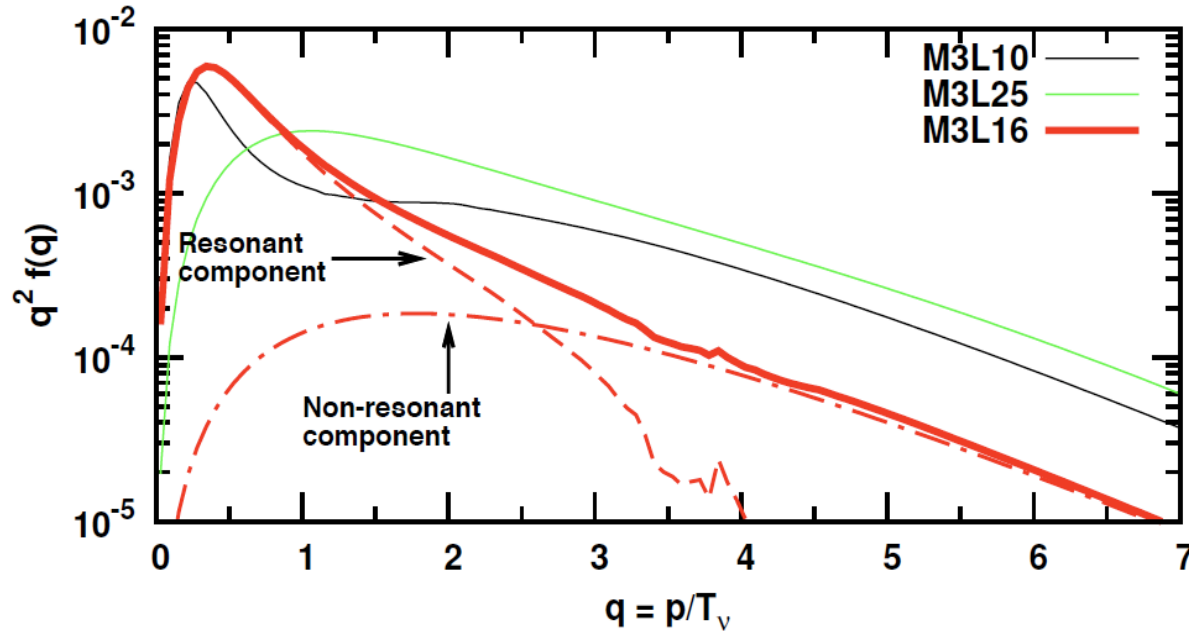
# Lyman- $\alpha$ and Cold+Warm Dark Matter - II

$$\text{X-ray flux} \sim \theta^2 M_{\text{sterile}}^5$$

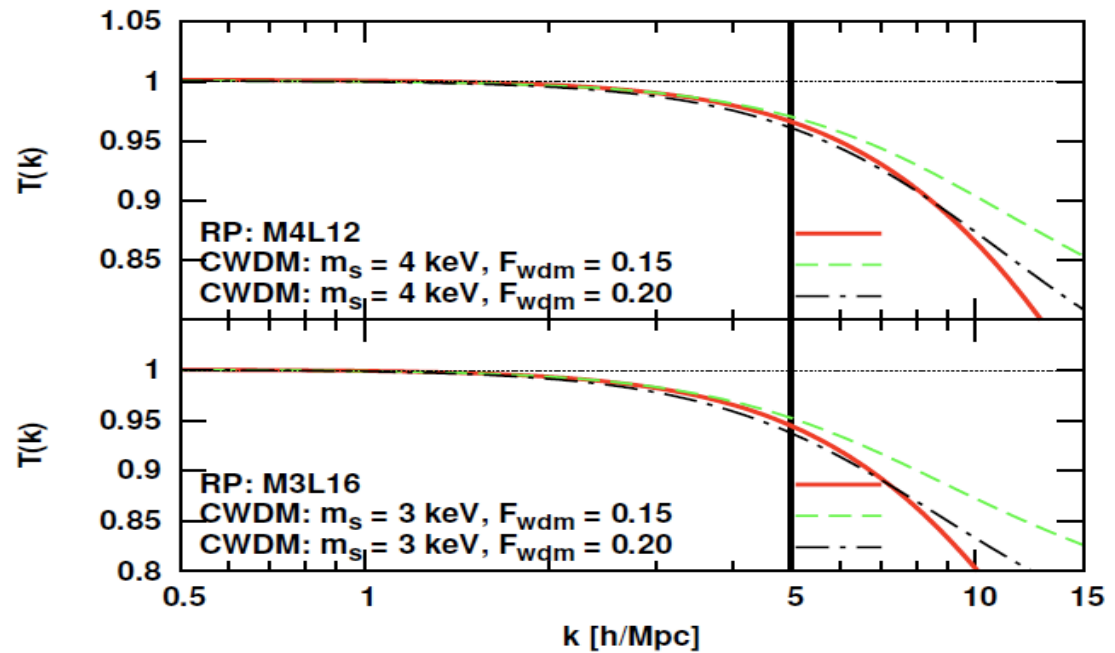


For  $m > 5$  keV any fraction of WDM  $< 0.6$  is allowed - frequentist analysis 99.7% C.L.  
For  $m > 5$  keV any fraction of WDM  $< 0.35$  is allowed - bayesian analysis 95% C.L.

