

# Forward-backward correlations between intensive observables

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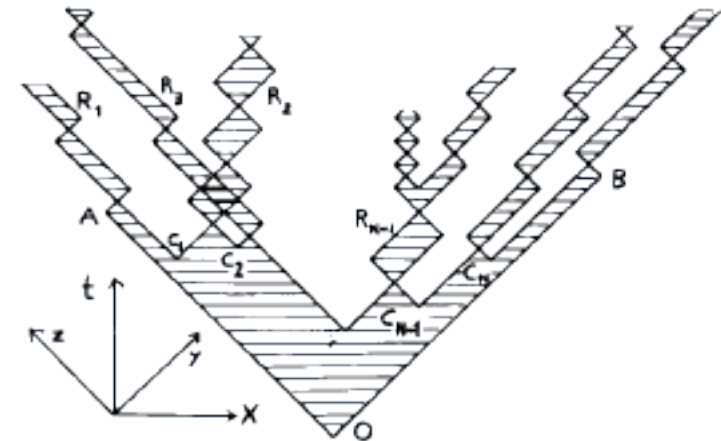
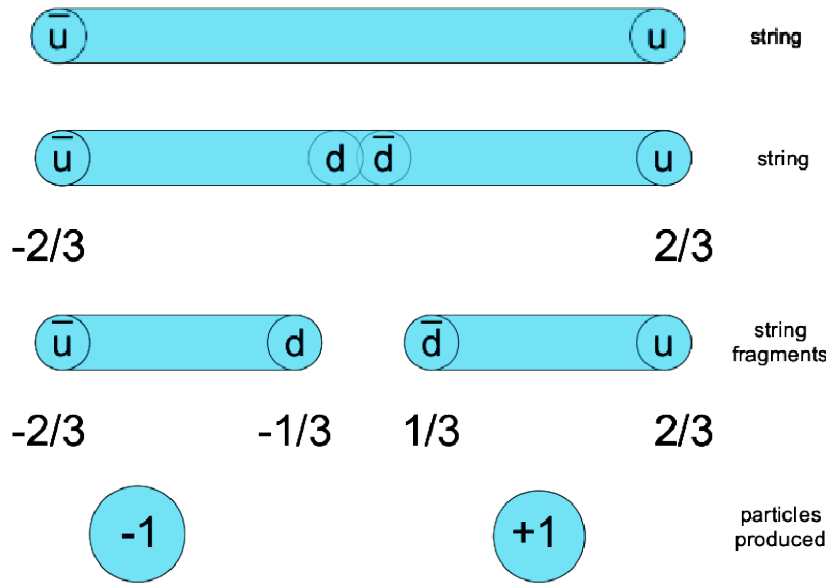
3rd International Conference on the Initial Stages in  
High-Energy Nuclear Collisions (InitialStages2016)

23-27 May 2016

Centro de Congressos, Instituto Superior Técnico, Alameda Campus

# String models

- The soft QCD processes is not described by usual perturbation theory
- The model of quark-gluon strings, stretched between projectile and target partons
  - semiphenomenological approach to the multiparticle production

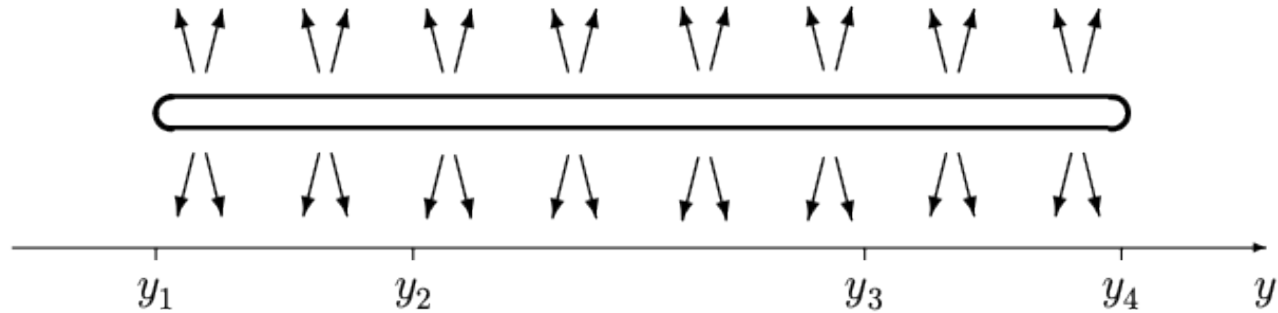


X. Artru and G. Mennessier, Nucl Phys B 70 (1974) 93  
 "String Model and Multiproduction",

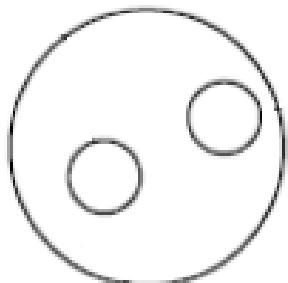
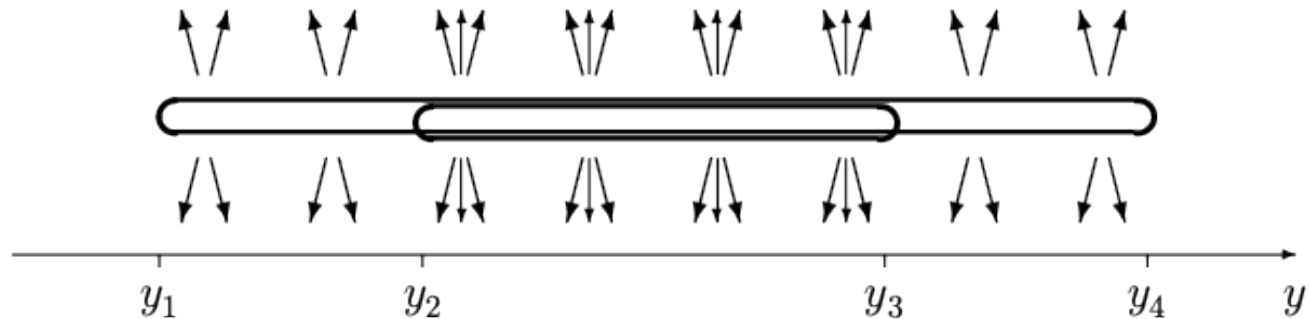
- Correlations play crucial role:
  - causality requires appearance of long-range correlations – if they exist – at the very early stages between particles detected in separated rapidity intervals

# String in rapidity space

- Uniform and independent distribution of particles on rapidity from  $y_{\min}$  to  $y_{\max}$

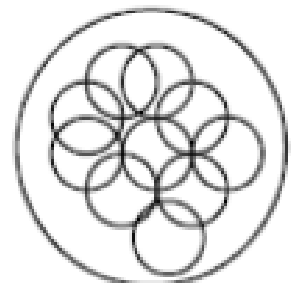
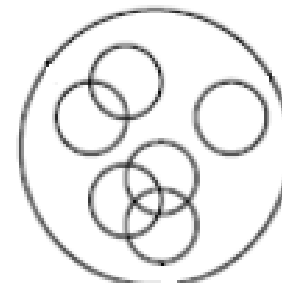


- Can study string overlaps:



Multi-parton interactions

heavy ions



-->>>  $\sqrt{s}$  increases -->>>

-->>>

-->>>

# String fusion

$$Q^2(n) = \left( \sum_{i=1}^n \vec{Q}_i(1) \right)^2 = \sum_{i=1}^n Q_i^2(1) + \sum_{i \neq j} \vec{Q}_i(1) \cdot \vec{Q}_j(1)$$

$$\langle Q^2(n) \rangle = nQ^2(1)$$

overlaps

SFM

$$C = \{S_1, S_2, \dots\}$$

$S_k$  – area covered k-times



$$\langle \mu \rangle_k = \mu_0 \sqrt{k} \frac{S_k}{\sigma_0} \quad \langle p_t^2 \rangle_k = p_0^2 \sqrt{k} \quad \langle p_t \rangle_k = p_0 \sqrt[4]{k}$$

$S_k$  – area, where k strings are overlapping,  $\sigma_0$  single string transverse area,  $\mu_0$  and  $p_0$  – mean multiplicity and transverse momentum from one string

String fusion mechanism predicts:

- decrease of multiplicity
- increase of  $p_T$
- growth of  $p_T$  with multiplicity in pp, pA and AA collisions
- growth of strange particle yields
- results are in a good agreement with the experiment

M. A. Braun, C. Pajares, Nucl. Phys. B 390 (1993) 542.

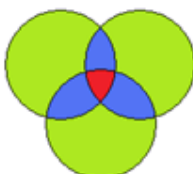
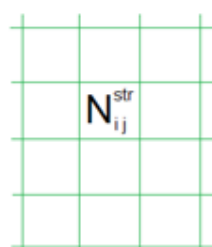
M. A. Braun, R. S. Kolevatorov, C. Pajares, V. V. Vechernin, Eur. Phys. J. C 32 (2004) 535.

