

# Theory & FCC-ee

G.F. Giudice



## 10<sup>th</sup> FCC-ee physics workshop

4-5 Feb 2016

### FCC-ee mini-workshop: Physics behind precision

2-3 Feb 2016

Filtration plant  
(222-R-001)  
CERN, Geneva,  
Switzerland



What physics  
can be discovered  
with the FCC-ee  
unequaled precision?

Note:  
every day from 10:30 to 12:30  
**FCC academic training**  
<http://indico.cern.ch/e/472105/>

### Registration

10th FCC-ee general workshop  
<http://indico.cern.ch/e/FCCee10>

FCC-ee mini-workshop  
<http://indico.cern.ch/e/FCCeePrecision>

### Organizing committee

10th FCC-ee general workshop	FCC-ee mini-workshop
Alain Blondel	Patrizia Azzi
John Ellis	Freya Blekman
Christophe Grojean	Elizabeth Locci
Patrick Janot	Fulvio Piccinini
	Roberto Tenchini

LHC Run 1 taught us that  
we live in a metastable state



I don't refer to the EW vacuum,  
but to the HEP community

- State of confusion about what lies beyond the SM
- Any new hint in EXP or TH can make our present state collapse into unknown directions

# Many of our past expectations have been shattered

- Technicolor** → based on naturalness  
→ no fundamental Higgs
- Supersymmetry** →  $m_h \lesssim 120$  GeV,  
 $\tilde{m}_t \lesssim 300$  GeV,  $\tilde{m}_g \lesssim 1$  TeV
- Extra dimensions** → hell breaks loose at TeV
- Composite Higgs** →  $\Delta\text{BR}_h \sim O(1)$

No!

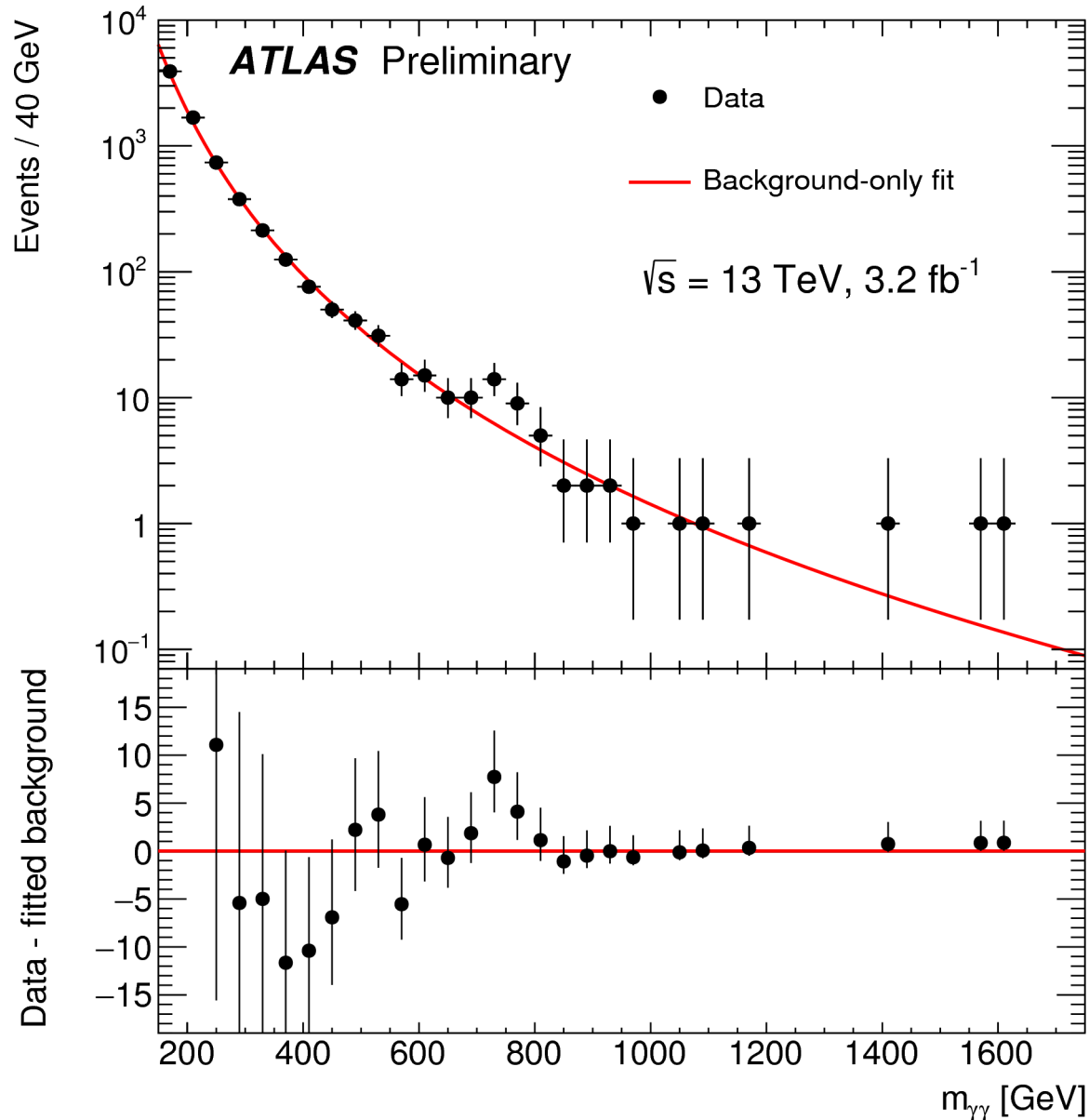
No!

No!

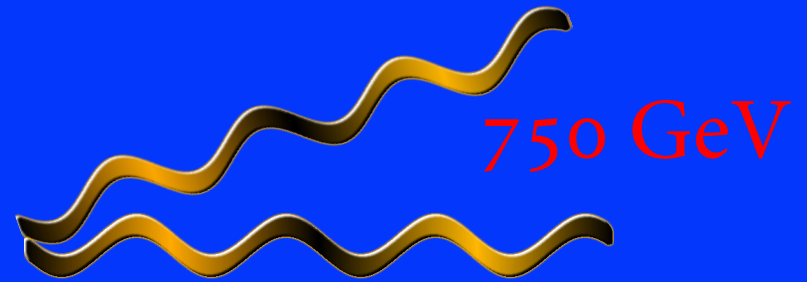
No!

Is the naturalness principle not valid for EW  
or are we implementing it in the wrong way?

