

Top quark physics at lepton colliders

loosely based on presentations at the 2015 **LC top workshop**



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Behind Precision Workshop, CERN, february 2016

Acknowledging input/contributions from:

F. Bach (DESY), W. Bernreuther (RWTH Aachen), A. Hoang (U. Vienna), P. Marquard, P. Ruiz-Femenia (MPI), M. Stahlhofen (DESY)
F. Richard, F. le Diberder, R. Poeschl (LAL Orsay) M. Boronat, J. Fuster, I. Garcia, M. Perelló, E. Ros (IFIC Valencia)



Top quark physics

One of (at least) two SM particles to escape (direct) scrutiny at lepton colliders

It is **important** to know its properties: contributions through loops

- Top mass, width

It is a quark we **can** characterize well: top-anti-top tagging, polarization

- Production asymmetries

If top is part of the hierarchy problem, is the top sector part of the solution too?

- Top quark Yukawa coupling

Is top connected to new physics?

- FCNC decays



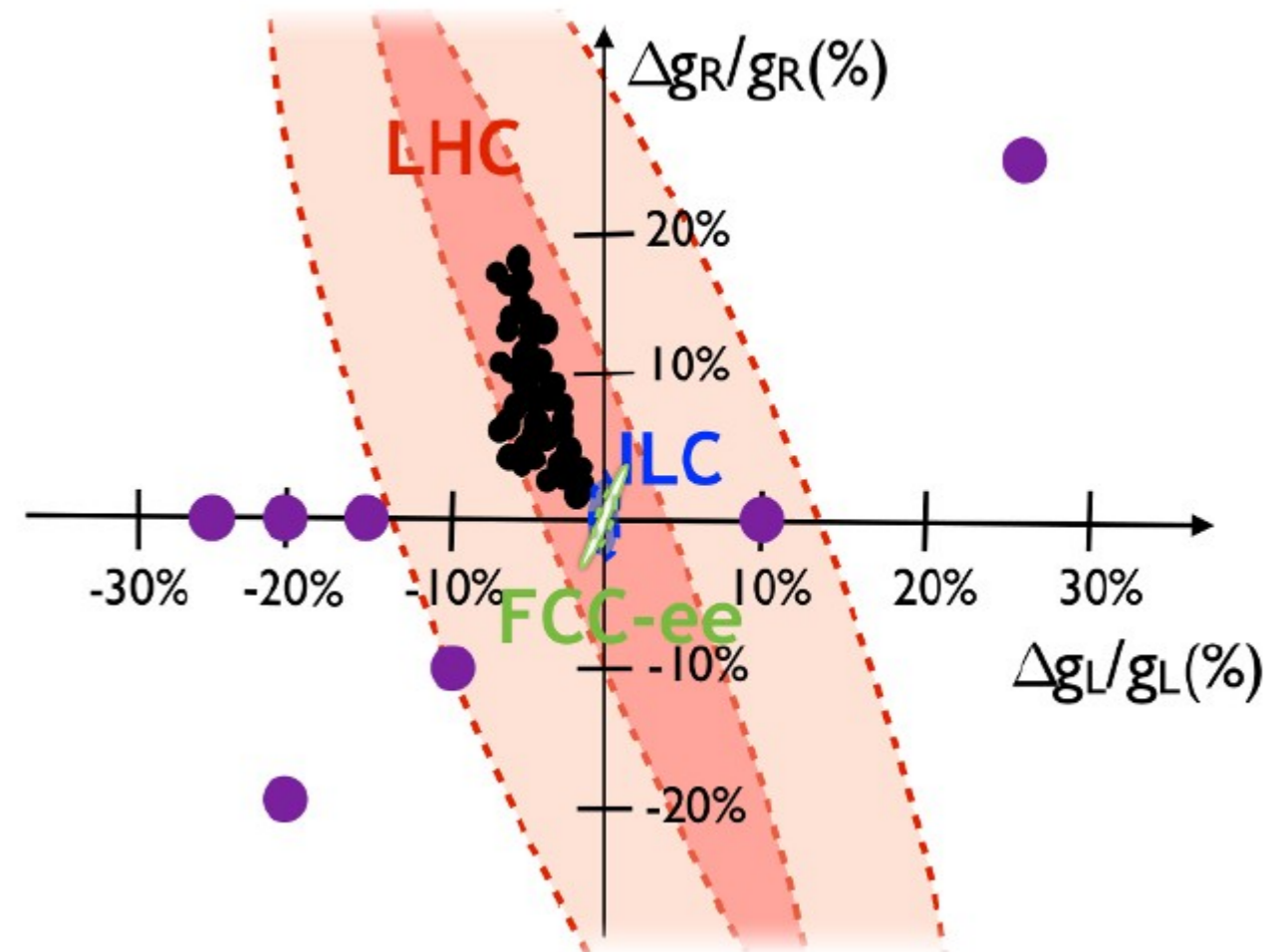
BSM physics

Certain classes of SM extensions predict sizable deviations from the SM prediction for the $t\bar{t}Z$ coupling

Extra dimension models typically yield order 10% deviations for $\Lambda \sim 1$ TeV

See: Stefania de Curtis, this workshop

- 5D models proposed by several authors
Richard, arXiv:1403.2893
- 4D Composite Higgs Model
Barducci, de Curtis, Moretti, Pruna, JHEP 08 (2015)



The SM precision measurement IS the search for new physics

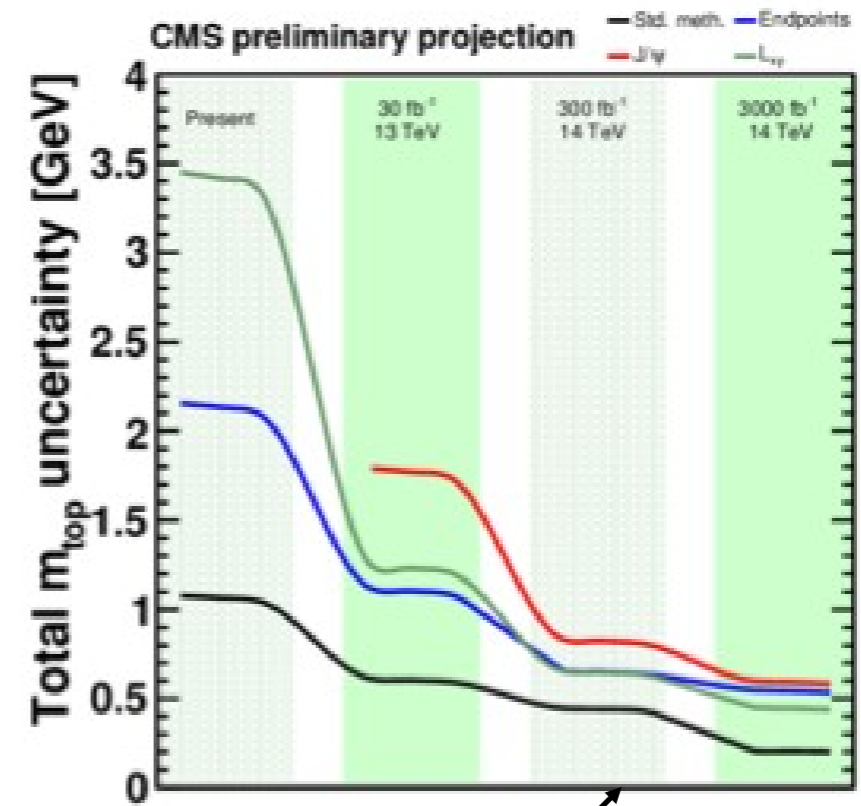
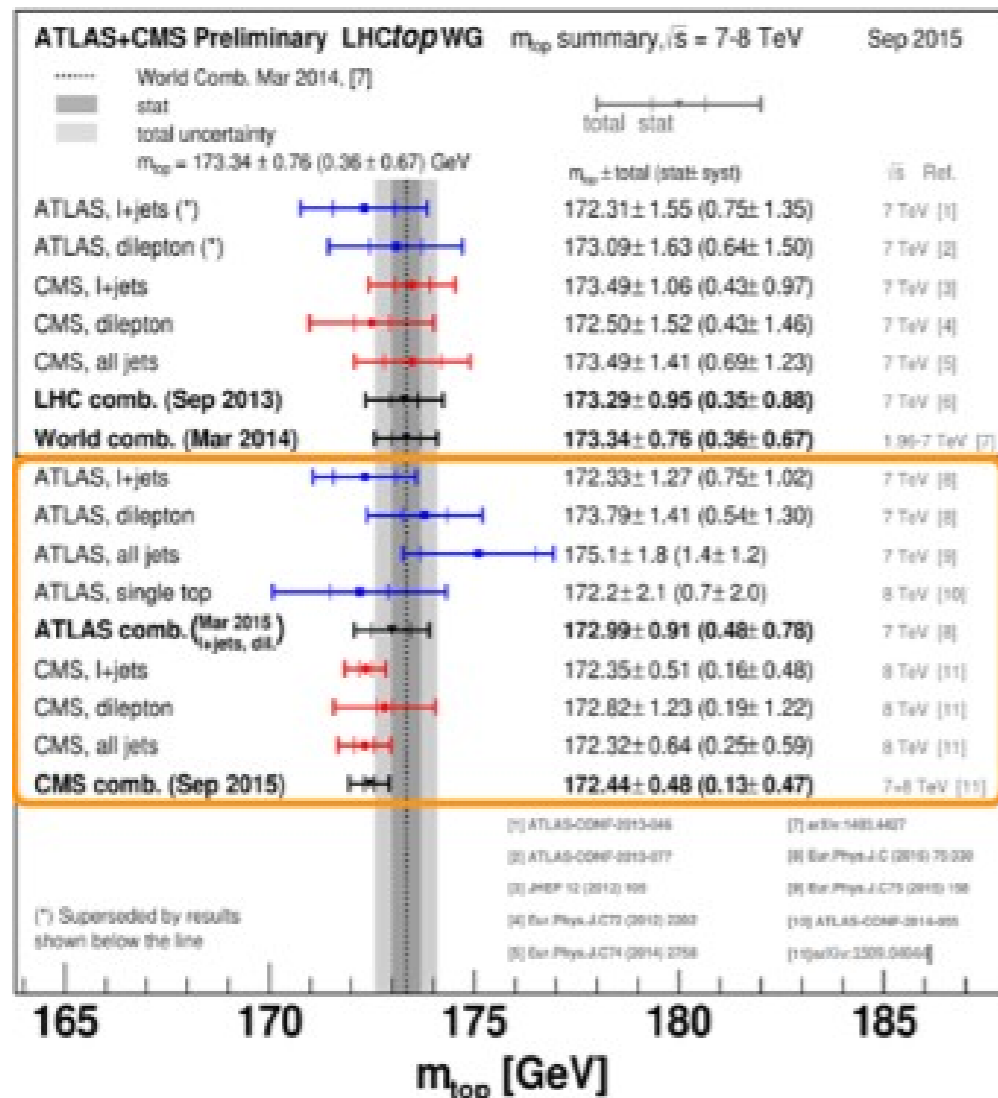
Current status: Top Mass

Hadron colliders (LHC and Tevatron) achieved a precision in the measurement of the top mass of **~ 0.76 GeV in March 2014**

arXiv:1403.4427

Combination of consistent set of measurements from 4 experiments (ATLAS, CMS, CDF and D0)

New results from CMS even more precise
~ 0.5 GeV September 2015

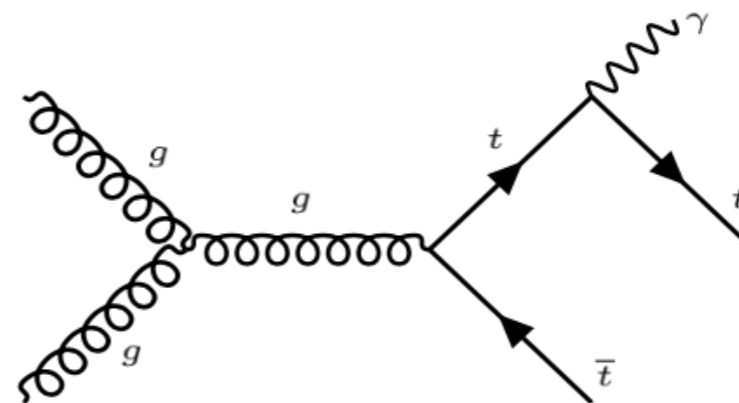
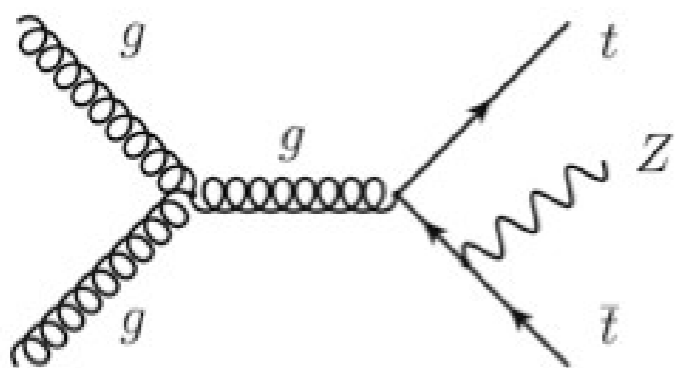


LHC already exceeding prospects
 CMS expects 200 MeV after 3000 fb⁻¹
 (conventional method, CMS-FTR-13-017-PAS)
 based on "assumptions [that] are optimistic but not unrealistic"

Issues with interpretation not accounted for.
 A showstopper? See: Gennaro Corcella



Current status: EW couplings



Complex, multi-channel analysis.

5 σ observation for all top + EW associated production channels!!

	ttW	ttZ	tt γ
ATLAS	5.0 σ ArXiv:1509.05276	4.2 σ ArXiv:1509.05276	5.3 σ (7 TeV) ArXiv:1502.00586
CMS	4.8 σ ArXiv:1510.01131	6.4 σ ArXiv:1510.01131	CMS-PAS-TOP-13-011

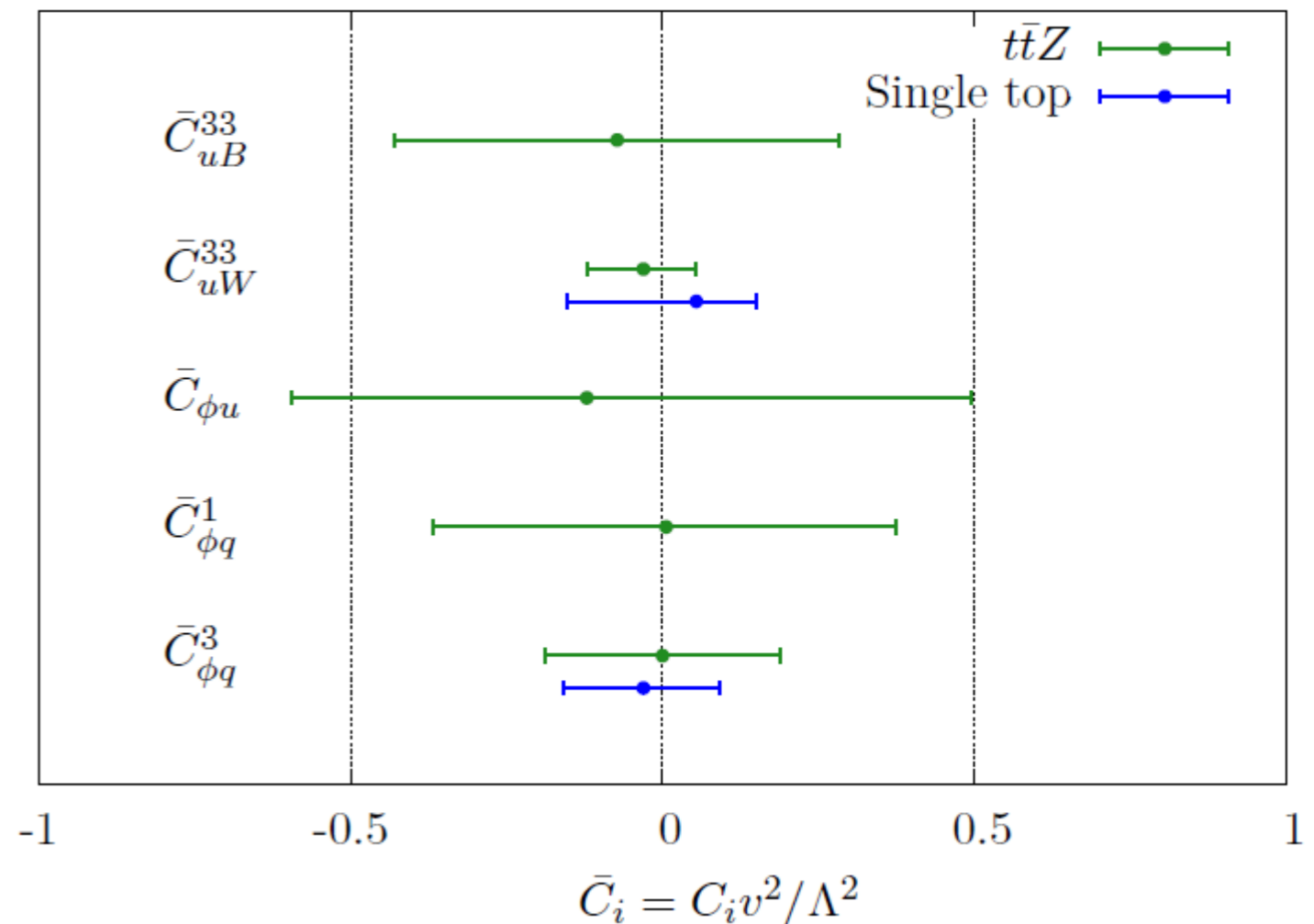
LHC prospects

Data from Tevatron and LHC (from cross-sections to spin correlations) provide precise multi-dimensional constraint

