

# Effective theories, dark matter and neutrinos

RICHARD HILL

TRIUMF & Perimeter Institute & U. Chicago

Aspen Winter Meeting  
15 January 2016

# Features work of the following students



M. Solon,  
( 2015 Sakurai thesis award  
U.Chicago → UC Berkeley/LBNL )



A. Meyer  
(U.Chicago/FNAL)

Thanks also: J. Arrington, M. Bauer, M. Betancourt, C. Blanco, T. Cohen, R. Gran, A. Kronfeld, G. Lee, G. Paz, M. Wetstein, and many others.

# Will discuss 3 “The Effective Theories” of WIMP dark matter

- heavy WIMP expansion
- heavy mediator expansion
- low velocity expansion

## and the relation between 3 aspects of Neutrino Physics

- neutrino models
- cross sections (particle physics)
- cross sections (nuclear physics)



cf. talks of S. Pascoli,  
M. Messier,  
K Heeger, ...

Two questions that I hope this talk will help introduce and address:

- What can the particle theorist do about neutrino cross sections at  $\sim$ GeV energies?
- Isn't this messy/nuclear physics?

Will see:

- interesting and solvable problems
- new tools, techniques and experimental handles available

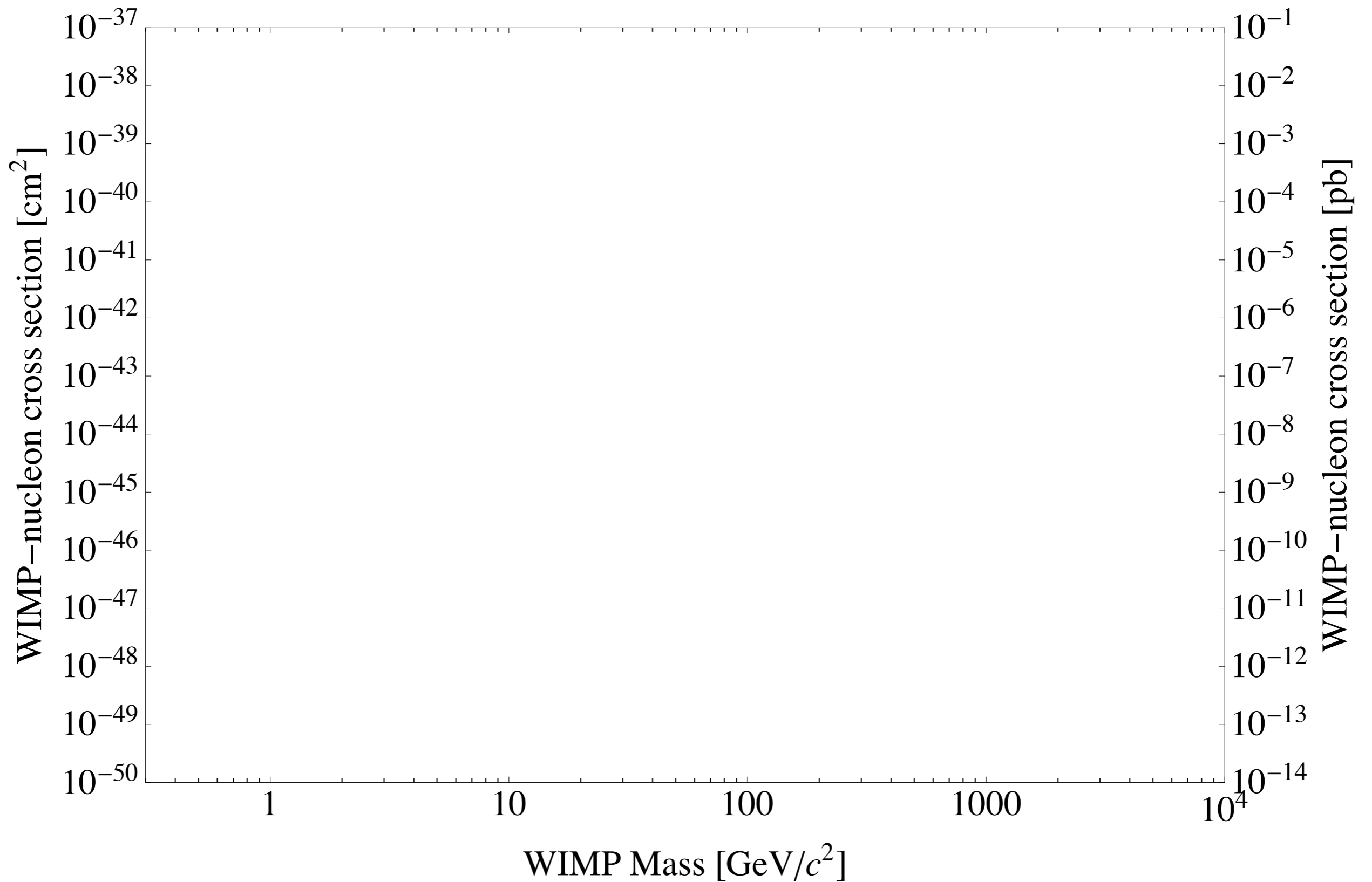
Need to go where the physics takes us. Nobody said that probing high scales was going to be easy

## Part I:

# The “The Effective Theories” of WIMP dark matter

- heavy WIMP expansion
- heavy mediator expansion
- low velocity expansion

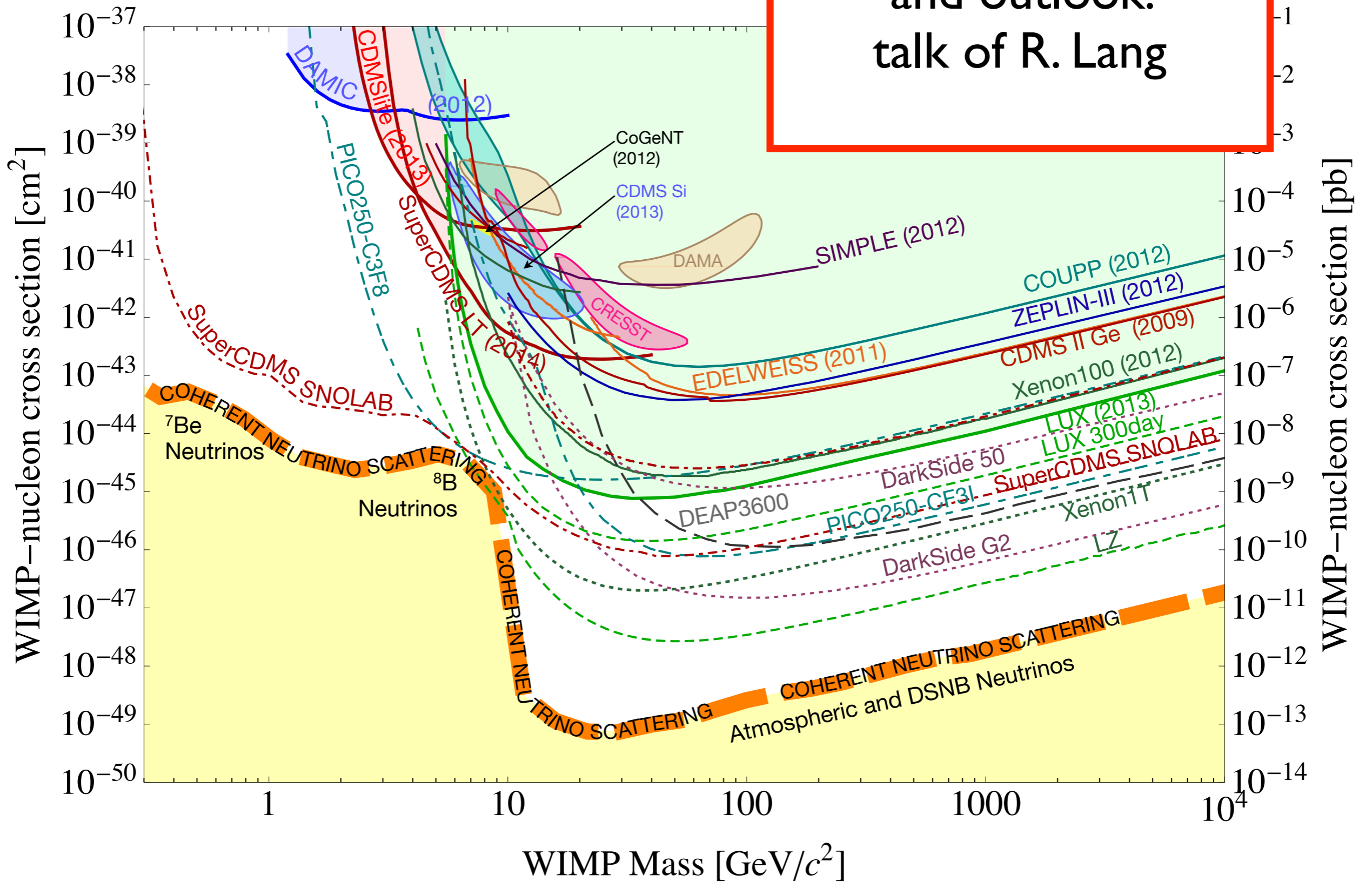
# A lot of space...



A lot of space remaining...



experimental status  
and outlook:  
talk of R. Lang



# The “The Effective Theories” of WIMP dark matter



- heavy WIMP expansion
- heavy mediator expansion
- low velocity expansion



## DM EFT I: Heavy WIMP expansion

- Present null results may point to  $\gtrsim \text{TeV}$  WIMP mass
- This regime has important challenges and simplifications

Take as basic WIMP:

$SU(3) \times SU(2) \times U(1)$

spin

1

3

0

s

Many results independent of WIMP spin, and elementary vs. composite nature of WIMP (e.g. wino, composite scalar, ...)

# Direct detection

## Many manifestations of heavy particle symmetry:

- hydrogen/deuterium spectroscopy

$$E_n(H) = -\frac{1}{2}m_e(Z\alpha)^2 + \dots \quad (m_e Z\alpha) \ll m_e$$

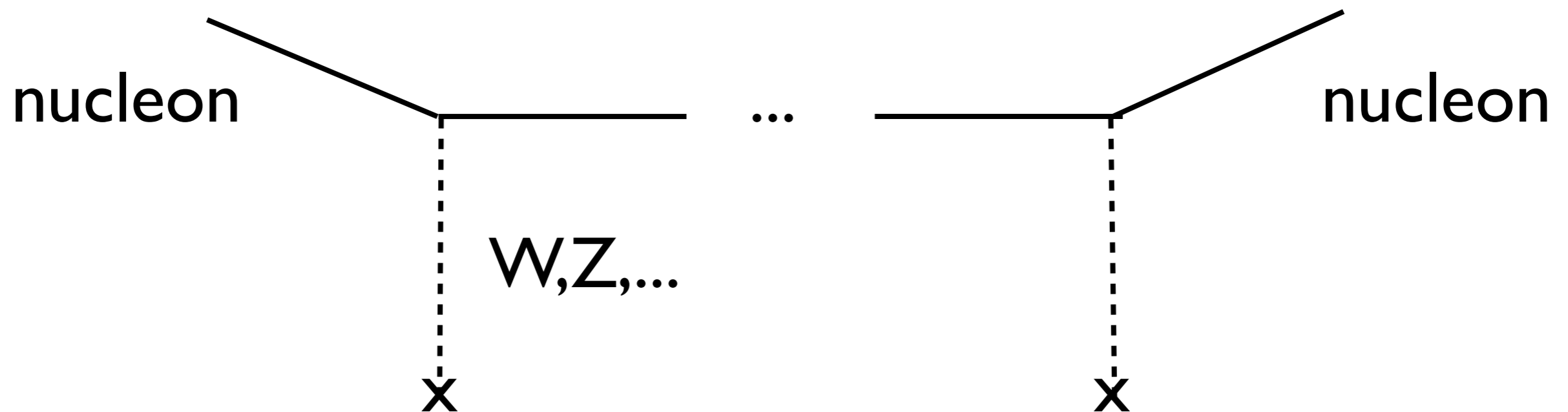
- heavy meson B/B\* transitions

$$F^{B \rightarrow D}(v' = v) = 1 + \dots \quad \Lambda_{\text{QCD}} \ll m_{b,c}$$

- DM interactions

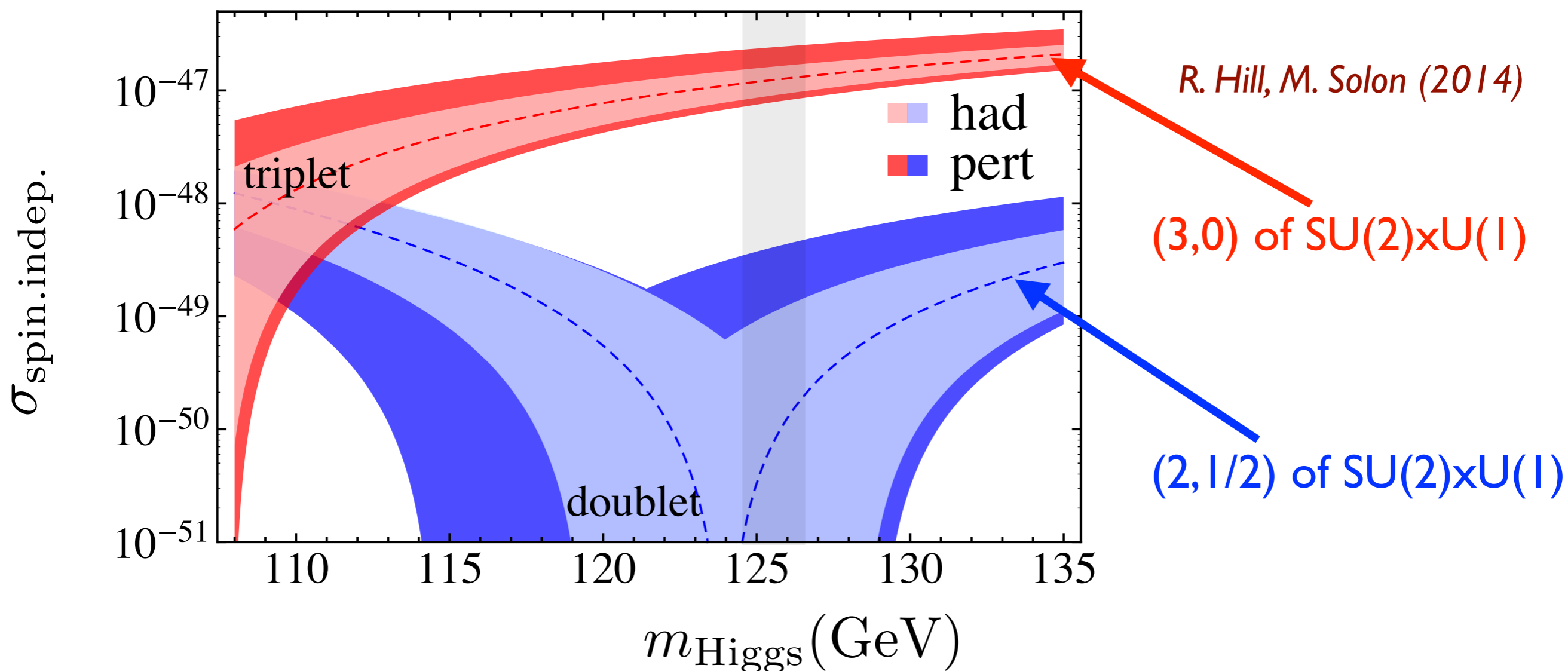
$$\sigma(\chi N \rightarrow \chi N) = ?$$

$$m_W \ll m_\chi$$



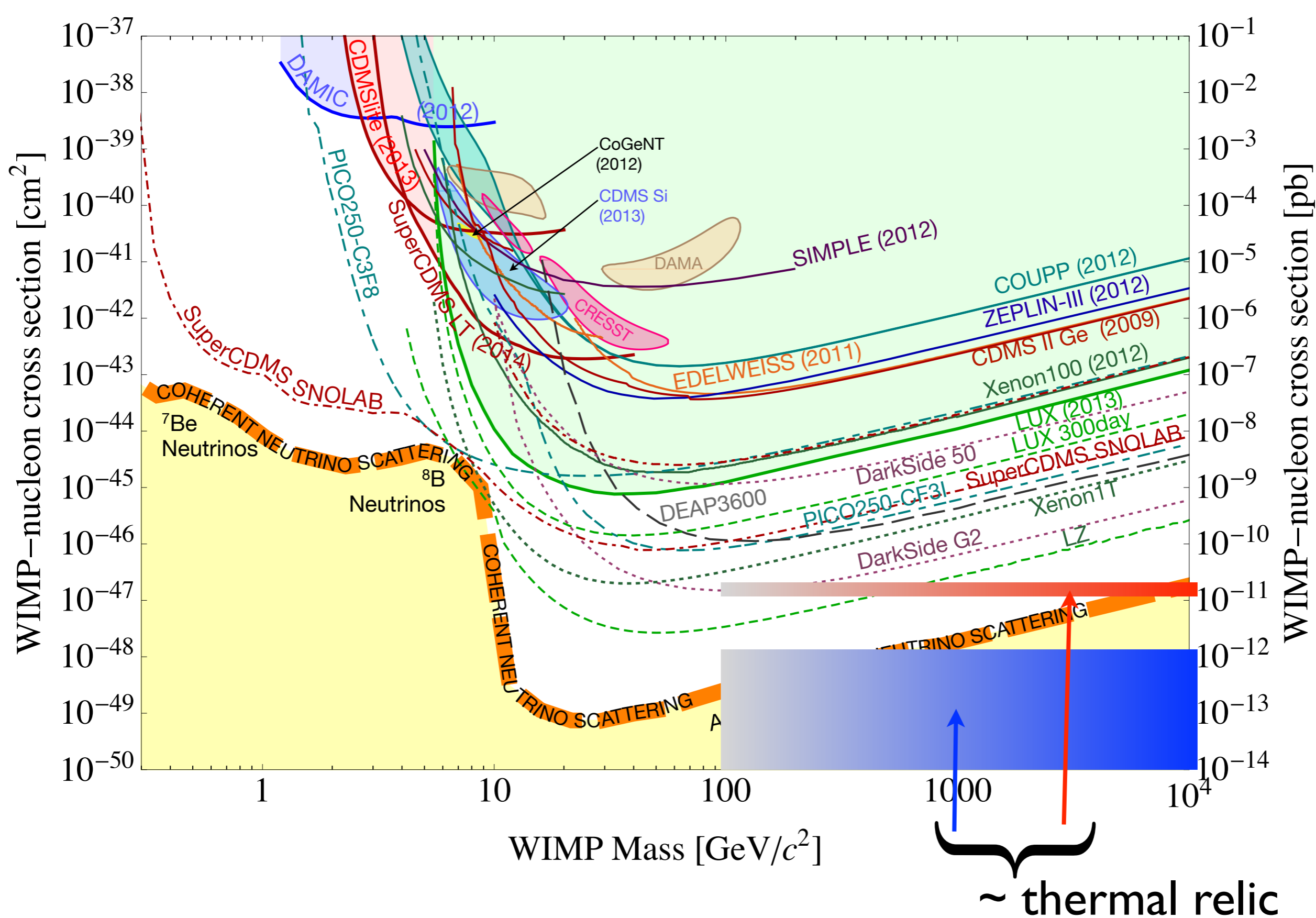
basic problem in SM physics: scattering of nucleon from SU(2)xU(1) source

# Benchmarks: large mass, low velocity limit



Suppressed versus dimensional estimate ( $\sim 10^{-45} \text{cm}^2$ )

- bino/wino, bino/higgsino admixtures *Hill, Solon 1309.4092, 1401.3339, 1409.8290*
- bino/sfermion admixtures *Berlin, Robertson, Solon, Zurek 1511.05964*
- I/M power corrections *C.-Y. Chen, A. Wijangco ...*

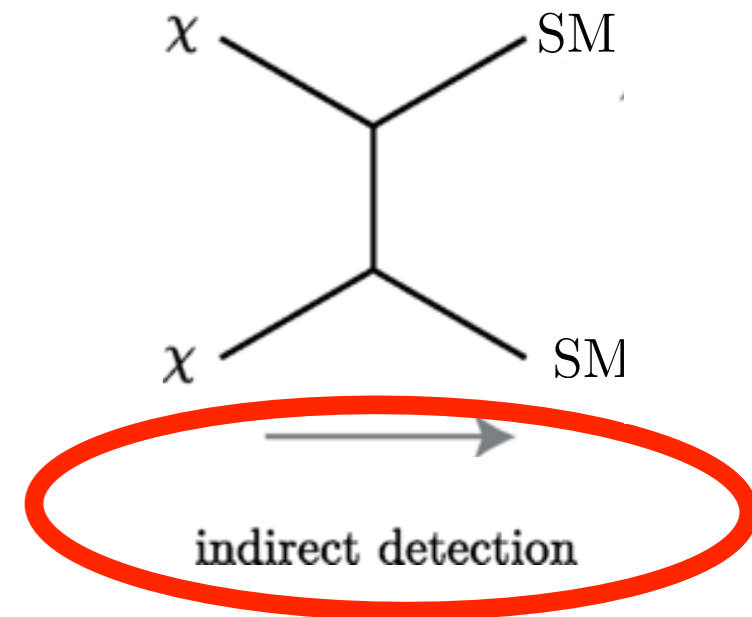


Strong motivation for pushing to neutrino floor at TeV mass

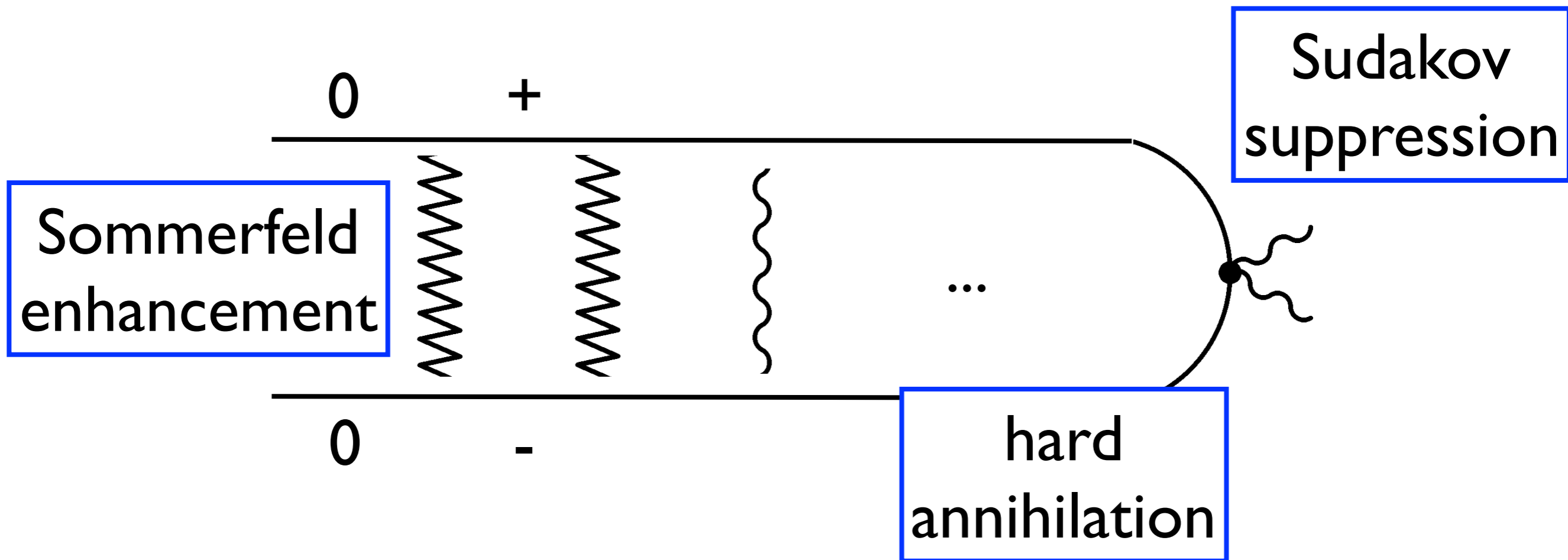
# Indirect detection

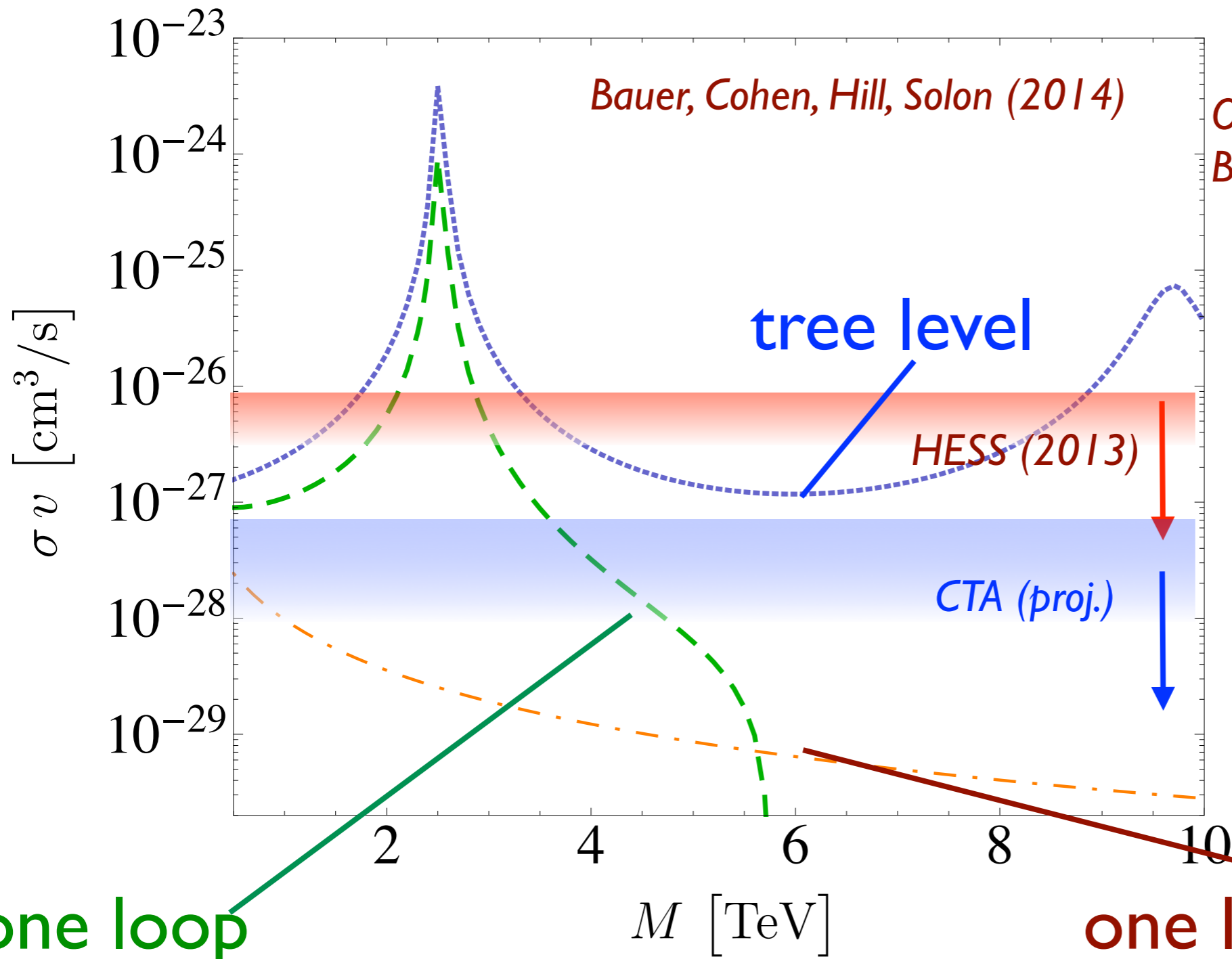
Recall basic WIMP:

$$SU(3) \times SU(2) \times U(1)$$
$$1 \quad 3 \quad 0$$



Photon line signal for heavy WIMP annihilation:





*Bauer, Cohen, Hill, Solon (2014)*

*see also:  
Ovanesyan, Slatyer, Stewart 2014,  
Baumgart, Rothstein, Vaidya 2014,  
Baumgart, Vaisya 2015, ...*

**tree level**

*HESS (2013)*

*CTA (proj.)*

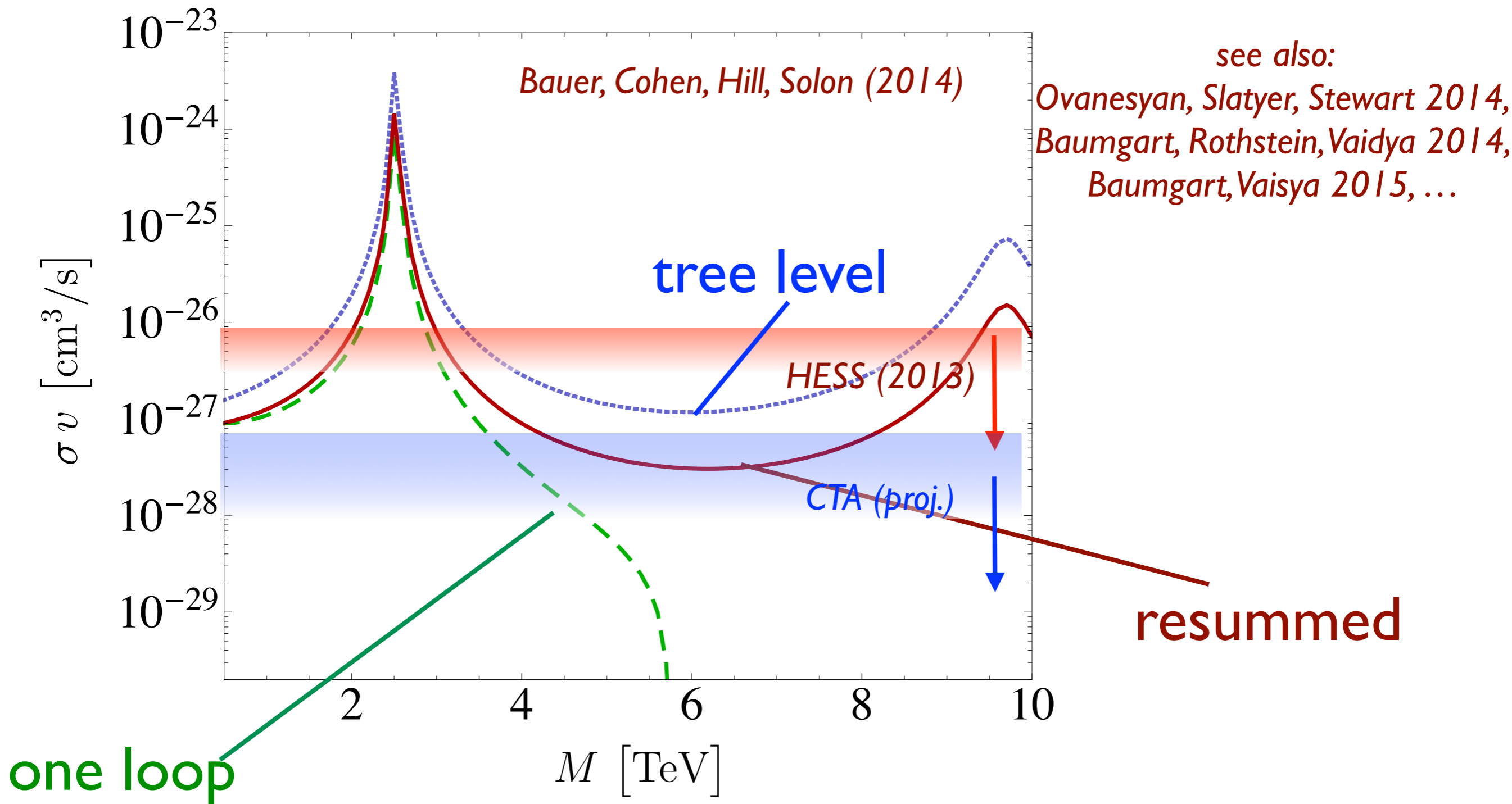
Photon line signal  
for “wino”  
annihilation

**one loop**

**one loop, neglect**

**wavefunction enhancement**

**Multi-scale field theory problem, breakdown of naive perturbation theory**



# The “The Effective Theories” of WIMP dark matter

- heavy WIMP expansion
- heavy mediator expansion
- low velocity expansion





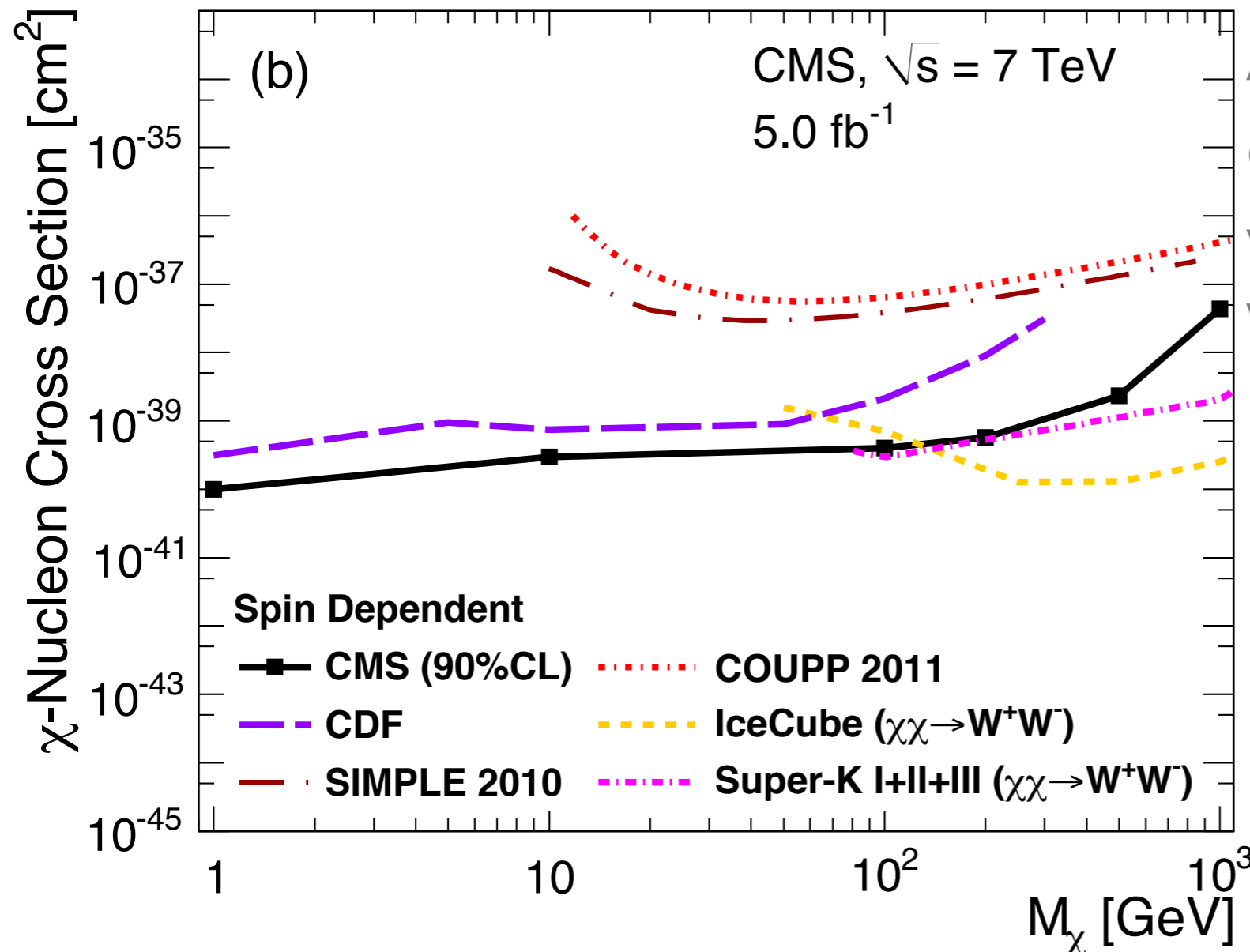
# Heavy Mediator expansion

Set-up:

$$\mathcal{L} \sim c_i \frac{1}{\Lambda^{d-4}} O_{\text{SM}} \times O_{\text{WIMP}}$$

*Goodman, Ibe, Rajaraman, Shepherd, Tait, Yu 2010, ...*

Majorana fermion: 10 operators through d=7



Axial-vector quark contact interaction with Dirac fermion WIMP

other examples, simplified model extensions: talks of T. Tait, F. Maltoni

# The “The Effective Theories” of WIMP dark matter

- heavy WIMP expansion
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- low velocity expansion



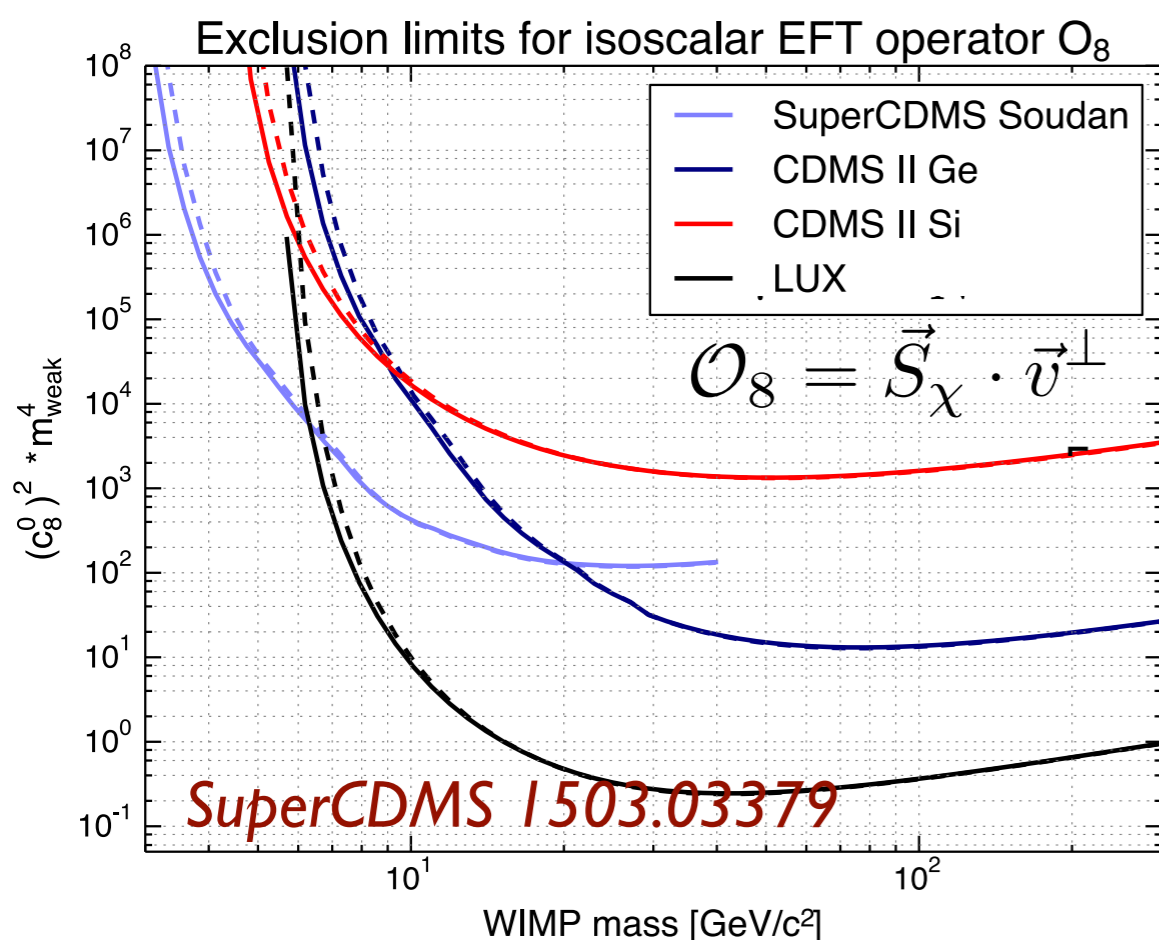
# Velocity expansion

Set-up

$$\mathcal{L} = N^\dagger \left\{ i\partial_t + \frac{\partial^2}{2m_N} + \dots \right\} N + \chi^\dagger \left\{ i\partial_t + \frac{\partial^2}{2m_\chi} + \dots \right\} \chi + \sum_i \frac{C_i}{\Lambda^{d-4}} N^\dagger (\dots) N \chi^\dagger (\dots) \chi$$

*Fitzpatrick, Haxton, Katz, Lubbers, Xu (2012), ...*

20 contact operators through  $1/M^4$



- tracing simplified models to non.rel. ops

*Dent, Krauss, Newstead, Sabharwal 1505.03117*

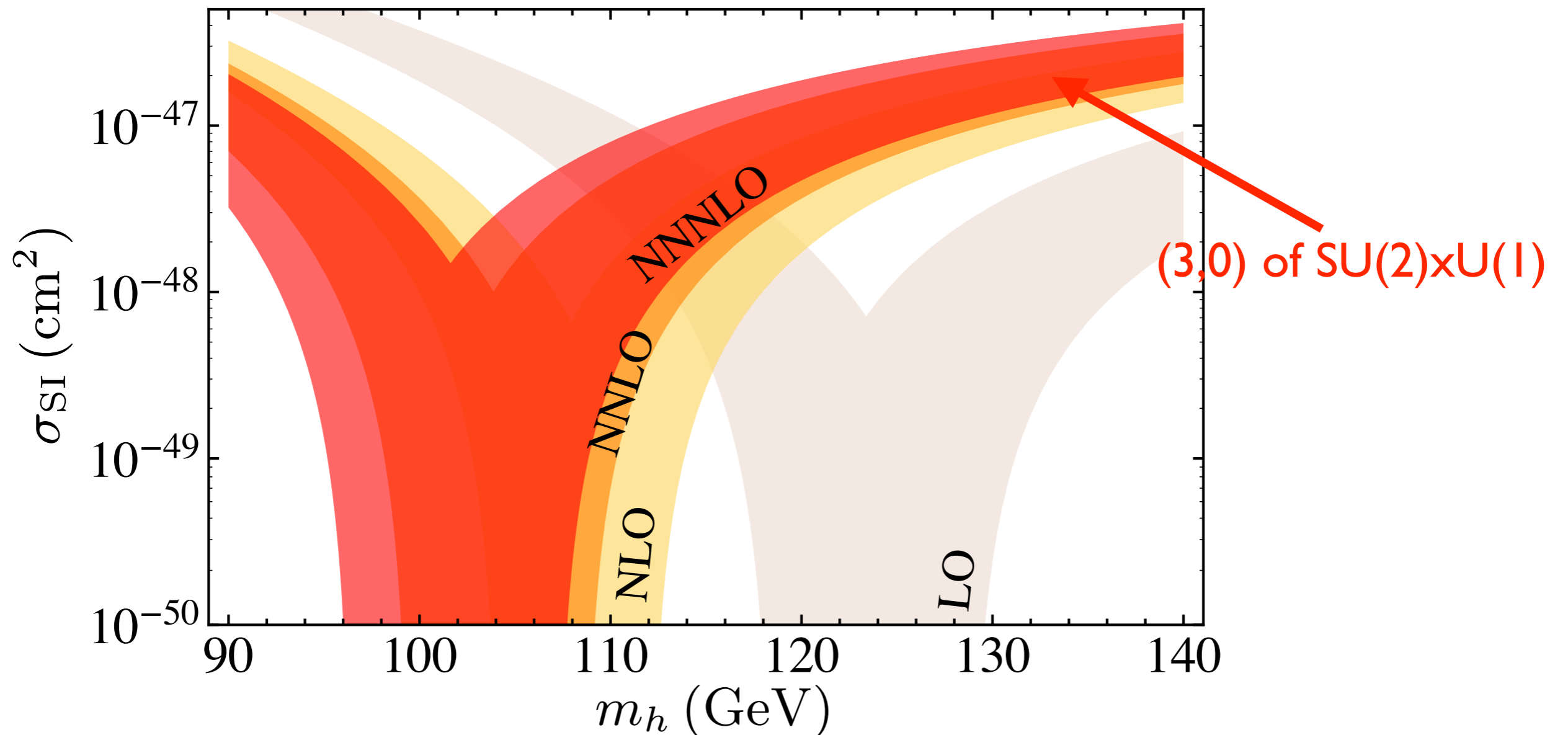
- related phenomenology

*Gluscevic, Gresham, McDermott, Peter 1506.04454*

Novel detector responses possible, especially for low-mass WIMPs

# QCD aspects of WIMP-nucleus scattering

perturbative QCD corrections:



NLO corrections essential for correct order of magnitude

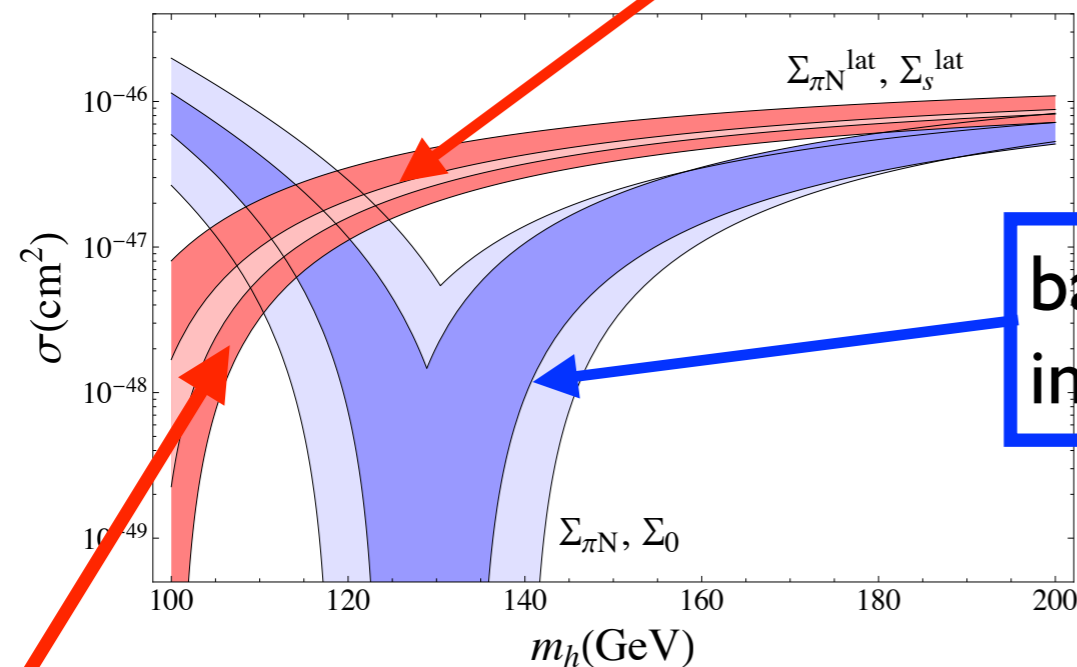
# QCD aspects of WIMP-nucleus scattering

nonperturbative matrix elements: important impact from lattice QCD

lattice QCD inputs

*Durr et al. 1109.4265*

*Junnarkar and Walker-Loud, 1301.1114*



baryon spectroscopy inputs

*Borasoy and Meissner, hep-ph/9607432*

*Pavan et al. hep-ph/0111066*

(3,0) of SU(2)xU(1)