# Lyman- $\alpha$ and resonantly produced sterile neutrinos - I

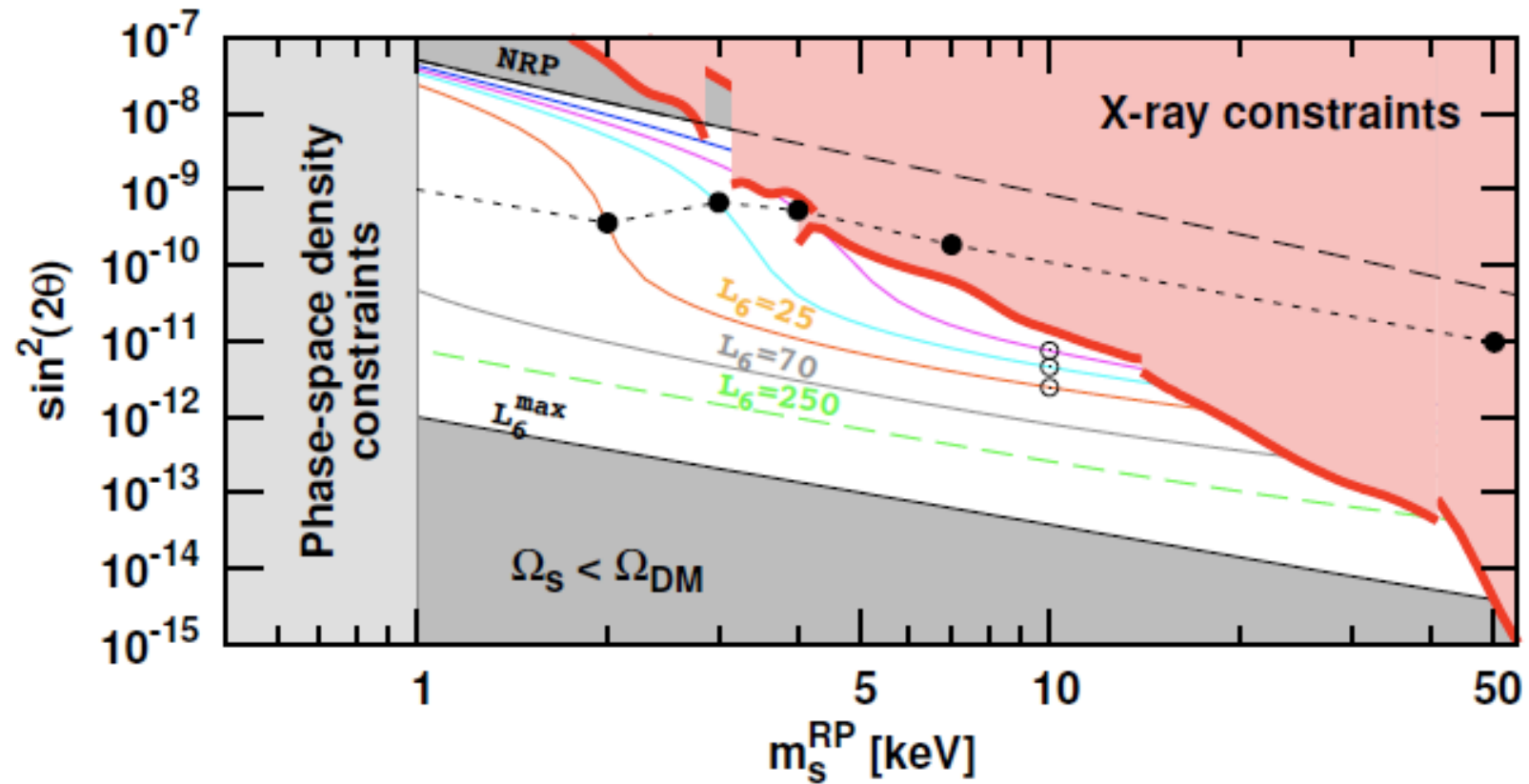


$L = 10^6 (n_{\nu_e} - n_{\bar{\nu}_e})/s$   
 Mass sterile = 3 keV



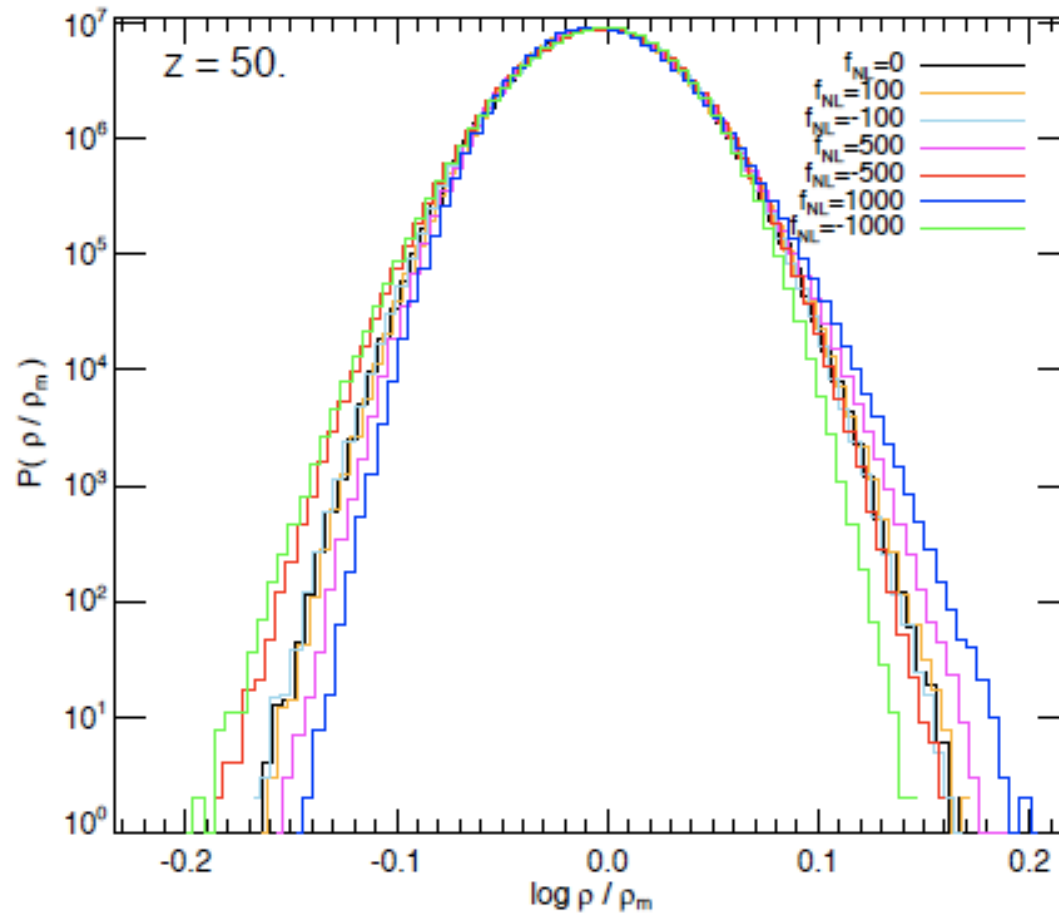


# Lyman- $\alpha$ and resonantly produced sterile neutrinos - II



# **PRIMORDIAL Non Gaussianities