

Hydrodynamical description of $dn/d\eta$ by CMS and TOTEM at 7 and 8 TeV

T. Csörgő^{1,2}, M. Csanád², C-B. Yang³ and Z-F Jiang³

¹ Wigner RCP, Budapest, Hungary

² ELTE University, Budapest, Hungary

³ CCNU, Wuhan, China

Intro to initial energy density estimate

Improving Bjorken's estimate

pp $dn/d\eta$ data @ 7 and 8 TeV

from TOTEM, and CMS/TOTEM

Cu+Cu, Au+Au@RHIC

Pb+Pb@LHC

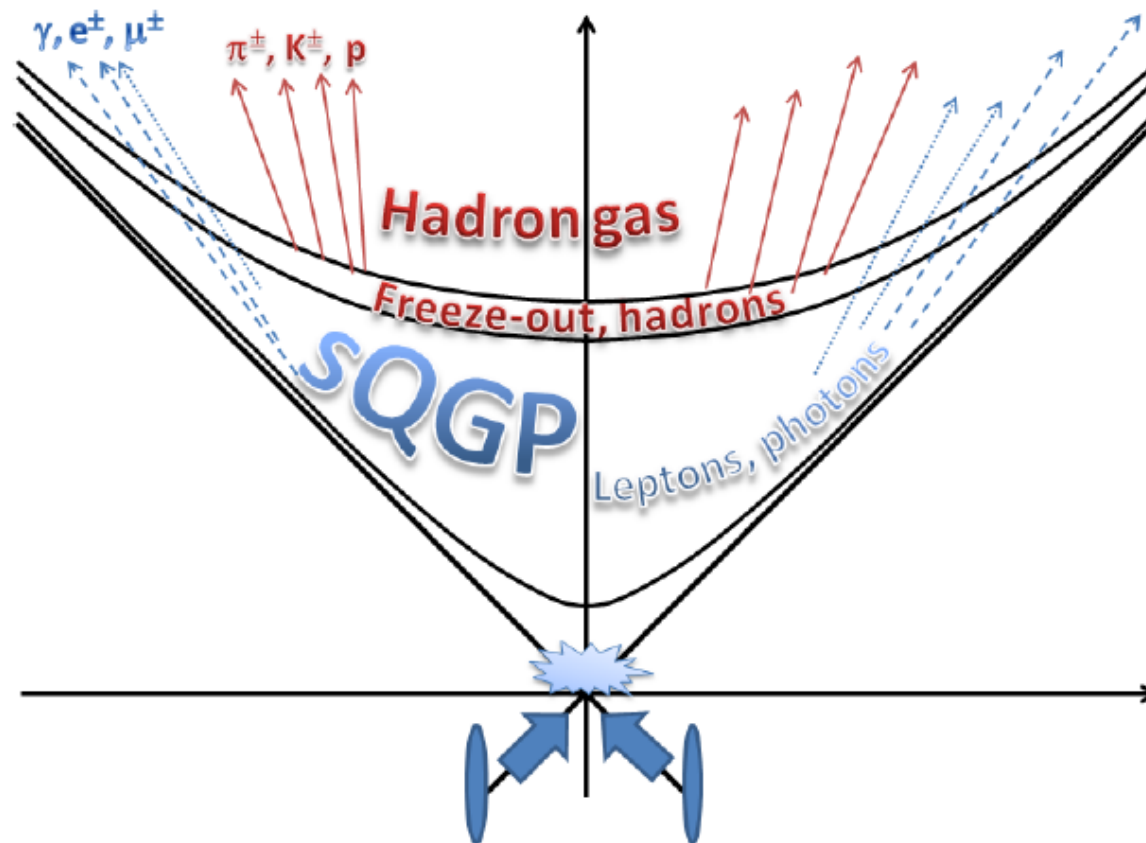
Implications

Summary

Predictions

Standard Hydro Model for A+A

- Strongly interacting QGP discovered at RHIC & created at LHC
- A hot, expanding, strongly interacting, perfect QG fluid
- Hadrons created at the freeze-out
- Leptons, photons “shine through”



Björken-estimate – hydro for p+p

Idea:

Initial energy density measurable from dE/dy

QGP critical ε : $\sim 1 \text{ GeV}/\text{fm}^3$

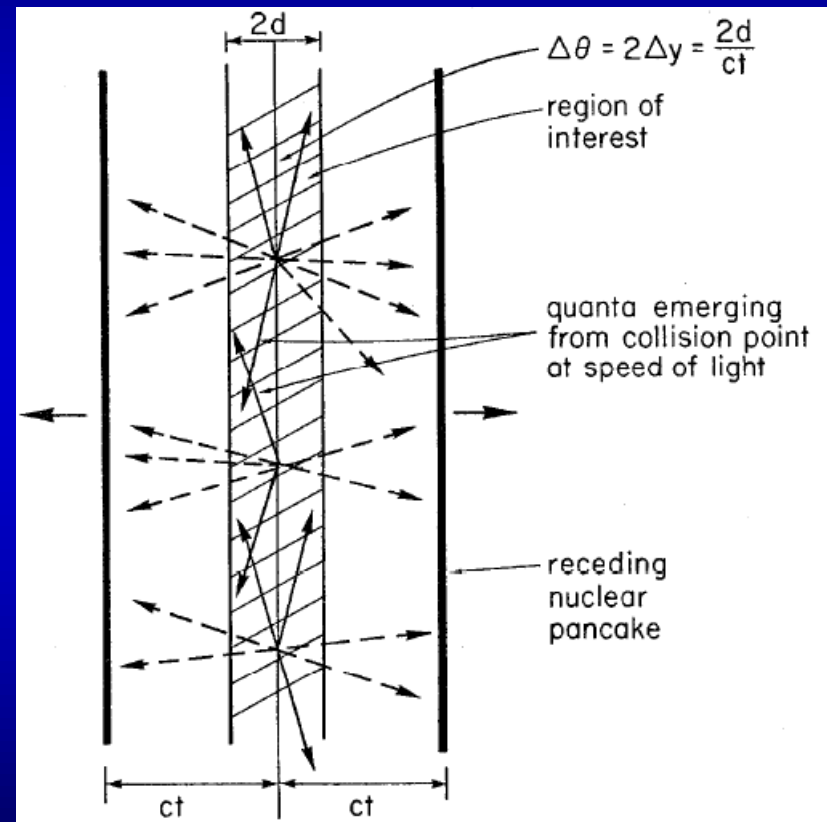
$dE/dy = \langle m_t \cosh(y) \rangle dn/dy$

Area from HBT

Top cited result:

J.D. Bjorken, Phys.Rev. D27 (1983)

$$\varepsilon_{Bj} = \frac{1}{R^2 \pi \tau_0} \frac{dE}{d\eta} = \frac{\langle E \rangle}{R^2 \pi \tau_0} \frac{dn}{d\eta}$$



IF $dn/d\eta$ is not flat: **Needs correction!**

Advanced estimate

**Need for correction:
dn/dy not flat, no rapidity plateau even @ LHC
Finite, accelerating!**

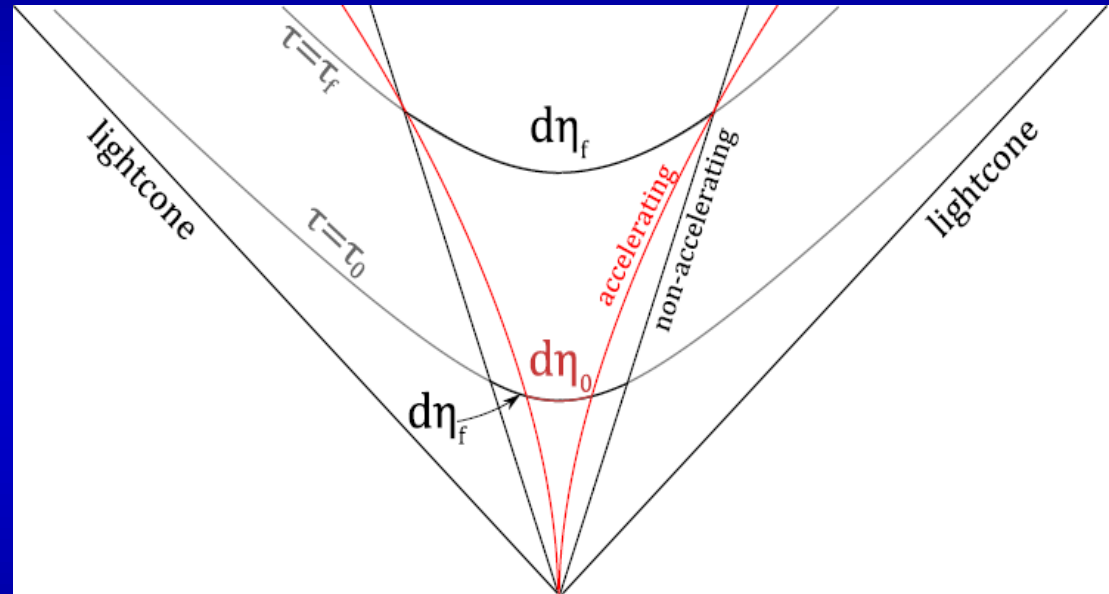
**Need:
accelerating solution
of relativistic hydro**

