# Dissipative dynamics for the expanding anisotropic quark-gluon plasma

#### **Mauricio Martinez Guerrero**

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#### **Outline**

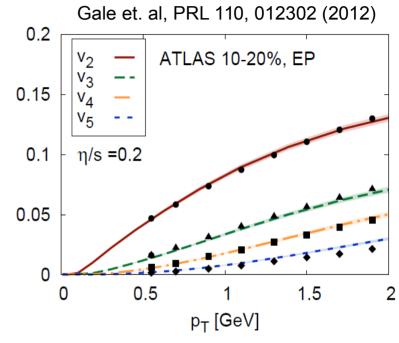
- Introduction
- Kinetic theory approach to highly anisotropic plasmas
  - Anisotropic hydrodynamics (aHydro)
  - Viscous anisotropic hydrodynamics (vaHydro)
- Phenomenological applications
  - First results on pA and AA collisions
  - Electromagnetic probes: photons and dileptons
- Conclusions and outlook

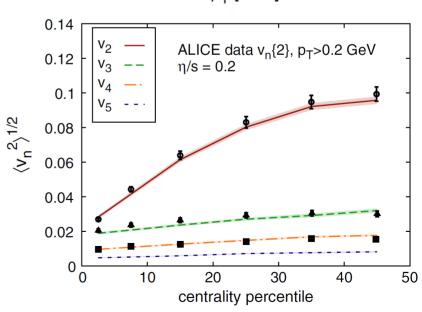
## Success of viscous hydrodynamics

- Viscous hydrodynamics provides a remarkable and successful phenomenological description of the expansion of the quark-gluon plasma
- The anisotropic flow coefficients v<sub>n</sub> are described with a small value of the shear viscosity over entropy ratio

$$\frac{\eta}{s} \sim \mathcal{O}\left(\frac{1}{4\pi}\right)$$

- Hydrodynamics requires as an external input
  - EOS: lattice QCD + hadron resonance gas
  - Hadronization and afterburning
  - Evolution for the dissipative hydrodynamical fields: 2nd order viscous hydro + transport coefficients
  - Initial Conditions: CGC, Glauber, etc
  - Pre-equilibrium dynamics: free streaming, Glasma, etc.





## Why do we need anisotropic hydro?

#### Anisotropies can be large at early times!!!

The pressure anisotropy in an expanding system (Bjorken) within the Navier Stokes limit

 $\left(\frac{P_L}{P_T}\right) \sim 0.35$ 

$$\pi_{NS} = -\frac{4\eta}{3\tau}$$

$$\left(\frac{P_L}{P_T}\right)_{NS} = \frac{P_{eq} - \pi_{NS}/2}{P_{eq} + \pi_{NS}}$$

For  $\eta$ /s=1/(4 $\pi$ ), T= 400 MeV,  $\tau_o$  = 0.5 fm/c (RHIC initial conditions)

$$\left(\frac{P_L}{P_T}\right)_{NS} \sim 0.5$$
 For  $\eta/\text{s}=1/(4\pi)$ , T= 600 MeV,  $\tau_o$  = 0.25 fm/c (LHC initial conditions)

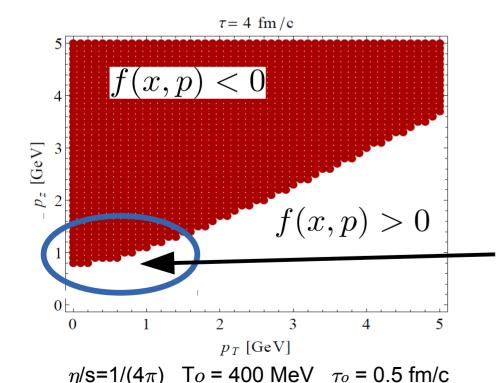
Sizable pressure anisotropies at early times!!!

