

The significance of neutrino cross-sections for astrophysics

A.B. Balantekin

University of Wisconsin-Madison

NUINT, May 2009
Sitges, Barcelona

Special: New Learning Series on Genetics, page 70

Complexity—the Science of Surprise | Your Inner Savant

Discover

FEBRUARY 2002

DISCOVER.COM

The
11
Greatest
Unanswered
Questions
of **Physics**

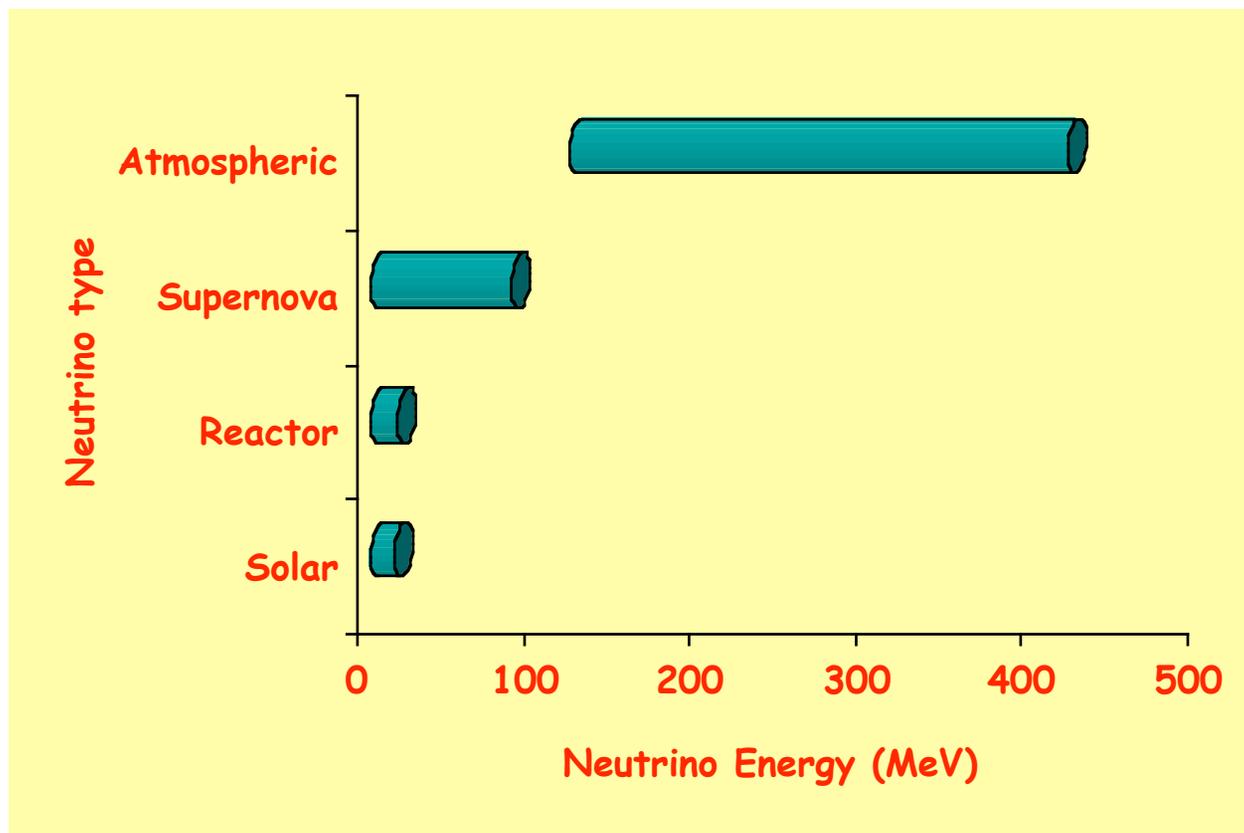
No.
9
What Is

U.S. National Academy of Sciences Report "Connecting Quarks with the Cosmos: Eleven Science Questions For the New Century"

Question 5

What are the masses of neutrinos, and how have they shaped the evolution of the Universe?

Answer requires knowing about Neutrino Interactions and Neutrinoless Double Beta Decay



Low-energy non-accelerator neutrinos so far observed

What part of the neutrino sky did we actually observe so far?

- **Below 100 MeV:** Solar neutrinos (SuperK, SNO, SAGE, Gallex, Homestake); neutrinos from SN1987A (Kamioka, IMB, Baksan); tail of atmospheric neutrinos.
- **Up to 1 TeV:** Atmospheric neutrinos (SuperK, others...).
- **Above 1 TeV:** Atmospheric neutrinos (Amanda); future data from Icecube.
- **Very high energies:** Only upper limits in neutrino fluxes

- Low-energy astrophysical neutrinos provide us tools for a new kind of astronomy looking at the interior of compact objects.

- Low-energy astrophysical neutrinos provide us tools for a new kind of astronomy looking at the interior of compact objects.
- They help us explore fascinating phenomena in the Cosmos as diverse as the birth of new stars and the origin of elements.

- Low-energy astrophysical neutrinos provide us tools for a new kind of astronomy looking at the interior of compact objects.
- They help us explore fascinating phenomena in the Cosmos as diverse as the birth of new stars and the origin of elements.
- It is a new tool complementary to other tools already in place: Various electromagnetic (optical or otherwise) telescopes (looking at the same object with light and neutrinos), LIGO (neutrinos accompanying gravitational collapse).

- Low-energy astrophysical neutrinos provide us tools for a new kind of astronomy looking at the interior of compact objects.
- They help us explore fascinating phenomena in the Cosmos as diverse as the birth of new stars and the origin of elements.
- It is a new tool complementary to other tools already in place: Various electromagnetic (optical or otherwise) telescopes (looking at the same object with light and neutrinos), LIGO (neutrinos accompanying gravitational collapse).
- We had already seen neutrinos from two (and only two) such objects: A main-sequence star (the Sun) and a core-collapse supernova (SN1987A).

Applications of ν -nucleus interactions

Theory and applications of Detector Response:
Detectors for solar, atmospheric, accelerator, and reactor neutrinos.

Input into astrophysics: Neutrino reactions in core-collapse supernovae, supernova nucleosynthesis, gamma-ray burst nucleosynthesis.

Tests of nuclear structure calculations: Shell Model, effective field theories.

Fundamental physics at low energies: e.g. determining proton strange form factors.

How can the neutrino cross-sections be calculated?

Low Energy ($0 < E < \sim 200 \text{ MeV}$)	Non-relativistic many-body theories (Shell Model, RPA); effective field theory	Solar and supernova neutrinos
Intermediate E ($\sim 200 \text{ MeV} < E < \sim 200 \text{ GeV}$)	Relativistic; hadronic \Rightarrow partonic d.o.f, superscaling ideas; quasielastic and resonance regime	Atmospheric neutrinos
High Energy ($\sim 200 \text{ GeV} < E < \text{EeV}$)	Deep-inelastic scattering, partonic d.o.f., x-scaling	Atmospheric ν 's, neutrinos from point sources, ...

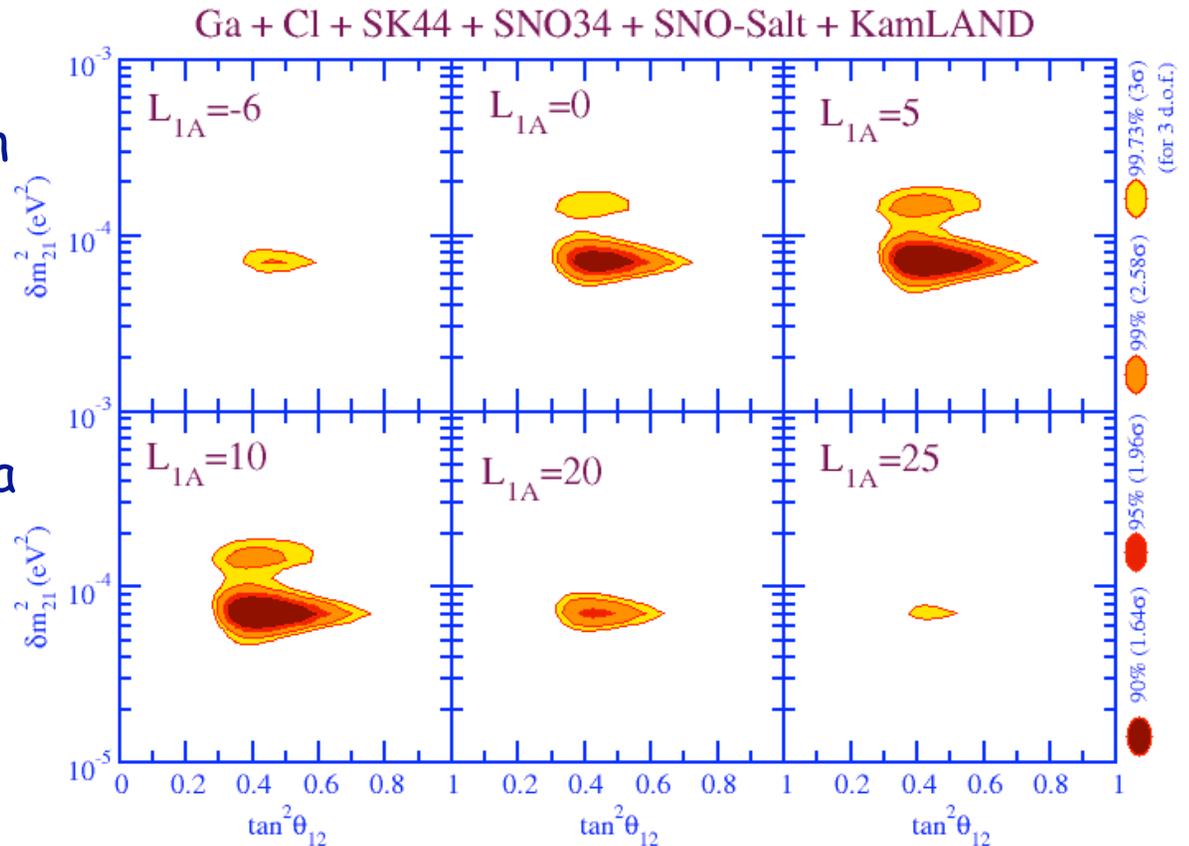
An approach from the first principles: Using effective field theory for low-energy neutrino-deuteron scattering

Butler, Chen

Below the pion threshold $^3S_1 \rightarrow ^3S_0$ transition dominates and one only needs the coefficient of the two-body counter term, L_{1A} (isovector two-body axial current)

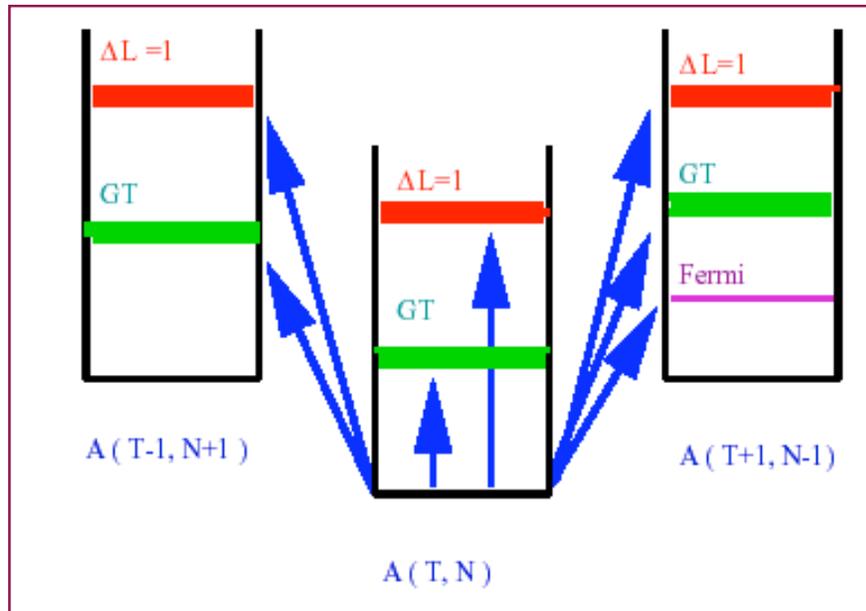
L_{1A} can be obtained by comparing the cross section $\sigma(E) = \sigma_0(E) + L_{1A} \sigma_1(E)$ with cross-section calculated using other approaches or measured experimentally. (e.g. use solar neutrinos as a source)

Difficult to go beyond two-body systems!