Two modifications:

$$\mathbf{y} \neq \eta$$

$$\eta_{\text{final}} \neq \eta_{\text{initial}}$$

**Advanced estimate
of initial energy density:**



$$\varepsilon = \varepsilon_{Bj} \frac{dy}{d\eta_f} \frac{d\eta_f}{d\eta_i}$$

A new solution of relativistic hydro

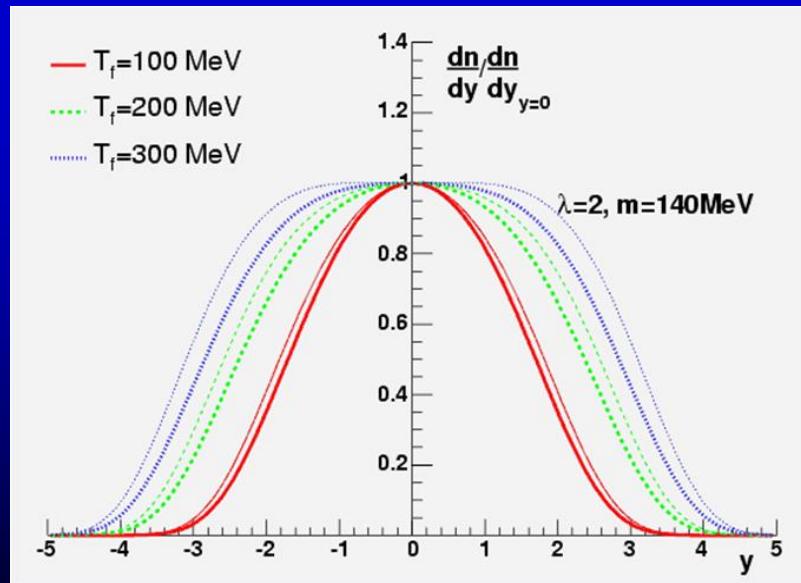
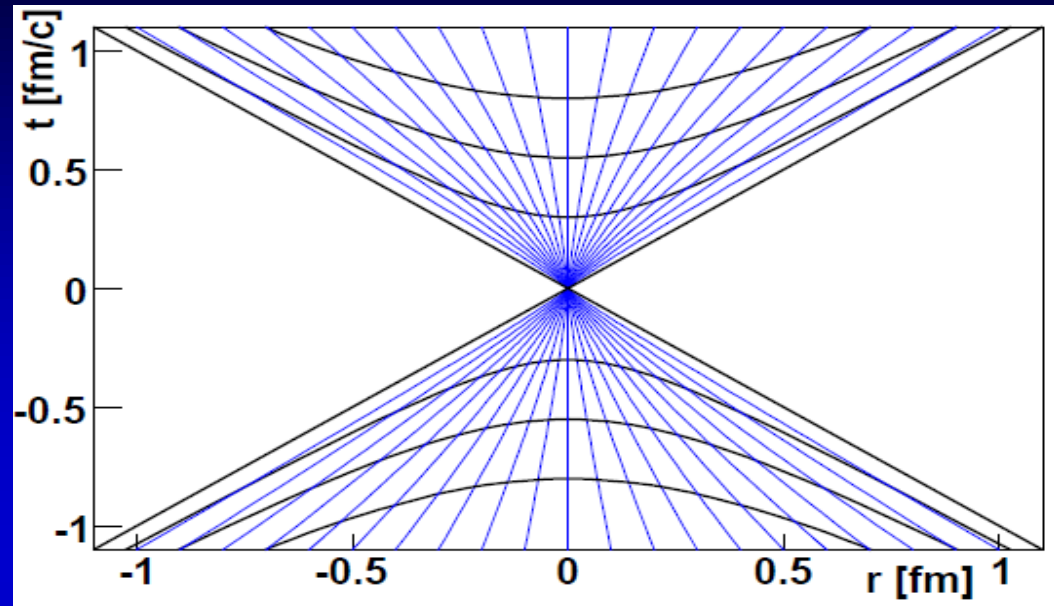
Velocity: $\tanh(\lambda\eta)$

Acceleration: $\lambda \neq 1$

Density: $(\tau/\tau_0)^\lambda$

dn/dy calculated, simple
but **NOT**
on a back-of-the-envelope,

Full details: 15 pages, 126 eqs
[arXiv:0709.3677](https://arxiv.org/abs/0709.3677) M.I. Nagy et al,
Phys. Rev. C.C77:024908,2008



Compare to RHIC data!
BRAHMS dn/dy measurement:
advanced initial ε estimate

Significant correction@RHIC!

Phys.Lett. B663 (2008) 306
nucl-th/0605070

Initial energy density at RHIC

Bjorken estimate from BRAHMS: 5 GeV/fm³

Advanced estimate gives:

Correction:

2-3x, result: 15 GeV/fm³, QCD EoS agreement!

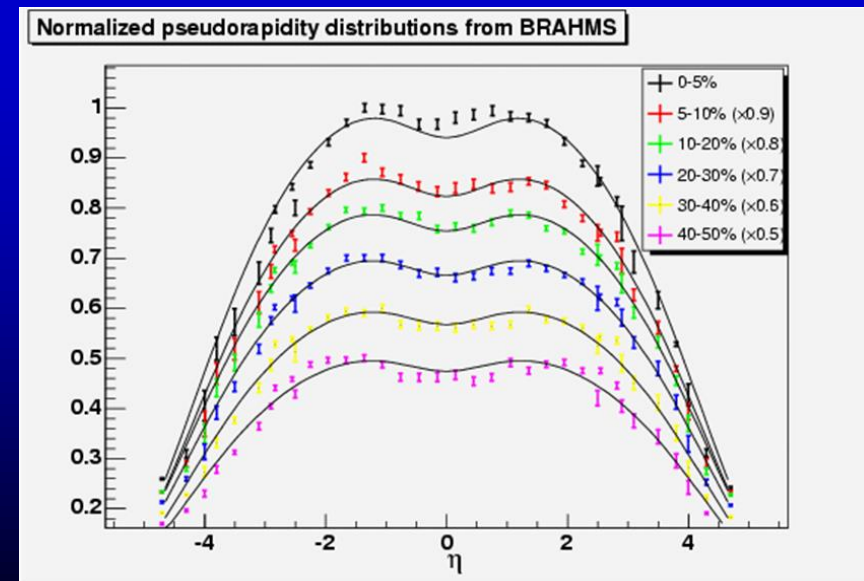
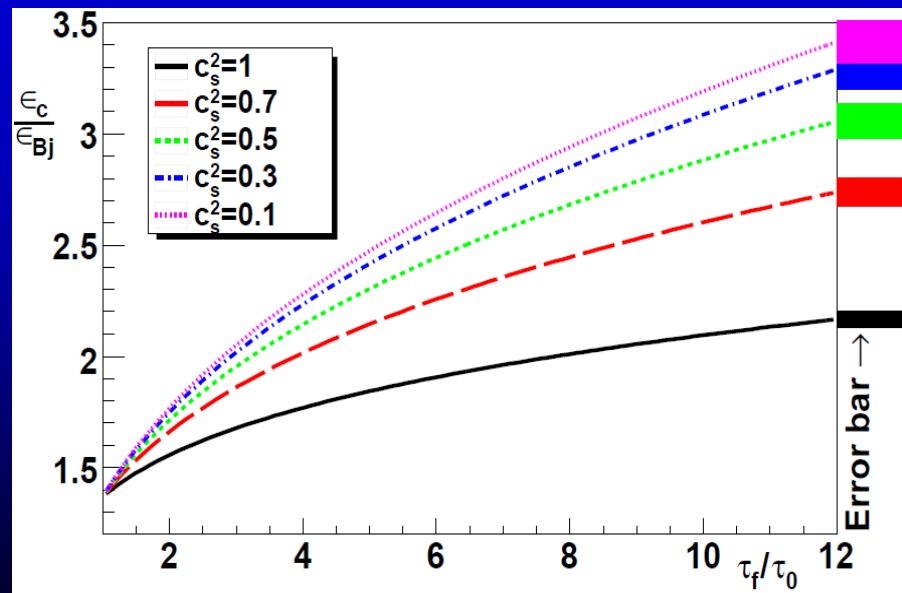
J.Phys.G35 (2008) 104128 (arXiv:0805.1562)

$$\mathcal{E} = \mathcal{E}_{Bj} (2\lambda - 1) \left(\frac{\tau_f}{\tau_i} \right)^{(\lambda-1)(2-c_{\text{sound}}^2)}$$