- recent work in  $n_f=2$  chiral perturbation theory

*Crivellin, Hoferichter, Procura (2014)*

*Hoferichter, Ruiz de Elvira, Kubis, Meissner (2015)*

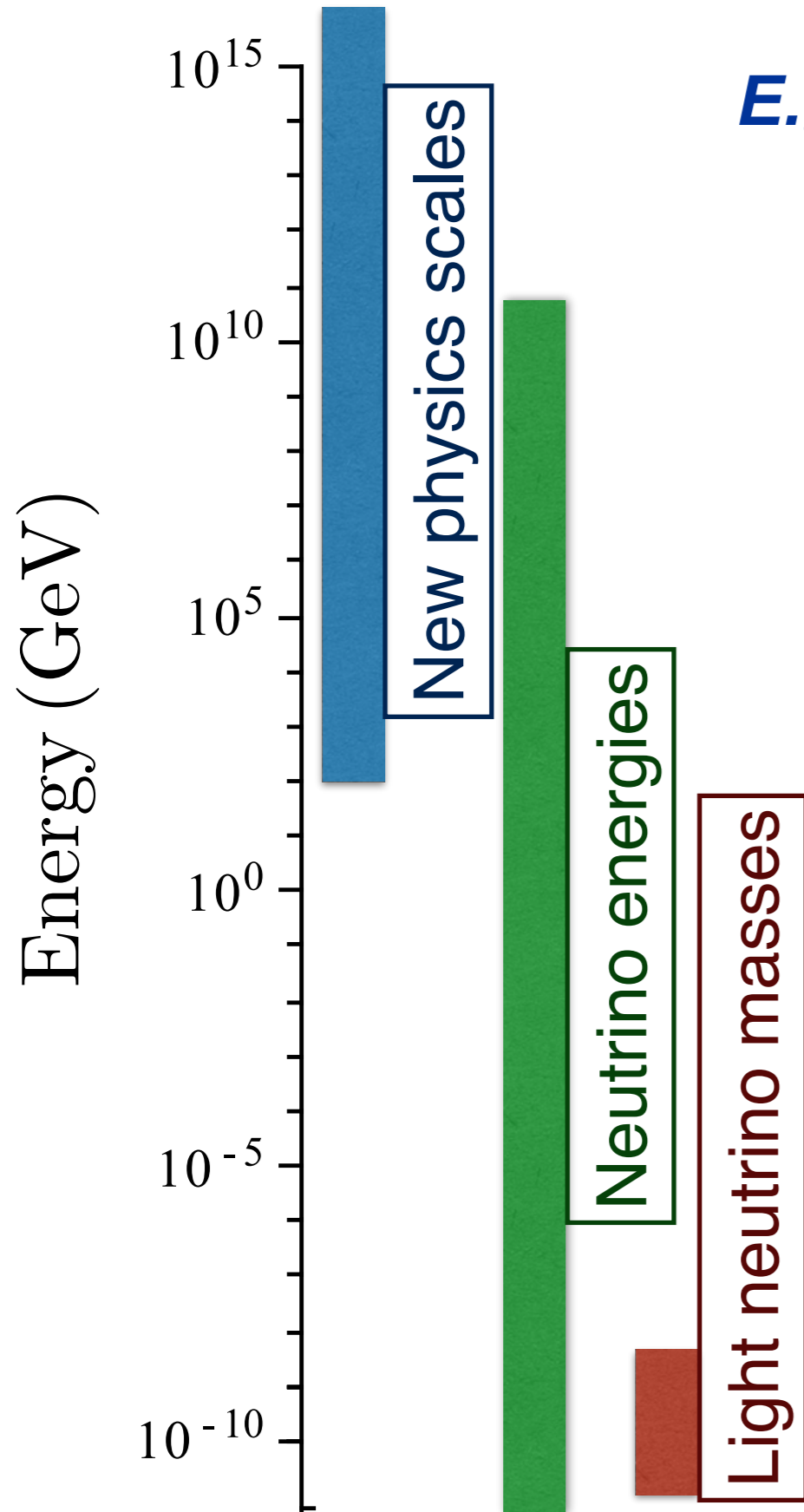
## Part 2:

# The particle physics of neutrino cross sections

## DM $\leftrightarrow$ neutrinos

- Compelling physics problems
- Particle/nuclear interplay
- Lattice QCD providing critical inputs

# Neutrino physics covers a vast range of energy scales

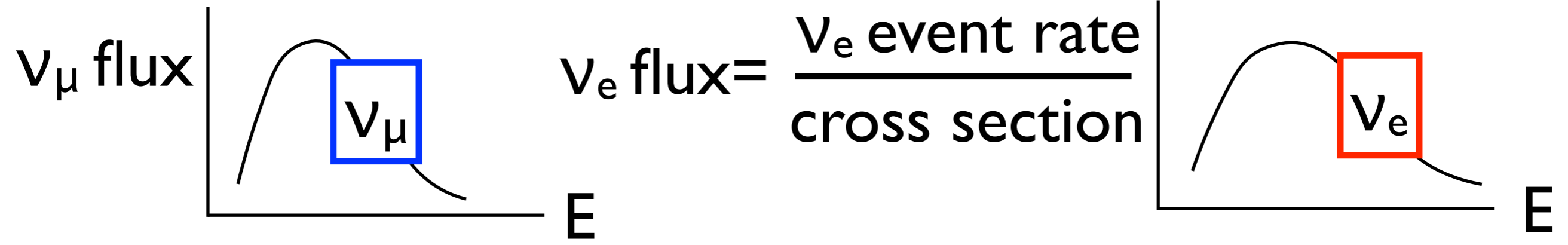


*E.g., at DUNE, NOvA, MINOS, T2K, ...*

- Probing  $\Lambda_{\text{New Physics}} \sim 10^{15} \text{ GeV}$
- Neutrino energies  $\sim \text{GeV}$
- Neutrino masses  $\sim 10^{-10} \text{ GeV}$

*Exploiting this window on high scale physics demands a dedicated theory effort*

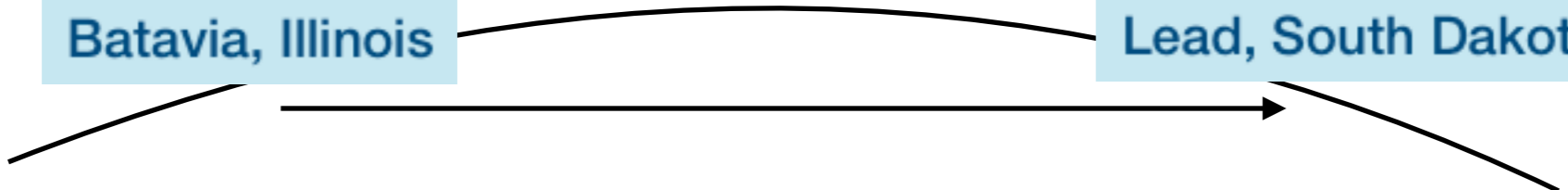
# probability of $\nu_\mu \rightarrow \nu_e \Rightarrow$ fundamental neutrino properties



E.g. DUNE

**FERMILAB**  
Batavia, Illinois

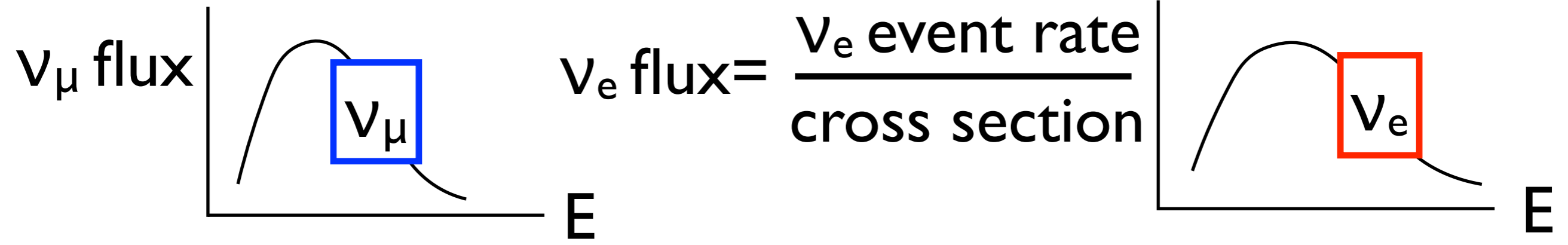
**SANFORD LAB**  
Lead, South Dakota



Cross section translates observed event rate to  $\nu_e$  appearance prob.



probability of  $\nu_\mu \rightarrow \nu_e \Rightarrow$  fundamental neutrino properties



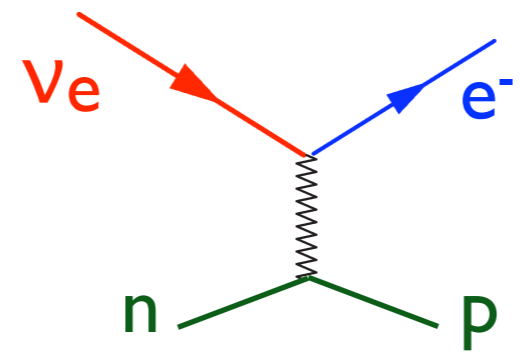
E.g. DUNE

FERMILAB  
Batavia, Illinois

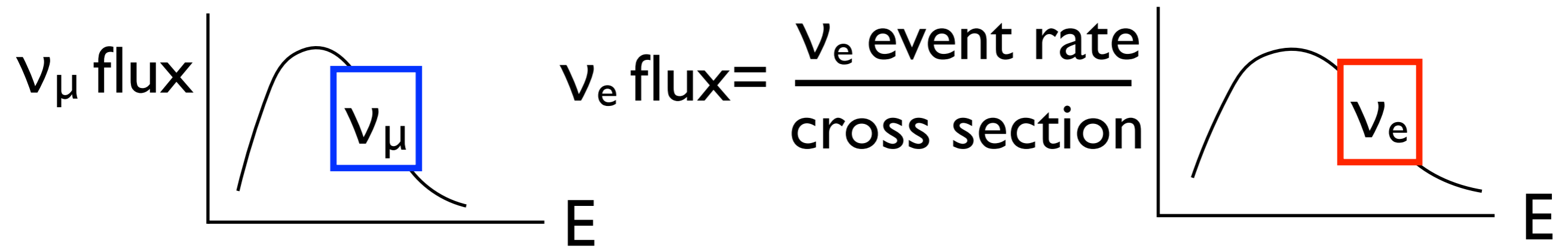
SANFORD LAB  
Lead, South Dakota

Cross section translates observed event rate to  $\nu_e$  appearance prob.

*Basic signal process: charged current quasi elastic scattering (large event sample, “reconstructible” neutrino energy, theoretically “clean”)*



probability of  $\nu_\mu \rightarrow \nu_e \Rightarrow$  fundamental neutrino properties



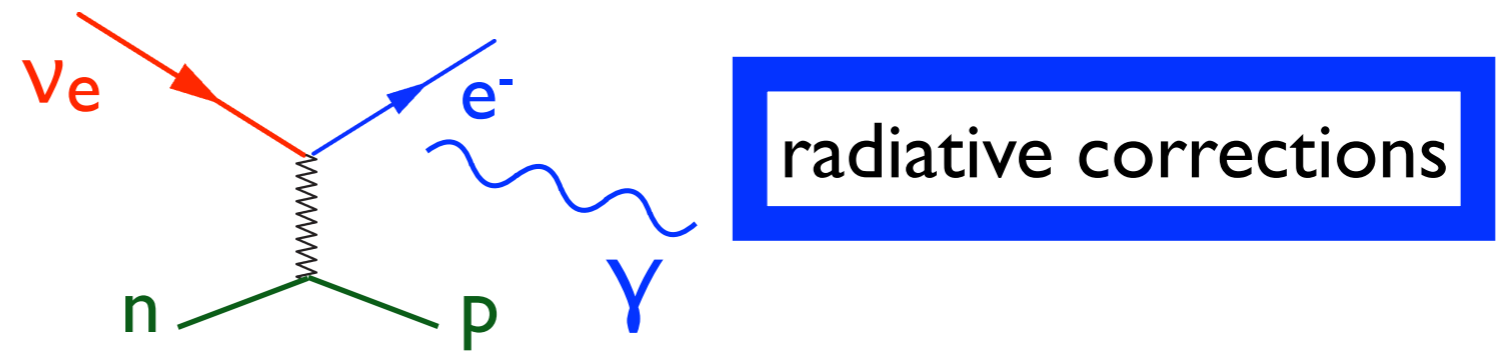
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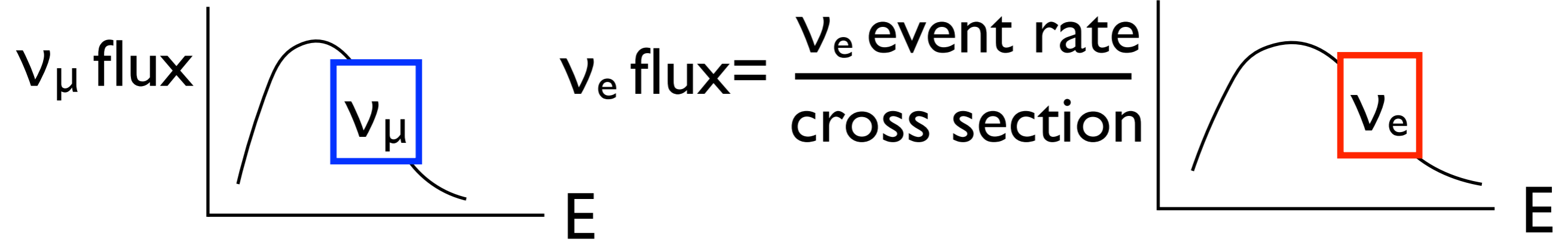
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# probability of $\nu_\mu \rightarrow \nu_e \Rightarrow$ fundamental neutrino properties



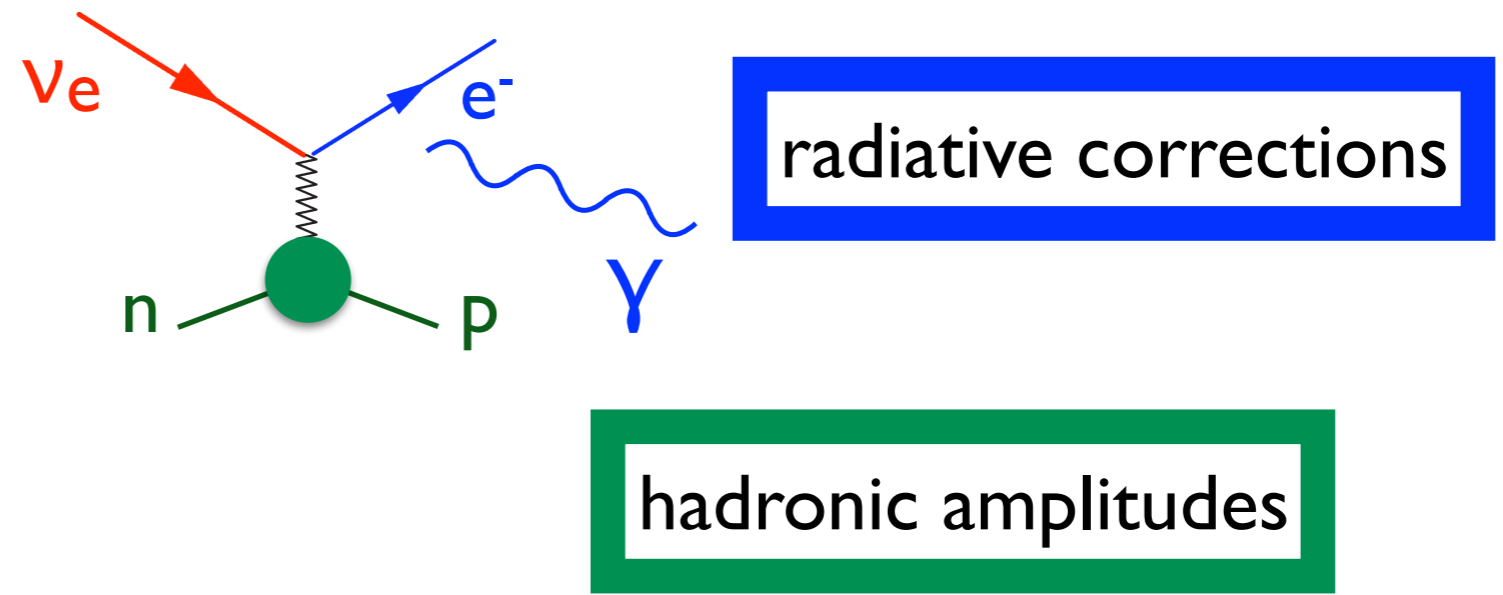
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FERMILAB  
Batavia, Illinois

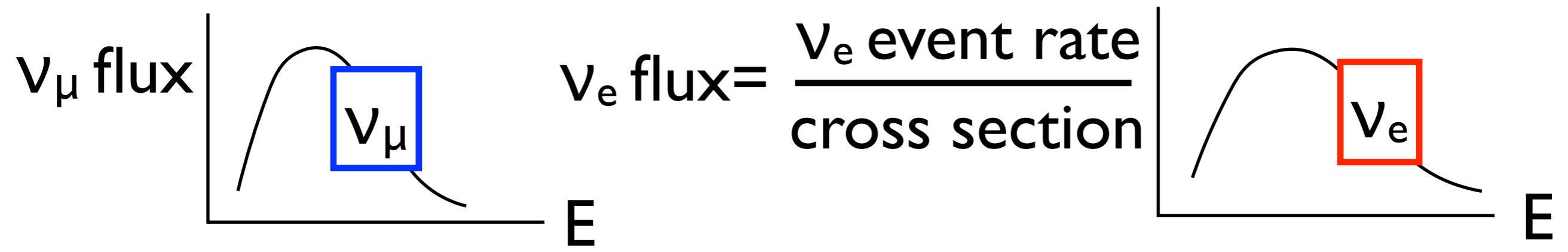
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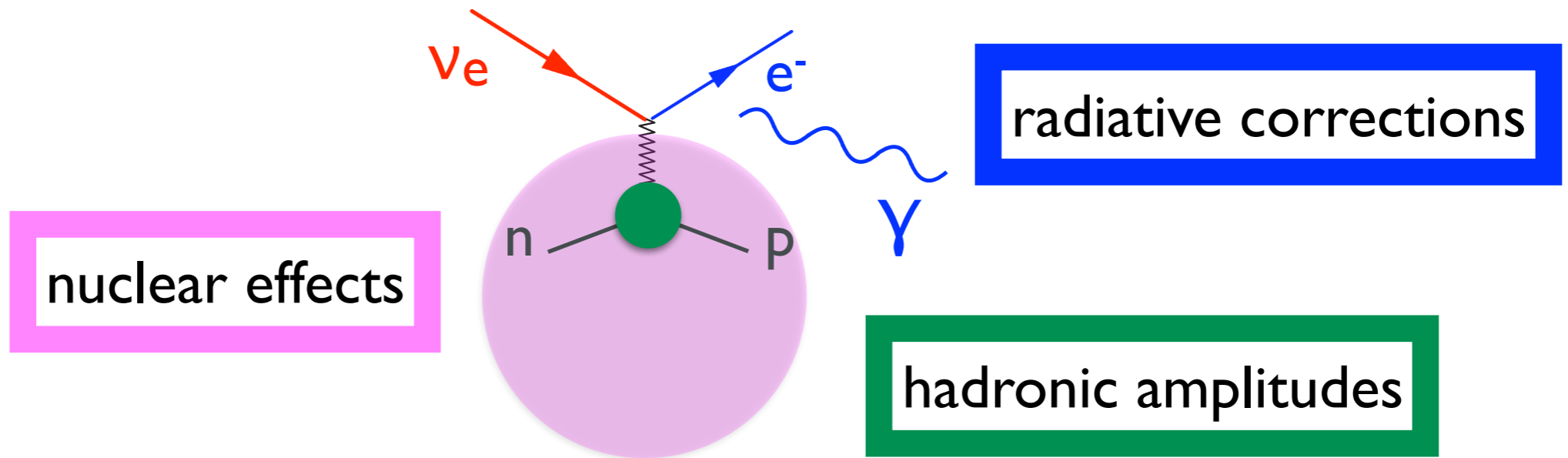
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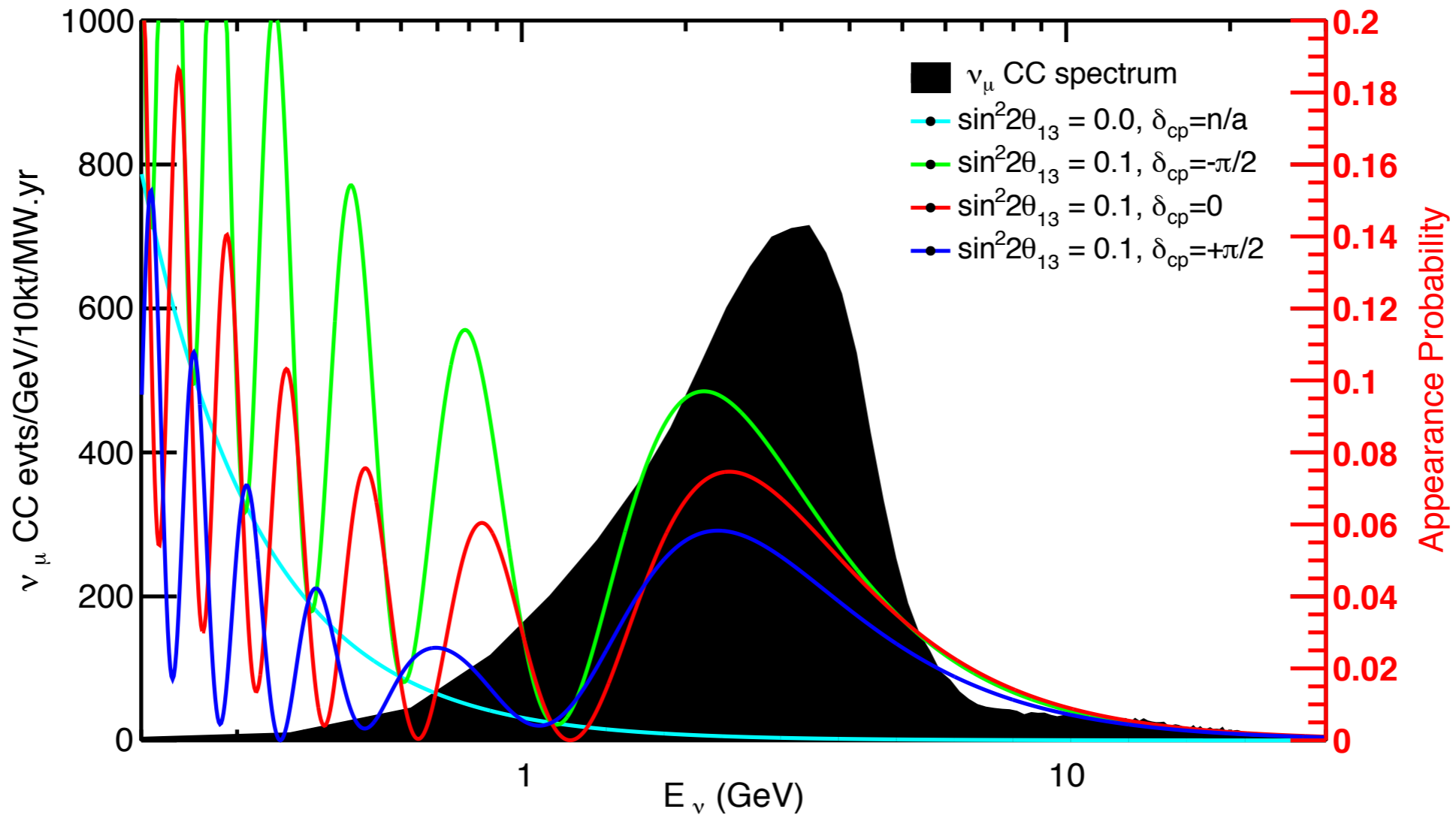
SANFORD LAB  
Lead, South Dakota

Cross section translates observed event rate to  $\nu_e$  appearance prob.

