



# Jet Measurements from CMS

Engin Eren (DESY)

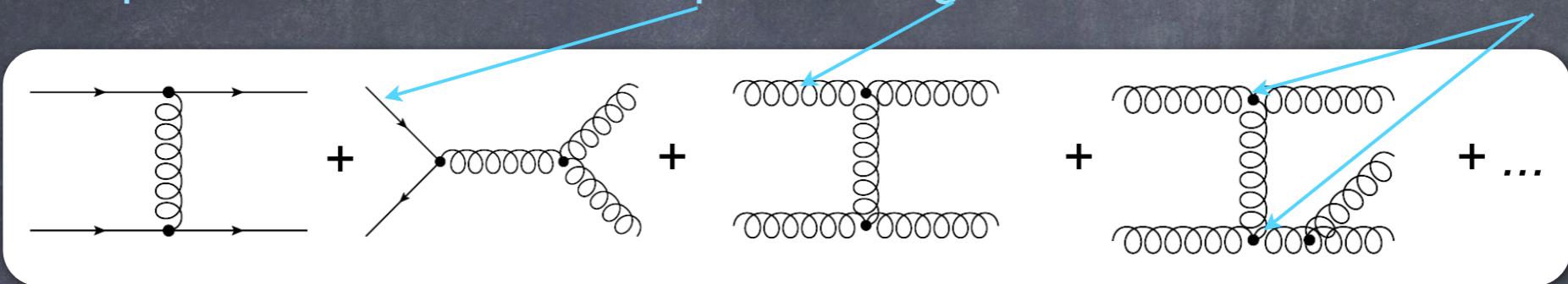
*Low-x meeting, 10.06.2016  
Gyöngyös, Hungary*

# Outline

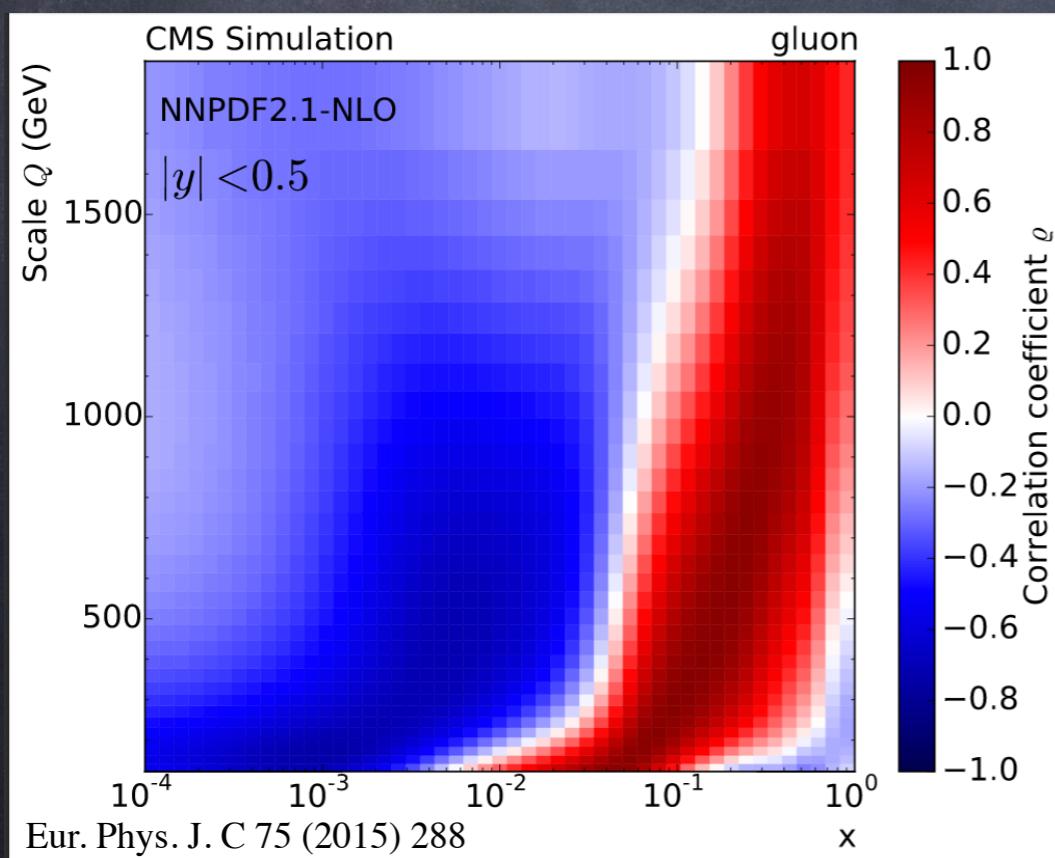
- Measurement of inclusive jet cross-section @2.76TeV
- Measurement of inclusive jet cross-section @8TeV
- Ratio of 2.76 TeV and 8 TeV cross-sections
- QCD analysis with inclusive jet cross-section @8TeV
  - ✓ Determination of strong coupling  $\alpha_S$
  - ✓ PDF parametrisation and sensitivity
  - ✓ Constraints on gluon PDF
- Measurement of inclusive jet cross-section @13TeV

# Probing QCD with Jet Cross Sections

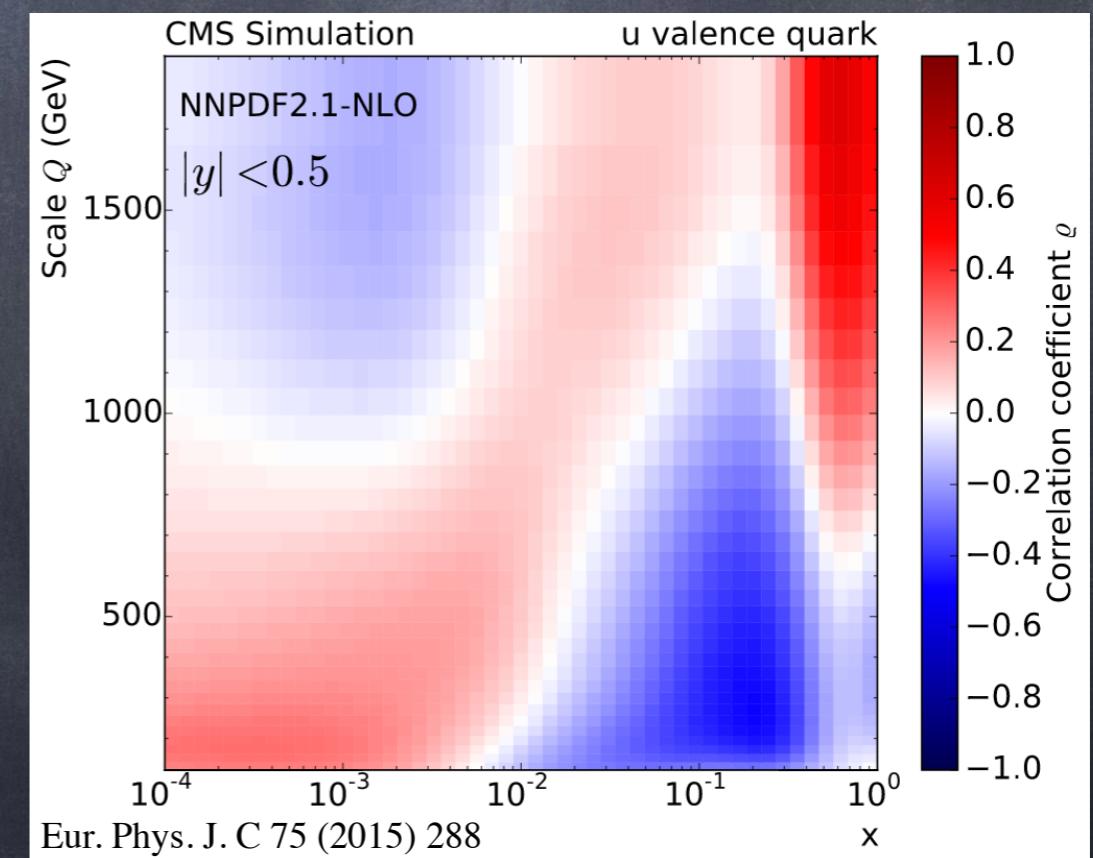
- Jet production sensitive to quark and gluon distributions, and to  $\alpha_s$



**Strong correlation between inclusive jet cross section and gluon at high-middle x**

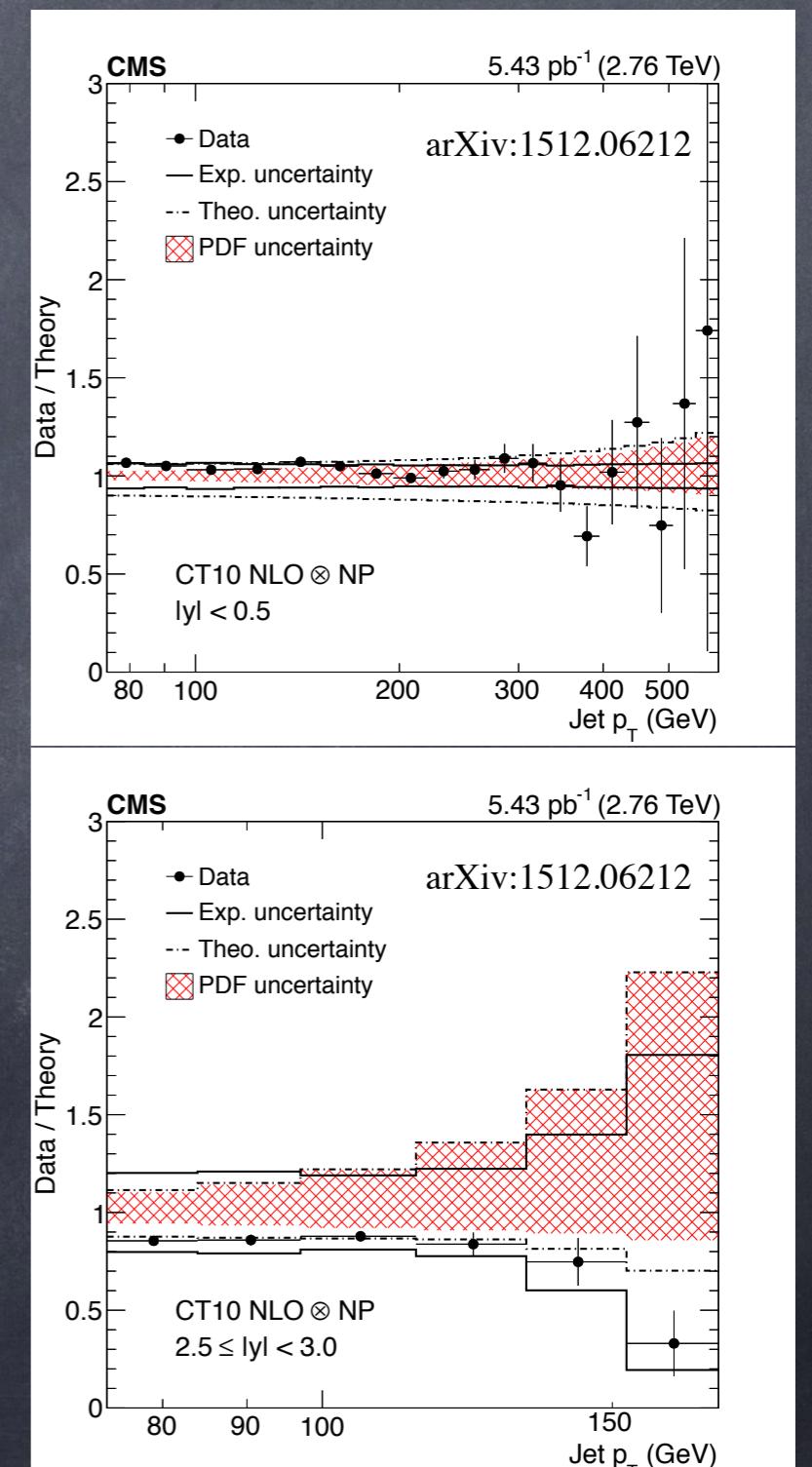
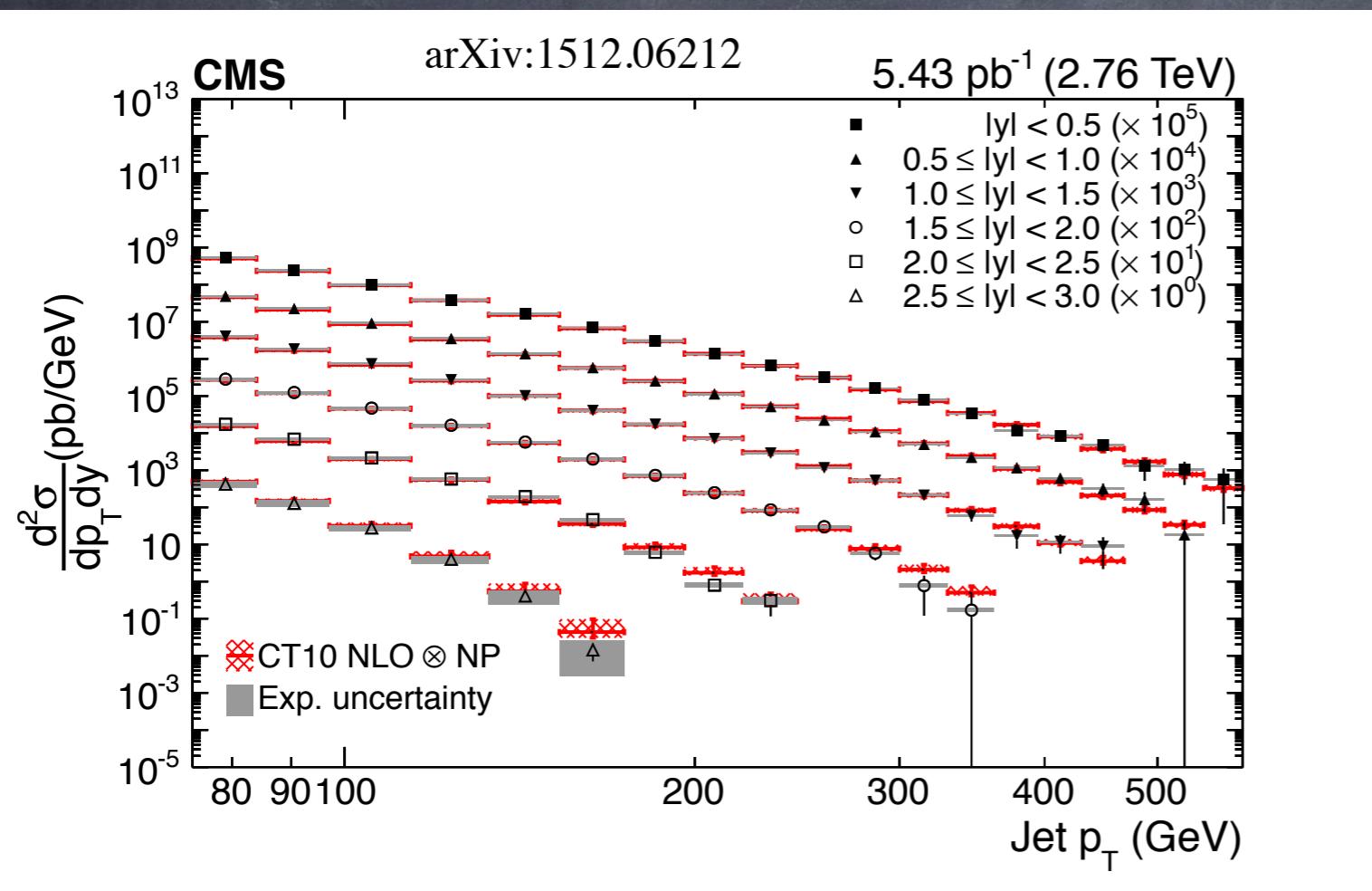