Corresponds to $T_{\text{ini}} \cong 2T_c \cong 340$ MeV

Consistent with PHENIX direct photon spectra

<http://arxiv.org/abs/arXiv:0804.4168> PRL 104:132301, 2010



Initial energy density for pp@7 TeV

Bjorken estimate:

Number of particles at midrapidity: ~ 7 (measured)

Average energy: $\langle m_t \rangle \sim 0.5$ GeV (measured)

Initial radius of the system R : ~ 1 fm ($R^2\pi = \sigma_{inel}/2$, or HBT)

Formation time τ_0 : 1 fm/c

Energy density from this:

$$\varepsilon_{Bj} = \frac{1}{R^2\pi\tau_0} \frac{dE}{d\eta} = \frac{\langle E \rangle}{R^2\pi\tau_0} \frac{dn}{d\eta} = \frac{0.5 \times 7 \text{ GeV} / c}{3.67 \text{ fm}^3 / c} \approx 0.95 \text{ GeV} / \text{fm}^3$$

Just below critical??

Correction may be important ...

Missed opportunity?

Energy density from TOTEM $dn/d\eta$

	TOTEM data		CMS data		Joint data	
Norm	10,51	$\pm 0,04$	7,39	$\pm 0,03$	7,48	$\pm 0,01$
T_f	0,12	fixed	0,122	$\pm 0,002$	0,117	$\pm 0,001$
Λ	1,073	$\pm 0,003$	1,061	$\pm 0,002$	1,0535	$\pm 0,0002$
χ^2/N_{DF}	2068/32		82,7/6		8502/42	

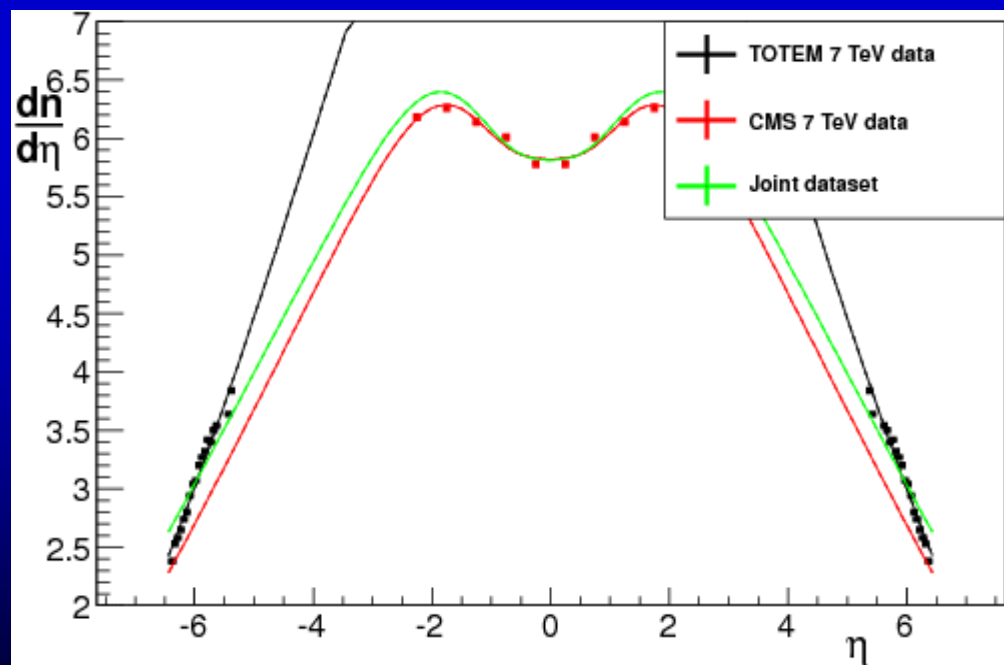
Errors of 0.1% (?)

Normalization (?)

NSD events in CMS

$\lambda \sim 1.05-1.1$

χ^2 too big (joint fit...)



Initial energy density in 7 TeV p+p?

Rough result: $\lambda \simeq 1.05-1.07$

$\sim 25\%$ correction

Input parameters:

$dn/dy: \sim 7$

Mean E: ~ 0.5 GeV

Radius: ~ 1 fm

Form. time: ~ 1 fm/c

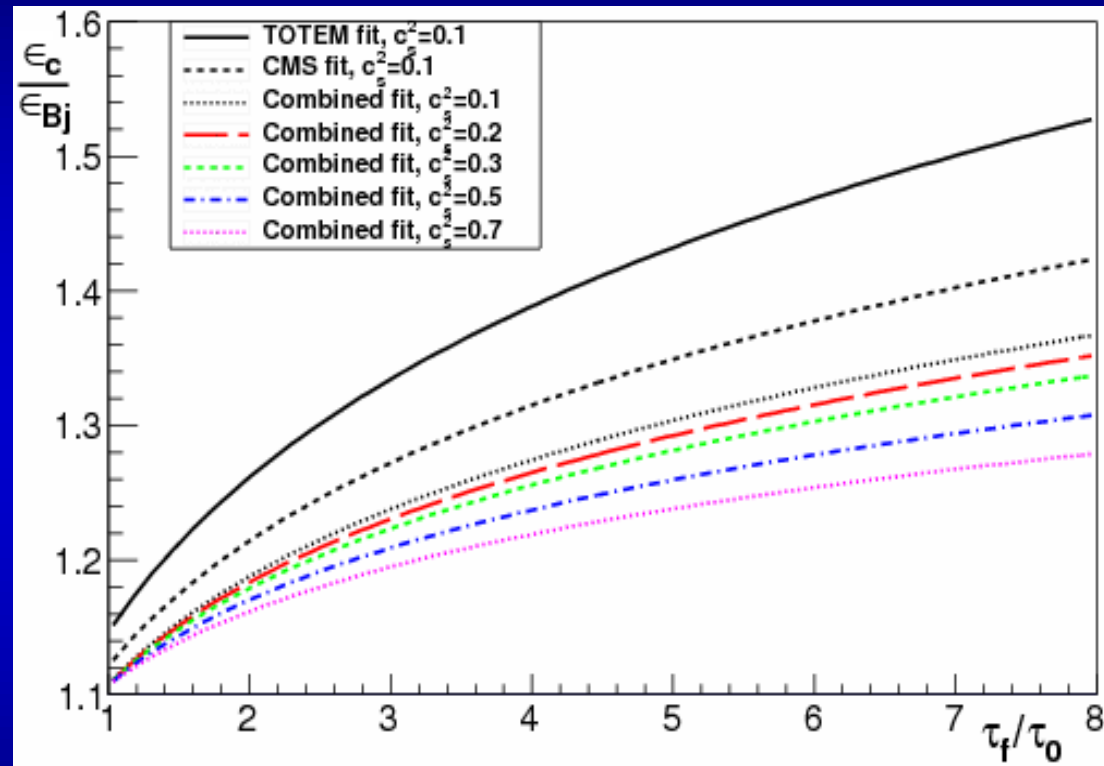
Corrected result:

~ 1.2 GeV/fm³

→

Initial ε just above the critical value of 1 GeV!

Small correction, but big difference in physics ...