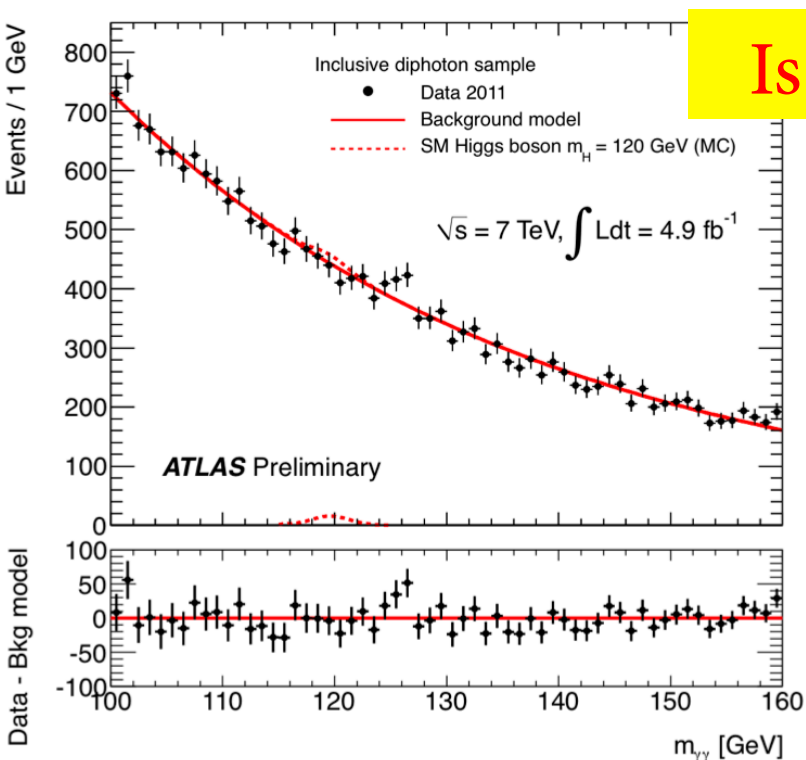
# The instability of our present state has been recently confirmed



# The epiphany of a new era...

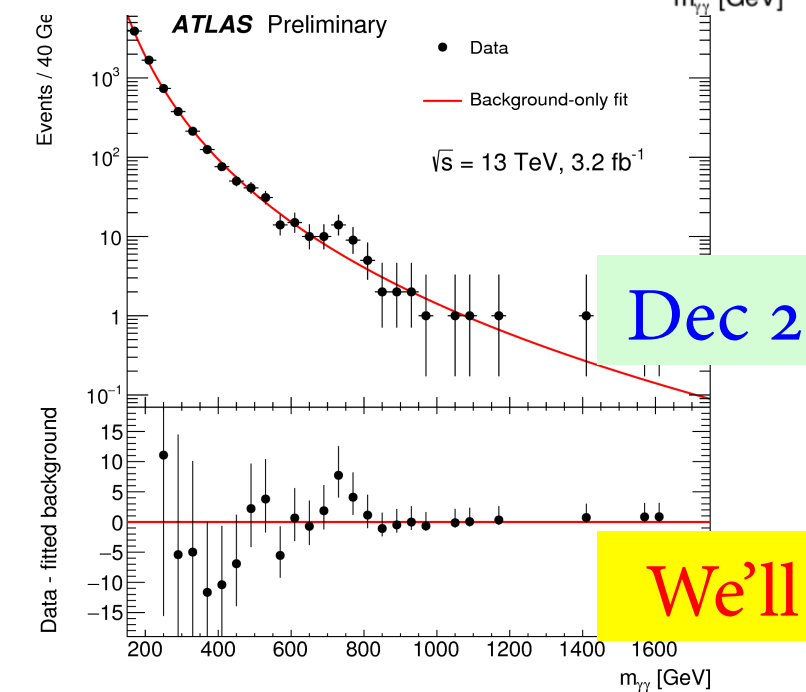
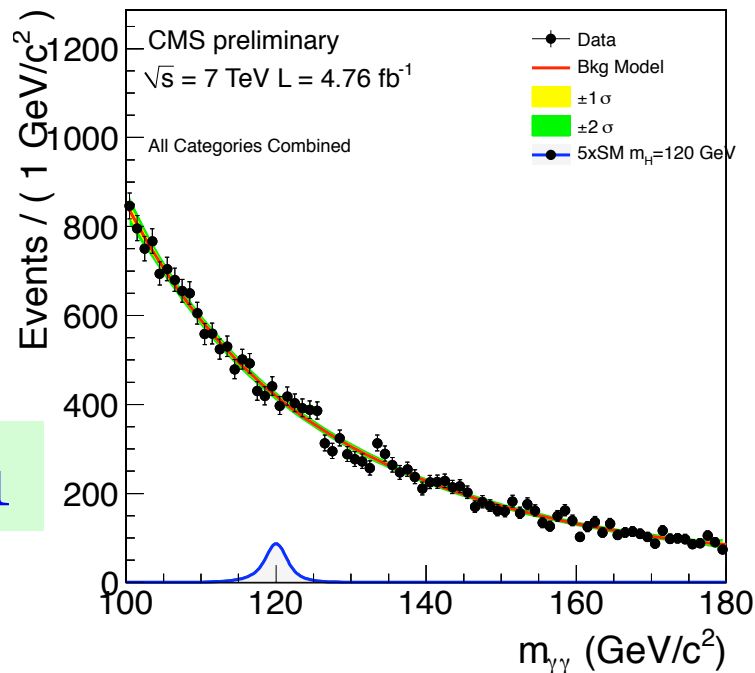


Most theoreticians were willing to abandon old customs  
(like spending time with their families during Christmas)  
to embrace the new religion



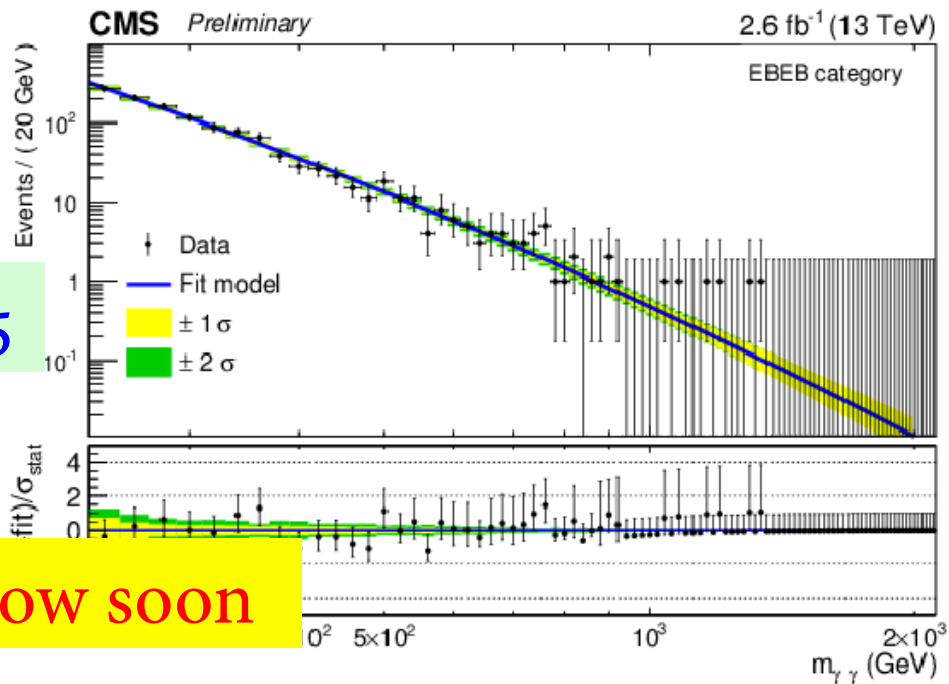
Is it true?