**Strong correlation between inclusive jet cross section and quark at high x**



# Inclusive Jet Cross Section at 2.76TeV

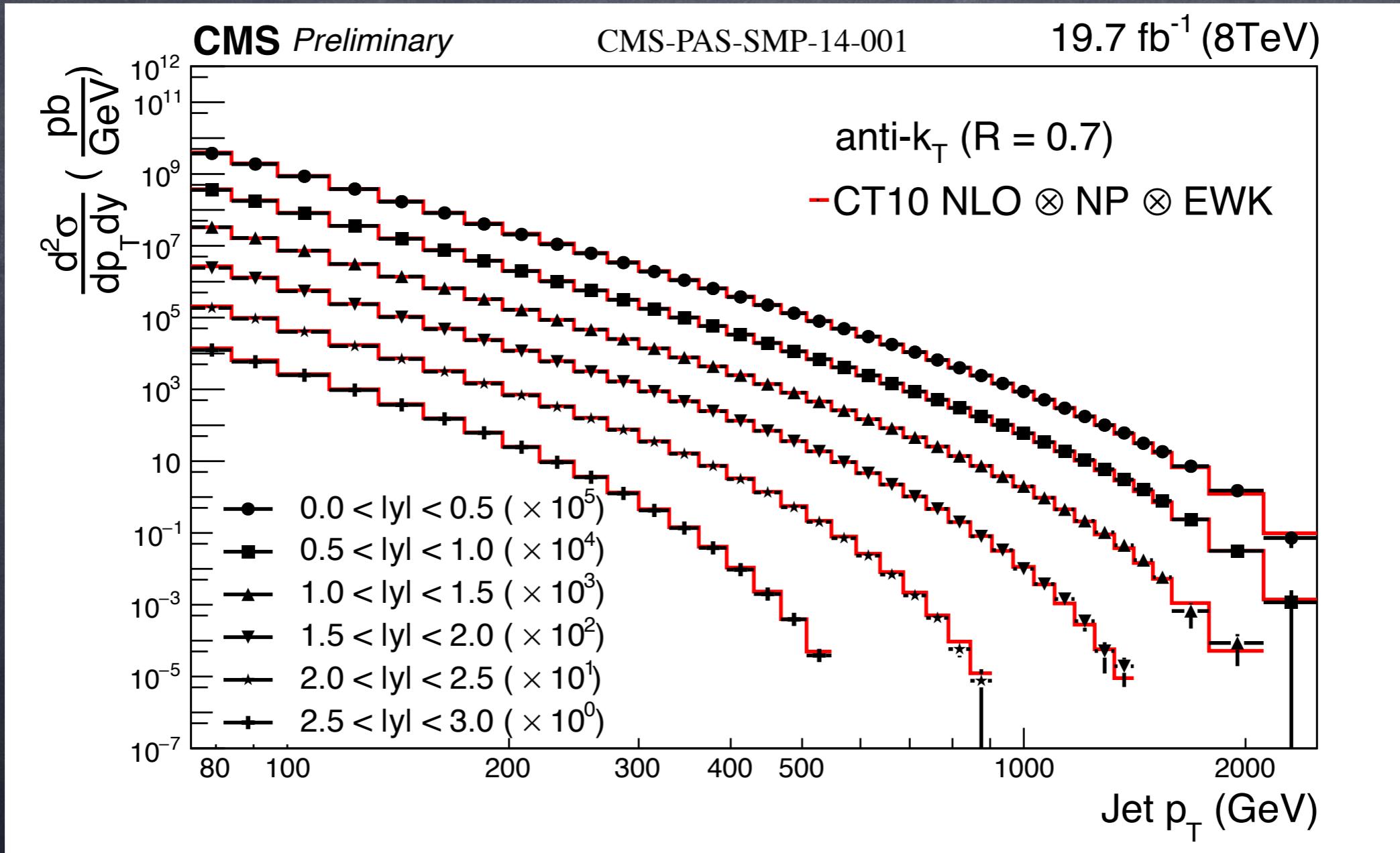
Measurement at  $\sqrt{s}=2.76$  TeV ( $L = 5.43 \text{ pb}^{-1}$ )  
 Anti- $k_T$ ,  $R=0.7$ ; double-differential cross sections as functions of  $p_T$  and  $y$ .



Transverse momenta range from  
 74 GeV to 592 GeV. Good  
 description by **NLO QCD**

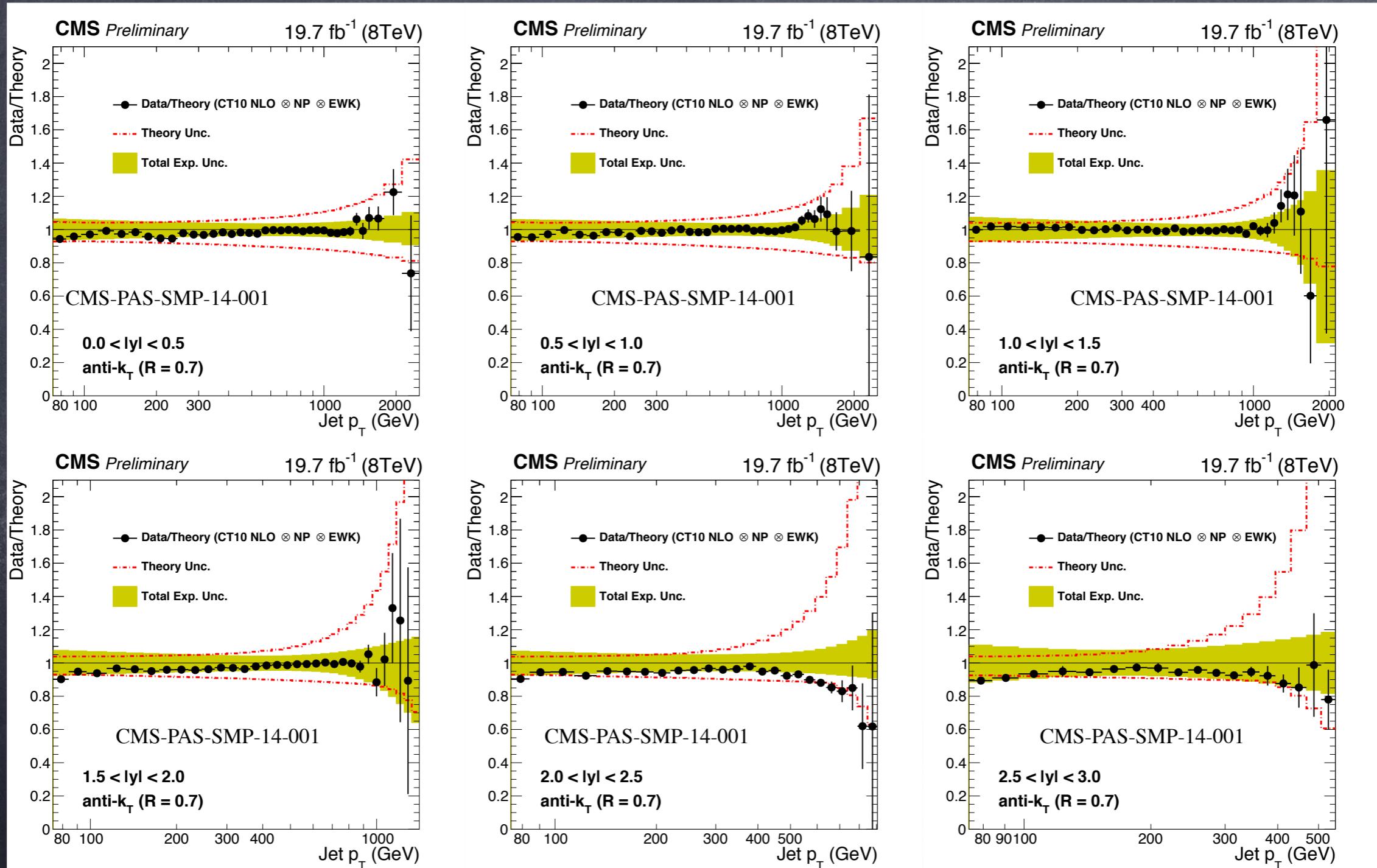
# Inclusive Jet Cross Section at 8TeV

Measurement at  $\sqrt{s}=8$  TeV ( $L = 19.7 \text{ fb}^{-1}$ )  
Anti- $k_T$ ,  $R=0.7$ ; double-differential cross sections as functions of  $p_T$  and  $y$ .



# Inclusive Jet Cross Section at 8TeV

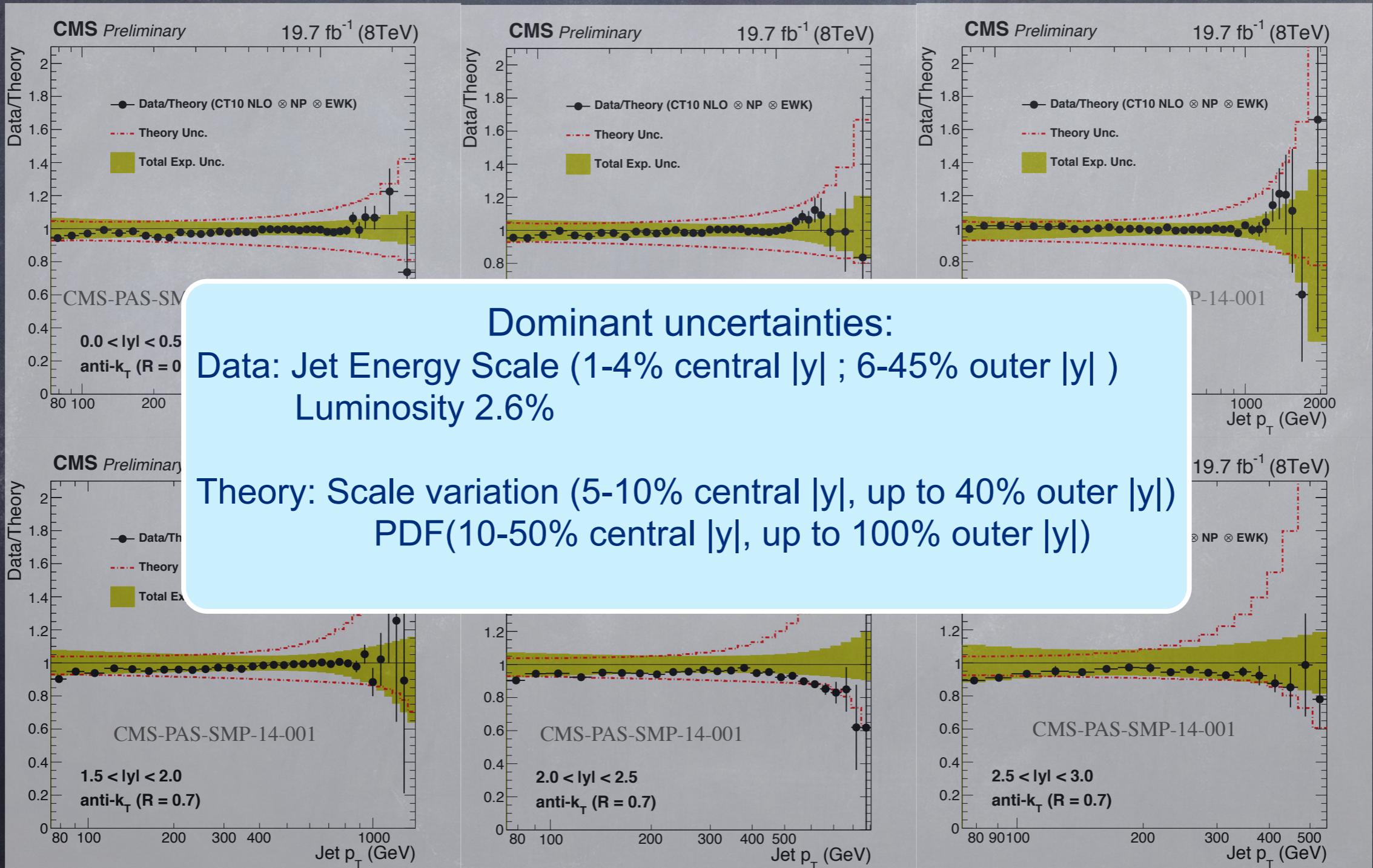
Data/Theory comparisons for 6 rapidity bins :