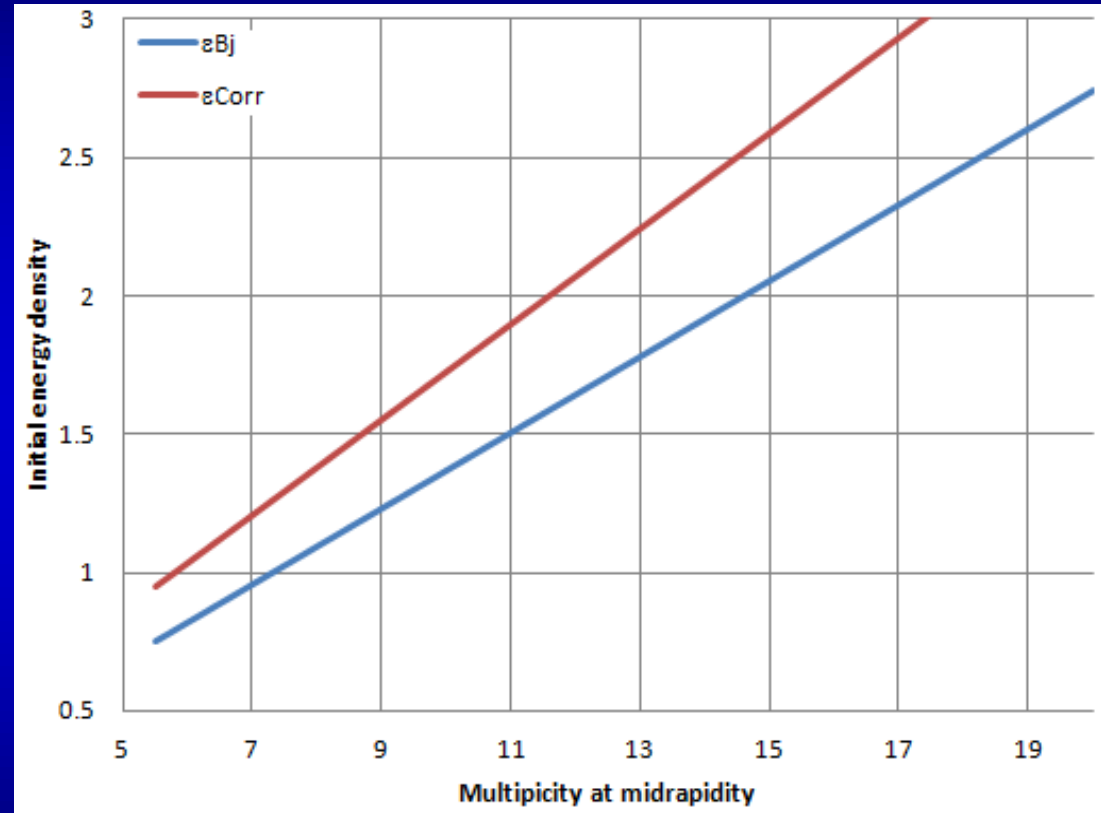
Dependence on particle number

Several multiplicity classes can be defined

CMS: $\langle n \rangle \sim 6-20$

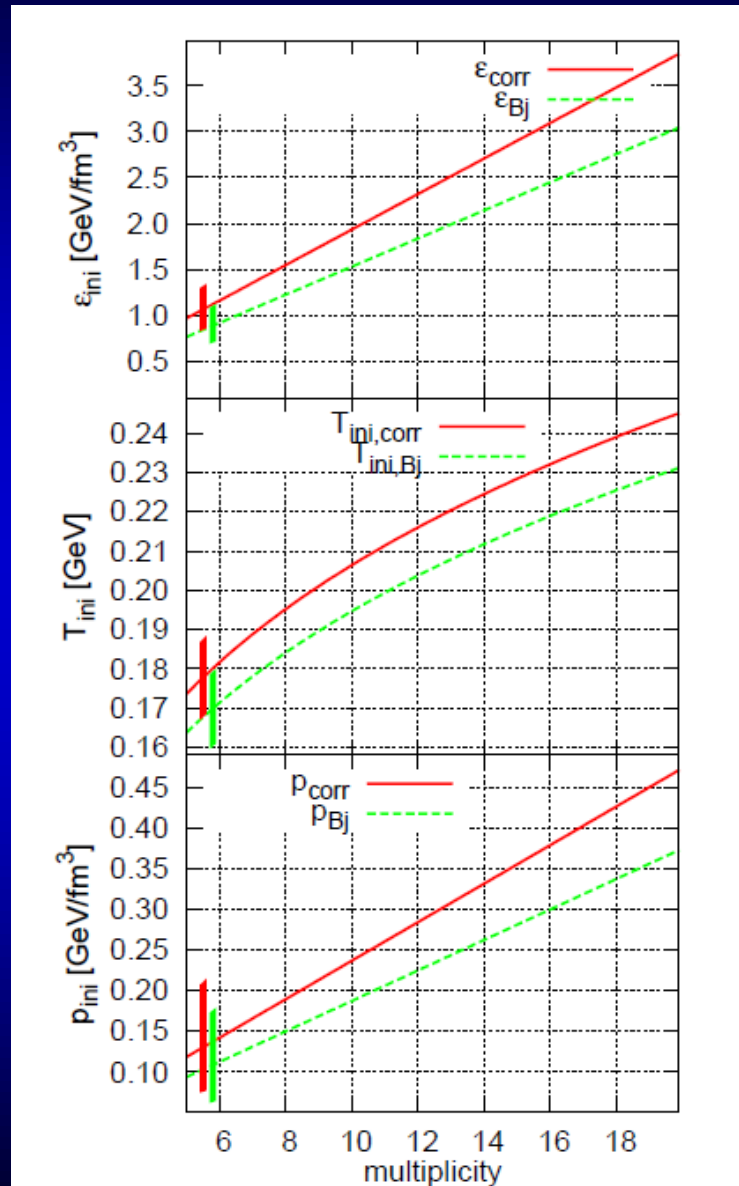
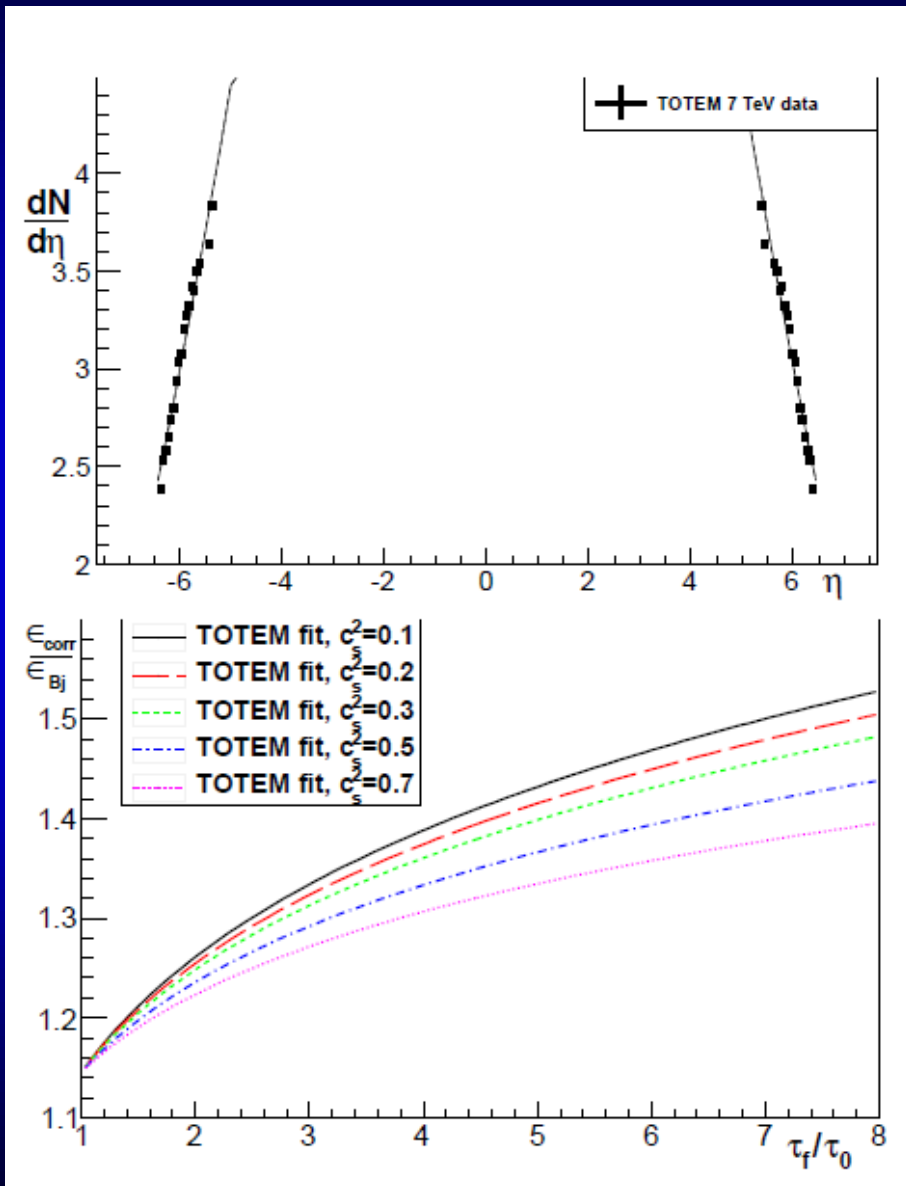
Bjorken result:
above critical
IF $\langle n \rangle \geq 7.5$