Dec 2011



Dec 2015

We'll know soon



# Lessons

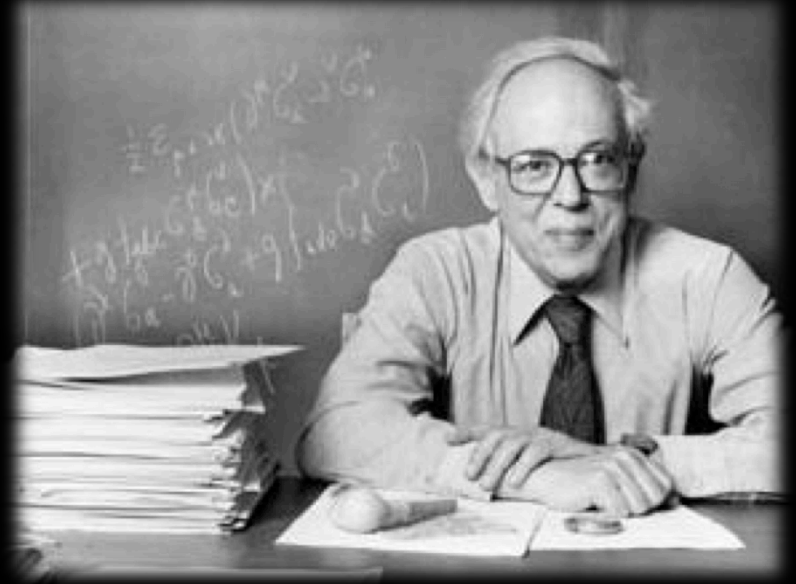
- Sociological behaviour of the HEP community
- We live in uncertain times: key questions can suddenly change
- Today measuring the Higgs properties is the central issue. No doubt it is a fundamental question, but will people care tomorrow as much as they care today?
- Most of what I say is irrelevant

Should we fear this state of confusion?



Today we live in the midst of upheaval and crisis. We do not know where we are going, nor even where we ought to be going. Awareness is spreading that our future cannot be a straight extension of the past or the present. [...] Progress leads to confusion leads to progress and on and on without respite. Every one of the many major advances [...] created sooner or later, more often sooner, new problems. These confusions, never twice the same, are not to be deplored. Rather, those who participate experience them as a privilege.

**Abraham Pais**



Confusion and not knowing where we are going may be great for theorists, but how can we plan future colliders while living in a metastable state?

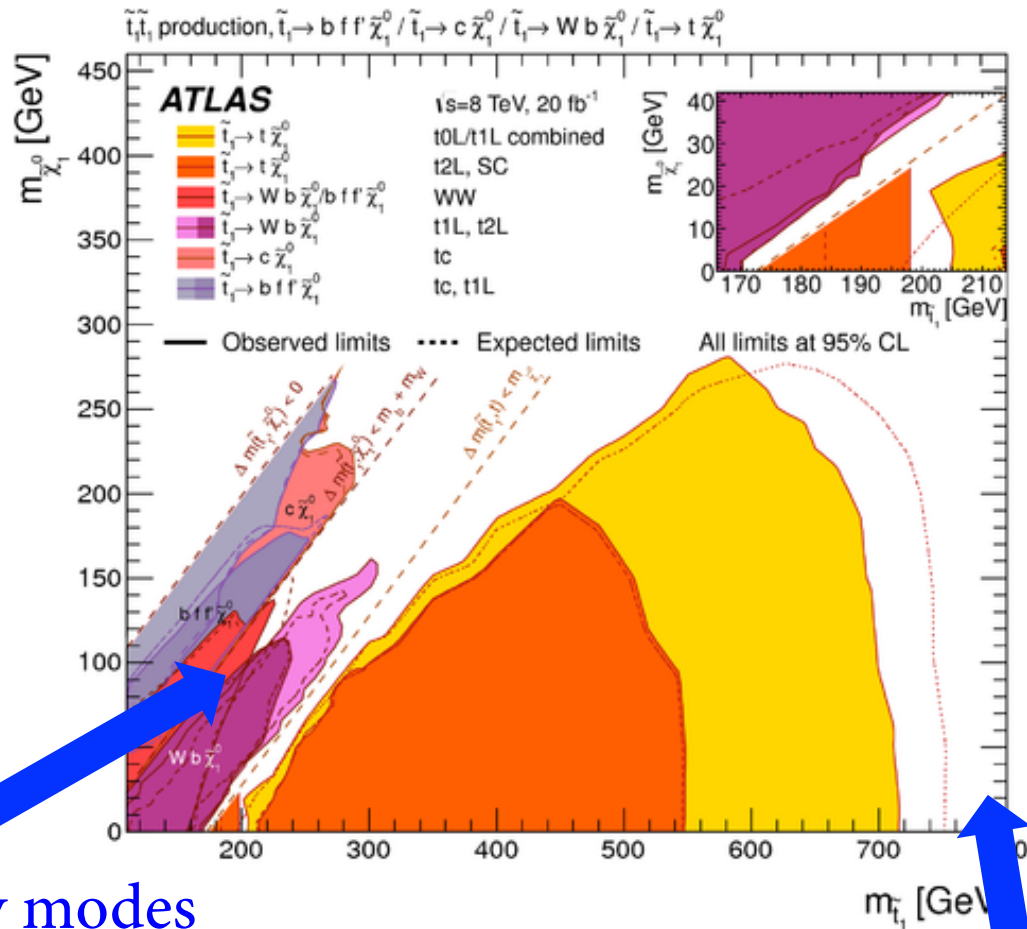
Does FCC-ee contribute to a diversified, farsighted, and ambitious HE program?

Are there new particles to be discovered at FCC-ee?

LHC is suffocating life at  $\sqrt{s} \lesssim 2 m_t$

LHC may leave holes where naturalness can hide

Exploring these holes is a crucial task: some of them may be accidental, but others have good theoretical justifications



## Difficult decay modes

- Soft final states  
(compressed spectra,  
stealth susy)
- Light quarks  
(flavour mixing,  
R violation)

Unnatural spectra  
(Split Susy & variations)

In some cases, the “holes” are  
the only way for discovery

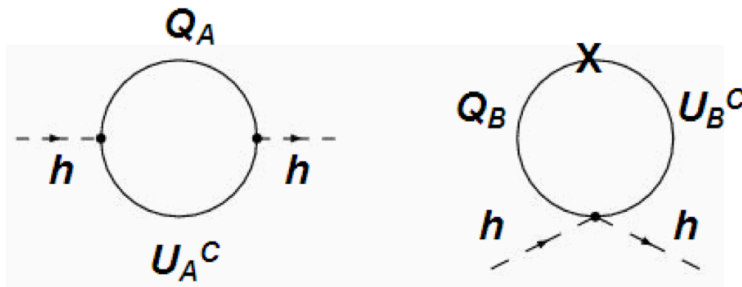
# Neutral naturalness

**Twin Higgs:** discrete symmetry on an enlarged Higgs sector implies an accidental global symmetry at one-loop

$$\Delta V = \frac{9g^2 \Lambda^2}{64\pi^2} (H_A^\dagger H_A + H_B^\dagger H_B)$$

