magnetic electric longitudinal transverse *h 2a* true false JUAS 2015 – RF Exam ID #: $\qquad \qquad$ Points: $\qquad \qquad$ of 20 Utilities: JUAS RF Course 2015 lecture script, personal notes, pocket calculator, ruler, compass, and your brain! (No cell- or smartphone, no iPad or wireless devices, text books or any other tools) **1. "Pillbox" Cavity (6 points)** Design a simple "pillbox" (cylindrical) cavity, made out of copper ($\sigma_{\text{copper}} = 58 \cdot 10^6$ S/m). The eigen-frequency of the lowest mode with longitudinal electric field components is 460 MHz. (The beam-pipe ports are neglected.) a) The field if the TM₀₁₀ mode das only field components. (Mark the correct answer: $\left(\frac{1}{2}p\right)$) b) What is the radius *a* of the cavity? (1 point) $a = 0.383 \lambda$ $\lambda = \frac{c_0}{c_0}$ f $a =$ 0.383 ⋅ 2.998 ⋅ 10⁸m s $\frac{20.58 \times 10^{6} \text{ m/s}}{460 \cdot 10^{6} \text{ s}}$ = 249.6 mm c) What height *h* of the cavity has to be chosen, to achieve an (unloaded) *Q*-factor of *Q* = 23500? (2 points) $Q=$ α $\frac{\pi}{\delta}$ [1 + α $\frac{1}{h}$ −1 = α $\sqrt{\delta(1 + \frac{a}{b})}$ $\frac{u}{h}$ 1 + α $\frac{a}{h}$ = α δQ $h =$ α \overline{a} $\frac{u}{\delta Q} - 1$ $\delta = |$ 2 $ω σμ$ $\delta = \frac{2 s}{2.460 \cdot 10^6} \frac{Vm}{5.2 \cdot 10^{-7} A} \frac{Am}{4.257}$ $\frac{2\pi}{2\pi \cdot 460 \cdot 10^6 \cdot 5.8 \cdot 10^{-7} A \cdot 4\pi \cdot 10^{-7} Vs} = 3.08 \ \mu m$ $h =$ $249.6 \cdot 10^{-3}$ m $\frac{149.6 \cdot 10^{-3} m}{3.08 \cdot 10^{-6} m \cdot 23500} - 1$ $= 101.9$ mm d) What is the 3-dB bandwidth of the resonance? (½ point) $Q=\frac{f_{res}}{16}$ $\frac{f_{res}}{\Delta f}$ \Rightarrow $\Delta f = BW = \frac{f_{res}}{Q}$ $\frac{res}{Q} =$ 460 · 10⁶ Hz $\frac{23500}{23500} = 19.6 \text{ kHz}$ $\mu = \mu_0 \mu_r$ $\mu_0 = 4\pi \cdot 10^{-7} \text{ Vs/(Am)}$ $\varepsilon = \varepsilon_0 \varepsilon_r$ ε_0 = 8.854 · 10⁻¹² As/(Vm) *c*⁰ = 2.998 ⋅ 10⁸ m/s $\sigma_{\text{copper}} = 58 \cdot 10^6 \text{ S/m}$

e) Sketch the *RLC* equivalent circuit of this resonant mode,

and determine the values. (1 point)

$$
\frac{R}{Q} = 128 \, \Omega \frac{\sin^2 \left(1.2024 \frac{h}{a}\right)}{\frac{h}{a}} = 128 \, \Omega \frac{\sin^2 \left(1.2024 \frac{0.1019 \, m}{0.2496 \, m}\right)}{0.1019 \, m}} = 69.9 \, \Omega
$$
\n
$$
R = \frac{R}{Q} \cdot Q = 69.9 \cdot 23500 = 1.64 \, M\Omega
$$
\n
$$
\omega_{res}L = \frac{1}{\omega_{res}C} = \frac{R}{Q}
$$
\n
$$
L = \frac{R}{Q \, 2\pi f_{res}} = \frac{1.64 \cdot 10^6 \, V}{23500 \cdot 2\pi \cdot A \cdot 460 \cdot 10^6} = 24.1 \, nH
$$
\n
$$
C = \frac{1}{4\pi^2 f_{res}^2 L} = \frac{1 \, s}{4\pi^2 \cdot (460 \cdot 10^6)^2 \cdot 24.1 \cdot 10^{-9} \, Vs} = 4.96 \, pF
$$

f) The cavity is fed from a RF power amplifier with a source impedance of *R^g* = 50 Ω. What is required transformer ratio of the coupling loop to match the cavity shunt impedance to the generator source impedance? ($\frac{y_2}{x_1}$ point)

$$
k = \sqrt{\frac{R}{R_{input}}} = \sqrt{\frac{1.64 \cdot 10^6 \,\Omega}{50 \,\Omega}} = 181.1
$$

g) Calculate the necessary RF power for a gap voltage of 1 MV. $(1/2 \text{ point})$

$$
P = \frac{V^2}{2 R} = \frac{10^{12} V^2 A}{2 \cdot 1.64 \cdot 10^6 V} = 304.9 kW
$$

2. Resonator analysis in the complex plane (2 points)

At the upper 3-dB point (definition see RF lecture script) of a 1 GHz resonator, the complex impedance measures $|Z(\omega=6.289 10^9 s^{-1})| = 707 Ω$.