Simultaneous fit to effective operators affecting top quark sector:

ArXiv:1506.08845

ArXiv:1512.03360



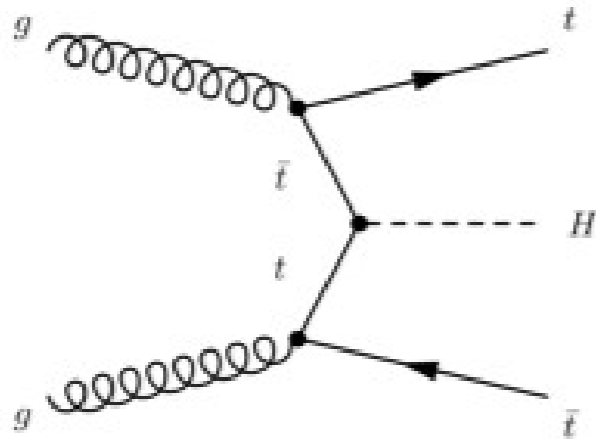
NLO predictions for associated production processes and prospects for full LHC programme

Roentsch and Schulze, arXiv:1501.05939 [hep-ph], JHEP 1407 (2014) 091

See also: Cen Zhang, this workshop

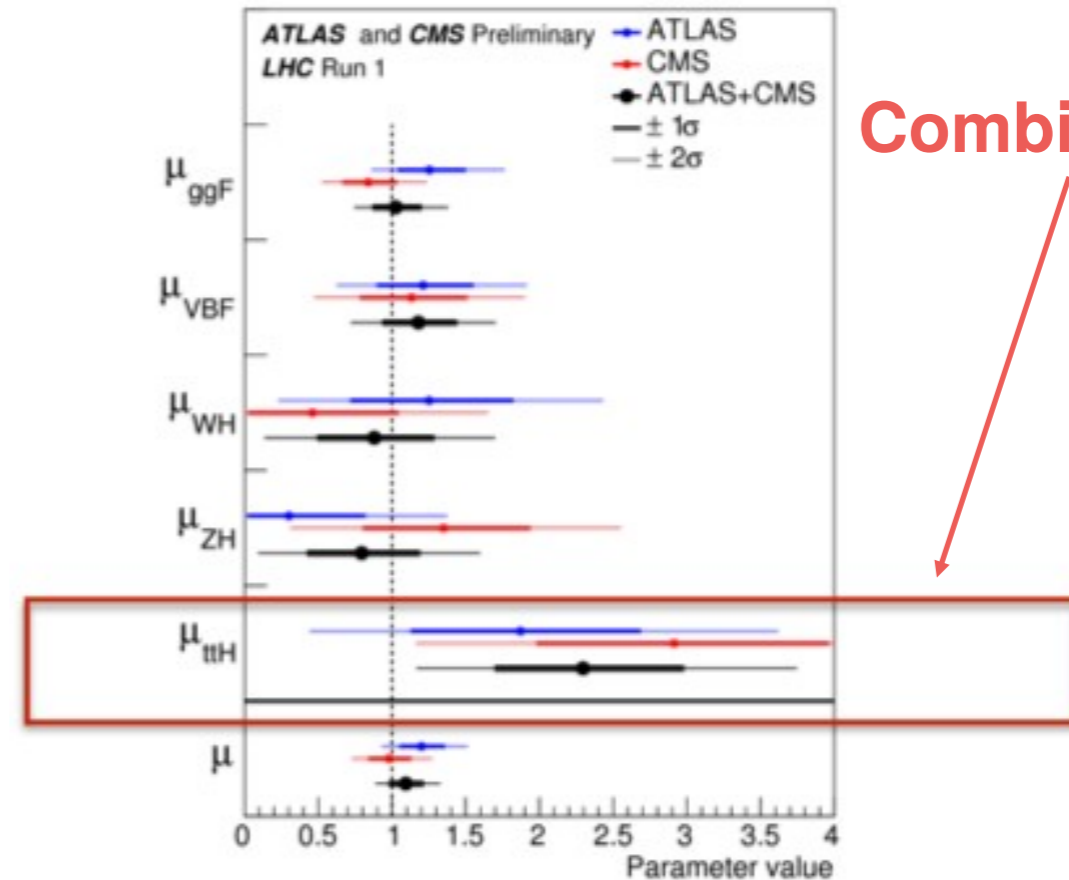


Current status: Yukawa Coupling



ttH searches have been **performed** at the LHC in all main Higgs decay modes at 7 and 8 TeV:

- Best fit signal strength ($\mu = \sigma/\sigma_{SM}$)
 - $\mu_{ttH} = 1.9^{+0.8}_{-0.7}$ - ATLAS
 - $\mu_{ttH} = 2.9^{+1.0}_{-0.9}$ - CMS
 - $\mu_{ttH} = 2.3^{+0.7}_{-0.6}$ - Combined
 - significance - 4.4σ obs (2.0σ exp)
- Combined upper limits on σ/σ_{SM}
 - 3.2 obs (1.4 exp) - ATLAS
 - 4.5 obs (1.7 exp) - CMS



Prospects for full LHC programme:

$K_u \rightarrow 14-15\%$ (300/fb)

$K_u \rightarrow 7-10\%$ (3000/fb) Snowmass Higgs report



Lepton colliders: precise predictions

For theory precision there is nothing like e^+e^-

Continuum

QCD corrections calculated to N²LO

Scale variations at N³LO estimated at ~ 0.3%.

Electroweak corrections are sizable, though.

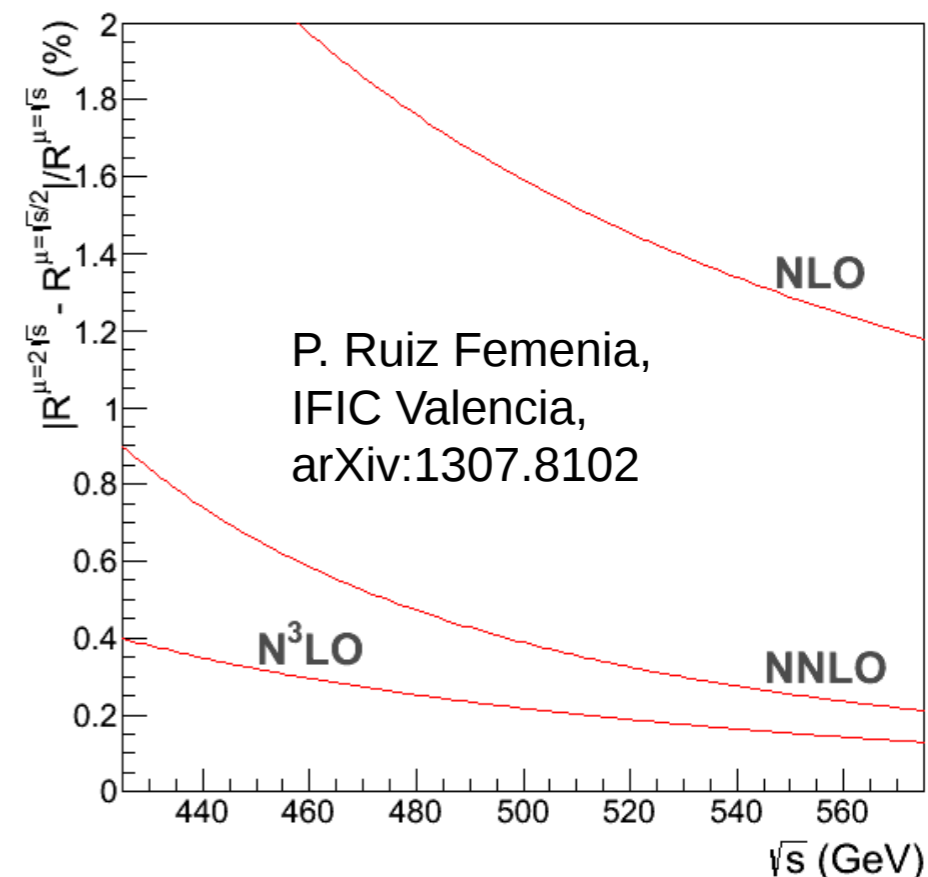
Needed: best, consensuated estimate of theory uncertainty versus \sqrt{s}

Parametric uncertainty:

Uncertainty on top mass/width propagates to x-sec:

- 0.2% at 380 GeV
- 0.1% at 420 GeV

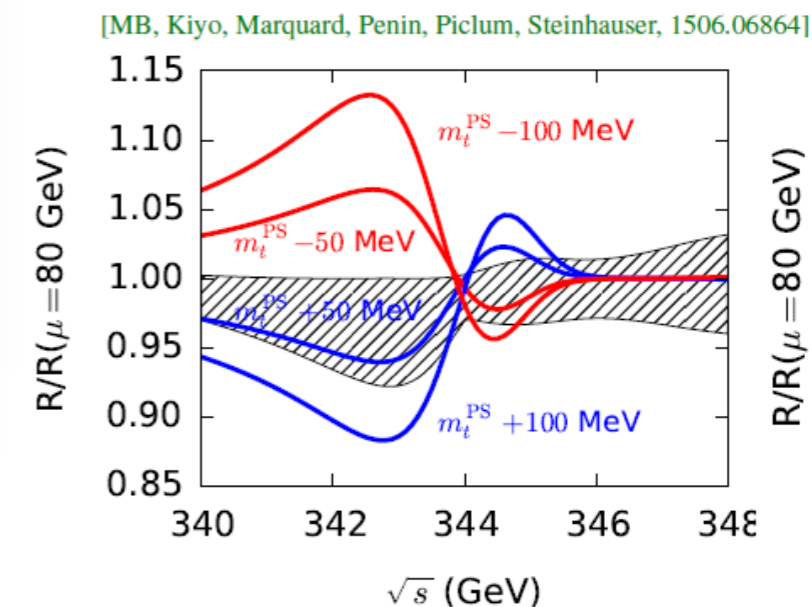
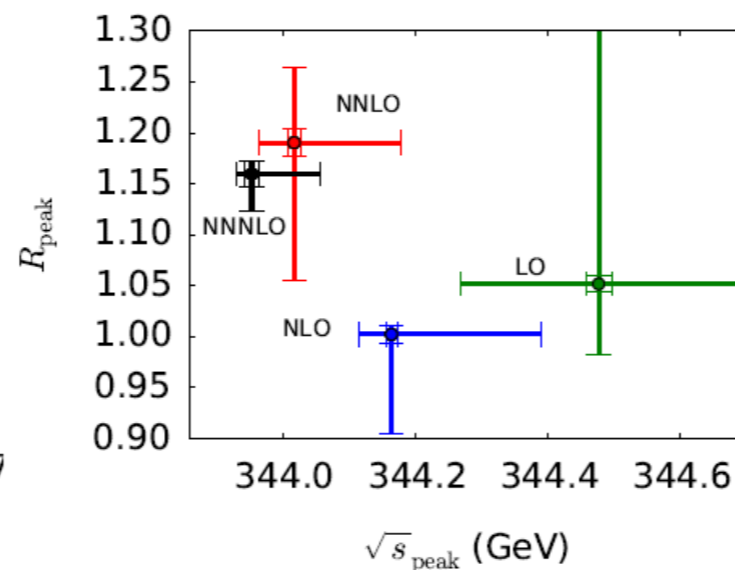
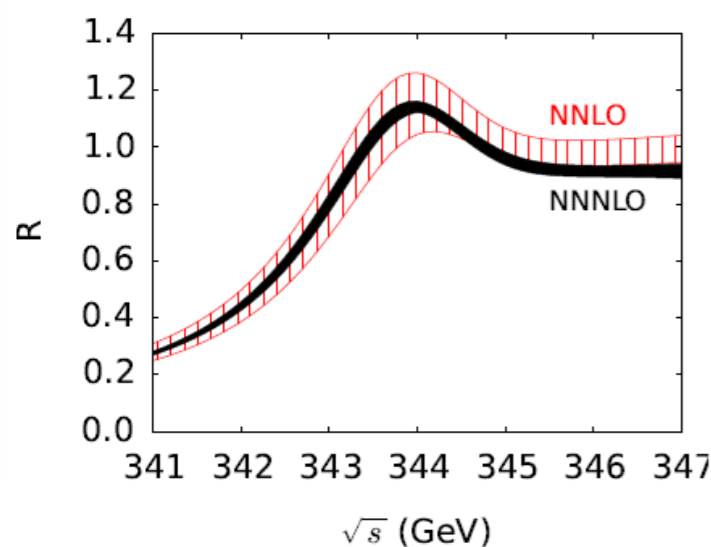
Variation in x-section due to scale variations



Threshold theory

Beneke/Kiyo: N³LO description of $t\bar{t}$ production at threshold

Beneke, Kiyo, Marquard, Penin, Piclum, Steinhauser, 1506.06864 [hep-ph]



Position shift for PS mass: 310 MeV (LO to NLO) 150 MeV (to NNLO) 64 MeV (to NNNLO)
Improvement of factor 3 in uncertainty in peak height.

Alternative approach proposed by Kiyo/Mishima/Sumino: perform calculation directly in terms of the $\overline{\text{MS}}$ mass (corrections LO \rightarrow NLO are large, but rapid convergence, final scale uncertainty seems smaller, arXiv:1506.06542)

See: Matthias Steinhauser, this workshop

Top pair threshold: MC status

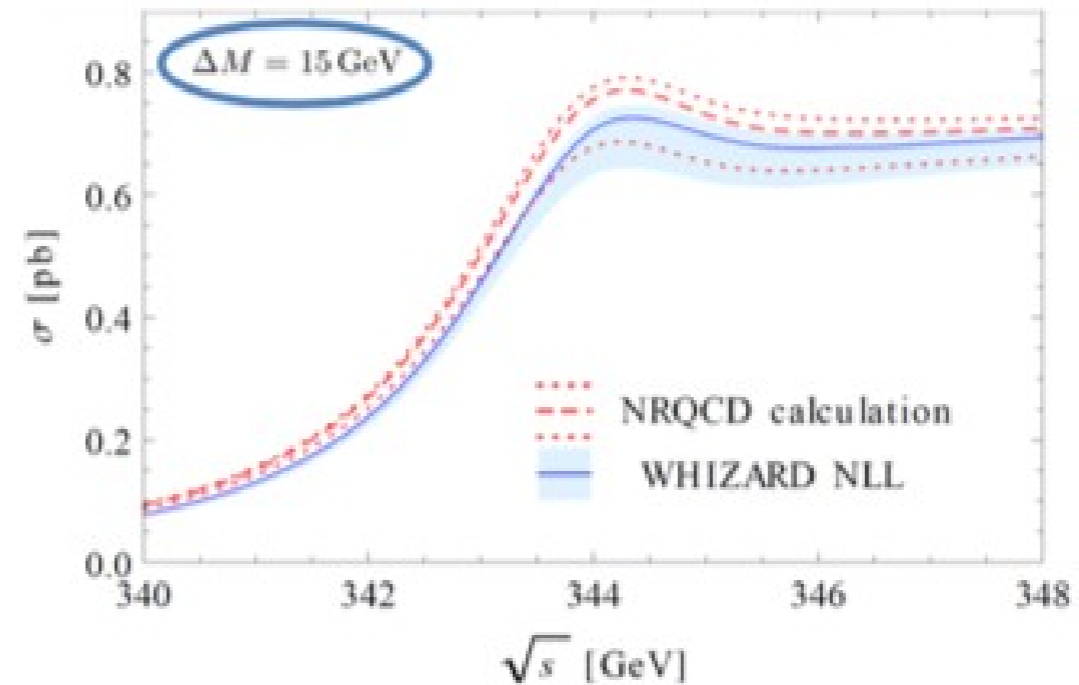
Now available: **NLO simulation of the $t\bar{t}$ threshold** in **WHIZARD** since version 2.2.3

More exclusive observables accessible

asymmetries, momentum distribution

Trivial incorporation of experimental reality:

