



DO WE LIVE INSIDE A BIG VOID?

COSMO 2009

CERN

7th September 2009

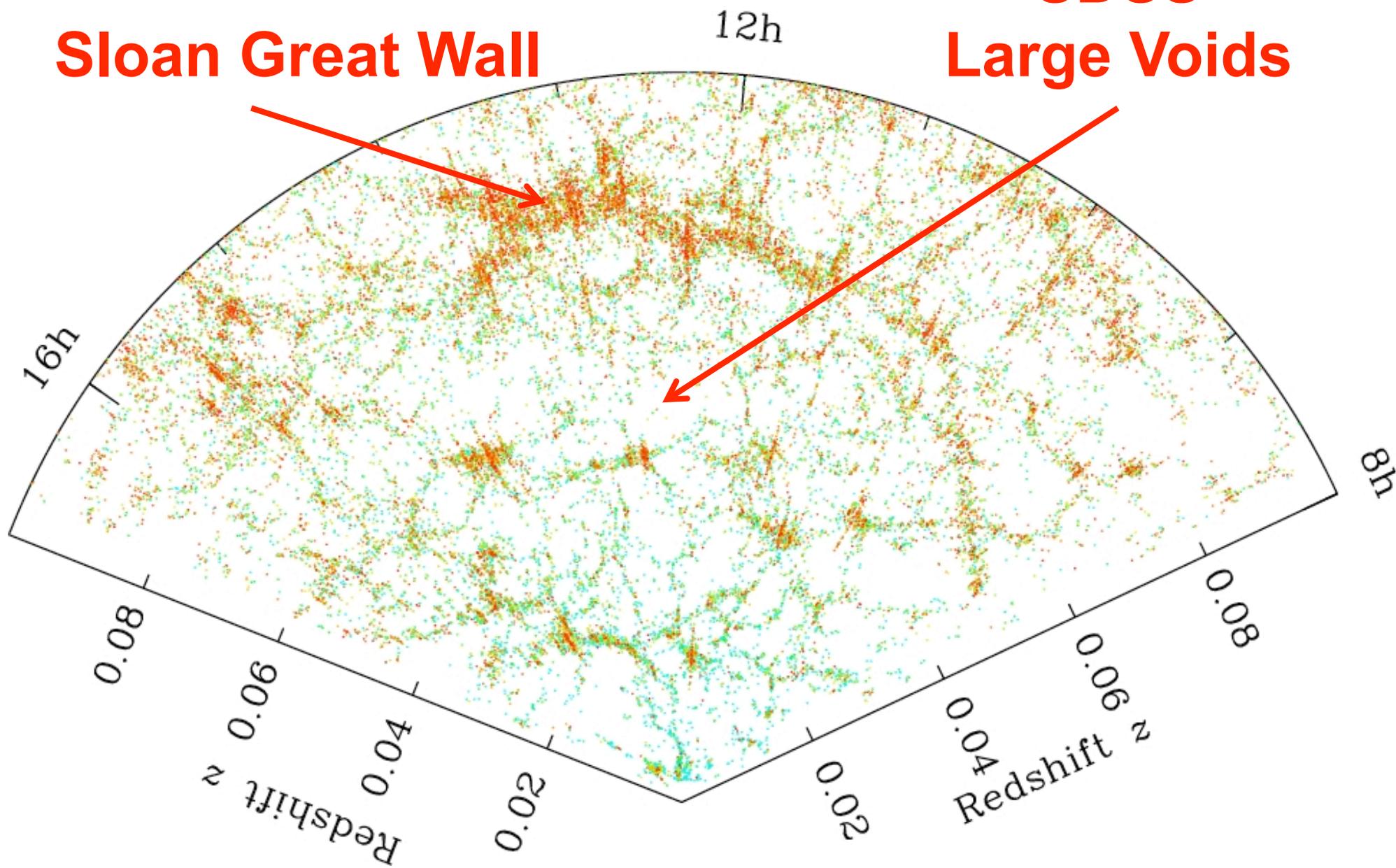
Juan García-Bellido

IFT-UAM/CSIC

CERN

Sloan Great Wall

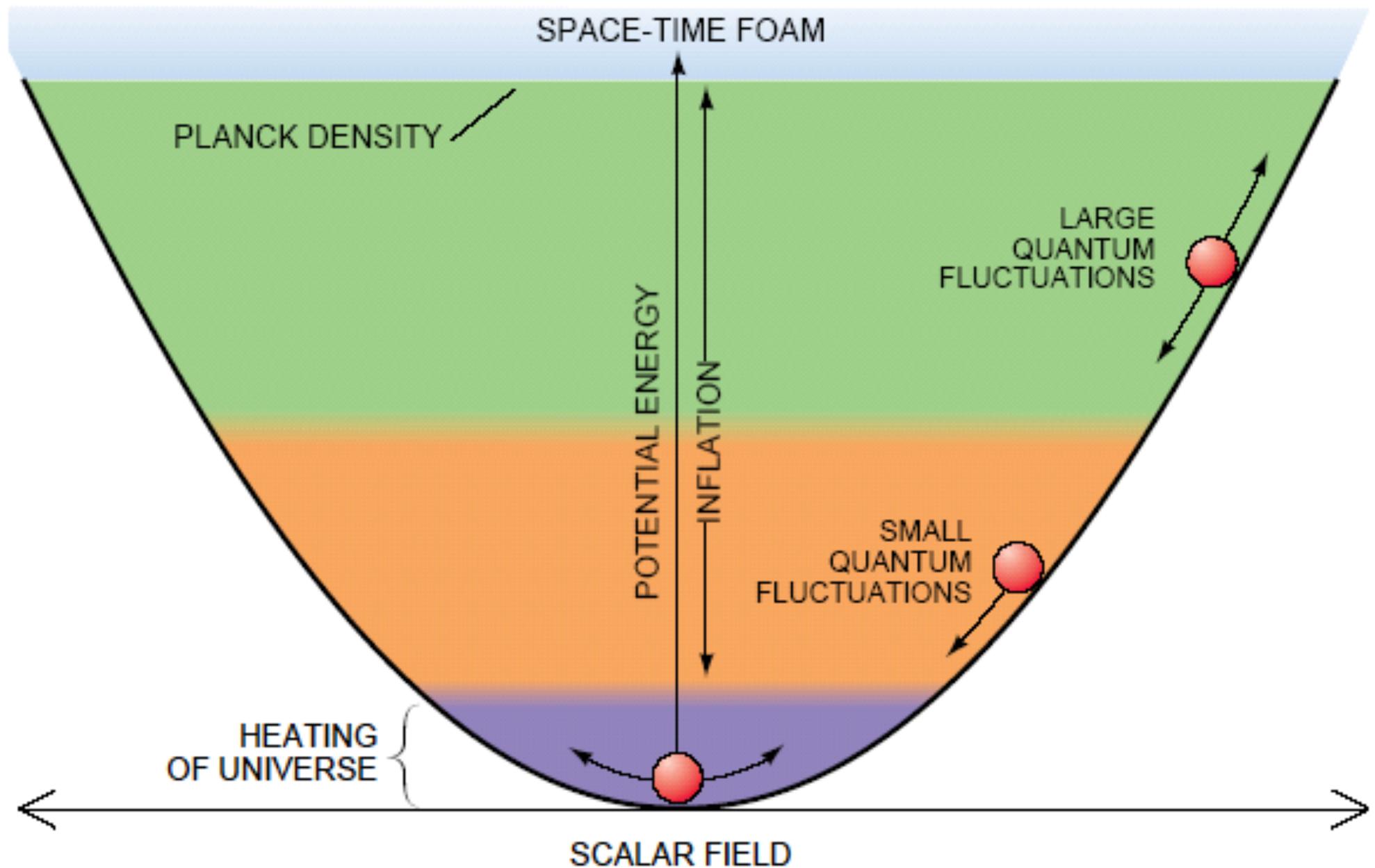
**SDSS
Large Voids**



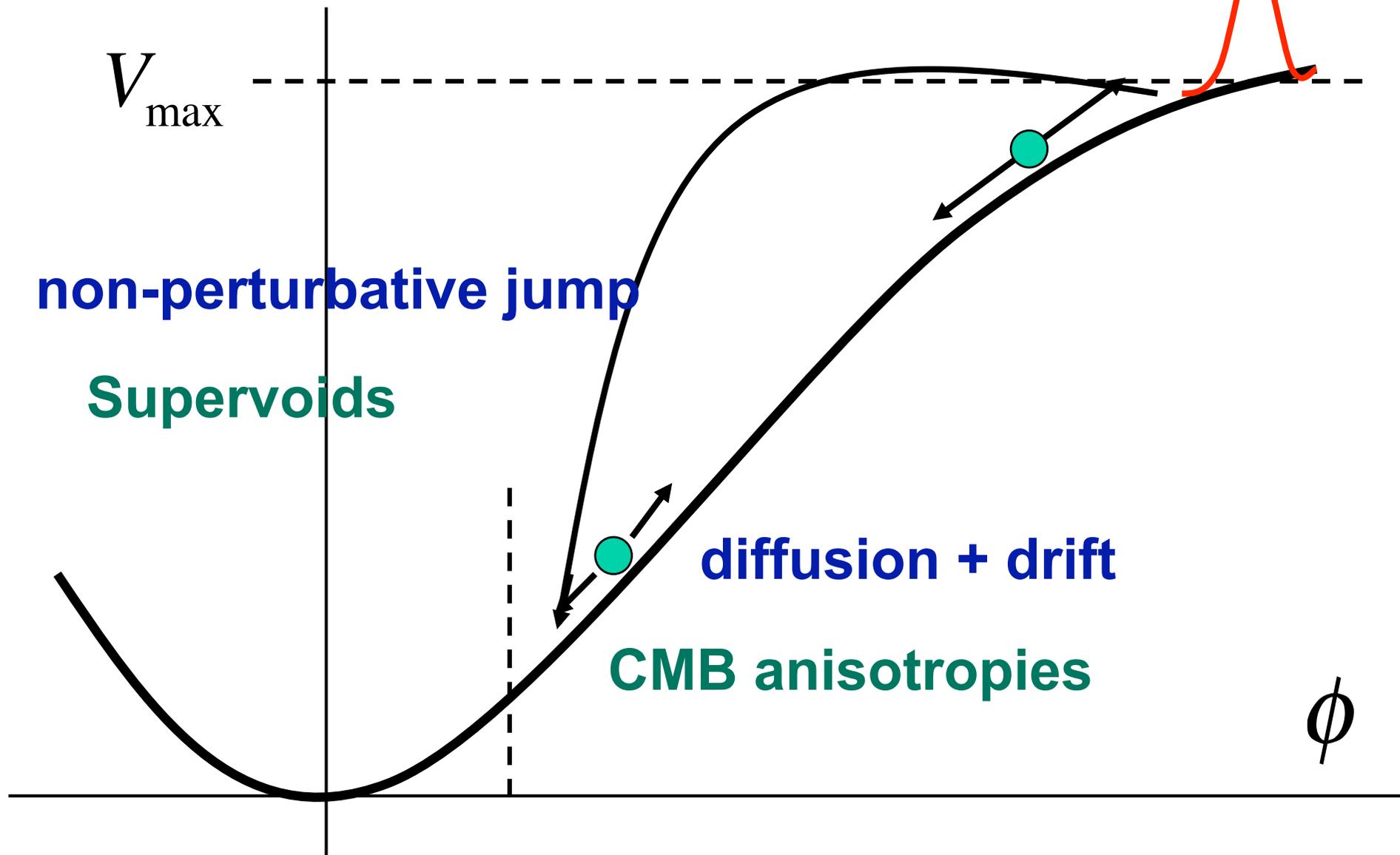
If we live in a highly
inhomogeneous
Universe...

what is
the origin of
dens. perturbations?