- a) With help of compass and ruler, sketch the locus of *Z(f)* in the complex Z-plane
	- Indicated upper and lower 3-dB points, as well as the points for resonant frequency and frequency limits $(f = 0, f \rightarrow \infty)$. (1 point)
	- Estimate the value of the shunt impedance *R*. (½ point)

 $R = 1 k\Omega$

 f_{res}

b) Determine the Q-value of the resonator. $(\frac{1}{2} \text{ point})$

$$
f_{3dB}^{+} = \frac{\omega_{3dB}^{+}}{2\pi} = 1.000925 \text{ GHz}
$$

\n
$$
BW = \Delta f = 2(f_{3dB}^{+} - f_{res}) = 2 \cdot (1.000925 \cdot 10^{9} - 10^{9}) \text{ Hz} = 1.85 \text{ MHz}
$$

\n
$$
Q = \frac{f_{res}}{\Delta f} = 540.8
$$

3. Smith chart (6 points)

a) Indicate points P_1 … P_5 in the Smith chart, assuming a reference impedance $Z_0 = 50$ Ω. From the Smith chart, determine the missing *Z* or *Γ*, and complete the table. (1½ points)

b) Indicate $|\Gamma| = 0.75$ in the Smith chart. (Hint: It is not a point) (¹/₂ point) c) At 400 MHz a complex load impedance measures *Zload* = (25+j67) Ω. i. Indicate the normalized z_{load} in the Smith chart, and look up • the reflection coefficient, $(\frac{1}{2}p^2 - p^2)$ ($\frac{1}{2}p^2 - p^2 = 1$ $\Gamma = 0.258 + j0.662 = 0.711\angle 68.7$ ° • the (voltage) standing wave ratio, $\sqrt{\frac{1}{4}}$ point) $SWR = 5.92$ • the return loss (in dB), $(\frac{1}{4} \text{ point})$ $ReturnLoss = 2.96 dB$ • the reflection loss (in dB) $(\frac{1}{4} \text{ point})$ $Reflection Loss = 3.06 dB$

for a reference impedance of Z ⁰ = 50 Ω.

(Hint: Use a ruler to determine |*Γ*| of *zload*, and compare it with value found at the "radially scaled parameters" Smith chart ruler at the bottom.)

- ii. With help of the Smith chart, sketch a lossless matching network, and determine the component values to adapt to a 50 Ω source impedance of the RF generator.
	- Define the locus path lossless elements to route from *zload* to the normalized reference impedance. (1 point) (Hint: Remember the Dellsperger Smith Chart computer exercises, only 2 lossless elements are required. Different solutions are possible.)
	- Determine the values of the lossless circuit elements. (2 points)

NORMALIZED IMPEDANCE AND ADMITTANCE COORDINATES

4. S-Parameters (2 points)

Match the ideal S-parameters in matrix form to the corresponding components.

$$
\mathbf{S}_A = \frac{1}{2} \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix} \qquad \mathbf{S}_B = \frac{1}{10} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \qquad \mathbf{S}_C = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 & j & 1 & 0 \\ j & 0 & 0 & 1 \\ 1 & 0 & 0 & j \\ 0 & 1 & j & 0 \end{bmatrix} \qquad \mathbf{S}_D = \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}
$$

a) Assign the S-matrices $(S_A ... S_D)$ to the components: (1 point)

b) Fill the missing dB and λ information (...). (1 point)

5. Multiple choice (4 points)

Tick the correct answer(s) like this: $\mathbb X$. (Except for questions 7. and 8., only one answer is correct)

- 1. A coaxial line is filled homogeneous with a dielectric material, e.g. PTFE ("Teflon"). The signal velocity of a coaxial line of same physical length, but filled with air is $\frac{y_2}{y_1}$ ($\frac{y_2}{y_2}$ point)
	- o identical
	- \times higher
	- o lower
- 2. TEM stands for (^{1/2} point)
	- o Transient Electro-Magnetics
	- o Transverse Electro-Magnetic mode
	- o Turbo Electric Motor
- 3. For a cylindrical ("pillbox") cavity, the eigen-frequencies are independent of the cavity height *h* dimension: (½ point)
	- o False, for any eigen-mode the resonance frequency depends on height *h* and radius *a*
	- o True only for the fundamental mode
	- χ True only for TM₀₁₀ and TM₁₁₀ modes

- o increased due to
- $\mathbb X$ reduced due to
- o independent of

the transit time factor.

- 5. Critical coupling (match at resonance) between resonator and generator occurs at (½ point)
	- o *Q^L = Qext*
	- χ $Q_L = Q_0/2$
	- o *QL = 2 Q⁰*
- 6. A 10 W RF generator is connected via a 20-dB attenuator to a 50 Ω load impedance. At the load we measure: $(\frac{1}{2} \text{ point})$
	- \circ 1 W
	- \circ -20 dBW
	- \mathbb{X} +20 dBm
- 7. What is true for 2-conductor transmission-lines? (½ point)
	-
	- χ Ideal for broadband (down to DC), low level signal transmission.
	- o The signal transmission is based on "modes".
	- o Low losses at high frequencies, therefore ideal for high power RF transmission.
- 8. What is true for waveguides? ([%] point)

- o Ideal for broadband (down to DC), low level signal transmission.
- χ The signal transmission is based on "modes".
- \times Low losses at high frequencies, therefore ideal for high power RF transmission.