# An infinite cone jet algorithm for identification of boosted W/Z/H

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## Outline

- Motivation
  - 'Fat jet' algorithms in ATLAS
  - Why implement just another one?
- The algorithm:
  - Lorentz invariant
  - Infinite cone
  - Automatic pileup/UE subtraction
  - No need for grooming of the reconstructed jet
- Results:
  - ▶ Tests on  $W' \rightarrow WZ$  MC: signal efficiency vs. background rejection is  $\simeq$ 50% vs. 1/1.5% for 350 <  $\rho_T^W <$  500 GeV,  $|y_W| <$  4.8

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- Tests on  $t \overline{t}$  data (13 TeV,  $\sim 1/{
  m fb}$ )
- Summary

As presented at Jet substructure and jet tagging meeting on Dec, 17: https://indico.cern.ch/event/446073/

## Motivation

- No need to reproduce arguments in favour of reconstruction of boosted W/Z/H as a single 'fat' jet
- A number of state-of-the-art 'fat jet' algorithms are routinely used in ATLAS (for exotics, high mass VV production, etc.). A typical chain includes jet reconstruction with a wide cone, removal of soft components from UE, ISR, pileup (grooming) and construction of jet structure variables to discriminate between the two cases:
  - color-neutral massive state ightarrow q ar q 
    ightarrow fat jet and
  - $\blacktriangleright$  colored combination of partons  $\rightarrow$  fat jet
- The existing algorithms typically involve several free parameters optimized on a case-by-case basis ( cf., e.g., CERN-PH-EP-2015-204 ):
  - cone size  $R \sim 1$  of the intital C/A or AntiKt jet
  - ▶ cone  $R_{sub} \sim 0.15 0.3$  to find subjets in the fat jet,  $f_{cut} \sim O(5\%)$  to remove soft constituents with  $\frac{p_T^{subjet}}{p_T^{-}} < f_{cut}$  (trimming)
  - $R_{cut}$  and  $z_{cut}$  in *pruning*: drop softer constituent in a pair-wise reclustering if  $\Delta R_{12} > R_{cut} \frac{2M_J}{p_J^T}$  or  $\frac{p_T^{(2)}}{p_T^{(1+2)}} < z_{cut}$
  - momentum balance  $y_{12}$  and mass-drop fraction  $\mu_{12}$  in *split-filtering*,  $\sqrt{y_{12}} = \frac{\min[p_T^{(1)}, p_T^{(2)}]}{m^{(1+2)}} \Delta R_{12}, \ \mu_{12} = \frac{\max[m^{(1)}, m^{(2)}]}{m^{(1+2)}}$ : while declustering the initial C/A jet, drop lower mass constituent if  $\sqrt{y_{12}} < \sqrt{y_{min}}$  or  $\mu_{12} > \mu_{max}$

## Motivation: why implement one more algorithm?

- Reconstruction of *color neutral*  $X \rightarrow jets$  must be **Lorentz invariant**:
  - $\blacktriangleright$  an interference between radiation off initial  $X\to q\bar{q}$  legs and off other color-disconnected legs is suppressed
  - ▶ properties of the hadronic final state in *color neutral*  $X \rightarrow q\bar{q}$  depend only on  $m_X$  and its polarization, there's no dependence on  $p_T(X)$
  - ► ⇒ no fixed cone, use only invariant combinations of objects' momenta to form the metrics for pair-wise object merging
- Unrelated soft components (UE, pileup) are to be rejected in course of jet reconstruction:
  - compare probability of occasional combination of two objects with the probability to produce them by splitting a single parent  $\sim q \rightarrow qg$ ,  $g \rightarrow gg$ ,  $g \rightarrow gg$ ,  $g \rightarrow q\bar{q}$
- Clustering history should follow the shower history
  - use known QCD splitting kernels as the metrics
- Eliminate the need for grooming on top of reconstruction, just use structure variables like  $D_2$  to discriminate between  $W/Z/H \rightarrow q\bar{q}$  and the QCD background
- Minimize the number of free parameters
- Shouldn't be too sophisticated, process specific and CPU consuming as shower deconstuction algorithms using global event topology (cf., e.g., ATLAS-CONF-2014-003)