in the IGM**

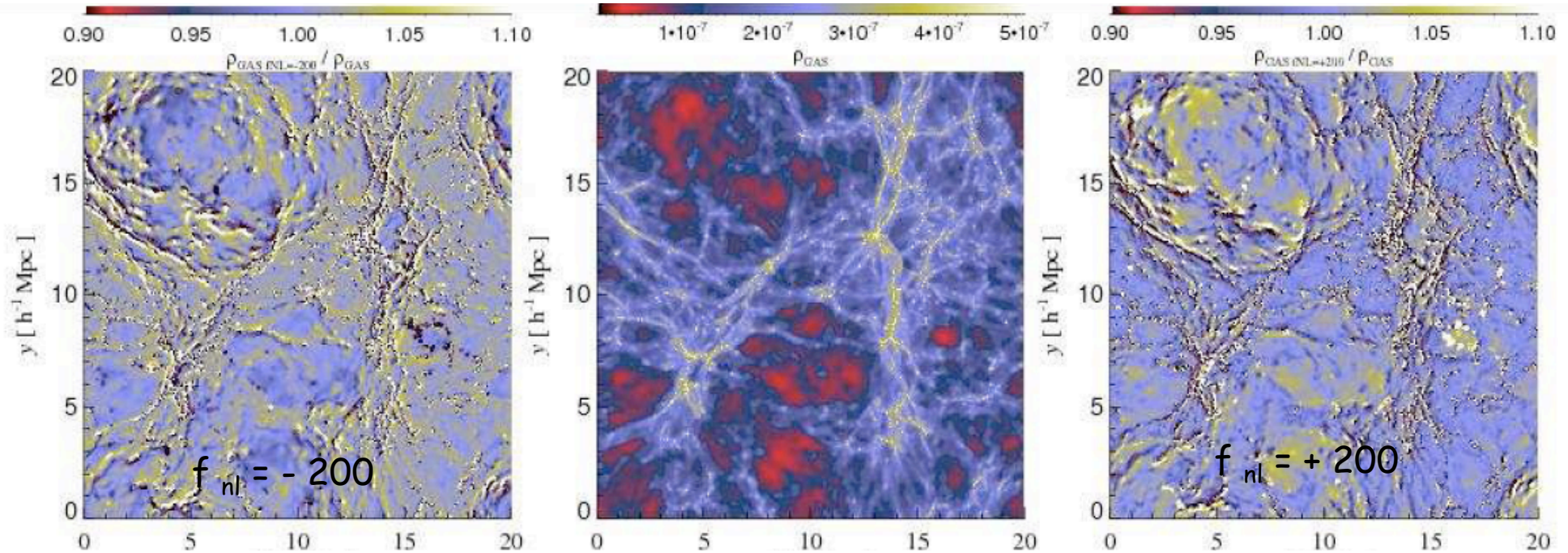
# N-body simulation in NG scenario: the mass distribution



$$\Phi_{NL} = f_{NL} (\Phi_L^2 - \langle \Phi_L^2 \rangle)$$

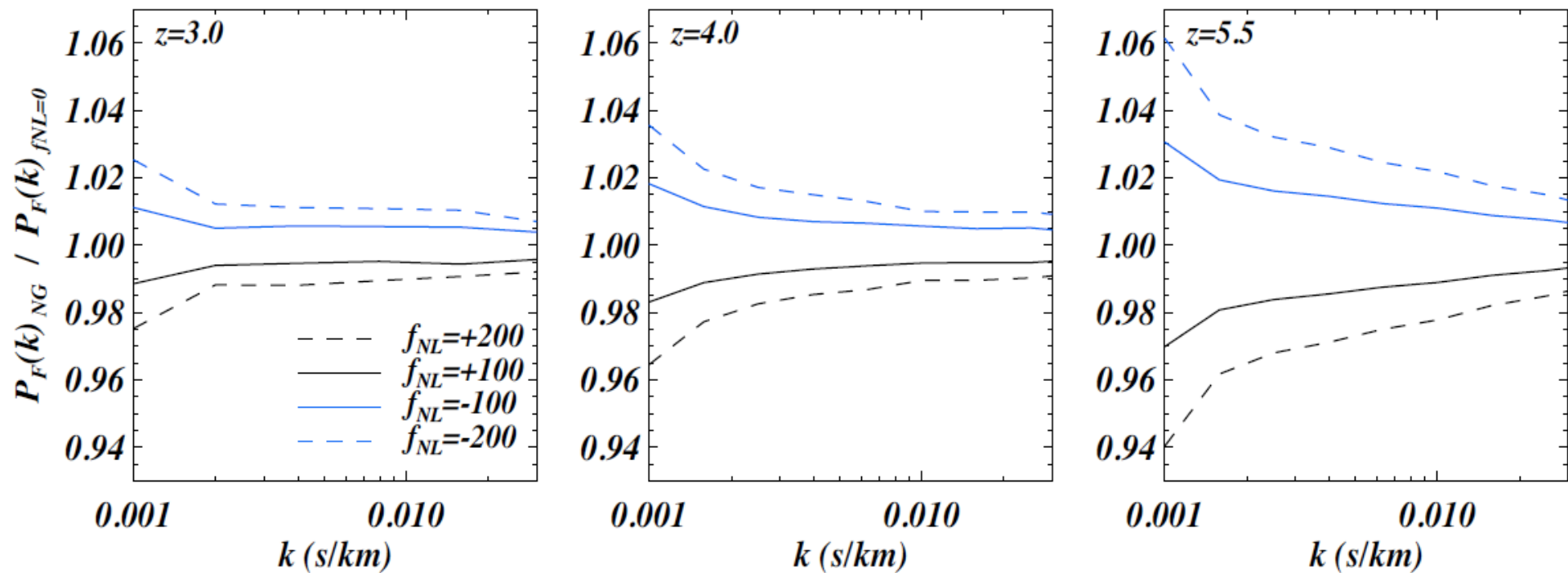
Mathis et al. 04  
Kang et al. 07  
Grossi et al. 07,09  
Hikage et al. 08  
Desjacques et al. 08