No mass to the extra Goldstones

Chacko, Goh, Harnik

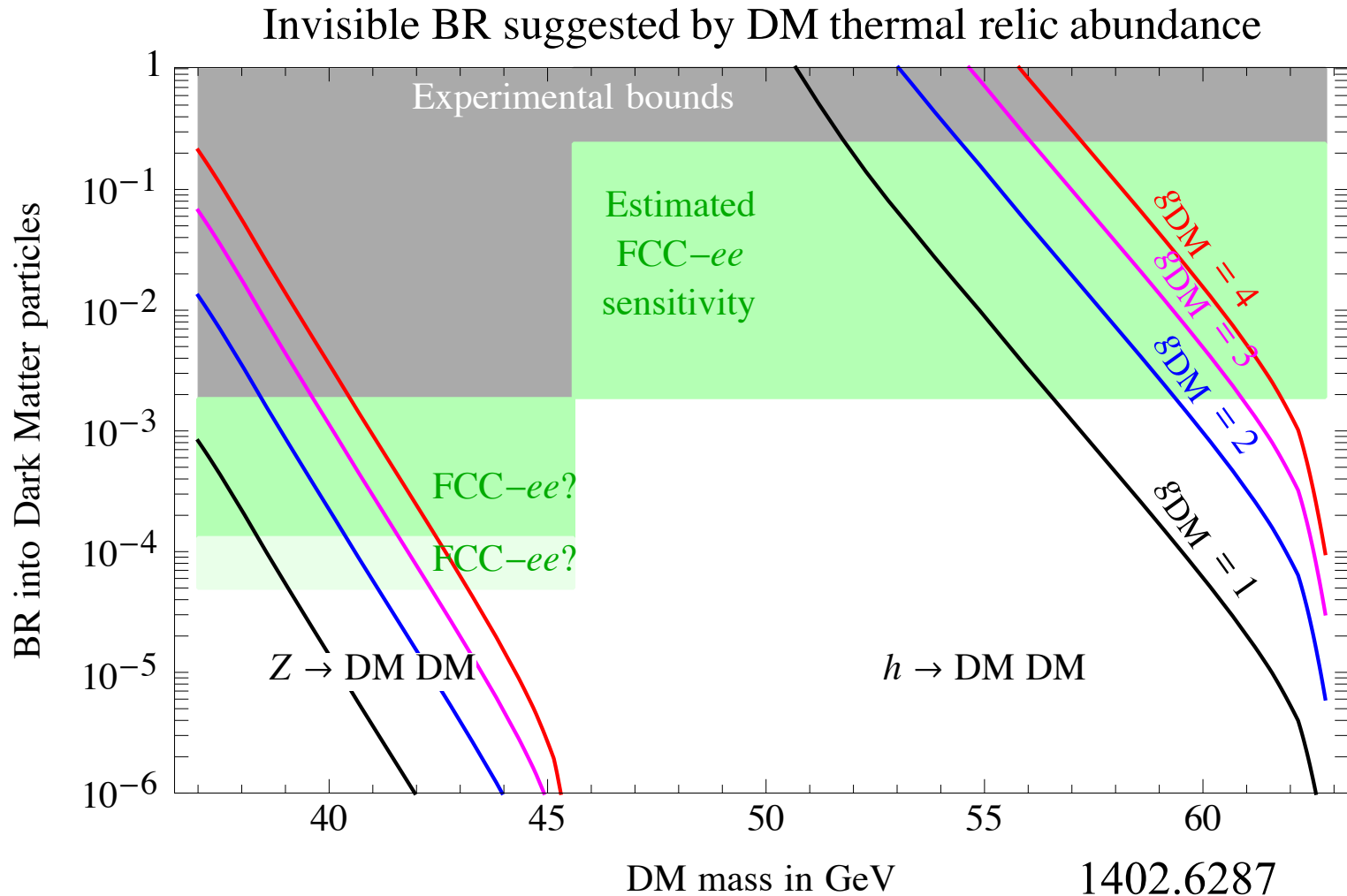


**Naturalness**  $\Rightarrow$  new states necessarily charged under EW, but not QCD

In general, LHC will leave “holes” in the search for EW particles

# Rare decays of $Z$ and $H$

Ex.: Near-resonant DM annihilation  
escapes direct detection



In general, weakly-interacting particles  
with 'difficult' decay modes can escape  
both LHC and FCC-hh

Examples:

- nearly-degenerate weak multiplets
- DM models

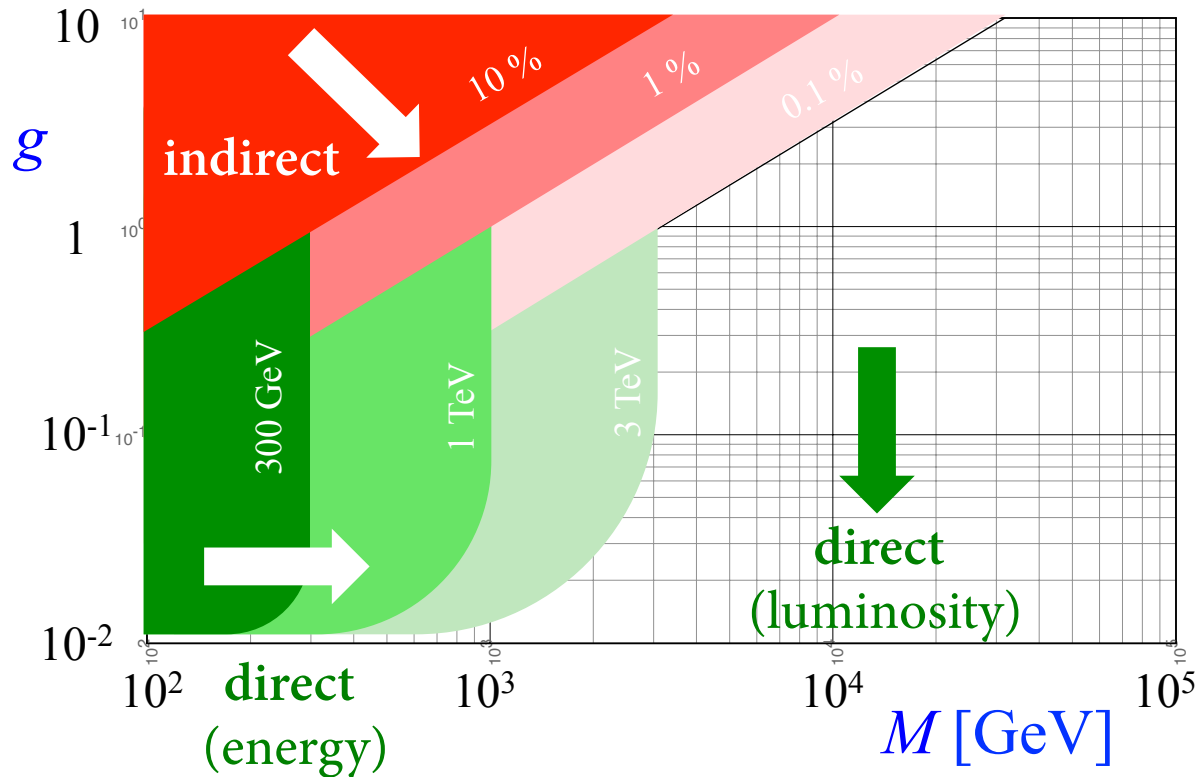
Testable beyond mass threshold through  
quantum corrections (see Strumia's talk)

