

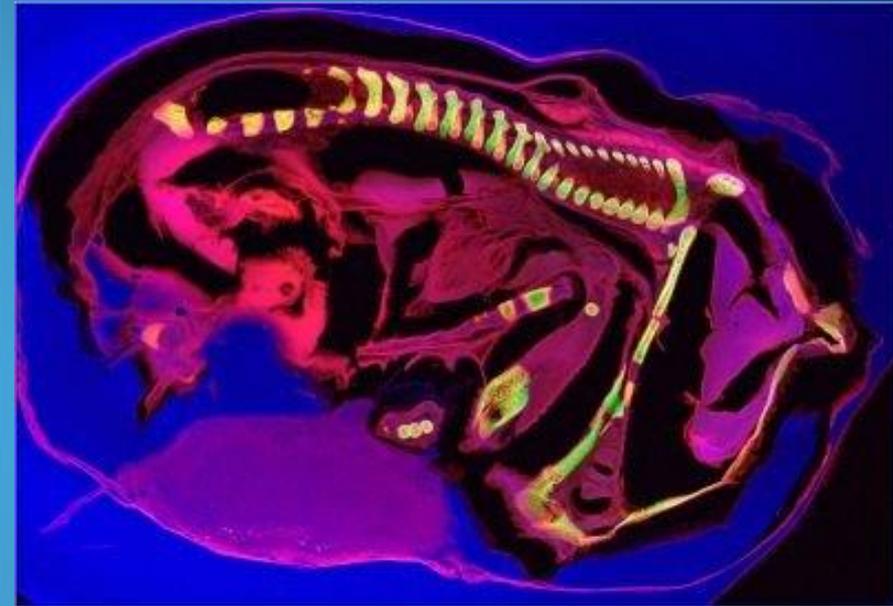
# Simultaneous x-ray transmission and fluorescence CT

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# Fluorescence imaging and XF microscopy



## Optical fluorescence combined with x-ray CT

'FMT-XCT: *in-vivo* animal studies with hybrid fluorescence molecular tomography-x-ray computed tomography', A. Ale et al, 2012, Nature Methods, 9, pp 615-620

## X-ray fluorescence imaging using XFM

Image: Mouse embryo, Euan Smith and Enzo Lombi, CRC CARE, University of South Australia