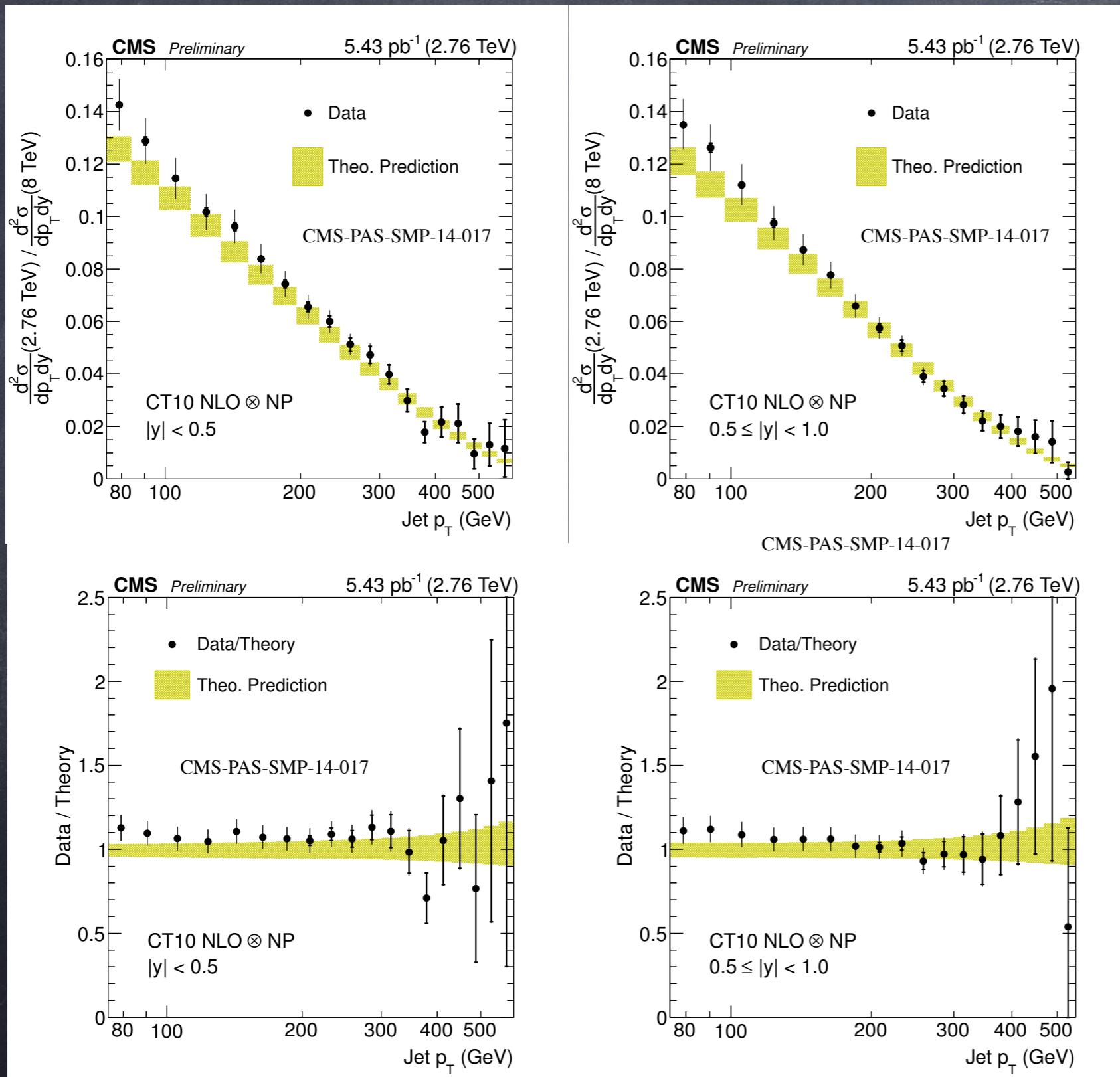
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# Inclusive Jet Cross Section at 8TeV

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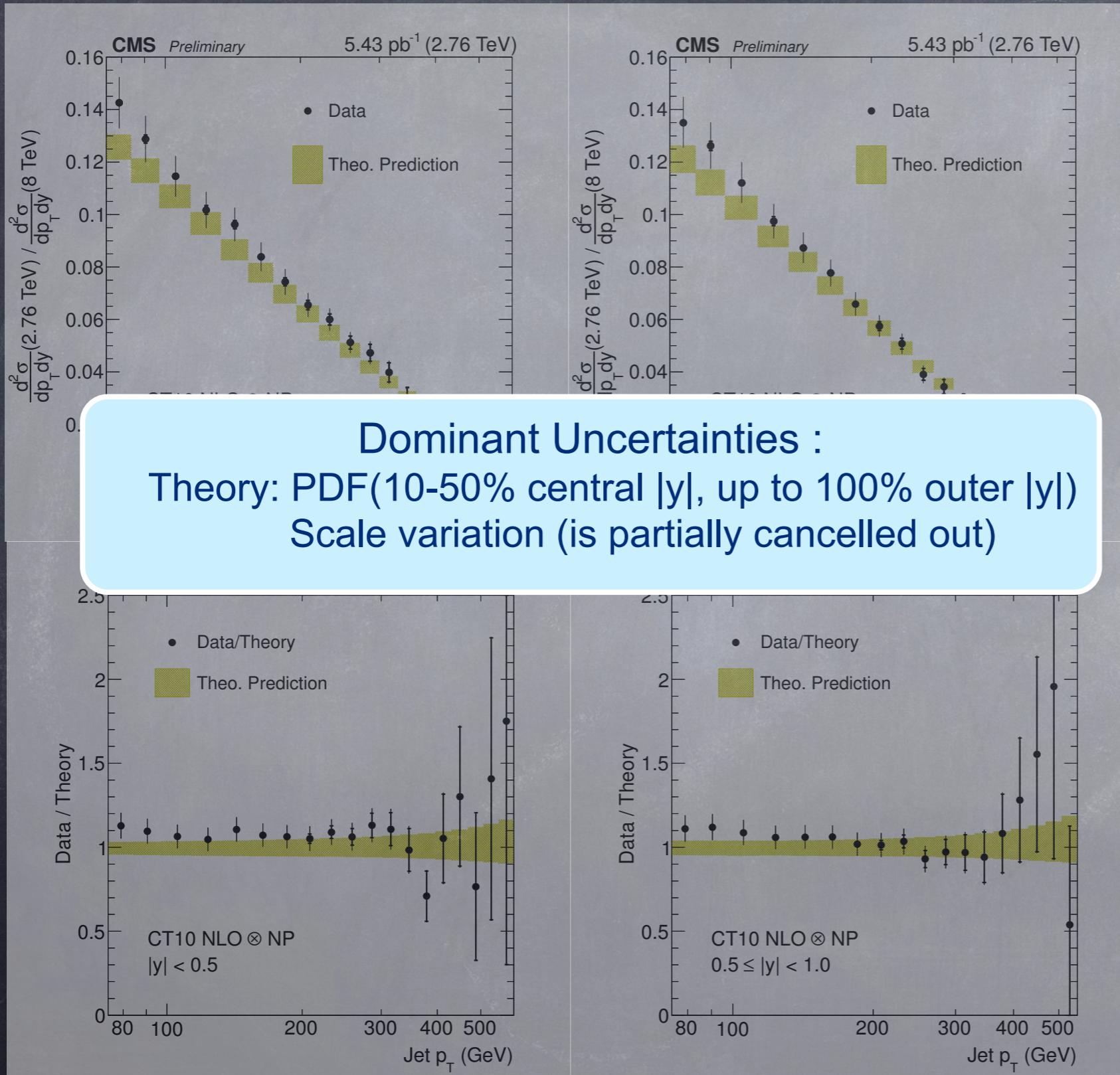
# Inclusive Jet Cross Section Ratio 2.76 / 8TeV



- Careful study of the uncertainty between 8 and 2.76 TeV is performed.
- Partial cancellation of systematic uncertainties!
- This measurement can be used to constrain Pdfs.

$$\rho = \frac{\sigma_{\text{Data}}^{2.76 \text{ TeV}} / \sigma_{\text{Theory}}^{2.76 \text{ TeV}}}{\sigma_{\text{Data}}^{8 \text{ TeV}} / \sigma_{\text{Theory}}^{8 \text{ TeV}}}$$

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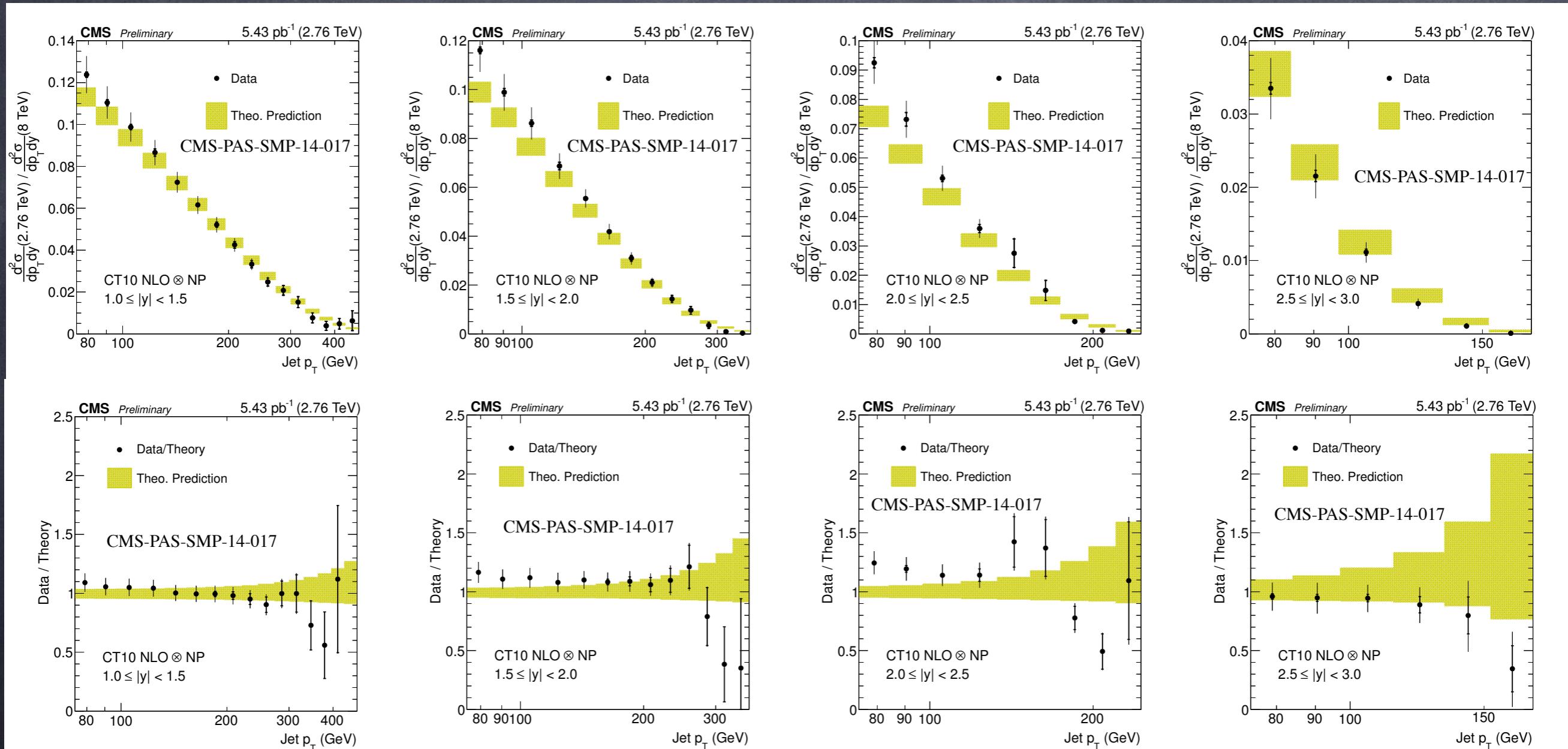


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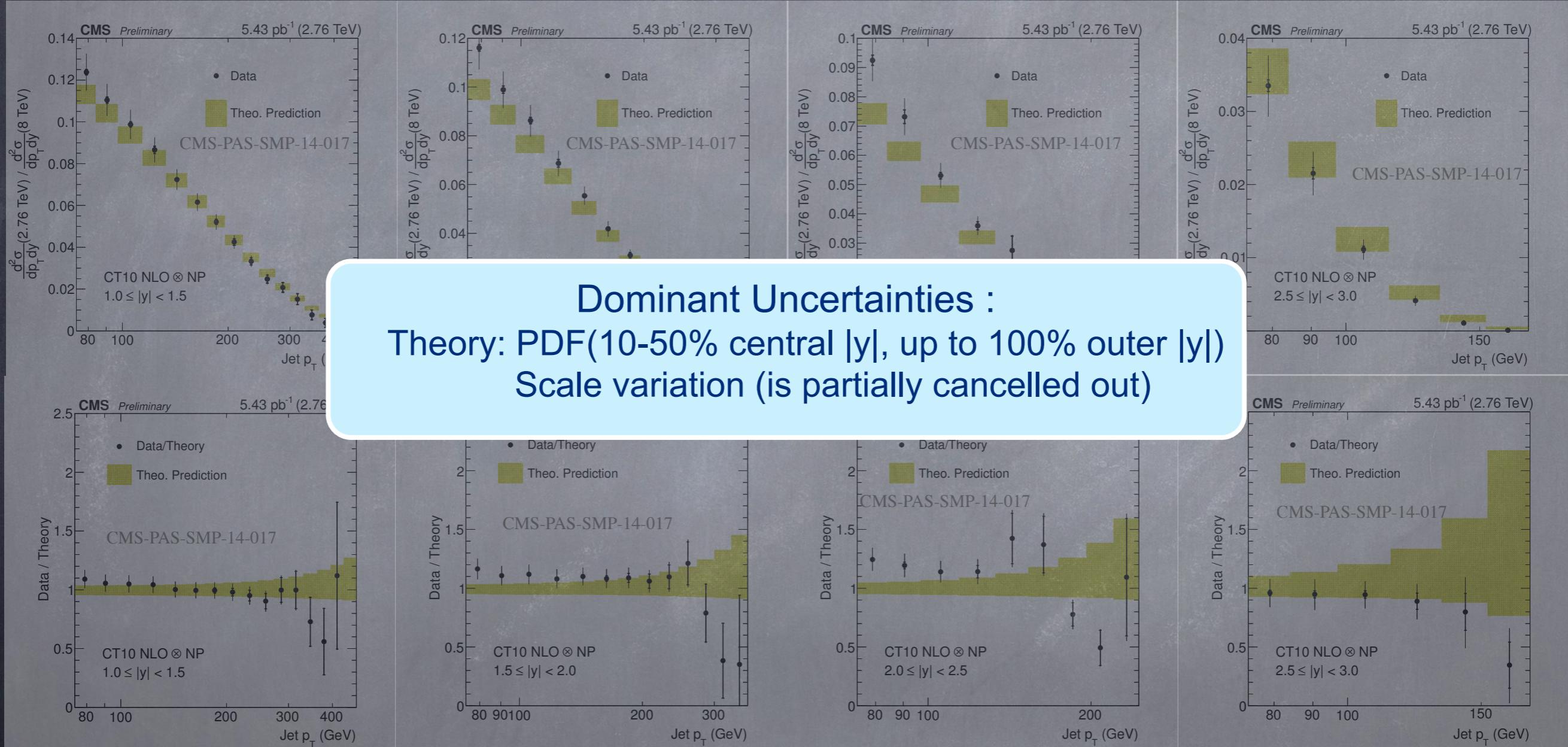
# Inclusive Jet Cross Section Ratio 2.76 / 8TeV

Other rapidity bins :