Basic signal process: charged current quasi elastic scattering  
(large event sample, “reconstructible” neutrino energy, theoretically “clean”)



$\nu_\mu$  CC spectrum at 1300 km,  $\Delta m_{31}^2 = 2.4e-03 \text{ eV}^2$

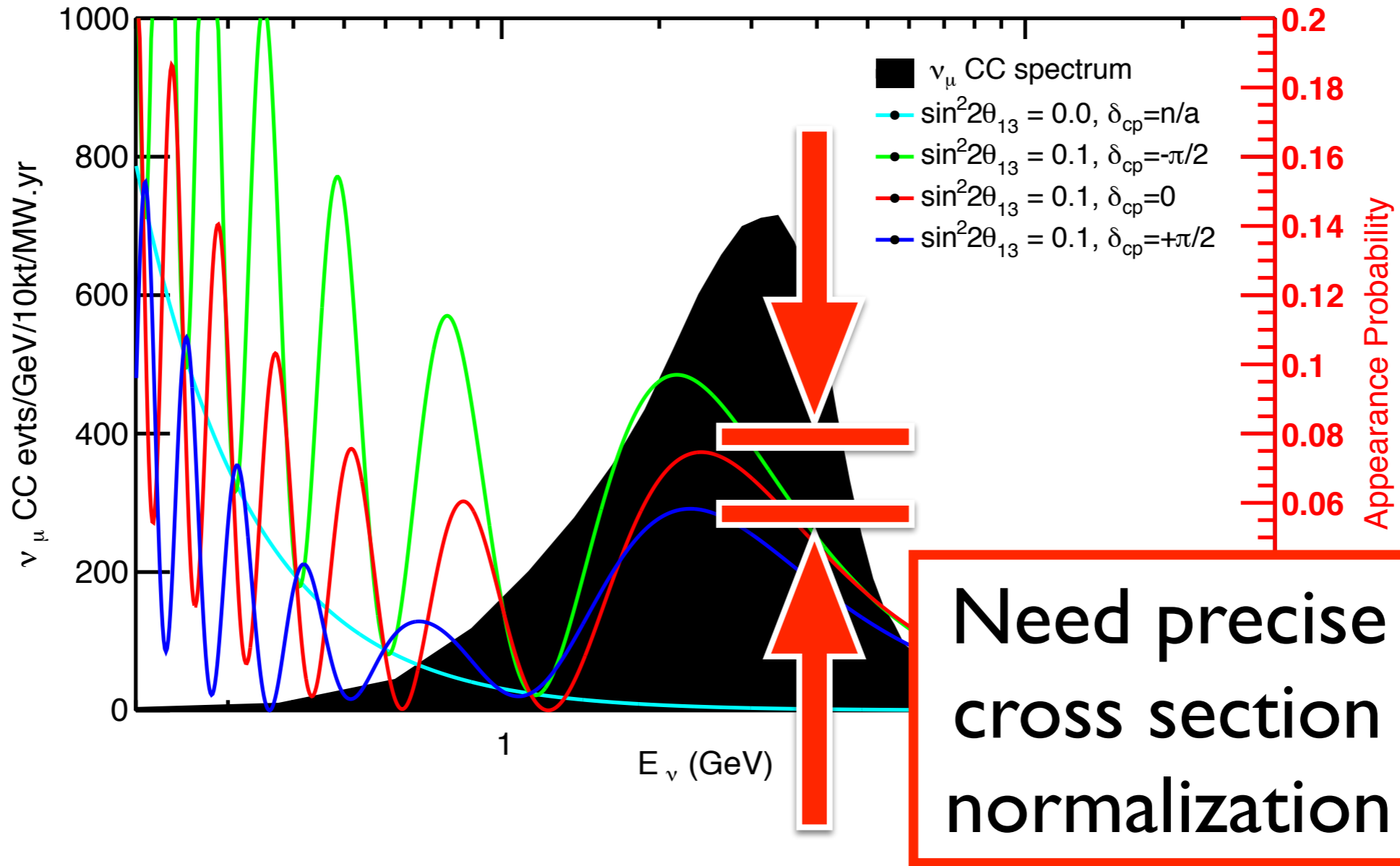


LBNE, 1307.7335

cf. Coloma, Huber et al., 1307.1243, 1311.4506;

Lalakulich and Mosel, 1311.7288

$\nu_\mu$  CC spectrum at 1300 km,  $\Delta m_{31}^2 = 2.4e-03 \text{ eV}^2$

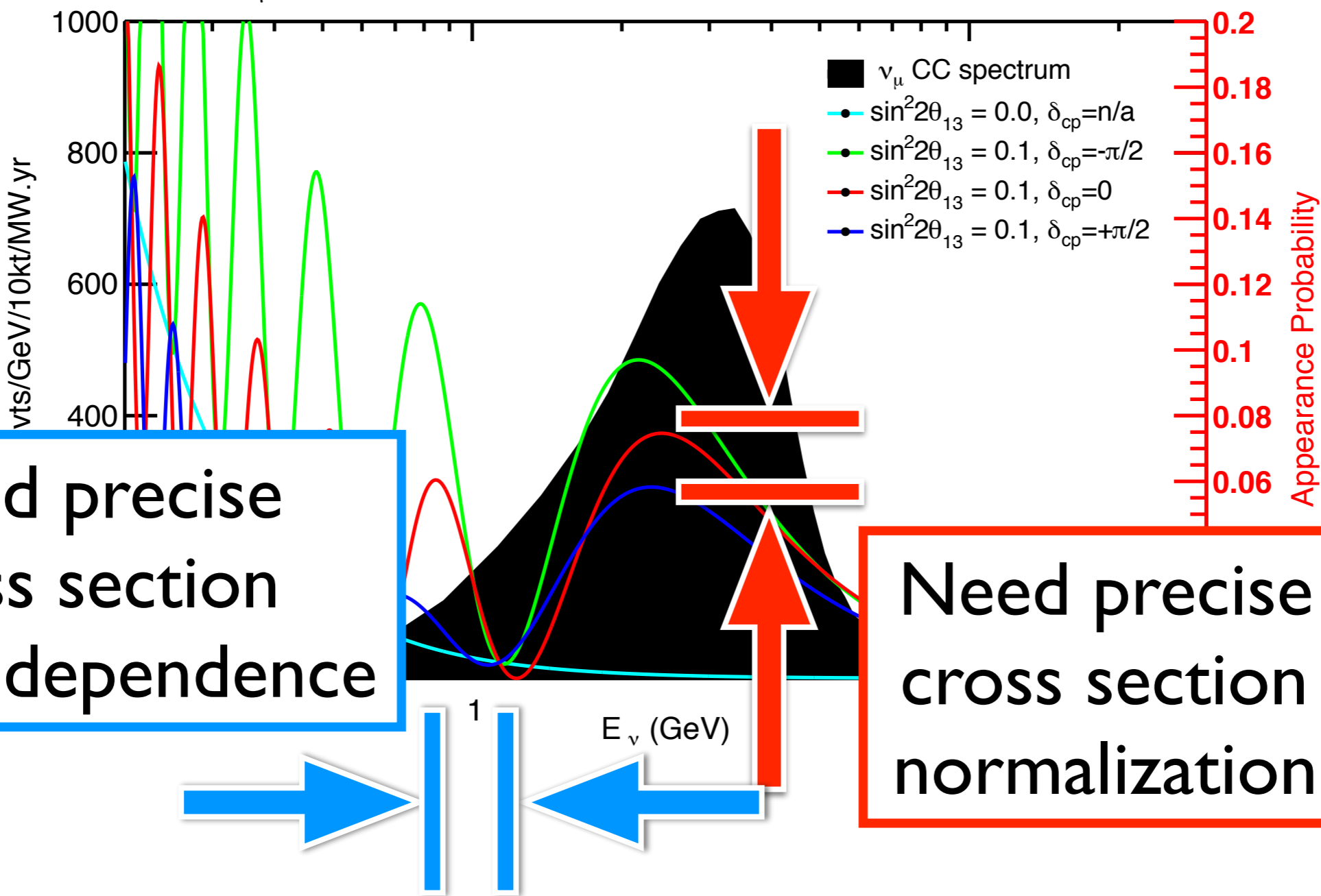


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Need precise cross section energy dependence

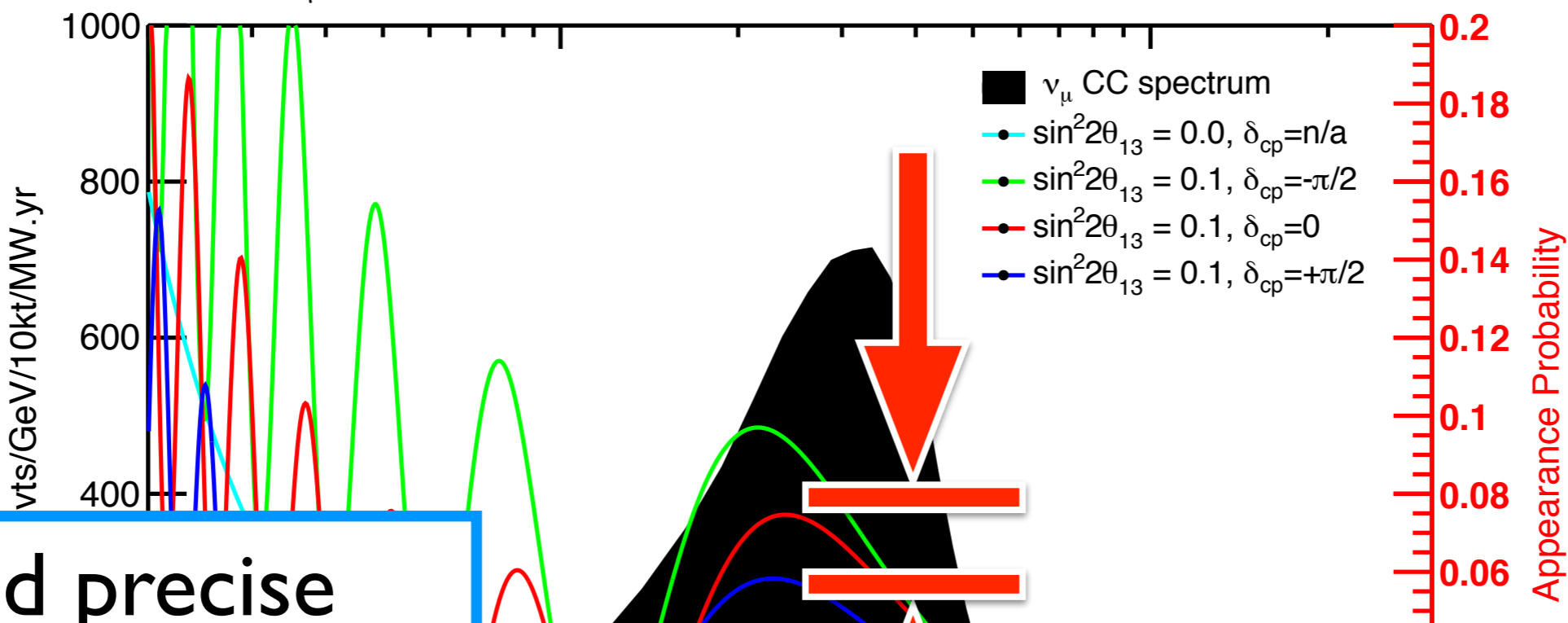
Need precise cross section normalization

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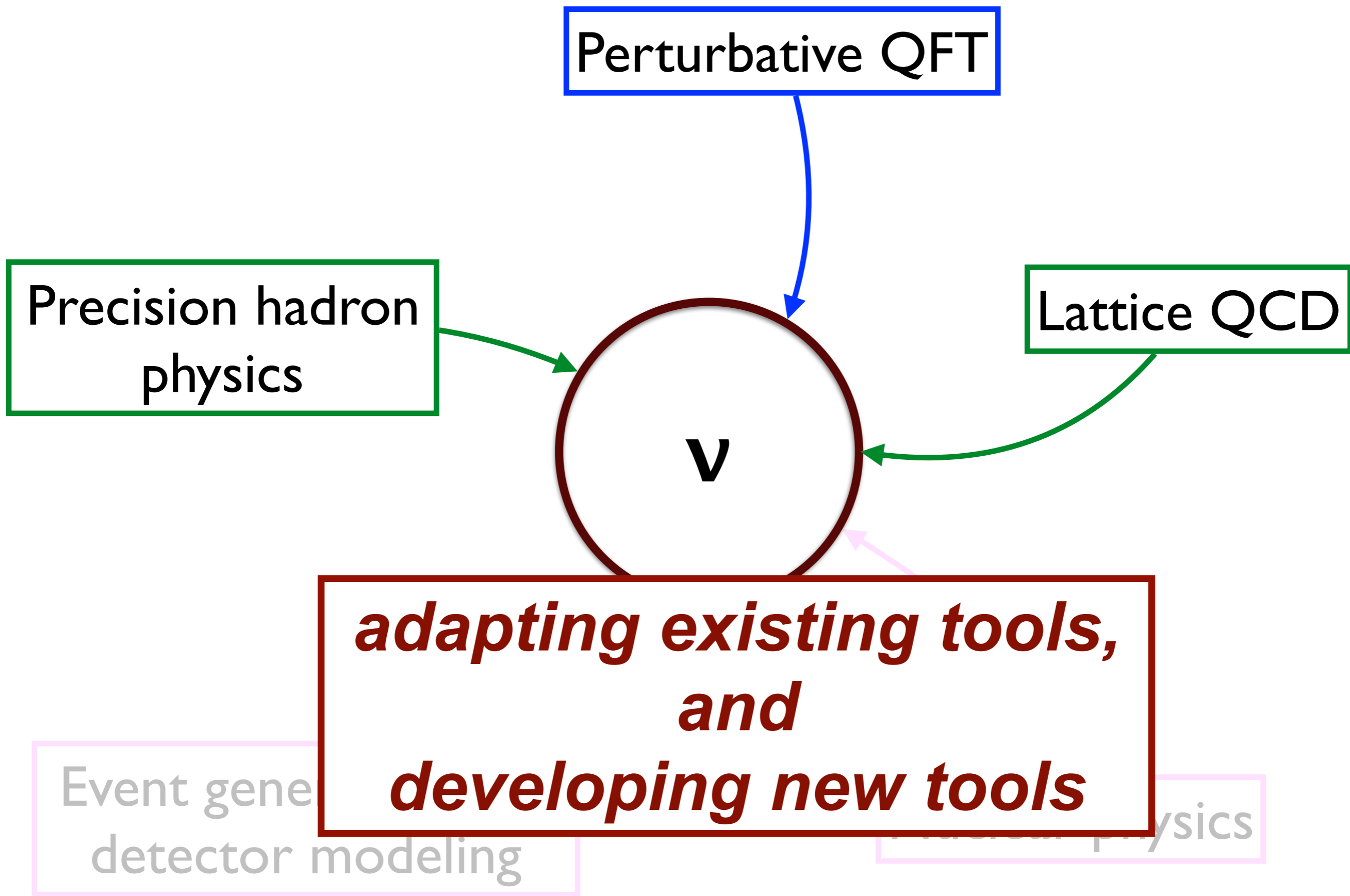
Many related activities and applications, over a wide energy range:

- sterile neutrino searches
- reactor, supernova, astrophysical, solar, cosmological  $\nu$ 's
- proton decay, ...

Focus here on  $\sim$ GeV  $\nu$  cross sections for oscillation experiments



*This is a challenging problem. HEP Theory is...*



*This is a challenging problem. HEP Theory is...*

# ***Connecting with other communities***

Precision hadron  
physics

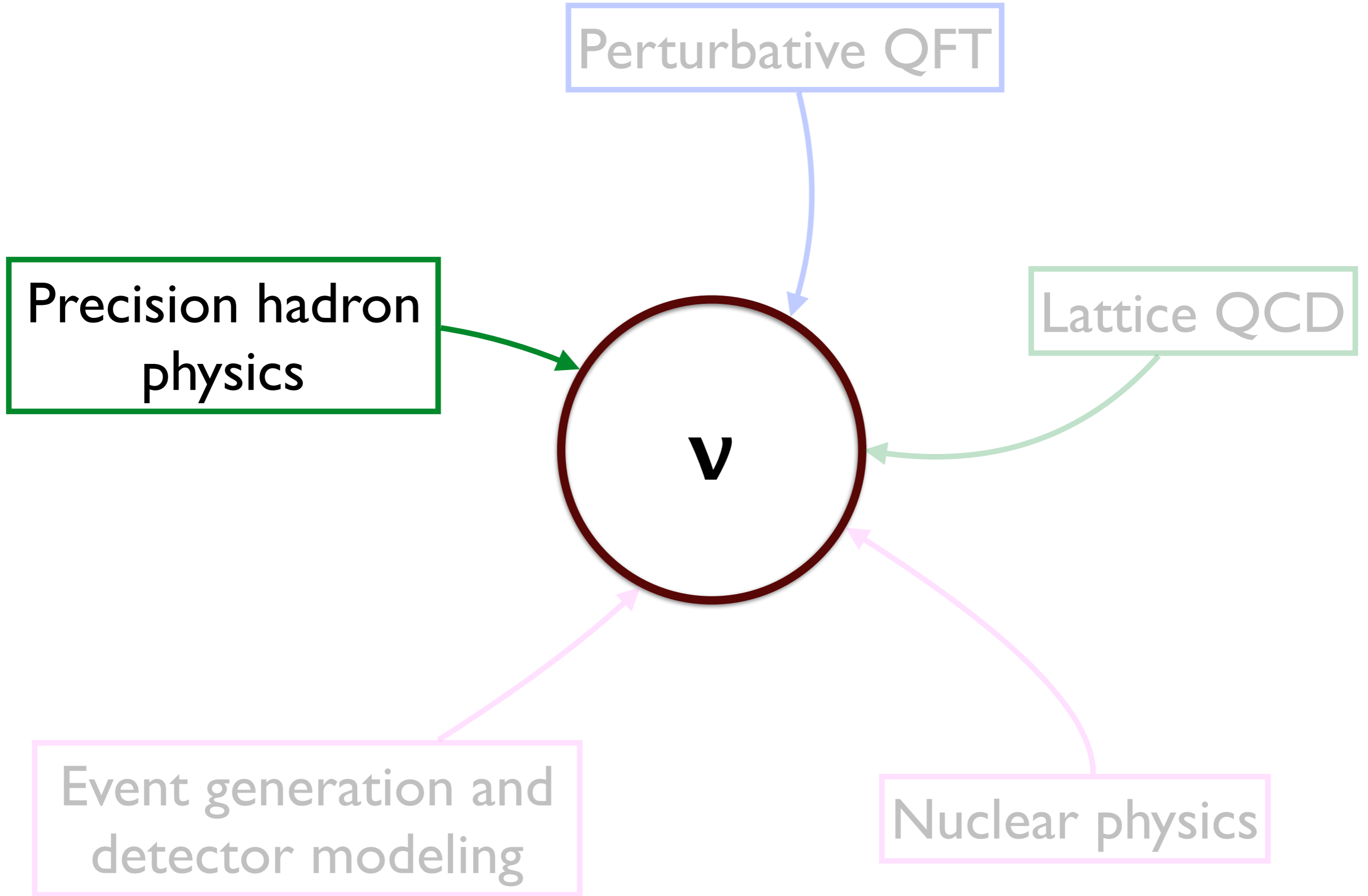
Lattice QCD

**v**

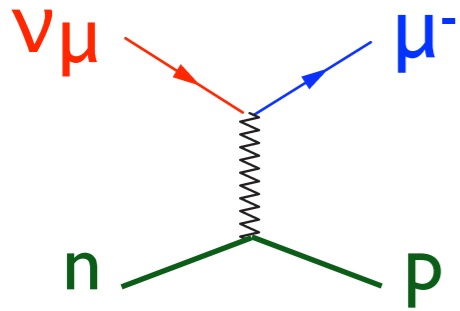
Event generation and  
detector simulation

Nuclear physics

*Begin with elementary targets*



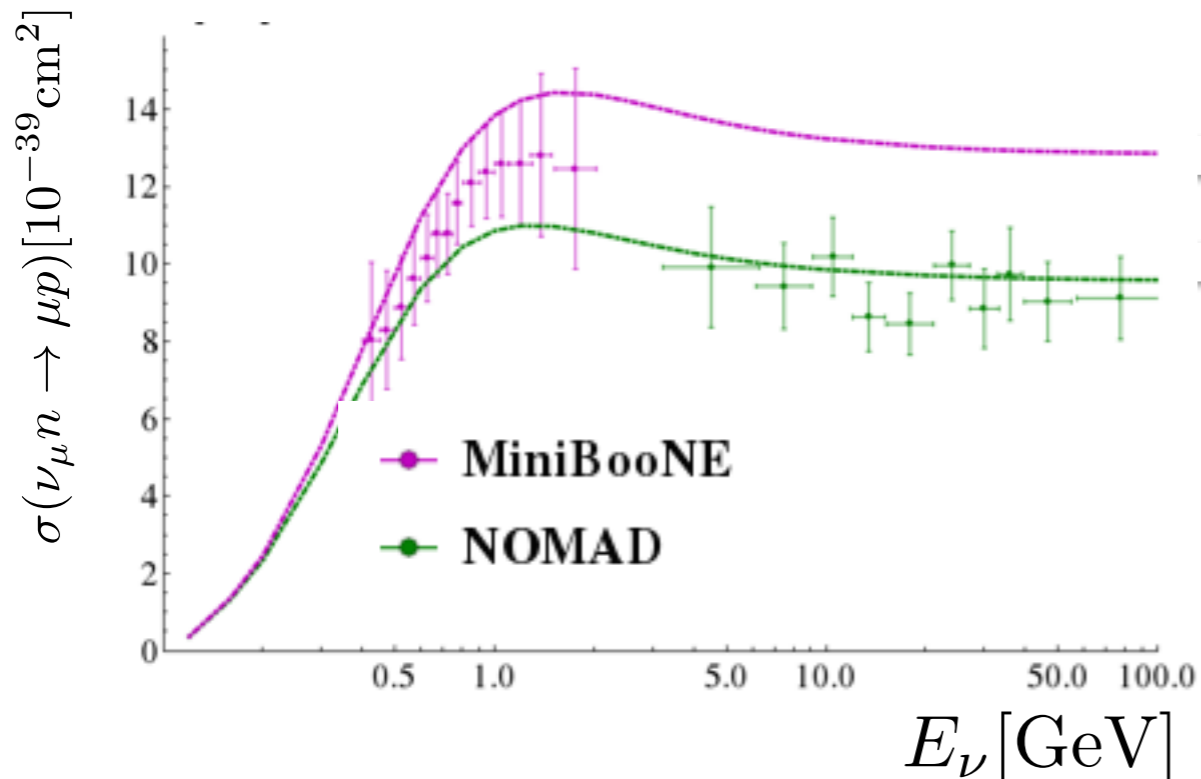
## Return to the basic process



$$\sigma(\nu n \rightarrow \mu p) = |\cdots \cdot F_A(q^2) \cdots|^2$$

poorly known axial-vector form factor

Large uncertainties in nucleon-level amplitudes, the basic building block for complete nuclear cross sections.