A.B. Balantekin and H. Yuksel

For SN the question is to find out what happens when a 50 MeV neutrino hits a nucleus? Where is the strength? What is g_A/g_V ?



As the incoming neutrino energy increases, the contribution of the states which are not well-known increase, including first- and even second-forbidden transitions.

At the lowest energies Shell Model is the best approach. Gamow-Teller strength is quenched in the Shell Model:

Nucleus	^{128}Sn	^{130}Sn	^{132}Sb	^{132}Te	^{133}Te
Transition	$0^+ \rightarrow 1^+$	$0^+ \rightarrow 1^+$	$4^+ \rightarrow 3, 4, 5^+$	$0^+ \rightarrow 1^+$	$\frac{3}{2}^+ \rightarrow \frac{1}{2}^+, \frac{3}{2}^+, \frac{5}{2}^+$
$T_{1/2\text{exp.}}$	59.07m	3.72m	2.79m	3.2d	12.5m
$T_{1/2\text{calc.}}$ (0.74)	32.21m	2.47m	1.56m	1.73d	6.42m
Renorm.	0.54	0.6	0.55	0.54	0.53

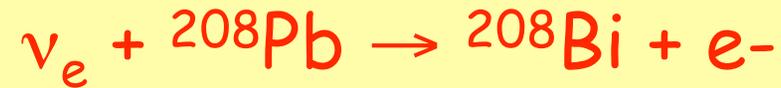
Beta-decay rates from Nowacki

At higher energies where the rate is sensitive to total strength and the energy of giant resonances there is a tendency to use RPA.

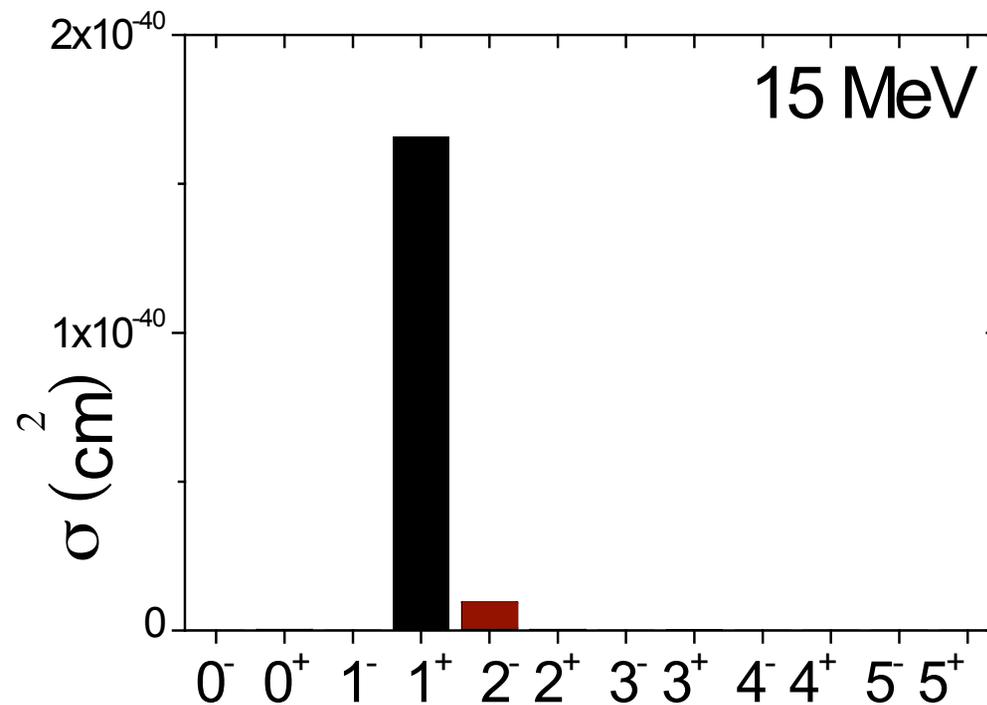
However some theoretical difficulties with RPA remain!

Example:

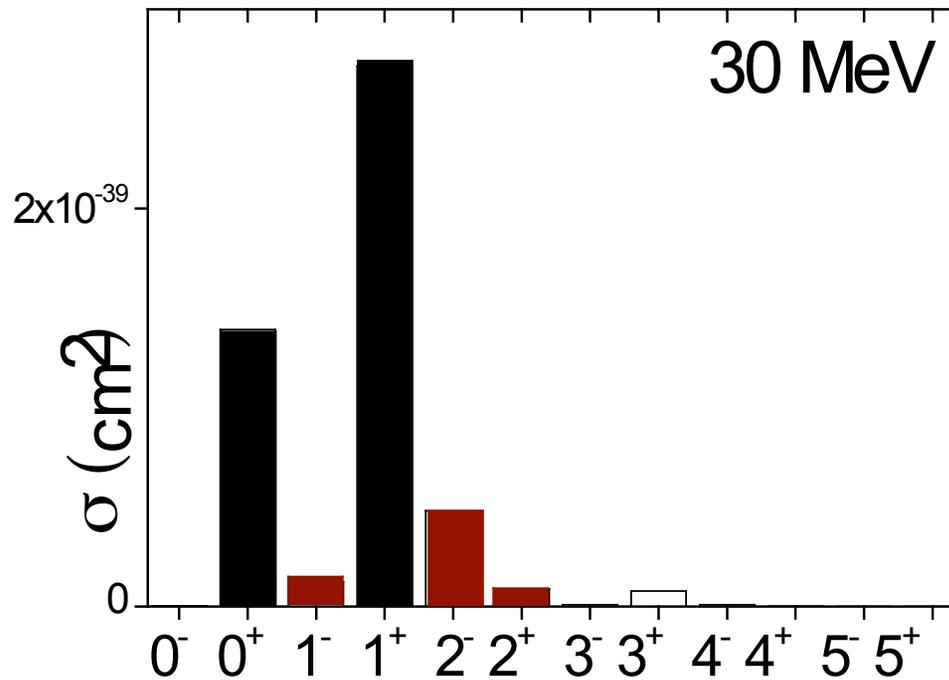
States once can excite in the reaction



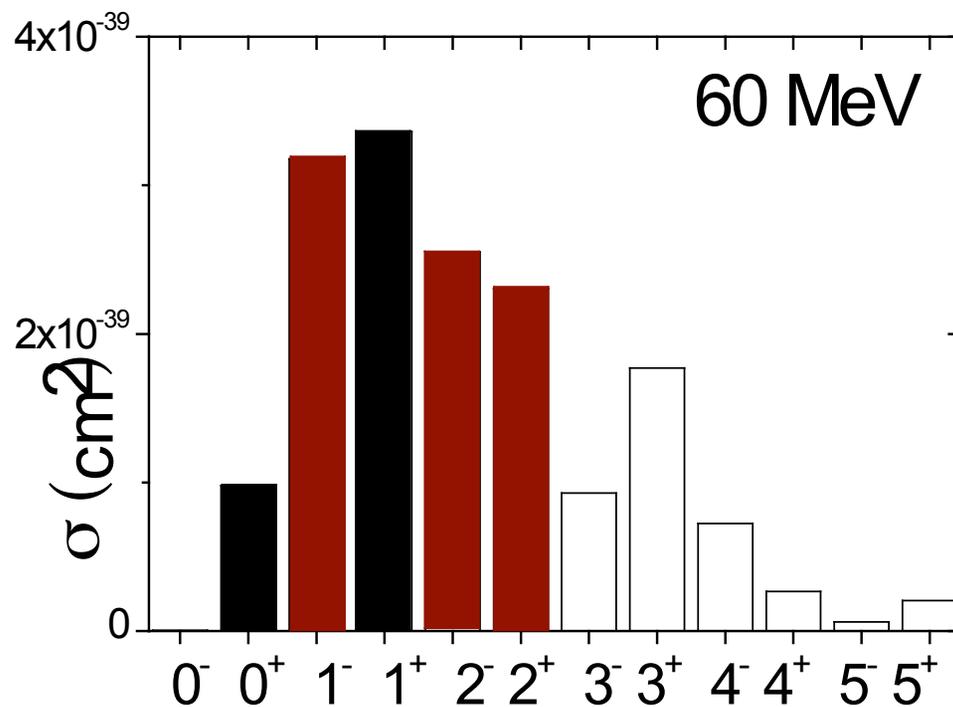
as a function of the neutrino energy



States once can excite in the reaction
 $\nu_e + {}^{208}\text{Pb} \rightarrow {}^{208}\text{Bi} + e^-$
as a function of the neutrino energy



States once can excite in the reaction
 $\nu_e + {}^{208}\text{Pb} \rightarrow {}^{208}\text{Bi} + e^-$
as a function of the neutrino energy