## Pressure anisotropies from kinetic theory

Linearizing around the equilibrium distribution function leads to viscous hydrodynamics

$$f(x,p) = \underline{f_{eq}(y_0)} + \underline{\delta f(x,p)}$$
 Isotropic in momentum space 
$$\delta f \ll f_{eq}$$

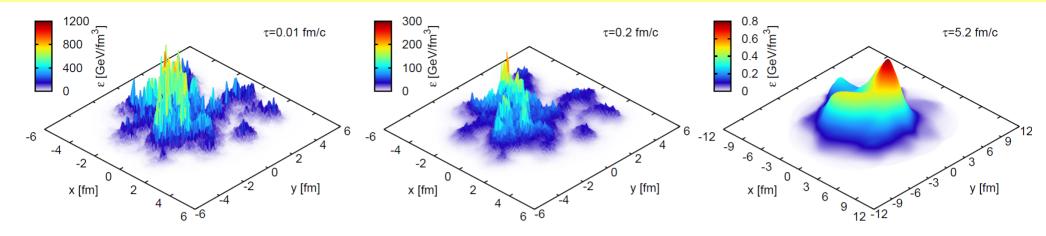
$$y_0 = \frac{(u \cdot p) - \mu}{T} = \frac{\sqrt{m^2 + |\mathbf{p}|^2} - \mu}{T}$$



$$\delta f = \frac{p_{\mu}p_{\nu}\pi^{\mu\nu}}{2(\mathcal{E} + \mathcal{P})T^2}$$
$$= \frac{\eta}{\mathcal{S}} \left( \frac{p_x^2 + p_y^2 - 2p_z^2}{3T^3\tau} \right)$$

For large anisotropies the expansion around equilibrium is not well defined even in the regions of the phase space where hydro should work

# Caveats of hydrodynamical models



#### **Initial Conditions**

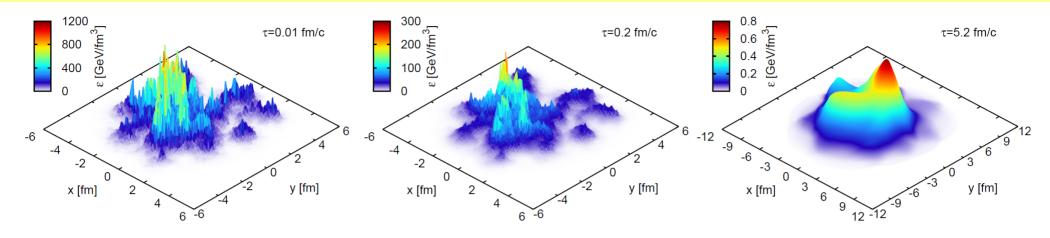
From an initial  $T^{\mu\nu}$  (given for example, by some pre-equilibrium stage prescription) the initial energy density and fluid velocity are obtained by solving

$$\epsilon_{eq.} = u_{\mu}u_{\nu} \mathcal{T}^{\mu\nu}$$

non-equilibrium energy-momentum tensor

- This procedure does not match all the components of the energy momentum tensor
- Gradients of velocity are large at early times  $\sim 1/\tau$

# Caveats of hydrodynamical models



#### What one would like to do

Match each component of the energy momentum tensor

$$T_{hydro}^{\mu\nu} \mid_{\tau_0} = T_{non-eq.}^{\mu\nu} \mid_{\tau_0}$$

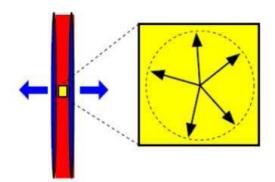
An interesting procedure to get  $T^{\mu\nu}(\tau_0)$  from pre-equilibrium dynamics

Our proposal: develop a theoretical framework that allows us to evolve all the components of  $T^{\mu\nu}$  from a far-fromequilibrium initial state which is highly anisotropic in momentum-space