# We are looking for new phenomena (not just particles)

## The strength of FCC-ee lies in precision

Direct searches probe  $M$  (with energy) and  $g$  (with luminosity)

Indirect searches probe  $g^2/M^2$



Indirect searches are more effective for **strongly**-int theories

Theoretical predictions are more reliable for **weakly**-int theories



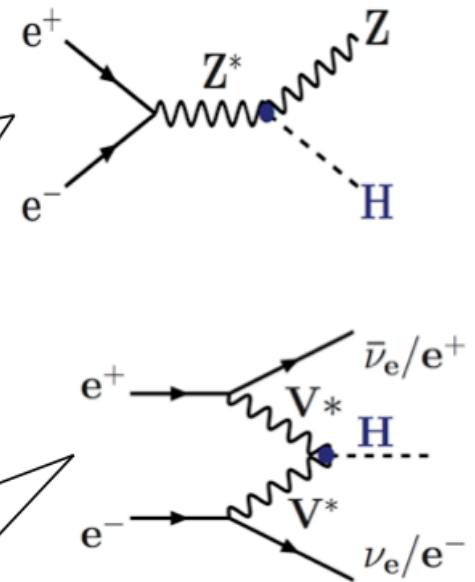
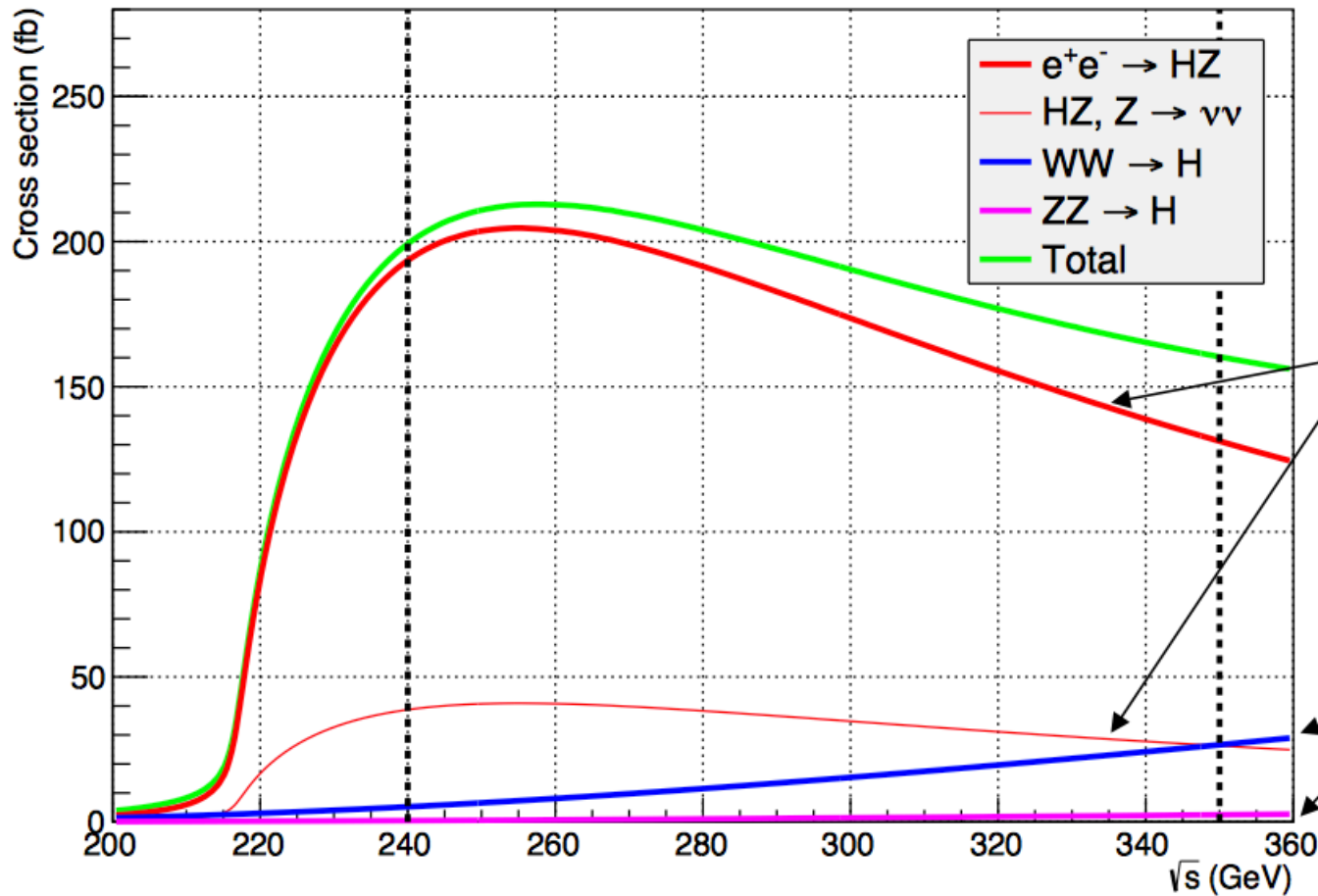
# LCC-ee 4 phases of precision physics

$$\begin{aligned} Z &\rightarrow 90 \text{ GeV} \\ WW &\rightarrow 160 \text{ GeV} \\ HZ &\rightarrow 240 \text{ GeV} \\ tt &\rightarrow 350 \text{ GeV} \end{aligned}$$

# Higgs production

- Large rate
- Recoil mass in  $e^+e^- \rightarrow HZ$  gives 0.05% precision in  $\sigma_{e^+e^- \rightarrow HZ}$  (hence in  $g_{HZZ}$ )
- Tagged Higgs invisible decays

Unpolarized cross sections



Error on	$\mu\mu$ Collider	ILC	FCC-ee
$m_H$ (MeV)	0.06	30	8
$\Gamma_H$ (MeV)	0.17	0.16	0.04
$g_{Hbb}$	2.3%	1.5%	0.4%
$g_{HWW}$	2.2%	0.8%	0.2%
$g_{H\tau\tau}$	5%	1.9%	0.5%
$g_{H\gamma\gamma}$	10%	7.8%	1.5%
$g_{H\mu\mu}$	2.1%	20%	6.2%
$g_{HZZ}$	—	0.6%	0.15%
$g_{Hcc}$	—	2.7%	0.7%
$g_{Hgg}$	—	2.3%	0.8%
$BR_{invis}$	—	<0.5%	<0.1%