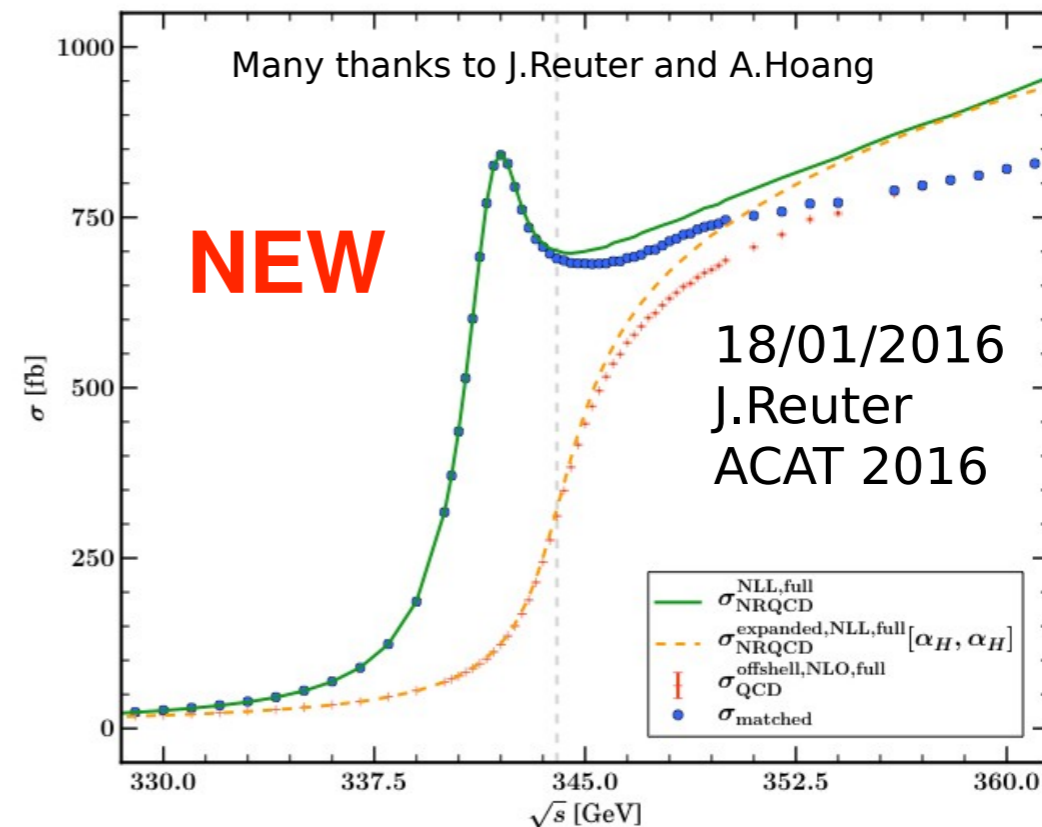
ISR and luminosity spectrum



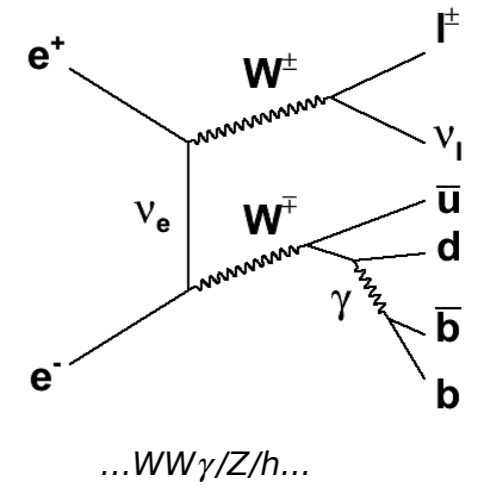
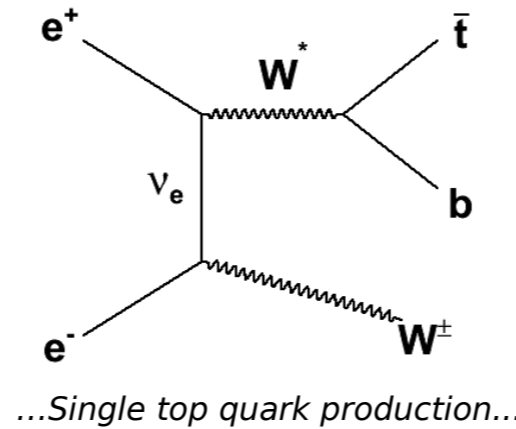
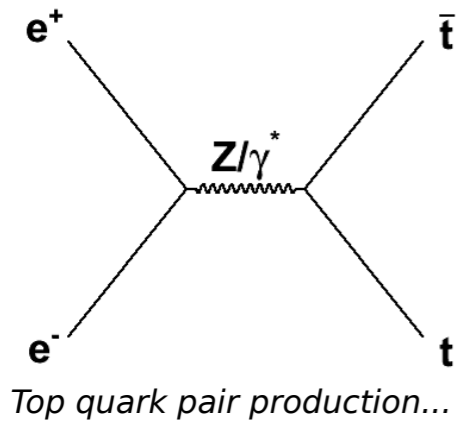
Match threshold & continuum calculations

- Matching procedure in place
- Uncertainty vs. \sqrt{s} in progress

See: Jürgen Reuter, Matthias Steinhauser



Challenge: selection



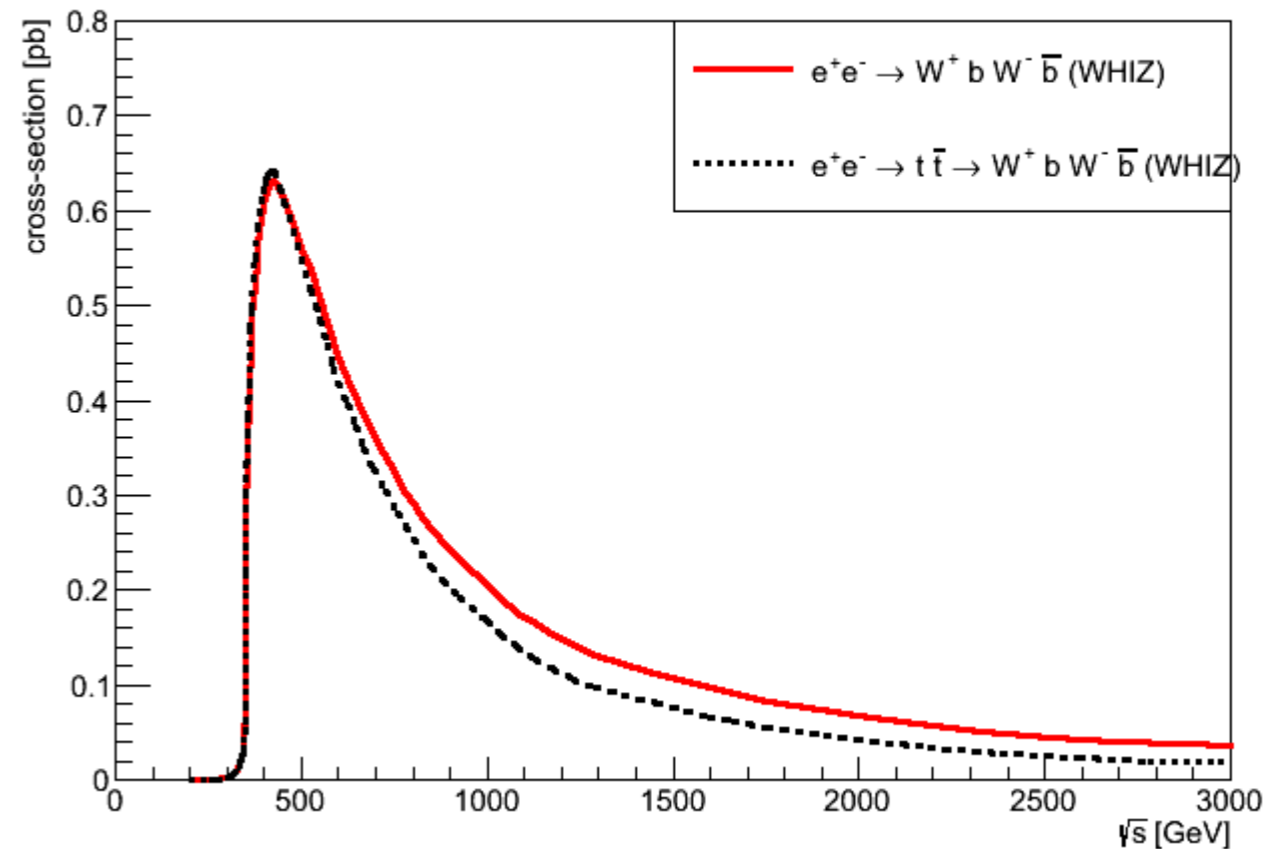
Maximum x-section for pair production ~ 0.6 pb
 peak well above threshold ~ 420 GeV
 Drop in (s-channel) cross-section at higher \sqrt{s}
 partially compensated by higher luminosity

$e^+e^- \rightarrow WbW\bar{b} \rightarrow 6$ fermions is
 “contaminated” by single top production:

- 380 GeV: $\sim 5\%$
- 500 GeV: $\sim 9\%$
- 3 TeV: $\sim 50\%$

As far as we can (at 500 GeV) single top is
 \sim indistinguishable from pair production

See: Garcia, Perello, Ros, Vos, Study of single top production at high energy electron-positron colliders, arXiv:1411.2355



Must measure rate and properties of WbWb production. For a precise comparison of data and prediction more theory work is needed!

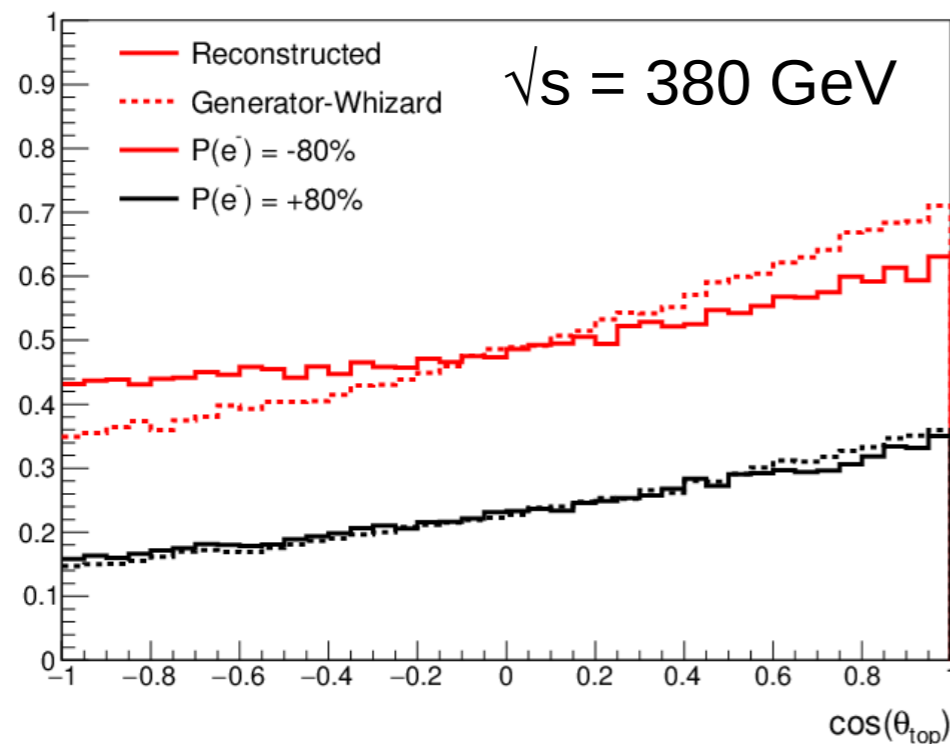


Challenge: reconstruction

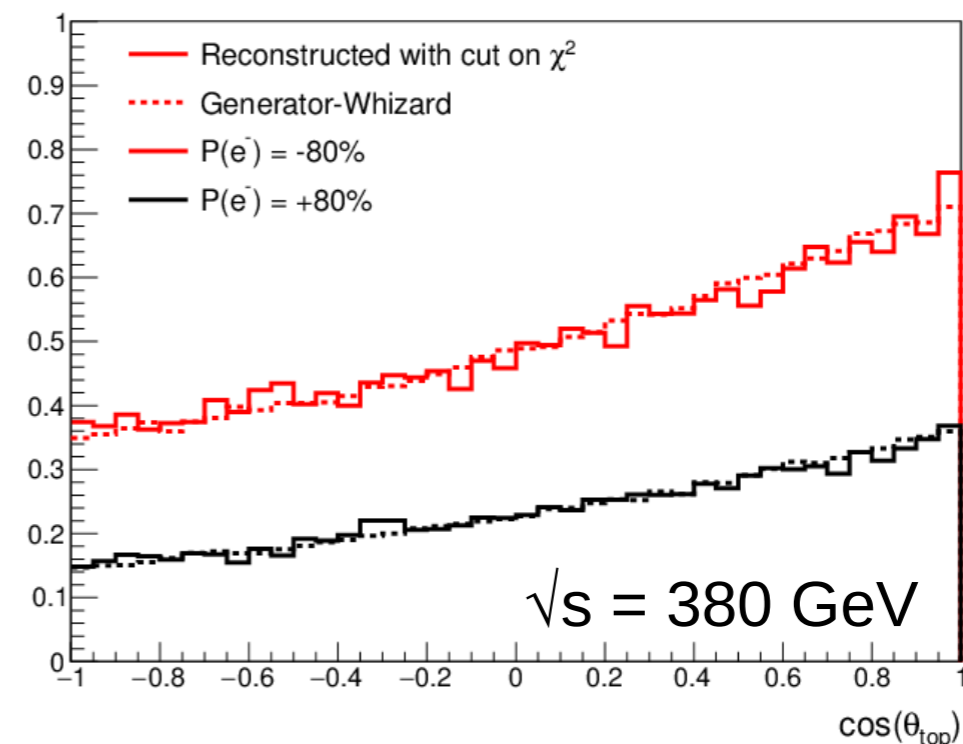
$t\bar{t}$ pairs at rest form a quite different final state than in at 500 GeV

- Full simulation results for CLIC@380 appearing (CERN + IFIC)
- A_{FB} much smaller and migrations due to ambiguity in b-W pairing more severe at 380 GeV than at 500 GeV (esp. for -80%, +30% polarization)
- Turning the crank on the usual machinery – a very tight cut on reconstruction quality – works at a rather high prize in statistics (and quite possibly modelling systematics)

Full simulation, “standard” reconstruction



Same + cut on reconstruction quality χ^2



Challenge: Boosted top quarks

TeV top quarks in CLIC high energy phase are “an entirely different beast”

- available statistics

- s-channel process: drop in x-section not compensated by increase in luminosity

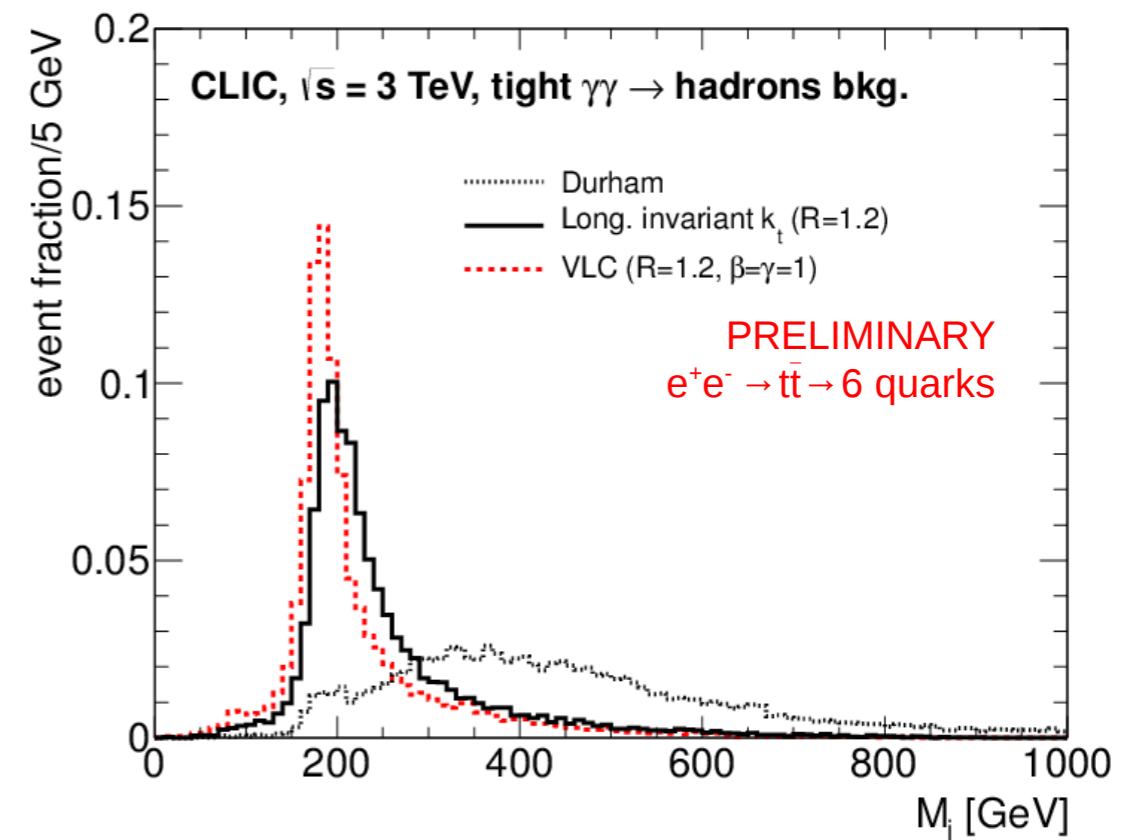
- selection

- What to do with the low-energy tail due to ISR and beam energy spread tail?
- Top-tagging: very striking signal, small backgrounds → high efficiency?
- Fat jet substructure to replace fermion counting? ($t\bar{t}$ – WW – $q\bar{q}$ separation)