Viscous Anisotropic hydrodynamics

## Viscous hydro vs. vaHydro



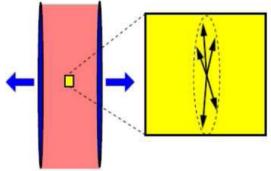
Viscous hydrodynamics

$$f(x,p) = f_{eq} + \delta f(x,p)$$

The equilibrium distribution  $f_{eq}$  function is isotropic in momentum space



All the momentum space anisotropies are perturbations around the equilibrium distribution function



Viscous anisotropic hydrodynamics

$$f(x,p) = f_a + \delta \tilde{f}(x,p)$$

The leading order distribution function fa encodes the largest anisotropies developed at early times



Deviations from the spheroidal form of the leading order term are treated as small perturbations

#### Foundations of vaHydro

$$f(x,p) = \underbrace{f_a(\sqrt{p_\mu p_\nu \Xi^{\mu\nu}},\Lambda(x))}_{\mbox{Local anisotropic background}} + \underbrace{\delta \tilde{f}(x,p)}_{\mbox{Residual dissipative corrections}}$$

## Foundations of vaHydro

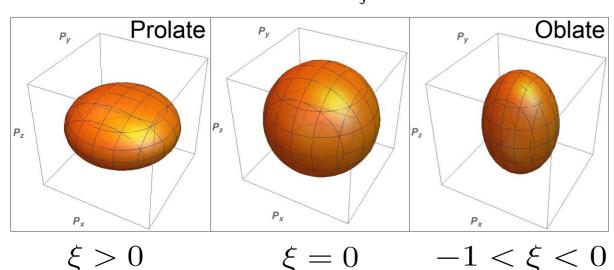
$$f(x,p) = \underbrace{f_a(\sqrt{p_\mu p_\nu \Xi^{\mu\nu}},\Lambda(x))}_{\mbox{Local anisotropic background}} + \underbrace{\delta \tilde{f}(x,p)}_{\mbox{Residual dissipative corrections}}$$

aHydro: large viscous effects are encoded in the leading order term.

$$f_a\left(\sqrt{p_{\mu}p_{\nu}\Xi^{\mu\nu}},\Lambda(x)\right) = f_{eq.}\left(\sqrt{p_T^2 + (1+\xi)p_z^2},\Lambda(x)\right)$$

$$\Xi^{\mu\nu} = u^{\mu}u^{\nu} + \xi z^{\mu}z^{\nu}$$

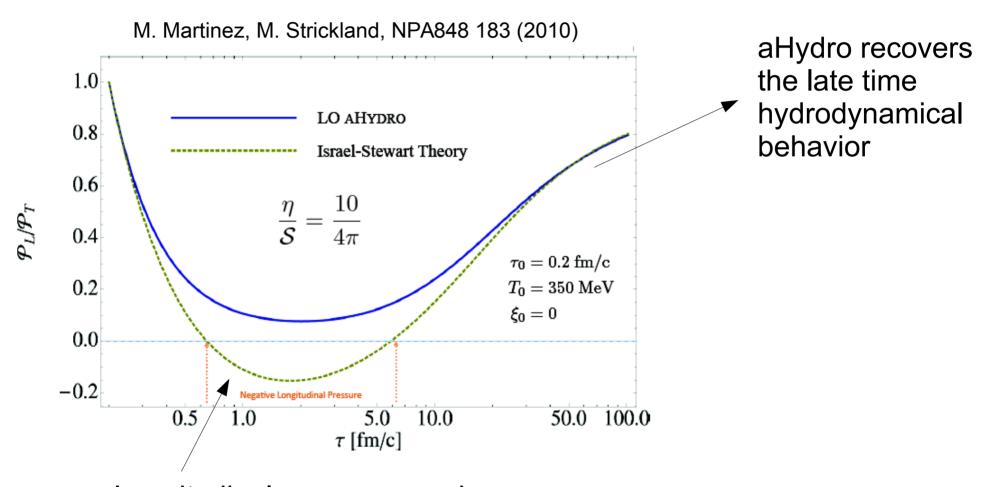
M. Martinez, M. Strickland, NPA848 183 (2010) Florkowski, Ryblewski, PRC83 034907 (2011)



- $\Lambda$  is the temperature-like scale
- ξ regulates the longitudinal component of the shear viscous tensor
- For simplicity no chemical potential

## Viscous hydro vs. aHydro

#### Consider Bjorken expansion and massless particles



Longitudinal pressure can be negative for IS theory.