Comparison of precision (after  $\sim 10$  yrs data)

Higher luminosity than LC (for  $\sqrt{s} \leq 400$  GeV)

Precise knowledge of beam energy

( $E_{beam} \sim 0.1$  MeV)

Triple Higgs through quantum corrections

McCullough 1312.3322

(P. Janot, talk at FCC-ee, 24 Sep 2015)

(A. Nisati, talk at IAS, 20 Jan 2016)

		$K_Y$	$K_W$	$K_Z$	$K_g$	$K_b$	$K_t$	$K_\tau$	$K_{Z\gamma}$	$K_\mu$
$300\text{fb}^{-1}$	ATLAS	[9,9]	[9,9]	[8,8]	[11,14]	[22,23]	[20,22]	[13,14]	[24,24]	[21,21]
$300\text{fb}^{-1}$	CMS	[5,7]	[4,6]	[4,6]	[6,8]	[10,13]	[14,15]	[6,8]	[41,41]	[23,23]
$3000\text{fb}^{-1}$	ATLAS	[4,5]	[4,5]	[4,4]	[5,9]	[10,12]	[8,11]	[9,10]	[14,14]	[7,8]
$3000\text{fb}^{-1}$	CMS	[2,5]	[2,5]	[2,4]	[3,5]	[4,7]	[7,10]	[2,5]	[10,12]	[8,8]

$$\Delta = \frac{v^2}{f^2} \Rightarrow \text{compositeness scale } 4\pi f > \sqrt{\frac{0.1\%}{\Delta}} \text{ 100 TeV}$$

Precise test of  $g_{Hcc}$ : Higgs couplings to 1<sup>st</sup> and 2<sup>nd</sup> generation may reveal secrets about flavour

$$H\bar{\psi}_L^{(3)}\psi_R^{(3)} + \frac{(H^+H)^{n_{ij}}}{\Lambda^{2n_{ij}}} H\bar{\psi}_L^{(i)}\psi_R^{(j)}$$

↓

$$m^{(3)} = O(v)$$

↓

$$m^{(ij)} = O\left(\frac{v^{2n_{ij}+1}}{\Lambda^{2n_{ij}}}\right)$$

$H\psi$

$$H\bar{\psi}_L^{(3)}\psi_R^{(3)} + \phi\bar{\psi}_L^{(ij)}\psi_R^{(ij)}$$

+ small mixing  $\phi - H$

$$\langle H \rangle \approx v \quad \langle \phi \rangle \ll v$$

$$y^{(3)} = \frac{m^{(3)}}{v}$$

$$y^{(ij)} = (2n_{ij} + 1) \frac{m^{(ij)}}{v}$$

Ghosh et al. 1508.01501

$$\frac{y^{(3)}}{y_{SM}^{(3)}} = 1$$

$$\frac{y^{(ij)}}{y_{SM}^{(ij)}} = 2n_{ij} + 1$$

0804.1753

Enhanced Higgs couplings  
to light generations

Suppressed Higgs couplings  
to light generations

# Couplings to 1<sup>st</sup> and 2<sup>nd</sup> generation quarks?

## Higgs exclusive decays

$$H \rightarrow V\gamma \quad V = \rho, \omega(y_u, y_d), \phi(y_s), J/\Psi(y_c)$$

Kagan et al. 1406.1722

## Couplings to electrons?

5- $\sigma$  observation with 75 ab<sup>-1</sup> on the Higgs resonance  
with energy spread less than Higgs width (4.1 MeV)

D'Enterria, Wojcik, Aleksan,  
8<sup>th</sup> FCC-ee Workshop, Paris 2014  
Jadach, Kycia 1509.02406

$\sqrt{s}$ (GeV):	90 (Z)	125 (eeH)	160 (WW)	240 (HZ)	350 ( $t\bar{t}$ )	350 (VV $\rightarrow$ H)
$\mathcal{L}/\text{IP}$ ( $\text{cm}^{-2} \text{s}^{-1}$ )	$2.2 \cdot 10^{36}$	$1.1 \cdot 10^{36}$	$3.8 \cdot 10^{35}$	$8.7 \cdot 10^{34}$	$2.1 \cdot 10^{34}$	$2.1 \cdot 10^{34}$
$\mathcal{L}_{\text{int}}$ ( $\text{ab}^{-1}/\text{yr}/\text{IP}$ )	22	11	3.8	0.87	0.21	0.21
Events/year (4 IPs)	$3.7 \cdot 10^{12}$	$1.3 \cdot 10^4$	$6.1 \cdot 10^7$	$7.0 \cdot 10^5$	$4.2 \cdot 10^5$	$2.5 \cdot 10^4$
Years needed (4 IPs)	2.5	1.5	1	3	0.5	3

D'Enterria 1601.06640

A lot of physics can be done with  $10^{12}$  Z ( $10^6$  at LEP<sub>1</sub>),  $10^8$  W pairs ( $10^4$  at LEP<sub>2</sub>),  $10^6$  top pairs (and  $3 \times 10^{10}$   $\tau$  pairs and  $2 \times 10^{11}$  b)

Observable	Measurement	Current precision	FCC-ee stat.	Possible syst.	Challenge
$m_Z$ (MeV)	Z lineshape	$91187.5 \pm 2.1$	0.005	$< 0.1$	QED corr.
$\Gamma_Z$ (MeV)	Z lineshape	$2495.2 \pm 2.3$	0.008	$< 0.1$	QED corr.
$R_\ell$	Z peak	$20.767 \pm 0.025$	0.0001	$< 0.001$	QED corr.
$R_b$	Z peak	$0.21629 \pm 0.00066$	0.000003	$< 0.00006$	$g \rightarrow b\bar{b}$
$A_{FB}^{\mu\mu}$	Z peak	$0.0171 \pm 0.0010$	0.000004	$< 0.00001$	$E_{\text{beam}}$ meas.
$N_\nu$	Z peak	$2.984 \pm 0.008$	0.00004	0.004	Lumi meas.
$N_\nu$	$e^+e^- \rightarrow \gamma Z(\text{inv.})$	$2.92 \pm 0.05$	0.0008	$< 0.001$	–
$\alpha_s(m_Z)$	$R_\ell, \sigma_{\text{had}}, \Gamma_Z$	$0.1196 \pm 0.0030$	0.00001	0.00015	New physics
$1/\alpha_{\text{QED}}(m_Z)$	$A_{FB}^{\mu\mu}$ around Z peak	$128.952 \pm 0.014$	0.004	0.002	EW corr.
$m_W$ (MeV)	WW threshold scan	$80385 \pm 15$	0.3	$< 1$	QED corr.
$\alpha_s(m_W)$	$B_{\text{had}}^W$	$B_{\text{had}}^W = 67.41 \pm 0.27$	0.00018	0.00015	CKM matrix
$m_t$ (MeV)	threshold scan	$173200 \pm 900$	10	10	QCD
$F_{1V,2V,1A}^{\gamma t, Z t}$	$d\sigma^{t\bar{t}}/dx d\cos(\theta)$	4%–20% (LHC-14 TeV)	(0.1–2.2)%	(0.01–100)%	–