N.S. Amelin, N. Armesto, C. Pajares, D. Sousa, Eur.Phys.J.C22:149-163 (2001), arXiv:hep-ph/0103060

G. Ferreiro and C Pajares J. Phys. G: Nucl. Part. Phys. 23 1961 (1997)

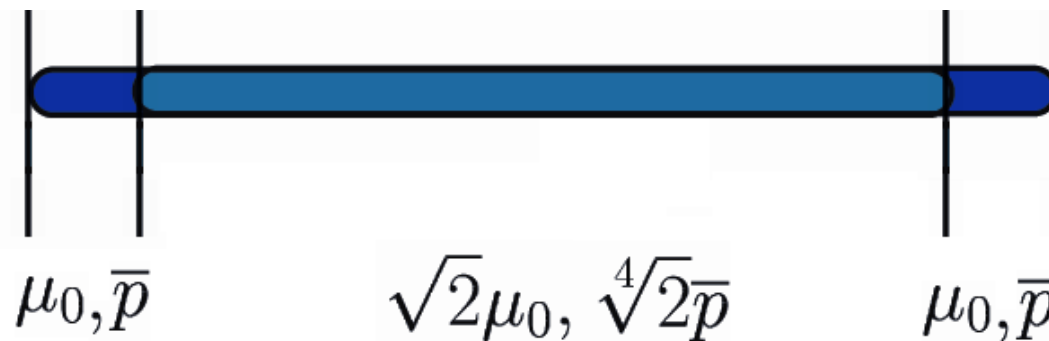
# String fusion

- Lattice realization of string fusion model

	"overlaps" (local fusion)		"overlaps" (local fusion)
SFM	<div style="display: flex; align-items: center;"> <div style="margin-right: 10px;"> <math>C = \{S_1, S_2, \dots\}</math>  <math>S_k</math> – area covered k-times                 </div>  <div style="margin-left: 10px; color: blue;">                     cellular analog of SFM                 </div> </div>		<div style="display: flex; align-items: center;"> <div style="margin-right: 10px;"> <math>C = \{N_{ij}^{str}\}</math>  <math>k_{ij} = N_{ij}^{str}</math> – “occupation” numbers                 </div>  </div>

V. V. Vechernin and R. S. Kolevato, Vestn. SPb. Univ., Ser. Fiz. Khim., No. 2, 12 (2004); hep-ph/0304295.  
 V. V. Vechernin and R. S. Kolevato, Vestn. SPb. Univ., Ser. Fiz. Khim., No. 4, 11 (2004); hep-ph/0305136.  
 I. A. Lakomov, V. V. Vechernin, PoS (Baldin ISHEPP XXI) 072 (2012).

- Fusion of finite rapidity strings



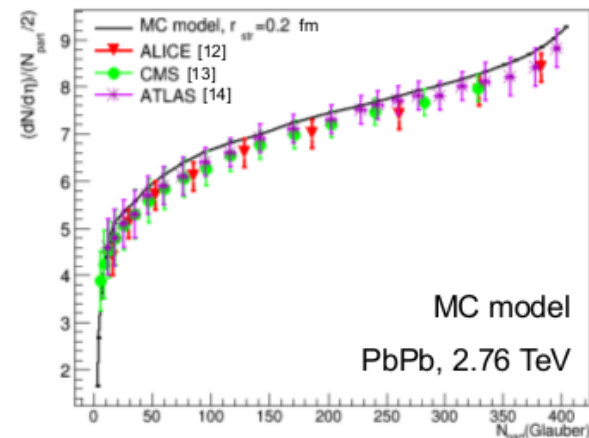
# Monte Carlo model

- Partonic dipole-based picture of nucleons interaction.
- Energy and angular momentum conservation in the initial state of a nucleon.
- The probability of dipoles are defined by their transverse coordinates [7-8]:

$$f = \frac{\alpha_s^2}{2} \ln^2 \frac{|\vec{r}_1 - \vec{r}'_1| |\vec{r}_2 - \vec{r}'_2|}{|\vec{r}_1 - \vec{r}'_2| |\vec{r}_2 - \vec{r}'_1|}$$

Multiplicity and transverse momentum are obtained in the approach of colour strings, stretched between projectile and target partons

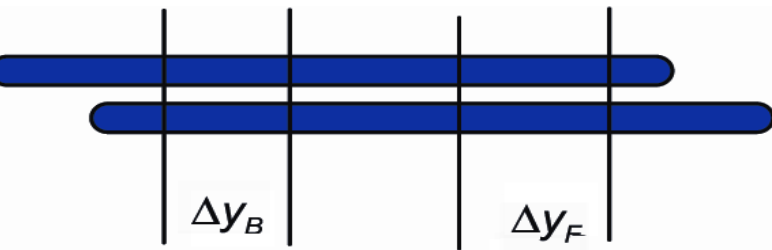
- The interaction of strings is realized in the accordance with the **string fusion** model
- Multiplicity from one string is distributed according to Poisson



V. N. Kovalenko.. Phys. Atom. Nucl. 76, 1189 (2013), arXiv:1211.6209 [hep-ph]

V. Kovalenko, V. Vechernin., PoS (Baldin ISHEPP XXI) 077, arXiv:1212.2590 [nucl-th], 2012

# Forward-backward correlations

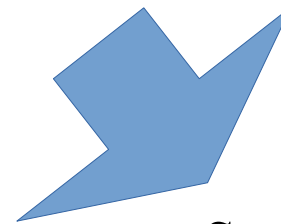


Select 2 variables in windows:

F, B:  $\left\{ \begin{array}{l} n \quad \text{-- number of charged particles in the window} \\ p_t = \frac{1}{n} \sum_{i=1}^n p_{ti} \quad \text{-- mean (in the event!) transverse momentum of charged particles in the given window} \end{array} \right.$

correlation coefficient

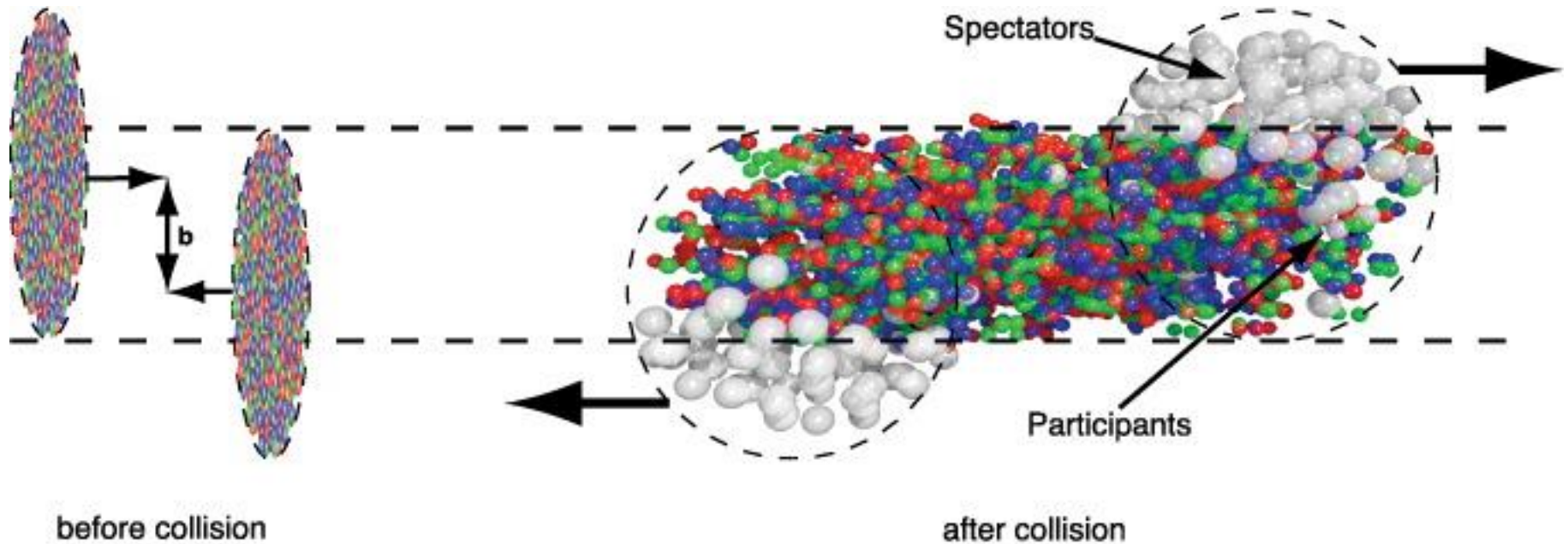
$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2}$$