Chaotic Inflation



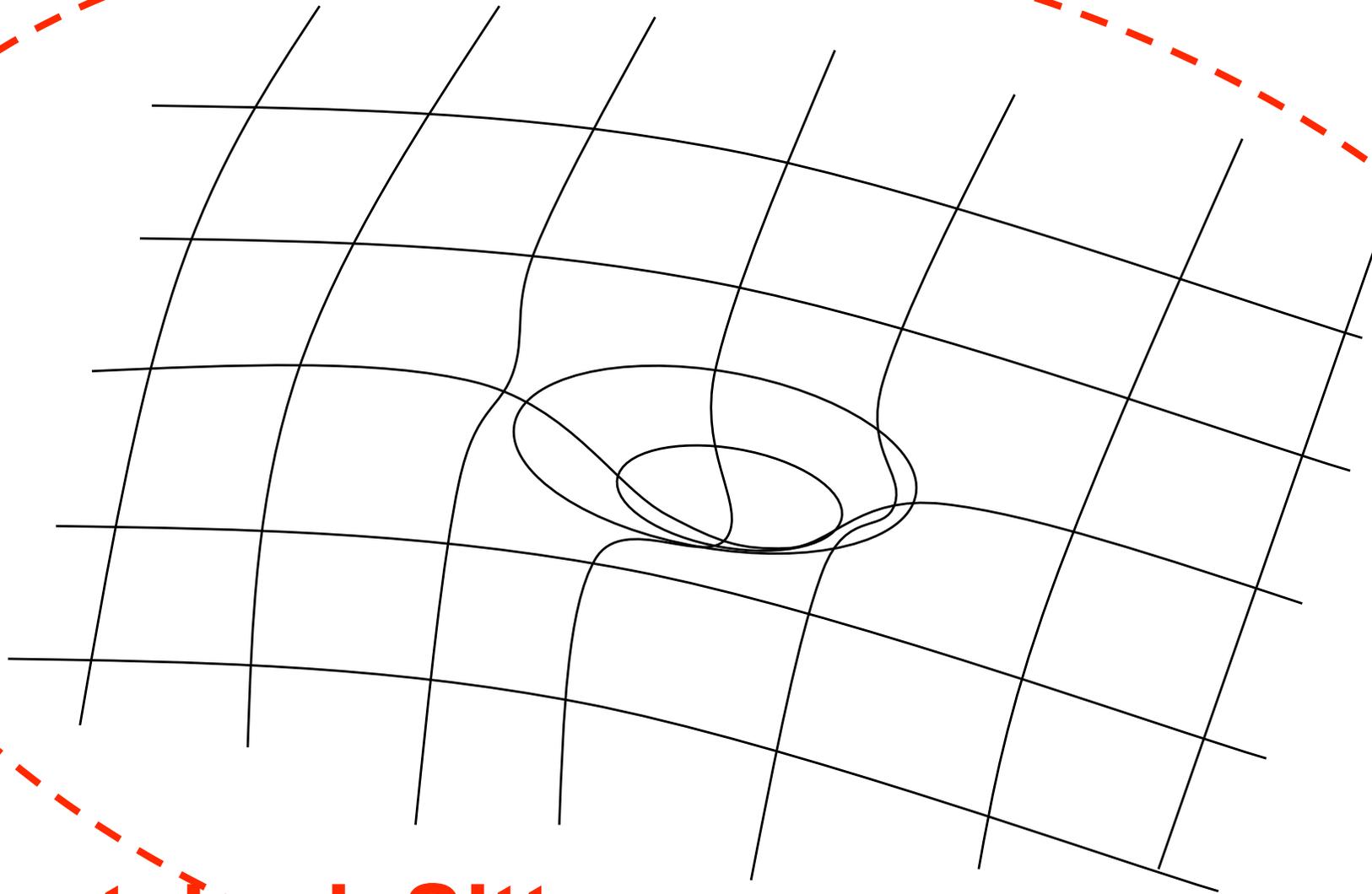
Eternal stochastic inflation



Linde & Mezhlumian (1995)

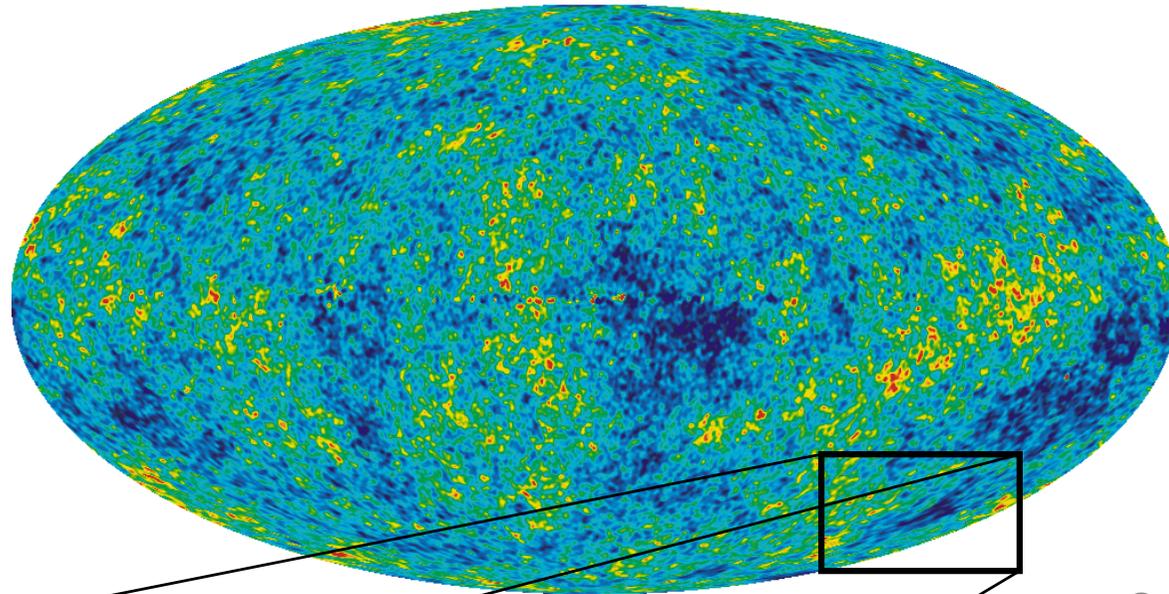
Infloid = Lemaitre-Tolman-Bondi Model

Linde & Mezhlumian (1995)

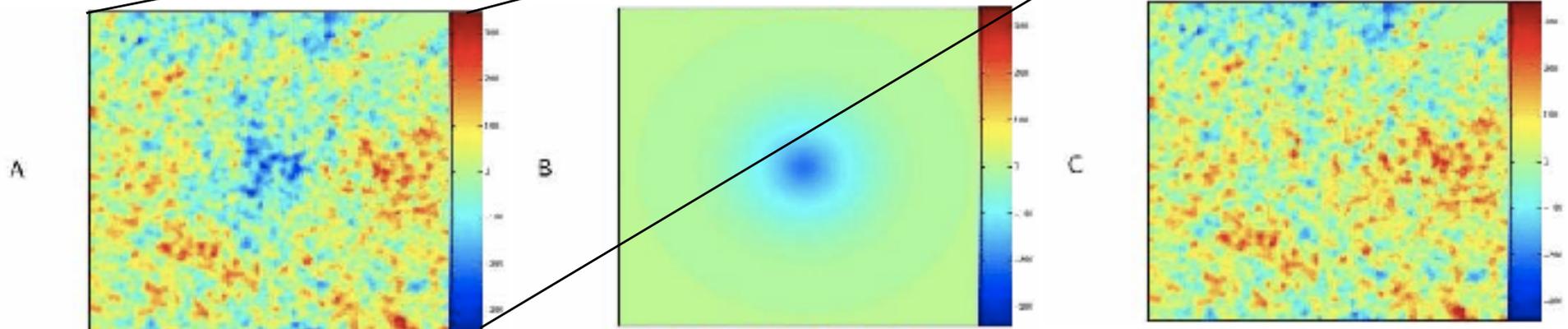


Einstein-deSitter

Could the Cold Spot in CMB be an “inflow” ?



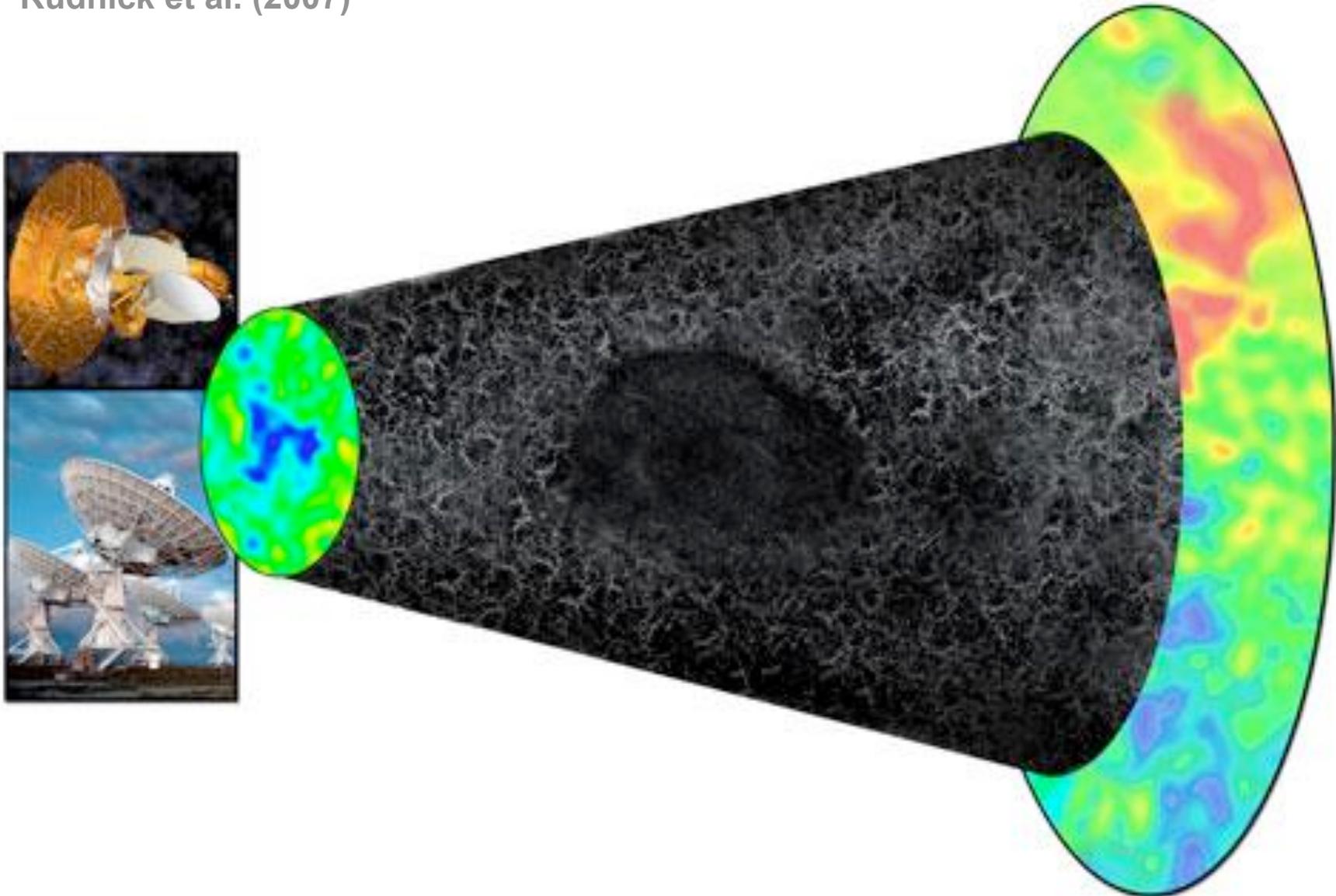
Cruz et al. (2006)