# First hydrodynamical simulation in NG scenario



# First hydrodynamical simulation in NG scenario: flux bispectrum

Local squeezed configuration  $k_1 \ll k_2 \sim k_3$



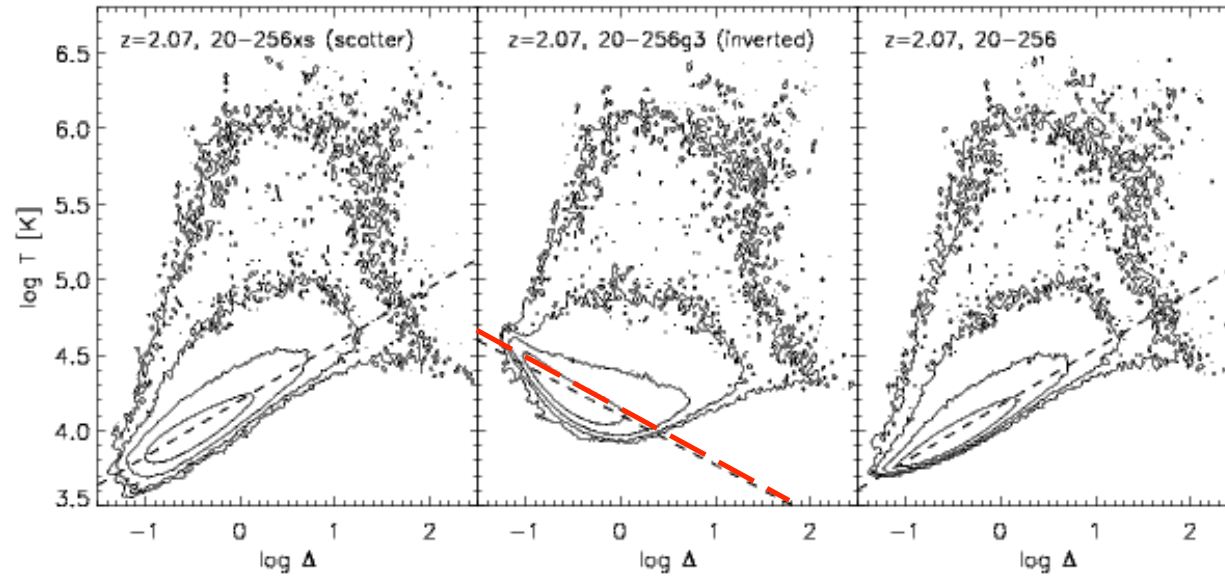
**SYSTEMATICS**

# Fitting the flux probability distribution function

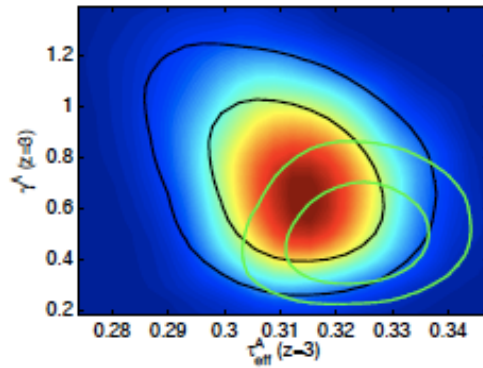
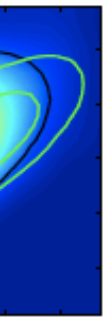
Bolton, MV, Kim, Haehnelt, Carswell (08)

$$T = T_0(1 + \delta)^{\gamma - 1}$$

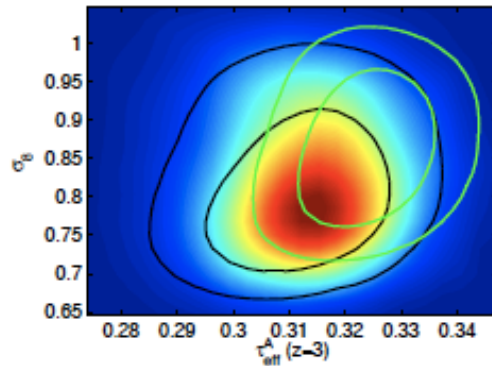
Inverted  
equation of state  
 $\gamma < 1$  means voids are  
hotter than mean  
density regions



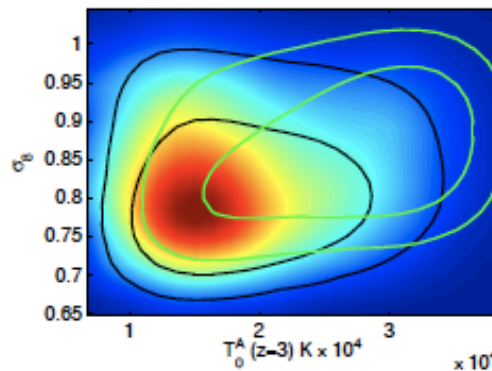
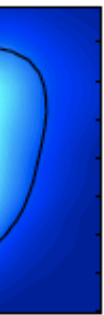
# Fitting the flux probability distribution function-II



1) Fitting all flux statistics at once (see Desjacques & Nusser 07) will make clear at which level we are affected by systematics



2) However, already from the flux PDF (one point statistics) there are very interesting constraints on thermal state of the IGM and on some cosmological parameters