Several types of correlation coefficient:

n-n , pt-n, **pt-pt**

# Centrality of AA collisions



- Nucleon-participants  $N_{part}$  - nucleons collided at least once
- Nucleon-spectators  $N_{spect}$  - nucleons, which didn't interact
- Number of nucleon-nucleon collisions  $N_{coll}$
- Multiplicity of charge particles  $N_{ch}$

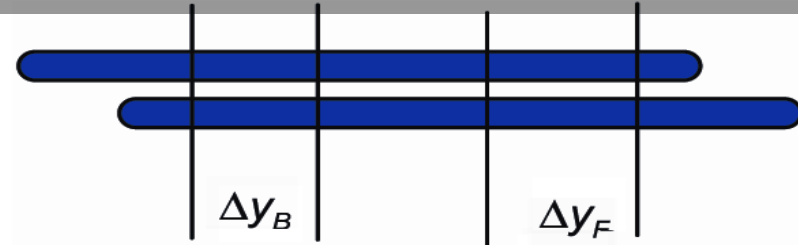


# Forward-backward correlations in AA

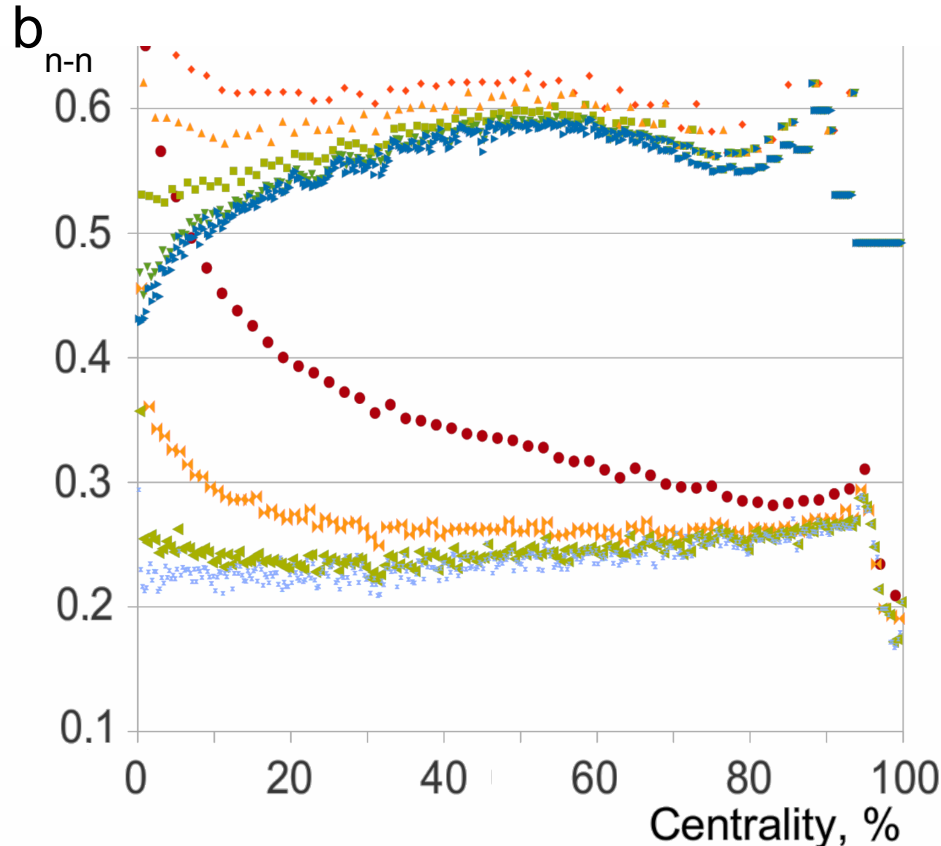
multiplicity – extensive variable

n-n correlation coefficient

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2}$$



- ▶ 0.25%*c*  $N_{part}$
- ▼ 0.5%*c*  $N_{part}$
- ▲ 1.5%*c*  $N_{part}$
- 1%*c*  $N_{part}$
- ◆ 2%*c*  $N_{part}$
- ⋈ 0.25%*c*  $v_{zero}$
- ▼ 0.5%*c*  $v_{zero}$
- ⋈ 1%*c*  $v_{zero}$
- 2%*c*  $v_{zero}$



Pb-Pb, 2.76 TeV

depends on

**method of centrality determination**

**width of centrality class**

V. Kovalenko, V. Vechernin. EPJ Web of Conferences 66, 04015 (2014), arXiv:1308.6618 [nucl-th]

# Mean pt-pt correlations in SF model

mean event transverse momentum – **intensive** variable

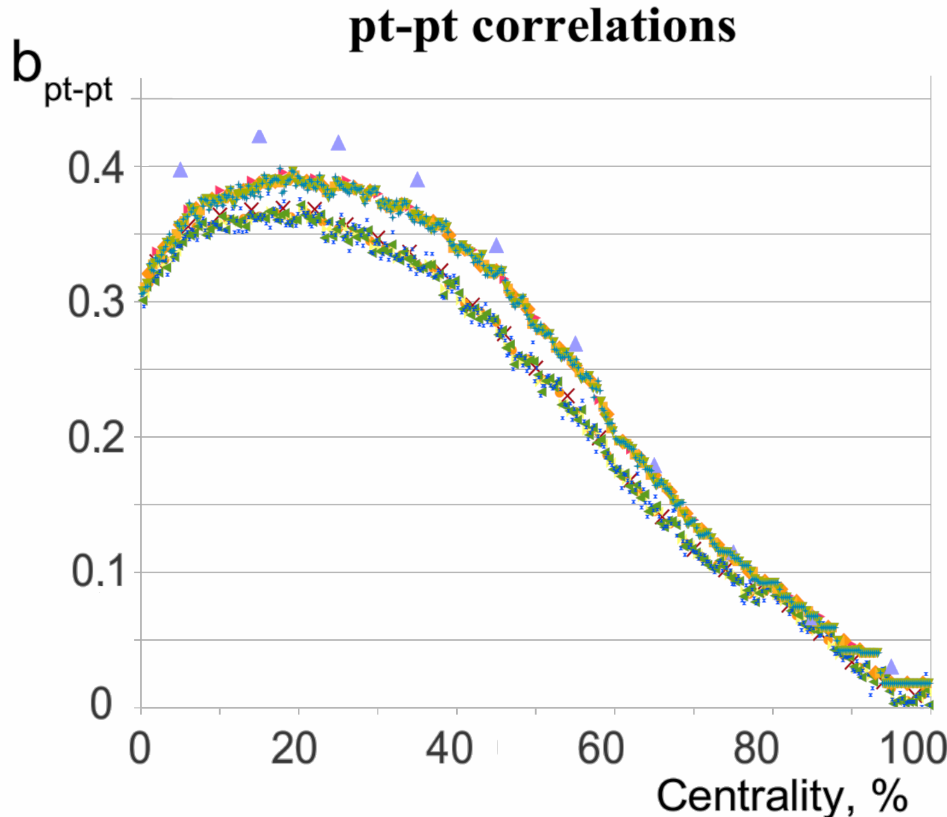
pt-pt correlation coefficient

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2}$$

$$B, F, \rightarrow p_t = \frac{1}{n} \sum_{i=1}^n p_{ti}$$

Pb-Pb, 2.76 TeV

- ✦ 0.25% $c$   $N_{\text{part}}$
- ▼ 0.5% $c$   $N_{\text{part}}$
- ▲ 1.5% $c$   $N_{\text{part}}$
- 1% $c$   $N_{\text{part}}$
- ◆ 2% $c$   $N_{\text{part}}$
- ▶ 4% $c$   $N_{\text{part}}$
- ▲ 10% $c$   $N_{\text{part}}$
- ✦ 0.25% $c$   $v_{\text{zero}}$
- ▼ 0.5% $c$   $v_{\text{zero}}$
- ✦ 1% $c$   $v_{\text{zero}}$
- 2% $c$   $v_{\text{zero}}$
- ✕ 4% $c$   $v_{\text{zero}}$