## The algorithm

- Starting from CaloCalTopoClusters with  $E_T^{clus} > 0.5, \ 1, \ 2 \ {
  m GeV}$  and  $|\eta^{clus}| < 4.8$
- Information from Inner Detector is not used, except for the number of type=1,3 vertices to estimate the pileup in the given event
- 4-momenta of incoming partons estimated from  $\Sigma \vec{p}^{clus}$  and  $\Sigma \vec{p}^{\ell^{\pm}}$  also participate in the clusterisation (roughly speaking, to classify a part of the hadronic state as an ISR).
- For each pair of objects (single clusters or already merged clusters), a probability of occasional combination  $w_{comb}$  (when at least one of the objects comes from pileup+UE with the known density estimated from  $N_{vtx1,3}$  and hence with the known probability  $w_b$  for the given cluster to originate from pileup+UE) is compared to a probability  $w_{rad}$  to obtain this pair by splitting a common parent. If  $w_{comb} > w_{rad}$  then the pair is ignored, otherwise the pair is added to the list of candidates for merging. The pair with a maximum  $w_{rad}$  weight is merged and assigned a probability to come from signal  $w_s = 1-probability$  to come from pileup+UE from the pair's constituent with a maximum  $w_s$  ( $w_s$  calculation details are on the next slide).
- Objects with 4-momentum Q such that  $\sqrt{|Q^2|} > Q_{max} = const \cdot M_W$ , where const = 0.1 1 is a free parameter, are excluded from further merging  $(|Q^2|$  is used instead of a mass as incoming partons also undergo mergings with final state objects which give  $Q^2 < 0.$ )

## The algorithm: pileup estimate

Density of topoclusters from pileup can be estimated for the known  $N_{vt \times 1,3}$ .



The distribution does not scale linearly with  $N_{vt \times 1,3}$  and thus must be measured directly in MinBias events for each  $N_{vt \times 1,3}$ . For pileup estimation in the given event, it's convenient to divide  $\phi$  plane into four sectors:

• One centered in  $\phi$  at the maximum of  $E_T$  density,  $\phi_0 = \sum_{clus} p_T^{clus} \phi^{clus} / \sum_{clus} p_T^{clus}$  and with the half-width  $\sim$  leading jet  $\phi$  half-width:

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$$\Delta(\phi - \phi_0)^2 = \sum_{clus} p_T^{clus} (\phi^{clus} - \phi^0)^2 \Big/ \sum_{clus} p_T^{clus}$$

• The rest of  $\phi$  space is divided in three equal bins.

## The algorithm: pileup vs. signal probabilities

Given an expected value b of pileup/UE clusters in  $(\Delta p_T, \Delta \eta, \Delta \phi)$  bin, actually finding there  $n \ge 1$  clusters implies a modified probability for a single cluster to originate from pileup/UE:

$$w_b = rac{b}{n} rac{1+b+...b^{n-1}/(n-1)!}{1+b+...b^n/n!} \; ,$$

and hence the probability to originate from the signal  $w_s = 1 - w_b$ . A probability of an occasional combination of two objects (1) and (2),  $w_{comb} = 1 - w_s^{(1)} w_s^{(2)}$ , has to be compared with the probability to obtain (1) a (2) by splitting a common parent with 4-momentum  $Q = p^{(1)} + p^{(2)}$  (cf. well known QCD splitting kernels,  $\diamond$  more on the metrics ):

$$w_{rad} \sim \max[w_s^{(1)}, w_s^{(2)}] imes rac{lpha_{S}(Q^2)}{\pi} \cdot C rac{Q_0}{p_0^{(2)}} rac{p_T^{(2)} \Delta p_T^{(2)}}{Q^2} \Delta \eta^{(2)} rac{\Delta \phi^{(2)}}{2\pi}$$

If  $w_{rad} < w_{comb}$  then skip the (1)+(2) pair, otherwise add the pair to the list of candidates for merging with a weight  $w_{rad}$ .