Corrected estimate:
above critical
for ANY $\langle n \rangle$

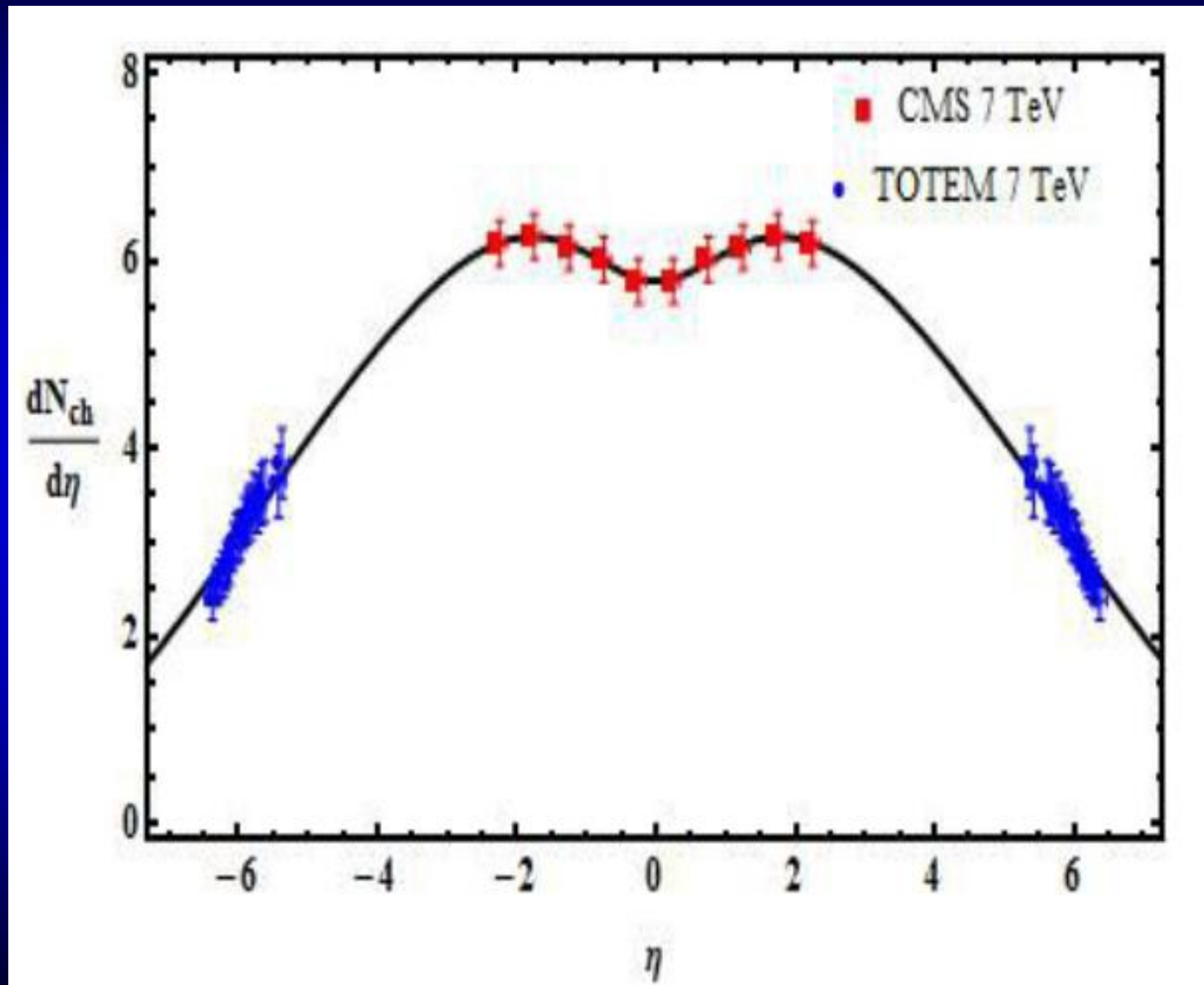


**QGP is formed in \sim ALL
p+p collisions at LHC @ 7 TeV**

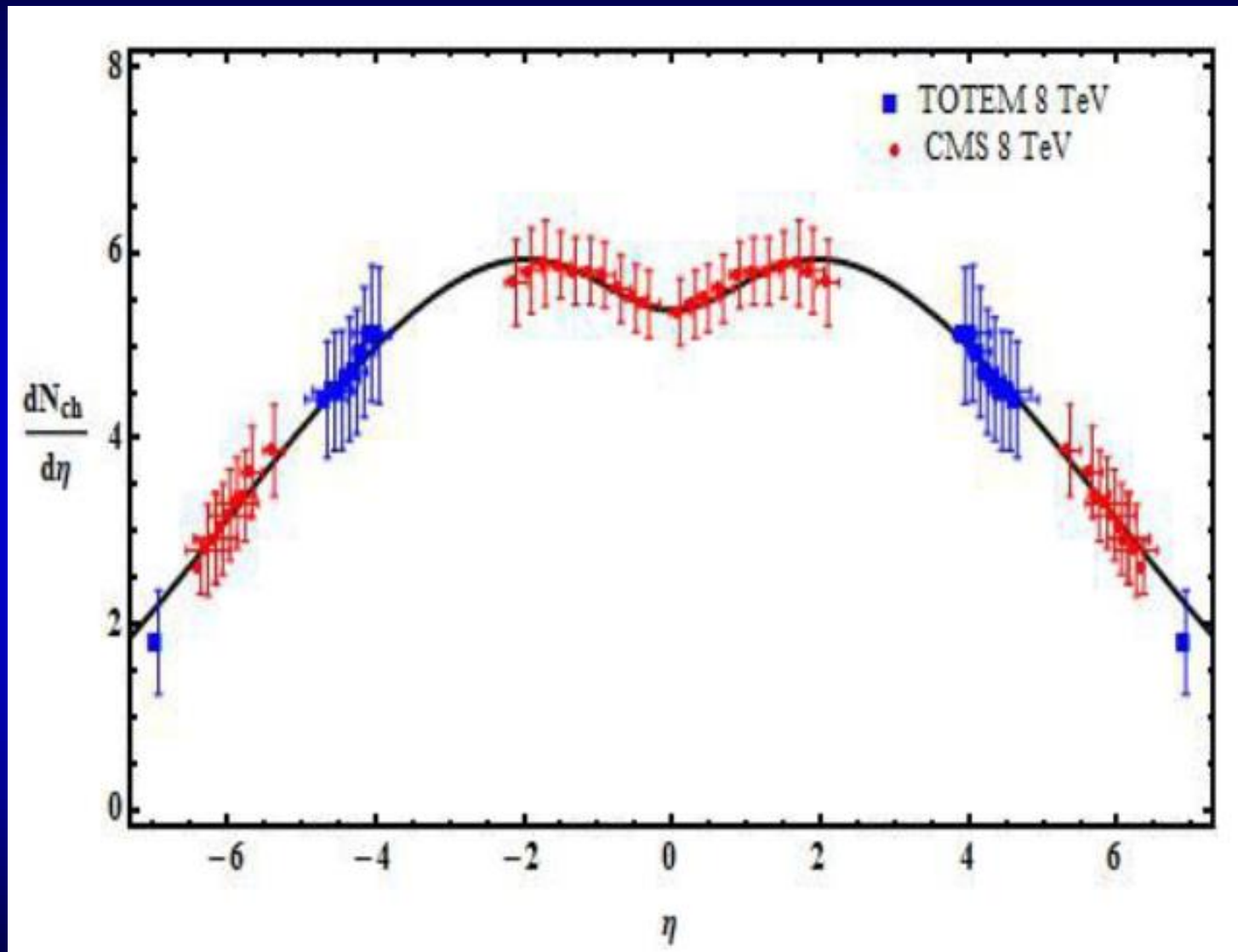