Similar findings: Florkowski, Ryblewski, PRC83 034907 (2011)

## Foundations of vaHydro

$$f(x,p) = f_a(\sqrt{p_{\mu}p_{\nu}\Xi^{\mu\nu}}, \Lambda(x)) + \delta \tilde{f}(x,p)$$

The energy-momentum tensor for an anisotropic plasma reads as

$$T^{\mu\nu} = \langle p^{\mu} p^{\nu} \rangle$$

$$= \underbrace{\mathcal{E}} u^{\mu} u^{\nu} - \underbrace{\mathcal{P}} + \underbrace{\tilde{\Pi}} \Delta^{\mu\nu} + \underbrace{\mathcal{P}}^{\mu\nu} + \underbrace{\tilde{\pi}}^{\mu\nu}$$

with

$$\mathcal{E} \equiv \langle (u \cdot p)^2 \rangle_a, \quad \tilde{\Pi} \equiv -\frac{1}{3} \langle \Delta^{\alpha\beta} p_{\alpha} p_{\beta} \rangle_{\tilde{\delta}}, 
\tilde{\pi}^{\mu\nu} \equiv \langle p^{\langle \mu} p^{\nu \rangle} \rangle_{\tilde{\delta}}, \quad \mathcal{P}_L \equiv \langle p_z^2 \rangle_a, 
\mathcal{P}_{\perp} \equiv \frac{1}{2} \langle (p_x^2 + p_y^2) \rangle_a, \quad \mathcal{P}^{\mu\nu} \equiv (\mathcal{P}_L - \mathcal{P}_{\perp}) z^{\mu} z^{\nu},$$

where 
$$\langle \cdots \rangle = \int_{\mathbf{p}} (\cdots) f$$
,  $\langle \cdots \rangle_a = \int_{\mathbf{p}} (\cdots) f_a$ ,  $\langle \cdots \rangle_{\tilde{\delta}} = \int_{\mathbf{p}} (\cdots) \delta \tilde{f}$ 

Bazow, Heinz, Strickland, PRC90,054910 (2014), Bazow, Martinez, Heinz, PRD93, 034002 (2016)

## Foundations of vaHydro

 Eqs. of motion of the energy density and fluid velocity are obtained from the conservation laws

$$D_{\mu}T^{\mu\nu} = 0$$

• Eqs. of motion of the residual dissipative currents are obtained from moments method (Denicol et. al, PRD85, 114047 (2012))

$$\dot{\tilde{\pi}}^{\mu\nu} = \int_{\mathbf{p}} p^{\langle\mu} p^{\nu\rangle} \underbrace{\delta\dot{\tilde{f}}}_{\mathbf{p}}$$

Use Boltzmann equation:

$$\delta \dot{\tilde{f}} = -\dot{f}_a - (u \cdot p)^{-1} \left( p \cdot \nabla (f_a + \delta \tilde{f}) - \mathcal{C}[f] \right)$$