robust

V. Kovalenko, V. Vechernin. EPJ Web of Conferences 66, 04015 (2014), arXiv:1308.6618 [nucl-th]

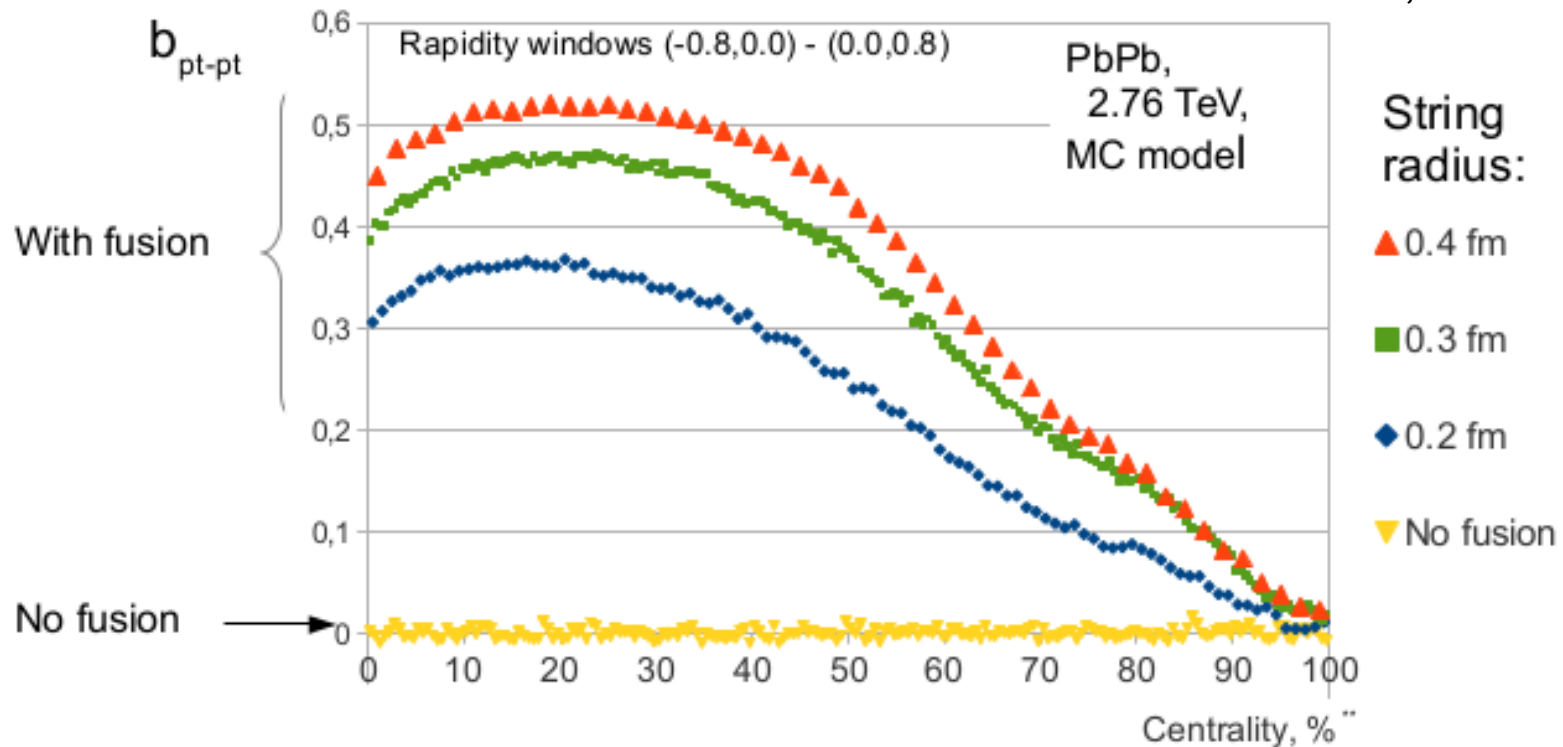
# Mean pt-pt correlations in SF model

correlation coefficient

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Pb-Pb, 2.76 TeV

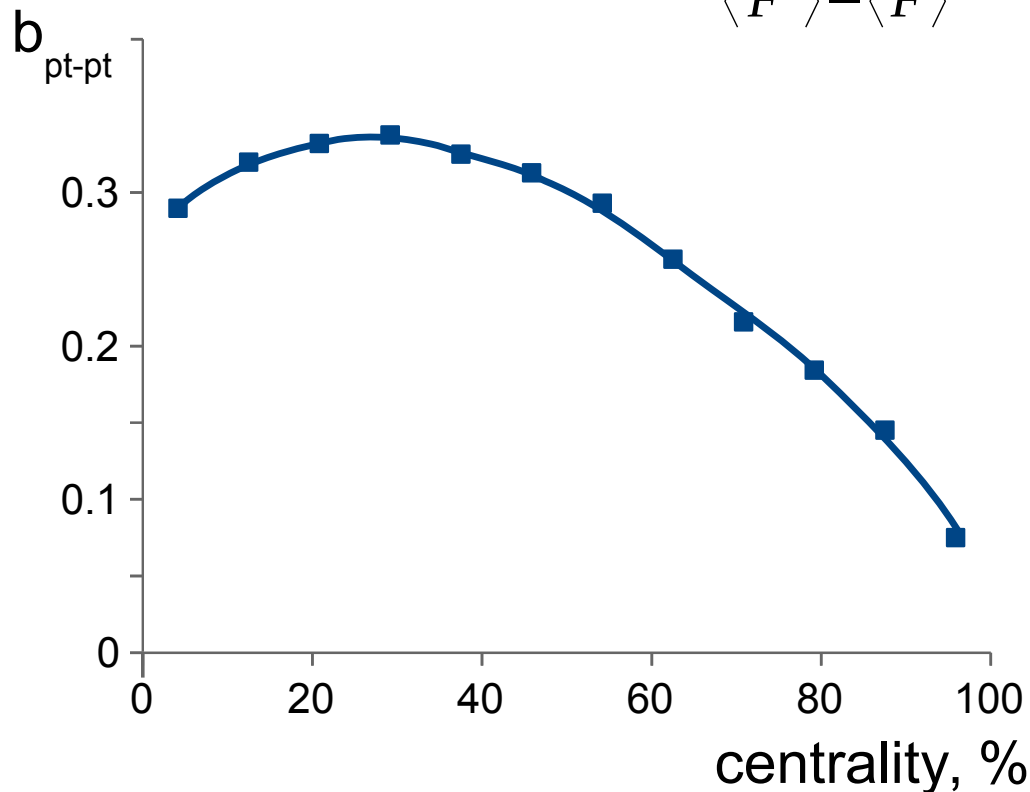


V. Kovalenko, V. Vechernin. EPJ Web of Conferences 66, 04015 (2014), arXiv:1308.6618 [nucl-th]

# Mean pt-pt correlations in different models

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2} \quad B, F, \rightarrow p_t = \frac{1}{n} \sum_{i=1}^n p_{ti}$$