**Different nucleon-level cross sections inferred from carbon data**

**But, different:**

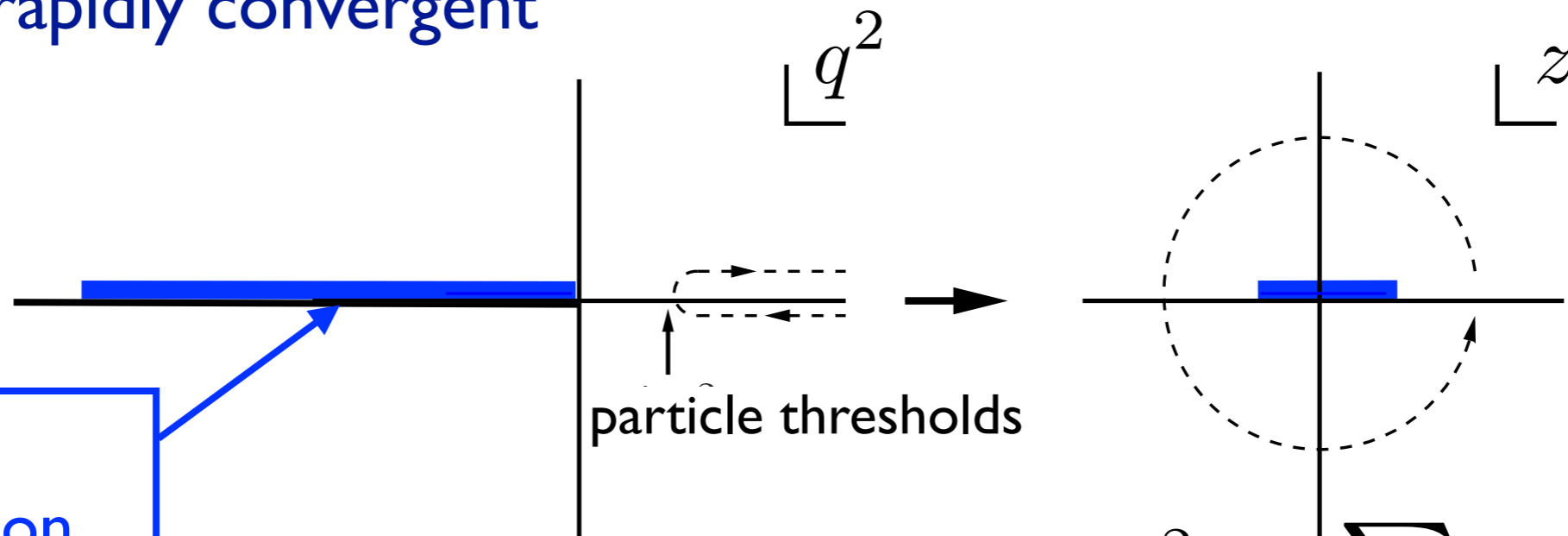
- nucleon form factors
- nuclear corrections

**Need elementary targets to break degeneracies**

# HEP toolbox is being applied to precision lepton-nucleon scattering

Basic problem: don't know form factor shapes, so don't know what we're constraining

Underlying QCD tells us that Taylor expansion in appropriate variable is rapidly convergent



experimental kinematic region

$$F(q^2) = \sum_k a_k [z(q^2)]^k$$

coefficients in rapidly convergent expansion encode nonperturbative QCD

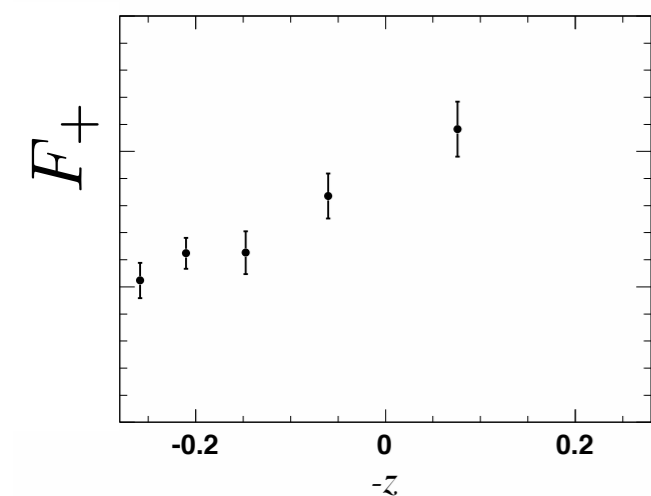
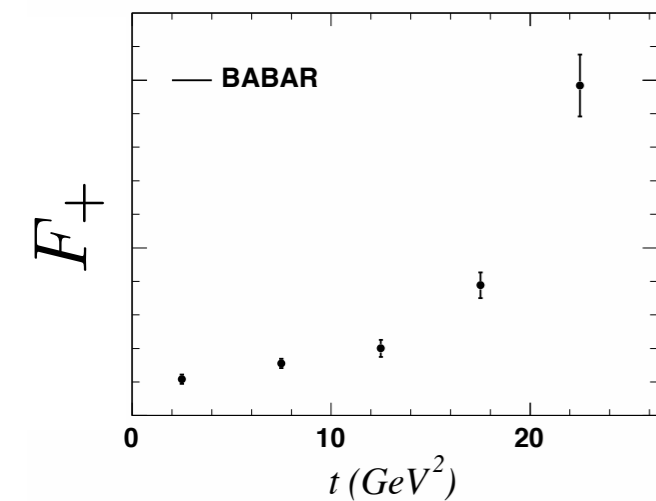
Systematically improvable, quantifiable uncertainties

This approach has been very successful in other processes

E.g.,  $B \rightarrow \pi e \nu$ :  $|z| < 0.28$

$$\frac{d\mathcal{B}}{dq^2} \sim |V_{ub}|^2 |F_+(q^2)|^2$$

*Becher, RJH hep-ph/0509090*



simple shape in z

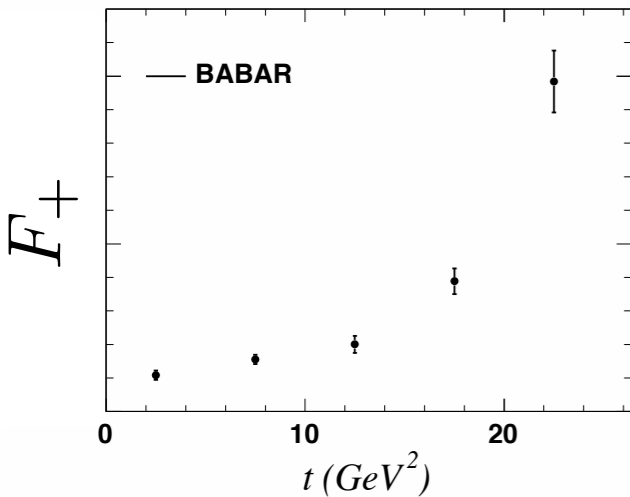
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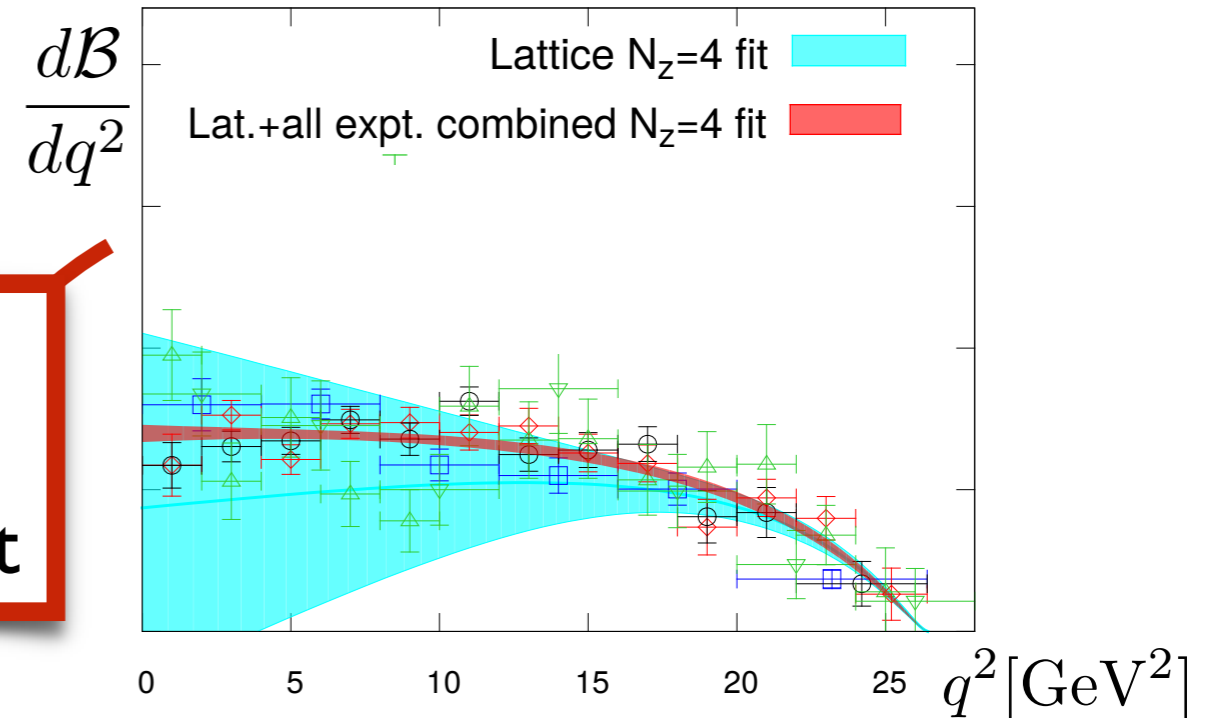
$$\frac{d\mathcal{B}}{dq^2} \sim |V_{ub}|^2 |F_+(q^2)|^2$$

Becher, RJH hep-ph/0509090

Fermilab lattice/MILC 1503.07839

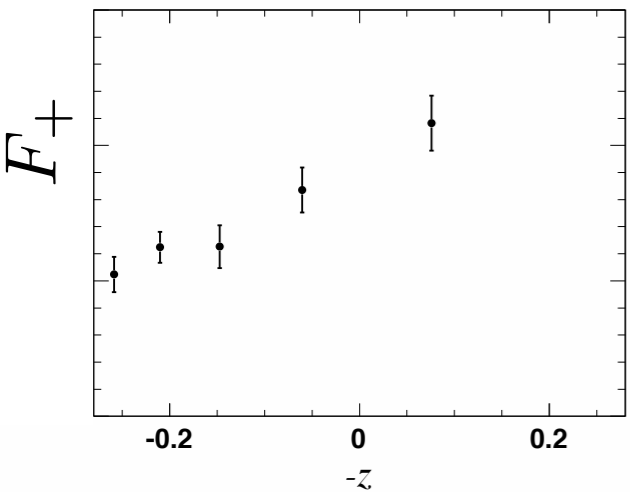


systematic combination of lattice, experiment

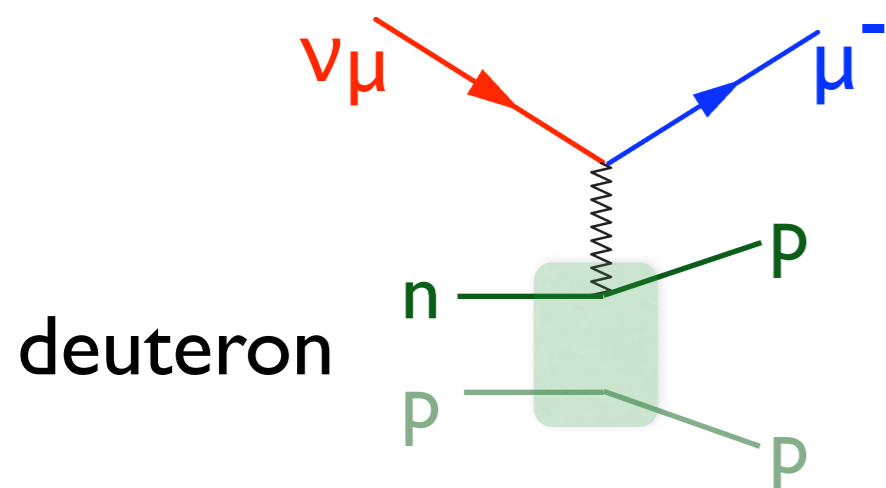


simple shape in z

world's best determination of  $|V_{ub}|$

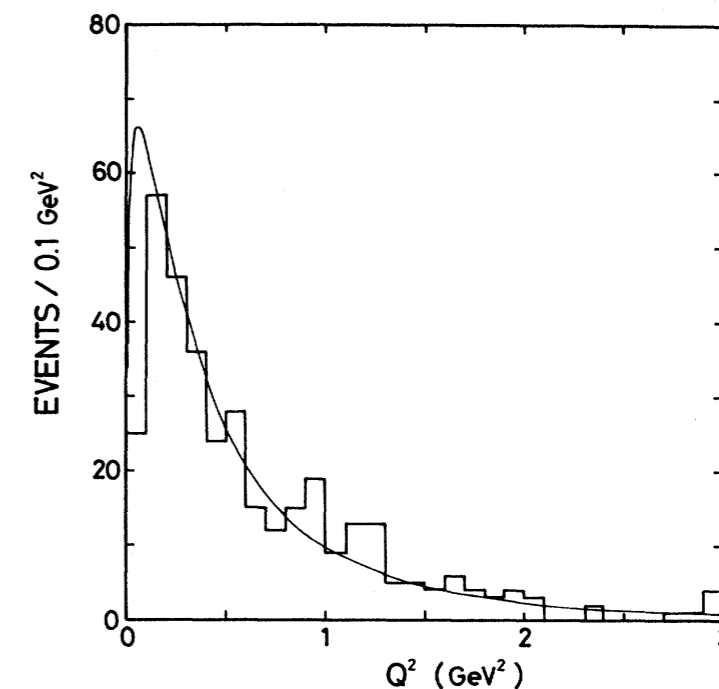


# Adapt these tools for neutrino - hadron scattering



E.g.,  $\nu_\mu + n \rightarrow \mu^- + p$ ,  
 $0 < Q^2 < 3 \text{ GeV}^2$

$|z| < 0.35$



*[Fermilab 15-foot deuterium bubble chamber, PRD 28, 436 (1983)]*

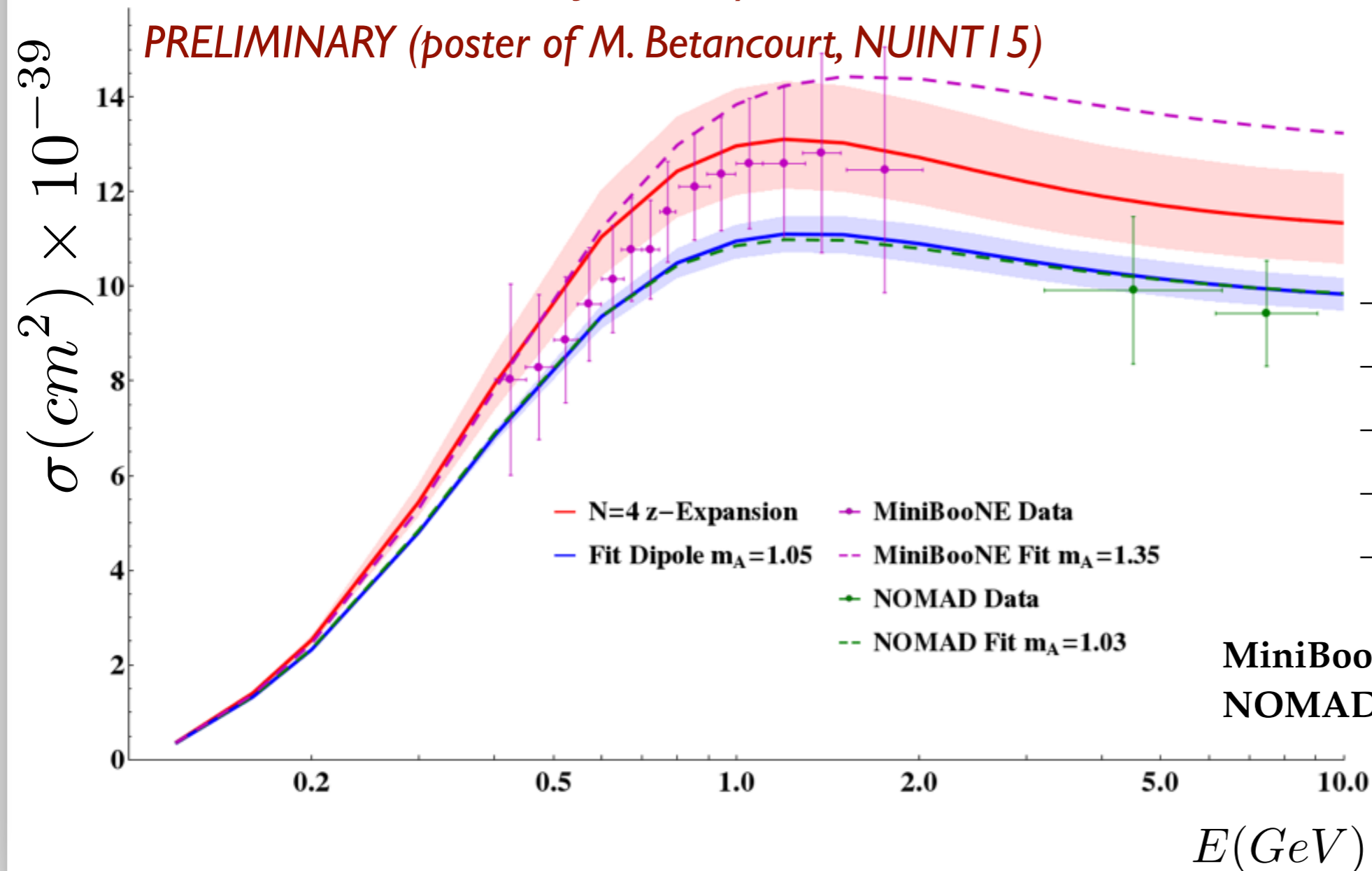
## Revisit deuterium bubble chamber data

- small(-ish) nuclear effects
- small(-ish) experimental uncertainties
- small statistics,  $\sim 3000$  events in world data



M. Betancourt, R. Gran, RJH, A. Meyer,

PRELIMINARY (poster of M. Betancourt, NUINT15)



### Dipole

$\chi^2/\text{DOF}$	168/122
$m_A$	1.05(4)

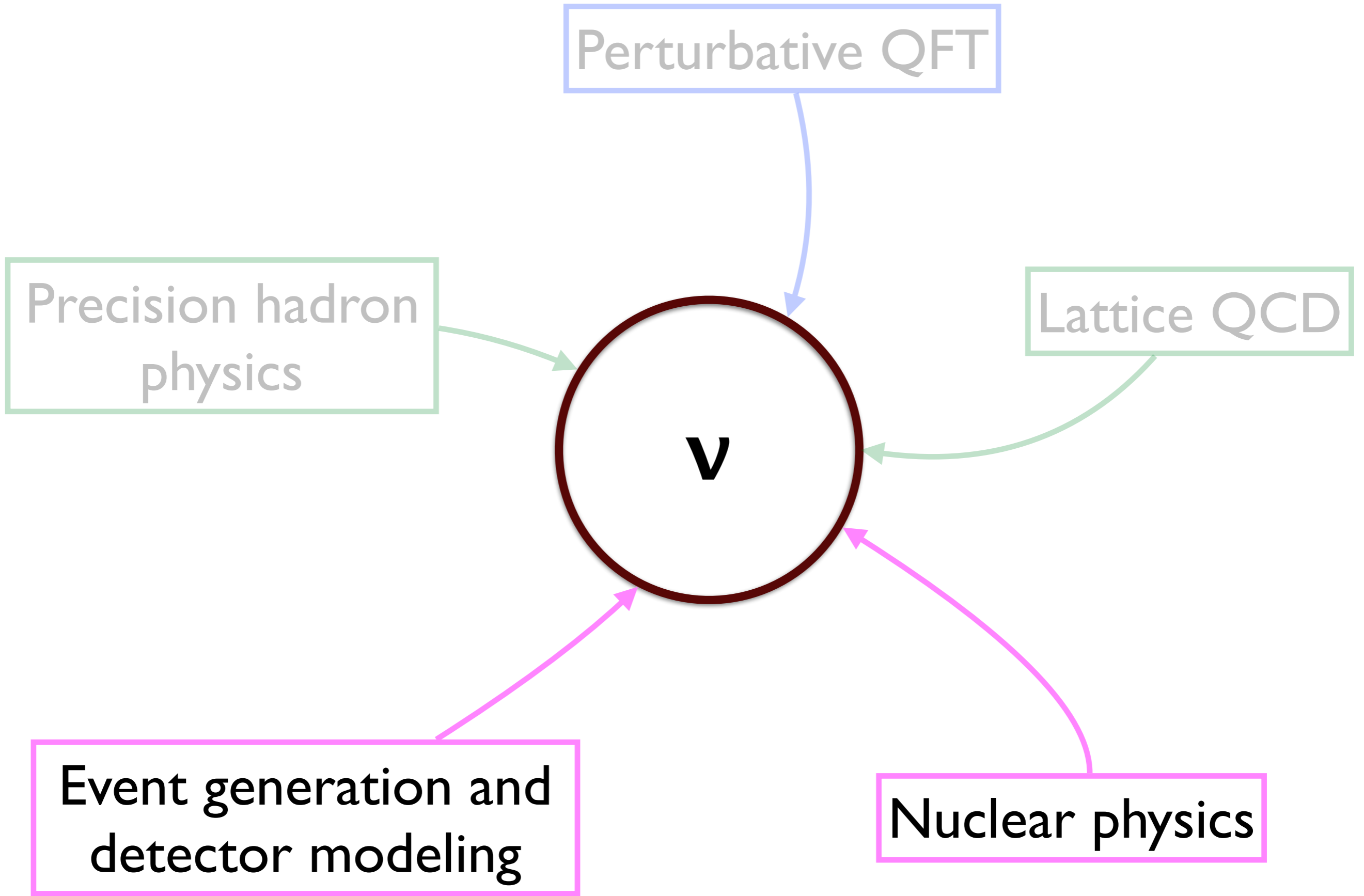
### z-Expansion

$\chi^2/\text{DOF}$	167/119
$a_1$	$2.36^{+0.21}_{-0.19}$
$a_2$	$-0.61^{+0.42}_{-0.39}$
$a_3$	$-5.4^{+1.6}_{-1.7}$
$a_4$	$5.2^{-2.2}_{+2.5}$

MiniBooNE: Phys. Rev. D 81 (2010)

NOMAD: Eur. Phys. J. C 63 (2009)

$\Rightarrow$  **nucleon-level amplitudes and cross sections with complete error budget !**



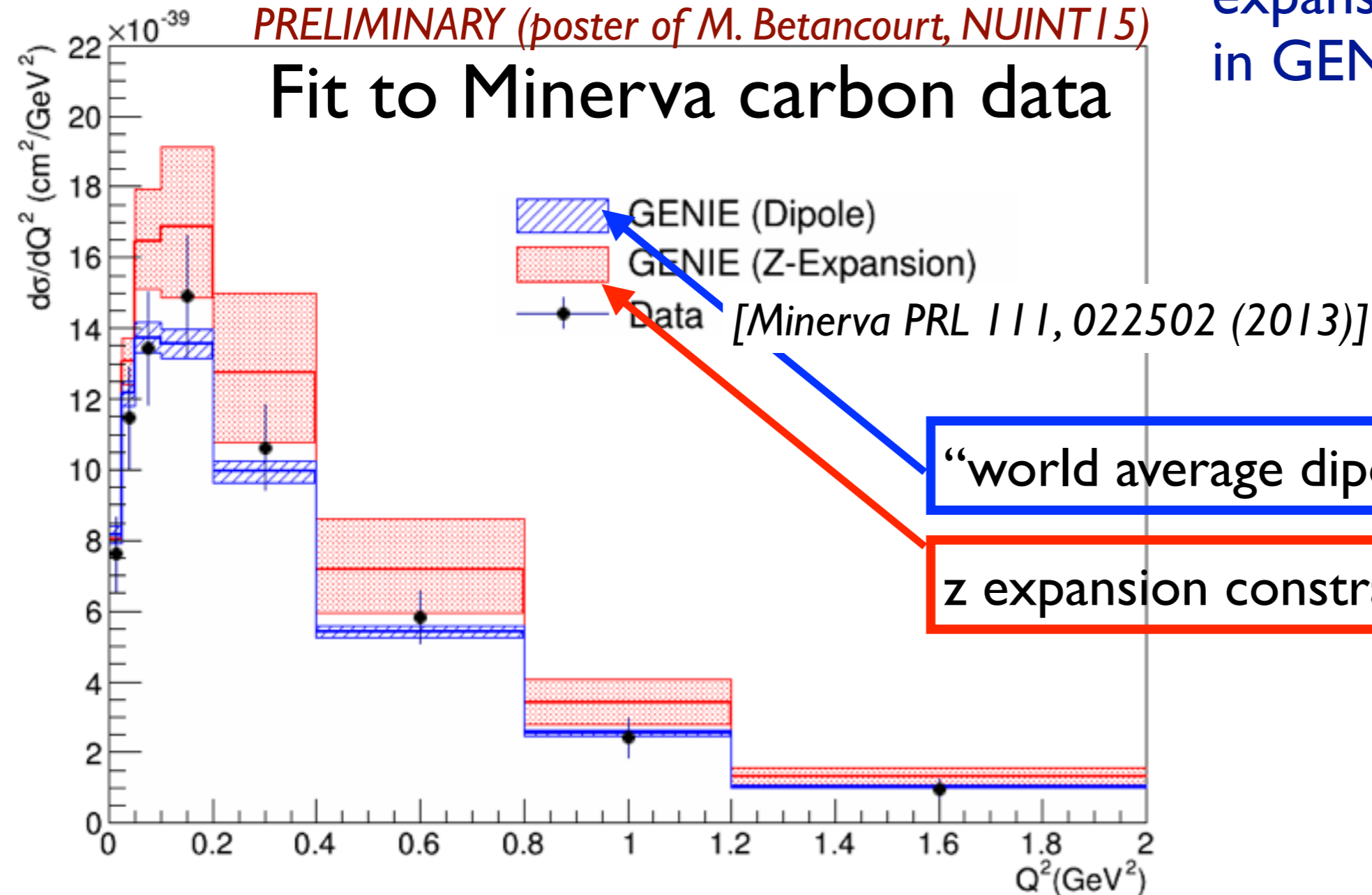
# Propagate errors to nuclear cross sections

New module for z expansion and reweighting in GENIE event generator

A. Meyer

PRELIMINARY (poster of M. Betancourt, NUINT15)