# XFCT in practice



*Cigar Beetle*

100 angles

5  $\mu\text{m}$  steps

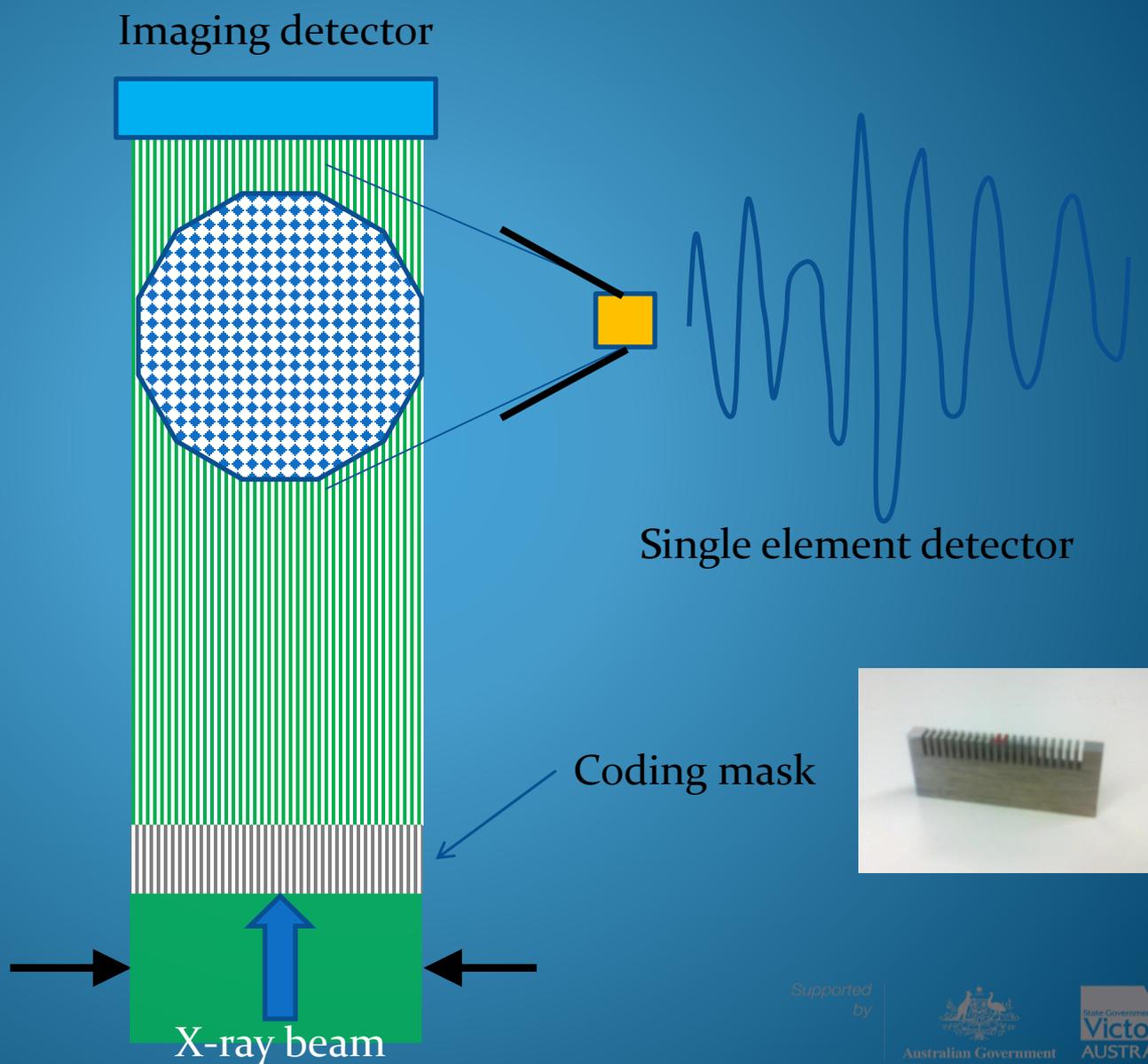
1.25 ms dwell

3 \* 2 mm FoV

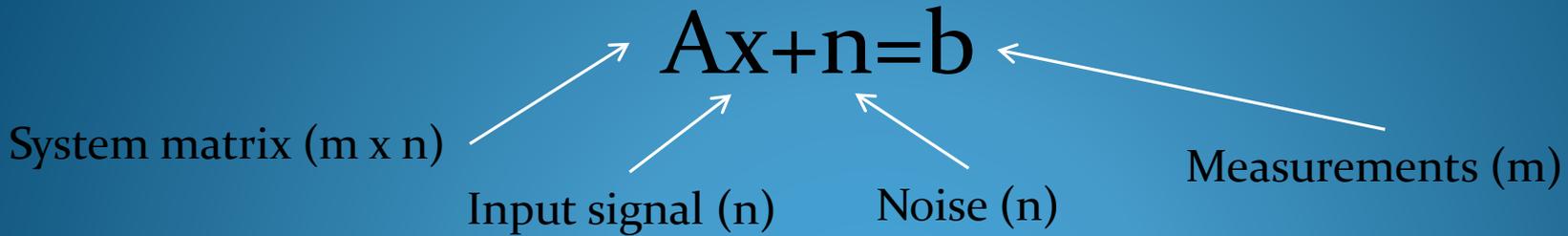
8 hrs total dwell

Measured in 34  
hrs due to line  
overheads

# Coded Beam Fluorescence Imaging (CBFI)



# Linear algebra model of an imaging system



But most often:

$Ax - b \neq 0$  ( $A$  is not invertible)