A large void, approximately 2 Gpc in size

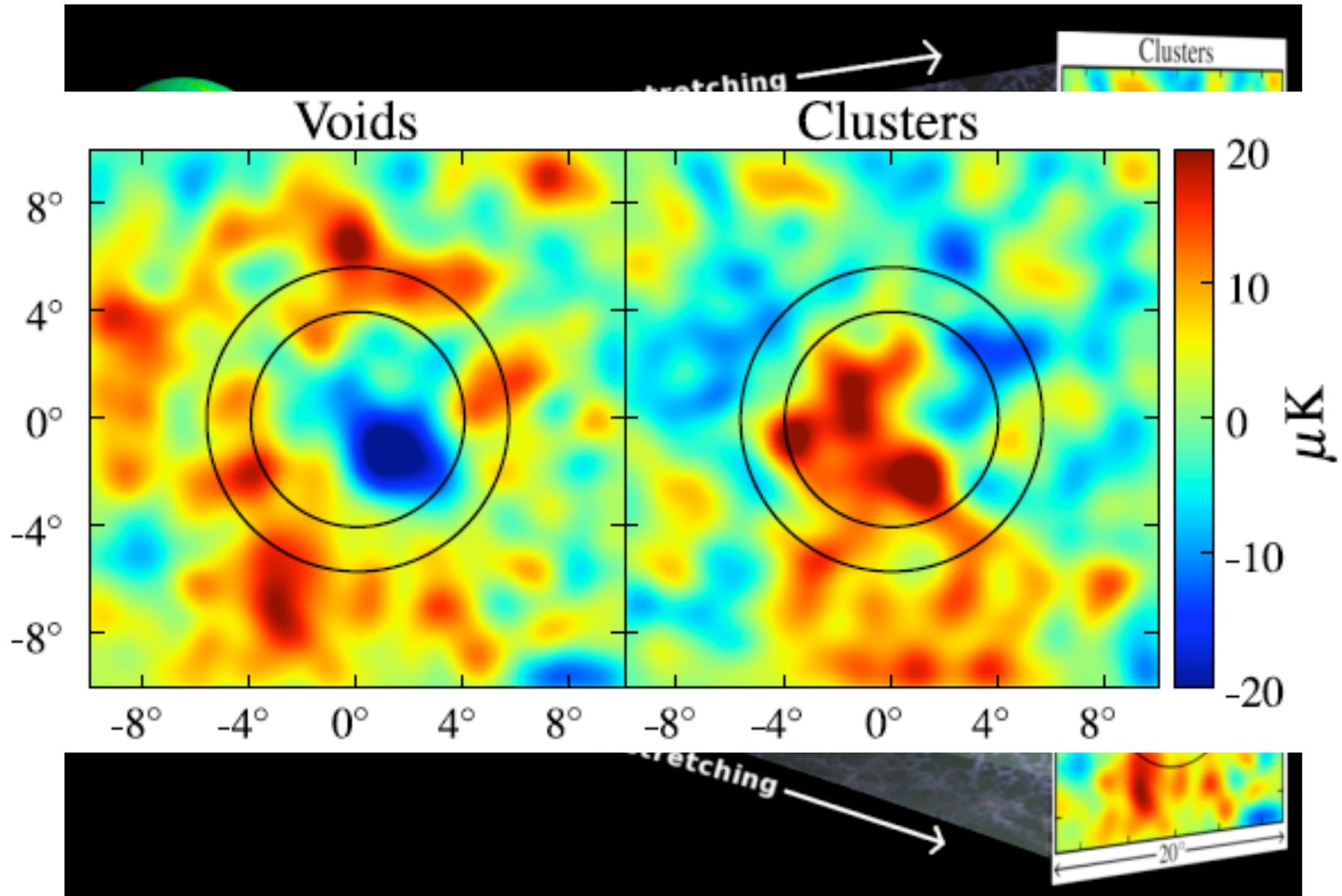
Could the Cold Spot in CMB be an “inflow” ?

Rudnick et al. (2007)



Voids and Superclusters in SDSS

Granett et al. (2008)



The Lemaître-Tolman-Bondi Model

Celerier (1999), Tomita(2000), Moffat (2005), Alnes et al. (2005)

- Describes a space-time which has spherical symmetry in the spatial dimensions, but with time and radial dependence:

$$ds^2 = -dt^2 + X^2(r, t) dr^2 + A^2(r, t) d\Omega^2$$

- From the 0-r part of the Einstein-Equations we get:

$$X(r, t) = A'(r, t) / \sqrt{1 - k(r)}$$

- One can recover the FRW model setting:

$$A(r, t) = a(t) r \quad k(r) = k r^2$$

The Lemaitre-Tolman-Bondi Model

- Matter content:

$$T_{\nu}^{\mu} = -\rho_M(r, t) \delta_0^{\mu} \delta_{\nu}^0.$$

- The other Einstein equations give:

$$\frac{\dot{A}^2 + k}{A^2} + 2\frac{\dot{A}\dot{A}'}{AA'} + \frac{k'(r)}{AA'} = 8\pi G \rho_M$$

$$\dot{A}^2 + 2A\ddot{A} + k(r) = 0$$

- Integrating the last equation:

Enqvist & Mattsson(2006)

$$\frac{\dot{A}^2}{A^2} = \frac{F(r)}{A^3} - \frac{k(r)}{A^2}$$

The Lemaitre-Tolman-Bondi Model

García-Bellido & Haugbølle (2008)

- All we need to specify:

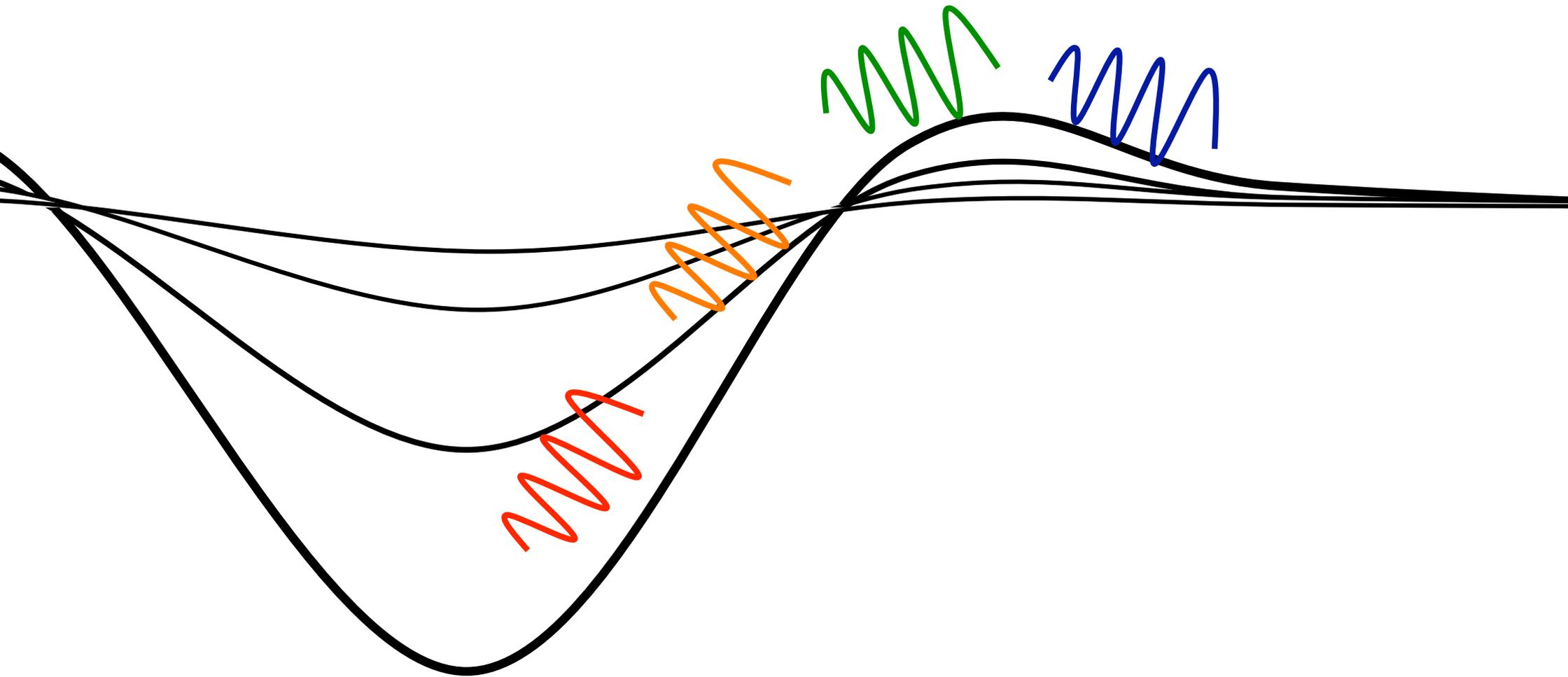
$$F(r) = H_0^2(r) \Omega_M(r) A_0^3(r)$$

$$k(r) = H_0^2(r) \left(\Omega_M(r) - 1 \right) A_0^2(r)$$

- Then the Hubble rate can be integrated to give $A(r,t)$:

$$H^2(r, t) = H_0^2(r) \left[\Omega_M(r) \left(\frac{A_0(r)}{A(r, t)} \right)^3 + (1 - \Omega_M(r)) \left(\frac{A_0(r)}{A(r, t)} \right)^2 \right]$$

Density profile



Light Ray Propagation

- By looking at the geodesic equation, we can find the equation of motion for light rays:

$$\frac{dt}{dN} = -\frac{A'(r, t)}{\dot{A}'(r, t)} \quad \frac{dr}{dN} = \frac{\sqrt{1 - k(r)}}{\dot{A}'(r, t)}$$

where $N = \ln(1+z)$ are the # e-folds before present time.