*C* is an unknown color factor ( $C_A$  for  $g \to gg$ ,  $C_F$  for  $q \to qg$ ...) which has to be considered as a second free parameter of the algorithm as we ignore different color combinations. In what follows *C* is fixed so that  $\frac{\alpha_S(M_Z)}{\pi} \cdot C = 0.1$ .

## The algorithm: step by step

- Prepare a list of objects to merge: CaloCalTopoClusters + the two incoming partons with 4-momenta estimated from  $\Sigma \vec{\rho}^{clus}$  and  $\Sigma \vec{\rho}^{\ell^{\pm}}$
- 2 Define  $(p_T, \eta, \phi)$  binning to have a meaningful probability,  $w_b$ , for any cluster to originate from pileup, given the known  $N_{vt \times 1,3}$  in the event
- 3 Load pileup  $(p_T, \eta, \phi)$  density collected in MinBias events with the same  $N_{vt \times 1,3}$
- 4 Assign  $w_b$  and  $w_s = 1 w_b$  to each cluster as explained on the previous slide.
- 5 For each pair of objects:
  - Find a probability of occasional combination of objects (1) and (2), i.e. that at least one of them comes from pileup/UE,  $w_{comb} = 1 w_s^{(1)} w_s^{(2)}$
  - Find a probability w<sub>rad</sub> to split a hypothetic common parent into objects (1) and (2), see the previous slide.
  - If w<sub>rad</sub> < w<sub>comb</sub> go to the next pair, else add (1)+(2) pair to the list of candidates for merging with a weight w<sub>rad</sub>
- **(**) Merge the pair (1)+(2) with a maximum  $w_{rad}$  weight (if it exists) into a single object, assign to the latter a probability to come from the signal  $w_s = \max[w_s^{(1)}, w_s^{(2)}]$ ; otherwise, there's nothing to merge, STOP.
- If  $|Q_{(1+2)}^2|^{1/2} > Q_{cut}$  then the merged object is considered a reconstructed jet and excluded from further mergings (if (1) stems from an incoming parton then freeze (2) as an ISR jet and vice versa)
- (1) if any unfrozen objects remain, go to '5'; STOP otherwise.

MC tests:  $W' \rightarrow Z(\mu\mu)W(\rightarrow hadrons)$ ,  $M_{W'} = 1$  TeV



Signal:  $W'(1 TeV) \rightarrow Z(\mu\mu)W(q\bar{q})$  with truth W:  $350 < p_T^W < 500$  GeV, mc15\_13TeV.302221.MadGraphPythia8EvtGen\_A14NNPDF23L0\_HVT\_Agv1\_VcWZ\_llqq\_m1000 Background: Z + jets, truth Z:  $280 < p_T^Z < 500$  GeV mc15\_13TeV.361\*.Sherpa\_CT10\_Zmumu\_Pt280\_500\_{CVetoBVeto,CFilterBVeto,BFilter} Reco. selection: STACO  $\mu^+\mu^-$  with  $p_T > 20$  GeV,  $|\eta| < 2.47$ ,  $71 < M_{\mu\mu} < 111$  GeV; max.  $p_T$  Jet,  $350 < p_T^J < 500$  GeV,  $|y_J| < 4.8$ 

### MC tests: $W'(1 TeV) \rightarrow ZW$ , subjet kinematics Upon $M_J$ cut retaining 68% of the signal:



Step back: decluster fat jet into two subjets it was built from, use  $\min[p_T^{subjet}/p_T^J] > 0.1$  to discriminate between QCD dijets and dijets from *longitudinally polarized W* 

$$R_{J}^{eff} = \frac{\sum {p_{T}^{clus} \Delta R(clus, J)}}{\sum {clus} {p_{T}^{clus}}},$$
  
not informative after  $M_{I}$  cut

## MC tests: $W'(1 TeV) \rightarrow ZW$ , $C_2^{(1)}$ , $D_2^{(1)}$ , $\tau_{21}^{(wta)}$



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MC tests:  $W'(1 TeV) \rightarrow ZW$ , all cuts Before substructure cuts: With all cuts:





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## MC tests: $W' \rightarrow Z(\mu\mu)W(\rightarrow hadrons)$ , $M_{W'} = 500$ GeV



Signal:  $W'(500 \, GeV) \rightarrow Z(\mu\mu)W(q\bar{q})$  with truth W:  $200 < p_T^W < 250 \, \text{GeV}$ , mc15\_13TeV.302216.MadGraphPythia8EvtGen\_A14NNPDF23L0\_HVT\_Agv1\_VcWZ\_llqq\_m0500 Background: Z + jets, truth Z:  $p_T^Z < 280 \, \text{GeV}$ mc15\_13TeV.361\*.Sherpa\_CT10\_Zmumu\_Pt140\_280\_{CVetoBVeto,CFilterBVeto,BFilter} Reco. selection: STACO  $\mu^+\mu^-$  with  $p_T > 20 \, \text{GeV}$ ,  $|\eta| < 2.47$ ,  $71 < M_{\mu\mu} < 111 \, \text{GeV}$ ; max.  $p_T$  Jet,  $200 < p_T^J < 250 \, \text{GeV}$ ,  $|y_J| < 4.8$ 

## MC tests: $W'(500 \, GeV) \rightarrow ZW$ , subjet kinematics Upon $M_J$ cut retaining 68% of the signal:



Step back: decluster fat jet into two subjets it was built from, use  $\min[p_T^{subjet}/p_T^J] > 0.2$  to discriminate between QCD di-jets and di-jets from *longitudinally polarized W* 

$$R_{J}^{eff} = \frac{\sum \limits_{clus} p_{T}^{clus} \Delta R(clus, J)}{\sum \limits_{clus} p_{T}^{clus}},$$
  
not informative after  $M_{I}$  cut

## MC tests: $W'(500 \, GeV) \rightarrow ZW$ , $C_2^{(1)}$ , $D_2^{(1)}$ , $\tau_{21}^{(wta)}$



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## MC tests: $W'(500 \, GeV) \rightarrow ZW$ , all cuts

#### Before substructure cuts:

With all cuts:



Z.\_.8W/J.\_..

pT,y

M, 68% pT\_\_\_/pT

intermediate mass. • see relaxed cuts in backup

 $\tau_{21}^{wta}$ 

 $tar{t}$  13 TeV data,  $\mathcal{L}_{int}\simeq 1.4/{
m fb}$ 

# $\begin{array}{l} \textbf{Data preselection:} \\ = 1 \; \mu^{\pm} : \; \mu_{T}^{\mu} > 20 \; \text{GeV}, \; |\eta^{\mu}| < 2.47, \; \texttt{ptcone20} / p_{T}^{\mu} < 0.2; \\ \geq 1 \; \texttt{AntiKt4EMTopoJets:} \; p_{T}^{jet} > 20 \; \text{GeV}, \; |\eta^{jet}| < 2.5, \\ \texttt{MV2c20} > -0.5; \\ \sum E_{T}^{calo} > 300 \; \texttt{GeV} \\ (using \; \texttt{a customized EXOT11 derivation}) \end{array}$

Data&MC selection:

$$\begin{split} &\mu^{\pm}: \, \texttt{ptcone20} / p_{T}^{\mu} < 0.01, \, \cos(\vec{p}_{T}^{\mu}, \vec{E}_{T}^{mis}) > 0.6, \\ &|\vec{p}_{T}^{\mu} + \vec{E}_{T}^{mis}| > 50 \, \text{GeV}; \\ &\geq 1 \, \texttt{AntiKt4EMTopoJets}: \, p_{T}^{jet} > 20 \, \text{GeV}, \, \texttt{MV2c20} > -0.44; \end{split}$$

Leading fat jet:  $p_T^J > 150$  GeV,  $|y^J| < 4.8$ 

#### MC samples:

```
W + jets:
mc15_13TeV.361*.Sherpa_CT10_Wmunu_Pt{0...500}_{CVetoBVeto,
CFilterBVeto.BFilter}
```

```
tī:
```

mc15\_13TeV.410000.PowhegPythiaEvtGen\_P2012\_ttbar\_hdamp172p5

\_nonallhad

• Selections were not optimised, still  $W \rightarrow Jet$  peak sitting on a combinatorial background from  $t\bar{t}$  is visible  $\Rightarrow$ 