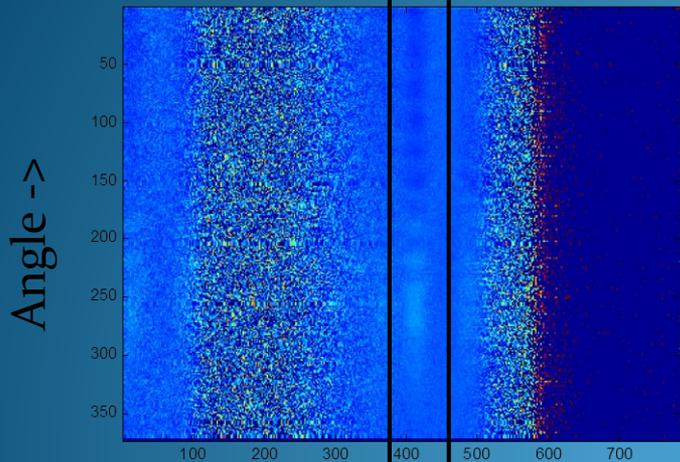
And there are many solutions ( $n \gg m$ ).

The problem is grossly under determined

- But we can use statistical convex optimisation methods to find a best estimate.
- First attempt was with Maximum Likelihood Expectation

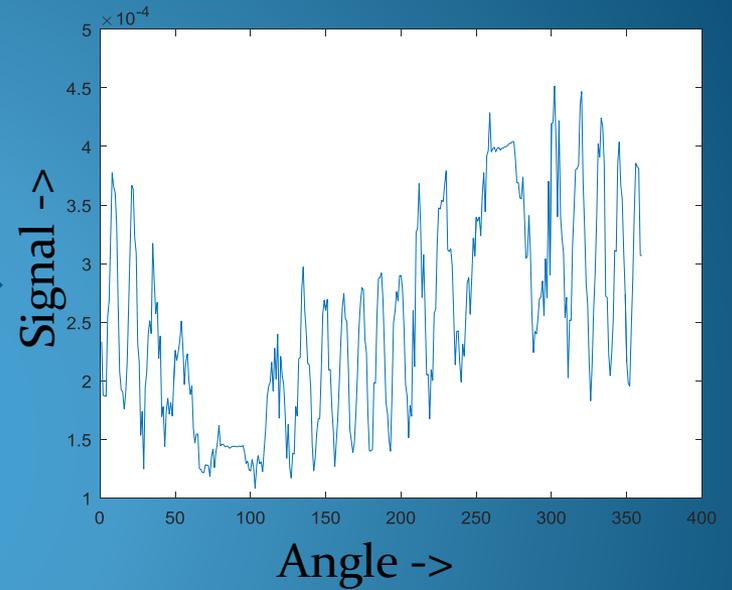
# Data

Spectra stack