D'Enterria 1601.06640

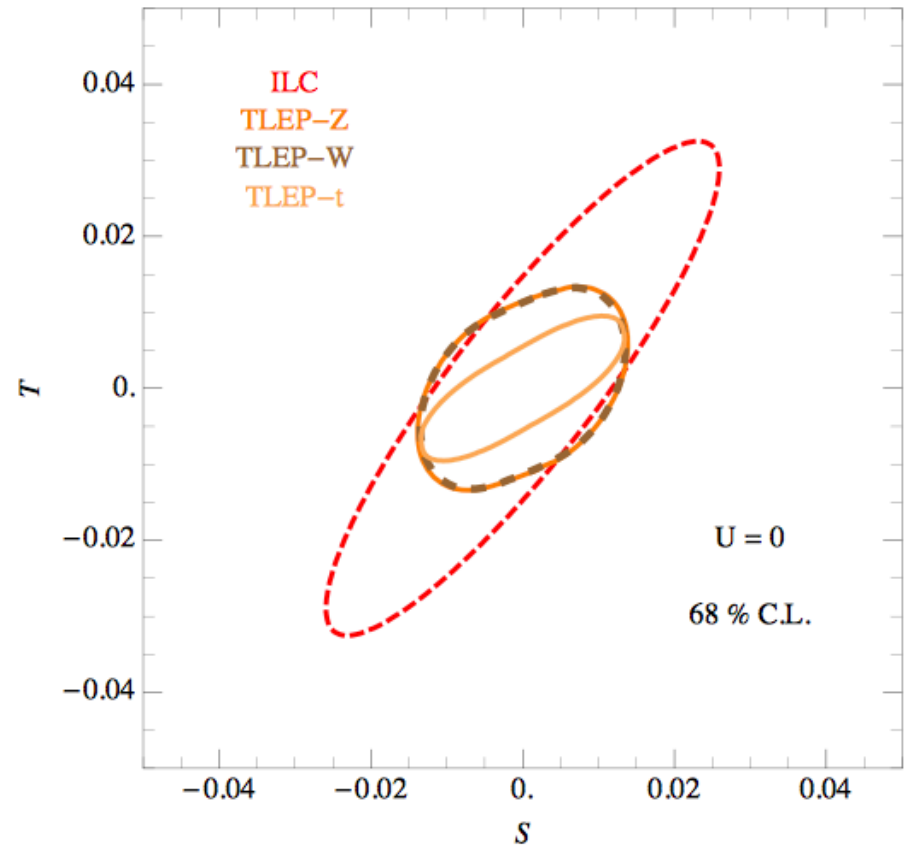
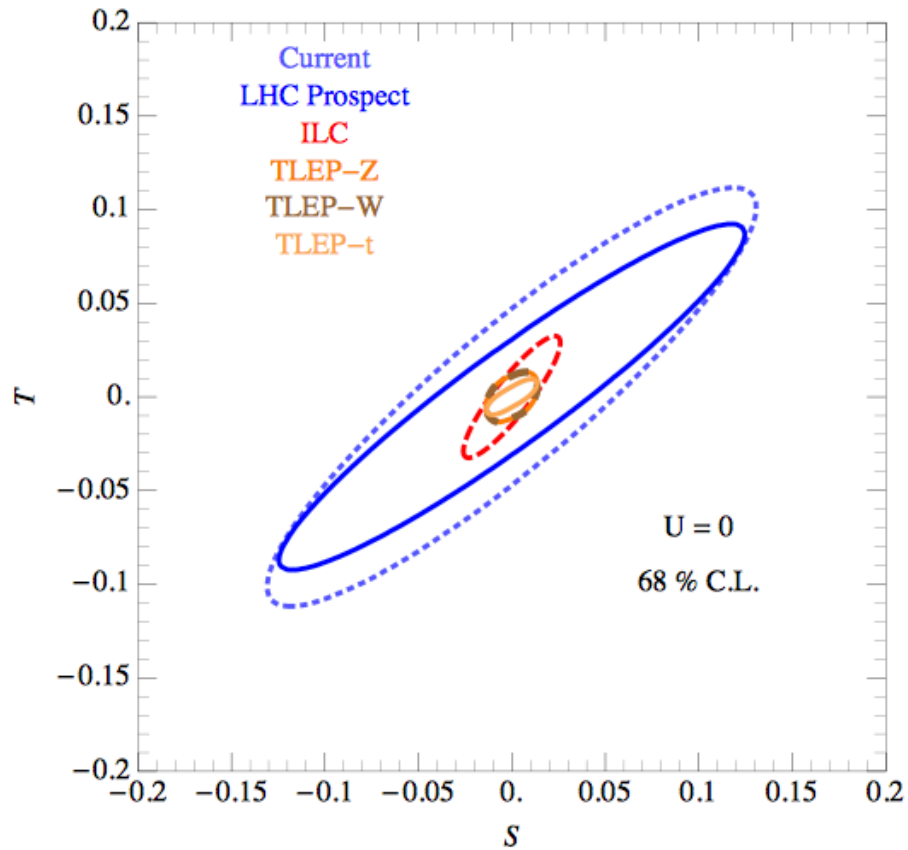
$$\delta m_Z \approx 100 \text{ keV} \quad (\delta m_{Z\text{today}} / \delta m_Z \approx 20)$$

$$\delta m_W \approx 500 \text{ keV} \quad (\delta m_{W\text{today}} / \delta m_W \approx 30, \delta m_{W\text{LHC}} / \delta m_W \approx 16)$$

$$\delta N_\nu \approx 10^{-4} \times 10^{-4} \quad (\delta N_{\nu\text{today}} / \delta N_\nu \approx 8\text{-}20)$$

$$\delta \alpha_s(m_Z)_{\text{today}} / \delta \alpha_s(m_Z) \approx 10\text{-}100 \quad (\text{see Workshop on high-precision } \alpha_s \text{ measurements from LHC to FCC-ee, 12-13 Oct 2015})$$

$$\delta \alpha_{\text{QED}}(m_Z)_{\text{today}} / \delta \alpha_{\text{QED}}(m_Z) \approx 3\text{-}4$$