- reconstruction

- no ambiguity for highly boosted tops

systematic comparison just starting



FCNC top decays: $t \rightarrow c h$

F. Zarnecki: Measurement of FCNC top decays at ILC/CLIC studied at parton level.

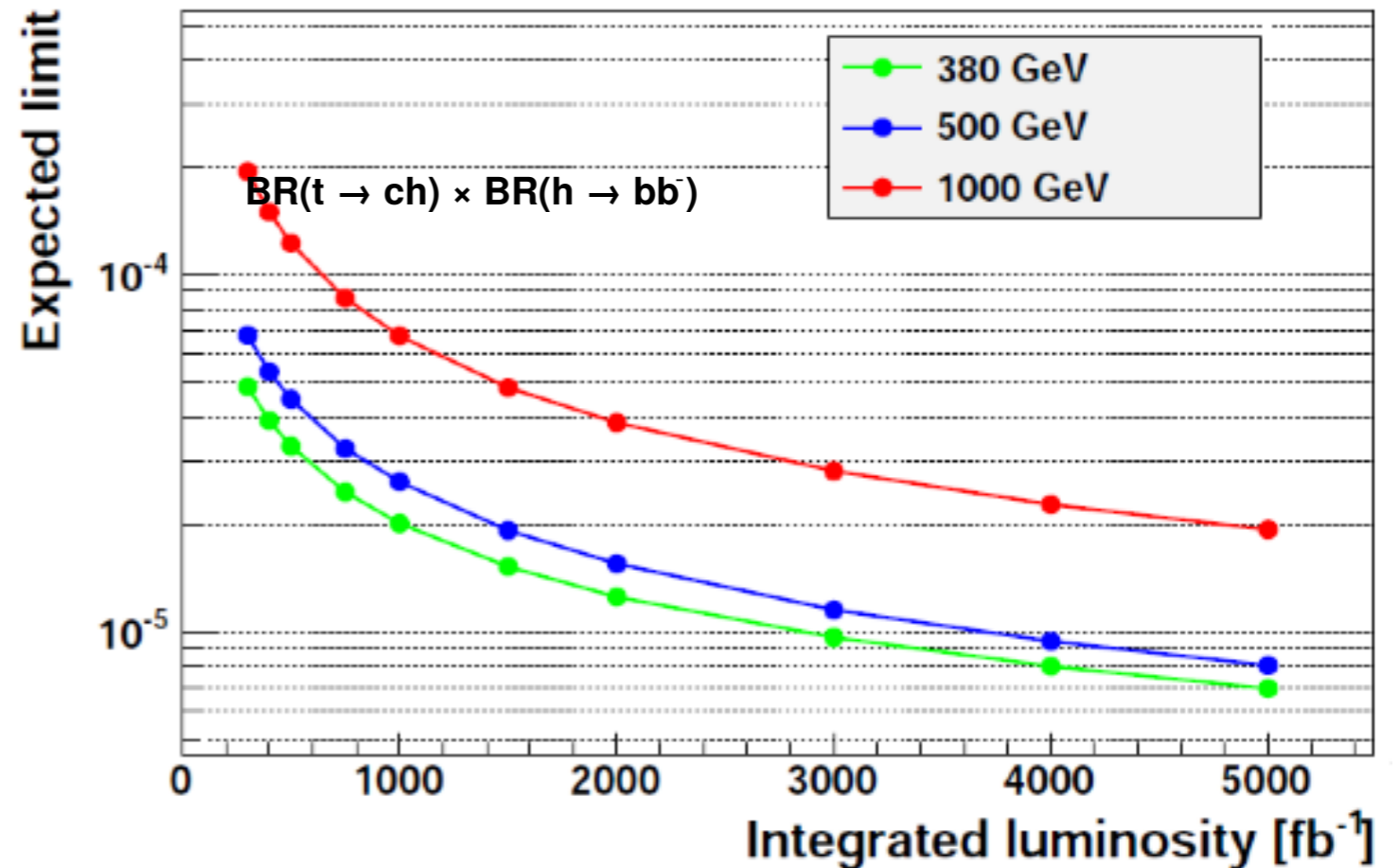
Top workshop Valencia July 15

<https://indico.cern.ch/event/381148/session/5/contribution/4/attachments/759420/1674930/toplc2015.pdf>

Decay $t \rightarrow c h$ is most interesting:

- well constrained kinematics
- test of Higgs boson couplings
- seems to be most difficult for LHC

Two Higgs Doublet Model (2HDM)
as a test scenario



Expected limits on $BR(t \rightarrow c h) \times BR(h \rightarrow b b)$ $\sim 10^{-5}$

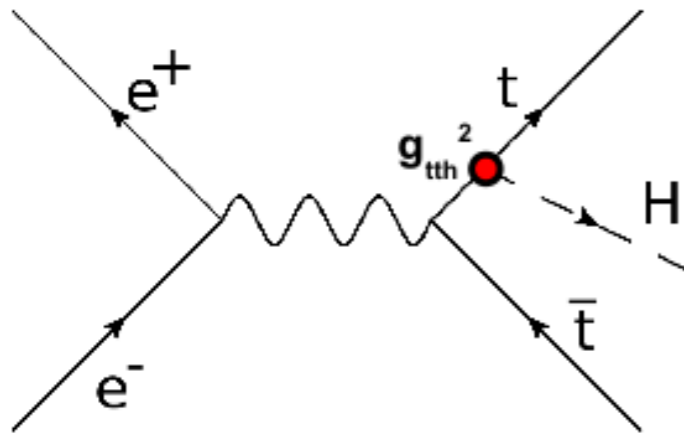
depending on the energy, luminosity and detector parameters in a H-20 LC full program

Order of magnitude improvement wrt Snowmass expectation for LHC + lumi upgrade



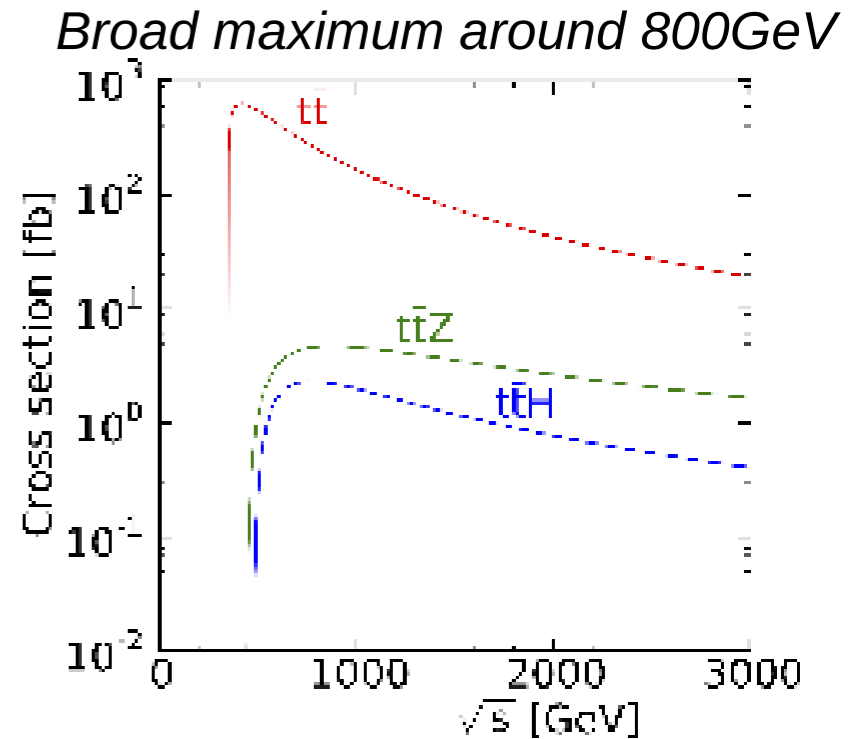
Top Yukawa coupling: ttH at LC

The top Yukawa coupling g_{tth} can be measured directly



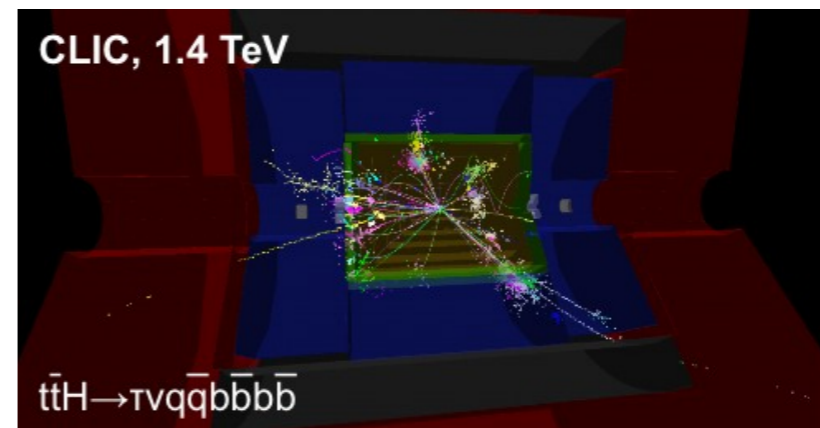
$$\frac{\Delta g_{tth}}{g_{tth}} = c \cdot \frac{\Delta \sigma}{\sigma}$$

No Higgsstrahlung: $c = 0.50$
 ILC 1 TeV: $c = 0.52$
 CLIC 1.4 TeV: $c = 0.53$



Recent studies based on full detector simulation

500 GeV, ILC (ILD):
 Yuji Sudo
1 TeV, ILC (ILD & SiD):
 Tony Price, Ph.R.,
 Jan Strube, Tomohiko Tanabe
1.4 TeV, CLIC (CLIC_SiD):
 Sophie Redford, Ph.R., Marcelo Vogel



About **4% precision on the top Yukawa coupling** achievable with 1ab^{-1}

Collider	LHC		ILC	ILC	CLIC
CM Energy [TeV]	14	14	0.5	1.0	1.4
Luminosity [fb^{-1}]	300	3000	1000	1000	1500
Top Yukawa coupling κ_t	(14 – 15)%	(7 – 10)%	10%	4%	4%

from
[arXiv:1311.2028](https://arxiv.org/abs/1311.2028)

Talk by Ph.Roloff at TopLC
 2015 - Valencia



Top mass from threshold scan

Threshold shape depends strongly on mass & width.
Normalization sensitive to α_s and top Yukawa coupling.

Kuhn, Acta Phys.Polon. B12 (1981) 347

Extract 1S/PS mass from scan (10 x 10/fb):

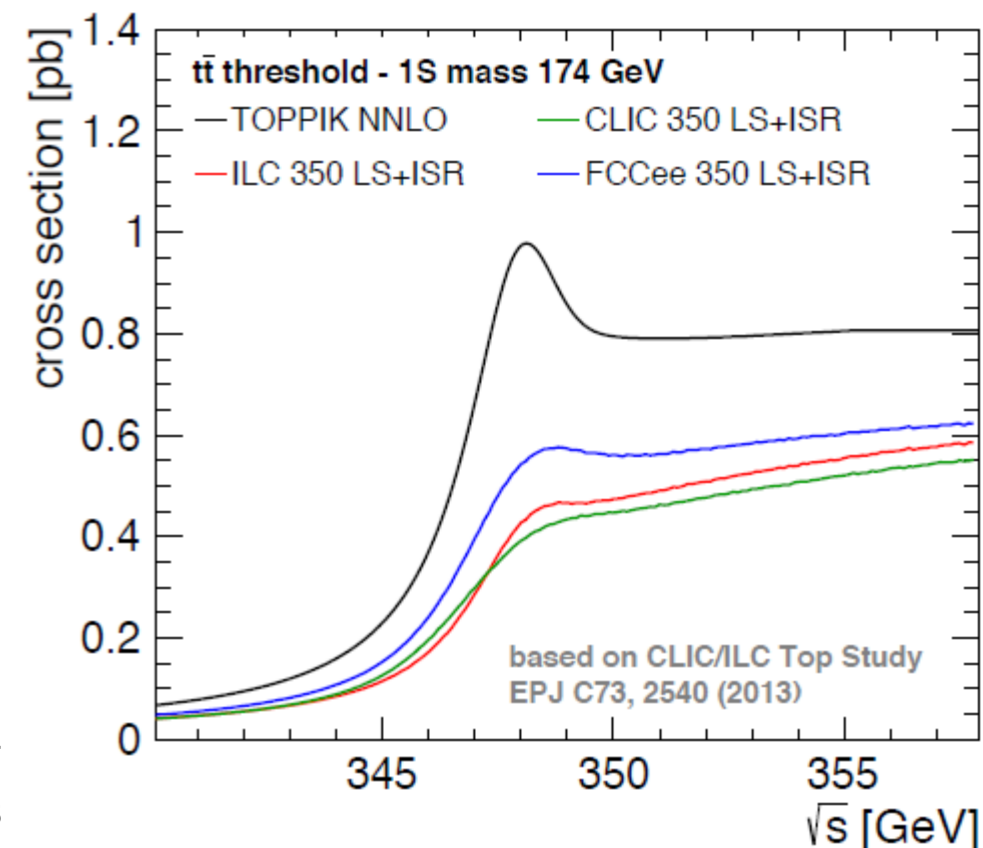
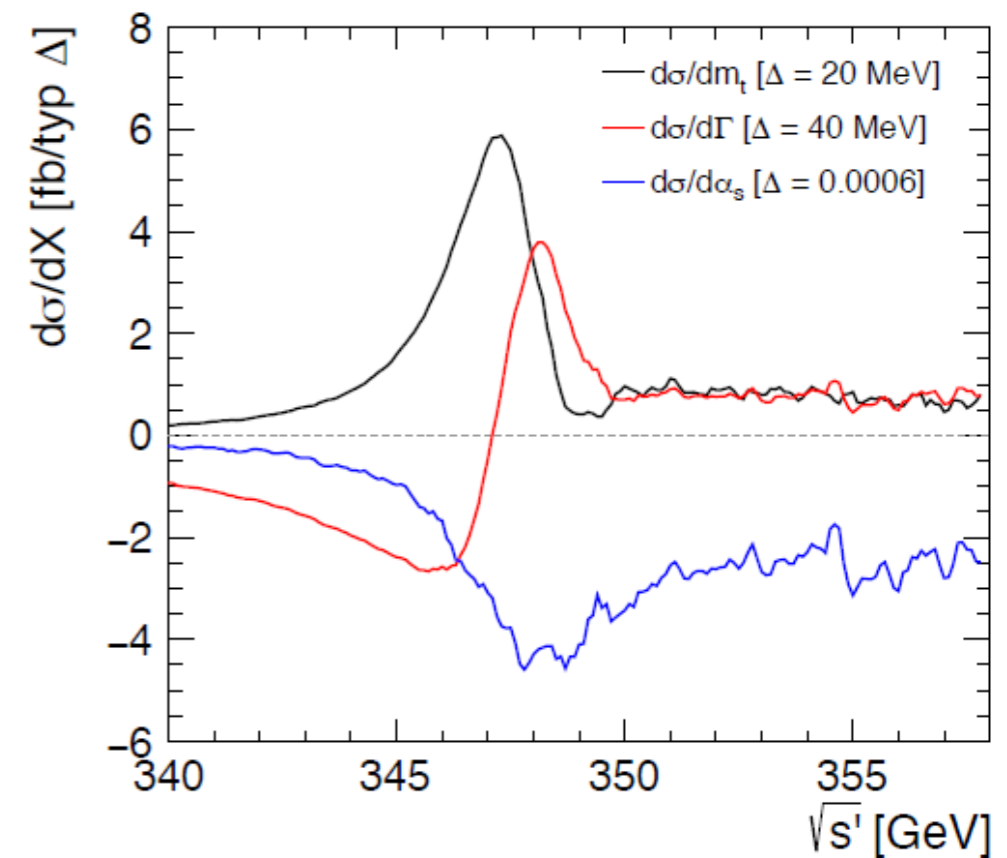
Martinez, Miquel, EPJ C27, 49 (2003)

Seidel, Simon, Tesar, Poss, EPJ C73 (2013)

Horiguchi et al., arXiv:1310.0563

Minor differences due to beam energy spectra of
ILC, CLIC and FCC-ee

Luminosity spectrum can be precisely
reconstructed using



Systematic uncertainties - theory

Extract mass with NNNLO calculation:

30 MeV theory uncertainty on 1S mass (M. Beneke/F. Simon, in progress)

Theory uncertainty in conversion from 1S to $\overline{\text{MS}}$ scheme:

3-loop calculation $\rightarrow \sim 100$ MeV

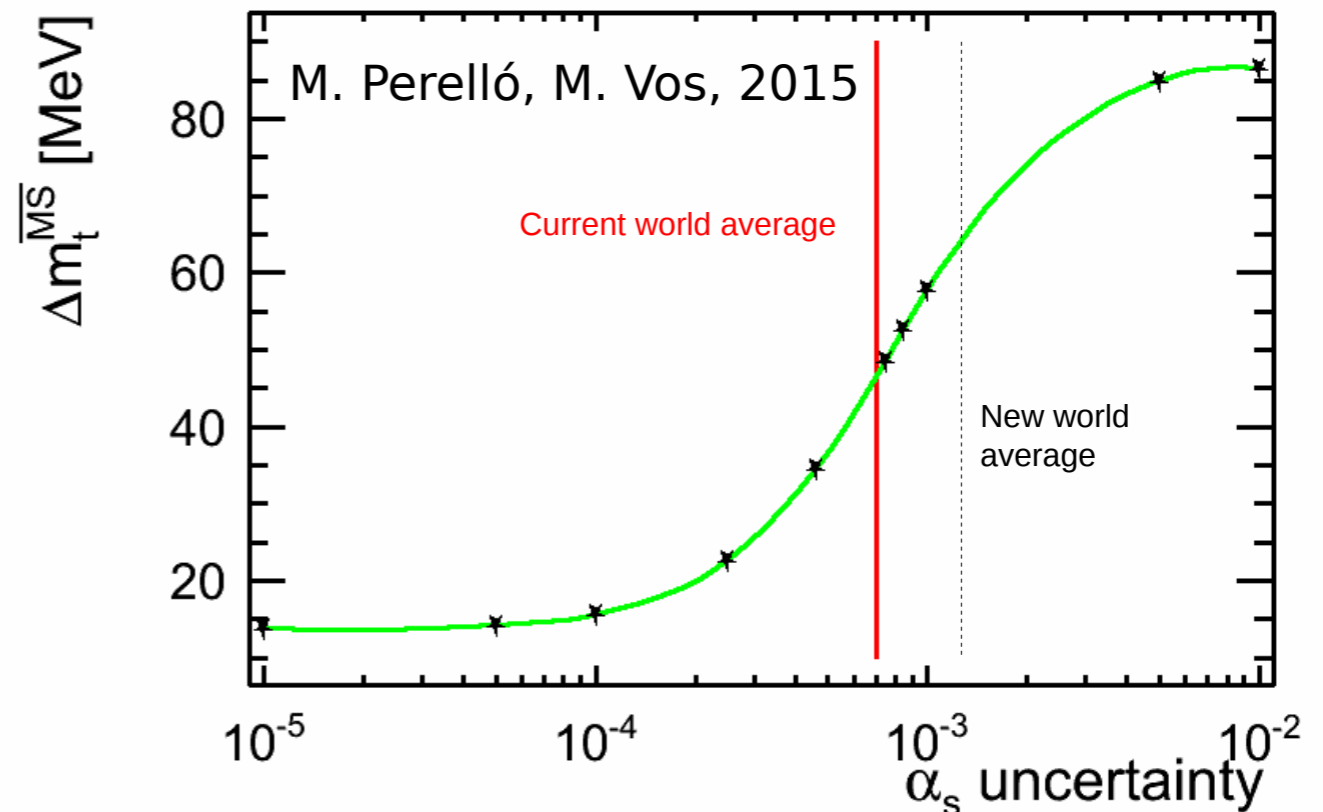
4-loop calculation $\rightarrow < 10$ MeV