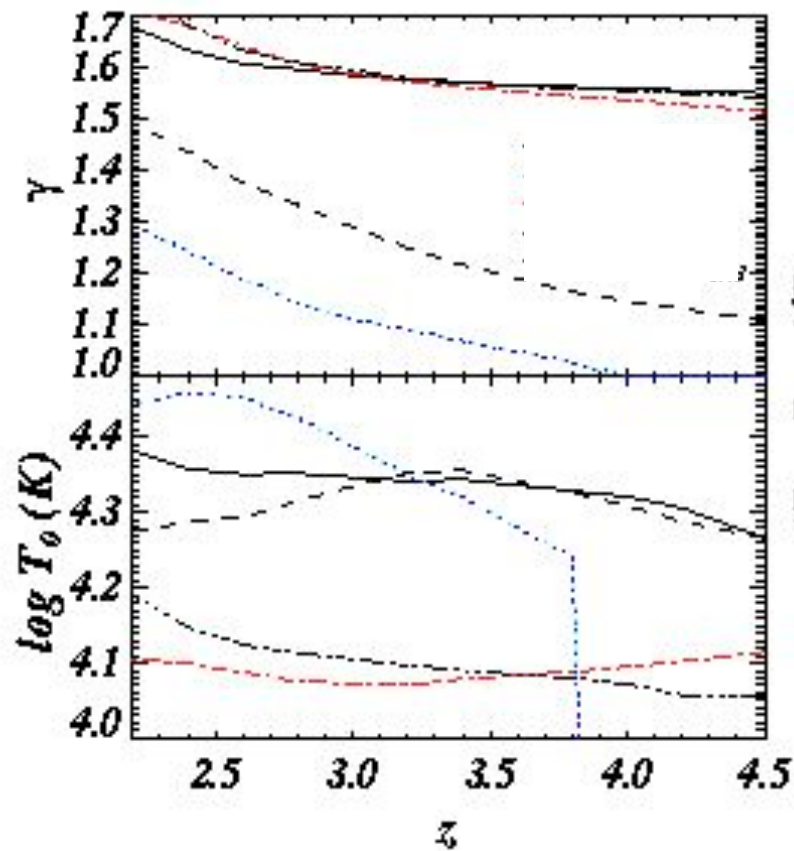
3) Flux power prefers a higher temp. than the flux pdf alone: joint constraints reasonable and still prefers a high  $\sigma_8$  than the CMB alone