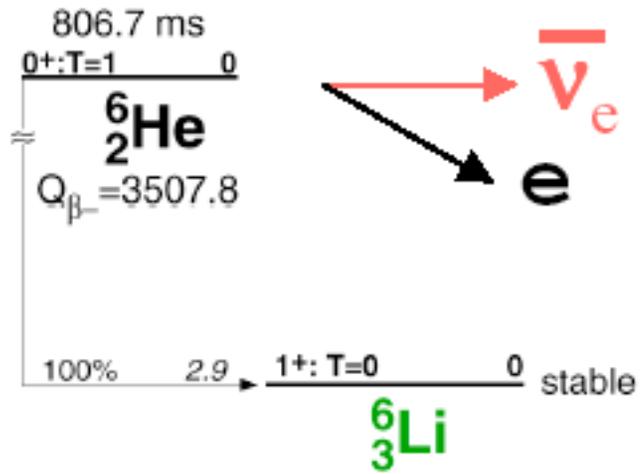
States

as a

energy

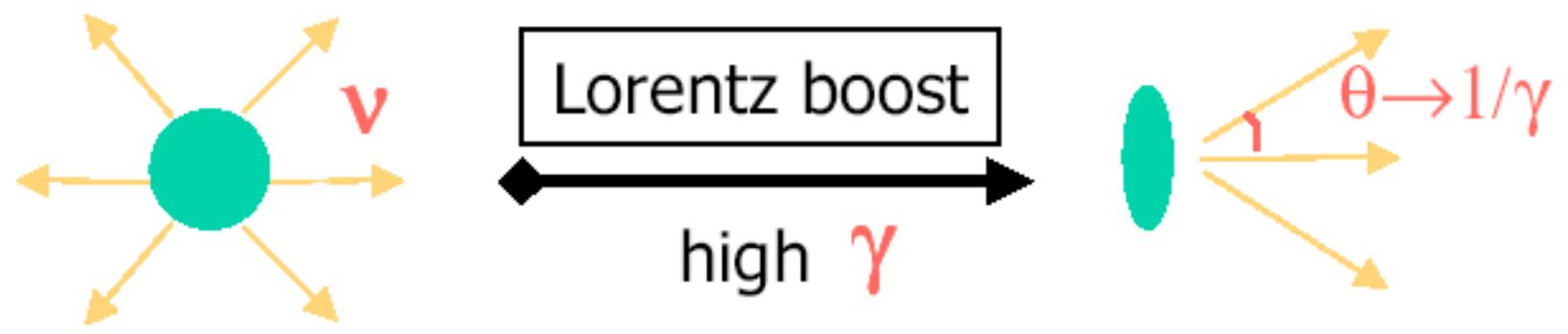
To experimentally study neutrino cross-sections at astrophysically relevant low-energies (i.e. to measure the spin-isospin response of the nuclei) one needs neutrinos with varying energies !

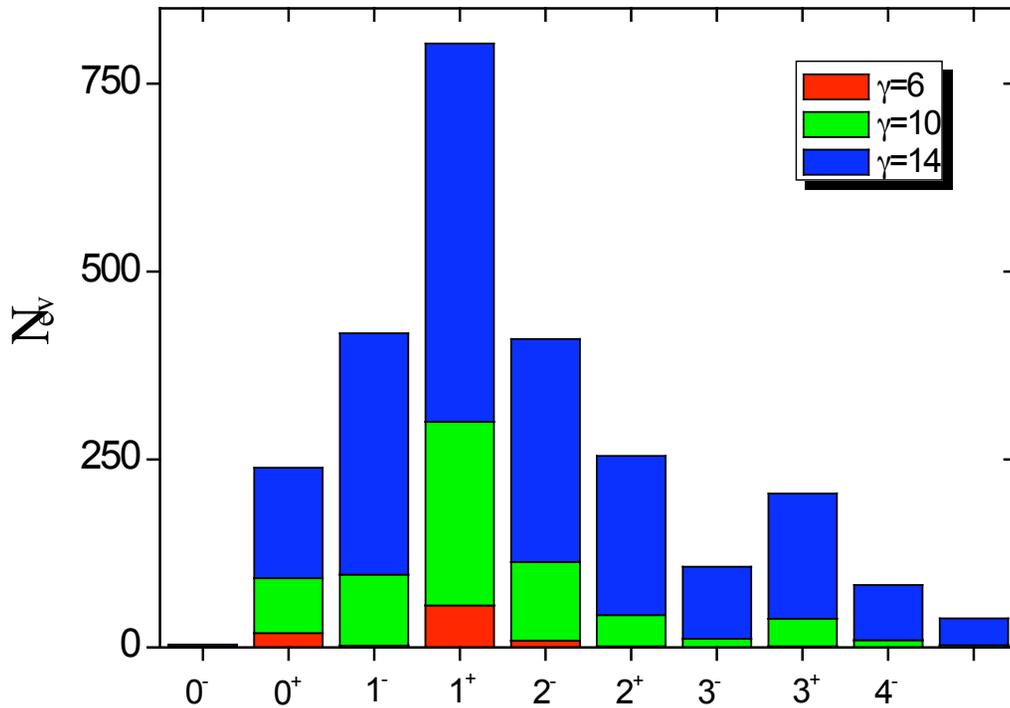
Beta-beam concept



Advantages:

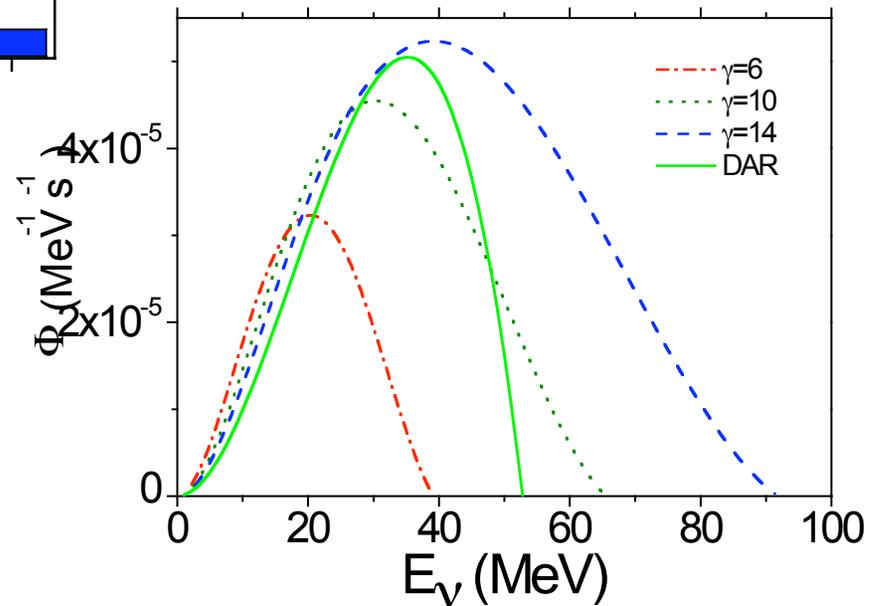
- Can be done at a facility studying exotic nuclei with radioactive beams
- Pure beams of a single neutrino flavor
- Well-known spectra
- Strong collimation at higher energies





With low-energy beta-beams it would be possible to do a systematic study of spin-isospin response of nuclei!

Lazauskas and Volpe,
Nucl.Phys.A792,219,2007



The weak-magnetism contribution to the cross-section for the reaction



Weak hadronic current

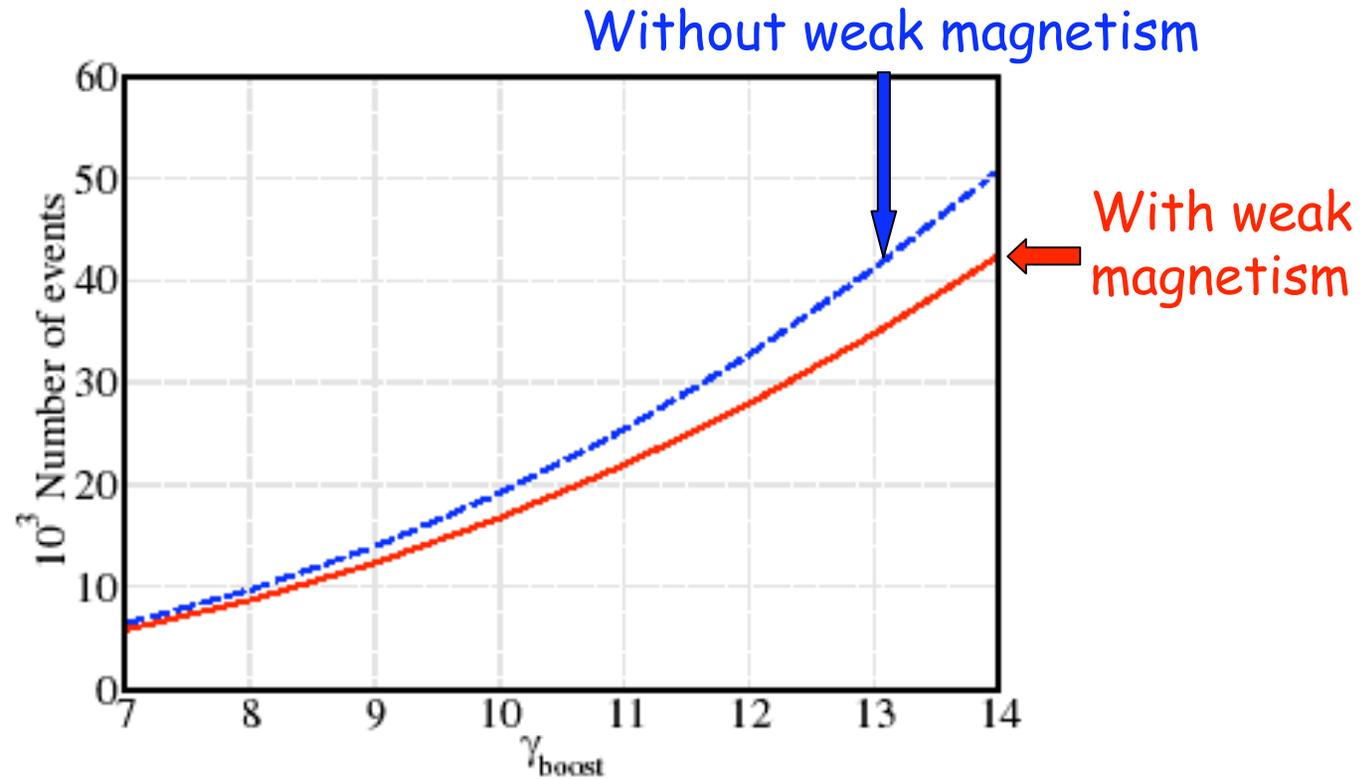
$$\frac{G_F \cos \theta_C}{\sqrt{2}} \left\{ \bar{u}_n \left[\gamma_\alpha (f_1 - g_1 \gamma_5) + \sigma_{\alpha\beta} k^\beta (f_2 + g_2 \gamma_5) + k_\alpha (f_3 + g_3 \gamma_5) \right] u_p \right\}$$

The Conserved Vector Current (CVC) hypothesis:

$$\lim_{q^2 \rightarrow 0} f_1(q^2) = 1; \quad \lim_{q^2 \rightarrow 0} f_2(q^2) = \frac{\mu_p - \mu_n}{2m_N}; \quad f_3(q^2) = 0$$

Weak magnetism

Weak magnetism contributions may increase the antineutrino mean free path in a supernova Horowitz



Expected number of events at a low-energy beta-beam over a year for antineutrino-proton scattering using a Water Cerenkov detector