(P. Marquard et al., [arXiv:1502.01030](https://arxiv.org/abs/1502.01030), PRL114 (2015))

Uncertainty on strong coupling constant strikes twice:

- as a degree of freedom in the fit to extract 1S mass (δM^{1S} goes from 12 MeV \rightarrow 42 MeV)
- as a parametric uncertainty in the 1S \rightarrow $\overline{\text{MS}}$ conversion

Top quark mass precision vs. prior knowledge of strong coupling strength



Top mass uncertainties

Statistical uncertainty:

Assuming $10 \times 10 \text{ fb}^{-1}$ → 18 MeV (*F. Simon, LCWS15*)
(depending on polarization and fit details several authors find 16-30 MeV)

Experimental systematic uncertainties:

5% uncertainty non- $t\bar{t}$ bkg → 18 MeV (*Seidel, Simon, Tesar, Poss*)
Single top “contamination” → < 30 MeV (*Boronat et al., arXiv:1411.2355*)
 10^{-4} precision on \sqrt{s} → 30 MeV (*Seidel, Simon, Tesar, Poss*)
Realistic uncertainty on lumi-spectrum → 10 MeV (*Sailer & Poss, EPJC (2014) 74:2833, F. Simon, AWLC14, arXiv:1411.7517*)

Theory uncertainty in 1S mass extraction:

Evaluation at NNNLO → 32 MeV? (*F. Simon, LCWS15*)

Theory uncertainty from M_S mass conversion:

4-loop calculation → 10 MeV? (*Marquard et al.*)
 α_s parametric uncertainty → 12-42 MeV (*M. Perelló*)

**With some faith in the progress of lattice QCD, 50 MeV seems like a reasonable goal
A quark mass to a precision of 3 parts in 10.000!!!**

Yukawa at threshold

Ishikawa et al., arXiv:1310.0563:

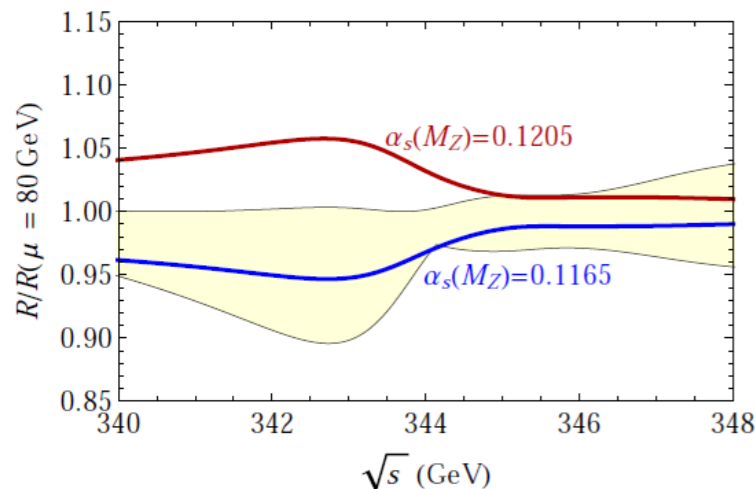
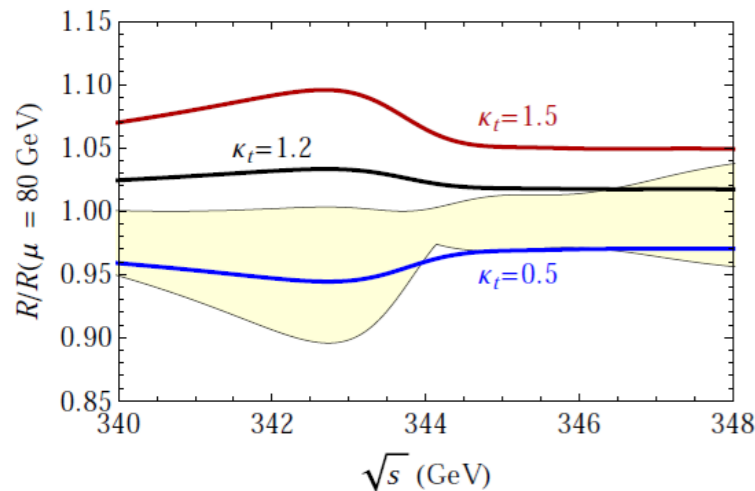
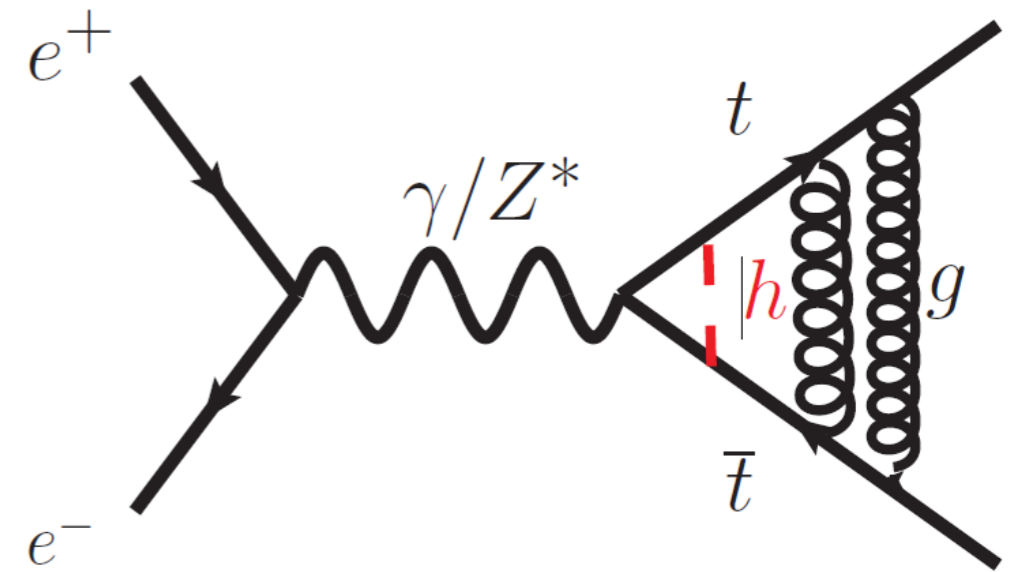
consider several observables (σ , A_{FB} , p)

two polarizations, 220 fb⁻¹ in total

extract properties from simultaneous fit

- $\Delta M \sim 16 \text{ MeV}$
- $\Delta \Gamma \sim 21 \text{ MeV}$
- $\Delta y \sim 4.2 \%$

Stat. Uncertainty only



Enhancement of 9%

~ independent of \sqrt{s} ... no shape information...

Feature is nearly degenerate with α_s

Have to assume very good α_s

NNNLO uncertainty approx. 3%

Theory uncertainty today: 18%

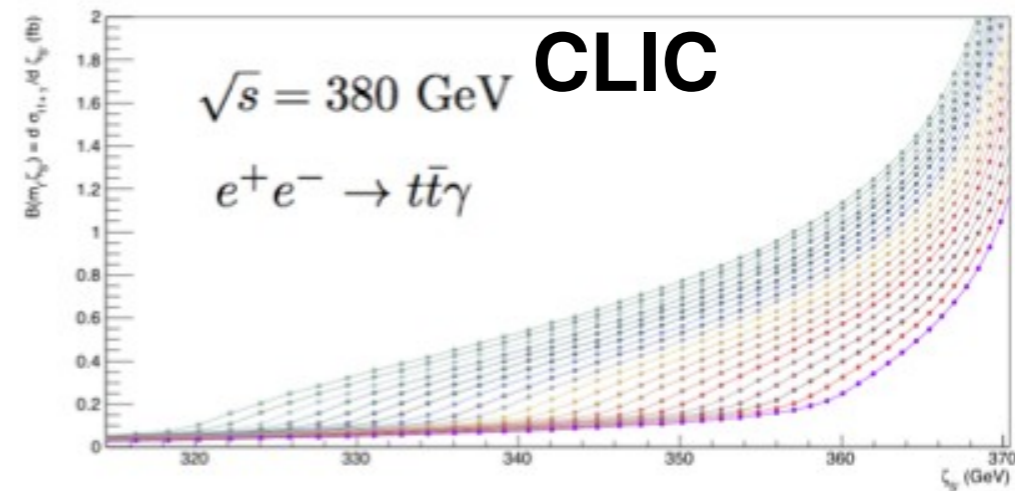
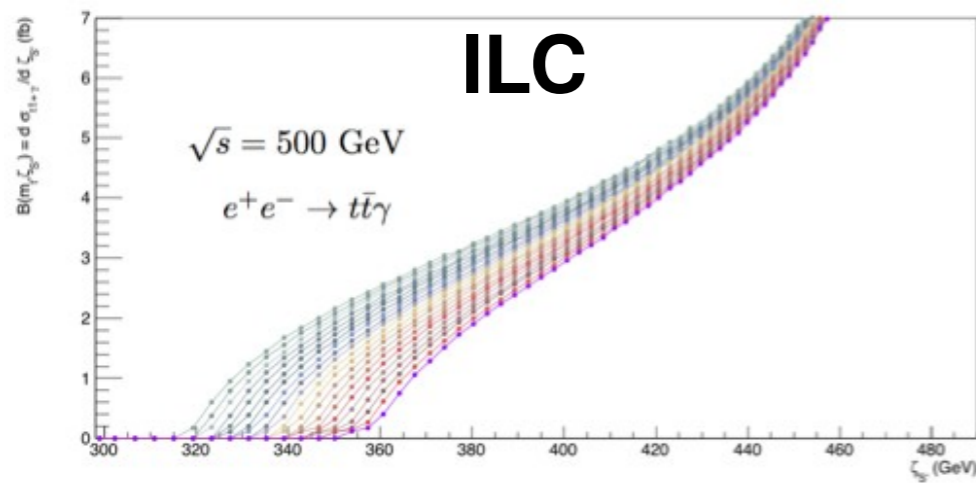
Beneke et al., Nucl. Phys. B899 (2015) 180-193: "Our results show that once theoretical uncertainties are taken into account, it is unlikely that such a high precision [i.e. 4.2%] can be achieved."

Top mass measurements: Alternative techniques

LC scenarios start above threshold (ILC@500GeV, CLIC@380GeV) → first measurement top mass

Extraction of the top quark mass from the differential $t\bar{t}\gamma$ and $t\bar{t}g$ cross-section versus s'

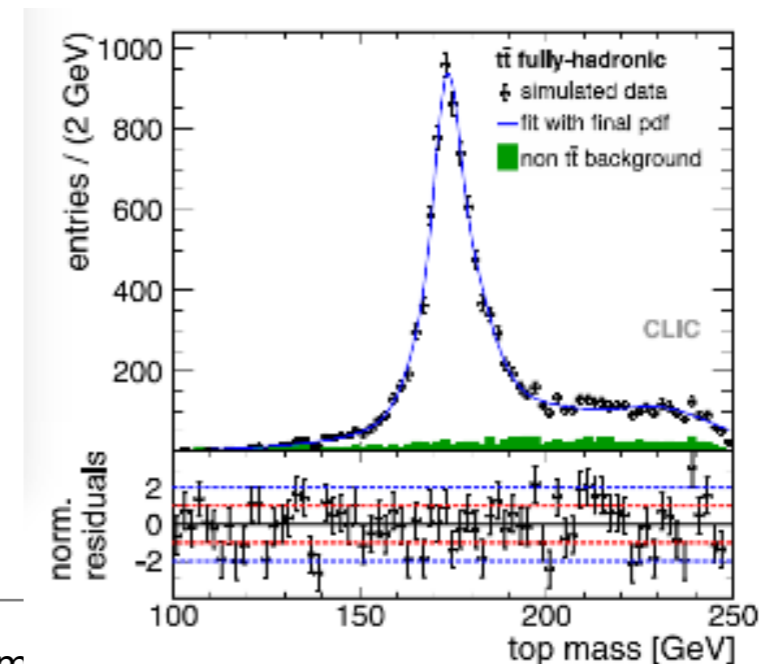
Precision seems competitive for $\sqrt{s} \sim 400$ GeV *Boronat, Fuster, Gomis, in preparation*
(cf. $m(b)$ at $m(Z)$ at LEP, EPJC73 (2013) 2438, ATLAS-CONF-2014-053)



Conventional measurement on top decay products

80 MeV stat. precision at 500 GeV
→ input to clarify MC mass interpretation

Seidel, Simon, Tesar, Poss, EPJ C73 (2013)



Top quark couplings: TDR times

measure

$$\sigma(+)\quad A_{FB}(+)$$

$$\sigma(-)\quad A_{FB}(-)$$

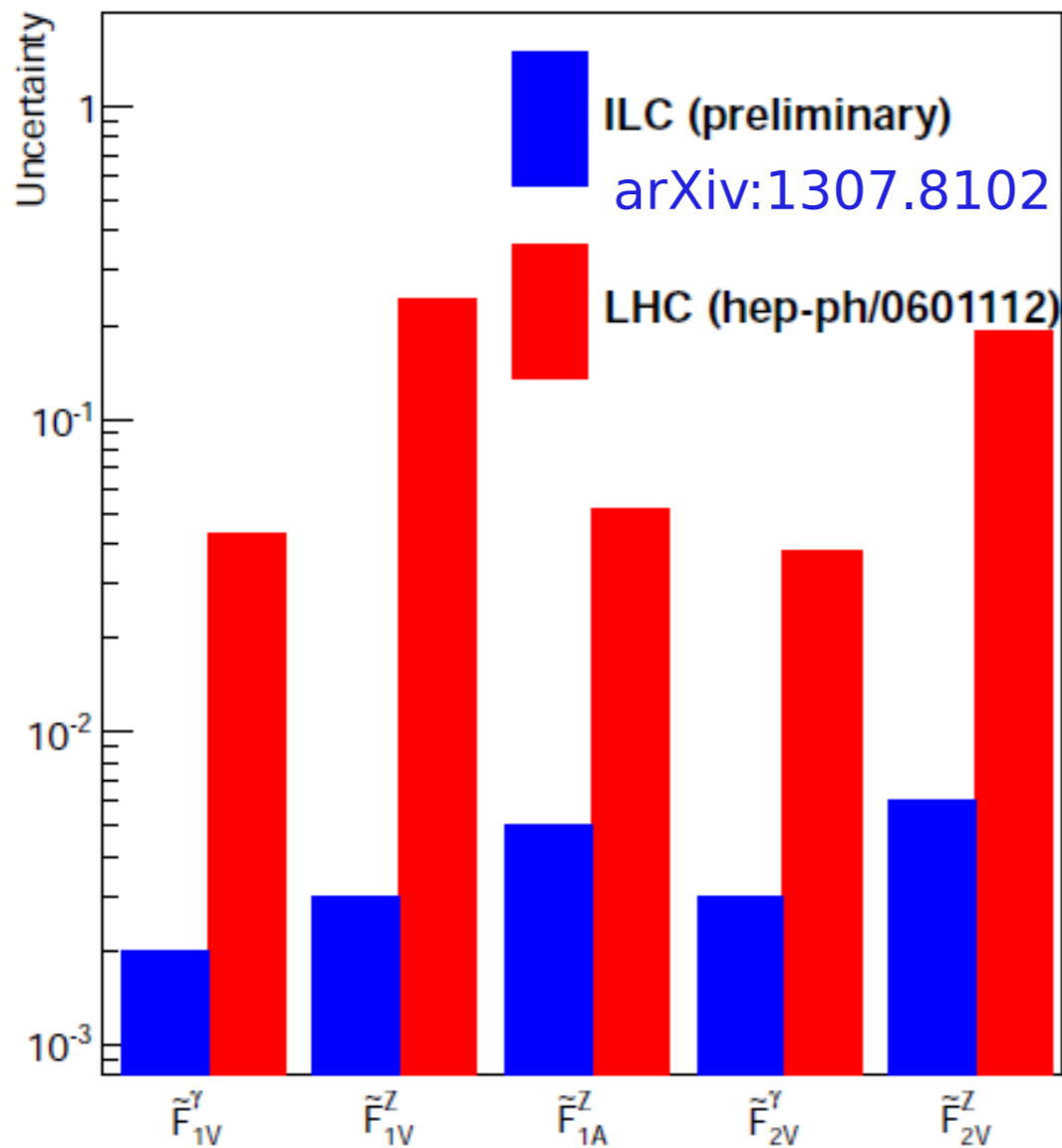
extract

$$\left. \begin{array}{l} (+ = e_R^-) \\ (- = e_L^-) \end{array} \right\} \Rightarrow \left\{ \begin{array}{l} F_{1V}^\gamma \quad * \quad F_{2V}^\gamma \\ F_{1V}^Z \quad F_{1A}^Z \quad F_{2V}^Z \end{array} \right\}$$

**Measure 2 observables
for 2 beam polarizations:**

- x-section
- FB asymmetry

**Extract form factors in groups
(assuming SM for remaining groups)**



Assumptions:

LHC: 14 TeV, 300/fb

LC: $\sqrt{s} = 500$ GeV, $L = 500$ /fb

$P(e^-) = +/- 80\%$, $P(e^+) = -/+ 30\%$

$\delta\sigma \sim 0.5\%$ (stat. + lumi)

$\delta A_{FB} \sim 1.8\%$ (stat., covers systematics?)