One needs a relation between the EOS. For conformal systems

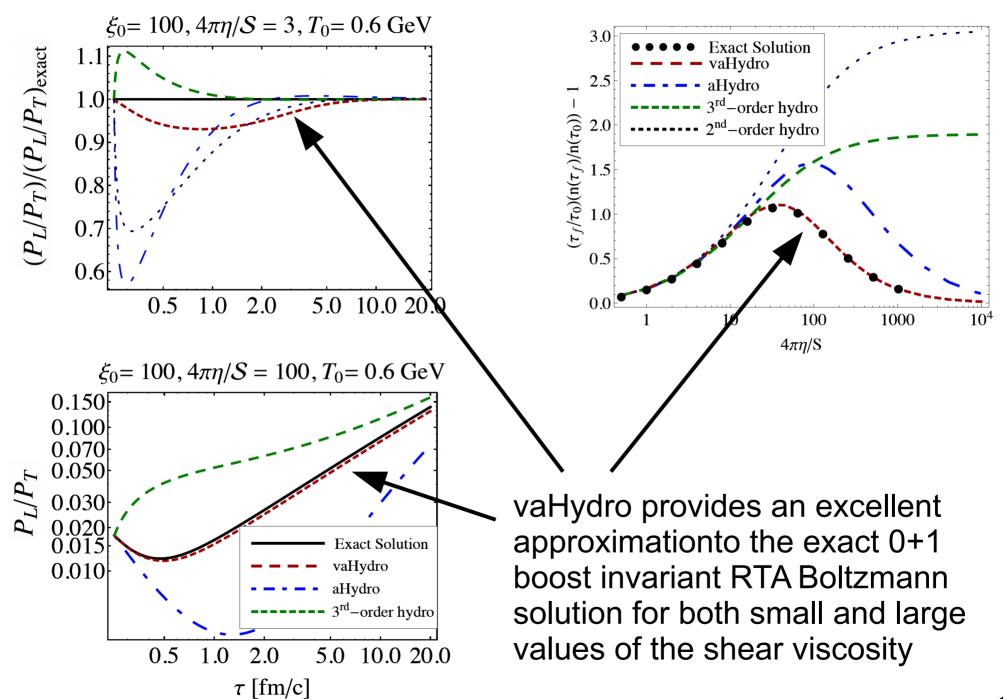
$$\mathcal{E} = 2\mathcal{P}_T + \mathcal{P}_L$$

• We require the dynamical Landau matching conditions. For instance

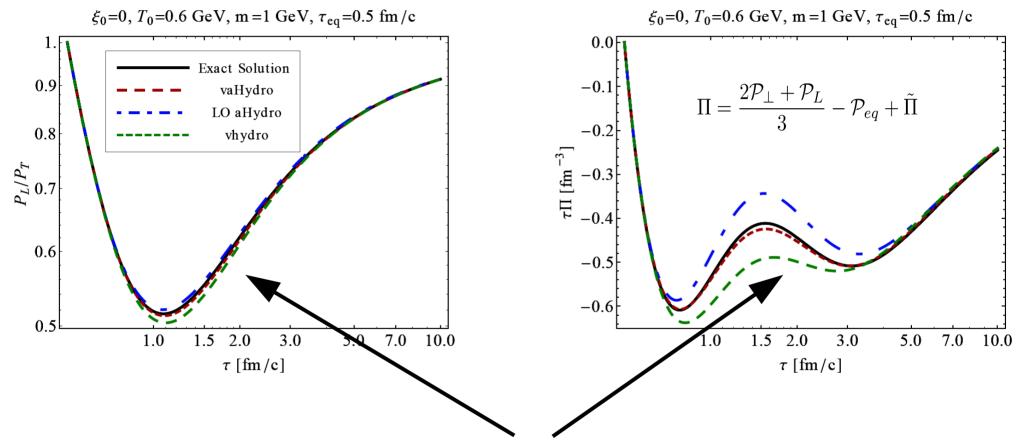
$$\mathcal{E}(\xi, \Lambda) = \mathcal{E}(T)$$

Other approaches: Molnar, Niemi, Rischke, arXiv:1602.00573
Florkowski, Tinti, Strickland, Ryblewski, NPA946, 29 (2016)