Results for TOTEM $dn/d\eta$ data@7 TeV



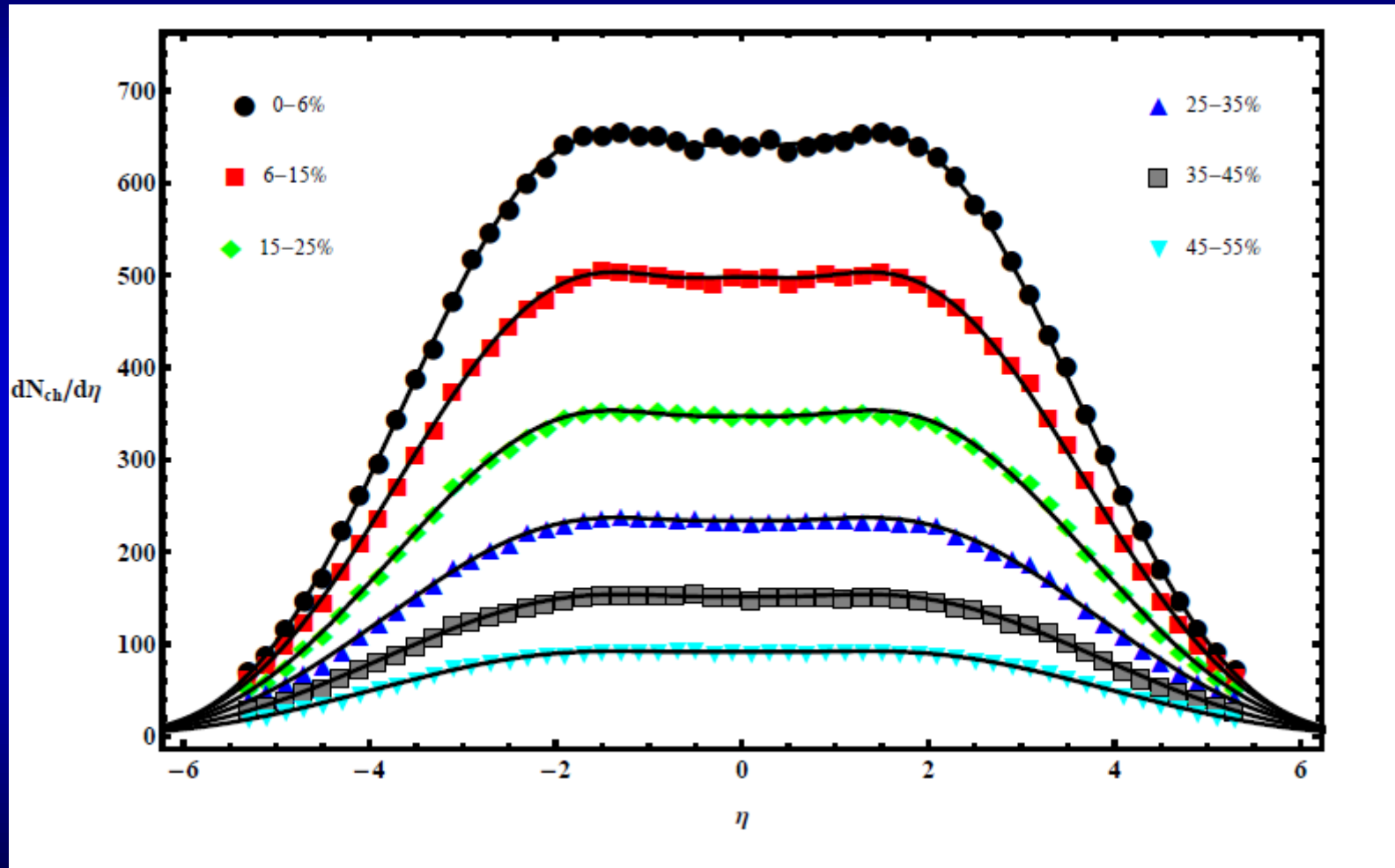
Results for CMS+TOTEM dn/dη data@7 TeV



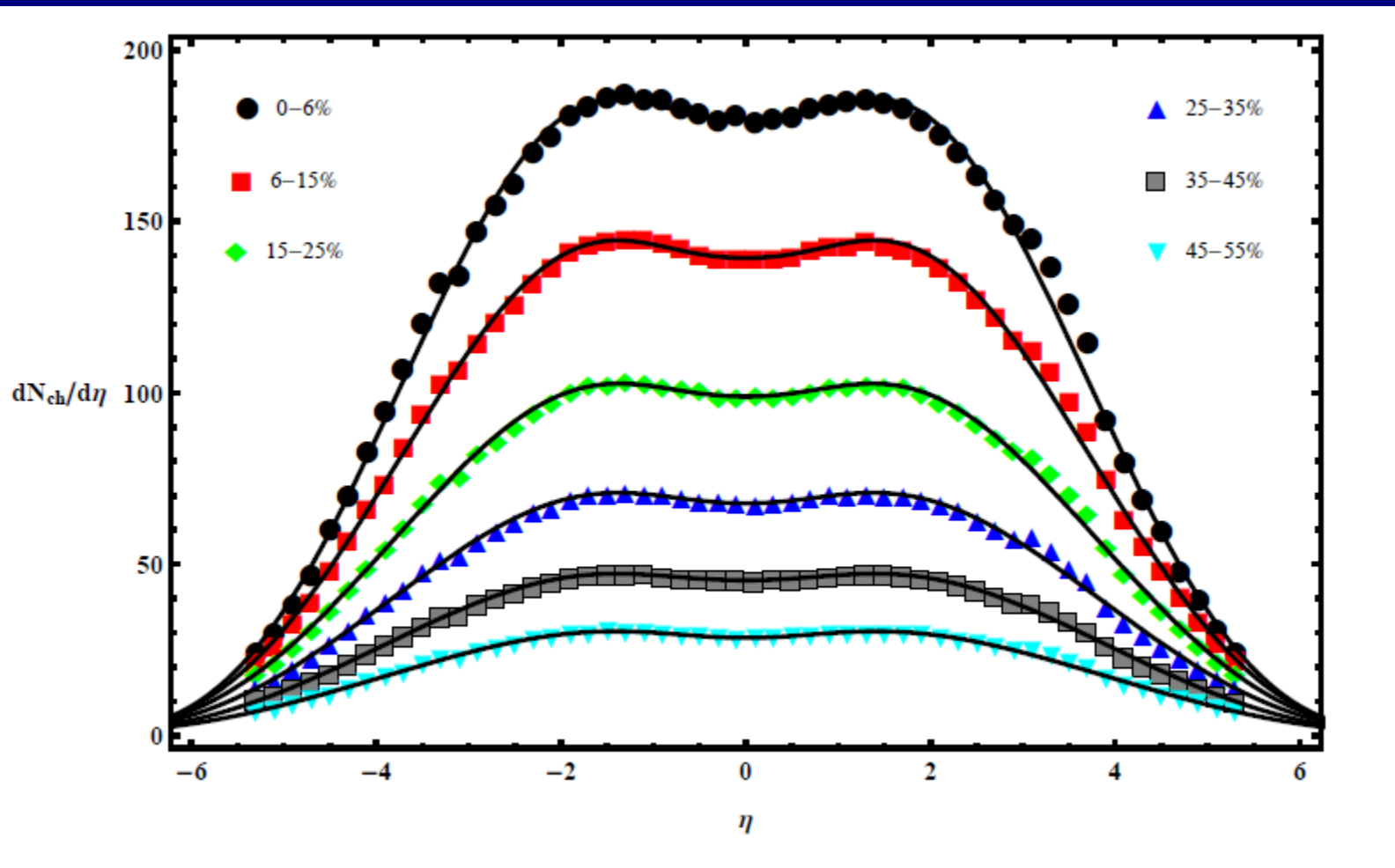
Results for CMS+TOTEM dn/dη data@8 TeV