- The various distances as a function of redshift are:

$$d_L(z) = (1 + z)^2 A[r(z), t(z)]$$

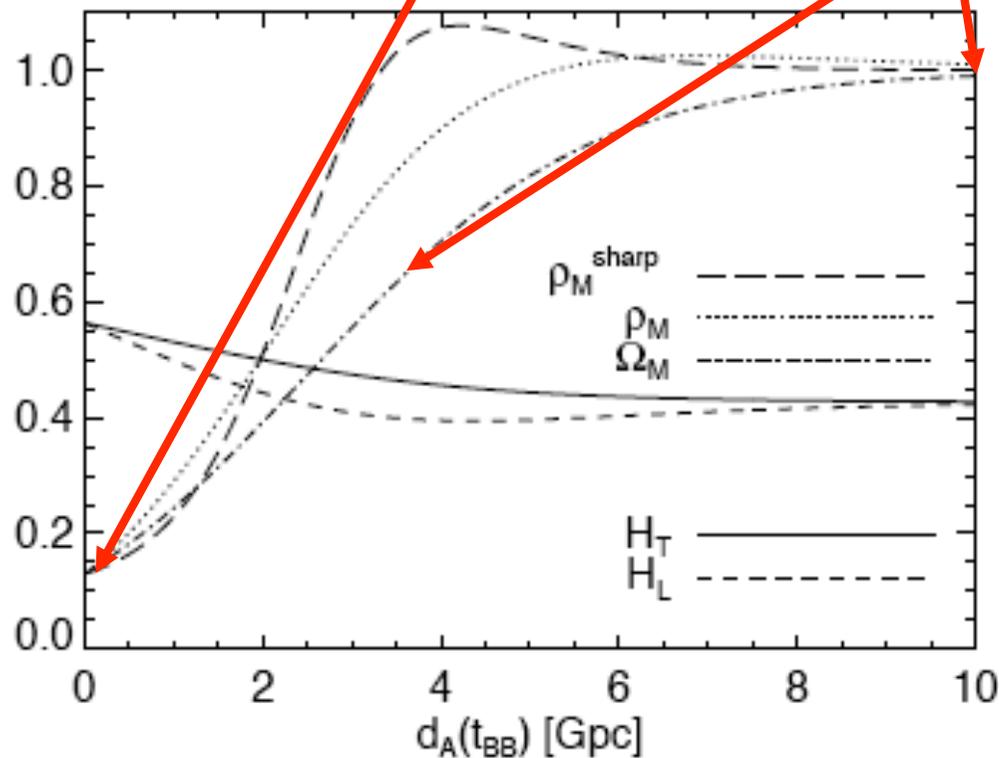
$$d_C(z) = (1 + z) A[r(z), t(z)]$$

$$d_A(z) = A[r(z), t(z)]$$

The LTB-GBH model

$$\Omega_M(r) = \Omega_{\text{out}} + (\Omega_{\text{in}} - \Omega_{\text{out}}) \left(\frac{1 - \tanh[(r - r_0)/2\Delta r]}{1 + \tanh[r_0/2\Delta r]} \right)$$

$$H_0(r) = H_{\text{out}} + (H_{\text{in}} - H_{\text{out}}) \left(\frac{1 - \tanh[(r - r_0)/2\Delta r]}{1 + \tanh[r_0/2\Delta r]} \right)$$

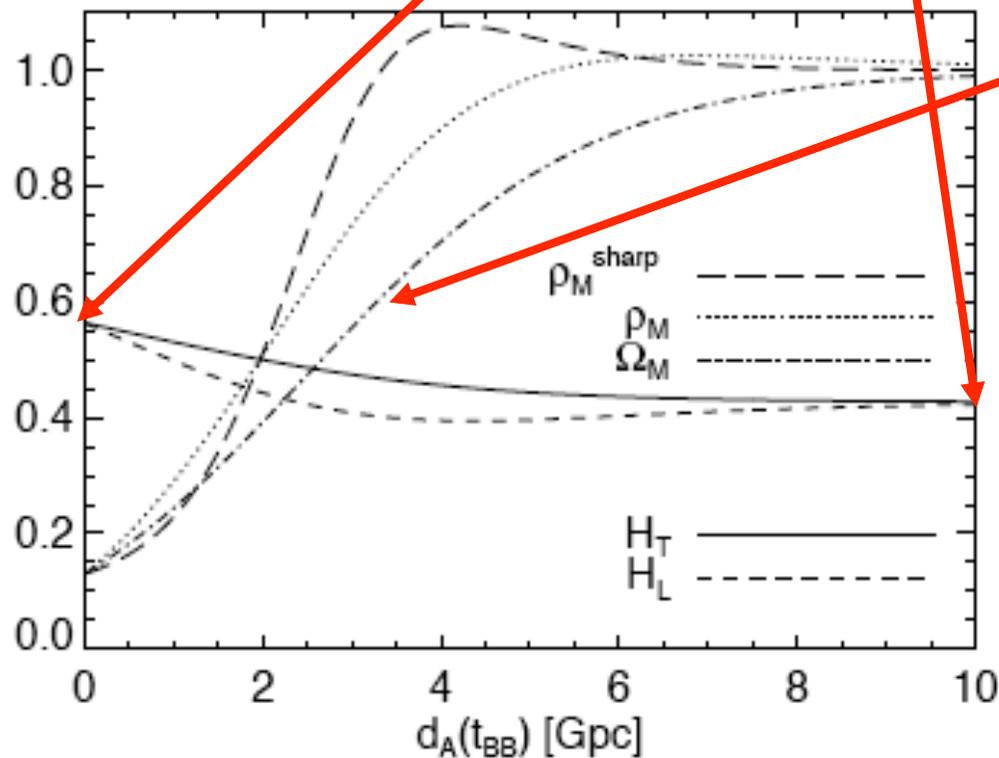


- If we assume asymptotic flatness, then the model has 5 parameters
- If we require a homogeneous Big Bang then the model has 4 parameters

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- If we assume asymptotic flatness, then **the model has 5 parameters**
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Constraining Cosmological Data

- Type Ia Supernovae: 307 SNIa Union Supernovae
Simple to do since we just fit against $d_L(z)$

- 1st acoustic peak in the CMB: $d_C(z_{\text{rec}})$ sound horizon $r_s(z)$

- Baryon Acoustic Oscillations:

Sound horizon

$$D_V(z) = \left[d_A^2(z)(1+z)^2 \frac{cz}{H_L(z)} \right]^{1/3}$$

3 distances

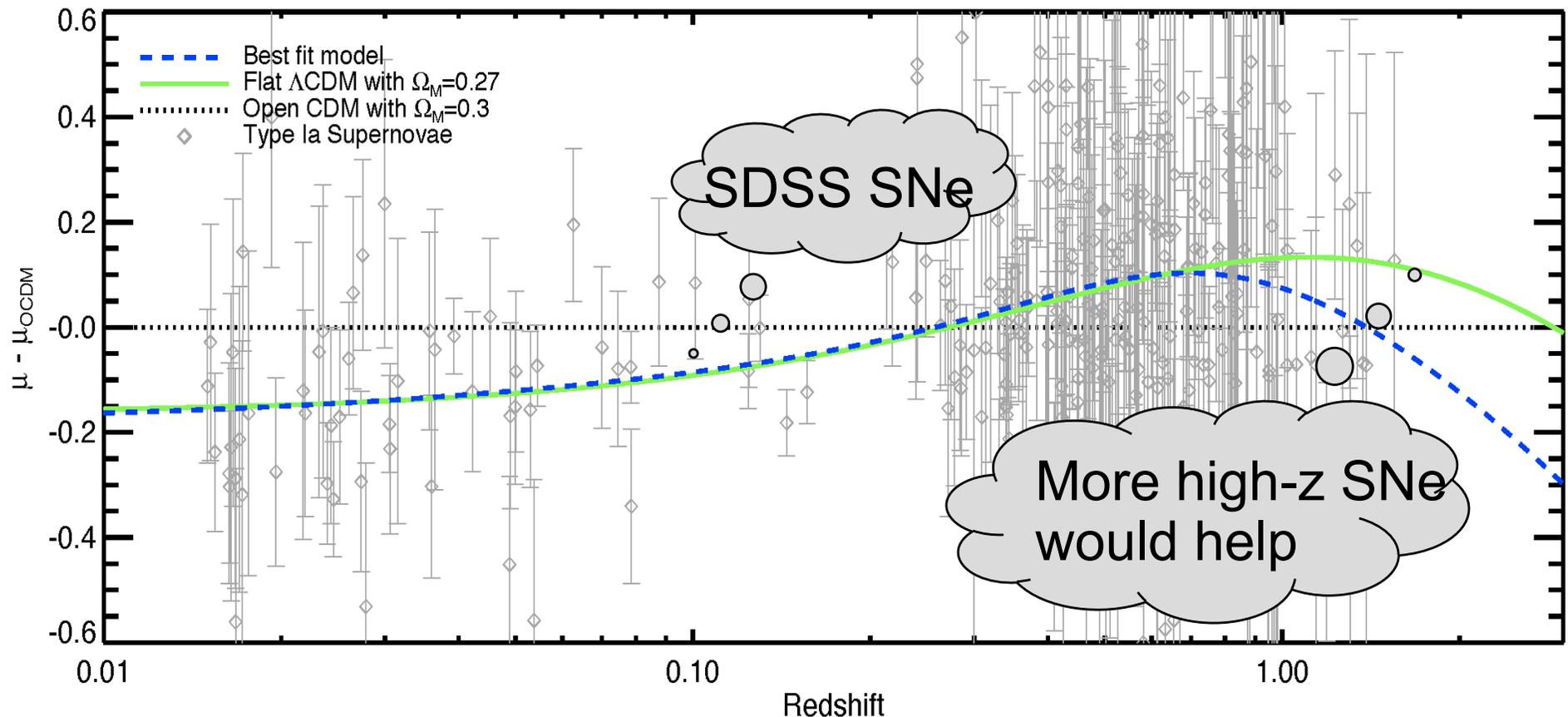
- Other constraints:

- $f_{\text{gas}} = \rho_b / \rho_m = \omega_b / (\Omega_m h^2)$
- Hubble key project: $H_0 = 72 \pm 8$ km/s/Mpc (1σ)
- Globular cluster lifetimes ($t_{\text{BB}} > 11.2$ Gyr)