Polarization needed to disentangle photon and Z-boson form factors!

Especially for ttZ LC precision is better than existing (model-dependent) limits from top decay, LEP T-parameter, B-factories (full comparison in progress)



BSM sensitivity vs. \sqrt{s}

Impact of new physics on cross-section and asymmetries depends on \sqrt{s}

$$\Gamma_{t\bar{t}(\gamma,Z)}^\mu = ie \left[\gamma^\mu \left[\tilde{F}_{1V}^{\gamma,Z} + \tilde{F}_{1A}^{\gamma,Z} \gamma^5 \right] + \frac{(p_t - p_{\bar{t}})^\mu}{2m_t} \left[\tilde{F}_{2V}^{\gamma,Z} + \tilde{F}_{2A}^{\gamma,Z} \gamma^5 \right] \right]$$

BSM impact on cross-section and A_{FB} increases strongly with \sqrt{s} for axial dipole moments and four-fermion operators;

→ factor 10 and more between 0.5 and 3 TeV

Much less pronounced increase for vector dipole moments, none for $F_{1V/A}^{\gamma,Z}$

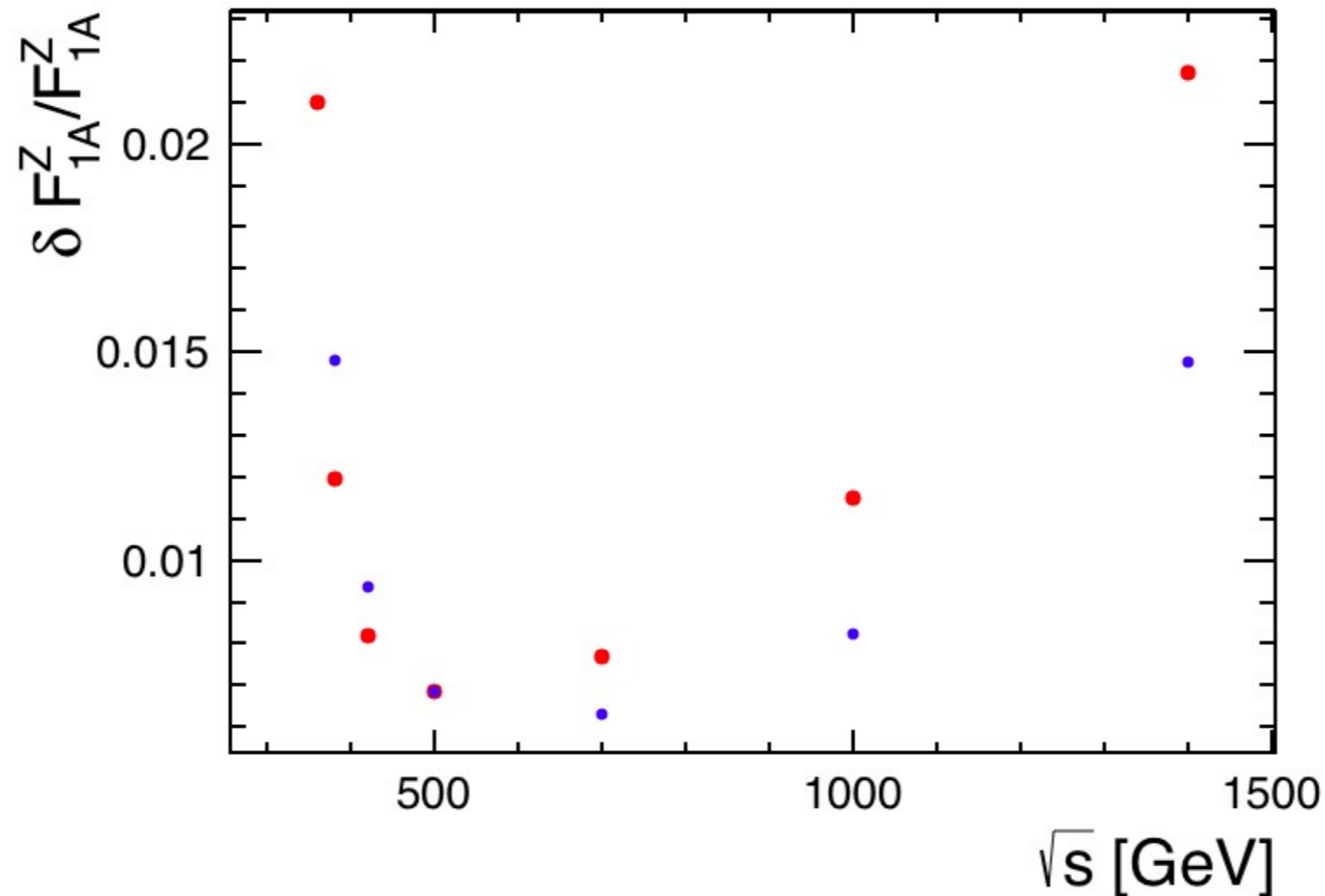
For details, see talk in CLIC workshop, CERN, January 2015:

<https://indico.cern.ch/event/336335/session/1/contribution/174>



Top quark couplings: sensitivity vs. \sqrt{s}

- Luminosity proportional to \sqrt{s}
- Flat Luminosity: 500/fb



Small cms energies:

- Vanishing axial vector coupling
- +
- Lumi decreases at linear colliders

High cms energies:

- Quickly decreasing cross section
- ... partially compensated by increasing luminosity

From Roman Poeschl, Wednesday top session

- F1AZ profits from somewhat higher energies (beta dependence)
 - Remark: Full disentangling for F1VZ and F2VZ at ~ 1 TeV
- $\sqrt{s} \sim 1$ TeV attractive option

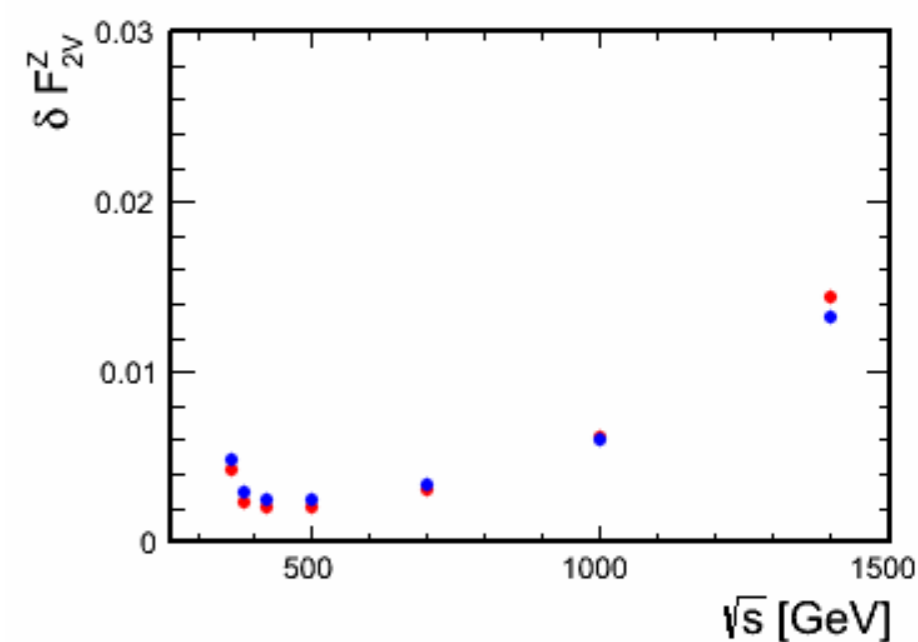
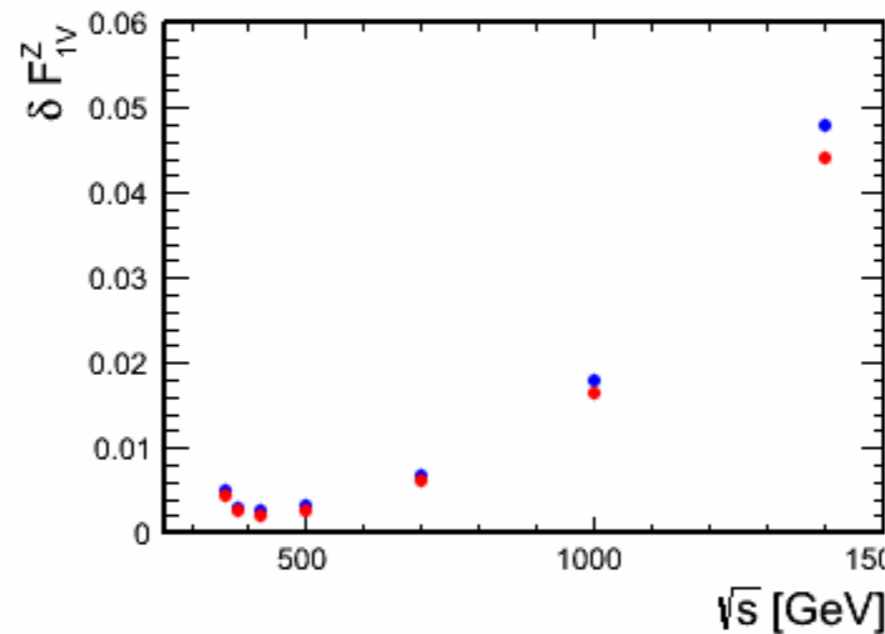
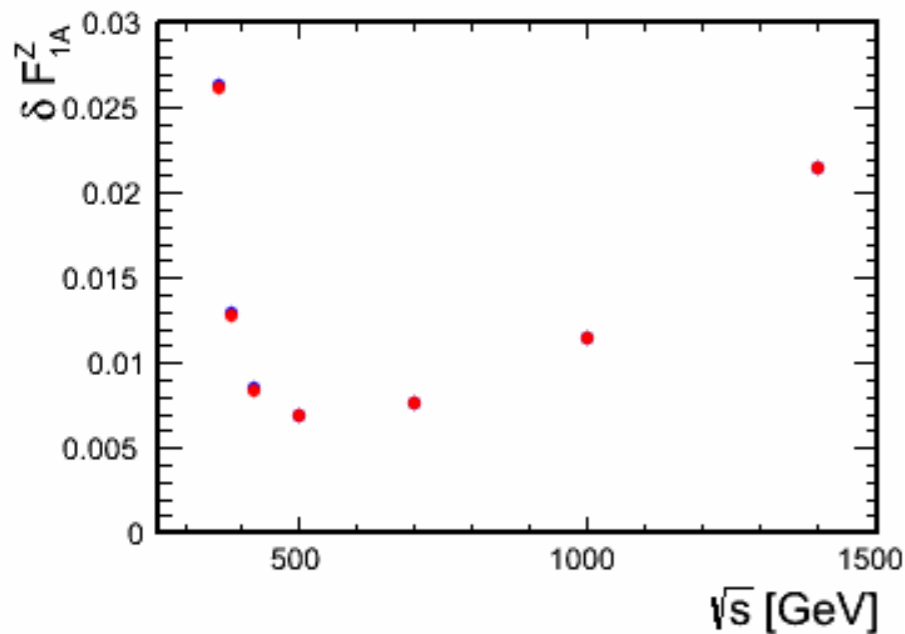


Top quark couplings: sensitivity vs. sqrt(s)

Simple evaluation of statistical uncertainty. A thorough full-simulation CLIC study started.

stat. dominated uncertainty:
 $\delta\sigma/\sigma \sim 1/\sqrt{N}$ $\delta A_{FB} = (1 - A_{FB}^2) \times \delta\sigma/\sigma$
 Integrated luminosity: $2 \times 250/\text{fb}$

● Nominal beam polarization
 (e^- 80%, e^+ 30%)
 ● Electron polarization only



F_{1V} ; shallow minimum \rightarrow optimal around 400 GeV

F_{1A} ; A_{FB} degraded strongly close to threshold \rightarrow 500 GeV

F_{2V} ; impact of new physics grows strongly with energy \rightarrow 1-3 TeV

Truly optimal: comprehensive program at several energies



Top quark couplings: Results

ILC@500GeV L=500fb⁻¹

$\mathcal{P}_{e^-}, \mathcal{P}_{e^+}$	$(\delta\sigma/\sigma)_{\text{stat.}} (\%)$	$(\delta A_{\text{FB}}^t/A_{\text{FB}}^t)_{\text{stat.}} (\%)$
-0.8, +0.3	0.47	1.8
+0.8, -0.3	0.63	1.3

CLIC@380GeV L=500fb⁻¹

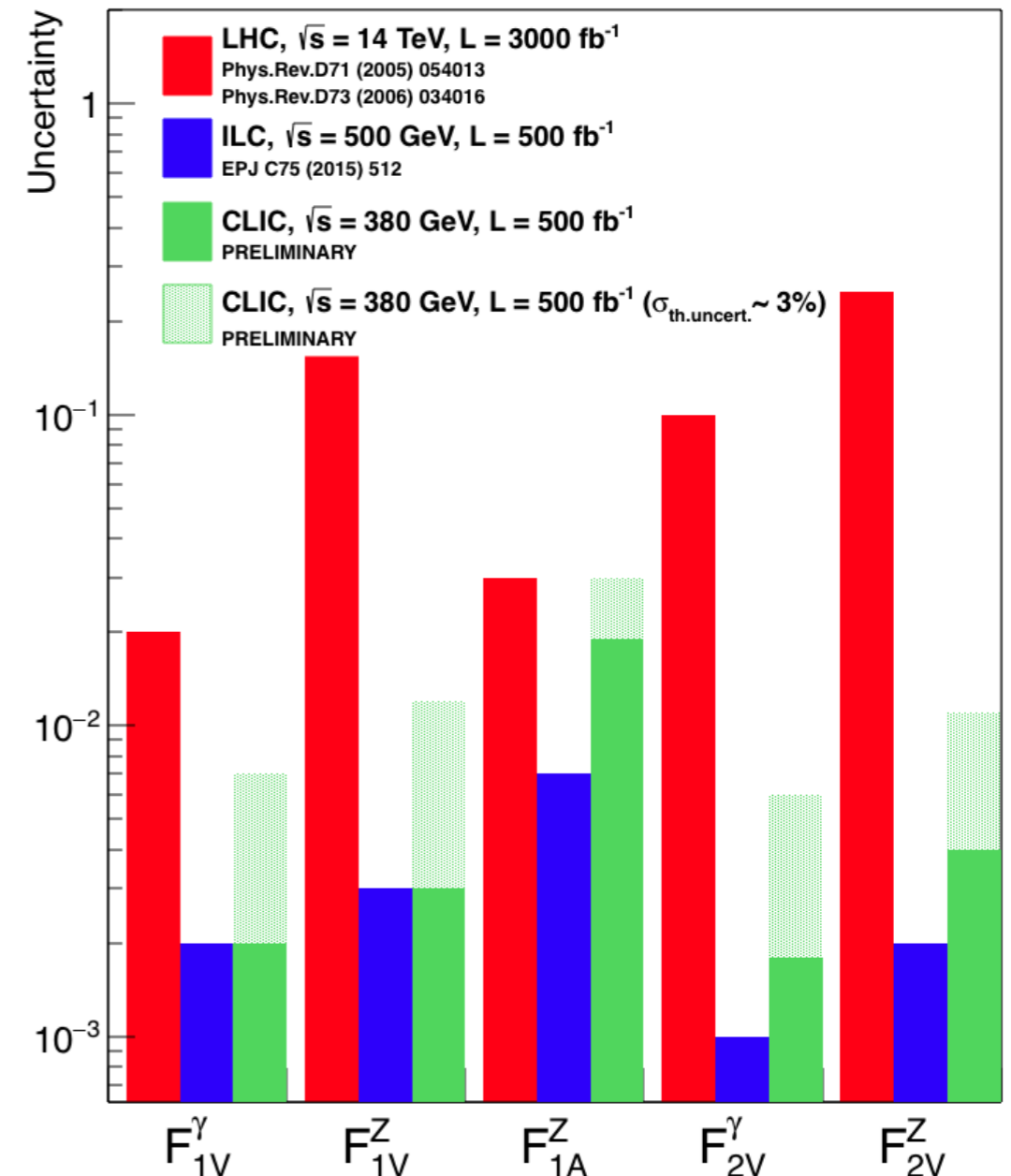
$\mathcal{P}_{e^-}, \mathcal{P}_{e^+}$	$(\delta\sigma/\sigma)_{\text{stat.}} (\%)$	$(\delta A_{\text{FB}}^t/A_{\text{FB}}^t)_{\text{stat.}} (\%)$
-0.8, 0	0.47	3.8
+0.8, 0	0.83	4.6

CLIC: similar precision to ILC except for the coupling F_{1A}^Z that suffers the large statistical error of $A_{\text{FB}}^t \sim 5\%$

Conservative scenario for CLIC: NNNL calculations at threshold predict a 3% theory uncertainty