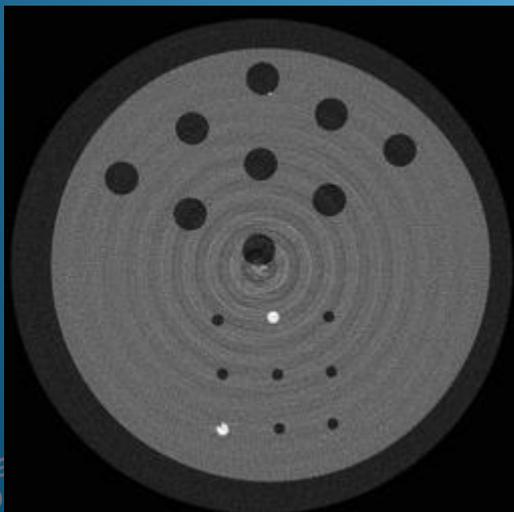


Peak analysis

Fluorescence emission signal



Tomogram



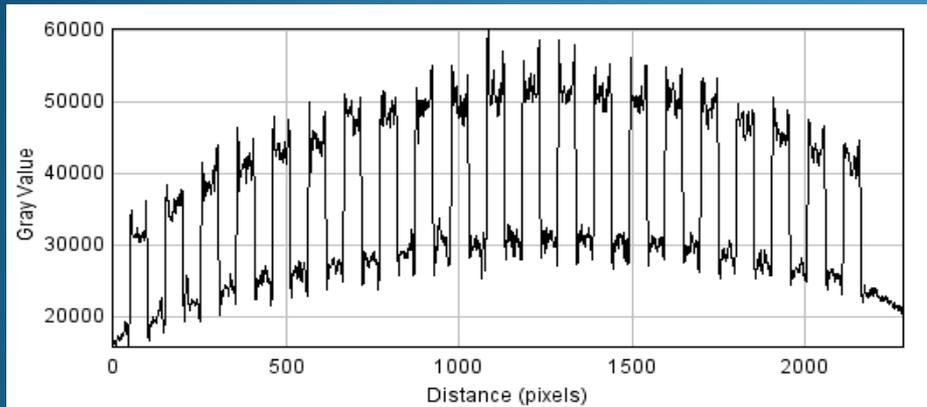
Experiment geometry

System matrix

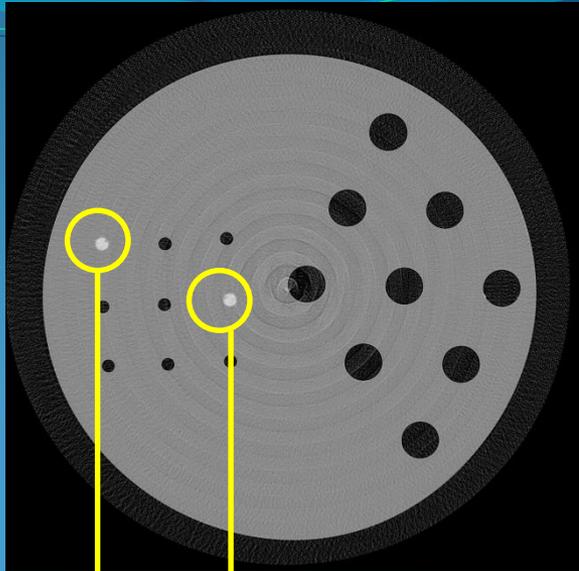


# Results

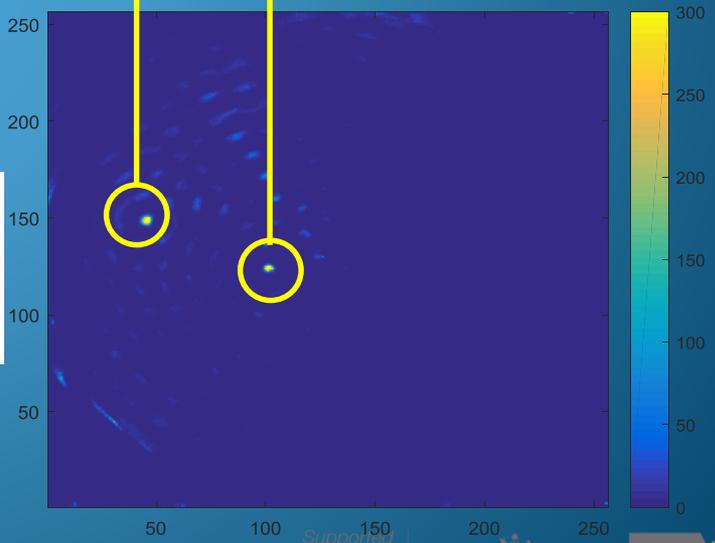
Horizontal profile of beam intensity,  
As seen by the imaging detector