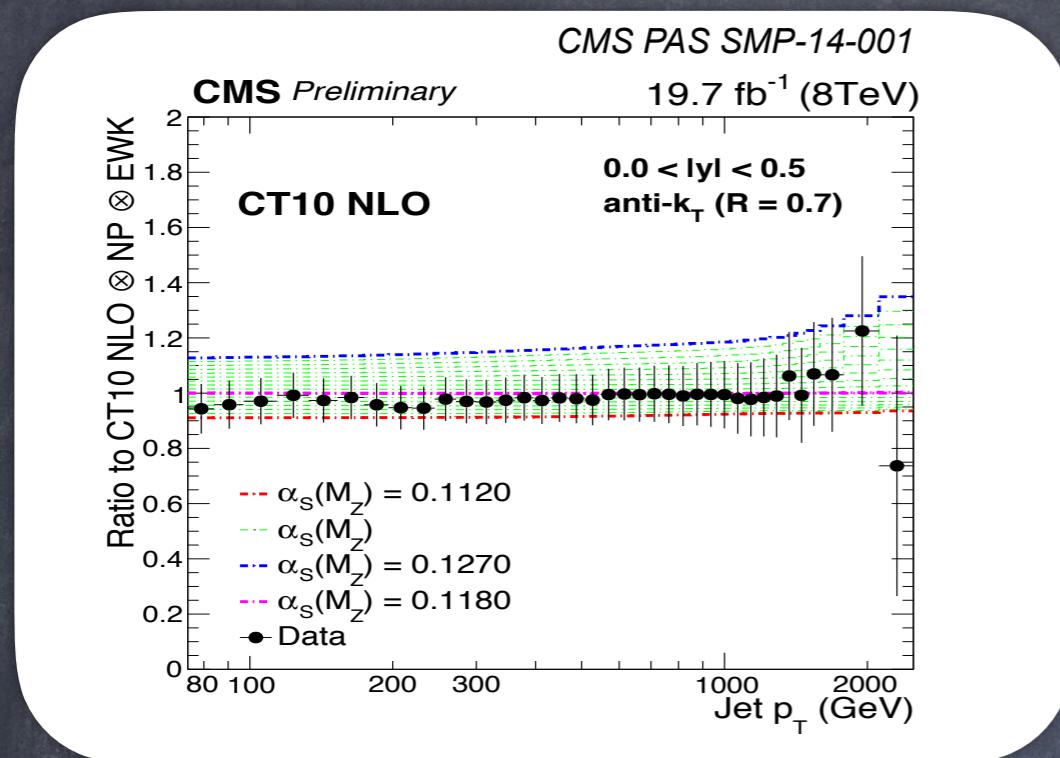


# Inclusive Jet Cross Section Ratio 2.76 / 8TeV

Other rapidity bins :



# Determination of strong coupling $\alpha_s$ : inclusive jets @ 8TeV



CMS jet cross section measurement  
 $\sqrt{s}=8\text{TeV}$  ( $19.7 \text{ fb}^{-1}$ ) CMS-PAS-SMP-14-001

compared to NLO QCD  $\otimes$  PDFs  
in each bin of  $p_T$  and  $y$   
different sets of PDFs used  
each set has its  $\alpha_s$  - dependence

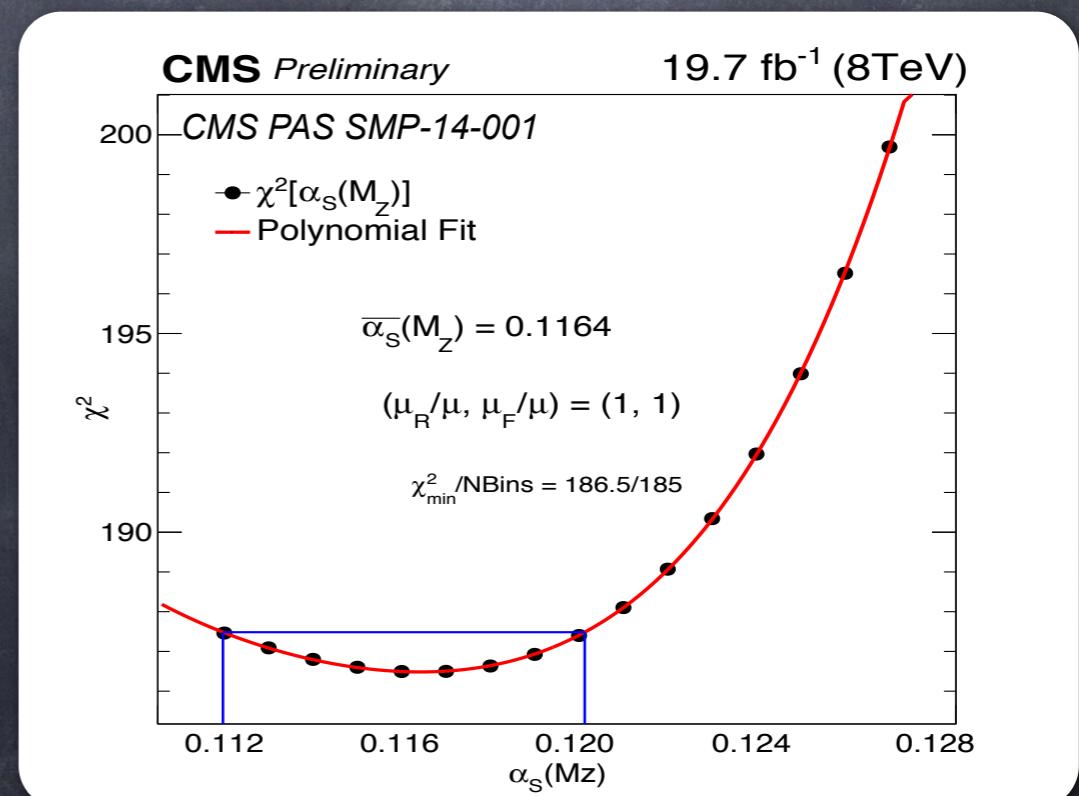
In each  $y$  bin, for each PDF,  $\alpha_s$  is determined by minimizing  $\chi^2$  between data and NLO

Similar results obtained with different PDFs

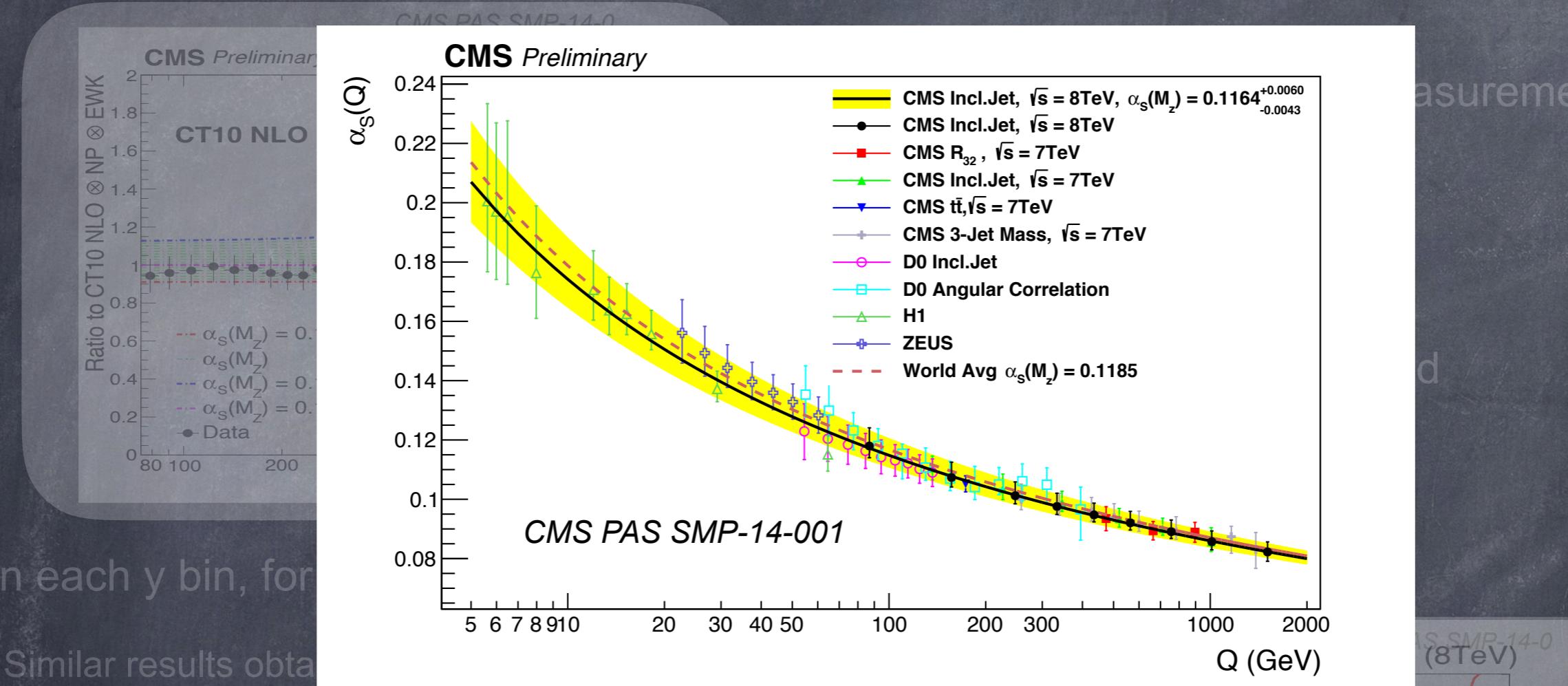
Using CT10NLO :

$$\alpha_s(M_Z) = 0.1164^{+0.0025}_{-0.0029} (\text{PDF})^{+0.0053}_{-0.0028} (\text{Scale}) \\ \pm 0.0001 (\text{NP})^{+0.0014}_{-0.0015} (\text{Exp})$$

Analysis performed in 9  $p_T$  bins  
 $\Rightarrow$  running of  $\alpha_s = \alpha_s(Q^2)$



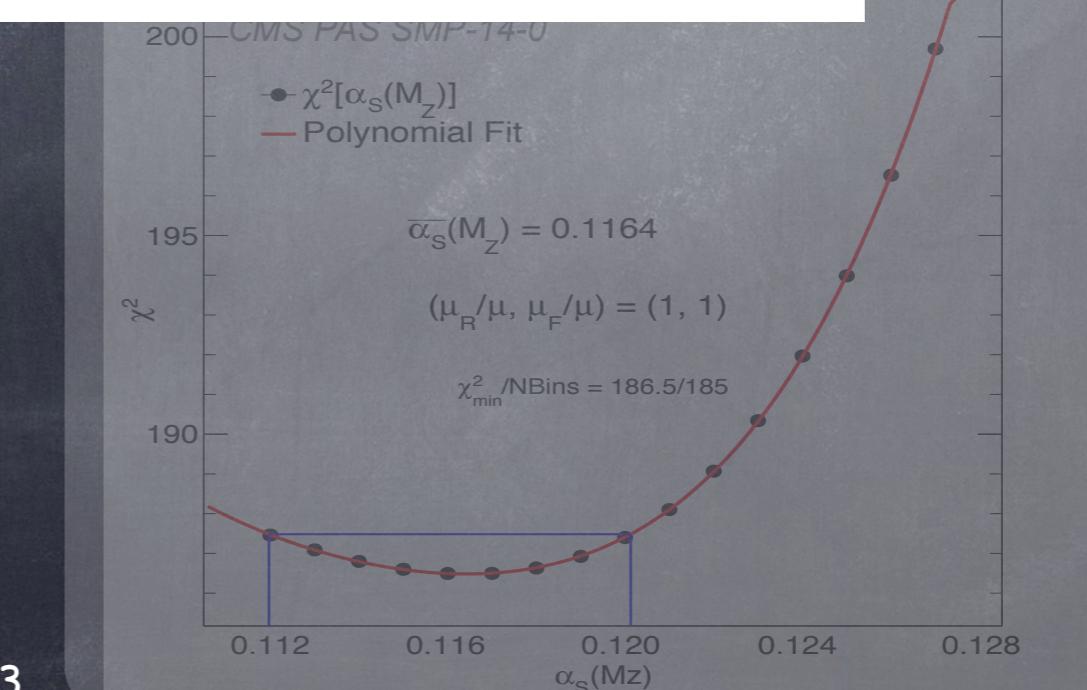
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# Impact of the CMS jet measurements on PDFs

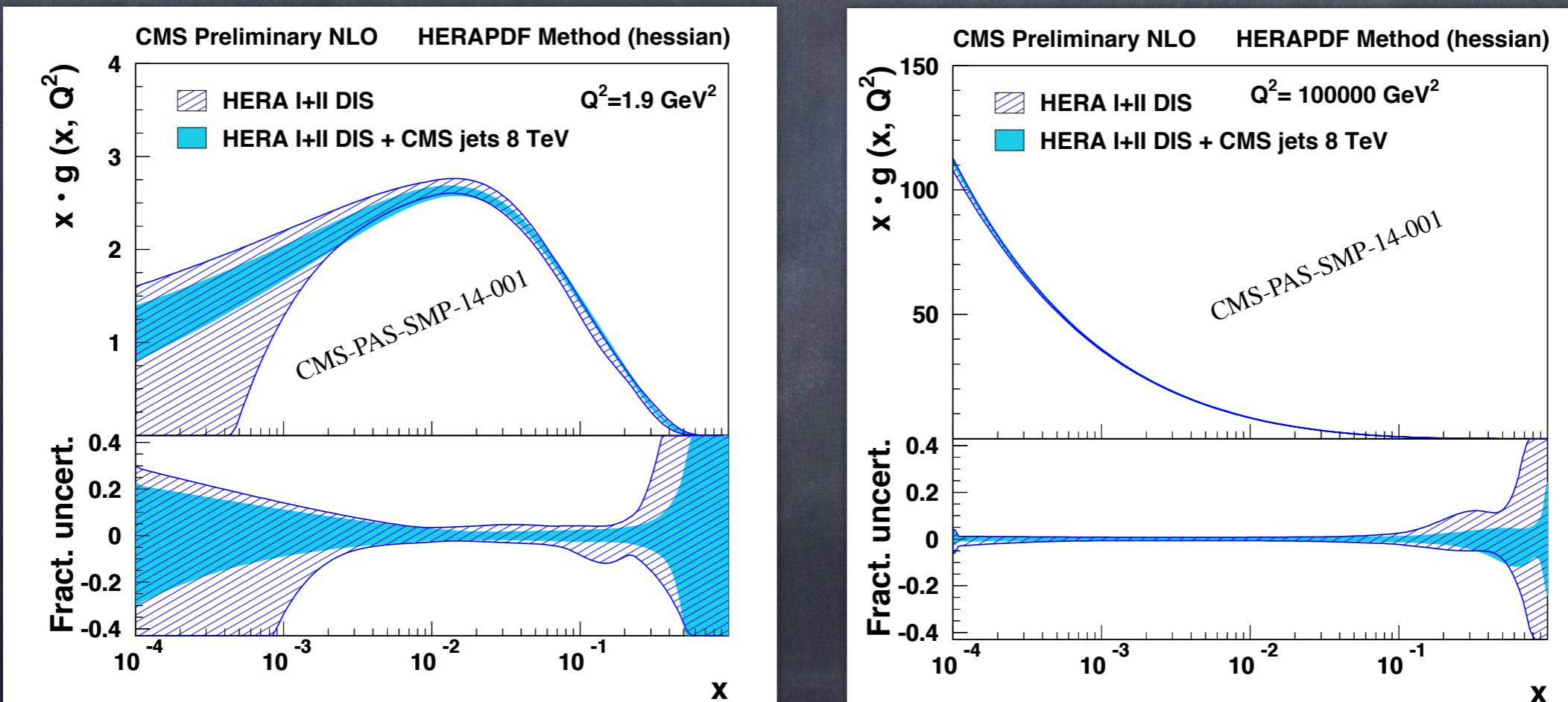
## QCD analysis at NLO

**Data:** combined HERA I+II DIS [Eur. Phys. J. C 75 (2015) 2604]

+ CMS inclusive jet production at 8 TeV,  $L = 19.71 \text{ fb}^{-1}$

**Theory for jet production in  $pp$ :** NLOJET++ version 4.1.3, interfaced via fastNLO

QCD scales  $\mu_r = \mu_f = p_{T\text{jet}}$ , strong coupling  $\alpha_S(m_Z) = 0.1180$ ;