Balantekin, de Jesus, Lazauskas, Volpe, 2006

Neutrino-electron scattering

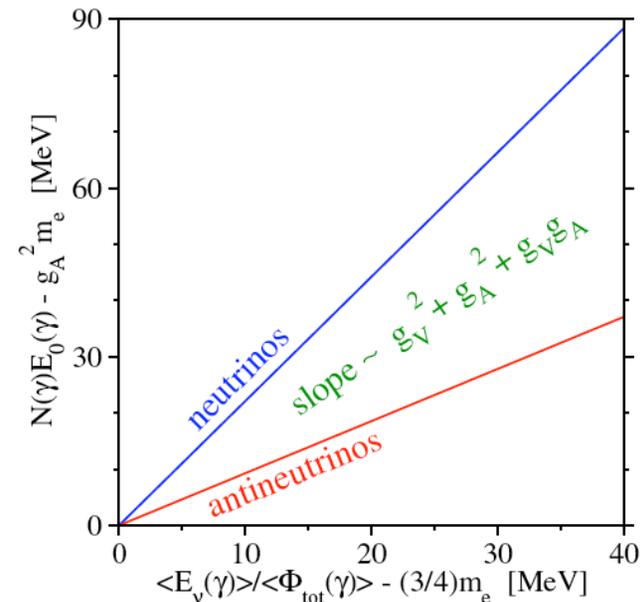
$$\frac{d\sigma_{(\nu,e)}}{dT_e} \sim (g_V^2 + g_A^2) + (g_V^2 - g_A^2) \left(1 - \frac{T_e}{E_\nu}\right)^2 + \dots$$

$$g_V = 1/2 + 2 \sin^2 \theta_W + \dots \quad g_A = \pm 1/2 + \dots$$

Averaging over the beta-beam flux, $\langle \phi \rangle$, gives

$$\langle \sigma_{(\nu,e)} \rangle \sim -g_V (g_V + g_A) m_e \langle \phi_\nu \rangle + \frac{4}{3} (g_V^2 + g_A^2 + g_V g_A) \langle E_\nu \rangle$$

Balantekin, J.H. de Jesus and C. Volpe, Phys. Lett. B **634**, 180 (2006)



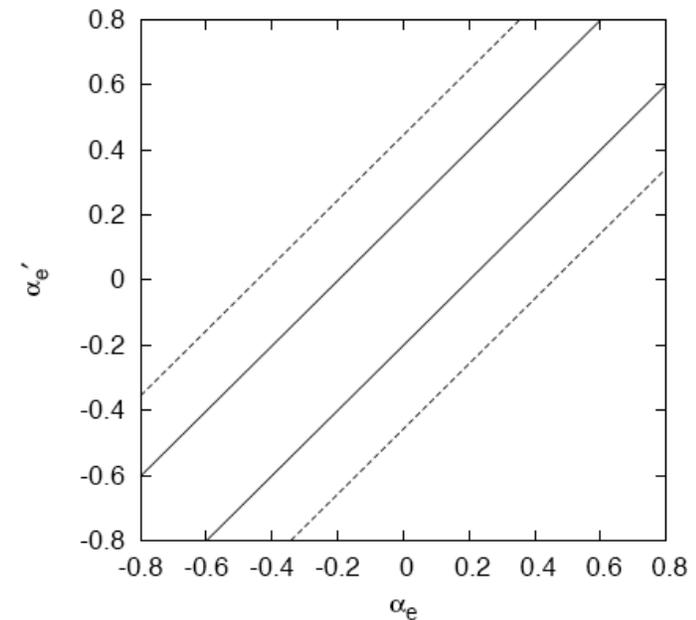
Testing flavor universality in ν neutral-current scattering

$$\sigma(\nu_e e^- \rightarrow \nu_e e^-) = \frac{G_F^2 E_\nu^2 m_e}{\pi(2E_\nu + m_e)^3} \left[\frac{16}{3}(g_A''^2 + g_V''^2 + g_A''g_V'')E_\nu^2 + 4m_e(2g_A''^2 + g_V''^2 + g_A''g_V'')E_\nu + m_e^2(3g_A''^2 + g_V''^2) \right]$$

$$g_{A(V)}'' = \left(1 + \frac{v^2}{\Lambda^2}(-\alpha_e + \alpha_e')\right) g_{A(V)}' + \left(1 + \frac{2v^2}{\Lambda^2}\alpha_e'\right)^2,$$

$$g_{A(V)}' = g_{A(V)} - \frac{v^2}{2\Lambda^2}(\alpha_e + \alpha_e'),$$

$$g_A = -\frac{1}{2}, \quad g_V = -\frac{1}{2} + 2\sin^2 \theta_W,$$



Balantekin, Sahin and Sahin, 2009

$\gamma = 530$

Solar Neutrinos-Open Questions:

- Can we test the relation between solar photon and neutrino luminosities? Is there a subdominant neutrino source?
- Does the Sun entirely work via the pp-chain? What is the contribution from the CNO cycle?
- Does the neutrino have a magnetic moment? If so, does it effect solar neutrino flux? Are there solar antineutrinos?
- Can we use neutrinos to measure solar properties such as density scale height?
- Can we use solar neutrinos to do physics beyond both the Standard Model of the Sun and the Standard Model of particle physics? Are the signatures for such physics generic?
- Once we are done with the solar **nuclear fusion** neutrinos, can we ever detect solar **plasma** neutrinos?

Solar Neutrinos-Open Questions:

- Correlation between solar photon luminosity and neutrino luminosity
- Does the solar neutrino flux contribute to the solar energy budget?
- Does the solar neutrino flux affect the solar wind?
- Can we detect solar neutrinos on a global scale?
- Can we detect solar neutrinos from a Model of the Sun's interior? Are there signatures for such neutrinos?
- Once we are done with the solar **nuclear fusion** neutrinos, can we ever detect solar **plasma** neutrinos?

All these questions
require knowledge of
either production or
detection cross
sections for neutrinos!

Special: New Learning Series on Genetics, page 70

Complexity—the Science of Surprise | Your Inner Savant

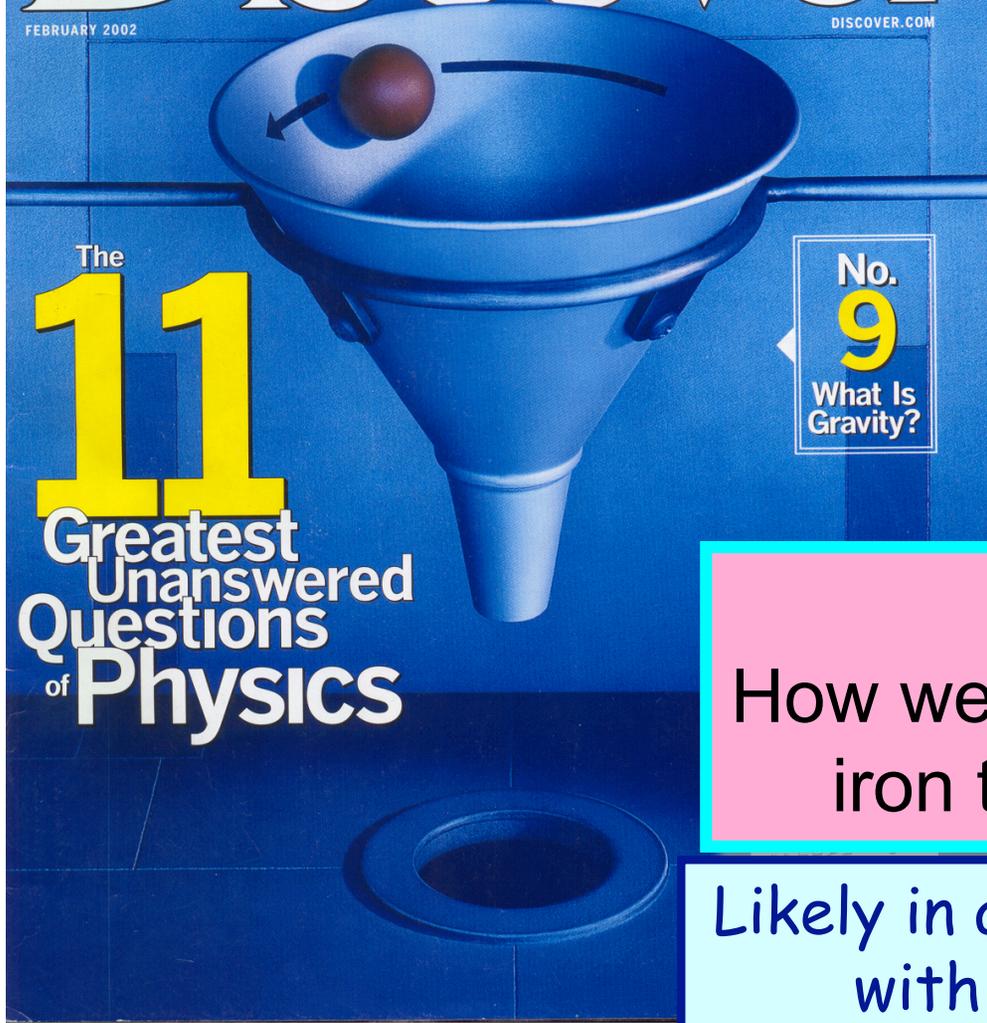
Discover

FEBRUARY 2002

DISCOVER.COM

The
11
Greatest
Unanswered
Questions
of **Physics**

No.
9
What Is Gravity?



U.S. National Academy of Sciences Report "Connecting Quarks with the Cosmos: Eleven Science Questions For the New Century"

Question 10
How were the elements from iron to uranium made ?