Fan et al. 1411.1054

$S$  and  $T$  improve by a factor 10, while ILC promises 2-3



With precision on  $S$  and  $T \sim 10^{-2}$

Strongly-interacting theory

$$S \approx 4\pi \frac{v^2}{M^2} \Rightarrow M \sim 10 \text{ TeV}$$

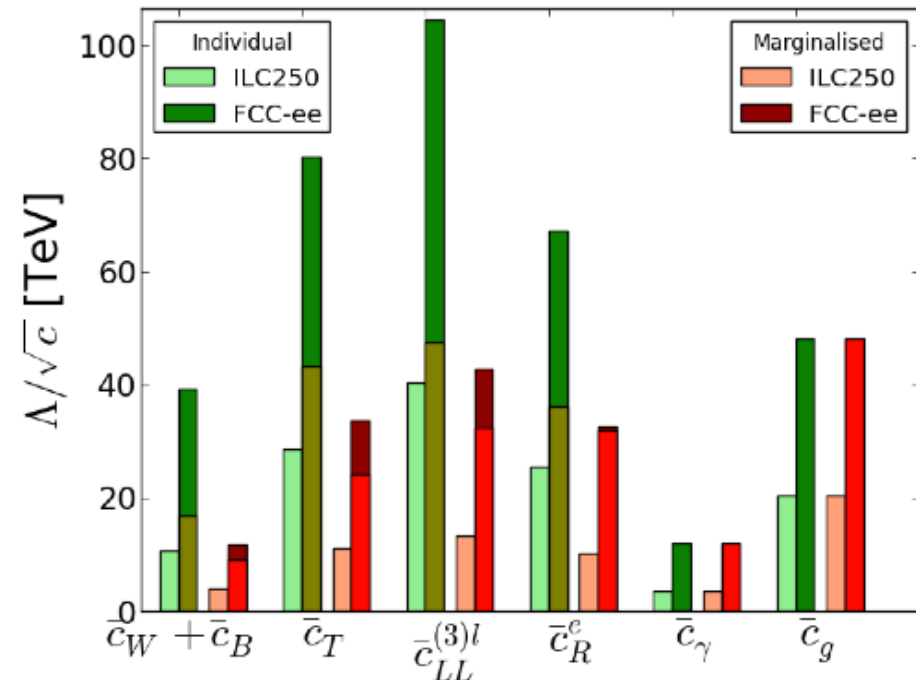
Weakly-interacting theory

$$S \approx \alpha_W \frac{v^2}{M^2} \Rightarrow M \sim 500 \text{ GeV}$$

(stop-like)

$$T \approx \frac{y_t^4}{64\pi^2 \alpha} \frac{v^2}{M^2} \Rightarrow M \sim 1 \text{ TeV}$$

FCC-ee can explore  
some FCC-hh territory



# EFT analysis misses correlations between EW & Higgs observables

$$\left(H^+ \vec{D}^\mu H\right) \left(H^+ \vec{D}_\mu H\right) \Rightarrow \Delta\rho \quad (T)$$

$$\partial^\mu \left(H^+ H\right) \partial_\mu \left(H^+ H\right) \Rightarrow \text{Higgs wavefunction } (\delta g_H)$$

Strong (model-dependent) correlation

Some examples:

# Composite Higgs

If dominant effect comes from

$$\frac{1}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H), \quad \xi \equiv \frac{v^2}{f^2}$$

Uniquely determined by  
the  $\sigma$ -model algebra

$$T = -\frac{3\xi}{8\pi \cos^2 \theta_W} \ln \frac{\Lambda}{m_h} = -0.7\xi \left( 1 + 0.2 \ln \frac{\Lambda}{10 \text{ TeV}} \right)$$

$$S = \frac{\xi}{6\pi} \ln \frac{\Lambda}{m_h} = 0.2\xi \left( 1 + 0.2 \ln \frac{\Lambda}{10 \text{ TeV}} \right)$$

$S, T \sim 10^{-2} \iff$  Higgs couplings: few %

Stop left

$$T = \frac{m_t^2}{4\pi \sin^2 \theta_W m_W^2} \delta g_{Hgg} = 1.6 \delta g_{Hgg}$$

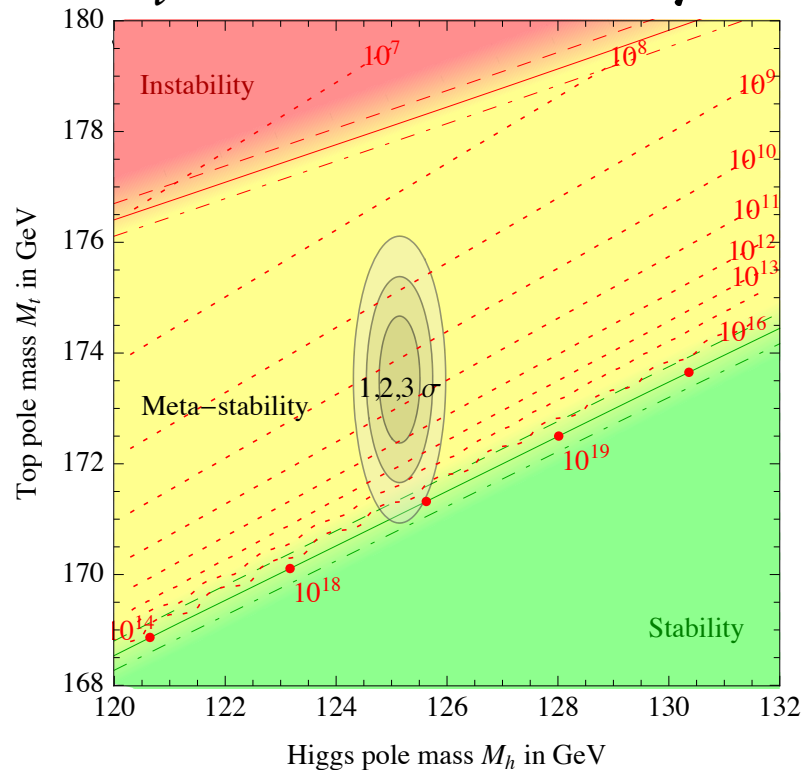
$T \sim 10^{-2} \iff$  Higgs-gluon coupling: 0.6%

# Top mass measurements at threshold

	$m_{\text{top}}$	$\Gamma_{\text{top}}$	$g_{\text{H}t\bar{t}}$
TLEP	10 MeV	11 MeV	13%
ILC	31 MeV	34 MeV	40%

	LHC		ILC		FCCee	
	exp.	th.	exp.	th.	exp.	th.
$\Delta m_W$ (MeV)	10	4	7	1.0	0.5	1.0
$\Delta m_{\text{top}}$ (MeV)	600	250	34	100	10	100
$\Delta m_H$ (MeV)	100		35		7	

$N^3\text{LO}$  calculations can relate such measurements to a well-defined  $m_t$  with an accuracy below 50 MeV



1307.3536

$m_t$  is an input not only in EW data, but also in flavour

Lattice QCD promises 1% precision in hadronic parameters in 10 yrs

Example:

$B_s \rightarrow \mu^+ \mu^-$  (first observed by CMS/LHCb in 2014 with 25% accuracy)

Theory prediction

$$BR(B_s \rightarrow \mu^+ \mu^-) = 3.33 \times 10^{-9} \left( 1 \pm 7.2\% \pm 3.06 \frac{\Delta m_t}{m_t} \right)$$

from CKM and hadronic parameters

strong dependence

# Conclusions

- LEP program turned out to be precision, although it aimed also at discovery
- LEP main legacy: SM as an EFT (separation of scales)
- FCC-ee aims at precision; can it make discoveries too (rare  $Z$ ,  $H$ ,  $t$  decays, 'holes' left by LHC)?
- FCC-ee main goal: probe the SM cutoff (new phenomena)
- FCC-ee can explore territory beyond LHC and fill 'holes' invisible to FCC-hh (rare decays, nearly-degenerate weak multiplets, DM models)