Pb-Pb, 2.76 TeV



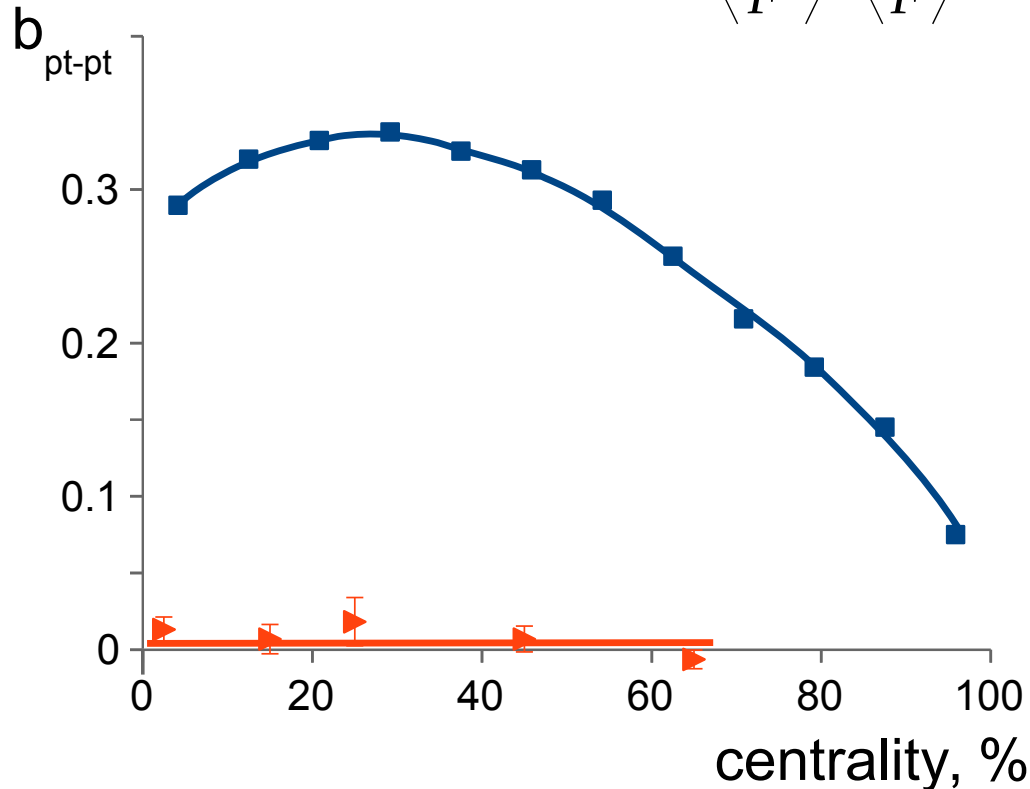
■ String fusion

Pb-Pb, 2.76 TeV, MC model with string fusion,  $r_{str} = 0.2$  fm, pseudorapidity windows  $(-0.8, -0.4)$ ,  $(0.4, 0.8)$ , no  $p_t$  cut

# Mean pt-pt correlations in different models

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2} \quad B, F, \rightarrow p_t = \frac{1}{n} \sum_{i=1}^n p_{ti}$$

Pb-Pb, 2.76 TeV



■ String fusion  
 ▶ THERMINATOR2

THERMINATOR 2 (THERMal heavy IoN generATOR 2)

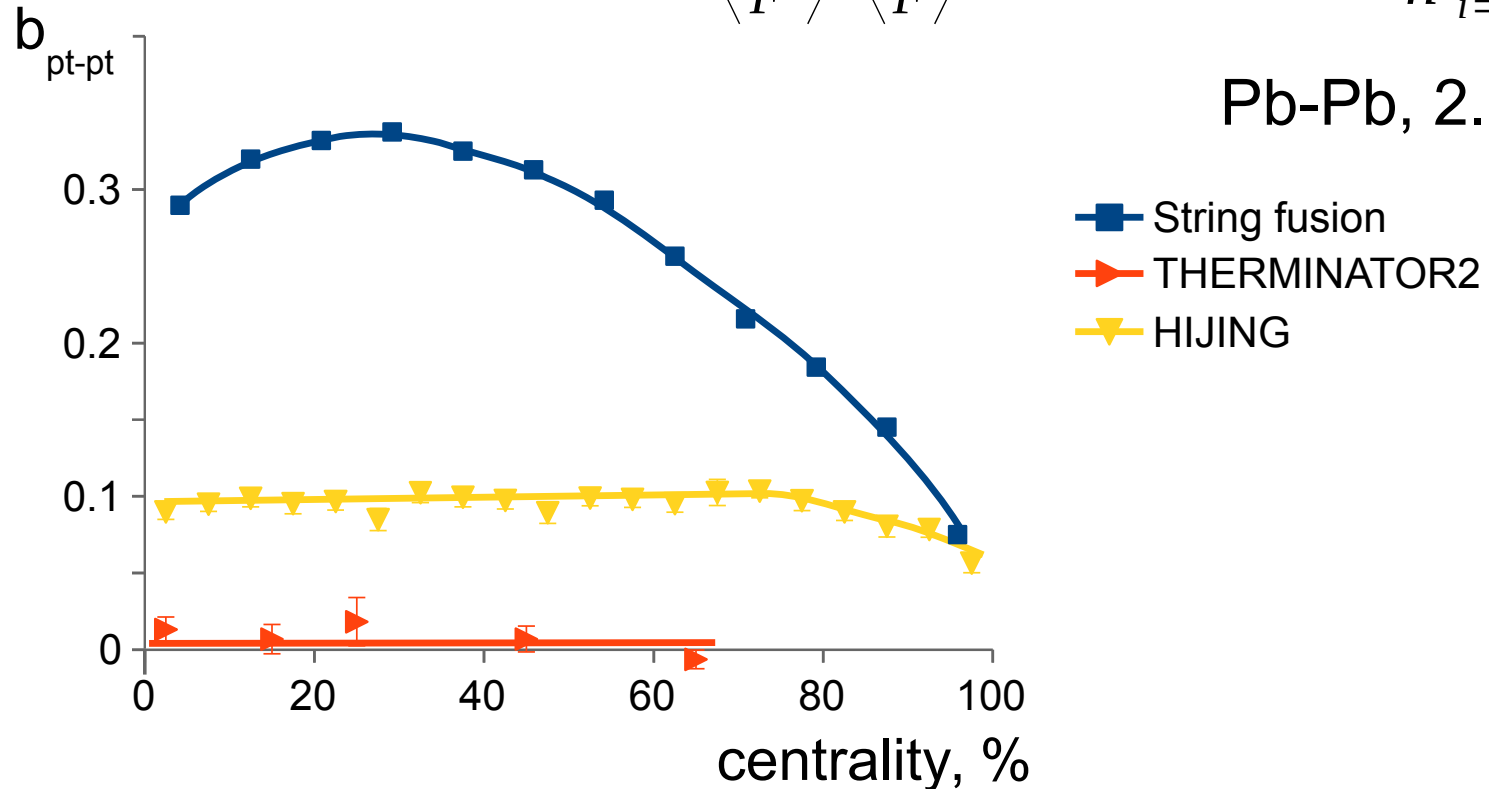
M. Chojnacki et al, Comput. Phys. Commun. 183, 746 (2012)

parametrized freeze-out hypersurface, Cooper-Frye + decays

# Mean pt-pt correlations in different models

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2} \quad B, F, \rightarrow p_t = \frac{1}{n} \sum_{i=1}^n p_{ti}$$

Pb-Pb, 2.76 TeV



HIJING (Heavy Ion Jet Interaction Generator)