 $\blacktriangleright D_2^{(1)}$  and  $\Delta R(J, b - jet)$  cuts







## Sensitivity to $Q_{max}$ (follow-up to the jet substructure meeting)



Do we really need  $Q_{max} < m_J$ , where  $m_J \simeq M(W, Z, H, top, ...)$  is the mass we are targeting? From  $\triangleright$  merging metrics it follows that a fat jet with mass  $m_J$  is merged from its two sub-jets carrying  $x_{1,2}$  fractions of jet momentum if  $x_{1,2}p_T^J \gtrsim \frac{m_J^2}{\sqrt{s}}e^{y_J-y_0}$ , where  $\sqrt{\hat{s}}$  and  $y_0$  are the mass and the rapidity of the hard final state. For lower  $p_T^J$  or  $x_{1,2}$  the softer subjet is merged with the beam.

## Can we reconstruct *t*-quark as a single jet? $(Q_{max} = 3M_W)$ Yes, if $x_{subjet1,2} p_T^t \gtrsim \frac{m_t^2}{\sqrt{3_{t-T}x}} e^{y_t - y_0}$ ,

where  $subjet_{1,2}$  is either W or b-jet and  $y_0$  is the rapidity of  $t\bar{t}X$  system in the laboratory frame.



Larger maximum on the plots is W, in case  $t \rightarrow Wb$  remains resolved.

## Can we reconstruct *t*-quark as a single jet? (continued)



## Can we reconstruct *t*-quark as a single jet? (DATA)



## Summary

- Jet reconstruction algorithm with an infinite cone and 'in-flight' pileup/UE subtraction gives reasonable results for boosted  $W \rightarrow jets$   $(M_W/p_T^W \ll 1)$  without grooming.
- For  $W' \rightarrow ZW$ ,  $350 < p_T^W < 500$  GeV,  $|y_W| < 4.8$  the algorithm +  $\tau_2^{wta}/\tau_1^{wta}$  cut yields 50% signal efficiency and QCD background rejection rate  $\simeq 60$ , comparable to C/A R = 1.0, 1.2 + grooming + substructure tagging used in ATLAS (cf. CERN-PH-EP-2015-204)
- The algorithm was also tested on  $tar{t} o W^\pm bW^\mpar{b} o \ell
  u bar{b}J$  '2015 data
- The algorithm is suitable for reconstruction of boosted t as well, if supplemented by  $D_2$  discrimination.
- The results are very preliminary.

## Any feedback would be highly appreciated, thank you!

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Backup

## Metrics at $Q^2 \sim 1 GeV^2$ ?

- Can one apply the QCD-motivated metrics at  $Q^2 \sim 1$  GeV<sup>2</sup> i.e., more generally, to clusters rather than to "microjets" well separated in momentum space?
- The microjects must be constructed using a reasonable pileup/UE-proof algorithm which doesn't merge soft clusters at distances greater than the average distance between two pileup/UE clusters in the event,  $\Delta R \gtrsim \left(N_{clus}^{PU+UE}/\Delta\eta \cdot 2\pi\right)^{1/2}$
- Two objects with 4-momenta p and k (let  $k^0 \sim 1 GeV \ll p^0$ ,  $\Delta R(p, k) = R$ ) coalesce if

$$\begin{split} N_{rad}|_{R} &\sim \alpha_{S}(p^{0}k^{0}R^{2}) \left[ \frac{C}{\pi} \right] \frac{\Delta k^{o}}{k^{0}R^{2}} \frac{\pi R^{2}}{2\pi} > \mu \frac{dN^{\prime o}}{dk^{0}d\Omega} \Delta k^{0}\pi R^{2} \\ &\Rightarrow \alpha_{S}(p^{0}k^{0}R^{2}) \gtrsim 2\pi\mu \frac{dN^{PU}}{dk^{0}d\Omega} k^{0}R^{2} \\ &\Rightarrow \frac{\alpha_{S}(p^{0}k^{0}R^{2})}{2} \gtrsim N^{PU} \Big|_{t=0} \end{split}$$