Fitting the Union Supernovae

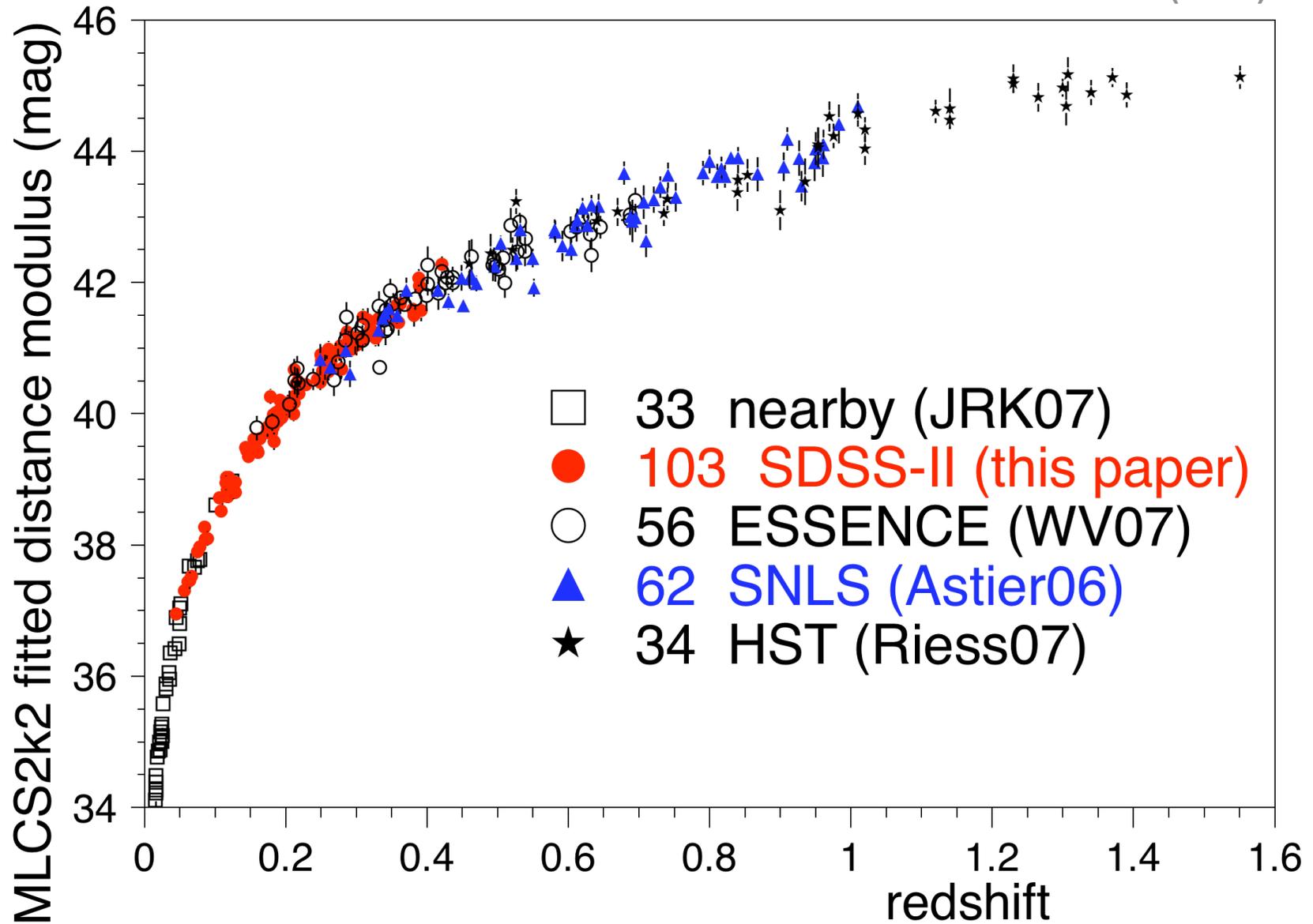
- The best fit GBH-model has no problem with SNe Ia
- One can always find a void model that fits SNe as Λ CDM

García-Bellido & Haugbølle (2009)



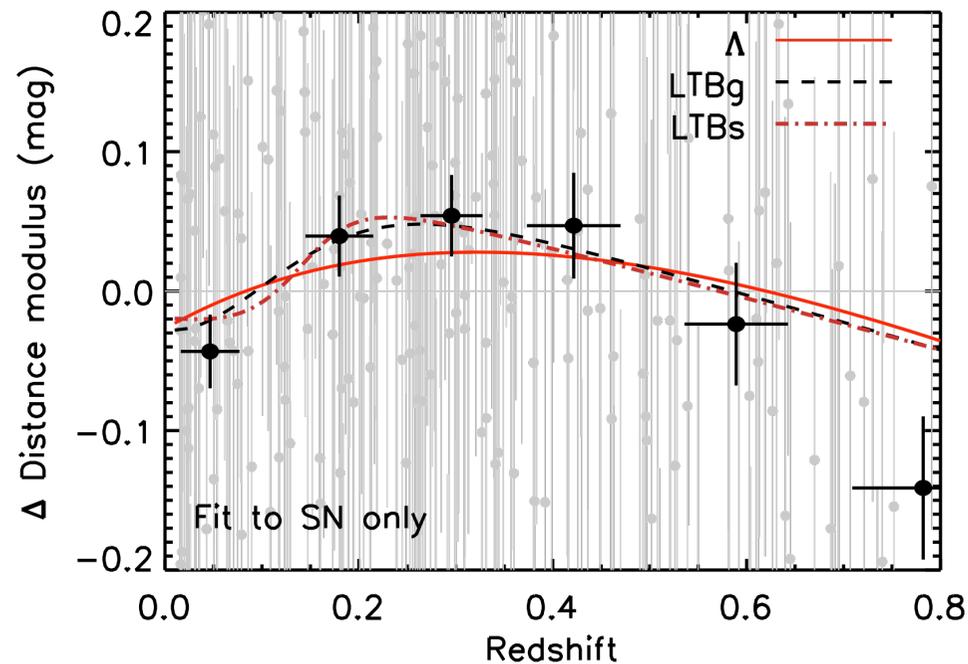
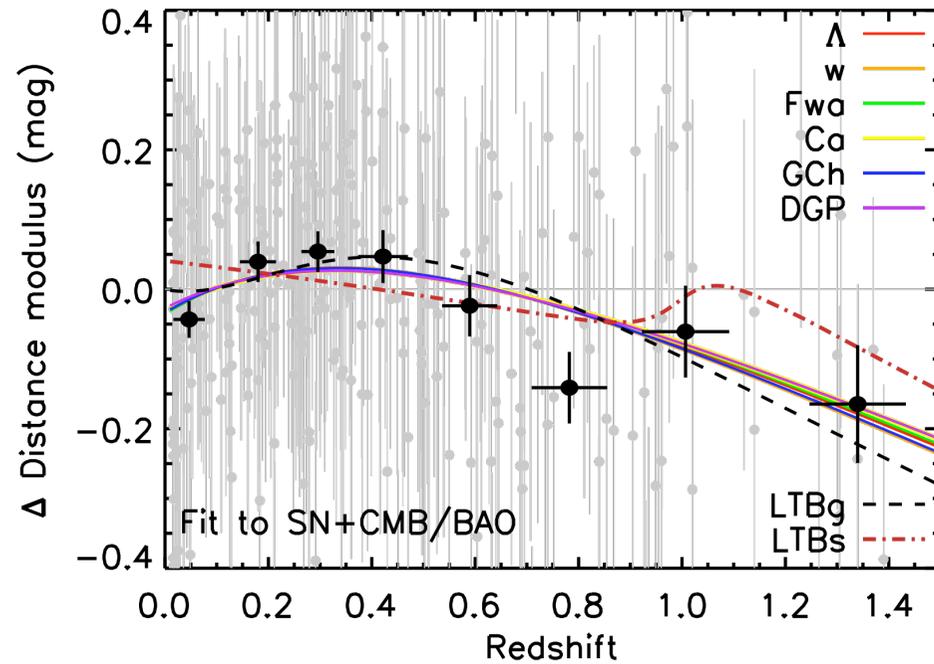
Fitting the SDSS II Supernovae

SDSS II SN team (2009)

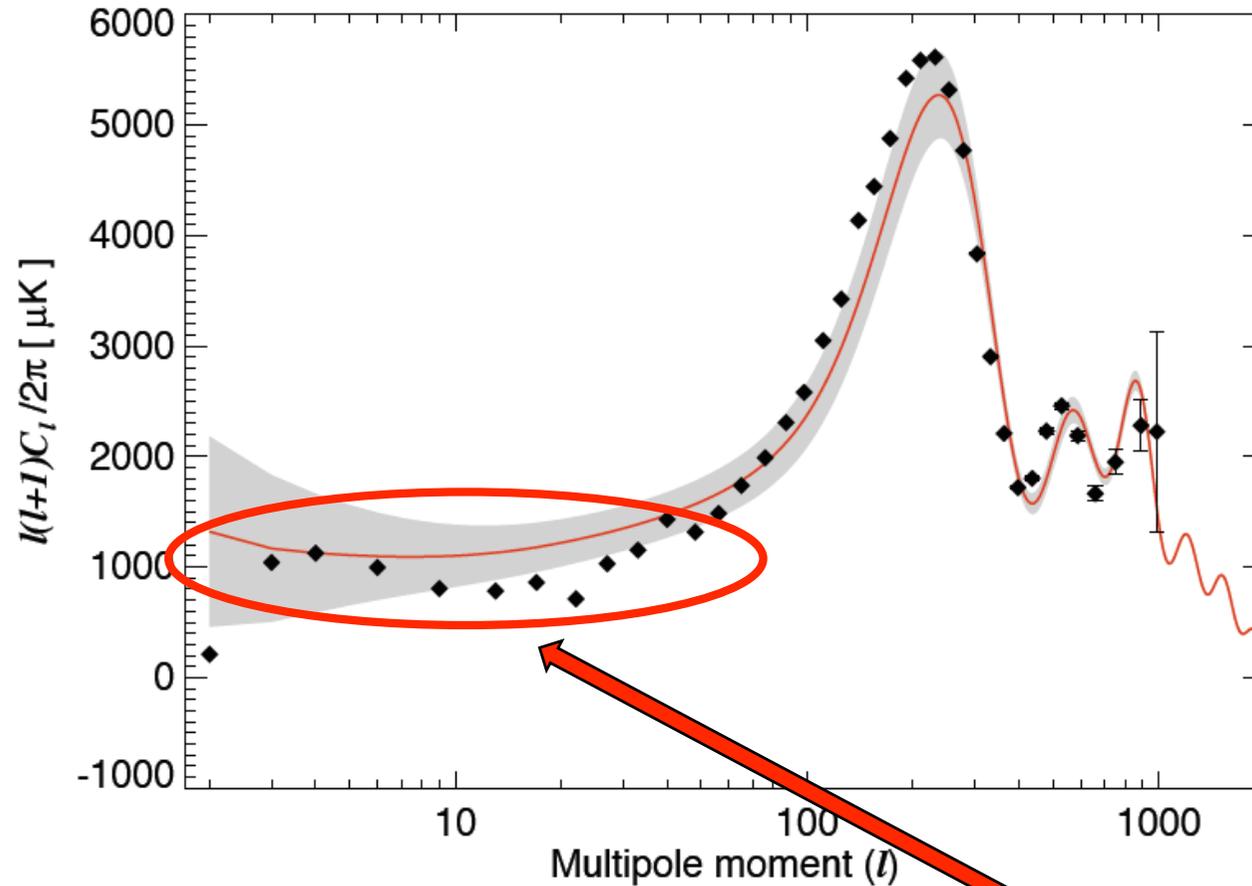


Fitting the SDSS II Supernovae

SDSS II SN team (2009)