Improvement in the uncertainty of the gluon distributions at high- $x$

# Impact of the CMS jet measurements on PDFs

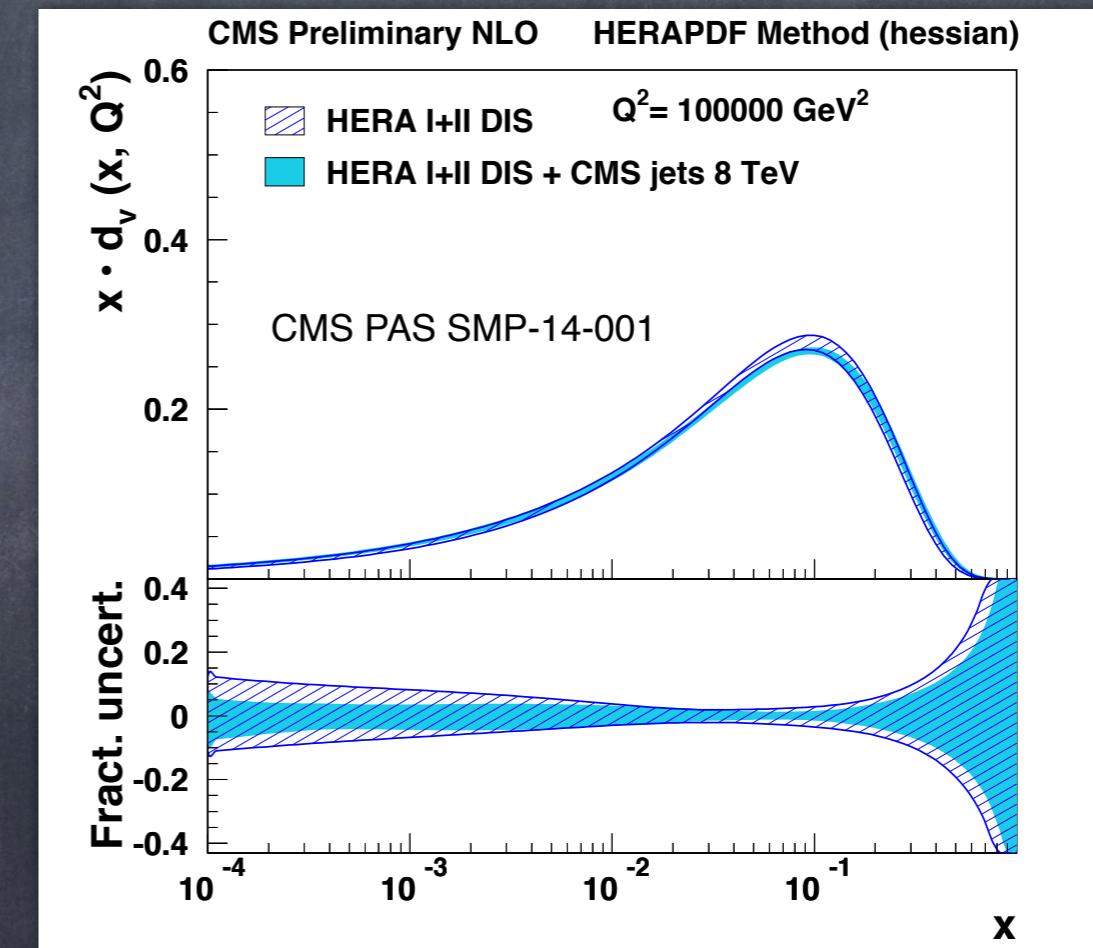
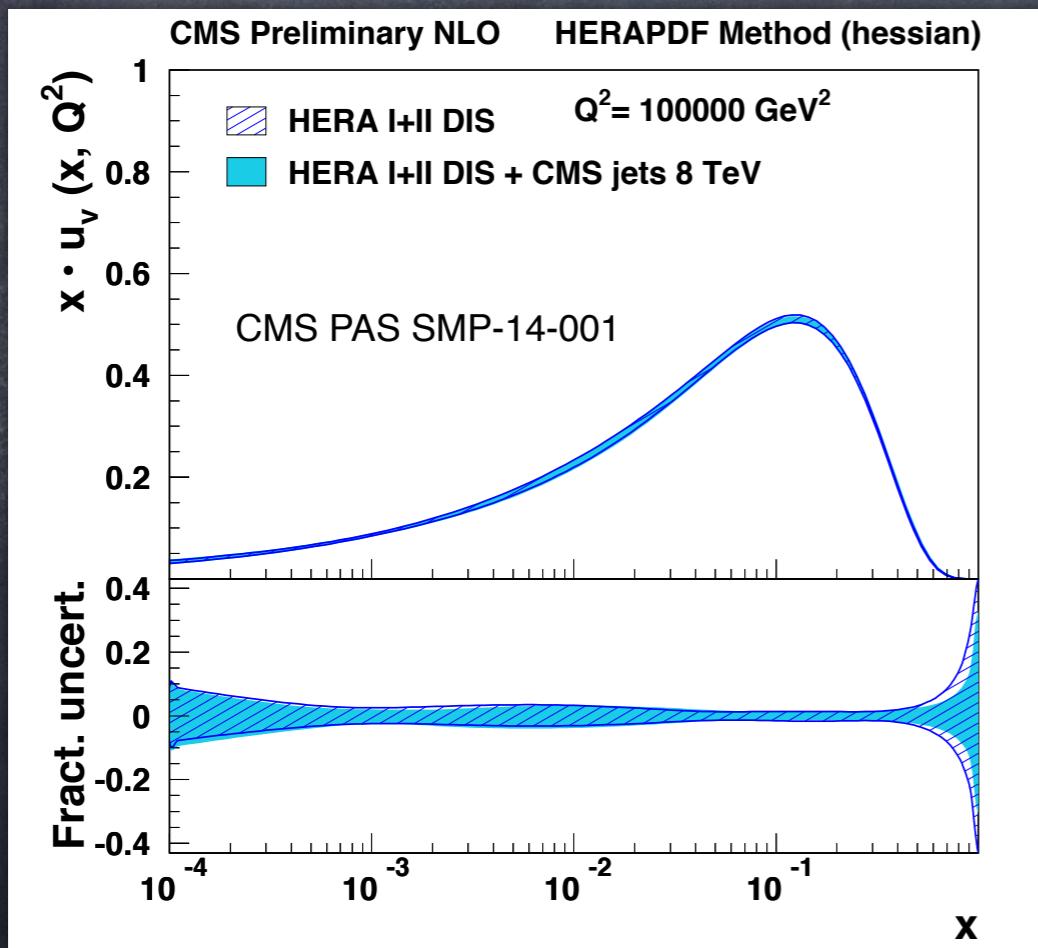
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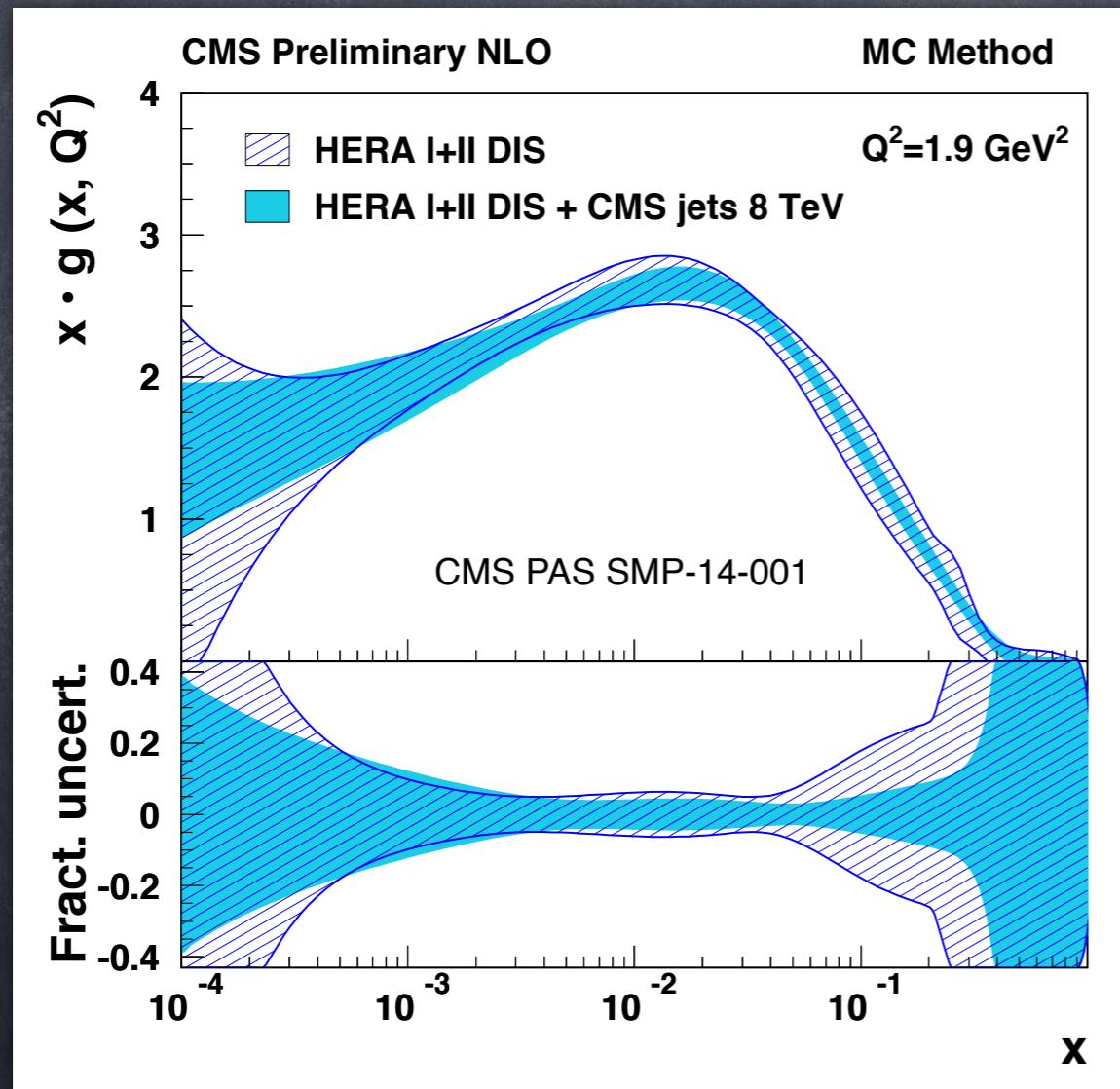
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Improvement in the uncertainty of the valence distributions at high-x