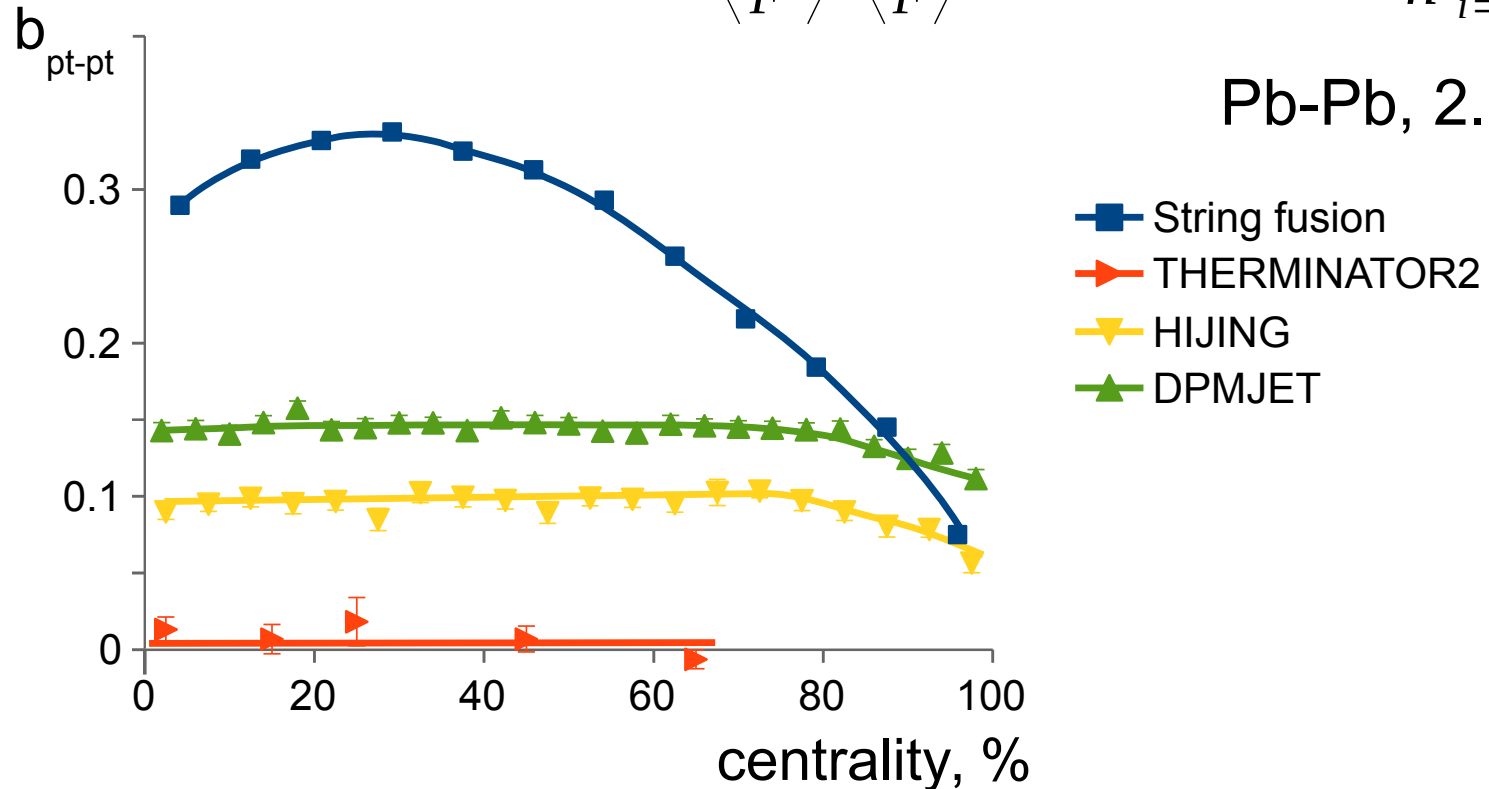
Xin-Nian Wang and Miklos Gyulassy, Phys.Rev.D 44, 3501 (1991)

Gluon shadowing + Jet quenching

# Mean pt-pt correlations in different models

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2} \quad B, F, \rightarrow p_t = \frac{1}{n} \sum_{i=1}^n p_{ti}$$

Pb-Pb, 2.76 TeV



DPMJET, two-component Dual Parton Model, based on the Gribov-Glauber approach

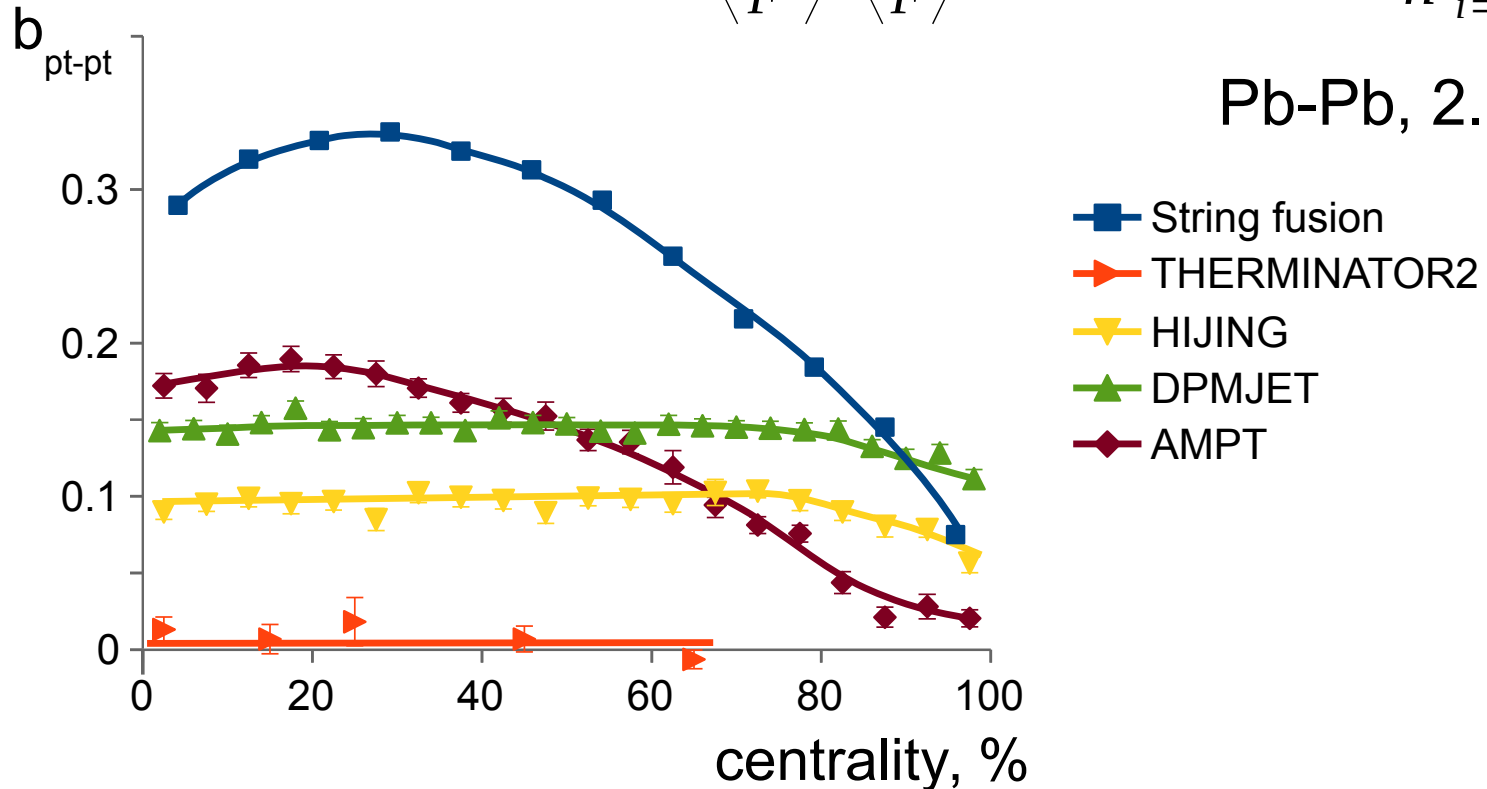
S. Roesler, R. Engel, J. Ranft, arXiv:hep-ph/0012252

Soft + hard, fragmentation of partons by the Lund model

# Mean pt-pt correlations in different models

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2} \quad B, F, \rightarrow p_t = \frac{1}{n} \sum_{i=1}^n p_{ti}$$

Pb-Pb, 2.76 TeV



AMPT (A Multi-Phase Transport Model for Relativistic Heavy Ion Collisions)

Zi-Wei Lin, et al, Phys. Rev. C 72, 064901 (2005)