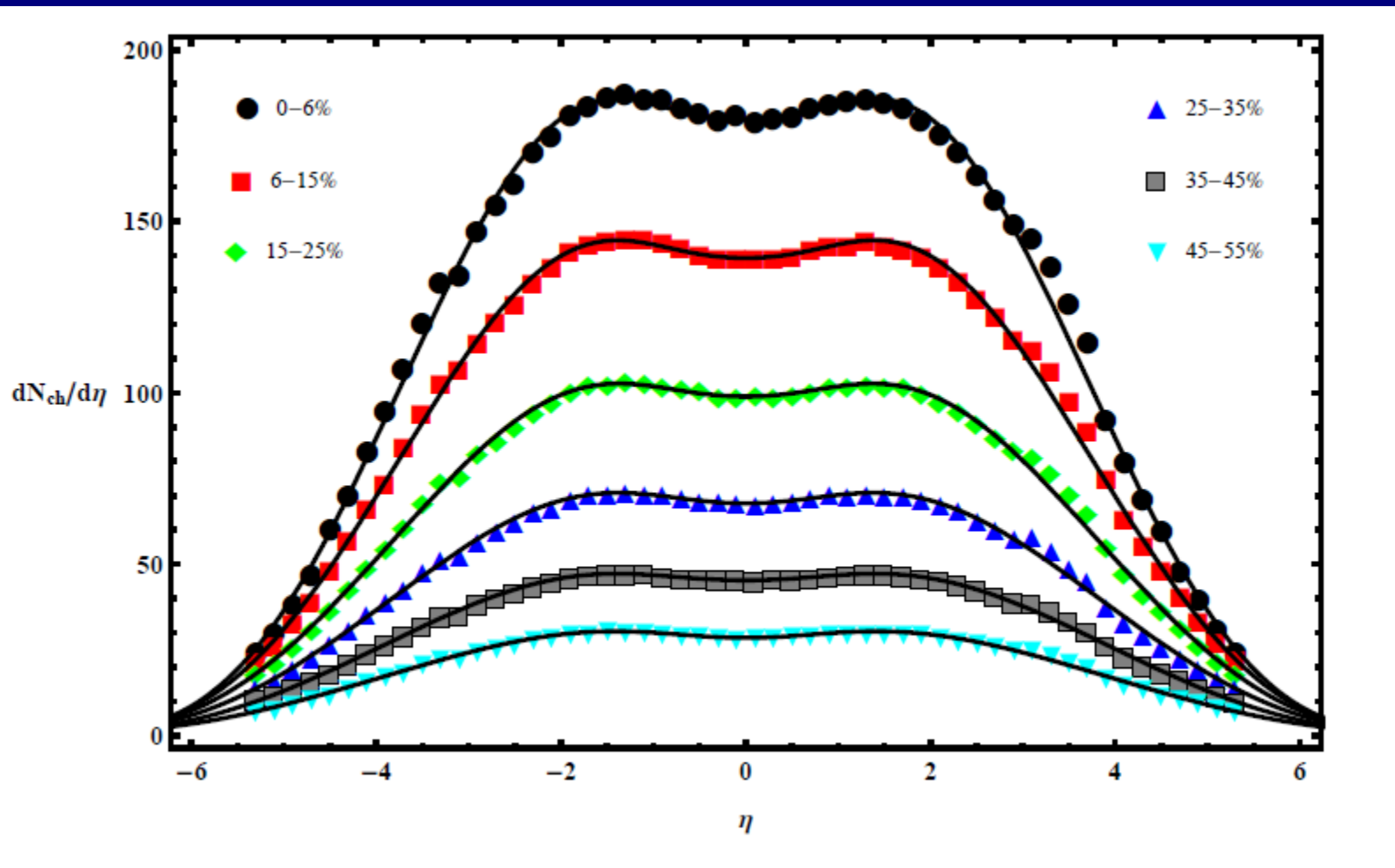
Cross-check: Au+Au at 200 GeV, PHOBOS data from RHIC



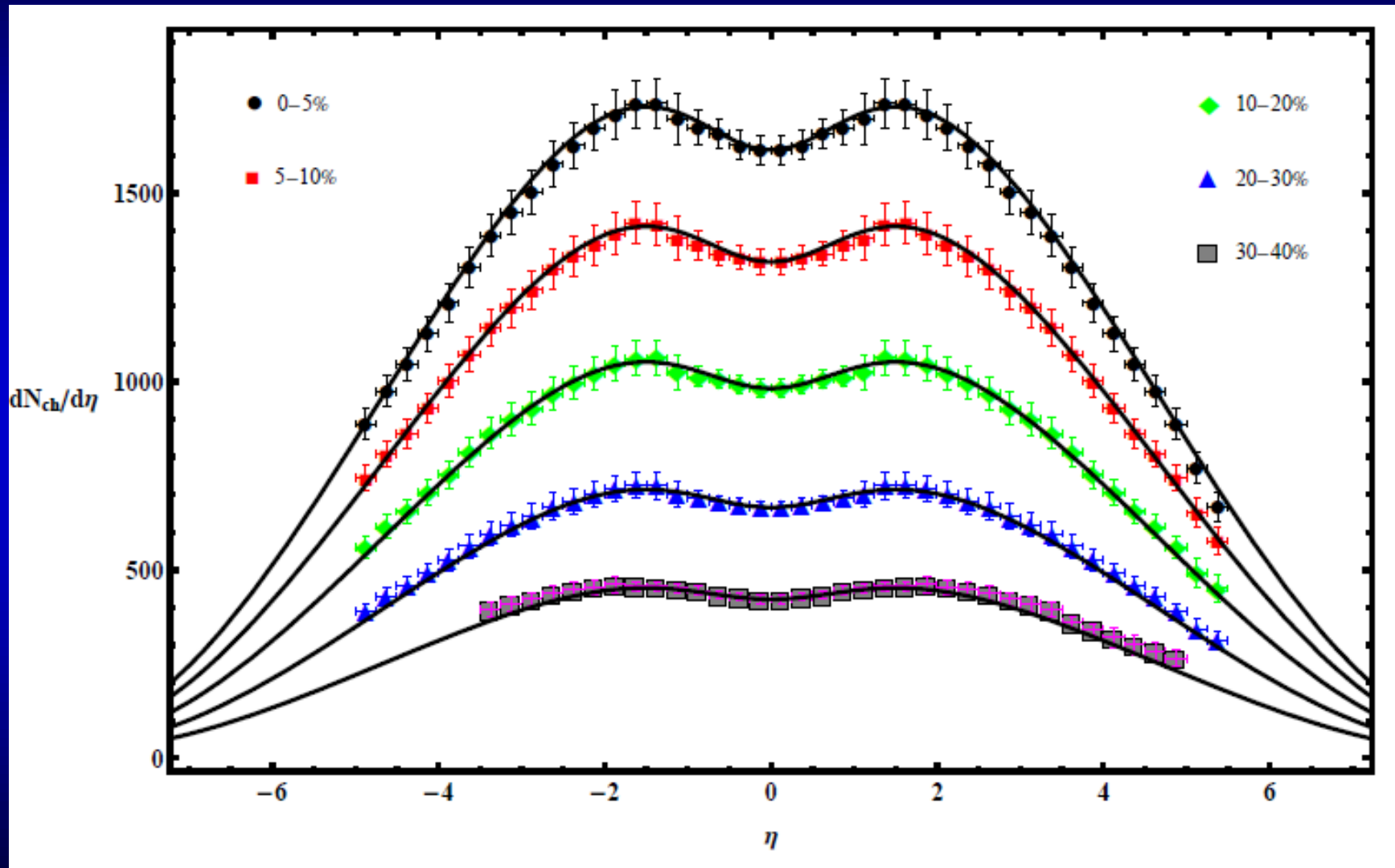
Cross-check: Cu+Cu at 200 GeV, PHOBOS data from RHIC