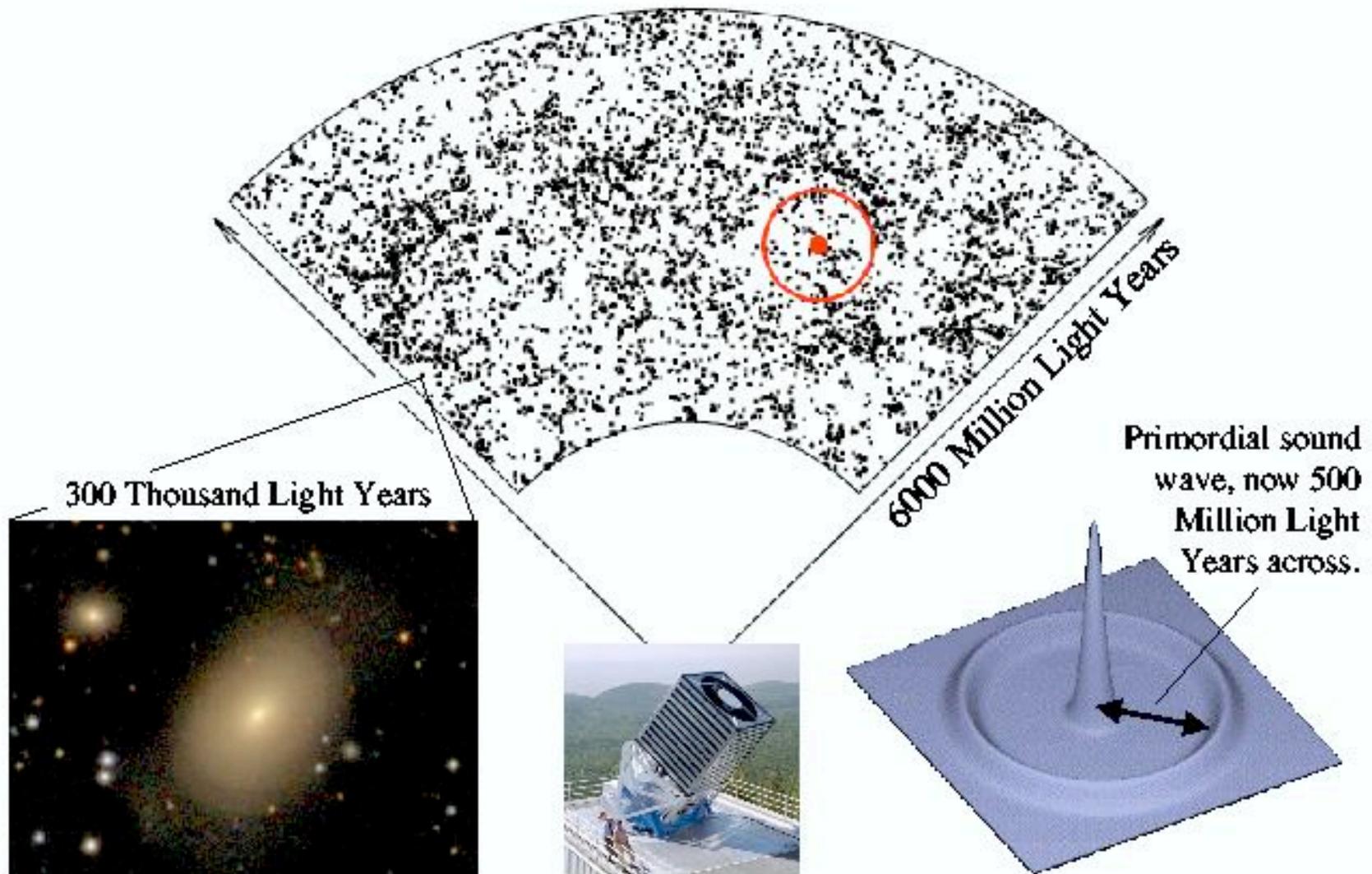


Fitting the acoustic peaks in the CMB



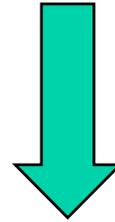
- The fit to the *first* peak is OK - we did *not* try to fit all data!
- LTB perturbation theory (work in progress) to explain low l (ISW)

Baryon Acoustic Oscillations



Radial BAO & LTB

$$\Delta z_{BAO}(z_i) = \frac{H(z_i)r_s}{c}$$



scaled distances:

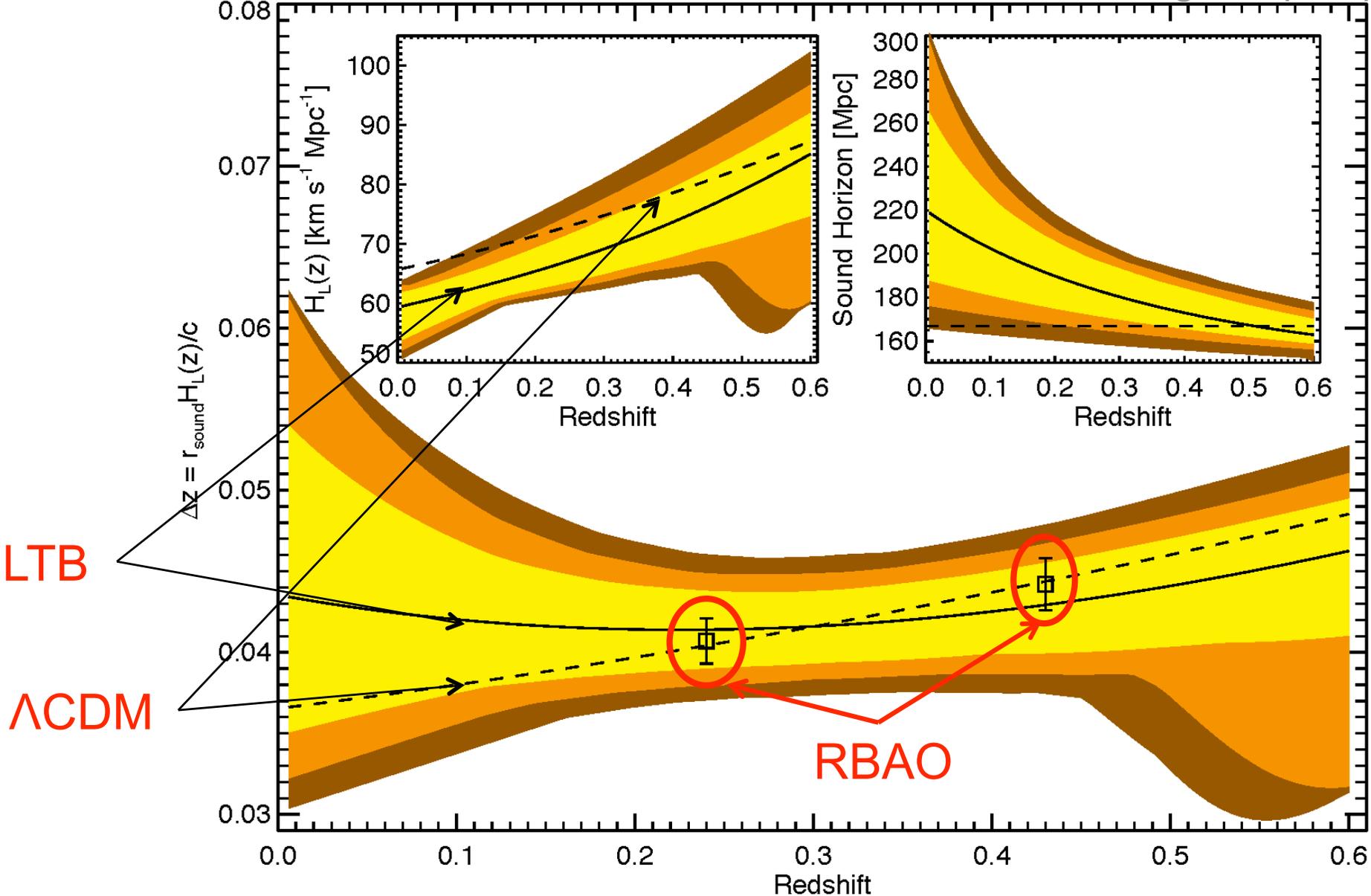
$$\Delta z_{LTB} = \frac{H_L(z)r_s(z)}{c}$$

r_s = sound horizon at recombination

Sample z range	z_m	r_{BAO} Mpc/h	σ_{st}	σ_{sys}	Δz_{BAO}	σ_{st}	σ_{sys}
0.15-0.30	0.24	110.3	2.5	1.35	0.0407	0.0009	0.0005
0.40-0.47	0.43	108.9	2.8	1.22	0.0442	0.0011	0.0005