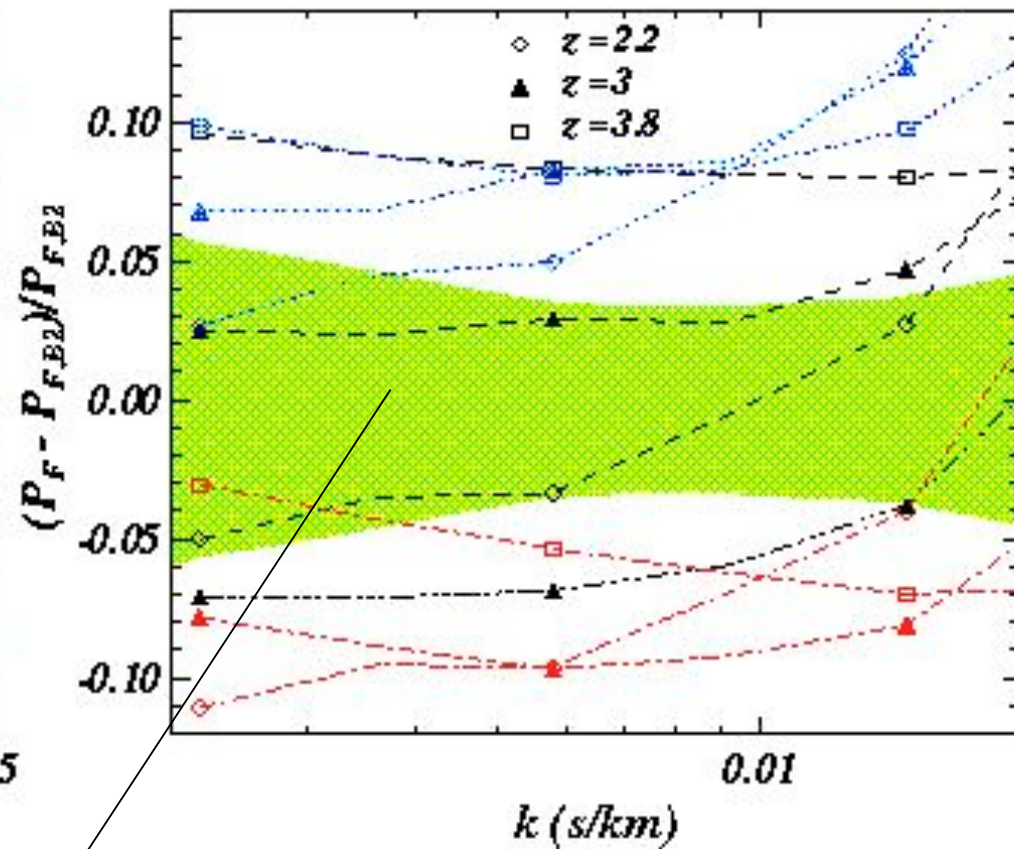
# Systematics: Thermal state

$$T = T_0 (1 + \delta)^{\gamma-1}$$

Thermal histories



Flux power fractional differences

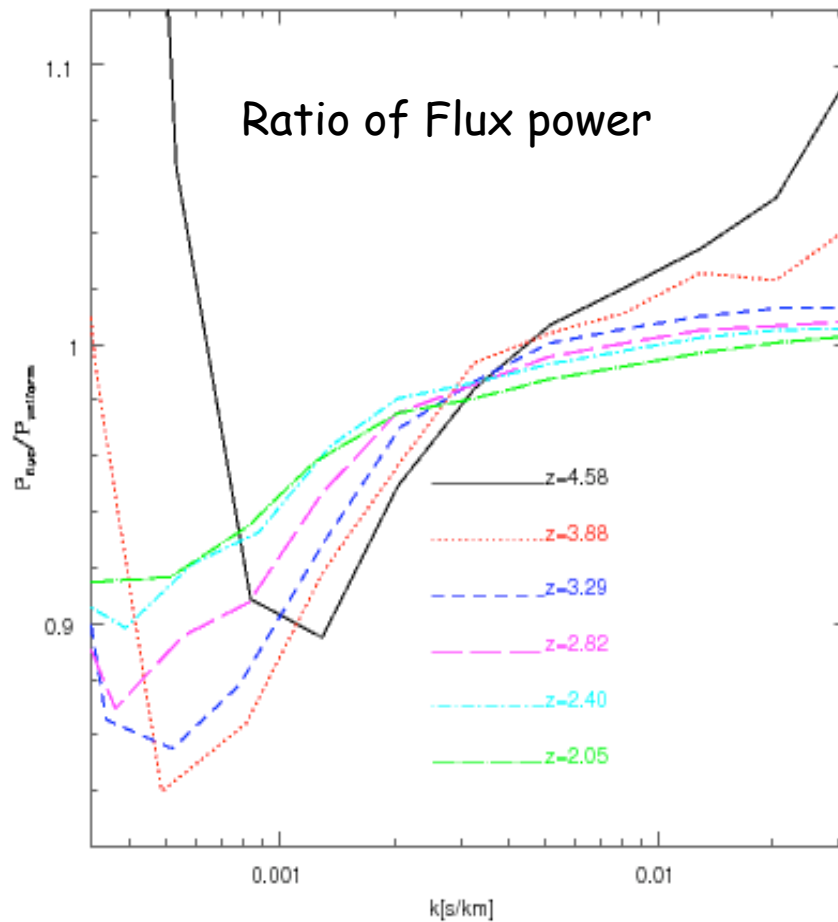


Statistical SDSS errors on flux power

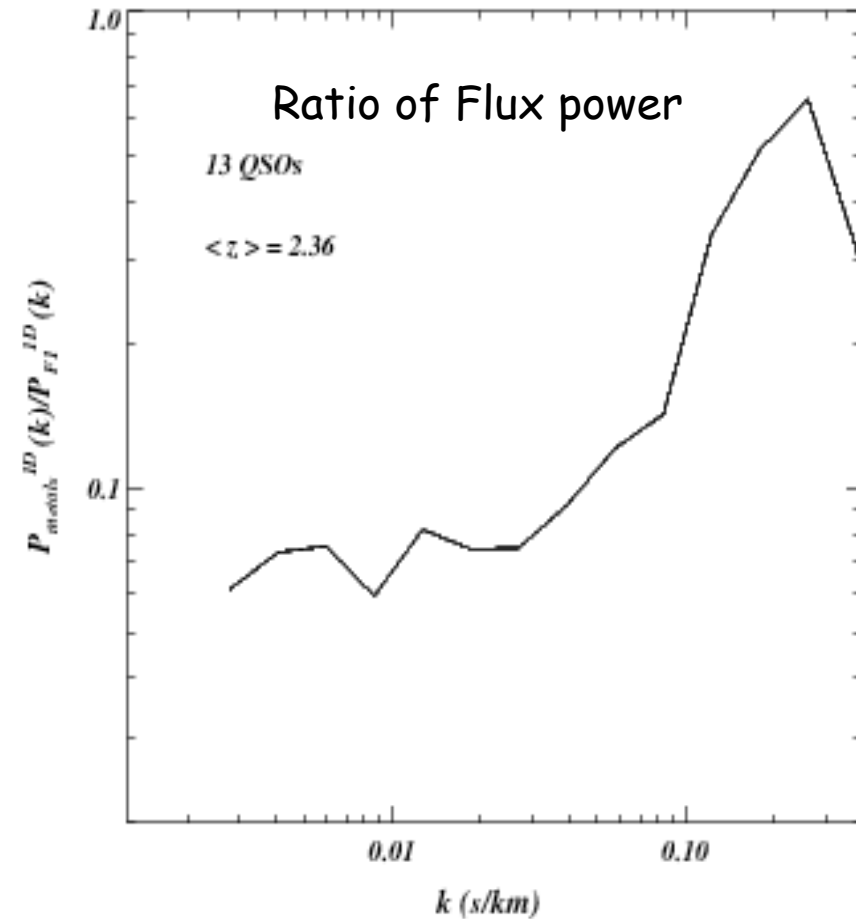
# Systematics: UV fluctuations and Metals

UV fluctuations from Lyman Break Galaxies

Metal contribution



McDonald, Seljak, Cen, Ostriker 2004  
Croft 2006  
Lidz et al. 2007



Kim, MV, Haehnelt, Carswell, Cristiani (2004)

**FUTURE**

# Future perspectives

BOSS (or SUPERBOSS) - SDSS III

150,000 (1,000,000) QSO spectra → tailored for BAO and  $P(k)$  studies

X-Shooter (taking data now) spectrograph

Medium resolution between SDSS and high res → at least 100 QSO spectra needed to improve constraints

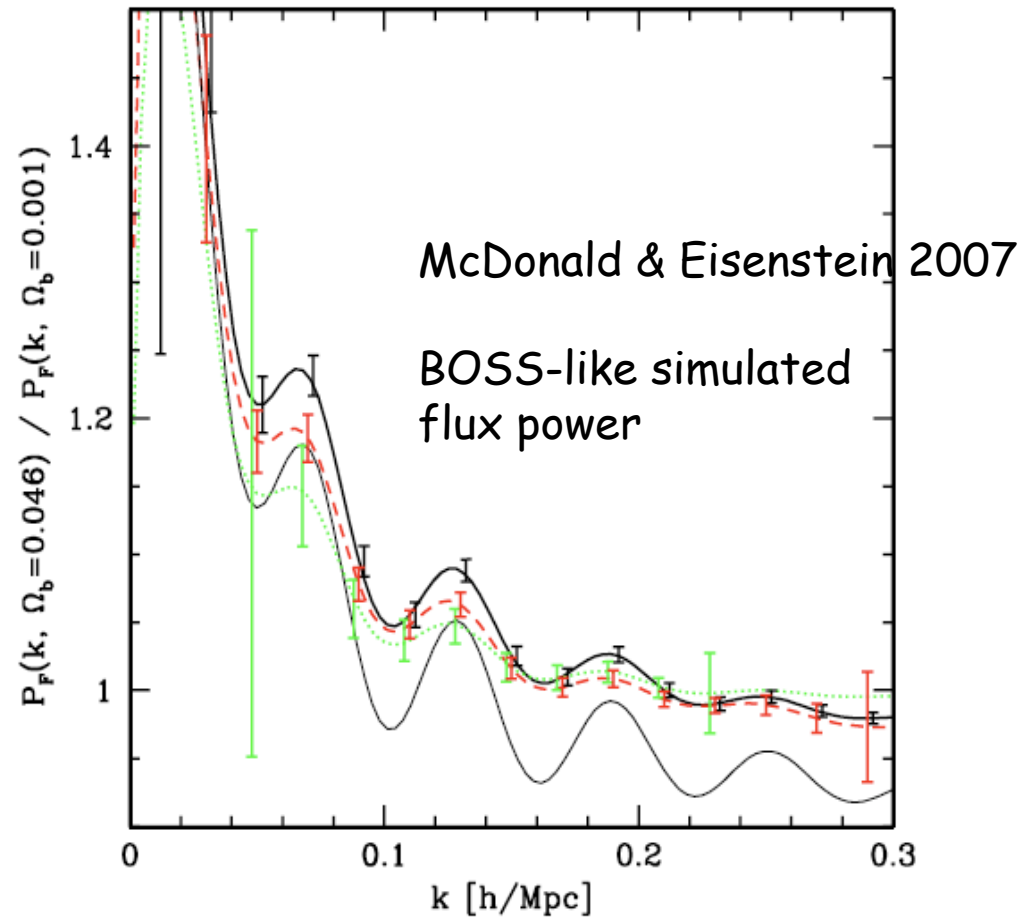
Independent analysis of thermal state using different statistics and constraints both on astrophysics and cosmological probes (e.g. Vallinotto, Xia's talks) at both HIGH and low redshift