ILC and CLIC can characterise the $t\gamma$ and ttZ vertices very precisely, **an order of magnitude better than LHC** prospects from associated production

$$\Gamma_{\mu}^{j\bar{j}X}(k^2, q, \bar{q}) = ie \left\{ \gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) - \frac{\sigma_{\mu\nu}}{2m_j} (q + \bar{q})^{\nu} (F_{2V}^X(k^2) + \gamma_5 F_{2A}^X(k^2)) \right\},$$



Matrix element on di-lepton final state

Khiem, Kou, Kurihara, le Diberder, Probing new physics using top quark polarization in the $e^+e^- \rightarrow t\bar{t}$ process at future Linear Colliders, [arXiv:1503.04247](https://arxiv.org/abs/1503.04247) [hep-ph]

GRACE six-fermion process without narrow-width approximation
(no ISR, no single top, no hadronization, no detector)

Show feasibility of kinematic reconstruction of the di-lepton final state: $e^+e^- \rightarrow t\bar{t} \rightarrow l^+ \nu_l \bar{\nu}_l b \bar{b}$

Optimal analysis extracts all ten form factors – simultaneously – from angular distribution using the (LO) matrix element

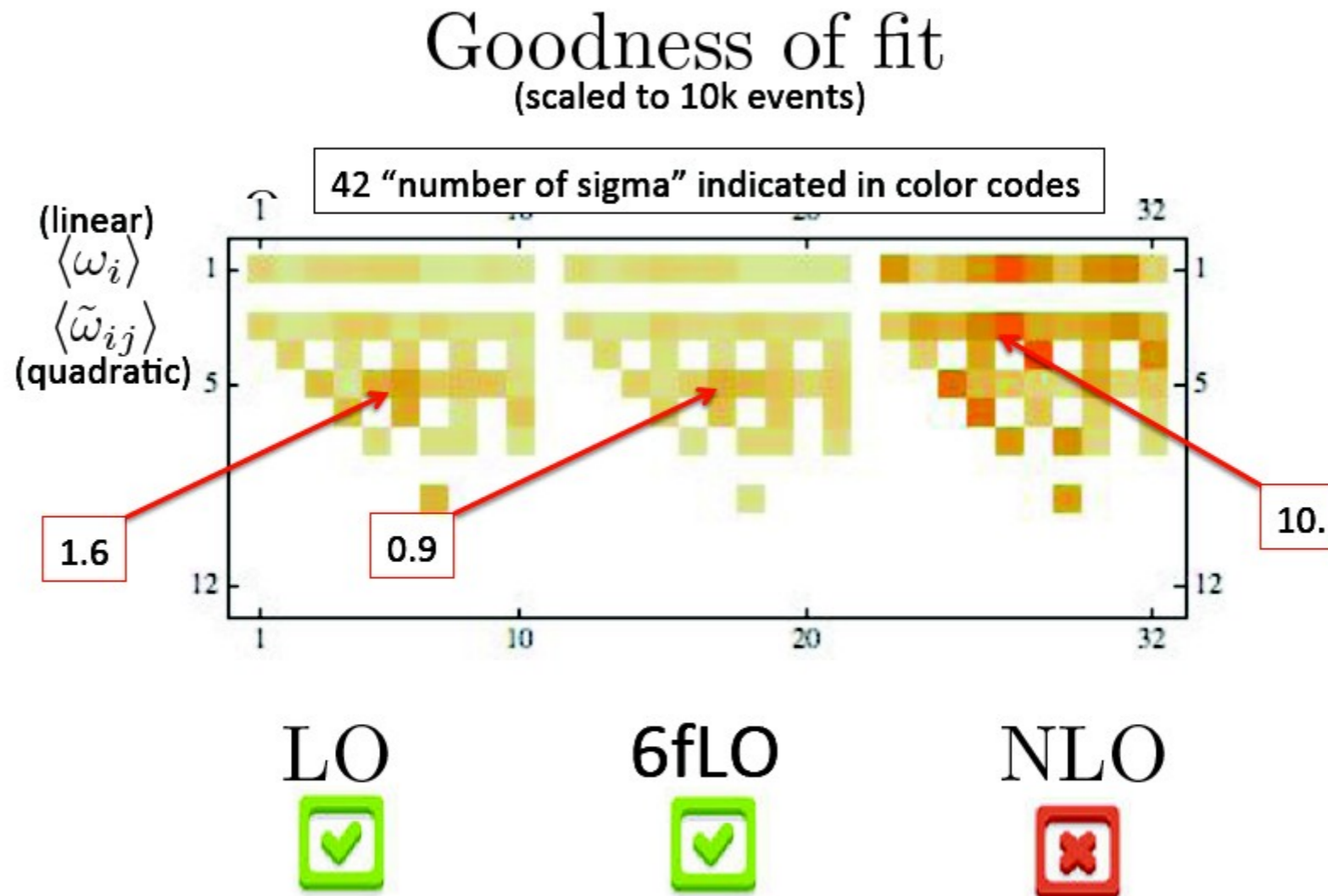
$\text{Re } \delta\tilde{F}_{1V}^\gamma$	$\text{Re } \delta\tilde{F}_{1V}^Z$	$\text{Re } \delta\tilde{F}_{1A}^\gamma$	$\text{Re } \delta\tilde{F}_{1A}^Z$	$\text{Re } \delta\tilde{F}_{2V}^\gamma$	$\text{Re } \delta\tilde{F}_{2V}^Z$	$\text{Re } \delta\tilde{F}_{2A}^\gamma$	$\text{Re } \delta\tilde{F}_{2A}^Z$	$\text{Im } \delta\tilde{F}_{2A}^\gamma$	$\text{Im } \delta\tilde{F}_{2A}^Z$
0.0037	-0.18	-0.09	+0.14	+0.62	-0.15	0	0	0	0
	0.0063	+0.14	-0.06	-0.13	+0.61	0	0	0	0
		0.0053	-0.15	-0.05	+0.09	0	0	0	0
			0.0083	+0.06	-0.04	0	0	0	0
				0.0105	-0.19	0	0	0	0
					0.0169	0	0	0	0
						0.0068	-0.15	0	0
							0.0118	0	0
								0.0069	-0.17
									0.0100

Sub-% precision. Note 0 correlation F2A with CP-conserving form factors

Lepton+jets final state, with same optimal ME extraction, yields factor two better precision



LO Matrix Element



Fitting a LO template to (all-order) data expected to lead to tension in the fit and bias of the parameters
Check fitting LO template to NLO-EW Monte Carlo \rightarrow large χ^2 indeed reveals a problem
Work ongoing to extend analysis to NLO



Comparison to FCC-ee

P. Janot, arXiv:1503.01325, arXiv:1510.09056 assesses potential of FCC-ee

- run right above threshold; study assumes 2.4 ab^{-1} at $\sqrt{s} = 365 \text{ GeV}$

(theory systematics close to threshold to be evaluated)

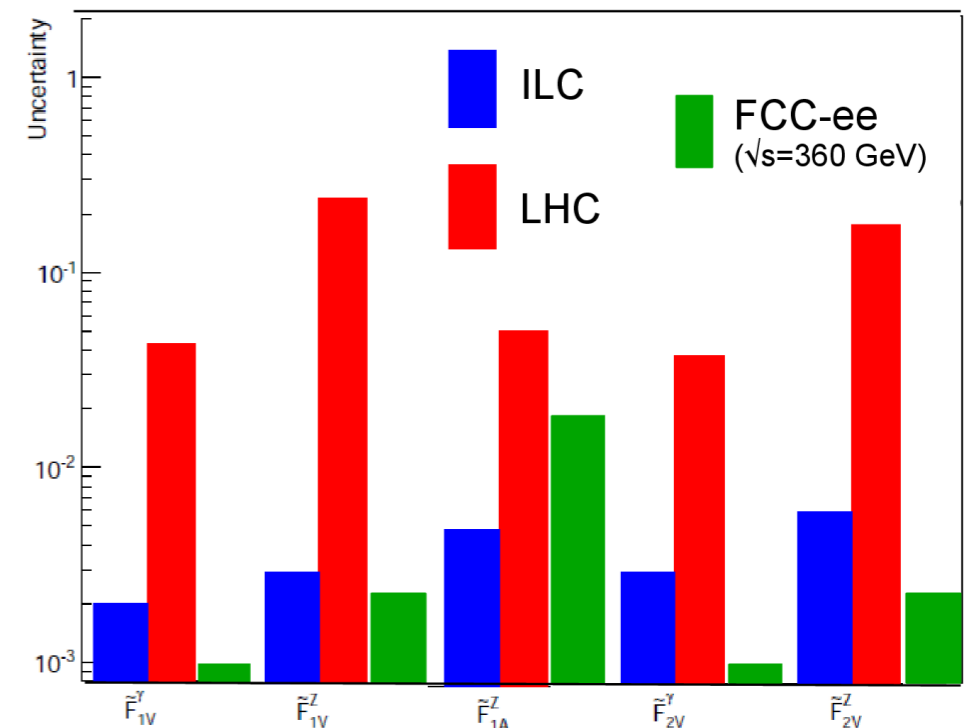
- no beam polarization, use final-state polarization instead

(ILC beam polarization expected to be known to 10^{-3} , can one understand final state polarization to that level?)

Fast simulation analysis based on lepton energy and angle yields:

- similar precision to ILC for Z couplings, except F1AZ

- significantly better than ILC for photon couplings

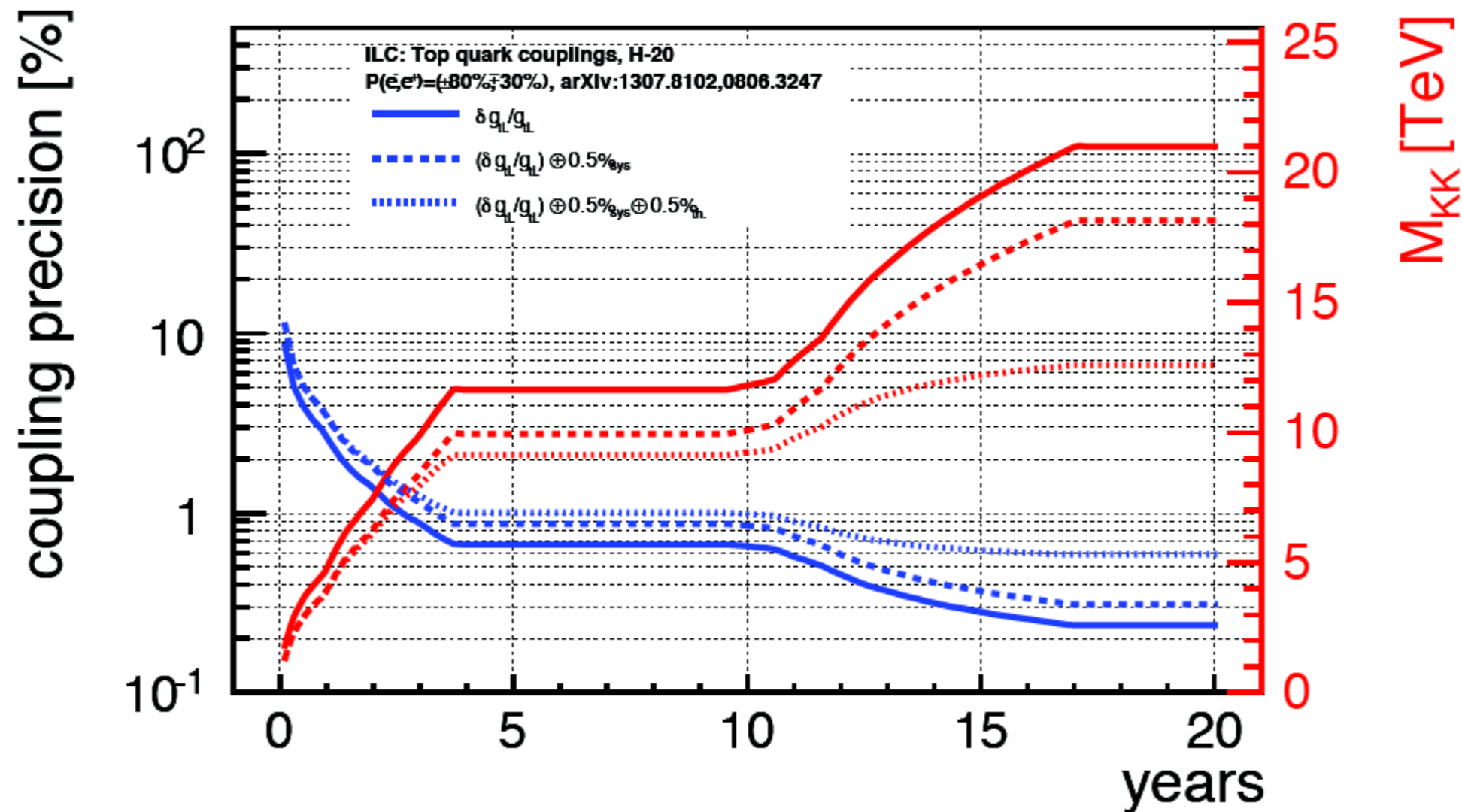


Good to see interest in this measurement
Full study needed to understand systematics



Complete 20-year ILC programme

H20: 500/fb @ 500 GeV, 200/fb @ 350 GeV, 500/fb @ 250 GeV, 3500/fb @ 500 GeV, 1500/fb @ 250 GeV



Sensitivity to new physics well beyond the direct kinematic reach
 Systematics may limit potential in the long run → detailed study



CP violating couplings

The “baseline” study was limited to CP-conserving form factors, but e^+e^- is known to do well also for CP-violating F2A at least since TESLA times

Reconstructing Bernreuther's optimal CP observables that measure differences in polarization orthogonal to production plane and in top quark flight direction.

In the lepton + jets final state:

$$O_+^{Re} = (\hat{q}_+^* \times \hat{q}_X) \cdot \hat{e}_+ \quad O_-^{Re} = (\hat{q}_-^* \times \hat{q}_X) \cdot \hat{e}_+$$
$$O_+^{Im} = -\left[1 + \left(\frac{\sqrt{s}}{2m_t} - 1\right)(\hat{q}_X \cdot \hat{e}_+)^2\right]\hat{q}_+^* \cdot \hat{q}_X + \frac{\sqrt{s}}{2m_t}\hat{q}_X \cdot \hat{e}_+ \hat{q}_+^* \cdot \hat{e}_+$$

Where q = charged lepton momentum, X = hadronic top system, e = positron momentum

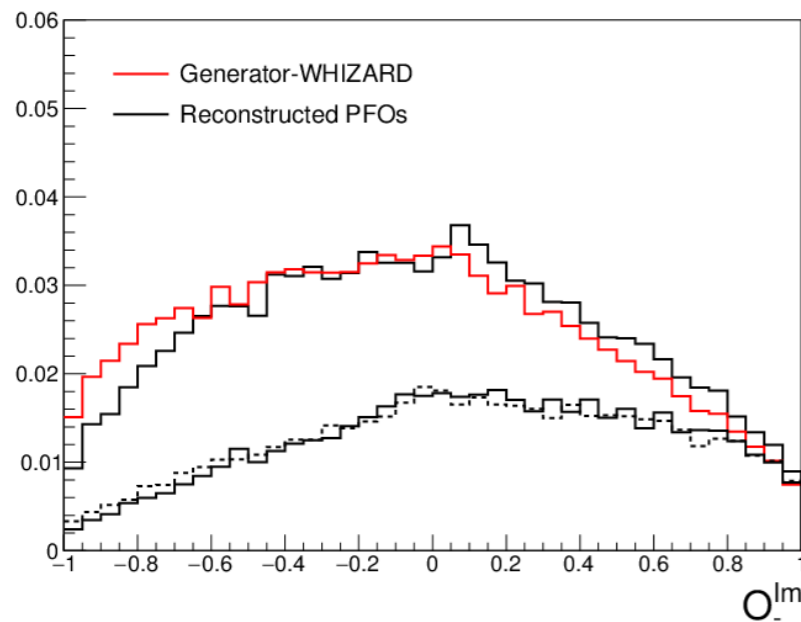
These observables have simple relations to the four F2A form factors:

$$A_{\gamma,Z}^{Re} = \langle O_+^{Re} \rangle - \langle O_-^{Re} \rangle = c_\gamma [P \text{Re}(F_{2A}^\gamma) + KZ \text{Re}(F_{2A}^Z)]$$