Shadowing, Zhang's Parton Cascade, string melting, A Relativistic Transport



# Conclusions and outlook

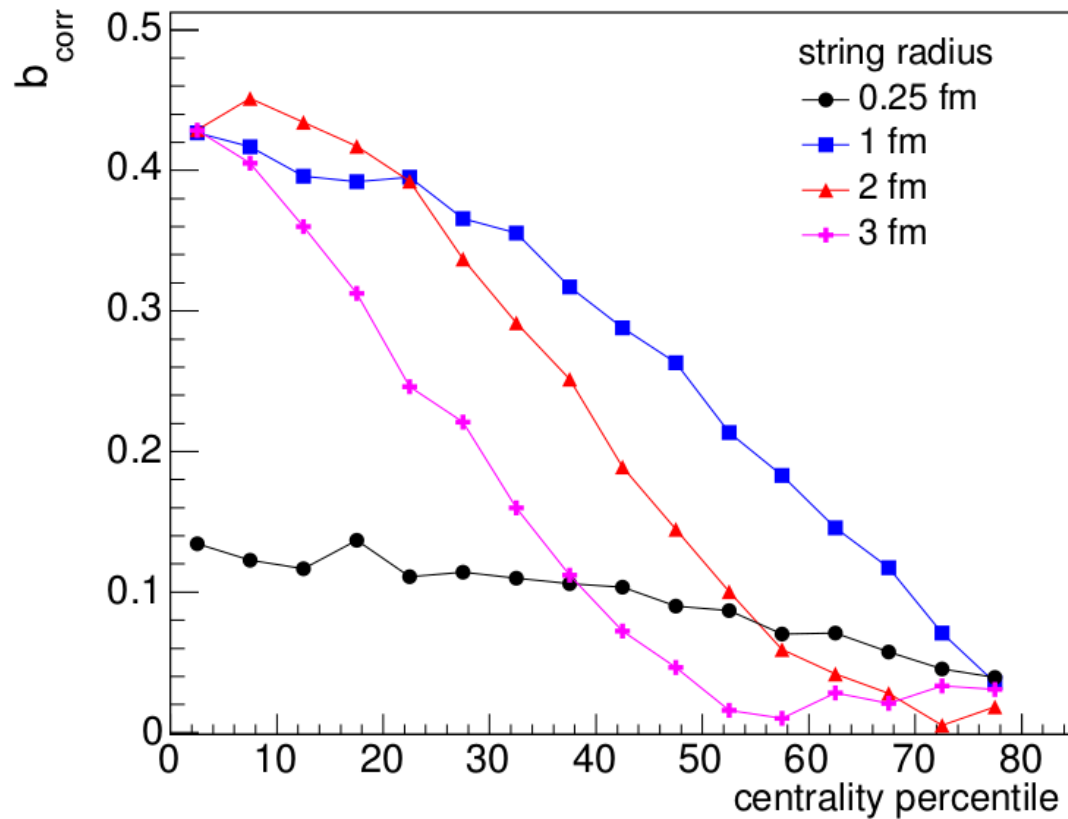
- Centrality determination and a width of centrality class influences the value of fluctuational and correlational observables
- Correlations between intensive observables are robust against the volume fluctuations and the centrality determination methods
- Pt-pt forward-backward correlations provide clear observable sensitive to the properties of the initial state of AA collisions
- This type of correlation is promising for the observation of the signatures of string fusion in relativistic heavy ion collisions at LHC energies.
- Would be interesting to study pt-pt correlations in Event-by-event hydrodynamical models, like iEBE-VISHNU or EKRT.

# Thank you!

# Backup

# String fusion

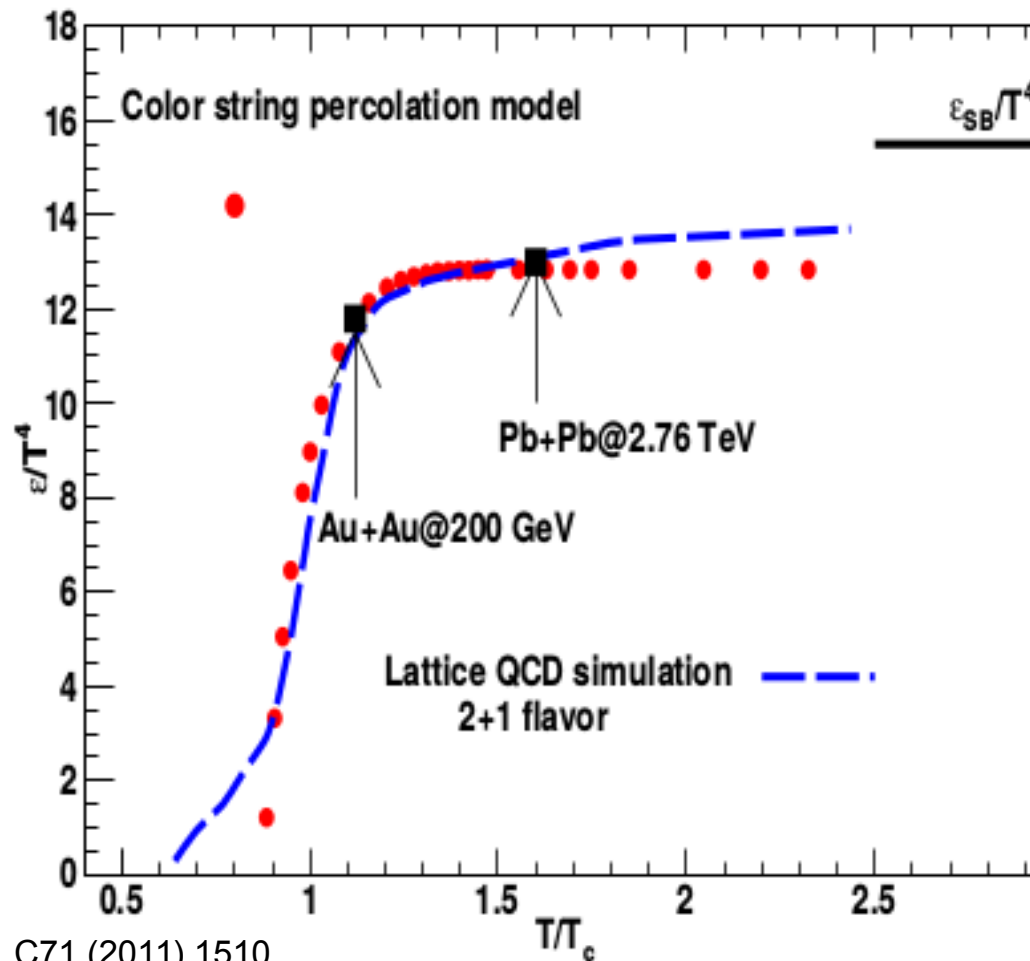
Mean transverse momenta correlations  
in MC toy model with repulsing strings



I. Altsybeev, AIP Conf.Proc. 1701, 100002 (2016) , arXiv:1502.03608 [hep-ph] .

# String fusion

In the recent papers it was shown that the equation of state of QGP ( $\epsilon/T^4$  as a function of  $T$ ) at zero chemical potential, obtained in the colour string percolation model is in a good agreement with the lattice results.



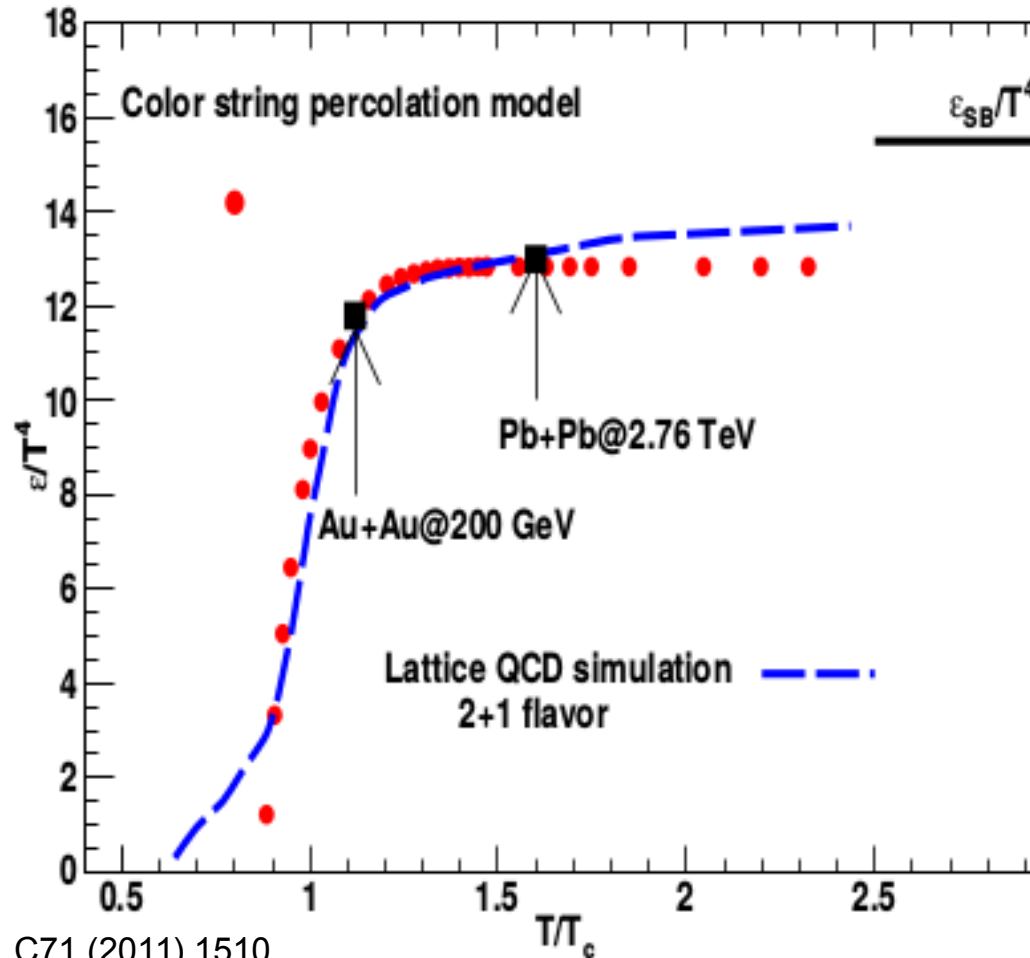
R.P. Scharenberg, B.K. Srivastava, A.S. Hirsch Eur.Phys.J. C71 (2011) 1510