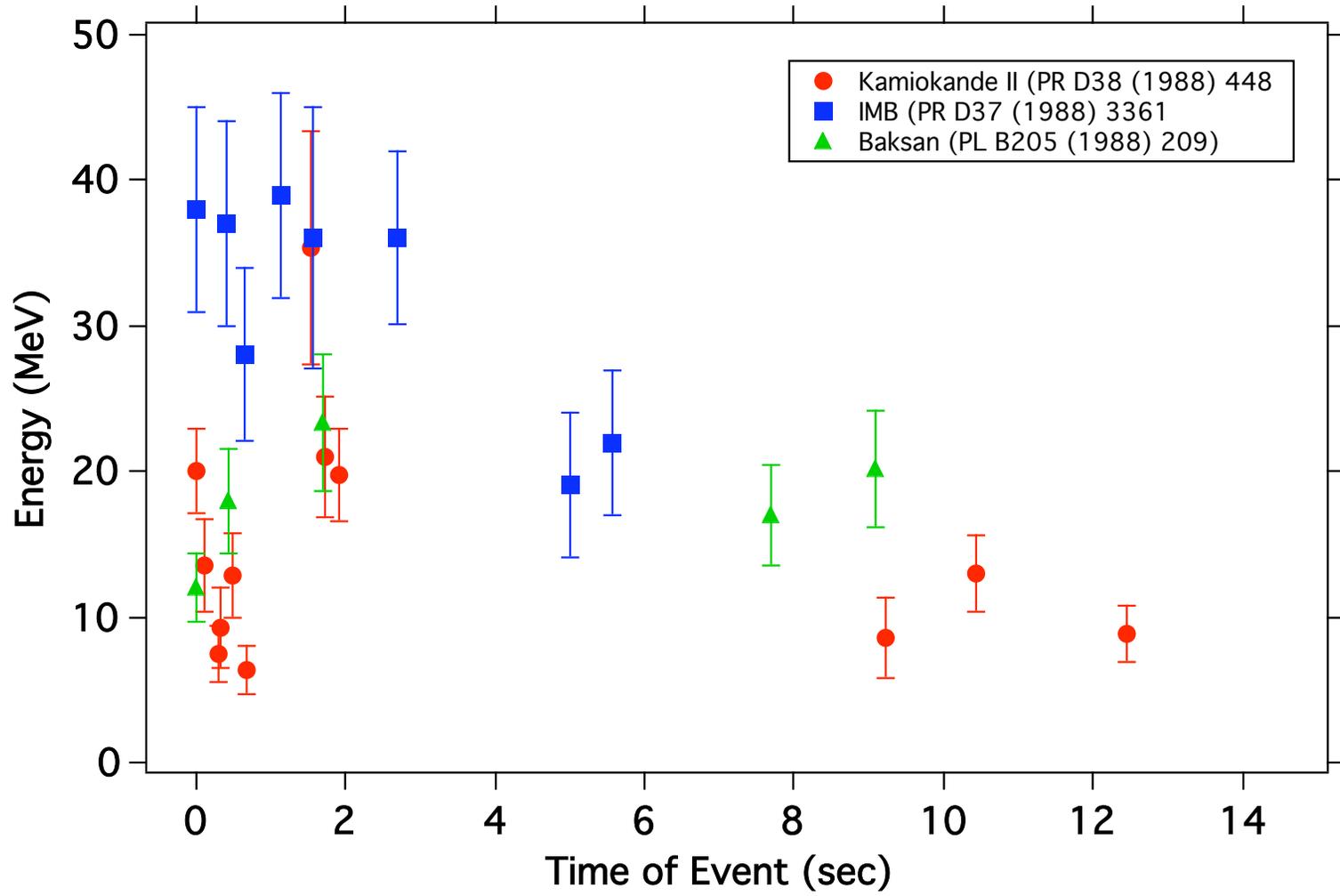
Likely in a core-collapse supernova with the aid of neutrinos

Neutrinos from core-collapse supernovae



- $M_{\text{prog}} \geq 8 M_{\text{Sun}}$
- $\Delta E \approx 10^{53} \text{ ergs} \approx 10^{59} \text{ MeV}$
- 99% of the energy is carried away by neutrinos and antineutrinos with $10 \leq E_{\nu} \leq 30 \text{ MeV}$
- 10^{58} Neutrinos!

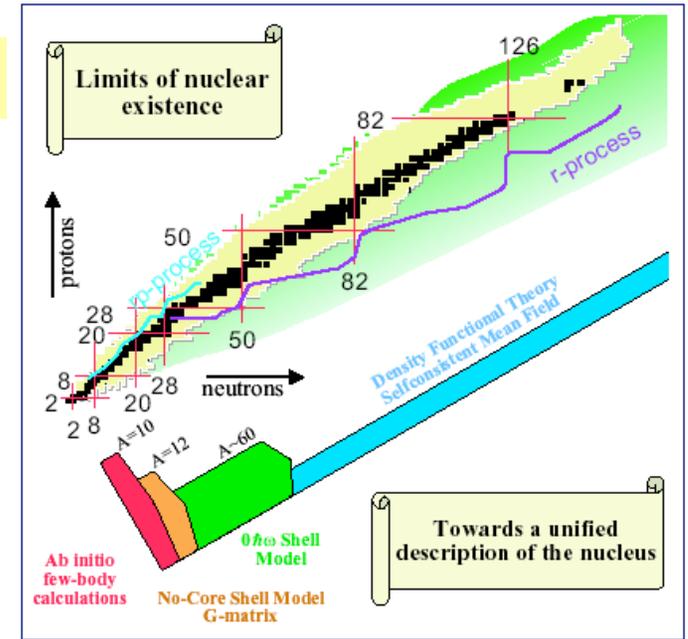
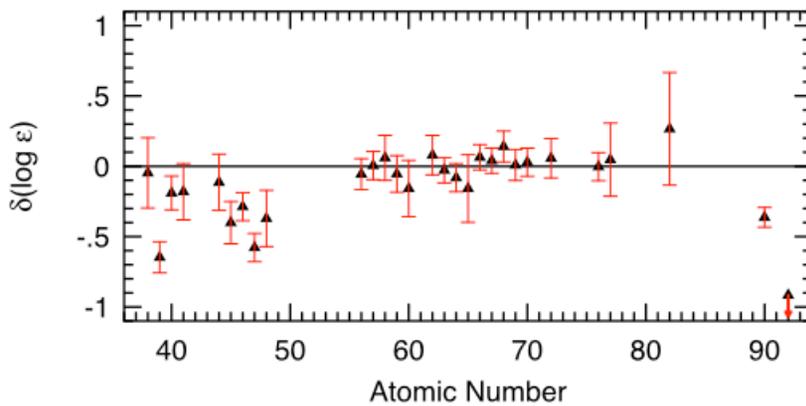
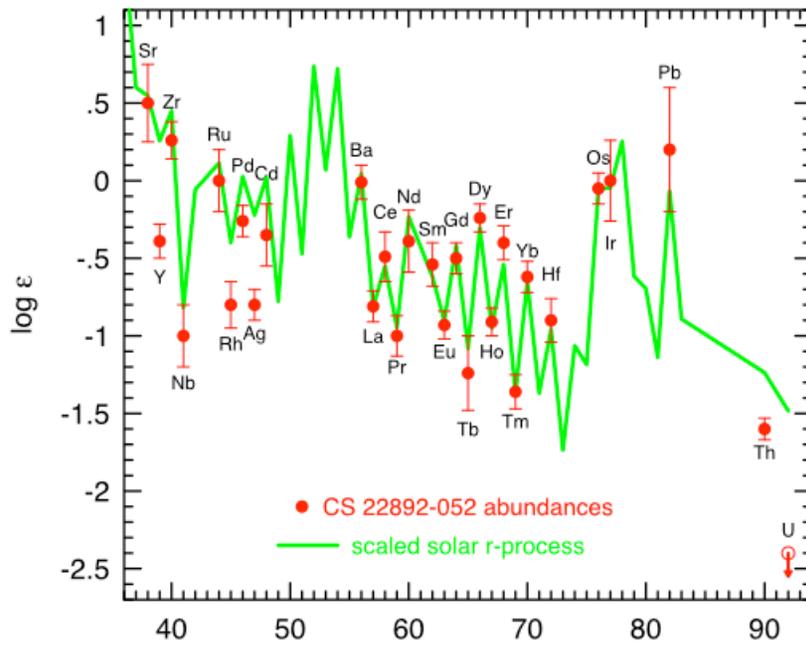
Neutrinos from SN1987A



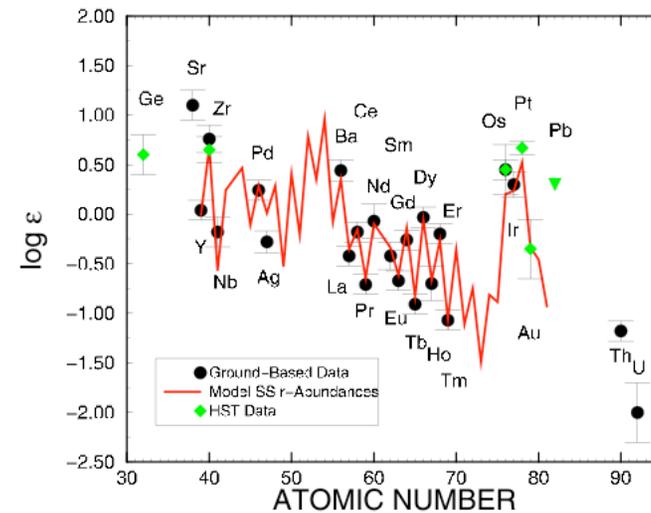
Observed r-process abundances

$[Fe/H] \approx -3.1$

Neutron-Capture Abundances in CS 22892-052

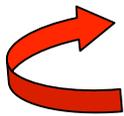


$A > 100$ abundance pattern fits the solar abundances well.



Life stages of a core-collapse supernova

1. Collapse and bounce epoch. $S/k \approx 1$
2. Shock-reheating epoch. $S/k \approx 40$
3. Hot-bubble epoch. $S/k \approx 75$ to 500?



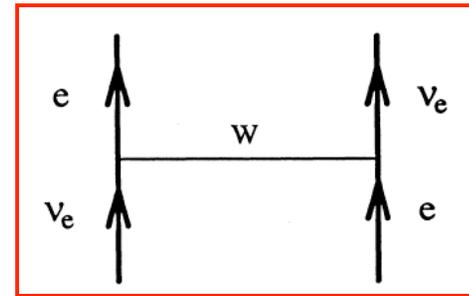
Possible site of r-process
nucleosynthesis

MSW effect

In vacuum: $E^2 = p^2 + m^2$

In a potential: $(E - \Phi)^2 = p^2 + m^2 \Rightarrow E^2 = p^2 + m_{\text{eff}}^2, m_{\text{eff}}^2 \approx m^2 + 2E\Phi$

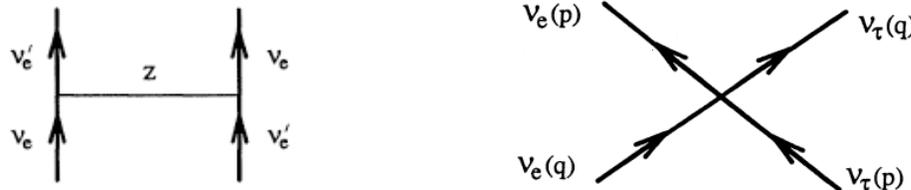
The potential is provided by the coherent forward scattering of ν_e 's off the electrons in dense matter.



There is a similar term with Z-exchange. But since it is the same for all neutrino flavors, it does not contribute to phase differences *unless* we invoke a sterile neutrino.

$$i \frac{\partial}{\partial t} \begin{pmatrix} \psi_e \\ \psi_x \end{pmatrix} = \begin{pmatrix} -\frac{\delta m^2}{4p} \cos 2\theta + \frac{1}{\sqrt{2}} G_F N_e & \frac{\delta m^2}{4p} \sin 2\theta \\ \frac{\delta m^2}{4p} \sin 2\theta & \frac{\delta m^2}{4p} \cos 2\theta - \frac{1}{\sqrt{2}} G_F N_e \end{pmatrix} \begin{pmatrix} \psi_e \\ \psi_x \end{pmatrix}$$

If the neutrino density itself is also very high then one has to consider the effects of neutrinos scattering off other neutrinos. This is the case for a core-collapse supernova.