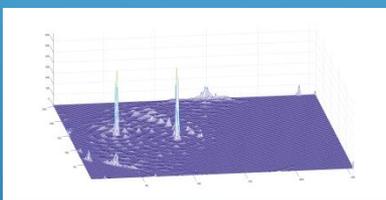
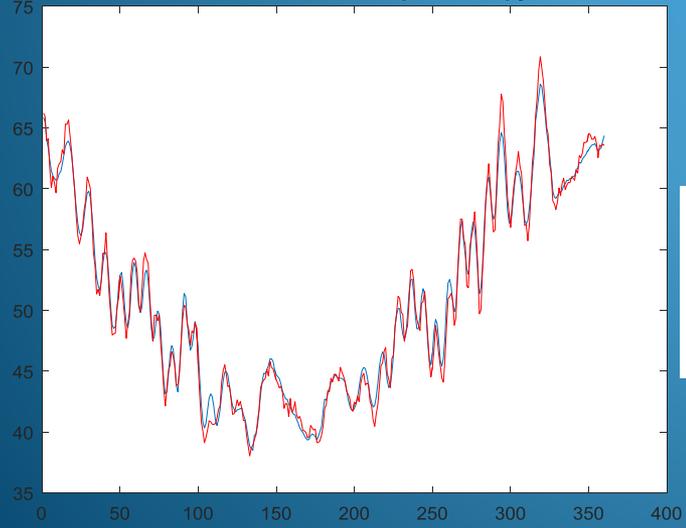
Reconstructed CT slice



Reconstructed fluorescence map



Estimated and measured spectroscopy data



# Compressed Sampling

“The world must not only be interpreted, it must be transformed”



This image is 1470 x 919 pixels ( $=1.35 \times 10^6$ )  
Each pixel uses 3 bytes (Red, Green, Blue)  
 $\Rightarrow 4.05 \times 10^6$  bytes

The .jpg file for this image is 122,022 bytes long  
 $\Rightarrow$  Compression  $\sim 33:1$

The .jpg file for this image is 22,544 bytes  
Compression 9.4:1

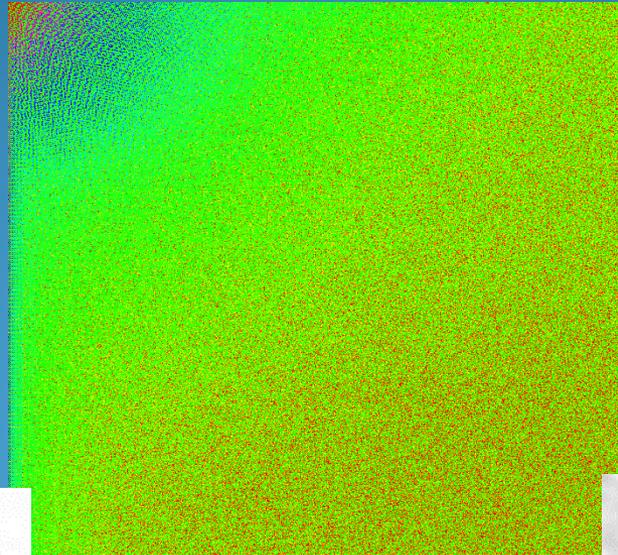
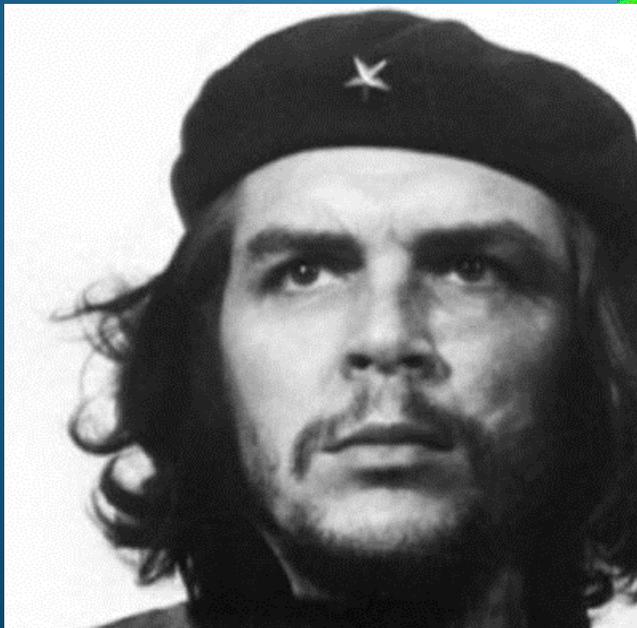
# Information sparsity in real images

DCT representation

Using a different basis to represent an image.