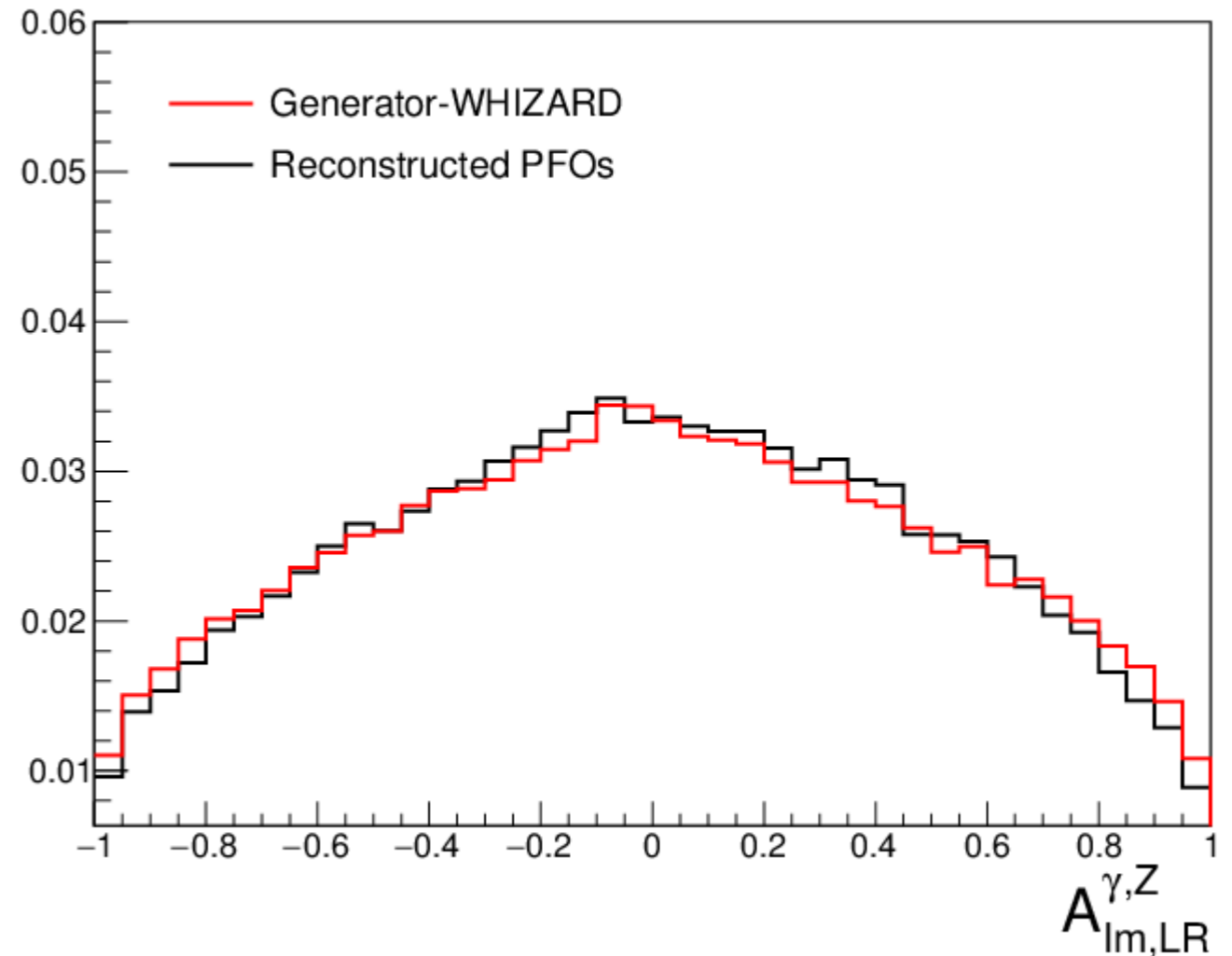
$$A_{\gamma,Z}^{Im} = \langle O_+^{Im} \rangle - \langle O_-^{Im} \rangle = d_\gamma [\text{Im}(F_{2A}^\gamma) + PKZ \text{Im}(F_{2A}^Z)]$$



F2A form factors



Significant migrations in the O_{im} distributions, largely cancel in asymmetry



Full simulation results exist for 500 GeV and 380 GeV.

Systematic uncertainties seem manageable.

Paper with updated numbers for LC potential in preparation

Top quark couplings: CPV Preliminary results

These observables have simple relations to the four F_{2A} form factors

$$A_{\gamma,Z}^{Re} = \langle O_+^{Re} \rangle - \langle O_-^{Re} \rangle = c_\gamma [P Re(F_{2A}^\gamma) + K Z Re(F_{2A}^Z)]$$

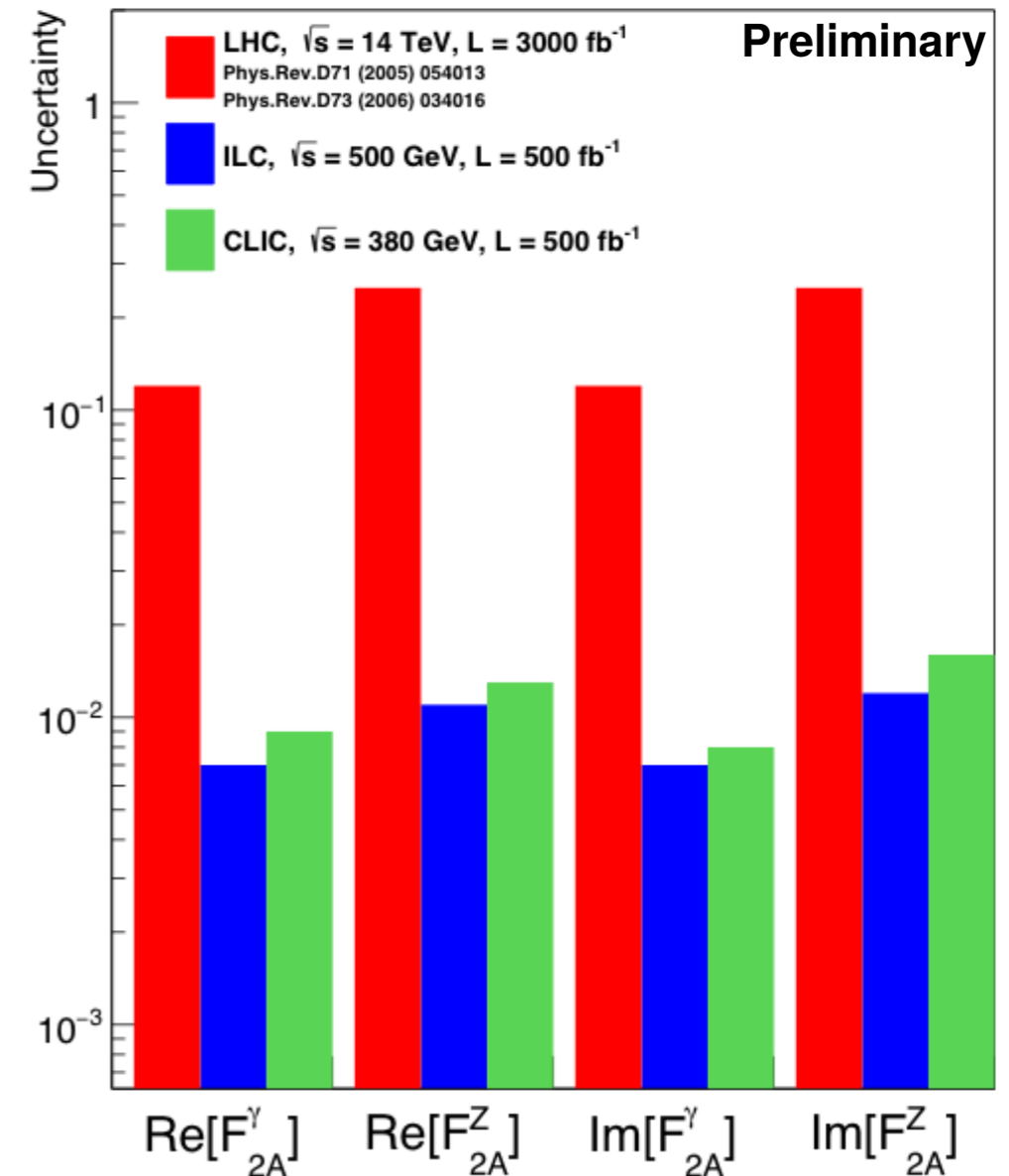
$$A_{\gamma,Z}^{Im} = \langle O_+^{Im} \rangle - \langle O_-^{Im} \rangle = d_\gamma [Im(F_{2A}^\gamma) + P K Z Im(F_{2A}^Z)]$$

One can easily isolate F_{2A} from previous lineal relations

Full simulations results exist for **ILC@500GeV** and **CLIC@380GeV**

Paper of LC potential in the CPV sector in preparation (IFIC-LAL collaboration)

Quantity	$Re[F_{2A}^\gamma]$	$Re[F_{2A}^Z]$	$Im[F_{2A}^\gamma]$	$Im[F_{2A}^Z]$
SM value at tree level	0	0	0	0
LHC	0.12	0.25	0.12	0.25
TESLA TDR	0.007	0.008	0.008	0.010
ILC@500 GeV	0.007	0.011	0.007	0.012
CLIC@380 GeV	0.009	0.013	0.008	0.016



Confirm sensitivity of TESLA TDR study



Top at lepton colliders: summary

Lepton Colliders have great top physics potential. Today's list, that only scratches the surface:

- Direct access to top quark Yukawa coupling, 4% precision ($\sqrt{s} > 550$ GeV)
- **Rare FCNC decays, BR ($t \rightarrow cH$) $\sim 10^{-5}$ ($\sqrt{s} \sim 500$ GeV or 380 GeV)**
- The ultimate top quark mass measurement, 50 MeV ($\sqrt{s} \sim 340$ -350 GeV)
- Exquisite BSM sensitivity through a characterization of $t\bar{t}Z/\gamma$ vertices
 - sub-% precision on CP-conserving couplings ($\sqrt{s} \sim 500$ GeV, **some degradation at 380 GeV**)
 - Sub-% precision on CP-violation ($\sqrt{s} \sim 500$ GeV/380 GeV)**

Specifically for circular colliders:

- *Expect 50 MeV precision on the top quark mass*
- *For couplings to Z/γ expectations similar to CLIC@380 GeV*
- *For Yukawa coupling, threshold scan allows $O(20\%)$ measurement*

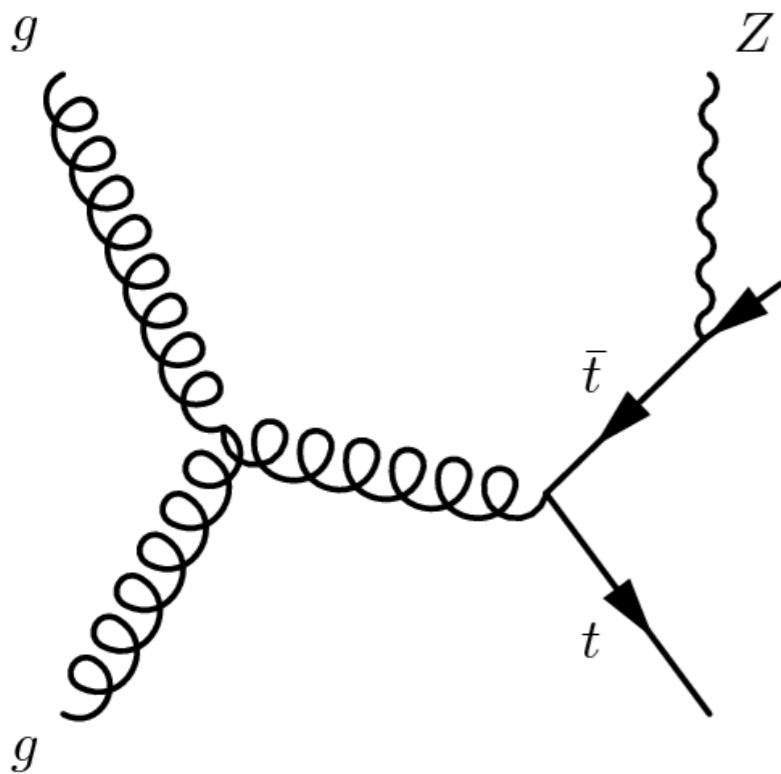
Do not compare “targets” (i.e. stat. only) to “prospects” (based on best estimate of all uncertainties)



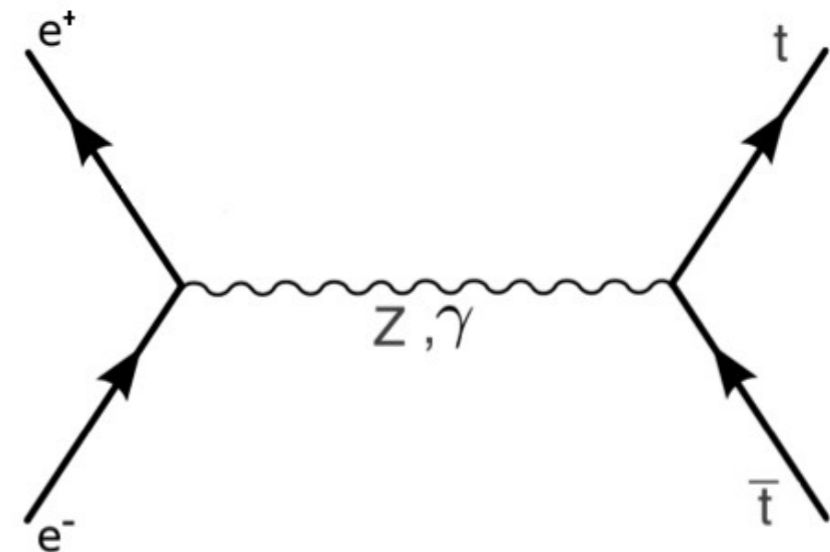
Top and Z/γ

Couplings of the top quark to neutral EW gauge bosons

At the LHC, $q\bar{q} \rightarrow Z/g \rightarrow t\bar{t}$ is inaccessible. Must use associated production



At a LC $e^+e^- \rightarrow t\bar{t}$ production is one of the most prominent 6f processes and readily isolated

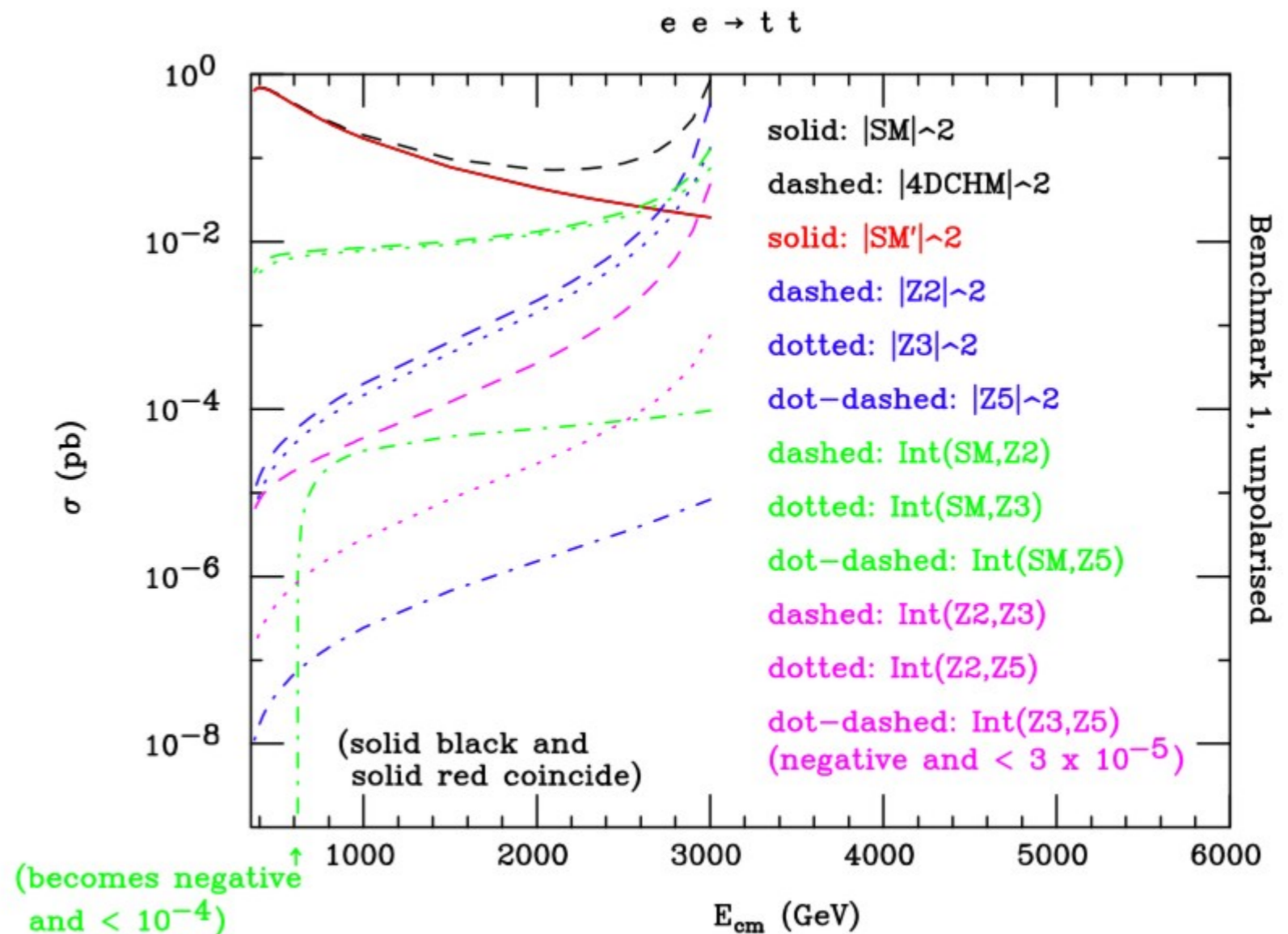


Some overlap with studies of tWb vertex at LHC (single top, top decay), and indirect sensitivity of LEP precision tests and B-factories

BSM physics: concrete model

A concrete example: the 4D Composite Higgs Model predicts for a benchmark point with $m_{Z'} \sim 3.1\text{-}4.3$ TeV

$\Delta\sigma = 4\%$ @380 GeV
 $= 9\%$ @500 GeV
 $= 53\%$ @1 TeV



4D Composite Higgs Model

Barducci, de Curtis, Moretti, Pruna, JHEP 08 (2015)



$$\frac{\delta y_t}{y_t} \sim \frac{(100 + 9) \times \frac{1}{2} \times \frac{\delta \sigma}{\sigma}}{9}$$

The expected statistical errors on top quark Yukawa coupling are 5.0% and 7.1% for the “Left” and “Right” polarization combinations, respectively, and 4.2% when combined (Table 3).

	“Left”	“Right”	Combined
cross section	0.84 %	1.2 %	
top quark Yukawa coupling	5.0 %	7.1 %	4.2 %