In core-collapse supernovae particle abundances are the isospin-mirror of the abundances for Big-bang nucleosynthesis!

Big-Bang: $n/p \ll 1$

Core-collapse SN: $n/p \gg 1$

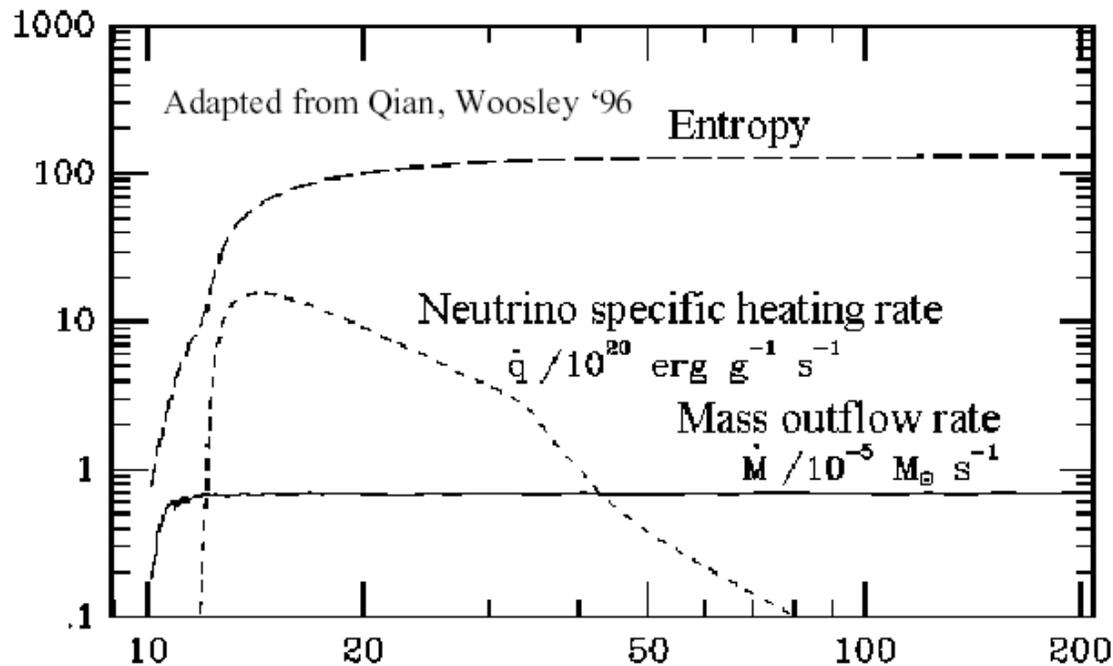
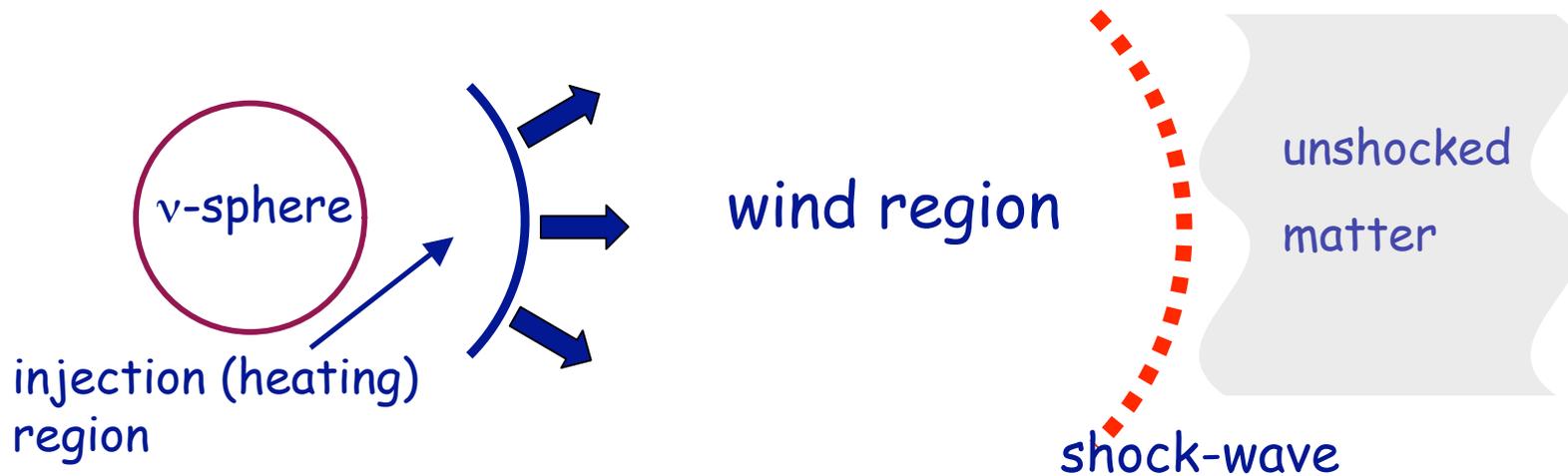
This makes core-collapse supernovae an ideal site for r-process nucleosynthesis which requires a lot of neutrons!

Yields of r-process nucleosynthesis are determined by neutron-to-proton ratio, n/p

Interactions of the neutrinos and antineutrinos streaming out of the core both with nucleons and seed nuclei determine the n/p ratio. ① Hence it is crucial to understand (and measure!) neutrino-nucleon as well as neutrino-nucleus cross-sections.

Before these neutrinos reach the r-process region they undergo matter-enhanced neutrino oscillations as well as coherently scatter over other neutrinos. ② Many-body behavior of this neutrino gas is not completely understood, but may have significant impact on r-process nucleosynthesis.

Neutrino-driven wind in post-core bounce supernova



Mass outflow rate in the wind region is approximately constant

Electron Fraction

$$Y_e = (n_{e^-} - n_{e^+}) / n_{\text{baryons}}$$

λ = reaction rate

$$\frac{dY_e}{dt} = \lambda_n - (\lambda_p + \lambda_n)Y_e + \frac{1}{2}(\lambda_p - \lambda_n)X_\alpha$$

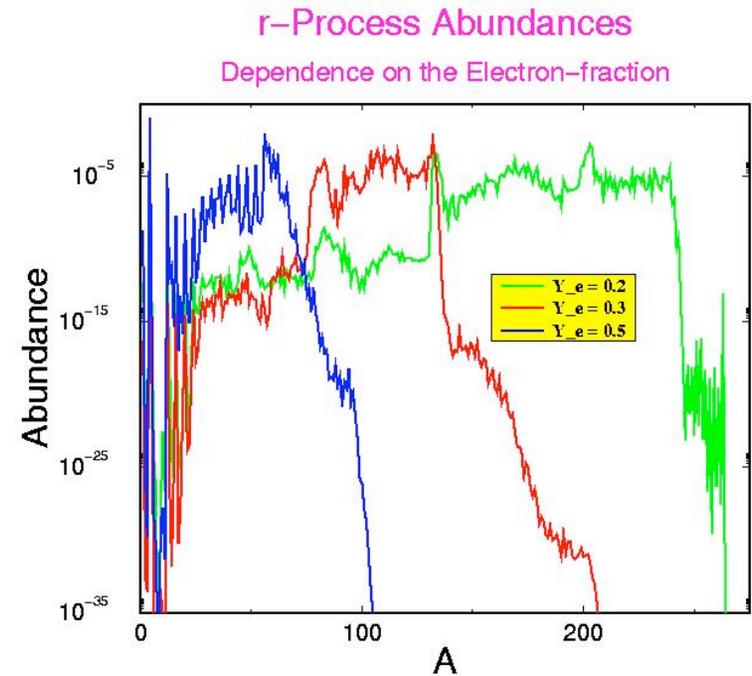
$\lambda_p = \lambda_{\nu e^-} + \lambda_{e^-}$
proton loss rate

$\lambda_n = \lambda_{\nu e^+} + \lambda_{e^+}$
neutron loss rate

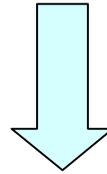
X_α alpha
fraction

Weak freeze-out radius: where neutron-to-proton conversion rate is less than the outflow rate

$$dY_e/dt = 0$$



$$dY_e/dt = 0$$



$$Y_e = \frac{\lambda_n}{\lambda_p + \lambda_n} + \frac{1}{2} \frac{\lambda_p - \lambda_n}{\lambda_p + \lambda_n} X_\alpha$$

If alpha particles are present

$$Y_e^{(0)} = \frac{1}{1 + \lambda_{\bar{\nu}_e}/\lambda_{\nu_e}}$$

If alpha particles are absent

$$Y_e = Y_e^{(0)} + \left(\frac{1}{2} - Y_e^{(0)} \right) X_\alpha$$

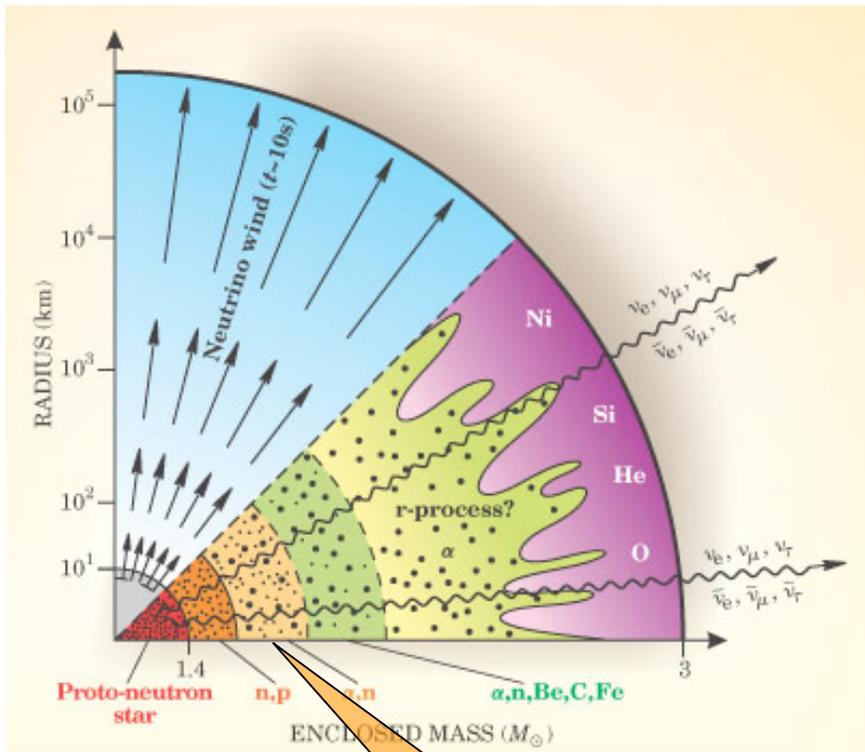
If $Y_e^{(0)} < 1/2$, non-zero X_α increases Y_e .
If $Y_e^{(0)} > 1/2$, non-zero X_α decreases Y_e .