Sound horizon and line of sight rate of expansion

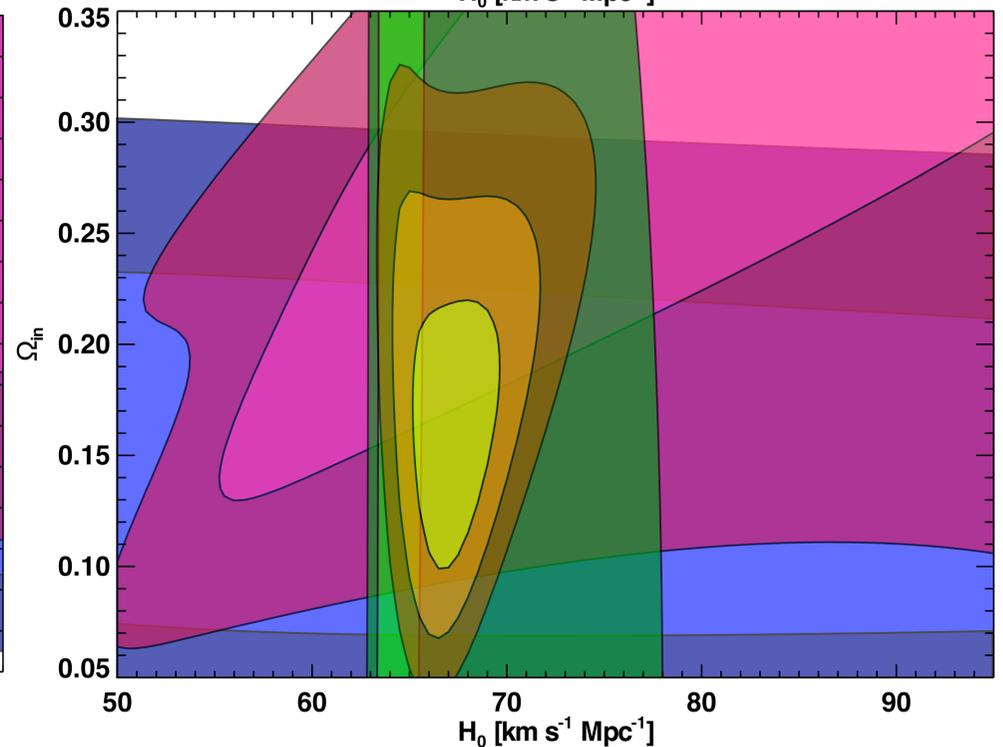
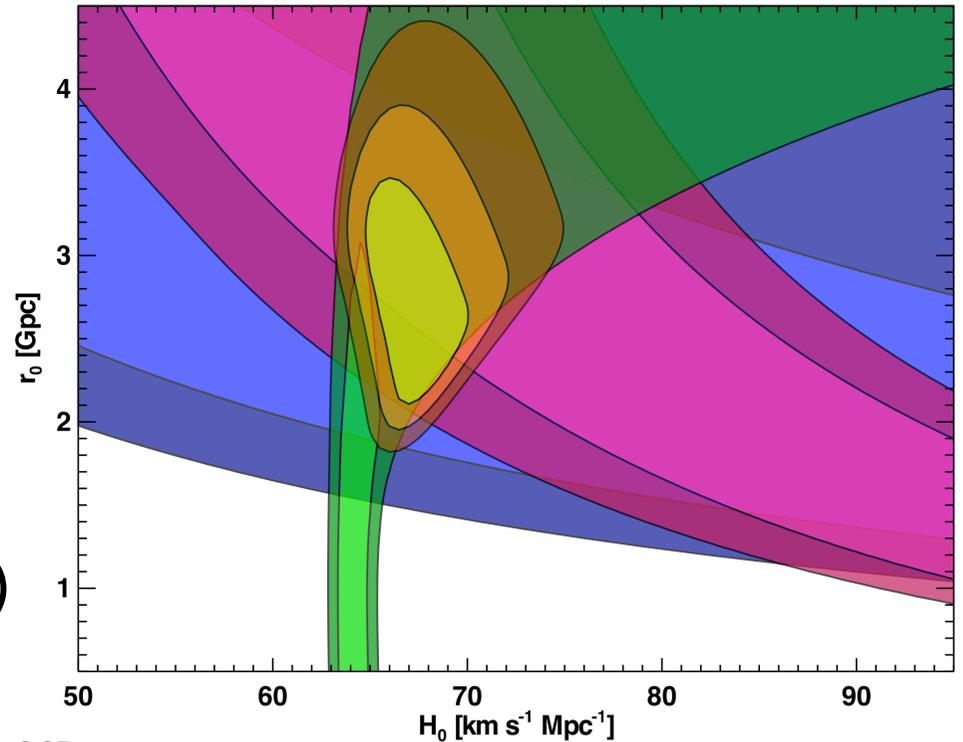
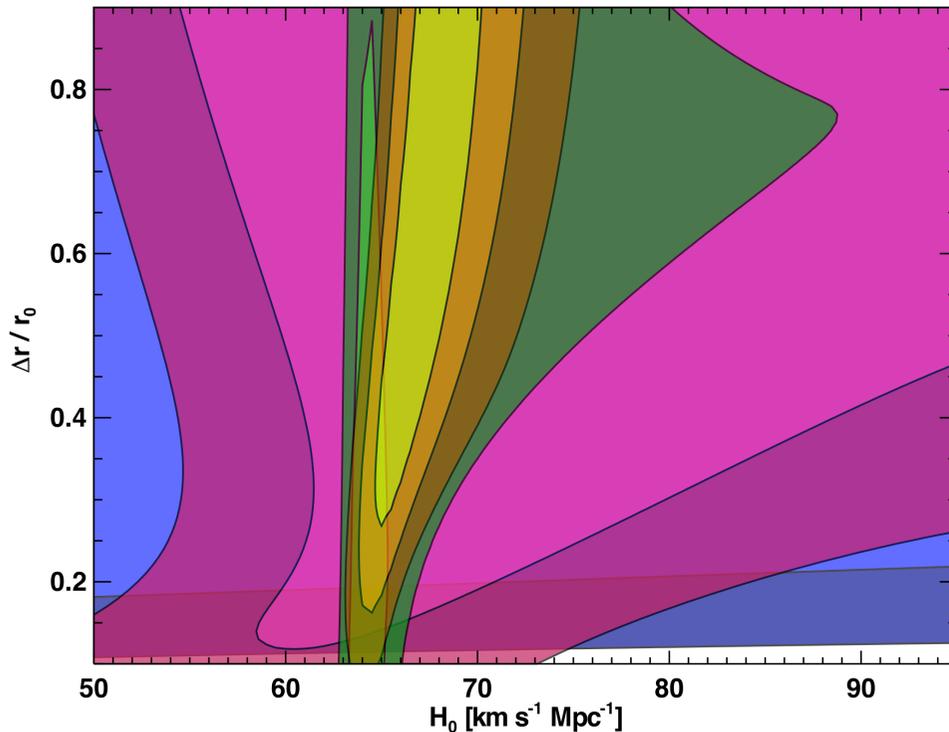
García-Bellido & Haugbølle (2009)



Scanning the model

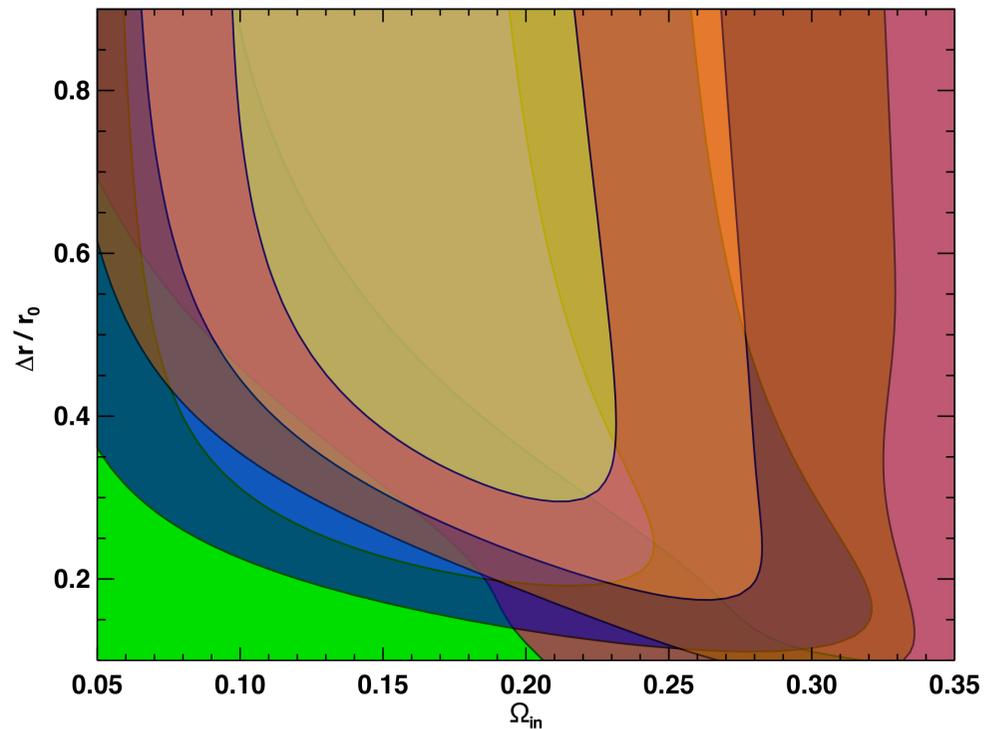
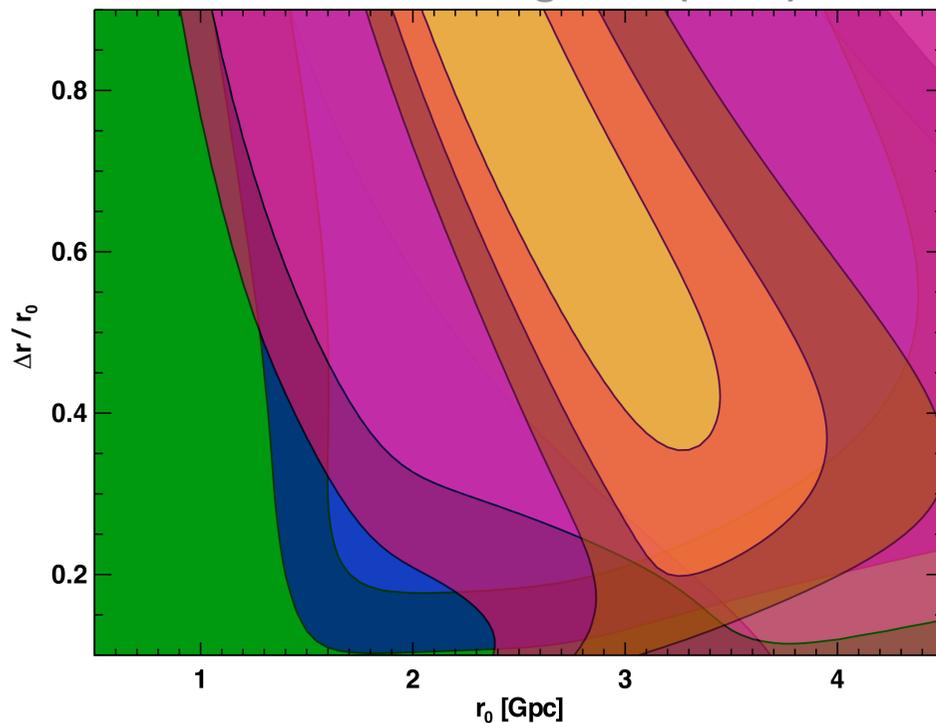
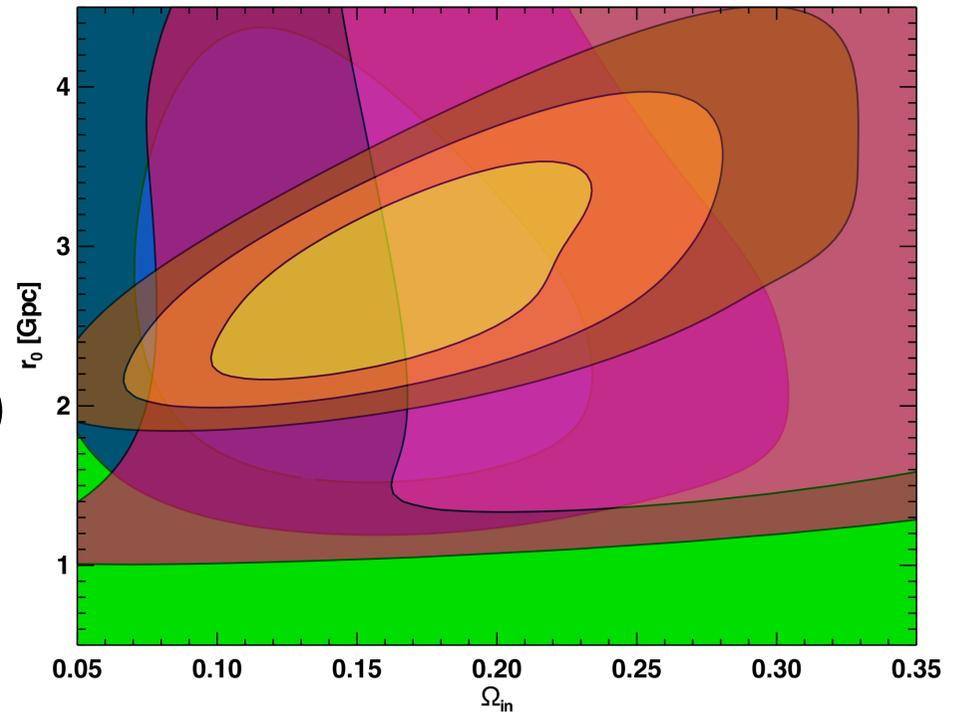
- Yellow: Everything, Blue: SNe
- Green: CMB. Purple: BAO
- Supernovae constrain Ω_{matter}
- CMB constrains the H_0 , ($\Omega_{\text{out}}=1$)