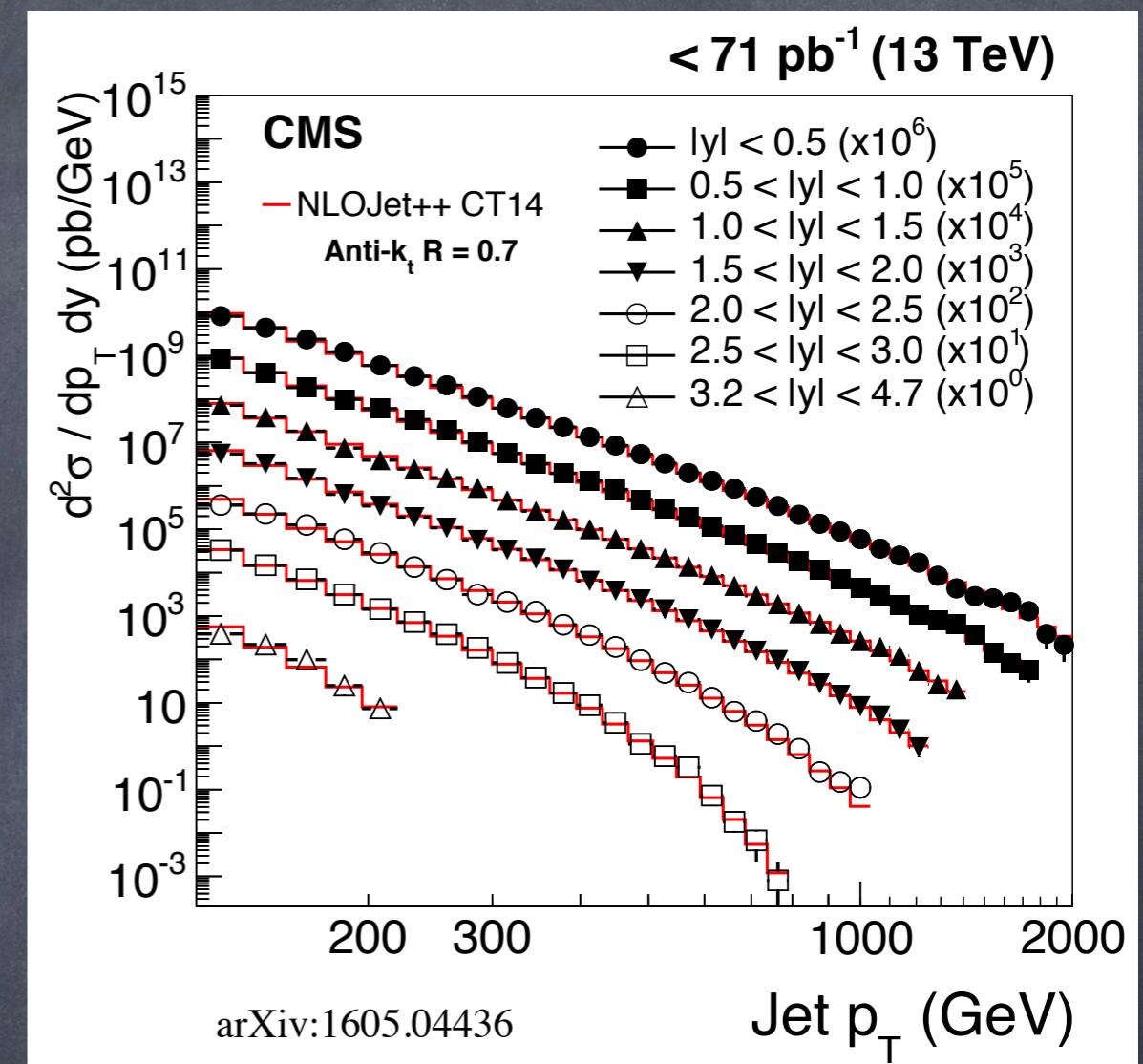
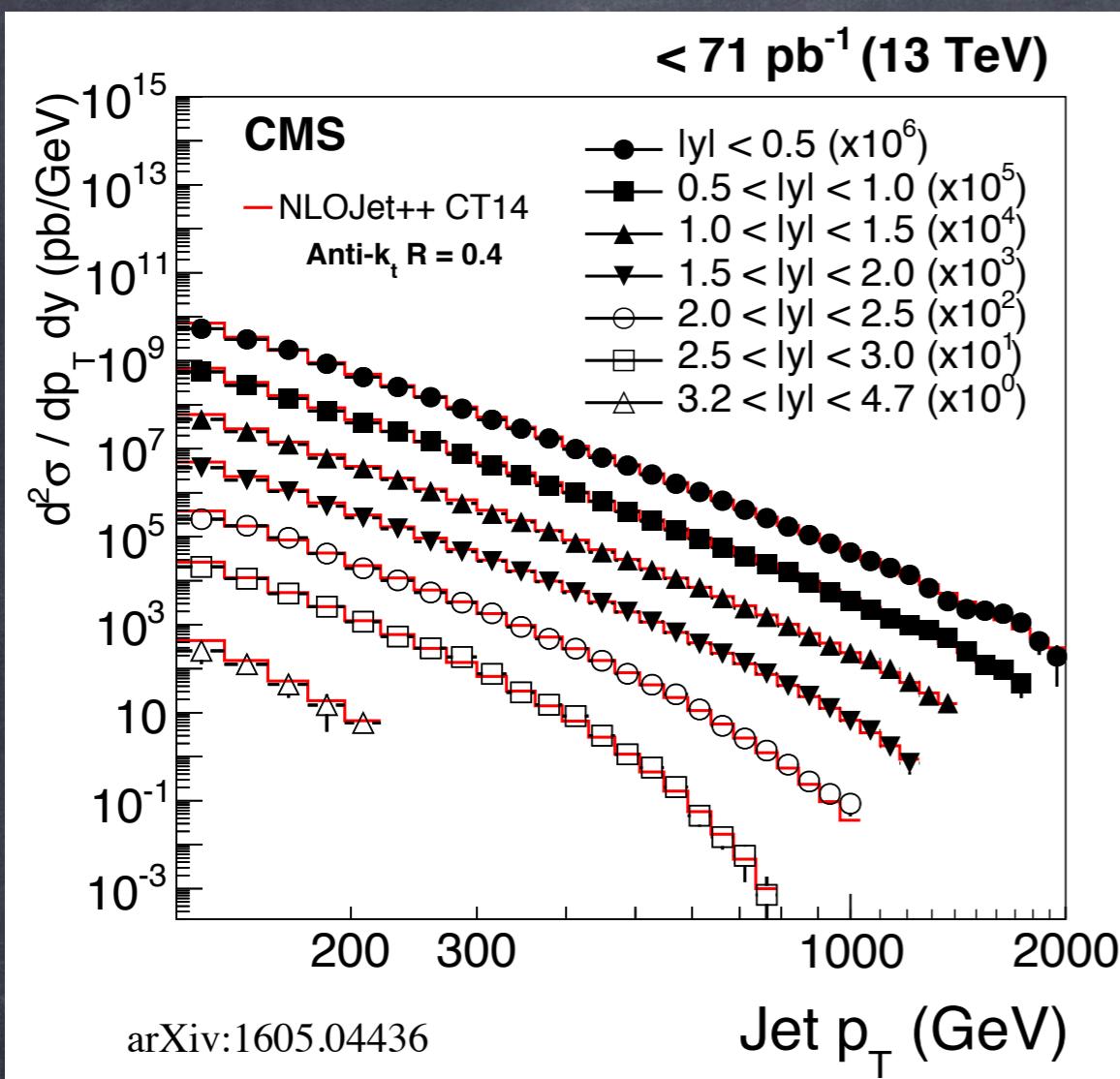
# Estimation of PDF Uncertainty with MC Method

- 200 of replicas allowing the central values of cross-sections to fluctuate within their systematic and statistical uncertainties.
- For each replica, **NLO QCD** fit is performed. Errors on the PDFs are estimated from the RMS of the spread of the curves.



Similar reduction of  
uncertainties observed  
as in hessian estimate

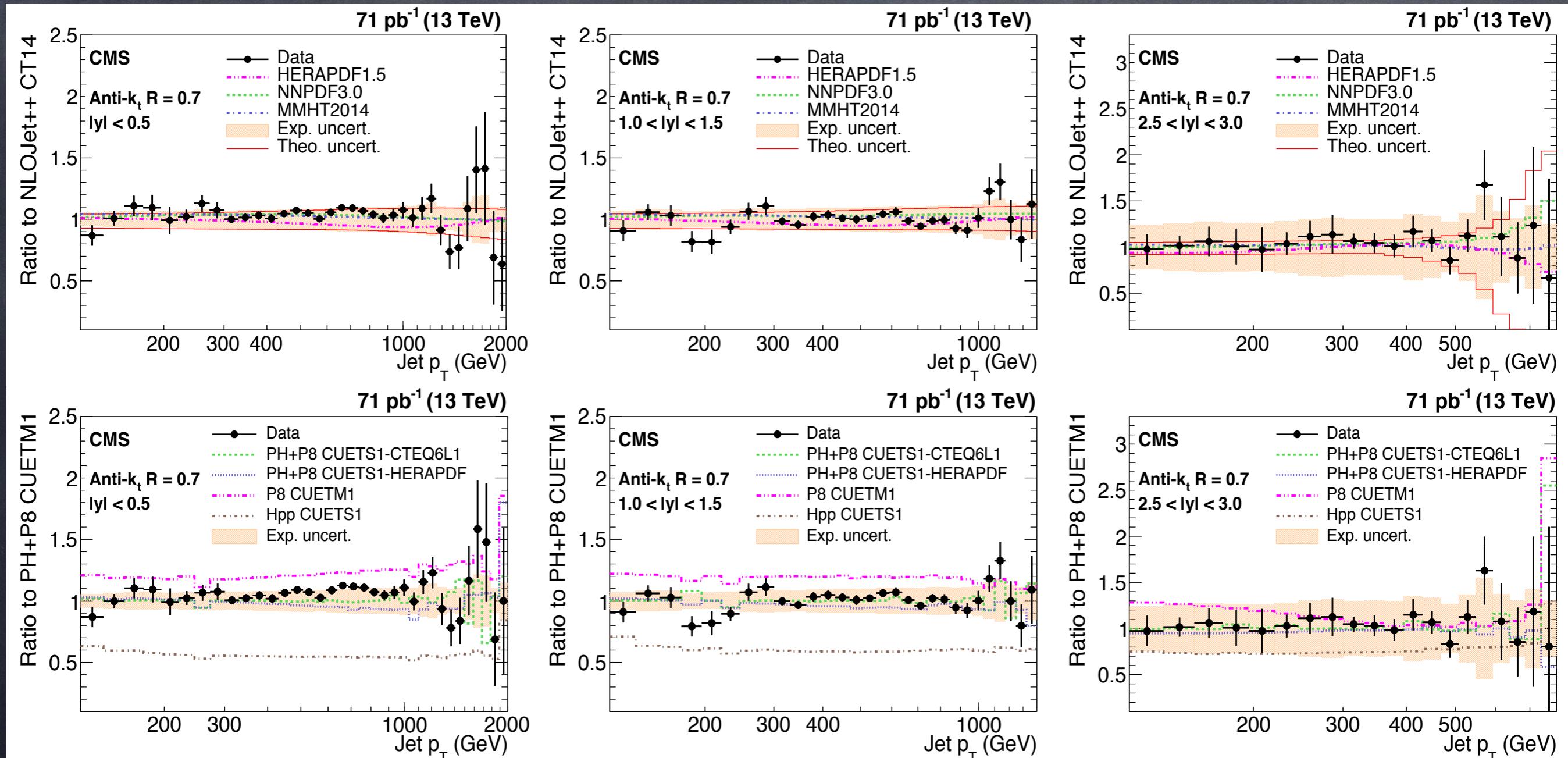
# Inclusive Jet Cross Section @ 13 TeV



Unfolded results compared to predictions from :

- NLOJet++ corrected for NP and electroweak effects
- POWHEG NLO dijet matrix element + Pythia UE simulation
- Pythia 8 and HERWIG++ LO

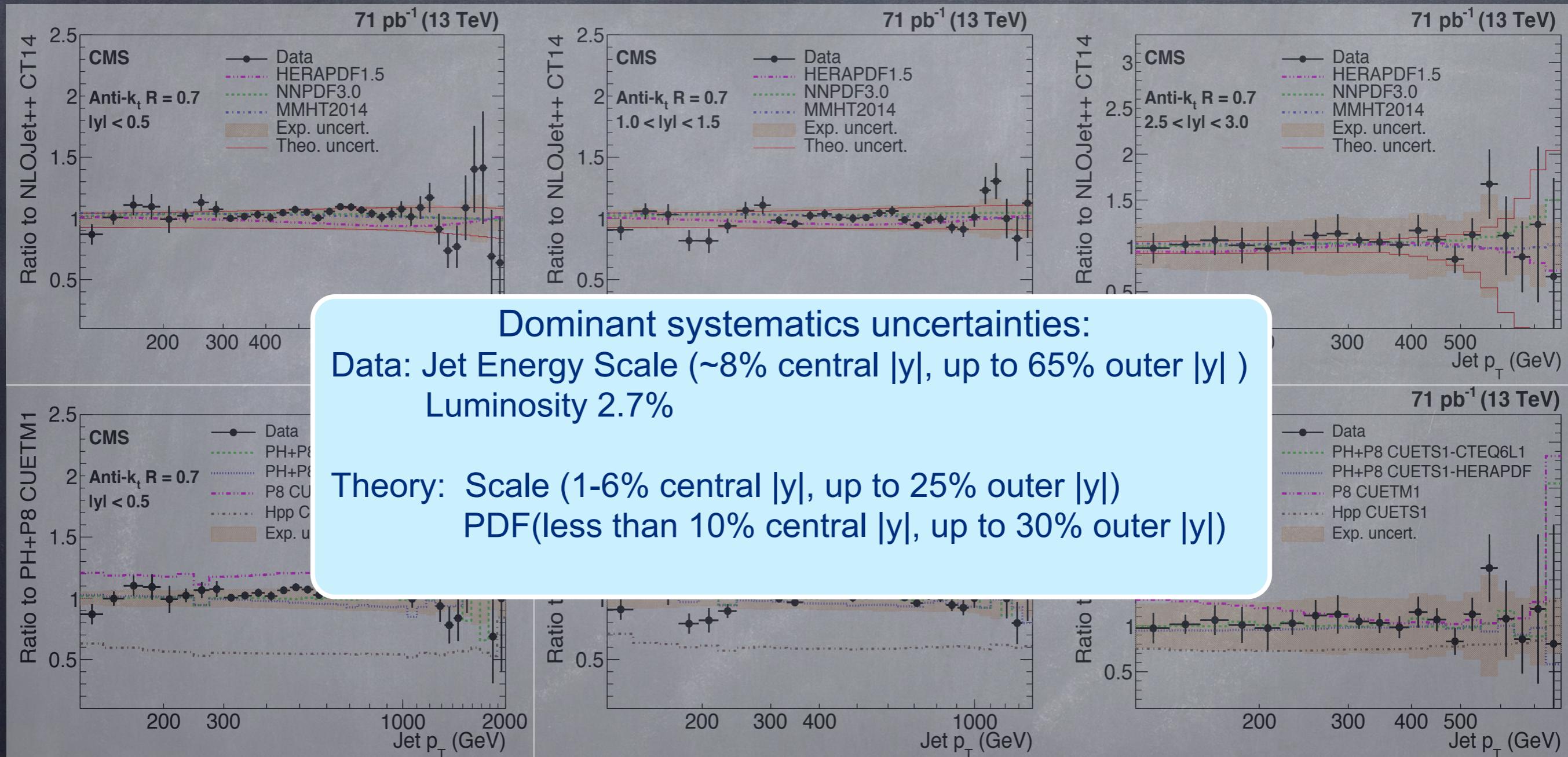
# Inclusive Jet Cross Section @ 13 TeV : Ratios