In Fourier space – the vector is sparse (lots of zeros, or near zeros)

Original image



Compressed image



99% of the sorted DCT coefficients set to zero

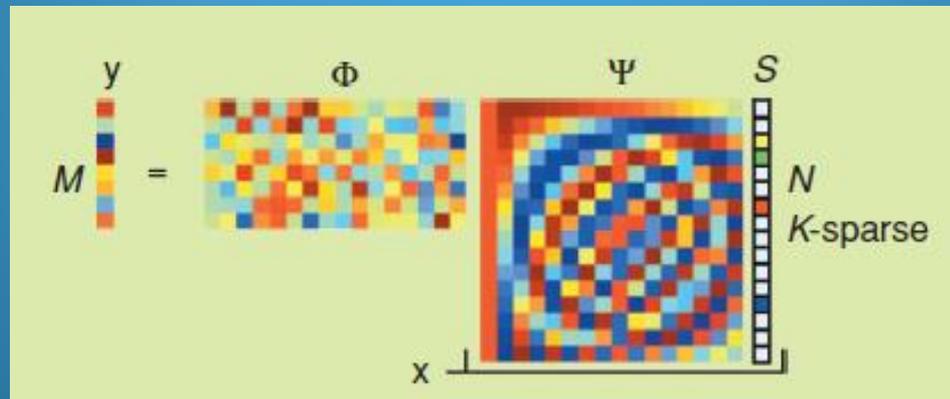


# Compressive Sensing

Making a measurement means taking an inner product between some measurement matrix and a **sparse** representation of our image  $x$  (e.g. using a DCT basis). Then solve for the best solution using convex optimisation.

The  $L_1$  norm is minimised.

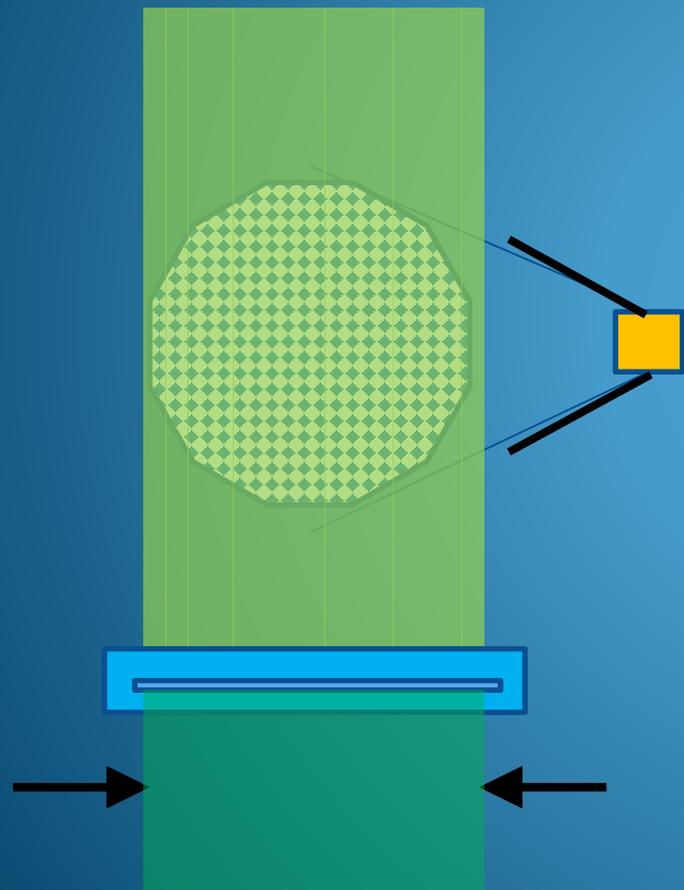
The resulting vector ( $y$ ) can be shown mathematically to be a very good approximation of  $S$ , even if  $M \ll N$