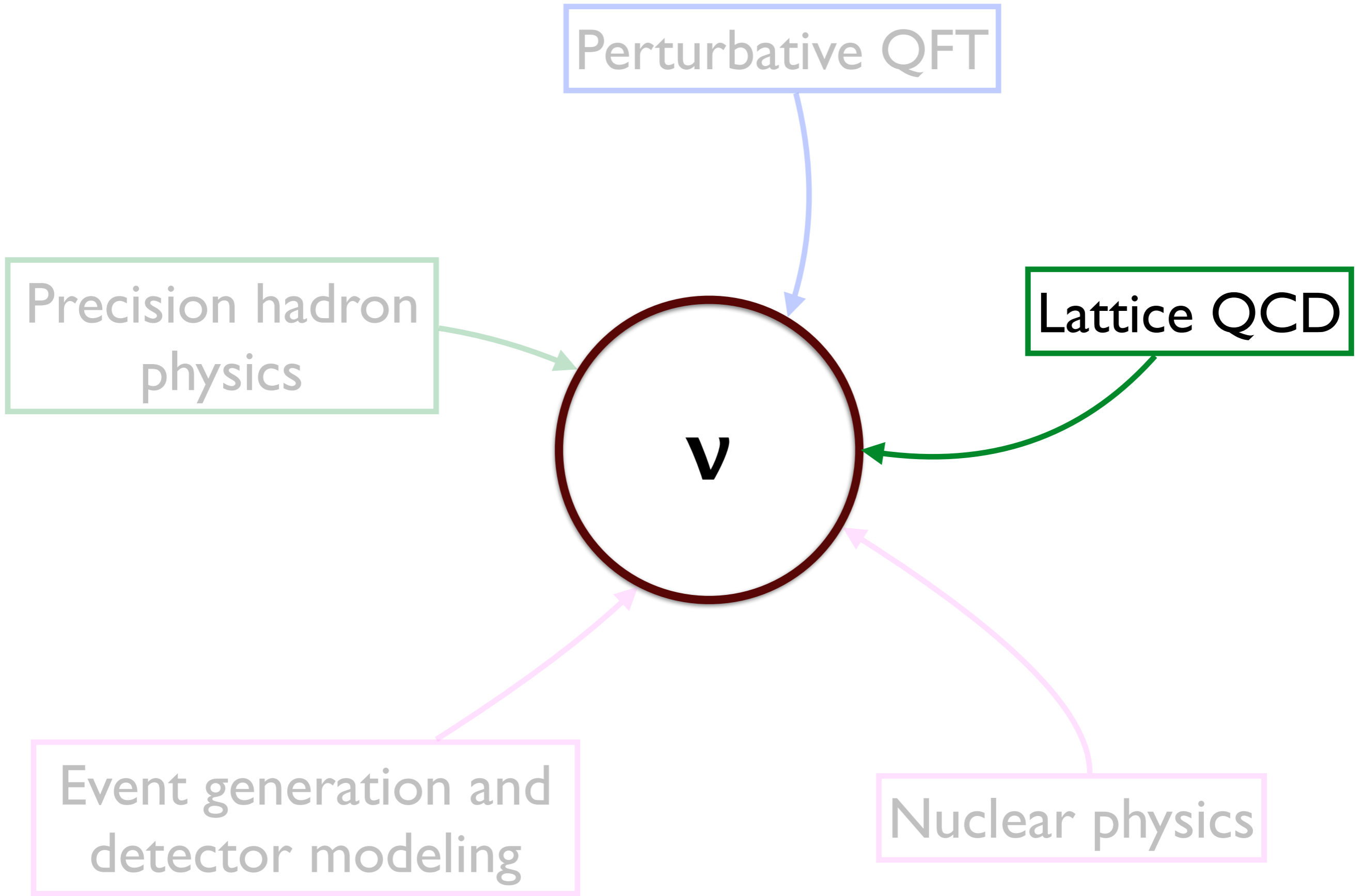
## Fit to Minerva carbon data



⇒ Robust constraints on nuclear parameters (cf. parton distribution function determination at colliders)

(example: backup slide)

⇒ Robust errors propagated to oscillation observables

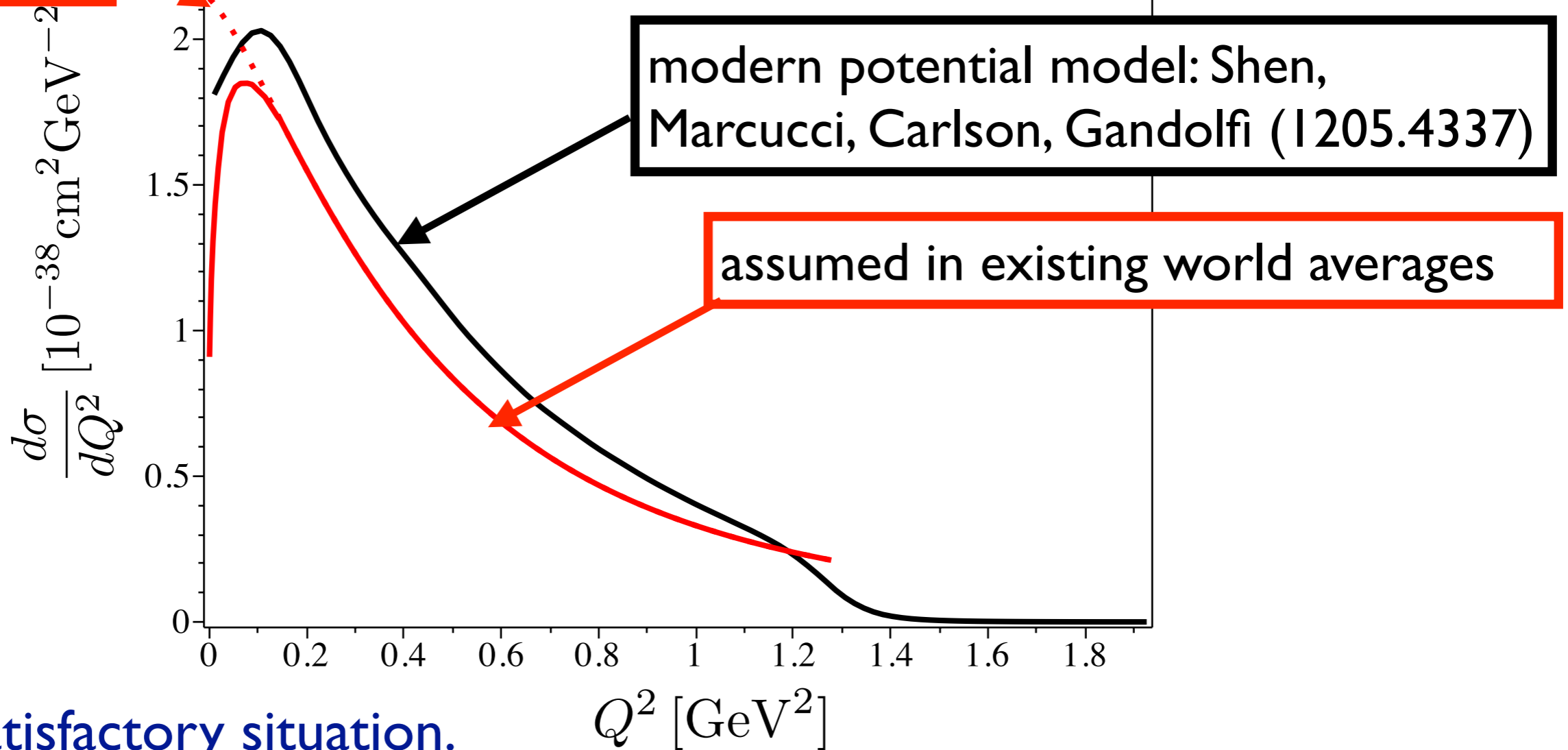


Realistic error bars for  $F_A(q^2)$  from deuterium are significant

Model dependence in deuteron corrections (and possibly issues with experimental systematics)

free neutron

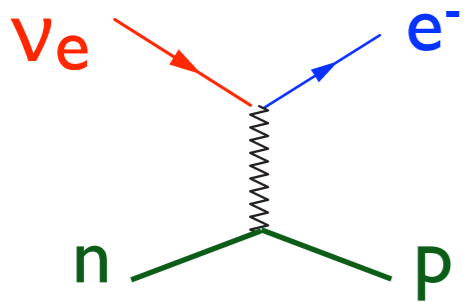
neutrino-deuteron cross section ( $E=1$  GeV)



An unsatisfactory situation.

( Important impacts beyond long baseline  $\nu$ 's:  $0\nu\beta\beta$ , muon capture, ... )

# Lattice QCD can constrain nucleon-level amplitudes from first principles



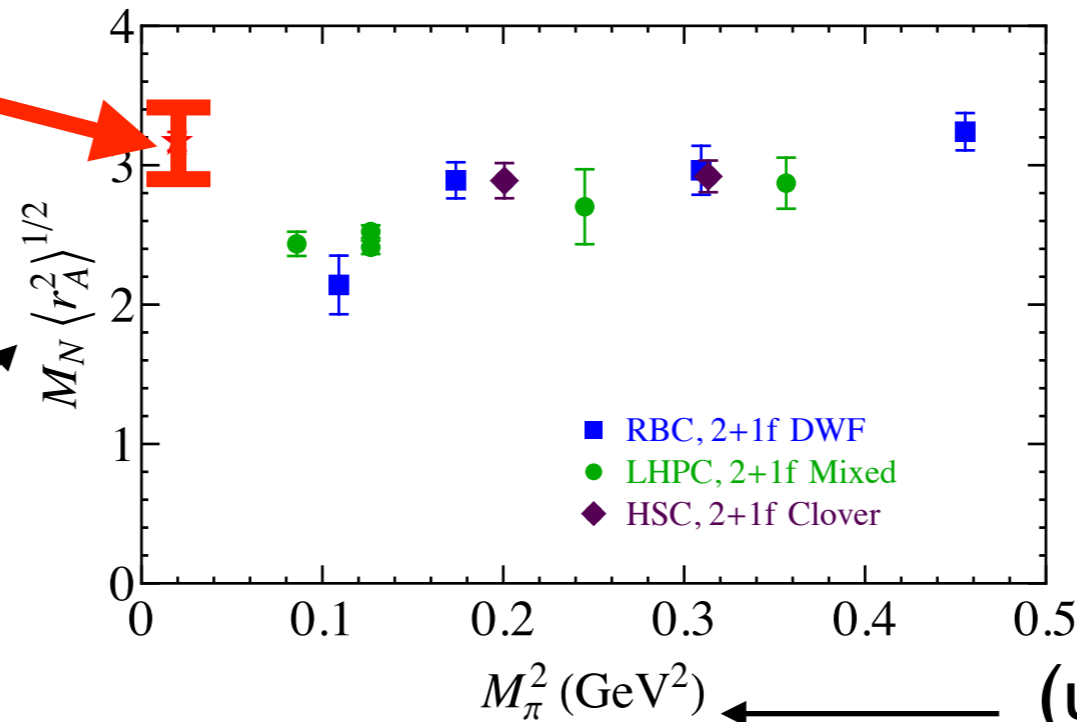
$$\sigma(\nu n \rightarrow ep) = |\cdots \mathbf{F}_A(q^2) \cdots|^2$$

A prime target is the nucleon axial form factor

**deuterium**

illustrative:  
dipole  $m_A = 1.0(1)$

$$\left. \frac{dF_A}{dq^2} \right|_{q^2=0} \propto r_A^2$$



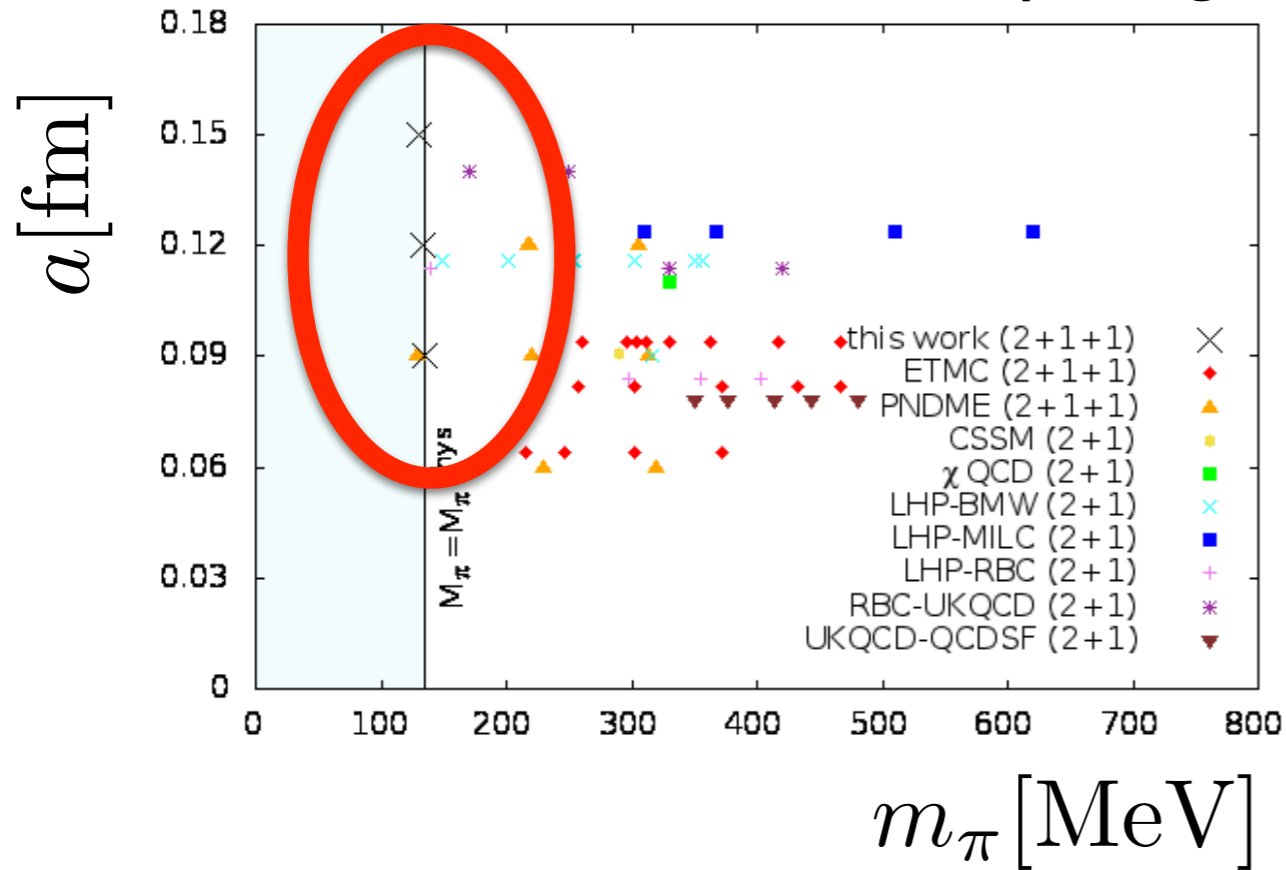
*compilation from  
Lin and Cohen 1104.4319*

(unphysical) pion mass

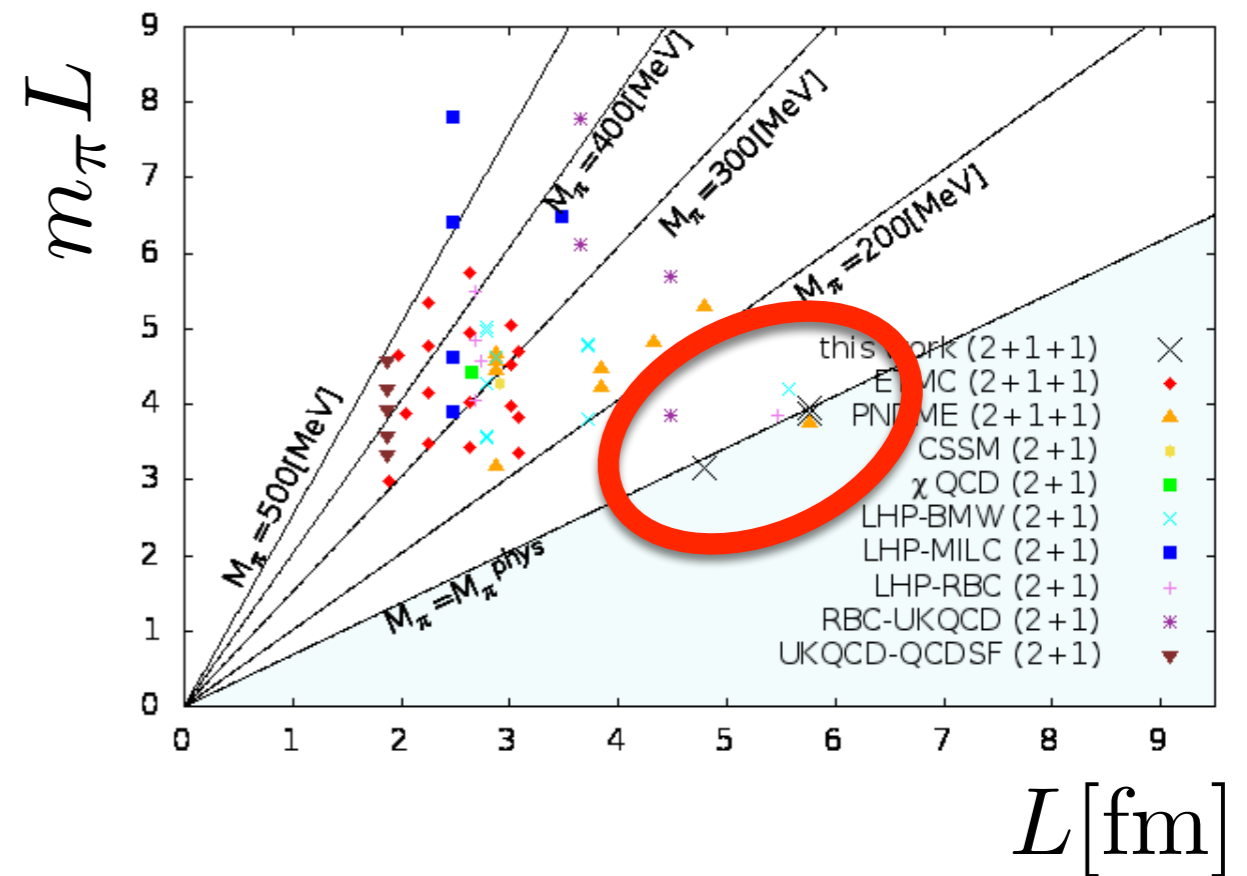
Lattice QCD is poised to compete with deuterium data.

Need lighter quarks, bigger and finer lattices

Pion mass vs. lattice spacing



Lattice Extent vs. Pion Mass



Big lattices, multiple spacings, physical quark masses

Other targets: neutral currents; resonance couplings and form factors; pion final states

Advantages: independent of detector-dependent radiative corrections and nuclear effects (and for lattice QCD: no underground safety hazard)

Perturbative QFT

Precision hadron physics

Lattice QCD

**v**

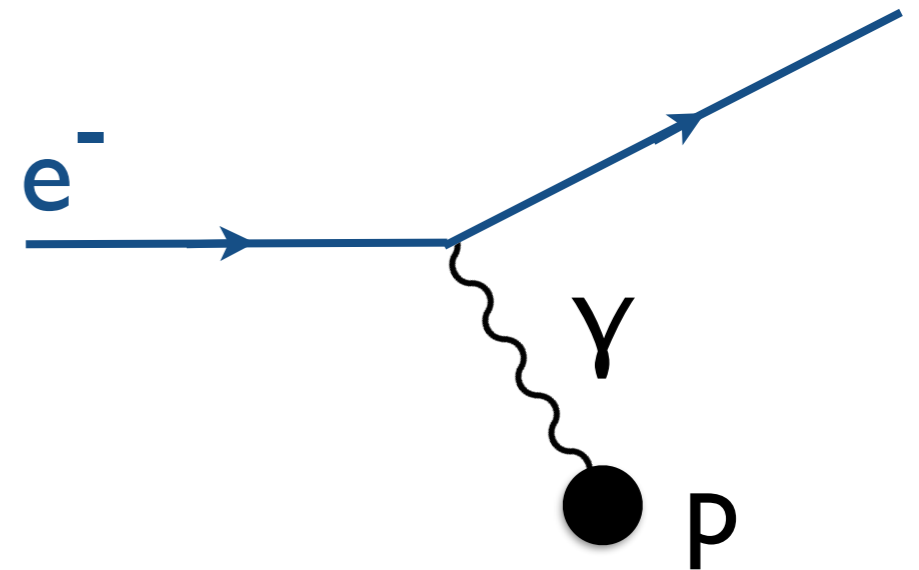
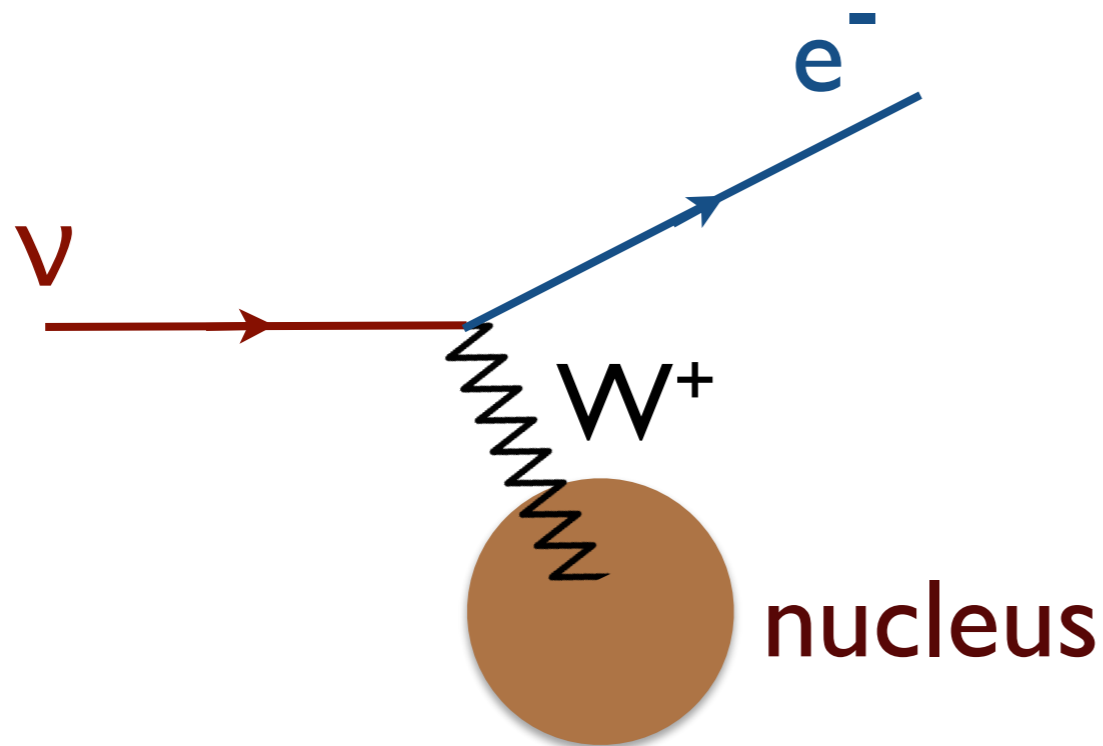
Event generation and detector modeling