arXiv:1605.04436

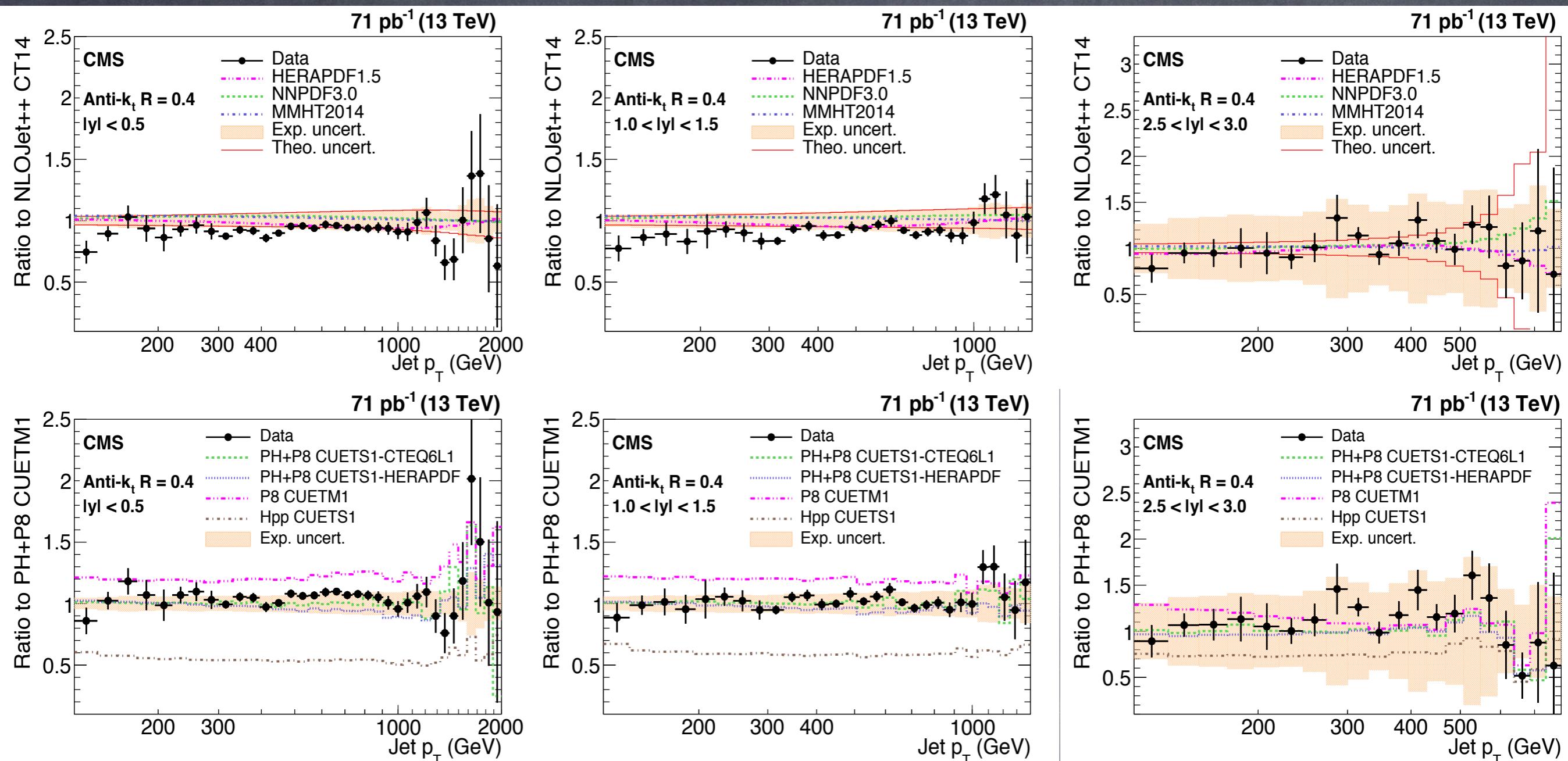
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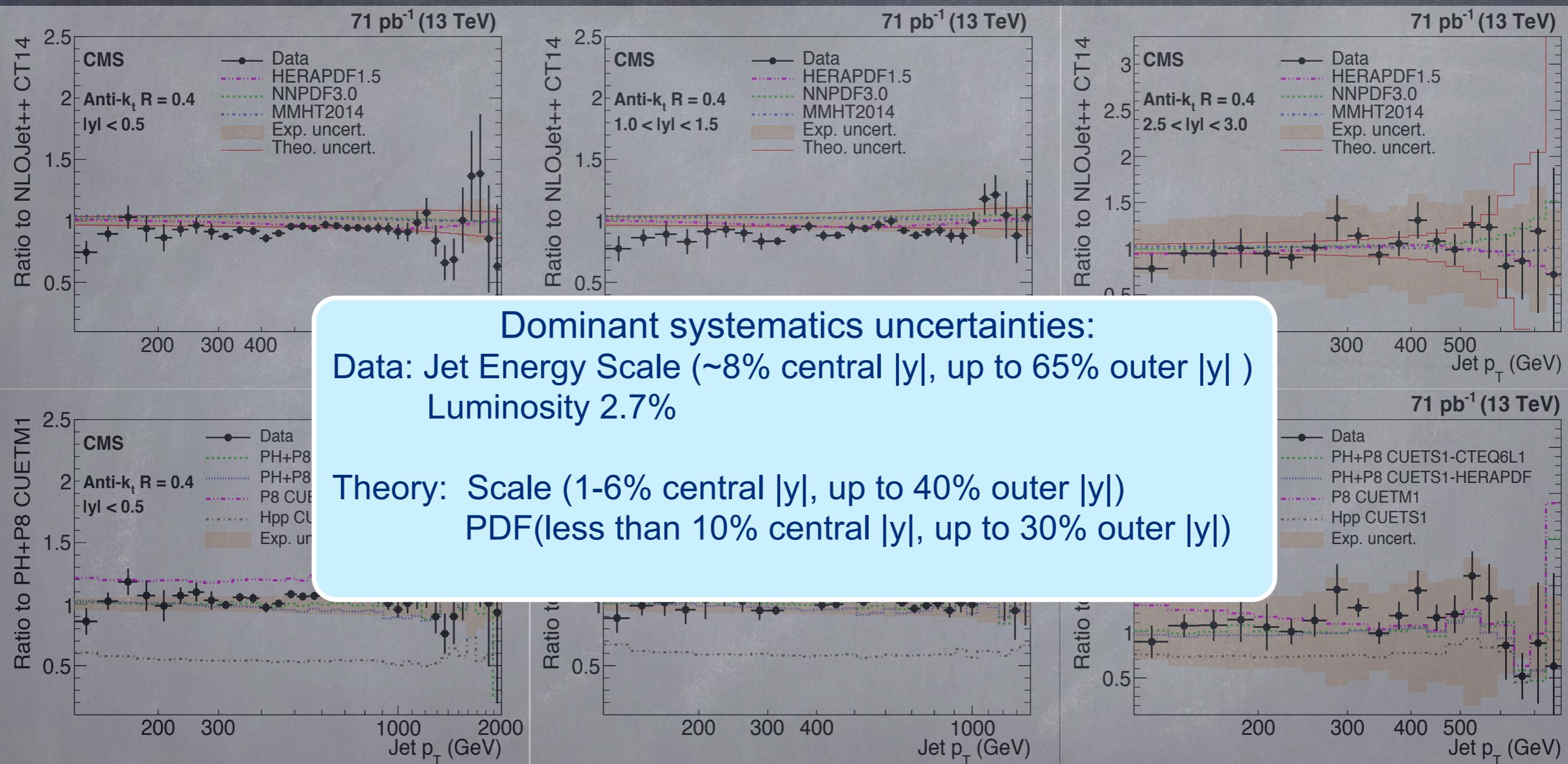
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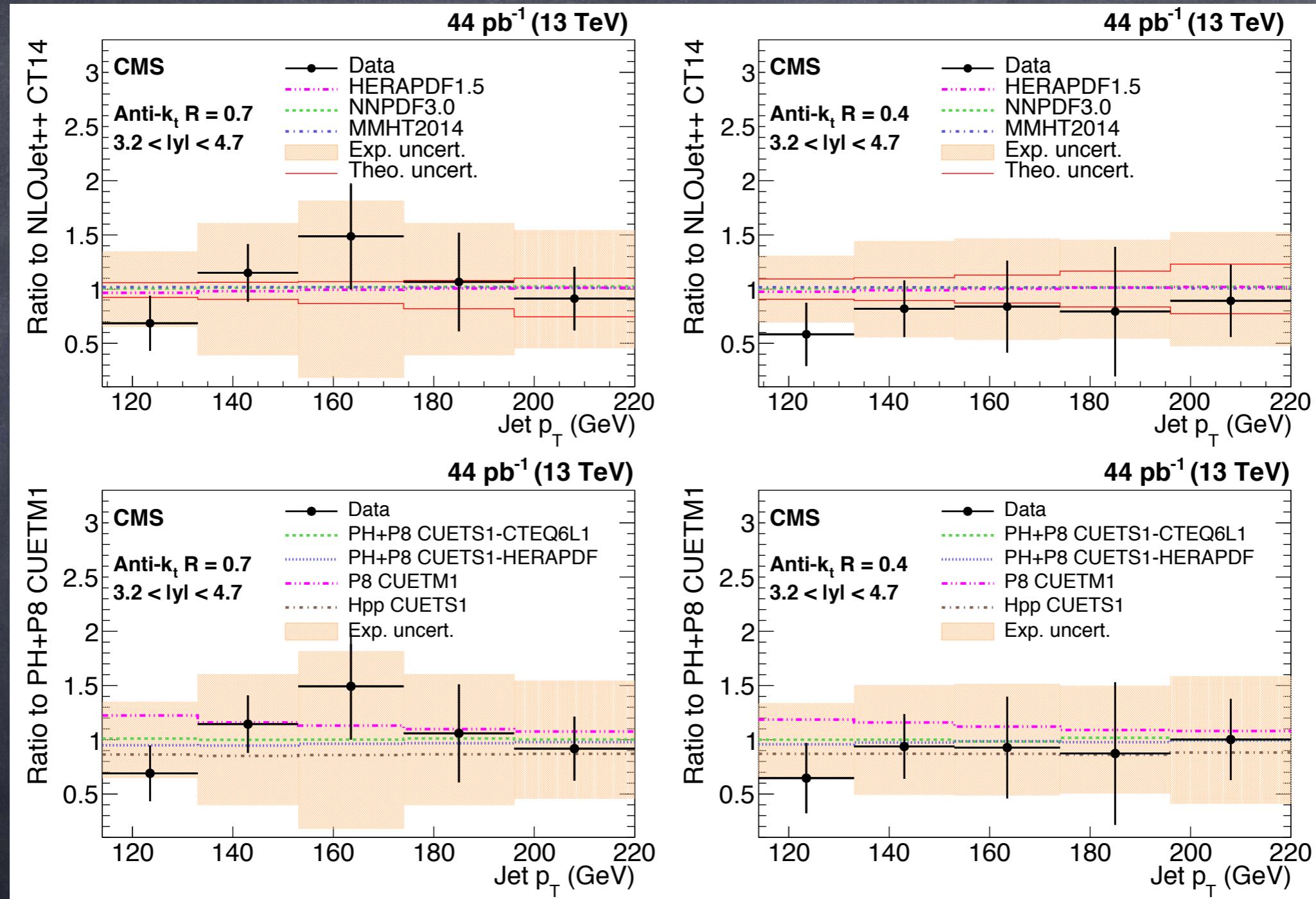
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# Inclusive Jet Cross Section @ 13 TeV : Forward region



arXiv:1605.04436

Predicted cross sections follow the data well in the outermost rapidity region

# Summary

- CMS experiment performed a wide range of jet measurements at various collision energies
- Double differential cross-sections are measured for inclusive jets :
  - ★  $p_T \in [74, 2500] \text{ GeV}$
  - ★  $|y| < 4.7$
- CMS Inclusive Jet @ 8 TeV Data :
  - ★ Precision of the gluon distributions improves.
  - ★ Extraction of strong coupling compatible with world average
- Fixed order NLO calculations describes well jet cross section in various rapidity bins but better for large R for clustering algorithm.
- MC event generators with NLO matrix element follow slightly better the data for jets clustered with small R.

# Backup Slides

# **QCD analyses of Inclusive Jets at 8 TeV.**

**QCD analysis at NLO, parton evolution in  $Q^2$  via DGLAP implemented in QCDNUM.  
xFitter version 1.1.1 is used.**

**Data in the QCD analysis:**

- HERA I+II combined inclusive DIS data, Charged and Neutral Current [[Eur. Phys. J. C 75 \(2015\) 2604](#)]
- Investigated CMS data :
  - Inclusive Jets @ 8 TeV [CMS-PAS-SMP-14-001]

**PDF Uncertainties :** Quadratic sum of experimental, model and parametrisation errors.

**Experimental uncertainties:** originate from uncertainties of the data

- Hessian error estimate: criterion  $\Delta\chi^2=1$  is applied
- MC Method (as a cross check)

**Model uncertainties:** originate from variations of model input parameters:

- Fraction of strange quarks in the sea  $f_s=0.31\pm0.08$
- Values of charm and beauty quark masses.
- $Q^2$  cut on inclusive DIS data.

**Parametrisation uncertainties:**

- Originate from variations on assumed parametrization

# QCD Analysis of Inclusive Jet Measurements at 8 TeV

Basic parametrization at the starting scale  $Q^2_0=1.9 \text{ GeV}^2$  :

Inclusive Jets @8TeV (18p)

$$\begin{aligned} xg(x) &= A_g x^{B_g} \cdot (1-x)^{C_g} (1+E_g x^2) - A'_g x^{B'_g} (1-x)^{C'_g} \\ xu_v(x) &= A_{u_v} x^{B_{u_v}} \cdot (1-x)^{C_{u_v}} \cdot (1+D_{u_v} x + E_{u_v} x^2) \\ xd_v(x) &= A_{d_v} x^{B_{d_v}} \cdot (1-x)^{C_{d_v}} \cdot (1+D_{d_v} x) \\ x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} \cdot (1-x)^{C_{\bar{U}}} (1+D_{\bar{U}} x) \\ x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} \cdot (1-x)^{C_{\bar{D}}} (1+D_{\bar{D}} x + E_{\bar{D}} x^2) \end{aligned}$$

Table 7: Partial  $\chi^2/n_{dp}$  per number of data points  $n_{dp}$  for the data sets used in the QCD analysis. The global  $\chi^2/n_{dof}$  per degrees of freedom of 1471/1216 is obtained, with correlated  $\chi^2$  of 94.

Data sets		Partial $\chi^2/n_{dp}$
HERA1+2 Neutral Current	$e^+ p E_p = 920 \text{ GeV}$	440/377
HERA1+2 Neutral Current	$e^+ p E_p = 820 \text{ GeV}$	416/379
HERA1+2 Neutral Current	$e^+ p E_p = 575 \text{ GeV}$	214/254
HERA1+2 Neutral Current	$e^+ p E_p = 460 \text{ GeV}$	210/204
HERA1+2 Neutral Current	$e^- p$	218/159
HERA1+2 Charged Current	$e^+ p$	46/39
HERA1+2 Charged Current	$e^- p$	50/42
CMS inclusive jets 8 TeV	$0 < y < 0.5$	53/36
	$0.5 < y < 1.0$	34/36
	$1.0 < y < 1.5$	35/35
	$1.5 < y < 2.0$	52/29
	$2.0 < y < 2.5$	49/24
	$2.5 < y < 3.0$	4.9/18

CMS-PAS-SMP-14-001

Normalization parameters  $A$  are determined by QCD sum rules  
 $B$ : define low- $x$  behaviour,  $C$ : high- $x$  shape