Courtesy Richard Baraniuk

- It turns out that the measurement matrix should be **random!**

# One way forwards for X-rays

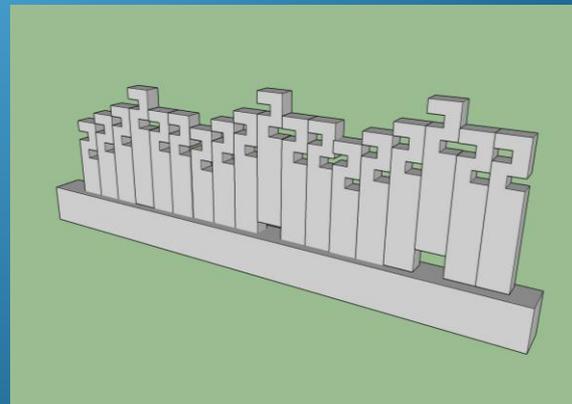


Fixed pattern, multi-row mask



Move through beam, one row at a time.

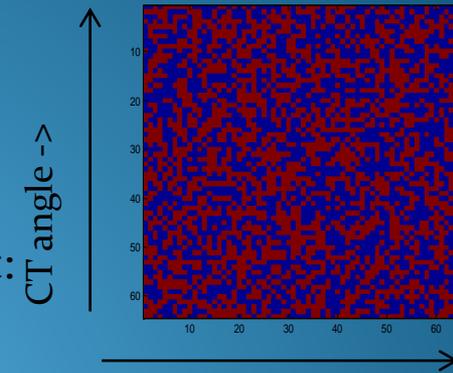
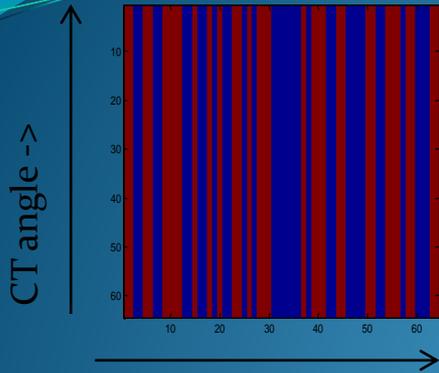
Variable electro-mechanical mask – using a microcontroller and a lot of micro servos.



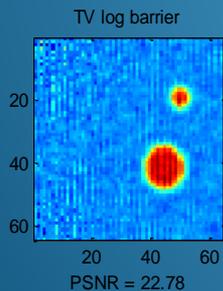
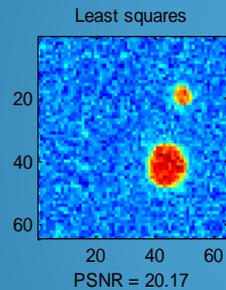
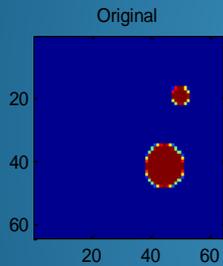
Fixed random mask

# CS Modelling

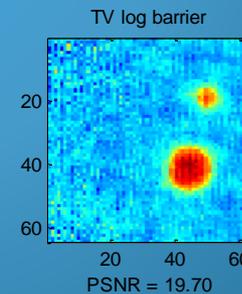
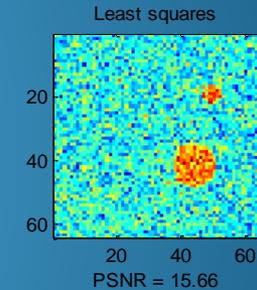
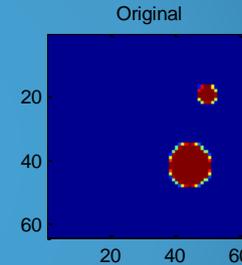
Variable random mask



The reconstructions shown here used the 'L1-Magic' Matlab convex function library from Emmanuel Candes\*. In particular the simplest: Basis Pursuit algorithm.



Using 1166 random measurements from 4096



Using 1166 random measurements from 4096

Using a 50% transparent fixed pattern mask a peak signal to noise ration (PSNR) of 22.8 was achieved. The test image was 64 x 64 pixels with two regions of fluorescence, each a different size.

For a 50% transparent variable pattern mask the calculated PSNR was 19.7.