Nuclear physics



# Consider related process: elastic electron-proton scattering:

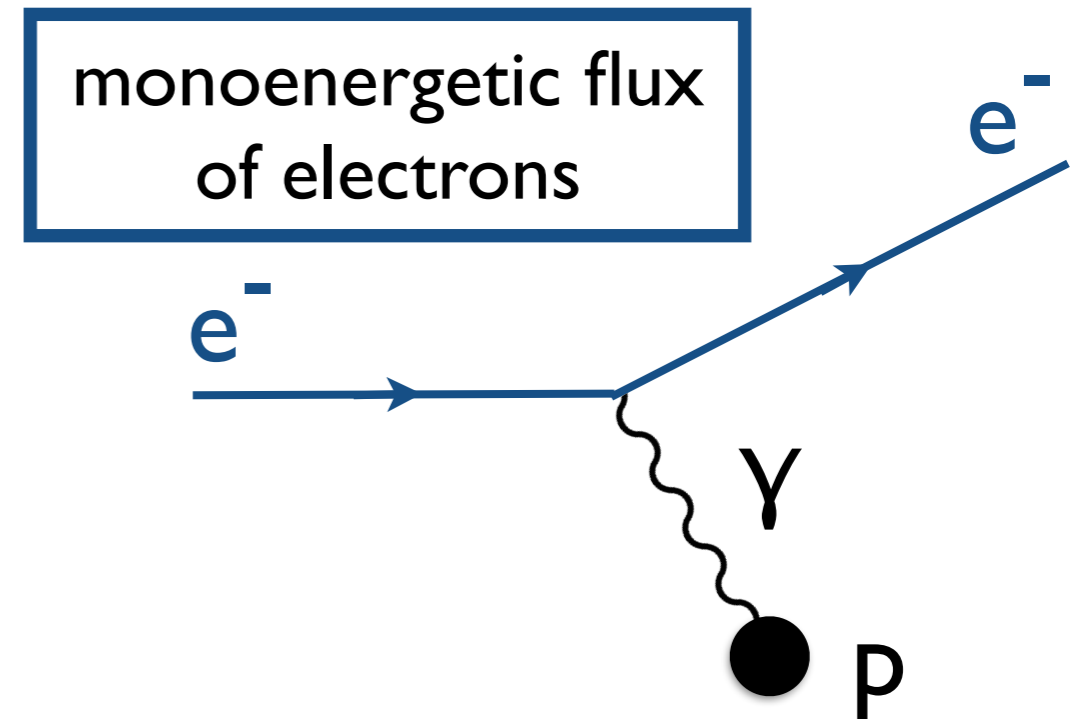
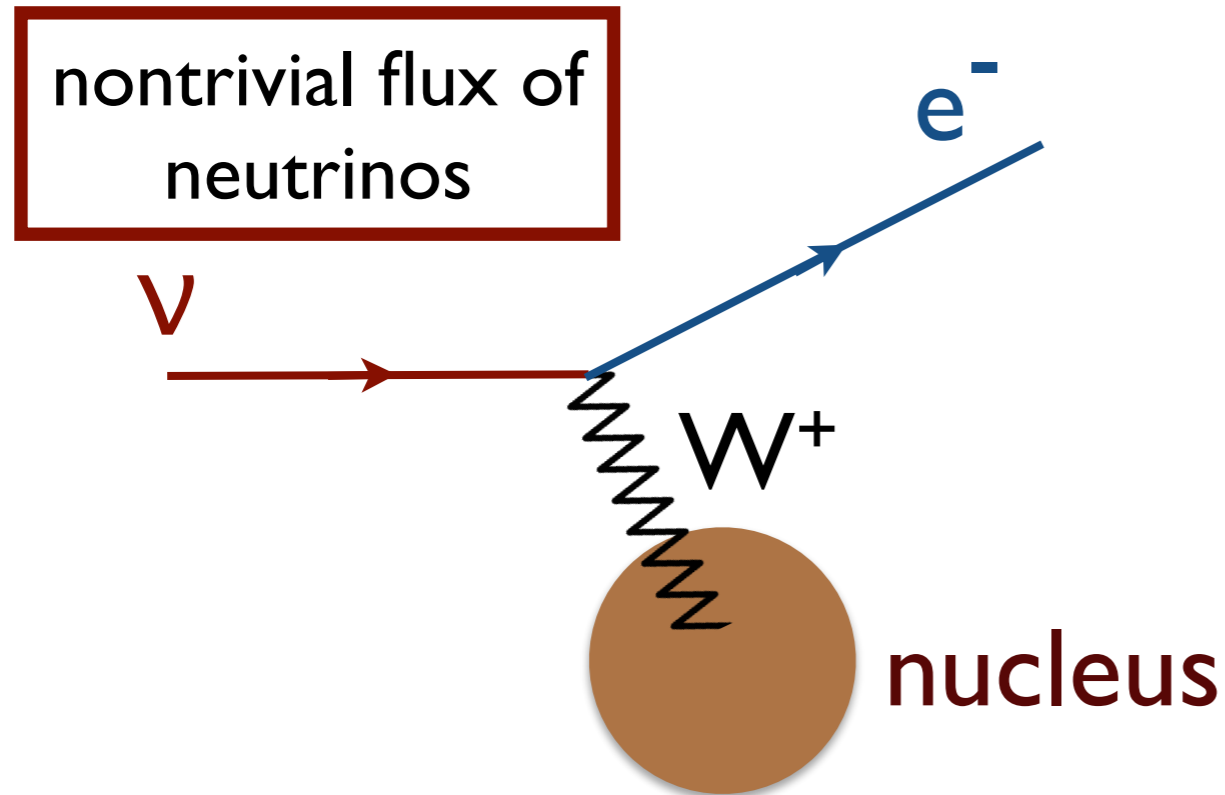
- *inputs to neutrino cross sections (vector form factors)*
- *a proving ground for both theory and experiment*



Do we understand this problem with controllable uncertainties?

# Look at related process: elastic electron-proton scattering:

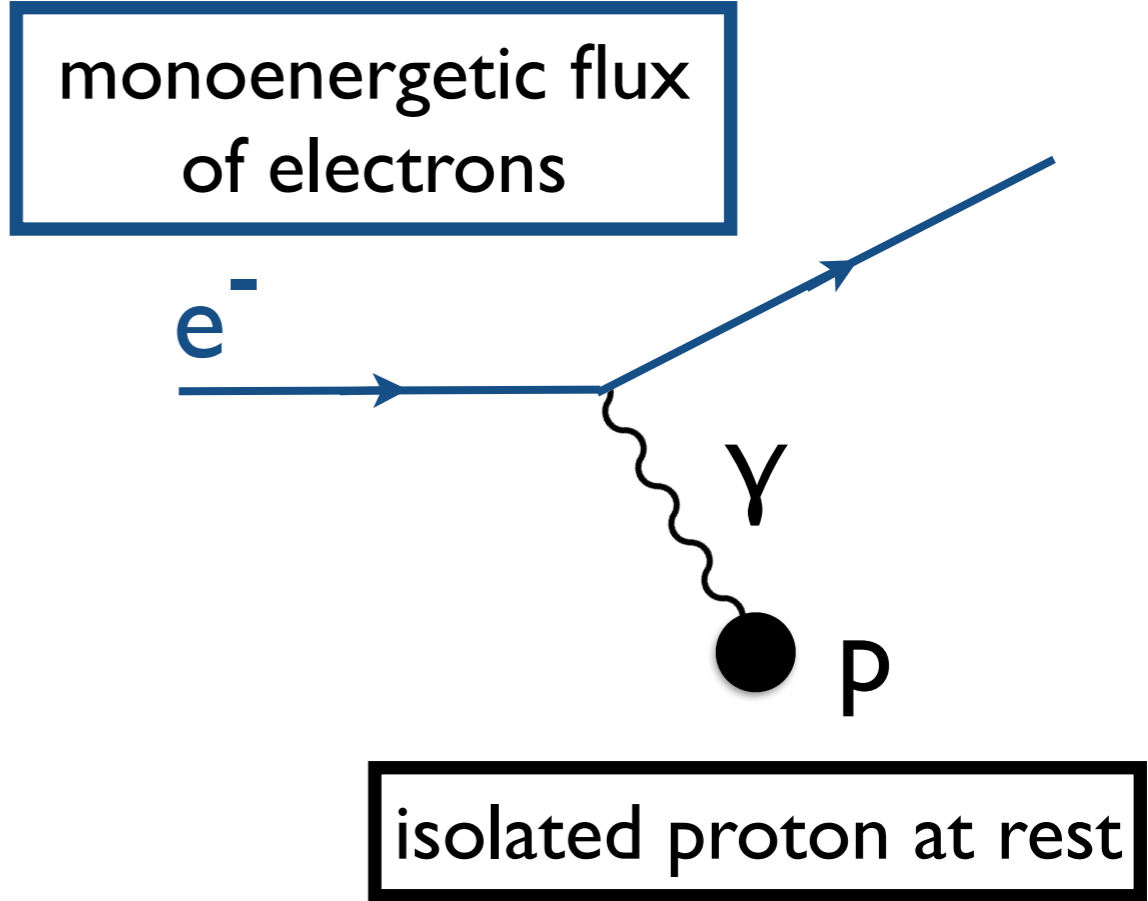
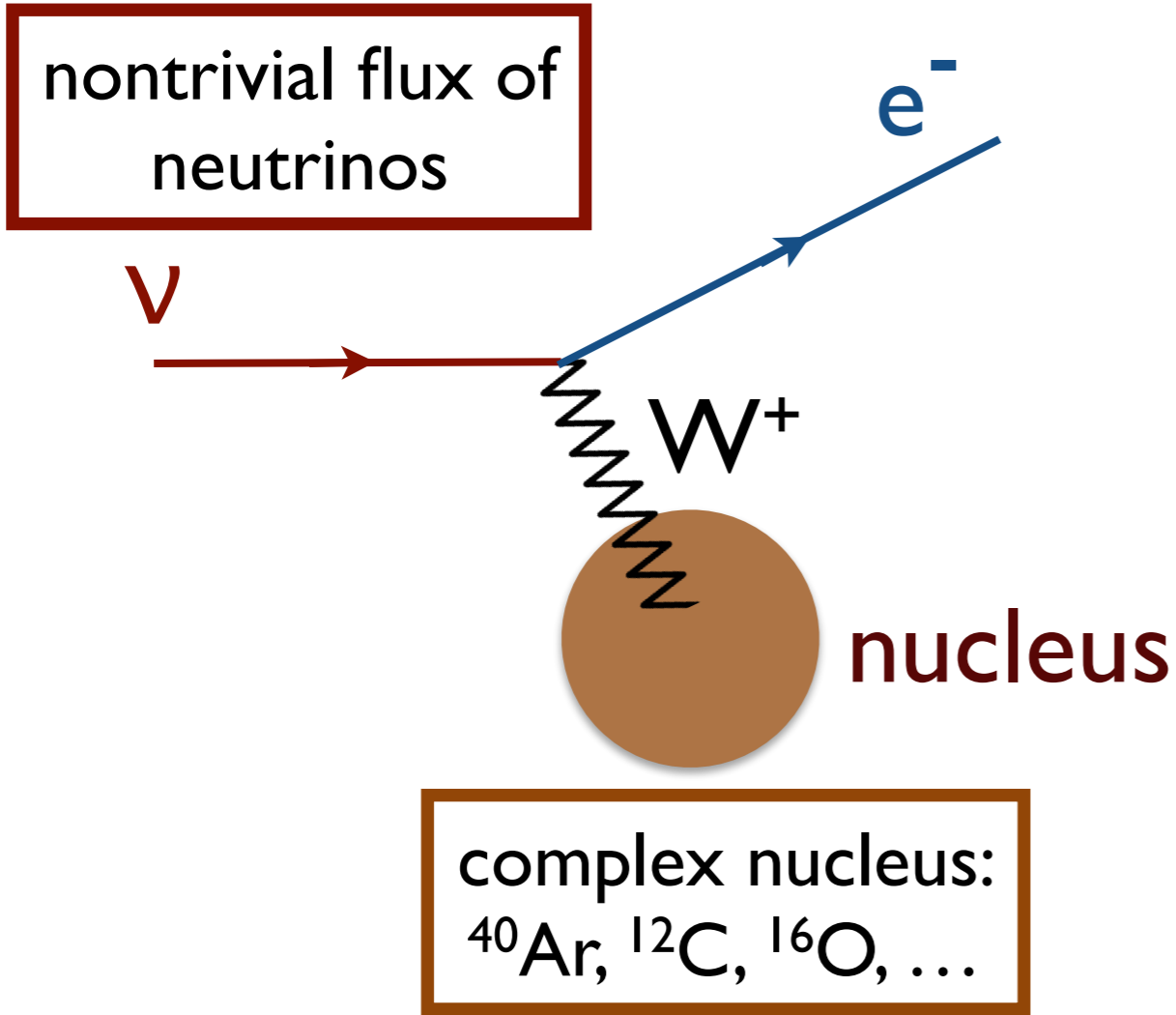
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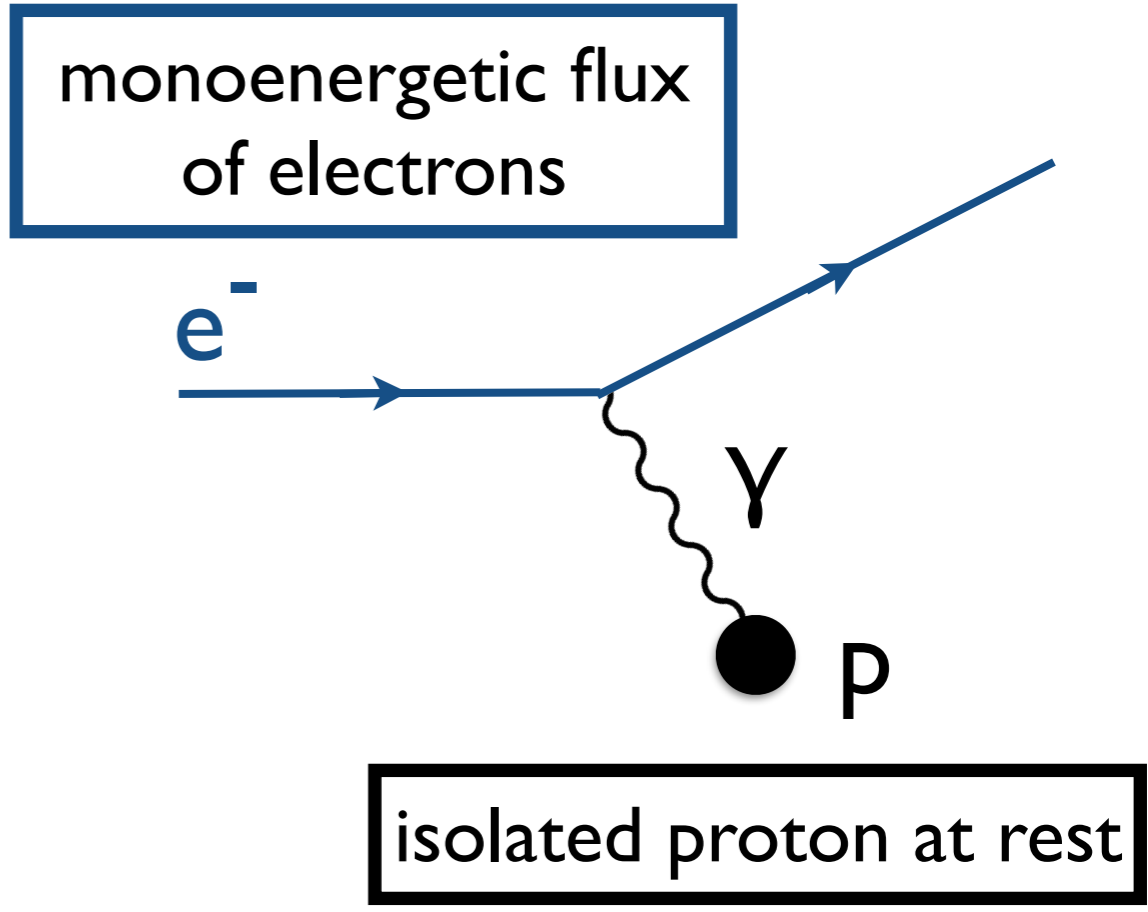
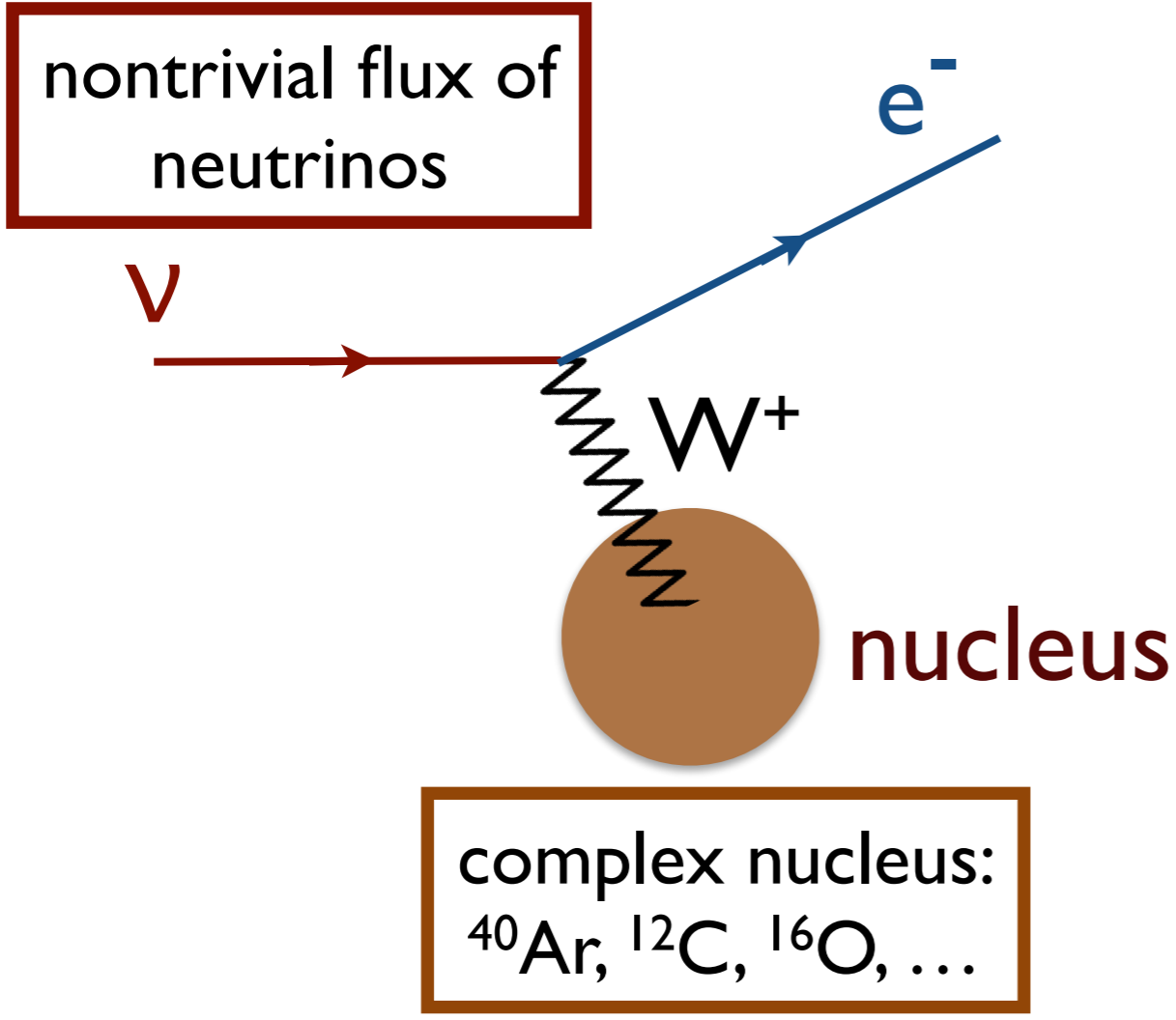
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Do we understand this problem with controllable uncertainties?

# Some facts about the Rydberg constant puzzle (a.k.a. proton radius puzzle)

1) It has generated a lot of attention and controversy



The New York Times

2) The *most mundane* resolution necessitates:

- $5\sigma$  shift in fundamental Rydberg constant
- discarding or revising decades of results in e-p scattering and hydrogen spectroscopy

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“The good news is that it’s not my problem”

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This is HEP's problem:

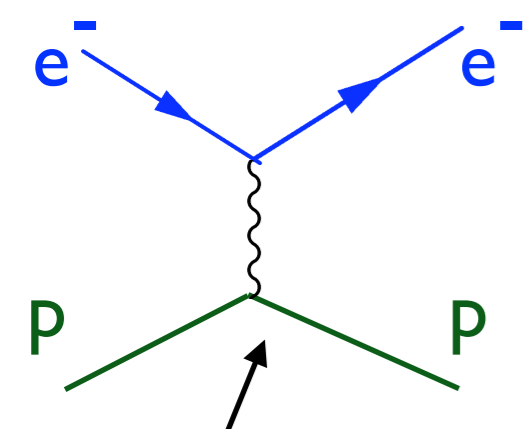
3) Systematic effects in electron-proton scattering impact neutrino-nucleus scattering, at a level large compared to DUNE precision requirements



**“The good news is that it’s not my problem”**

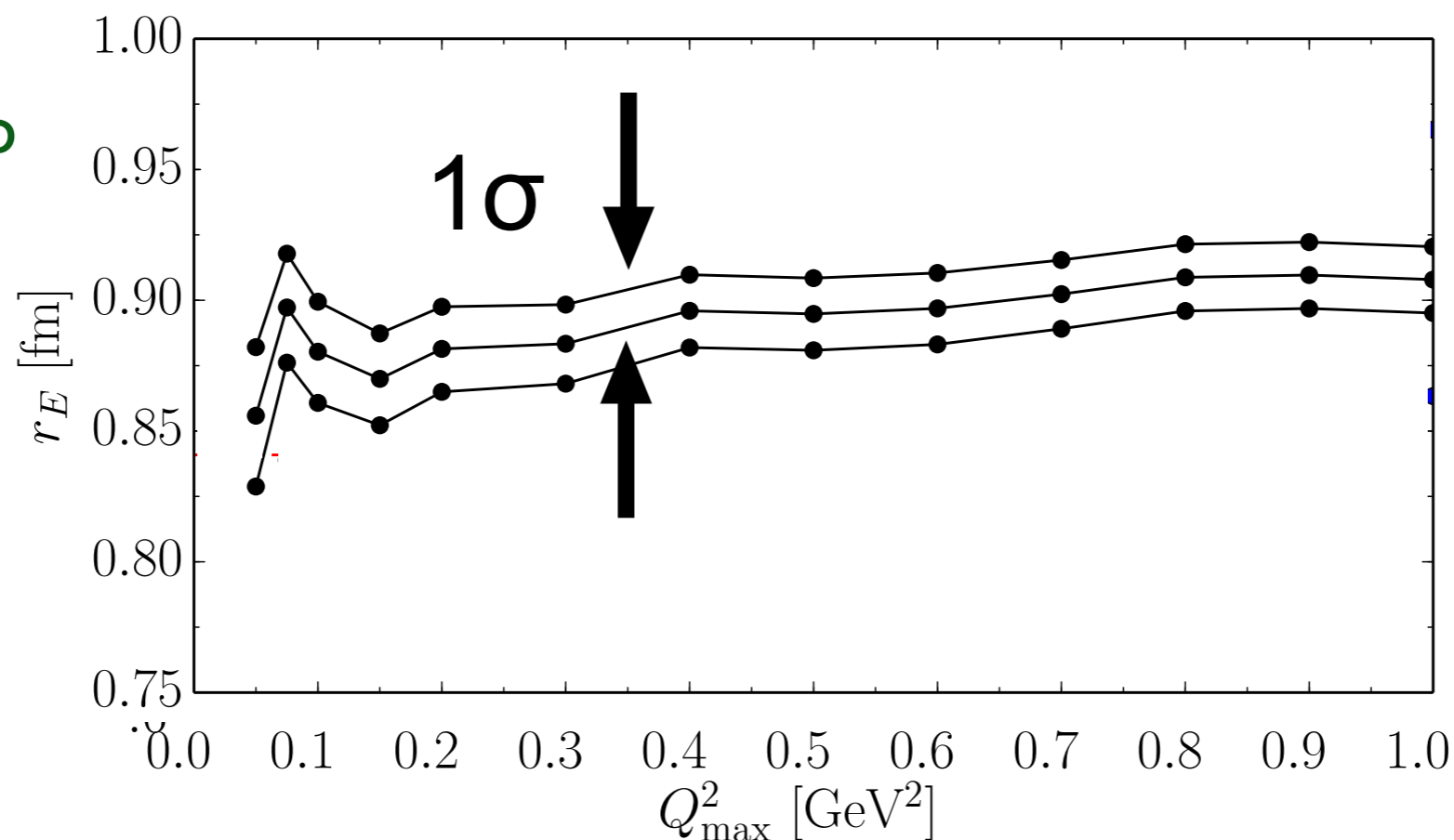
World e-p scattering dominated by 2010  
MAMI A1 dataset:  $0 < Q^2 < 1 \text{ GeV}^2$   
(  $|z| < 0.32$  )