Non-zero X_α
pushes Y_e to 1/2

Alpha effect

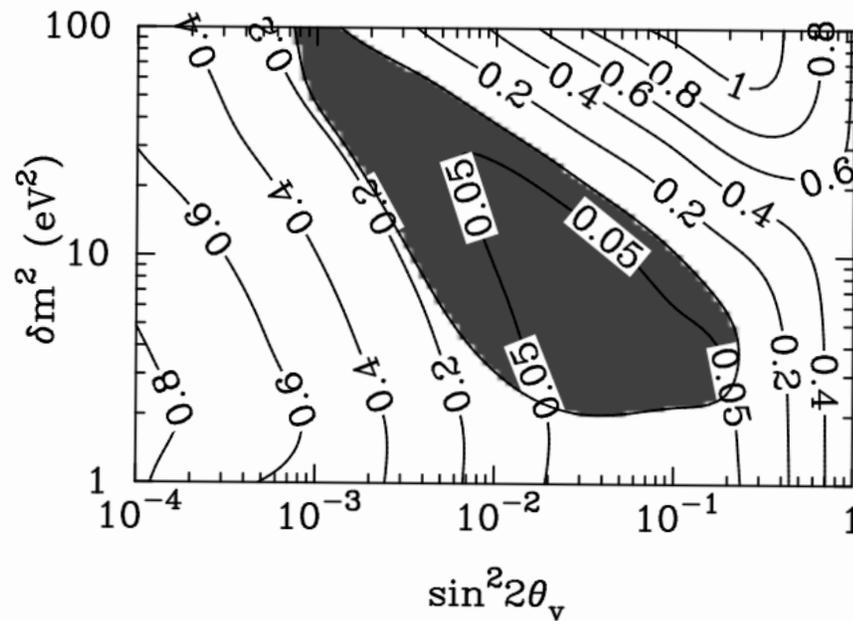
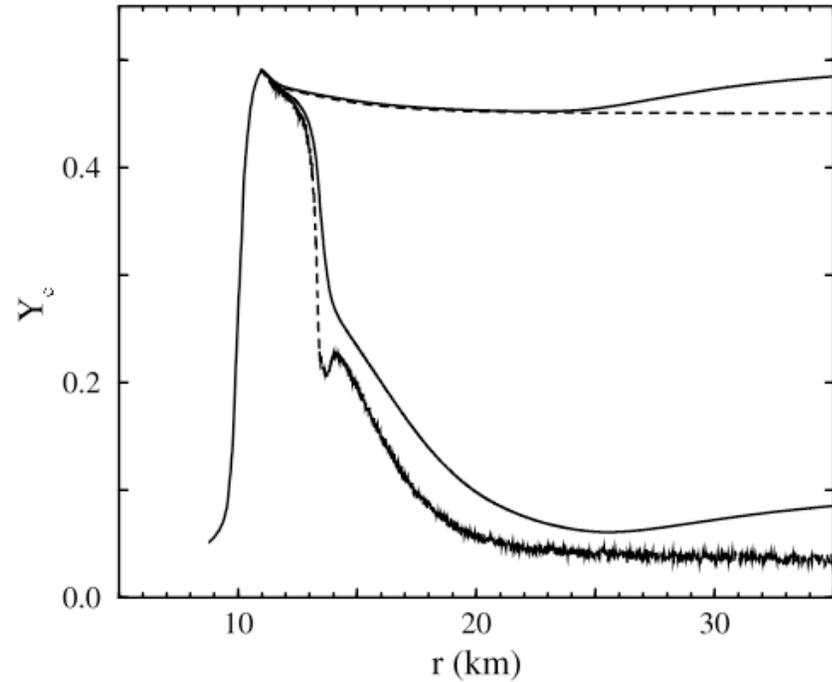
Fuller, McLaughlin, Meyer



Alpha effect

Active-sterile mixing

McLaughlin, Fetter, Balantekin,
Fuller, *Astropart. Phys.*, 18, 433
(2003)



Can neutrino magnetic moment help with the alpha problem?

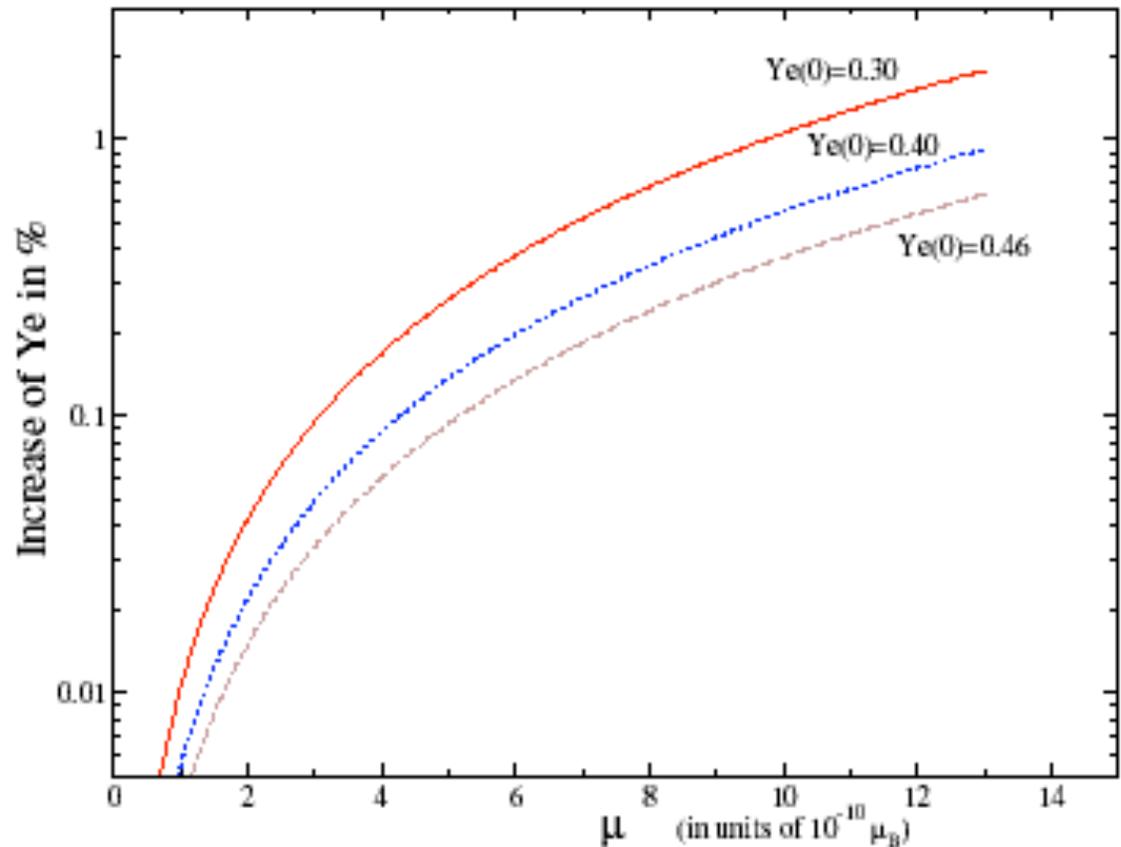
No!

For Dirac neutrinos

$\nu_{eL} \rightarrow$ sterile states

Both neutrinos and antineutrinos are reduced and the electron fraction increases!

Balantekin, Volpe,
Welzel, JCAP 09 (2007).



4 km away from the neutron star surface

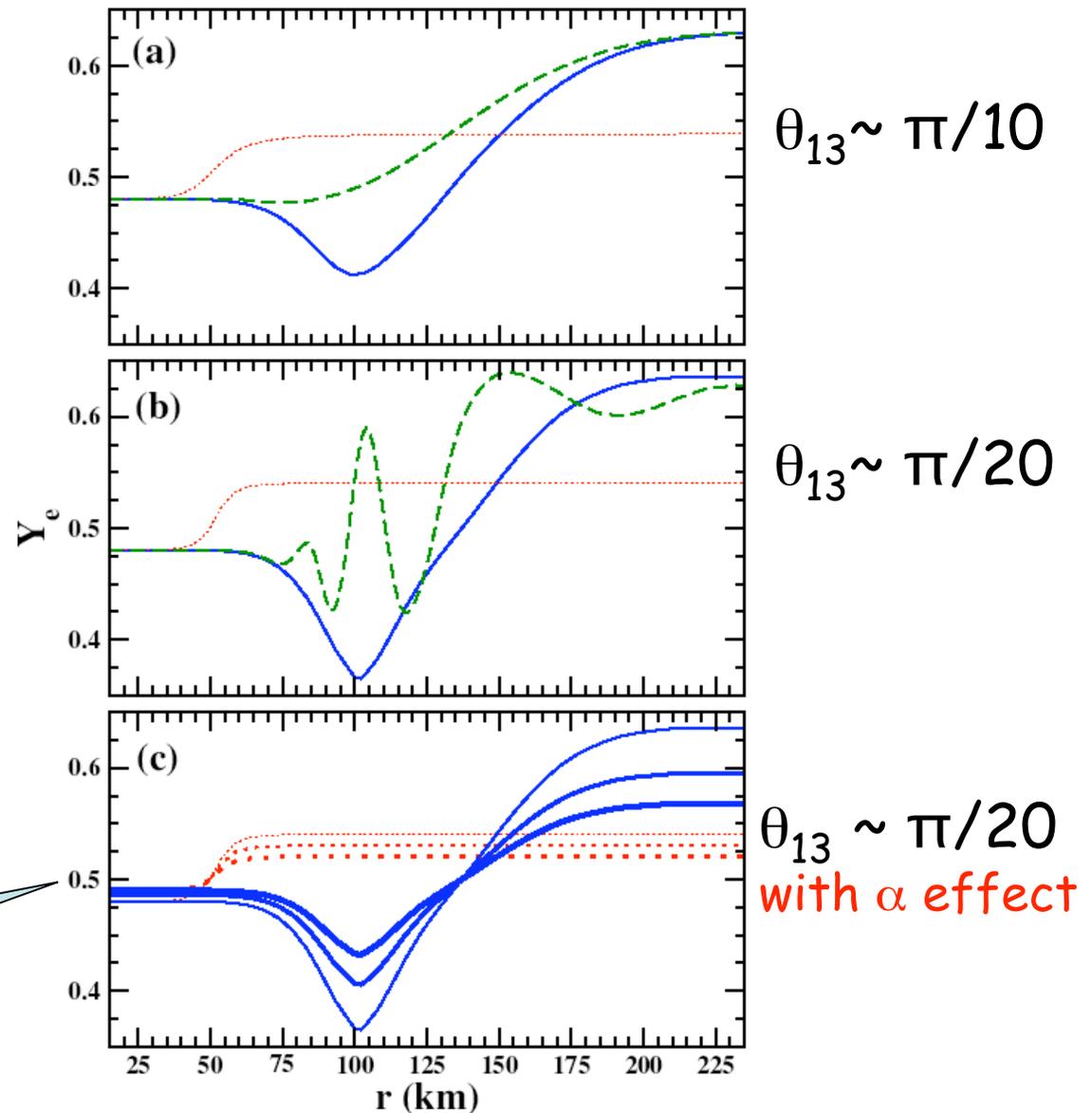
But...