E-ELT era: measuring the cosmic expansion

# Future perspectives : BAO

Importance of transverse direction:  
MV et al 2002; White 2003;  
McDonald & Eisenstein 2007;  
Slosar et al. 2009

about 20 QSOs per square degree  
with BOSS



# **COSMIC EXPANSION**

# Measuring the cosmic expansion?

$$1 + z(t_0, t_e) = \frac{a(t_0)}{a(t_e)} = \frac{a_0}{a}$$

$$dz = \frac{\partial z}{\partial t_0} dt_0 + \frac{\partial z}{\partial t_e} dt_e$$

$$\dot{z} = \frac{dz}{dt_0} = \frac{\partial z}{\partial t_0} + \frac{\partial z}{\partial t_e} \frac{dt_e}{dt_0} = \frac{\dot{a}(t_0)}{a(t_e)} - \frac{\dot{a}(t_e)}{a(t_e)} \frac{a(t_0)}{a(t_e)} \frac{1}{1+z}$$

$$\dot{z} = (1+z)H_0 - H(t_e)$$

## THE ASTROPHYSICAL JOURNAL

AN INTERNATIONAL REVIEW OF SPECTROSCOPY AND  
ASTRONOMICAL PHYSICS

VOLUME 136

SEPTEMBER 1962

NUMBER 2

THE CHANGE OF REDSHIFT AND APPARENT LUMINOSITY  
OF GALAXIES DUE TO THE DECELERATION OF  
SELECTED EXPANDING UNIVERSES

ALLAN SANDAGE

Mount Wilson and Palomar Observatories  
Carnegie Institution of Washington, California Institute of Technology

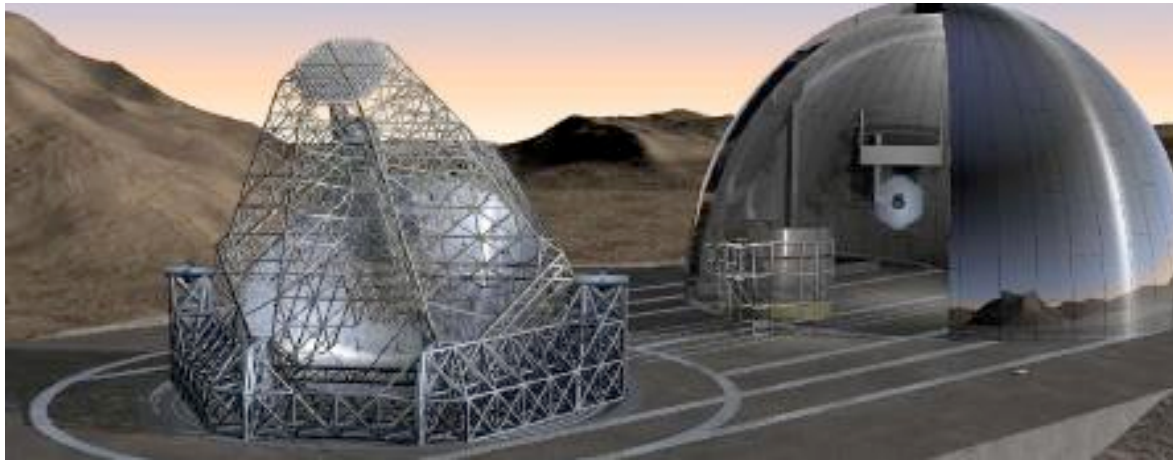
(With an Appendix by G. C. McVITTIE, University of Illinois Observatory, Urbana)  
*Received February 2, 1962; revised April 13, 1962*

This is a fundamental quantity not related at all to the FRW equations....

# COsmicDynamicEXperiment

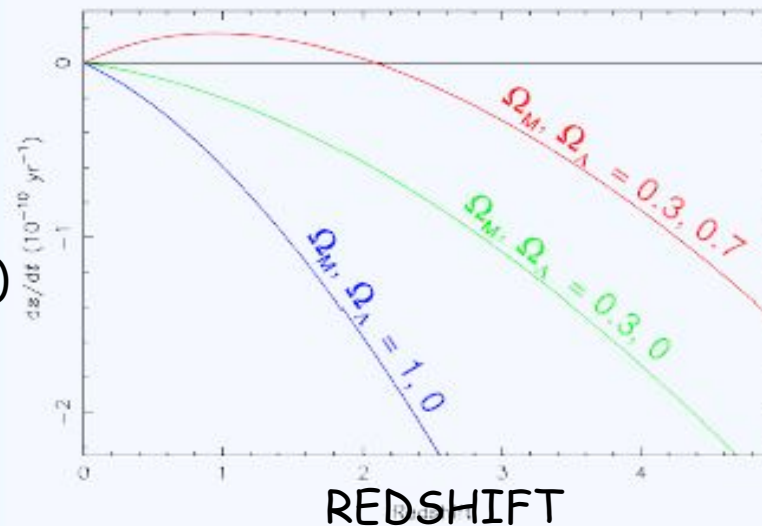
# CODEX-I

Ultra-stable spectrograph



$$\frac{d}{dt_0} \left[ 1+z = \frac{a(t_0)}{a(t_e)} \right] \Rightarrow \frac{dz}{dt_0} = (1+z) H_0 - H(z)$$