## Testing vaHydro: conformal systems

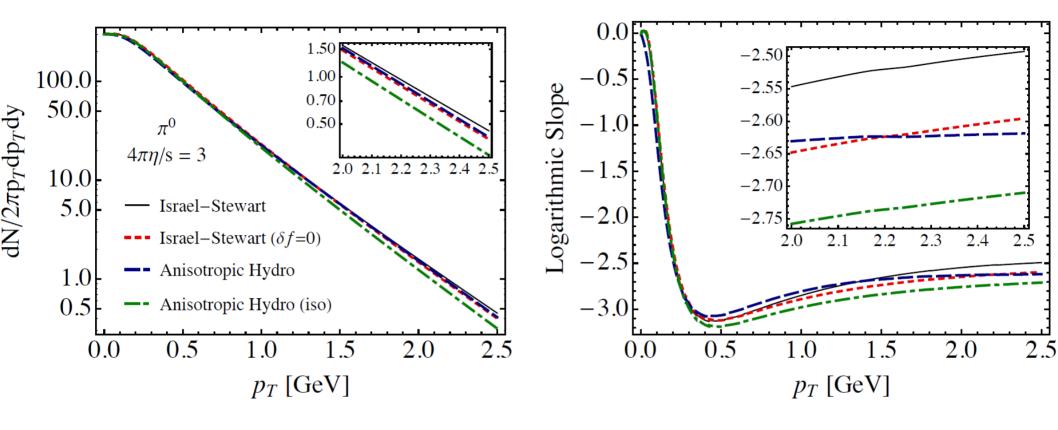


#### Testing vaHydro: nonconformal systems



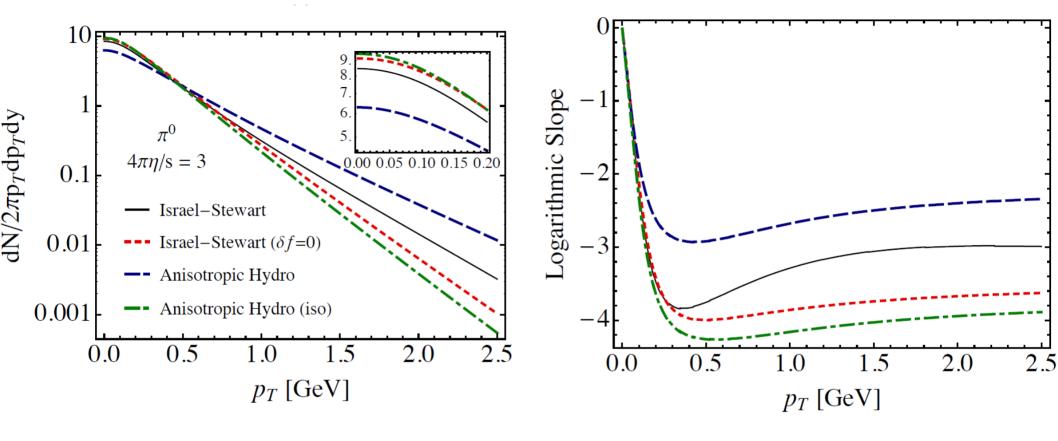
vaHydro provides an excellent approximation to the exact 0+1 boost invariant RTA Boltzmann solution for massive particles.

#### AA collisions: 1+1 dim. expansion



- Anisotropic hydro softens the transverse momentum spectrum since it reduces the pressure anisotropy and thus the transverse shear pressure.
- Larger differences between IS viscous hydro and anisotropic hydro are observed for large values of shear viscosity