One finds large-scale, collective flavor oscillations deep in the supernova envelope, which is sensitive to the value of θ_{13} .

Fuller, Qian, Raffelt, Duan, Sigl, Balantekin, Pehlivan, Carlson,....

ν luminosity:
 $L^{51} = 0.001, 0.1, 50$

Alpha abundance:
 $X_\alpha = 0, 0.3, 0.5$ (thin, medium, thick lines)

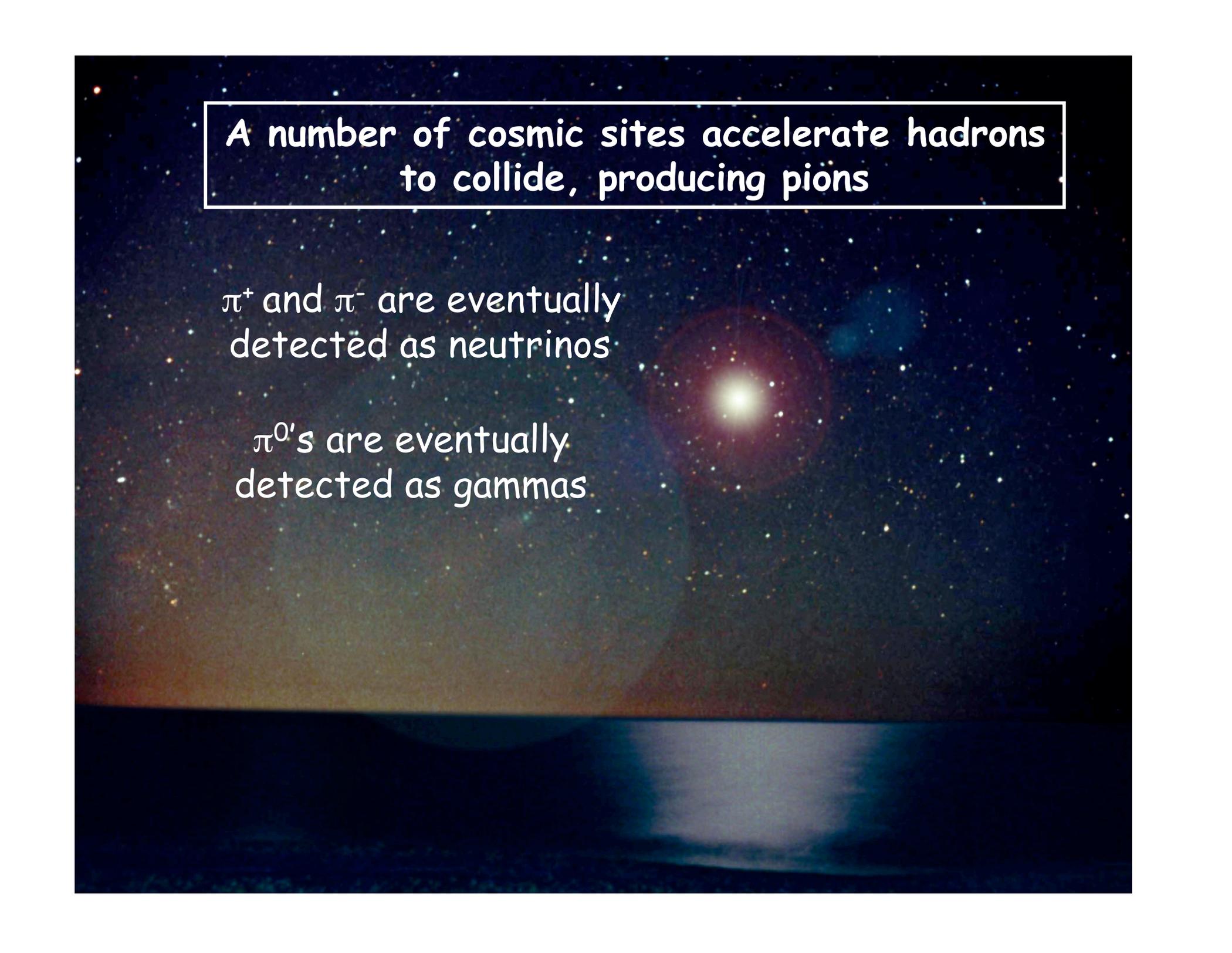


Balantekin and Yüksel, New J. Phys. 7, 51 (2005)

- Core-collapse supernovae indeed emit neutrinos. It would be nice to see a second one besides SN1987A.
- If you measure the neutrino spectra you learn a lot about the supernova mechanism. We need the time-dependence (neutronization burst, black-hole vs. neutron-star) and the flavor content of the neutrino spectra as well as the average energy and time-integrated luminosity (to understand the neutron star).
- Ability to observe supernovae in nearby galaxies would greatly improve the statistics.
- Diffuse supernova neutrinos give us a handle on the star-formation rate.
- Astrophysical extremes allow testing neutrino properties in ways that cannot be done elsewhere, e.g. ν - ν effect as an "emergent phenomenon".

- Core-collapse supernovae indeed emit neutrinos. It would be nice to see a second one besides SN1987A.
- If you measure the neutrino spectra you learn a lot about the star formation mechanism. We need the time-dependence of the star formation rate (burst, black-hole vs. neutron-star) and the neutrino spectra as well as the integrated luminosity (to understand the star formation rate).
- Ability to measure neutrino interactions! Galaxies would be greatly impacted.
- Diffuse supernova neutrino background depends on the star-formation rate.
- Astrophysical extremes allow testing neutrino properties in ways that cannot be done elsewhere, e.g. ν - ν effect as an "emergent phenomenon".

All of this also requires a detailed understanding of neutrino interactions!



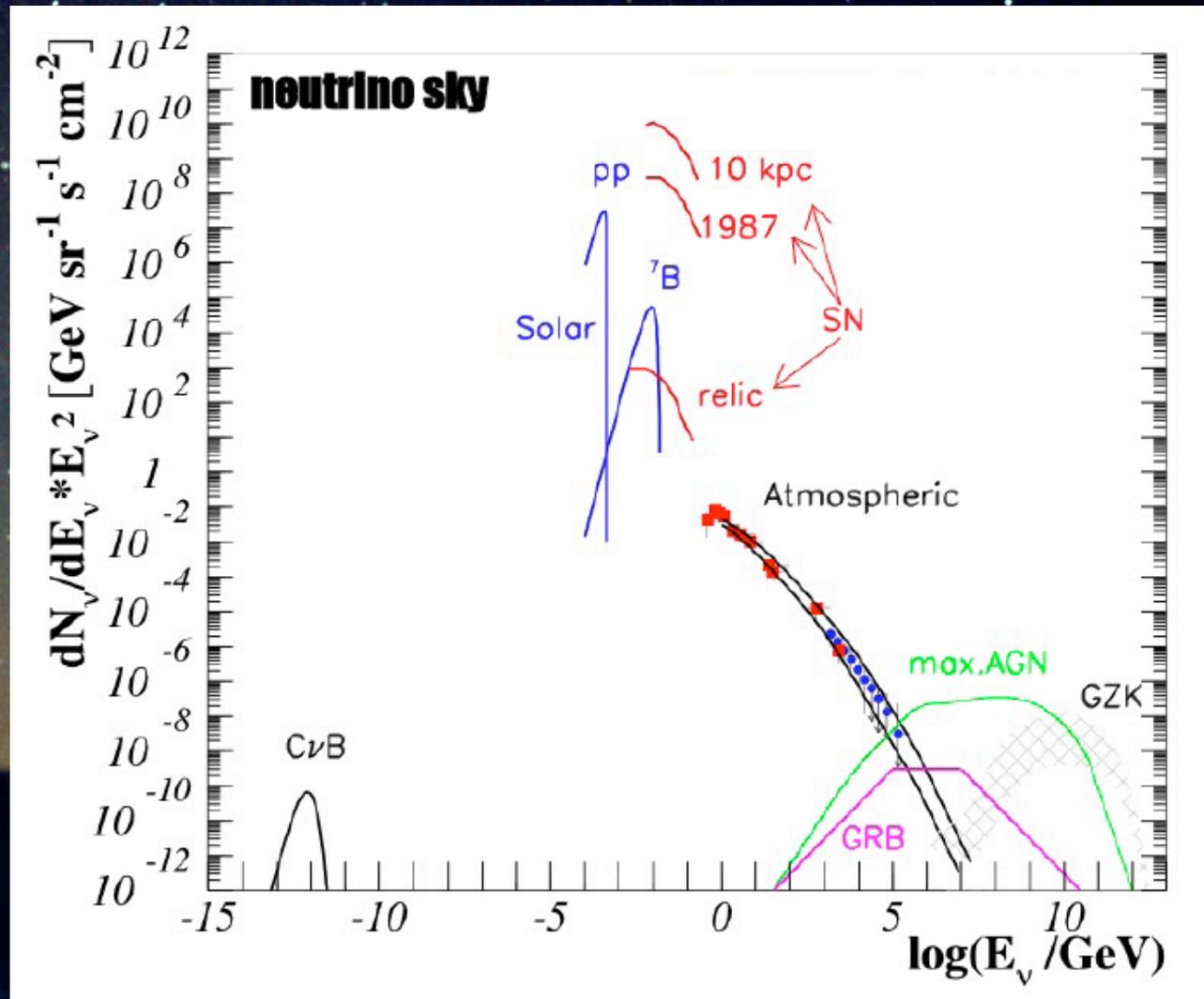
A number of cosmic sites accelerate hadrons
to collide, producing pions

π^+ and π^- are eventually
detected as neutrinos

π^0 's are eventually
detected as gammas

A number of cosmic sites accelerate hadrons to collide, producing pions.

π^+ and π^-
are
eventually
detected
as
neutrinos



Assessment of such cosmic neutrino sources requires understanding neutrino interactions at exceedingly high energies!

Conclusions

- Neutrino cross sections are often a crucial input in understanding a broad range of phenomena ranging from stellar evolution to core-collapse supernovae and gamma-ray bursts.
- Understanding neutrino interactions from very low to very high energies are often crucial in interpreting the data from a variety of astrophysical sources.
- At low energies (supernova and tail of atmospheric neutrinos) calculational tools are still being developed. At very high energies physics beyond the Standard Model is very likely to contribute.
- At astrophysical sites novel forms of neutrino interactions may emerge such as collective behavior driven by neutrino-neutrino interactions.