García-Bellido & Haugbølle (2009)



- The SNe and BAO pushes the void size to $r_0 > 1.8$ Gpc
- Some tension between RBAO and SNe (waiting for high-z SNe)
- Large degeneracy between r_0 and $\Delta r/r_0$

García-Bellido & Haugbølle (2009)



Marginalized errors

García-Bellido & Haugbølle (2009)

Model	H_0	H_{in}	H_{out}	H_{eff}
units	100 km s ⁻¹ Mpc ⁻¹			
GBH	–	0.58±0.03	0.49±0.2	0.43
Constrained	0.64±0.03	0.56	0.43	0.42

Model	Ω_{in}	r_0	Δr	t_{BB}
units		Gpc	r_0	Gyr
GBH	0.13±0.06	2.3±0.9	0.62(>0.20)	14.8
Constrained	0.13±0.06	2.5±0.7	0.64(>0.21)	15.3

!!

$$\chi^2_{\Lambda\text{CDM}} / d.o.f. = 1.021$$

$$\chi^2_{\text{LTB-GBH}} / d.o.f. = 1.036$$

A new observable: cosmic shear

García-Bellido & Haugbølle (2009)

$$\frac{d\Theta}{d\tau} = -\frac{1}{3}\Theta^2 - \sigma_{\mu\nu}\sigma^{\mu\nu} + \omega_{\mu\nu}\omega^{\mu\nu} - R_{\mu\nu}n^\mu n^\nu$$

$$\varepsilon \equiv \sqrt{\frac{3}{2}} \frac{\sigma}{\Theta} = \frac{H_T - H_L}{H_L + 2H_T} \quad \text{normalized shear}$$

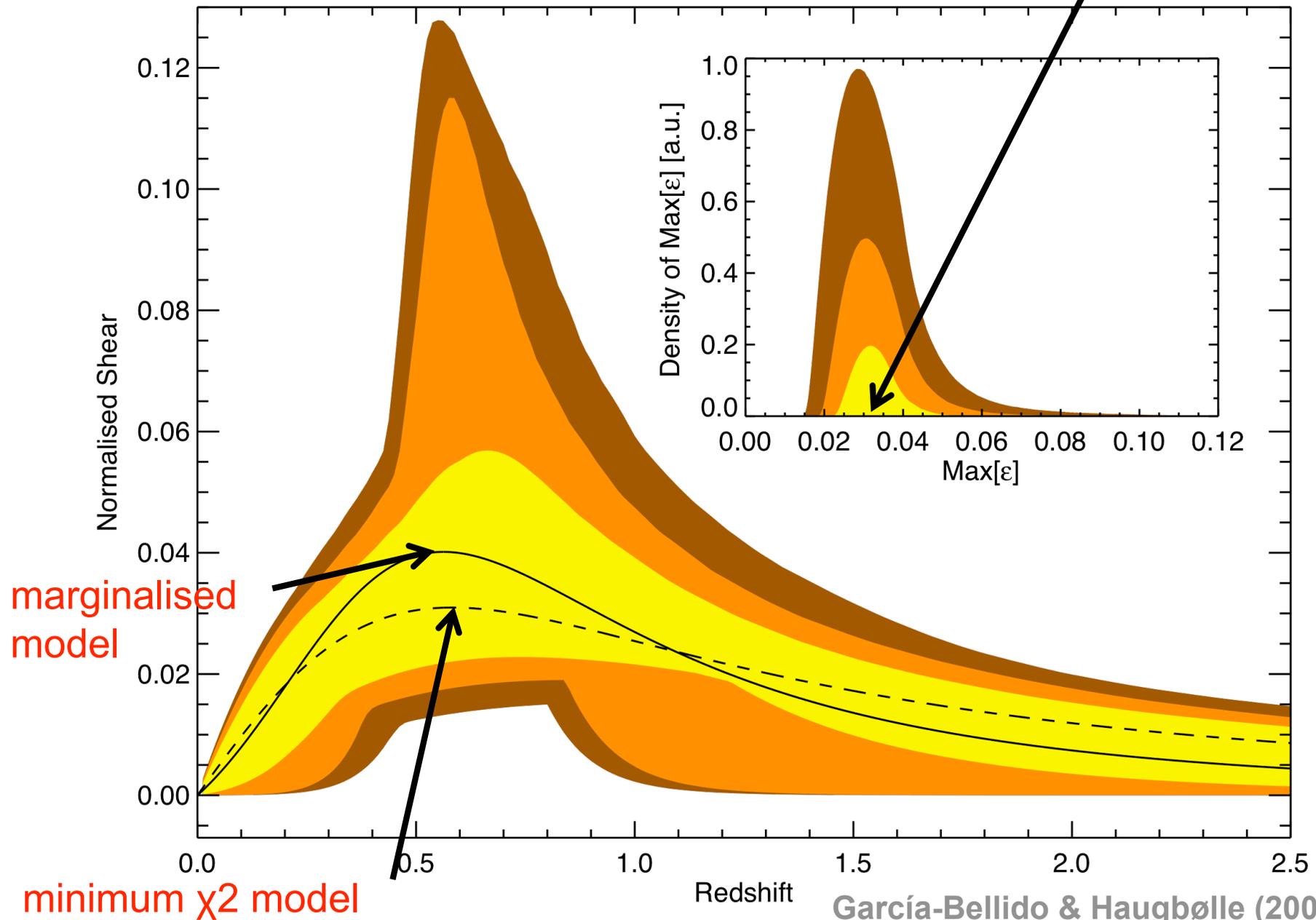
$$\varepsilon(z) = \frac{1 - H_L(z)[(1+z)d_A(z)]'}{3H_L(z)d_A(z) + 2 - 2H_L(z)[(1+z)d_A(z)]'}$$

FRW: $H_L = H_T = H$ shearless

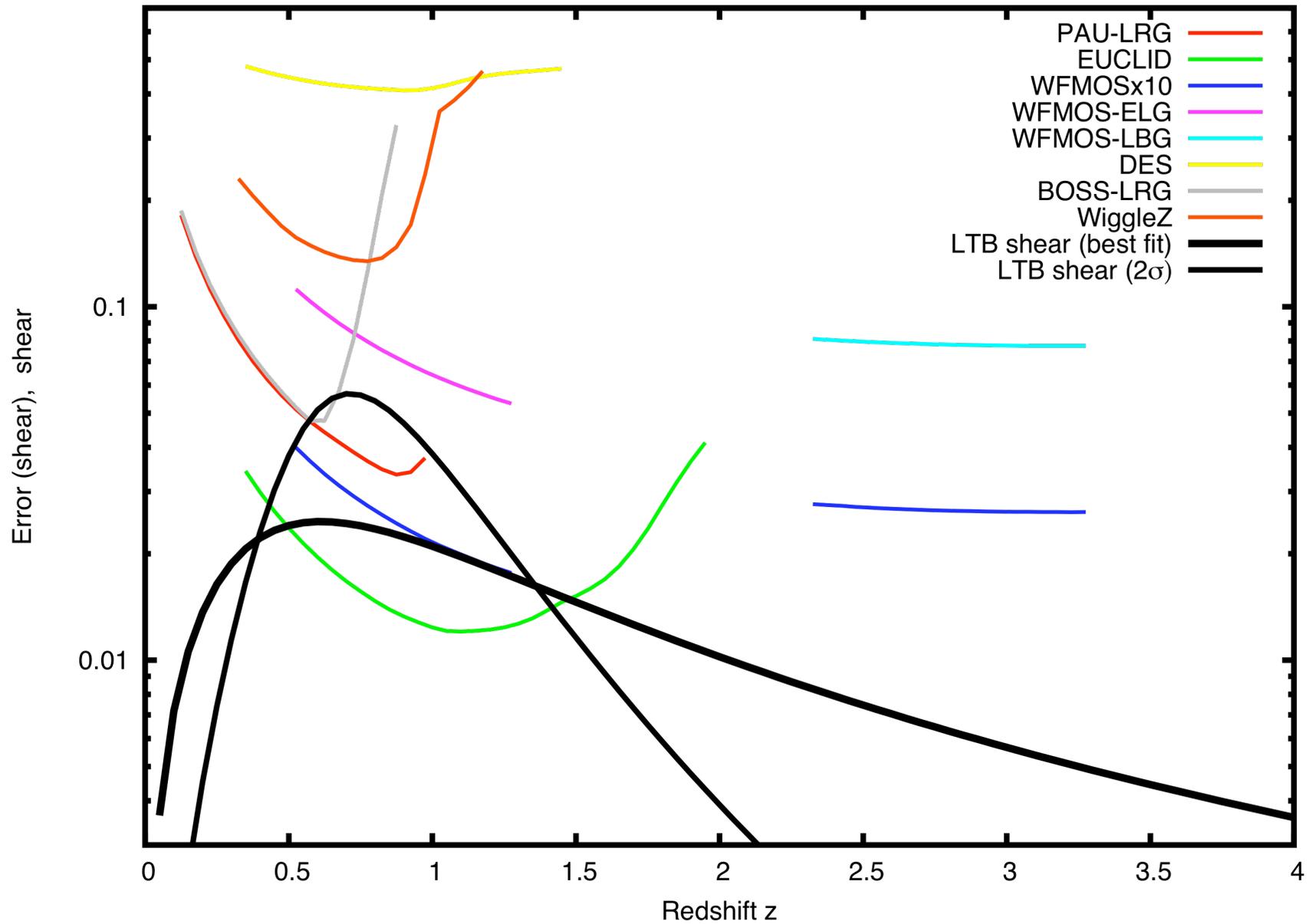
$$(1+z)d_A = \int dz/H(z) \quad \varepsilon(z) = 0$$

Normalized shear

$\epsilon \approx 2 - 5\%$ at maximum



Sensitivity to shear of future surveys



Discussion

- Void models, observationally, seem a real alternative to the standard model. While they break away from the Copernican Principle, they do not need dark energy.
- There is no coincidence problem either: It was there always. The question “Why Now?” becomes “Why Here?”
- A void model with a size of ~ 2 Gpc yields a perfect fit to observations constraining the geometry of the universe.
- The final test will be comparing the model to observations:
 - Cosmic shear + bulk flows near $z \sim 0.5$ (DES, PAU)
 - CMB, and matter power spectra (More theory: ISW)
 - Remote measurements of the CMB: The kinematic Sunyaev Zeldovich effect (ACT, SPT, Planck)