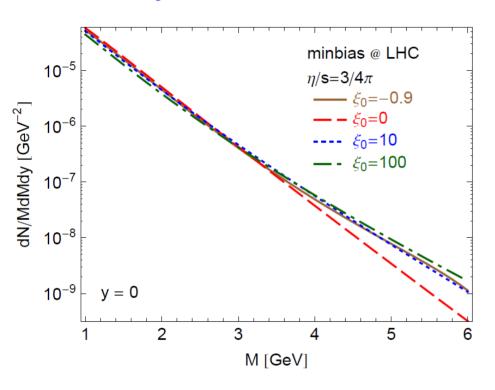
## pA collisions: 1+1 dim. expansion

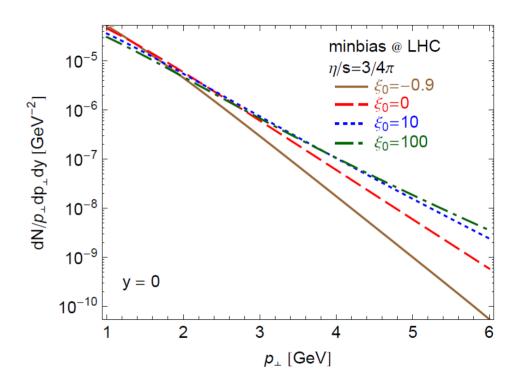


- aHydro improves the description of smaller systems compared to viscous IS hydro since the pressure anisotropies get larger.
- aHydro hardens the transverse momentum spectrum for smaller systems

#### Dileptons from an anisotropic plasma

3+1 dim. aHydro (no event by event fluctuations) R. Ryblewski, M. Strickland, PRD92 025026 (2015)



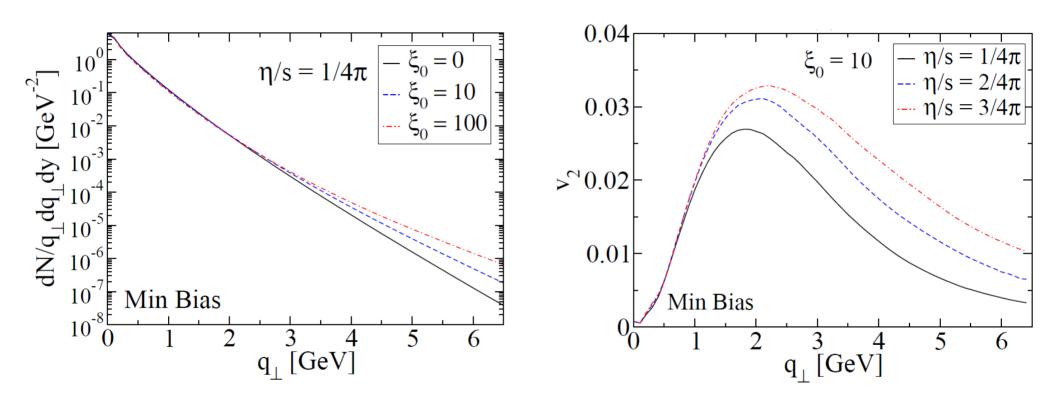


#### Dilepton yield is sensitive to the initial anisotropy

Bjorken expansion: Martinez, Strickland, PRL100 102301 (2007), PRC 78 034917 (2008), Eur. Phys. J C61 905 (2009)

#### Photons from an anisotropic plasma

3+1 dim. aHydro (no event by event fluctuations)
L. Bhattacharya, R. Ryblewski, M. Strickland, PRD93 065005 (2016)



Photon spectrum and photon elliptic flow coefficient v<sub>2</sub> are sensitive to the initial anisotropy!!!

#### Conclusions

#### Viscous Anisotropic Hydrodynamics:

- Improves the validity of fluid dynamic approach
  - at early time dynamics.
  - near the transverse edge of the fireball
- Exact solutions of the Boltzmann equation have helped to quantify the accuracy and validity of vaHydro.
- vaHydro handles large momentum-space anisotropies better than IS which are important during the evolution of the fireball.

#### Conclusions

#### Viscous Anisotropic Hydrodynamics:

- Sizable difference between the predictions of IS viscous hydro and anisotropic hydrodynamics are observed in smaller systems
- Dileptons and photons are sensitive to the initial anisotropy of the system

#### Outlook

#### Viscous Anisotropic hydrodynamics

- Chemical equilibrium of quarks and gluons
- Bottomonia suppression
- 3+1 numerical code of vaHydro (forthcoming OSU-Kent)
  - Event by event fluctuations with vaHydro

#### Anisotropic hydro meets cold atoms

Bluhm and Schaefer:

PRA92 043602 (2015), PRL116 115301 (2016)