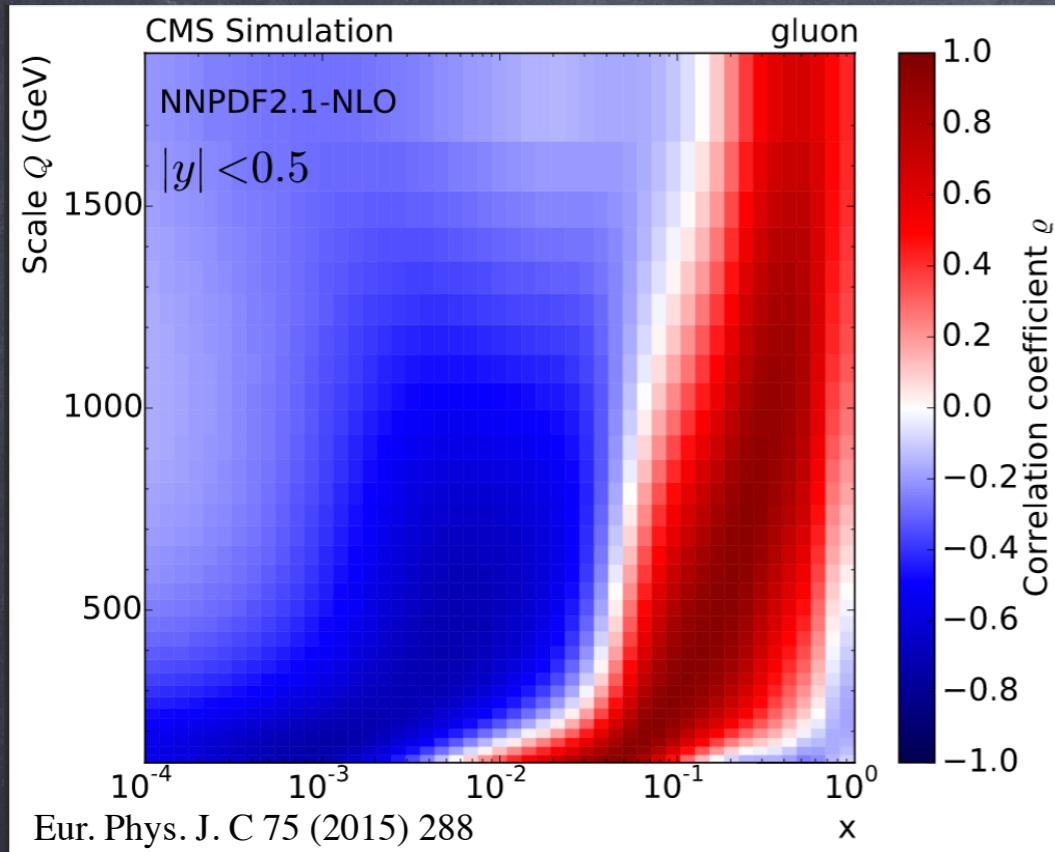
## $\chi^2$ definitions

$$\chi^2(m, b) = \sum_i \frac{[\mu_i - m_i(1 - \sum_j \gamma_j^i b_j)]^2}{\delta_{i, unc}^2 m_i^2 + \delta_{i, stat} \mu_i m_i (1 - \sum_j \gamma_j^i b_j)} + \sum_j b_j^2$$

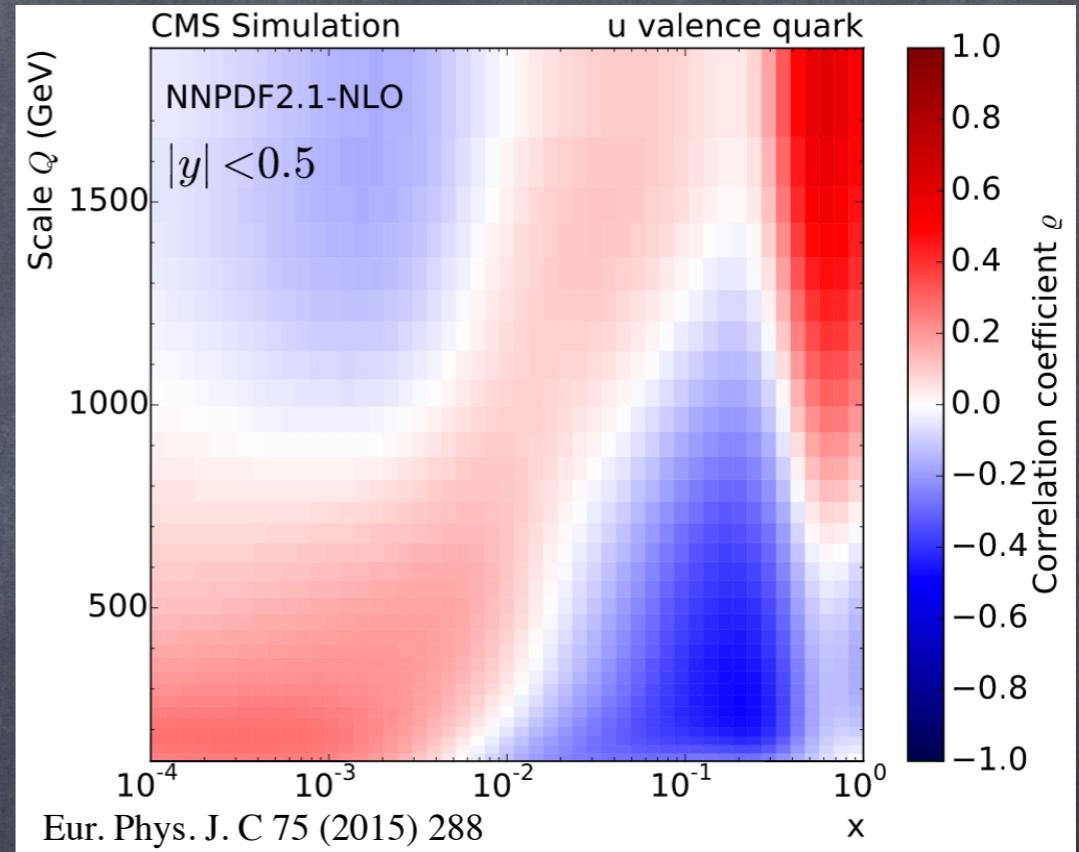
$$\chi^2(m) = \sum_{i,k} (m_i - \mu_i) C_{ik}^{-1} (m_k - \mu_k)$$

# Probing QCD with Jet Cross Sections

**Strong correlation between inclusive jet cross section and gluon at high-middle x**



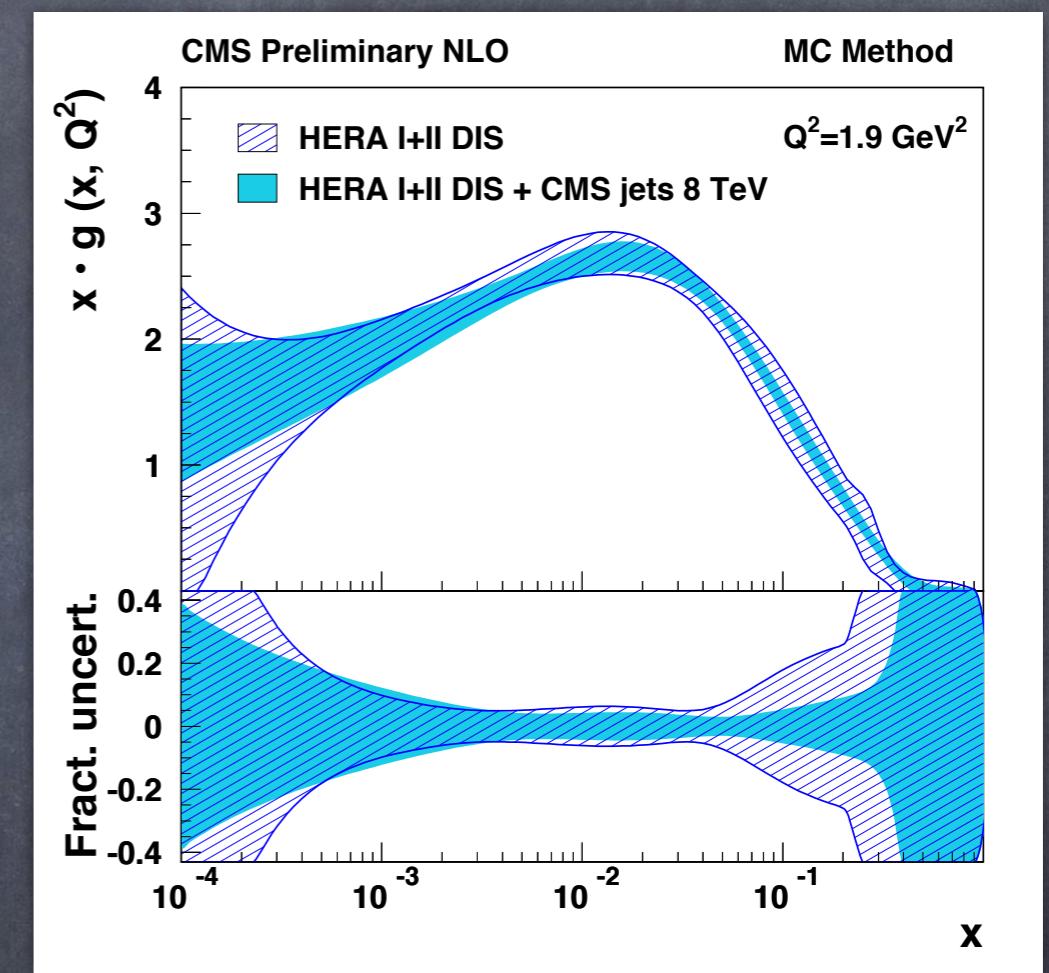
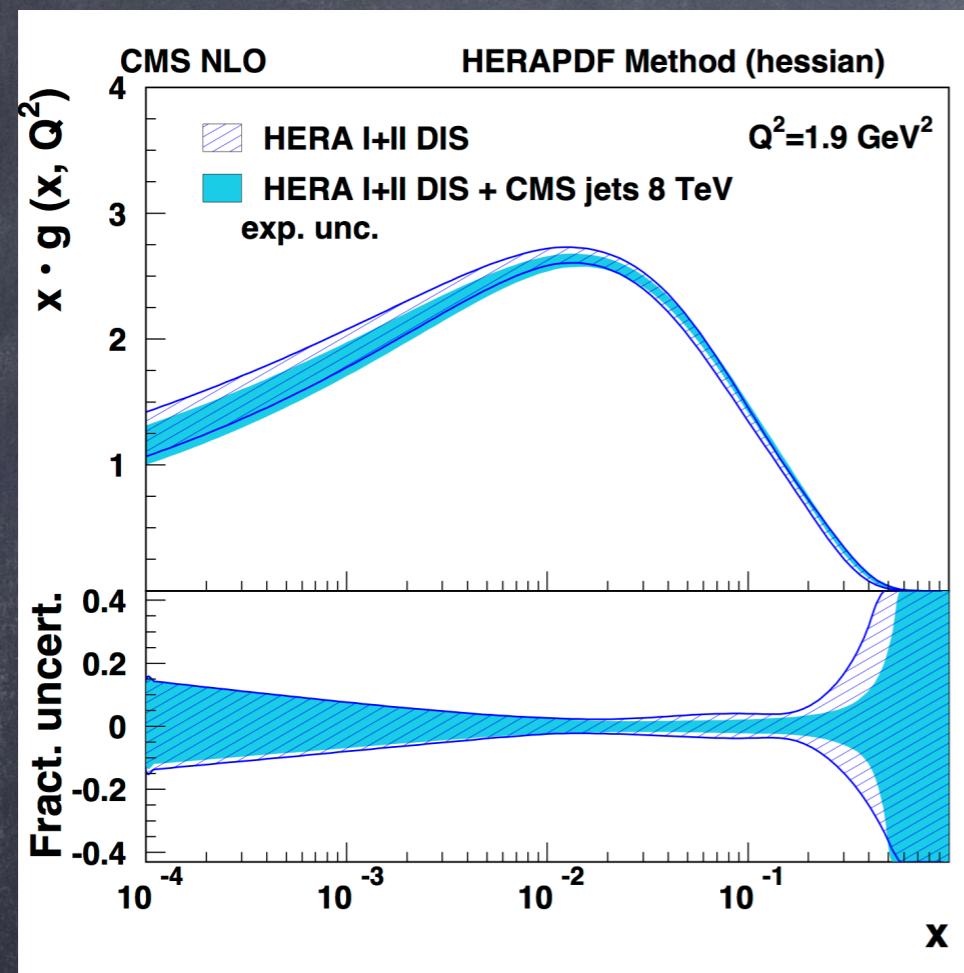
**Strong correlation between inclusive jet cross section and quark at high x**



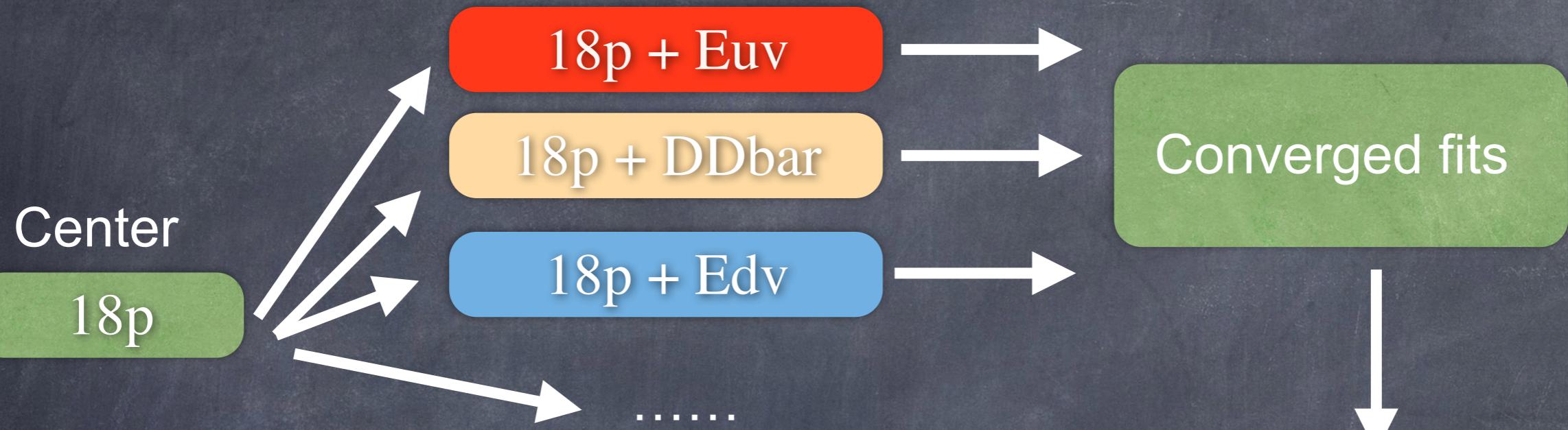
The potential impact of the CMS inclusive jet data can be illustrated by the correlation between the inclusive jet cross section  $\sigma_{\text{jet}}(Q)$  and the PDF  $xf(x, Q^2)$  for any parton flavour  $f$ . The NNPDF Collaboration [63] provides PDF sets in the form of an ensemble of replicas  $i$ , which sample variations in the PDF parameter space within allowed uncertainties. The correlation coefficient  $\rho_f(x, Q)$  between a cross section and the PDF for flavour  $f$  at a point  $(x, Q)$  can be computed by evaluating means and standard deviations from an ensemble of  $N$  replicas as

$$\rho_f(x, Q) = \frac{N}{(N-1)} \frac{\langle \sigma_{\text{jet}}(Q)_i \cdot xf(x, Q^2)_i \rangle - \langle \sigma_{\text{jet}}(Q)_i \rangle \cdot \langle xf(x, Q^2)_i \rangle}{\Delta_{\sigma_{\text{jet}}(Q)} \Delta_{xf(x, Q^2)}}. \quad (12)$$

# Hessian vs MC



# Parametrisation Uncertainty



- Get the largest difference
- Construct envelope