Let's freeze  $\alpha_S$  for  $Q^2 < 1 \text{GeV}^2$  at  $\alpha_S^{n_{Hav}=5}(1 \text{GeV}^2) \simeq \frac{1}{2}$  so that  $\alpha_S < \frac{1}{2}$  at any  $Q^2 \Rightarrow$  one needs  $N^{PU}|_{\ln \pi R^2} \lesssim \frac{1}{4}$  to merge the clusters rather then treat the pair as a random PU+UE induced combination. In other words, if one expects  $\ll 1 \text{ PU+UE}$  clusters in the given phase-space around a harder cluster but still finds a softer cluster there, then the two clusters are merged (and the combination is discarded otherwise)  $\Rightarrow$  The metrics is stable w.r.t. PU+UE and can be applied 'as is' for clusterisation of soft/collinear objects.

MC tests:  $W'(1 TeV) \rightarrow ZW$ , pileup stability



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MC tests:  $W'(500 GeV) \rightarrow ZW$ , leading fat jet  $p_T$ 



## MC tests: $W'(500 \, GeV) \rightarrow ZW$ , subjet kinematics vs PU



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## $W'(500\,GeV) ightarrow ZW$ , $C_2^{(1)}$ , $D_2^{(1)}$ , $au_{21}^{(wta)}$ w/o $p_{T}^{subjet}/p_{T}^J$ cut



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 $\epsilon_{signal}$  vs.  $\epsilon_{QCD \ bkg}$ ,  $350 < p_T(J) < 500 \ GeV$ (CERN-PH-EP-2015-204)



▲ back to main slide

MC tests:  $W'(500 \, GeV) \rightarrow ZW$ , pileup stability



MC tests:  $W'(500 \, GeV) \rightarrow ZW$ , leading fat jet  $p_T$ 



## MC tests: $W'(500 \, GeV) \rightarrow ZW$ , subjet kinematics vs PU



▲ To main slide

## $W'(500\,GeV) ightarrow ZW$ , $C_2^{(1)}$ , $D_2^{(1)}$ , $au_{21}^{(wta)}$ w/o $p_{T}^{subjet}/p_{T}^J$ cut



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 $W'(500 \, GeV) \rightarrow ZW$ , relaxed fat jet selection At generator level:  $200 < p_T^W < 250$  GeV, no  $y_W$  cut. Relaxed cuts at reco. level:  $150 < p_T^J < 300$  GeV,  $|y_J| < 4.8$ 

Poor  $p_T^J$  and  $m^J$  resolution:



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## *tī* 13 TeV data vs MC, structure variables



liun<sup>.</sup>0.45

0.4

0.35

- W+light - W+c

W+b

 $tar{t}$  13 TeV,  $0.6 < D_2^{(1)} < 1$  and  $\Delta R(J, b-jet) > 1$  cuts



 $D_2$  definition

$$E_{CF0}(\beta) = 1$$

$$E_{CF1}(\beta) = \sum p_{Ti}$$

$$E_{CF2}(\beta) = \sum p_{Ti}p_{Tj}(\Delta R_{ij})^{\beta}$$

$$E_{CF3}(\beta) = \sum p_{Ti}p_{Tj}p_{Tk}(\Delta R_{ij}\Delta R_{ik}\Delta R_{jk})^{\beta}$$

$$e_2^{(\beta)} = E_{CF2}(\beta)/E_{CF1}(\beta)^2$$

$$e_3^{(\beta)} = E_{CF3}(\beta)/E_{CF1}(\beta)^3$$

$$D_2^{(\beta)} = e_3^{(\beta)}/(e_2^{(\beta)})^3$$

▲ Back to main slide

## Reconstructed t mass vs. $m_{W/b}$ (1 < $D_2$ < 1.6 cut applied)