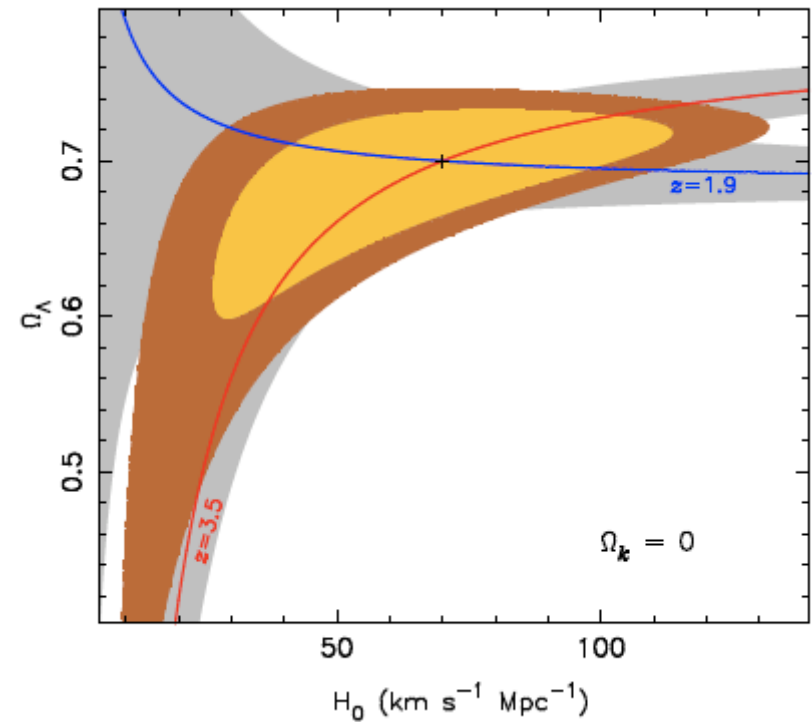
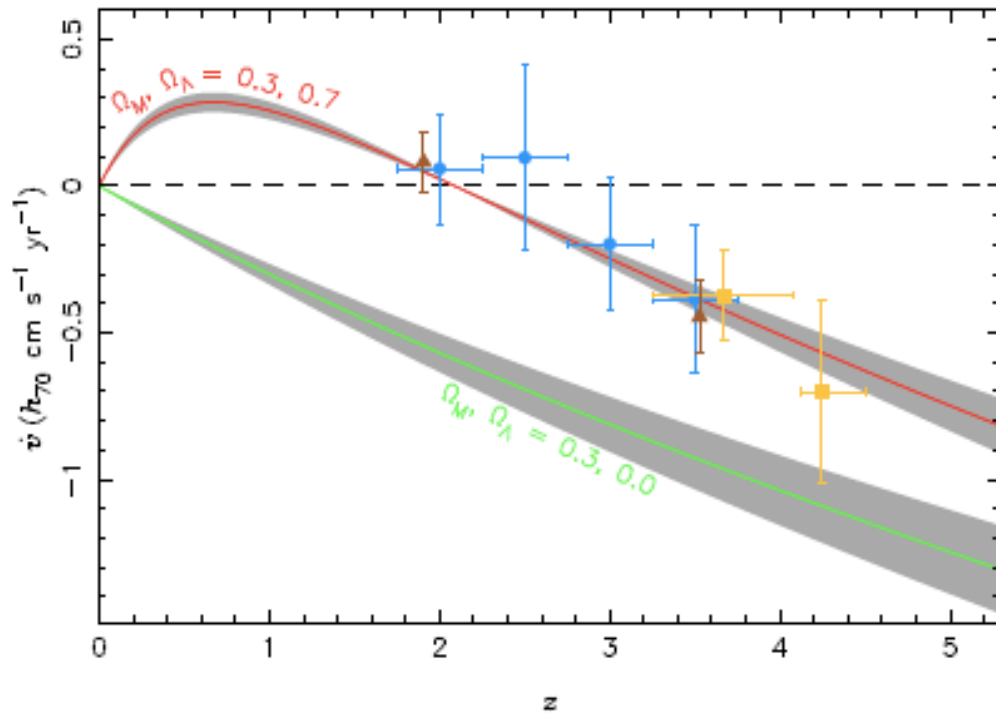
Dz/Dt  
(10<sup>-10</sup> yr<sup>-1</sup>)



$dz/dt$  as a function of redshift for different cosmological parameters as indicated and  $H_0 = 70 \text{ km/s/Mpc}$ .

For  $\Delta t = 10 \text{ yr}$  @  $z = 4$ :  
 $\Delta z \sim 9 \times 10^{-10}$   
 $\Delta \lambda \sim 1 \times 10^{-6} \text{ \AA}$   
 $\Delta v \sim 5.4 \text{ cm/s}$





Liske et al. 2008, MNRAS, 386, 1192

# SUMMARY

- Lyman- $\alpha$  forest is an important cosmological probe at a unique range of scales and redshifts in the structure formation era
- Current limitations are more theoretical (more reliable simulations are needed for example for neutrino species) than observational and statistical errors are smaller than systematic ones
- Need to fit all the IGM statistics at once (mean flux + flux pdf + flux power + flux bispectrum + ... ) to beat down systematics
- Tension with the CMB is still there. Very constraining for what happens at those scales: running (inflation), neutrinos, warm dark matter candidates ... **IMPORTANCE** of **SINERGIES** with cosmology and astrophysics and cross-correlations of observables in the SDSS-3 era