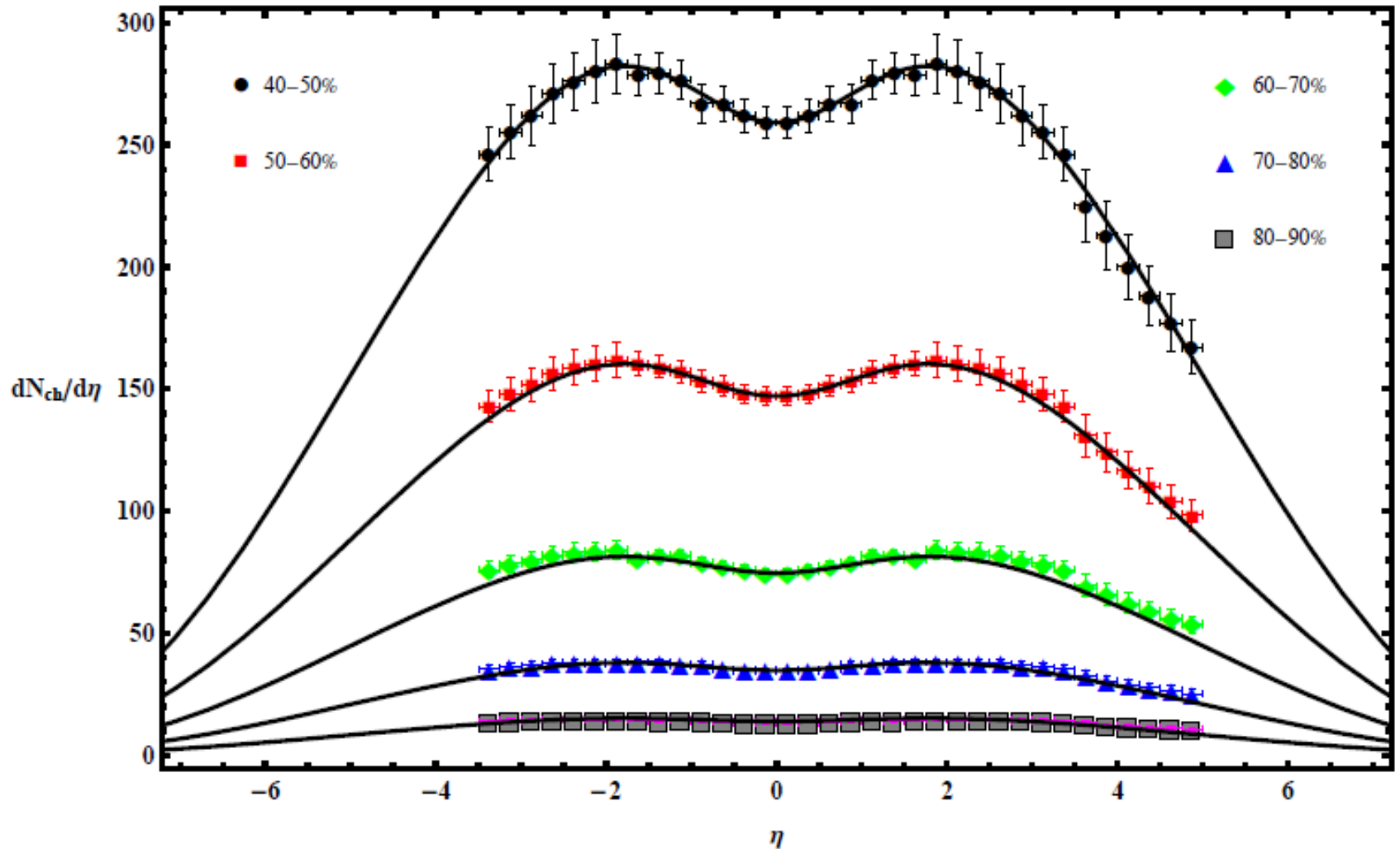
Cross-check: Cu+Cu at 200 GeV, PHOBOS data from RHIC



Heavy Ions at LHC: Pb+Pb at 2.76 TeV, ALICE data



Heavy Ions at LHC: Pb+Pb at 2.76 TeV, ALICE data, peripheral collisions



Summary

**Experimentally widely used Bjorken est. (1800+)
QGP critical energy density: 1 GeV/fm³**

**Advanced estimate from forward dn/dη
Results on the initial ε for c_s²=0.1, at τ_f/τ_{ini}=2**

	Bjorken	TOTEM fit	CMS fit	Combined fit
ε _{ini}	0.95 GeV/fm ³	1.20 GeV/fm ³	1.15 GeV/fm ³	1.13 GeV/fm ³

Small correction but important implications

- pp is not a good reference
- R_{AA} not such a good concept, need:
R_{AA} per unit length ≡ optical opacity,

[arXiv:0911.5015](https://arxiv.org/abs/0911.5015)

Implications

pp, pA, dA, AA are similar
But differ in sizes (multiplicity)

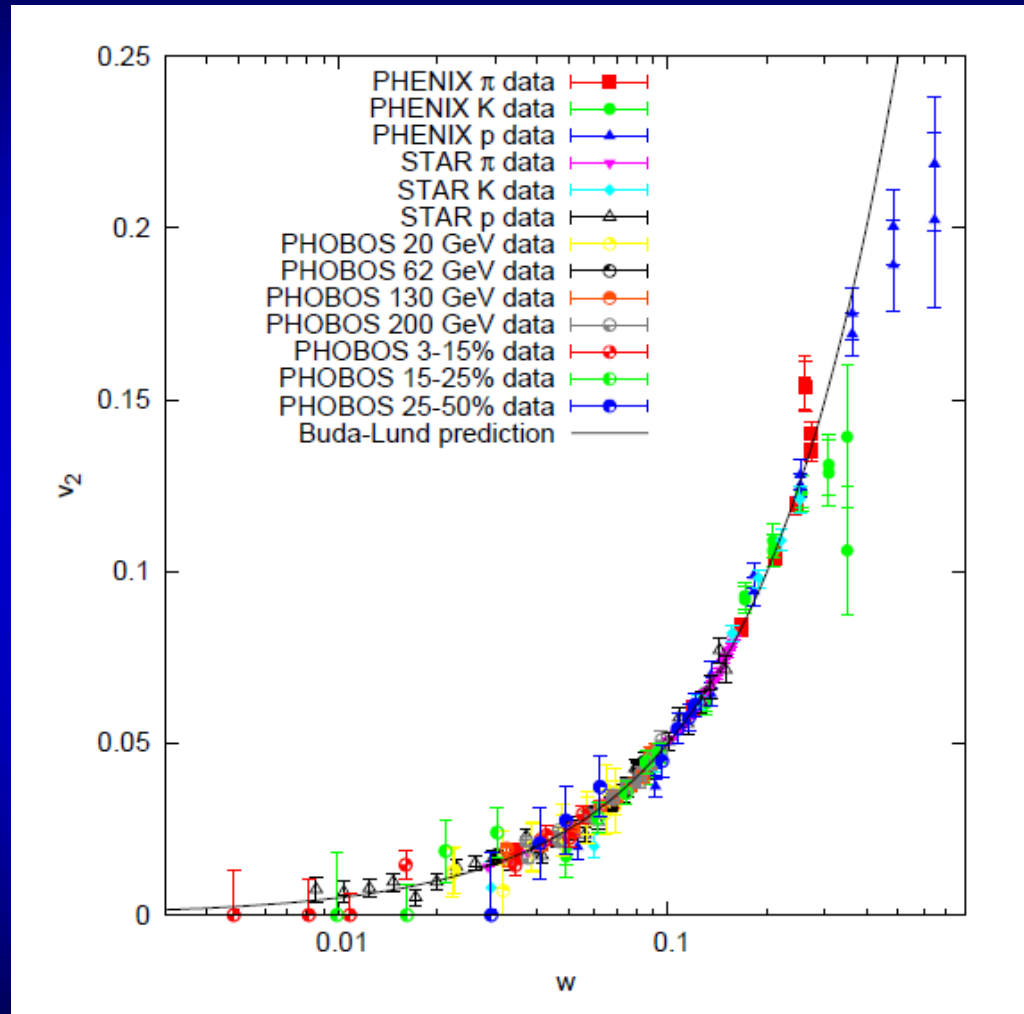
Need for an electron-proton and eA collider
to determine a clear reference

Prediction:
Scaling laws for spectra,
elliptic flows
and HBT radii in pp@ LHC

New result:
Initial energy density is
Larger than 1 GeV/fm³ in pp@LHC

Quark Matter even in pp@LHC

Prediction: UNIVERSAL hydro scaling of v_2 will hold for pp@LHC



[nucl-th/0512078](https://arxiv.org/abs/nucl-th/0512078) but new: v_2/n_q vs K_{ET}/n_q will be violated in p+p@LHC