J. Dias de Deus, C. Pajares, Phys.Lett. B642 (2006) 455-458

Brijesh K Srivastava, EP J Web of Conferences 70, 00032 (2014)

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R.P. Scharenberg, B.K. Srivastava, A.S. Hirsch Eur.Phys.J. C71 (2011) 1510

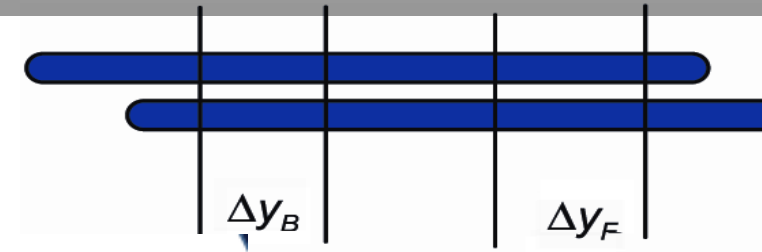
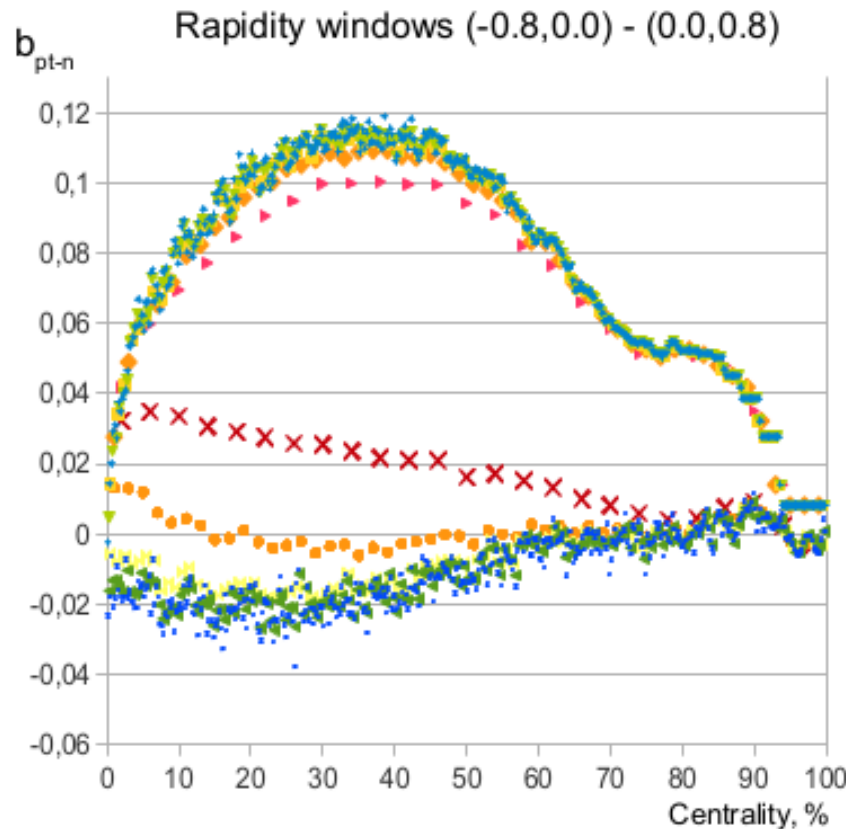
J. Dias de Deus, C. Pajares, Phys.Lett. B642 (2006) 455-458

Brijesh K Srivastava, EP J Web of Conferences 70, 00032 (2014)

# Long-range correlations and fluctuations

pt-n  
correlation  
coefficient

$$b = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2}$$



PbPb,  
2.76 TeV,  
MC model

- +  $b_{ptN}$  0.25% c Npart
- ▼  $b_{ptN}$  0.5% c Npart
- ▲  $b_{ptN}$  1.5% c Npart
- $b_{ptN}$  1% c Npart
- ◆  $b_{ptN}$  2% c Npart
- ▶  $b_{ptN}$  4% c Npart
- ⊠  $b_{ptN}$  0.25% c vzero
- ◀  $b_{ptN}$  0.5% c vzero
- ◀  $b_{ptN}$  1% c vzero
- $b_{ptN}$  2% c vzero
- ×  $b_{ptN}$  4% c vzero

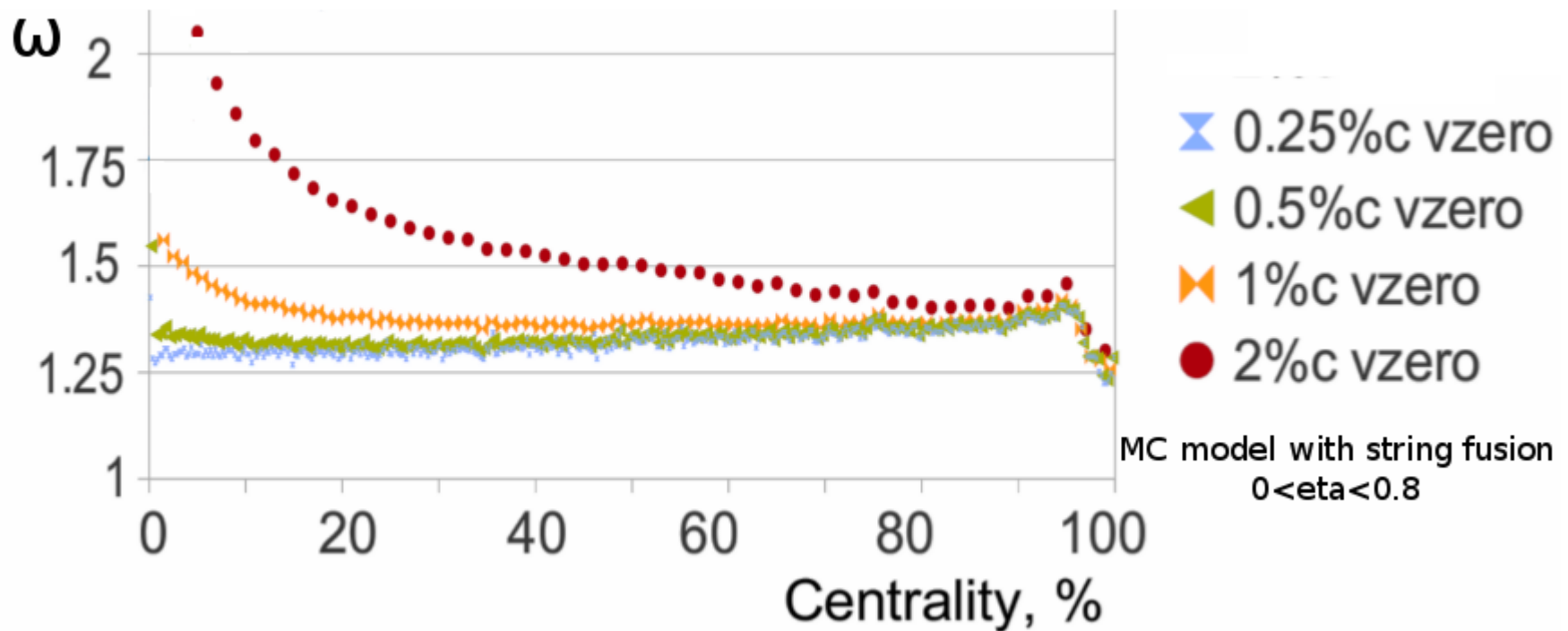
Pb-Pb, 2.76 TeV

# Long-range correlations and fluctuations

scaled variance  $\omega = \frac{\langle n^2 \rangle - \langle n \rangle^2}{\langle n \rangle}$



Pb-Pb, 2.76 TeV



V. Kovalenko, V. Vechernin. EPJ Web of Conferences 66, 04015 (2014), arXiv:1308.6618 [nucl-th]