*(details:  
backup slide)*



electric  
form factor

$$\frac{dF_E}{dq^2} \propto r_E^2$$

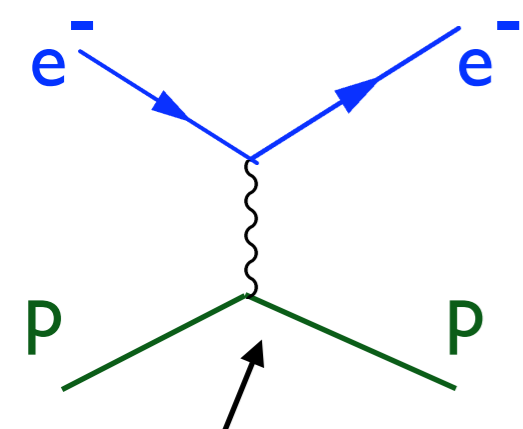


- Unexpected  $Q^2$  dependence of extracted radius, and potentially large radiative corrections
- For both e-p and  $\nu$ -N: large logarithms upset naive perturbation theory
- Work in progress to implement complete radiative corrections



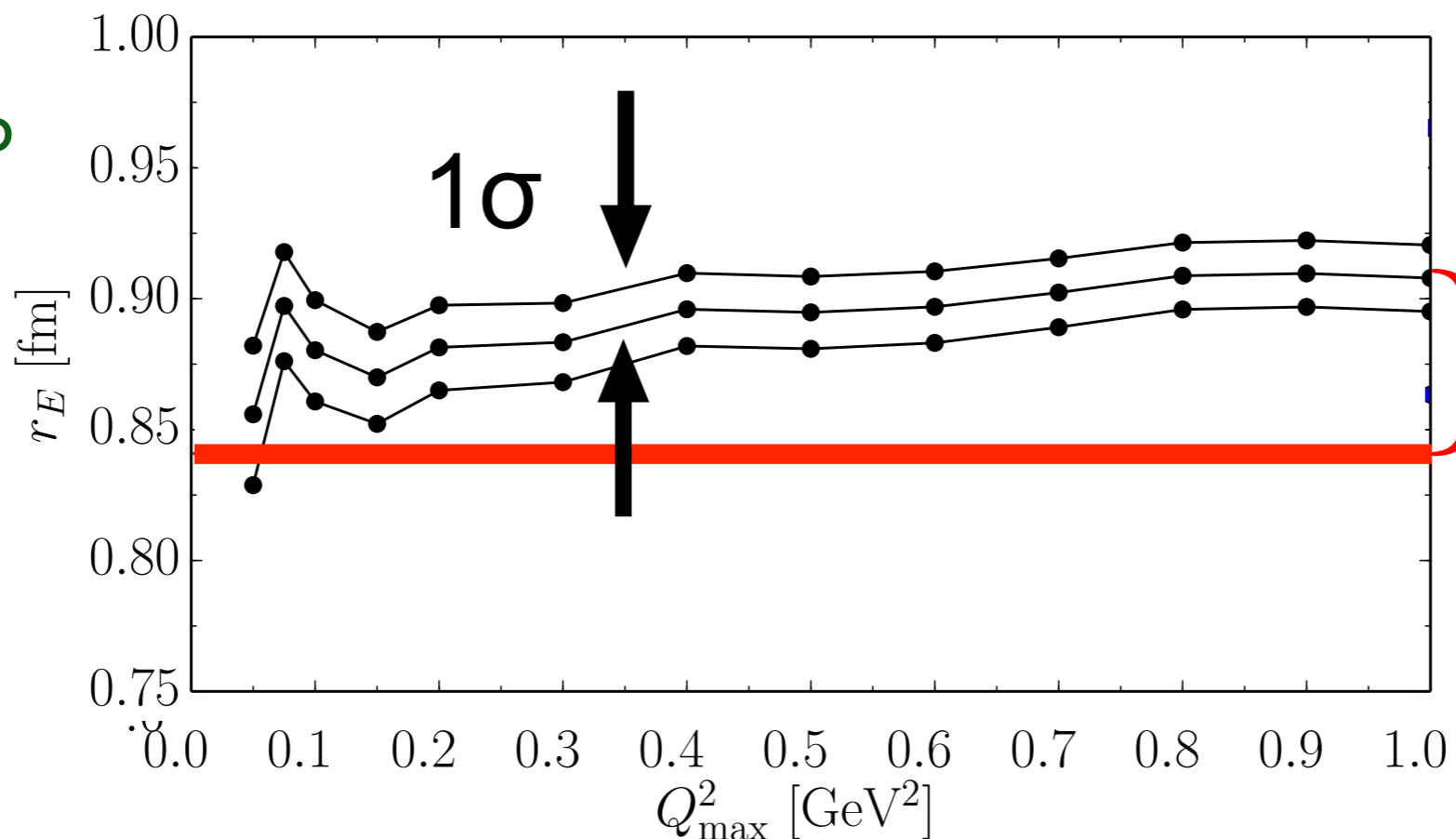
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(details:  
backup slide)



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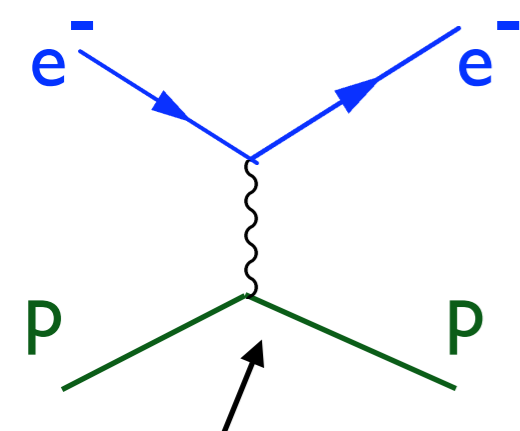


> 5σ  
discrepancy

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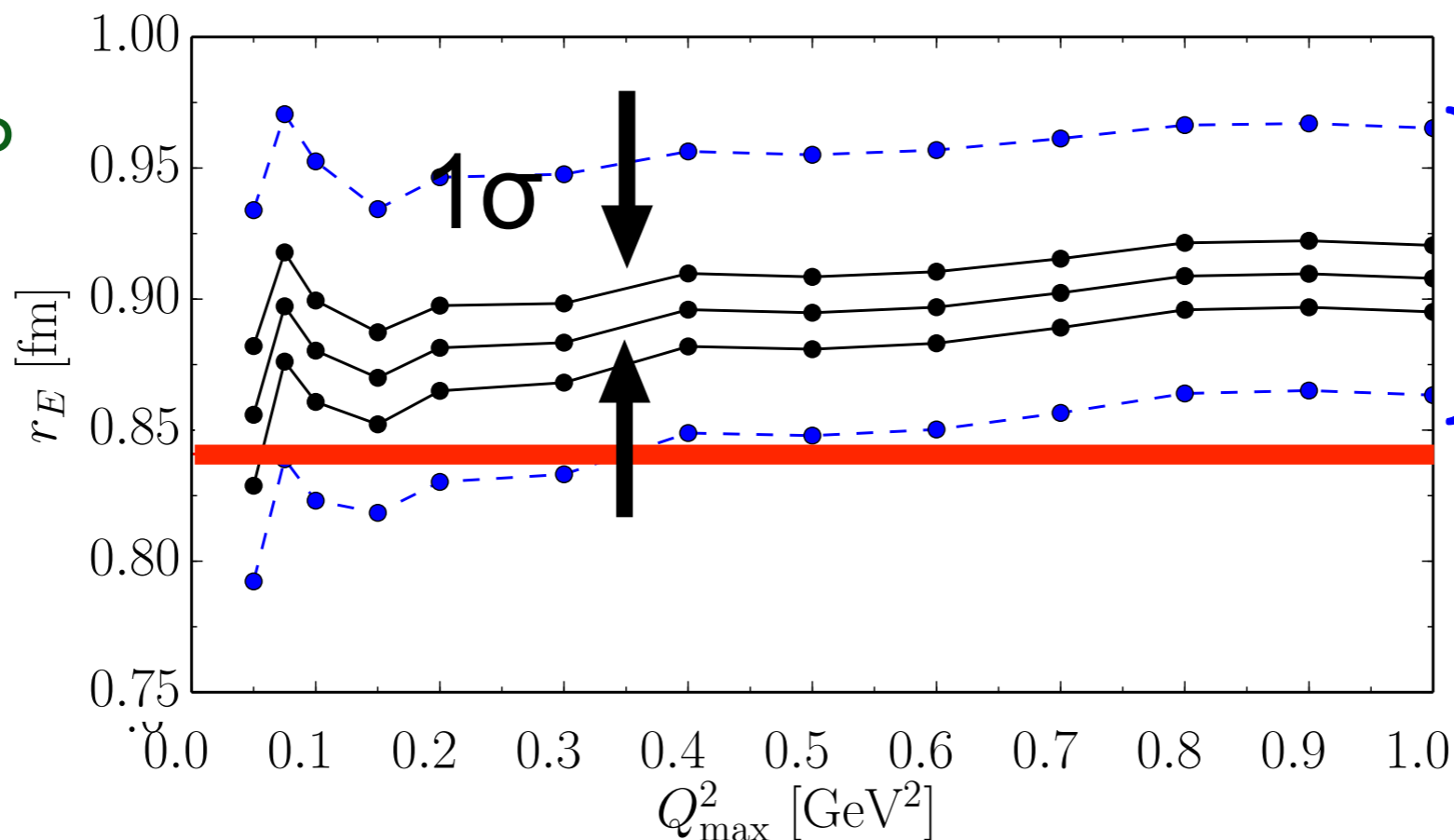
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electric  
form factor

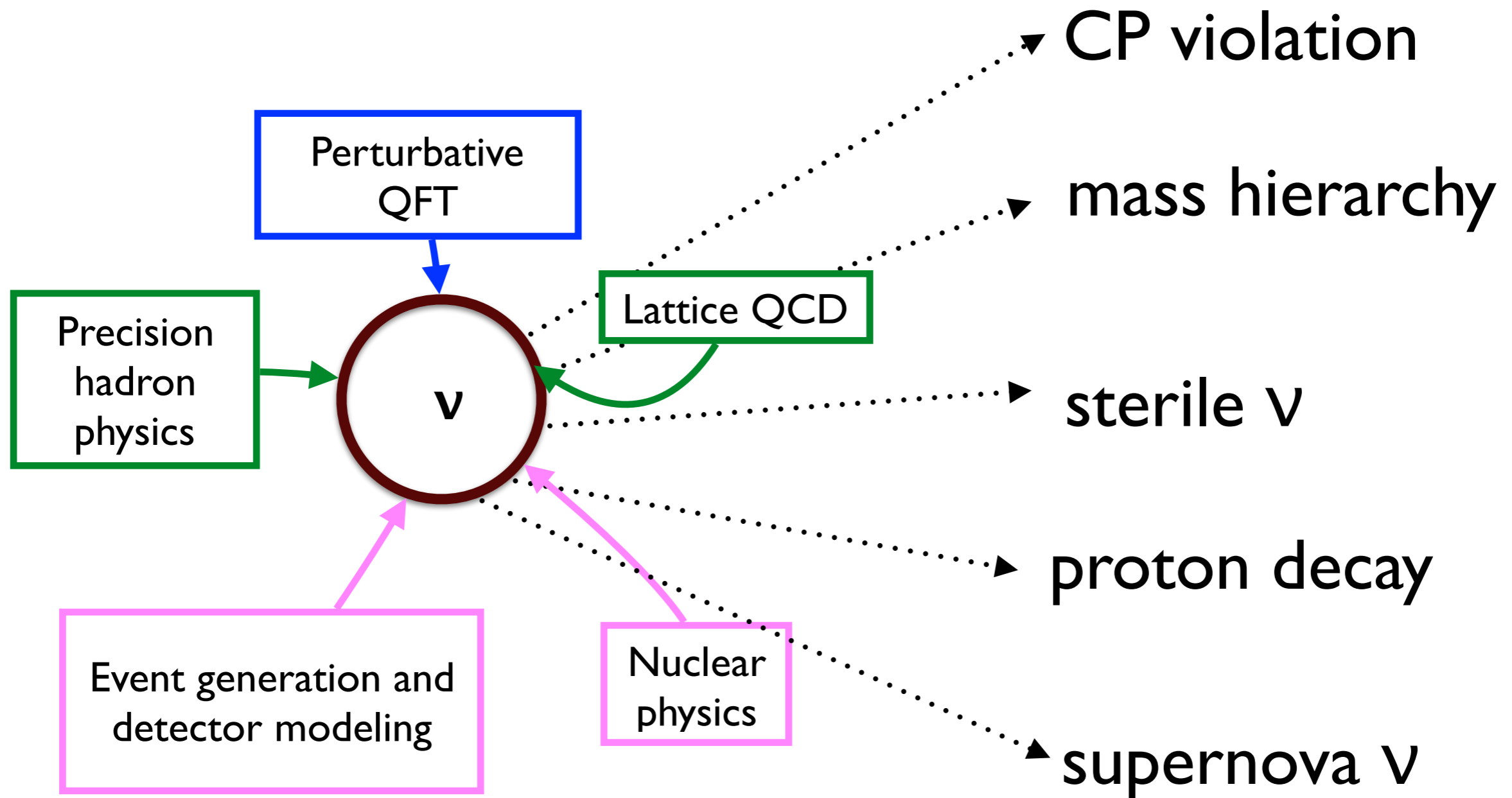
$$\frac{dF_E}{dq^2} \propto r_E^2$$



potentially  
large  
uncertainty  
from radiative  
corrections

- Unexpected  $Q^2$  dependence of extracted radius, and potentially large radiative corrections
- For both e-p and  $\nu$ -N: large logarithms upset naive perturbation theory
- Work in progress to implement complete radiative corrections

A systematic framework is being constructed to map elementary-target/  
lattice data through to oscillation observables



Much to do, and much to learn!

...

# Cross sections key to discoveries in the neutrino sector

## Particle theory has a critical role to play

- precision hadron physics: *building on CKM studies*
- radiative corrections: *renormalization, soft-collinear effective theory*
- lattice QCD

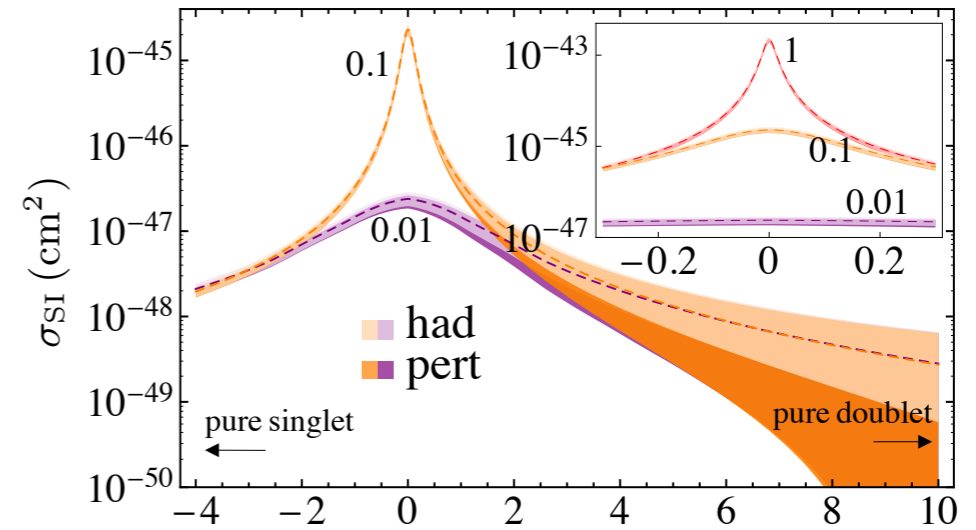
## Important connections: other intensity frontier initiatives

- lattice QCD & baryons: *neutrinos, DM, proton radius puzzle, nEDM, ...*
- radiative corrections: *neutrinos,  $g-2$ , proton radius puzzle, CKM, ...*
- nuclear effects and hadronic final state: *energy reconstruction in  $\nu$ -N scattering; atmospheric bkgd. to proton decay, ...*

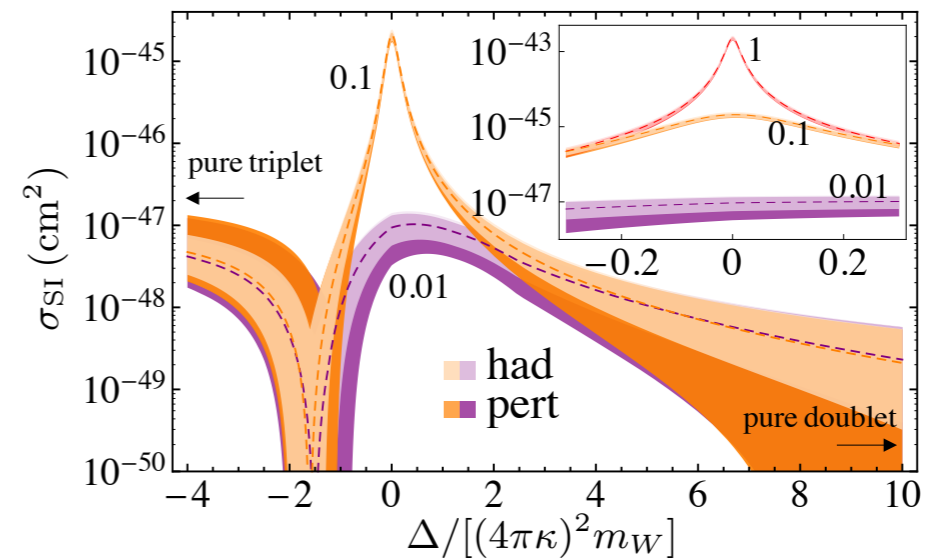
backup

# Additional states in the dark sector

singlet-doublet (e.g., bino-higgsino)



triplet-doublet (e.g., wino-higgsino)

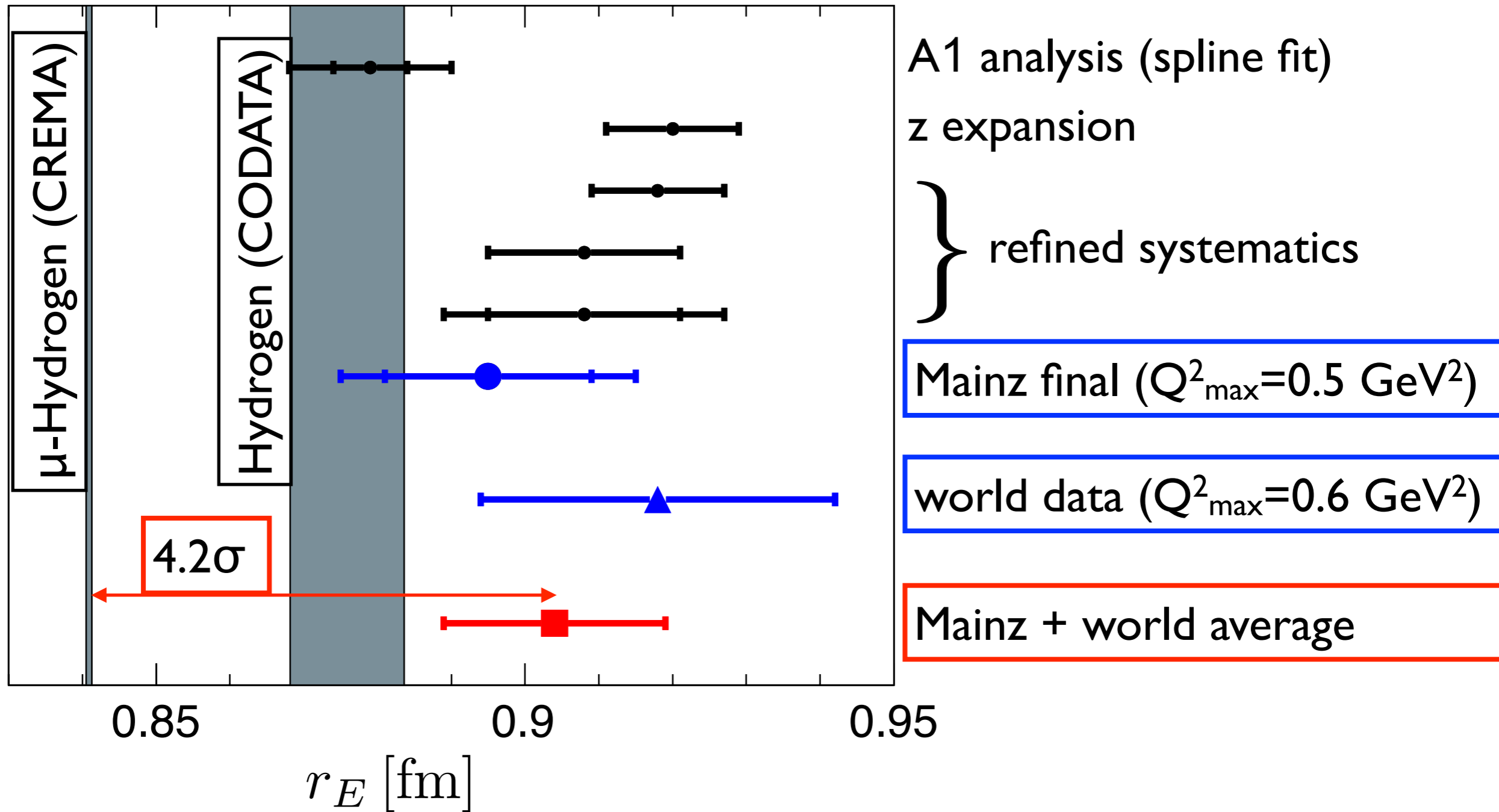


$\Delta$ : mass splitting of multiplets, in units where tree/loop crossover occurs at  $\sim 1$

interplay of mass-suppressed (tree level) and loop suppressed contributions

# experimental landscape: electron-proton scattering

G. Lee, J. Arrington, RJH, 2015



$$r_E^{\text{Mainz}} = 0.895(14)(14)$$

$$r_E^{\text{world}} = 0.918(24)$$

simple average:

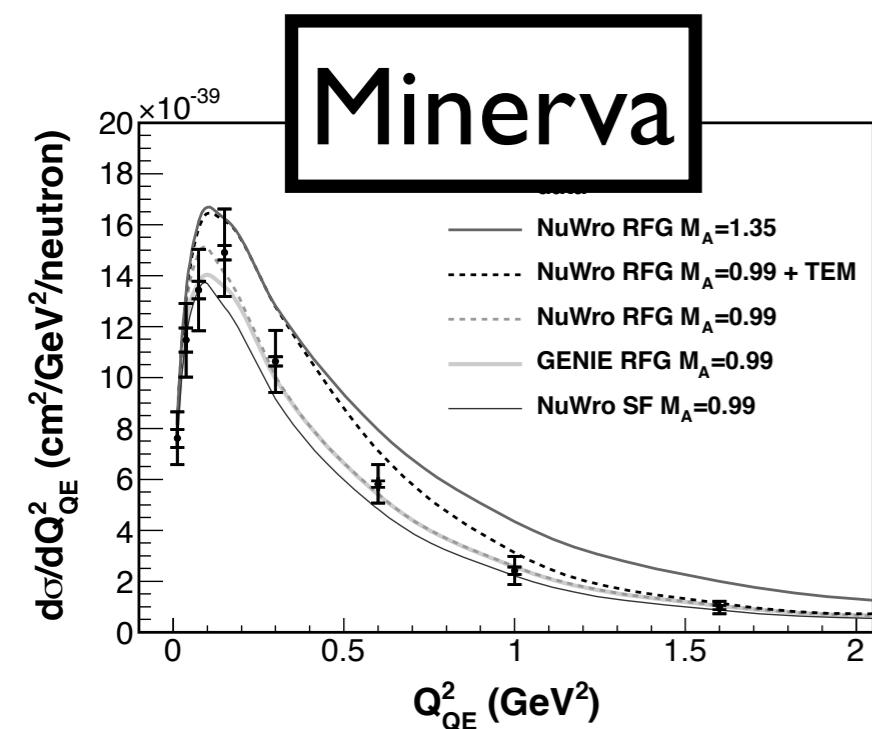
$$r_E^{\text{avg.}} = 0.904(15)$$

# Sample application of elementary target data: constrain and validate nuclear models

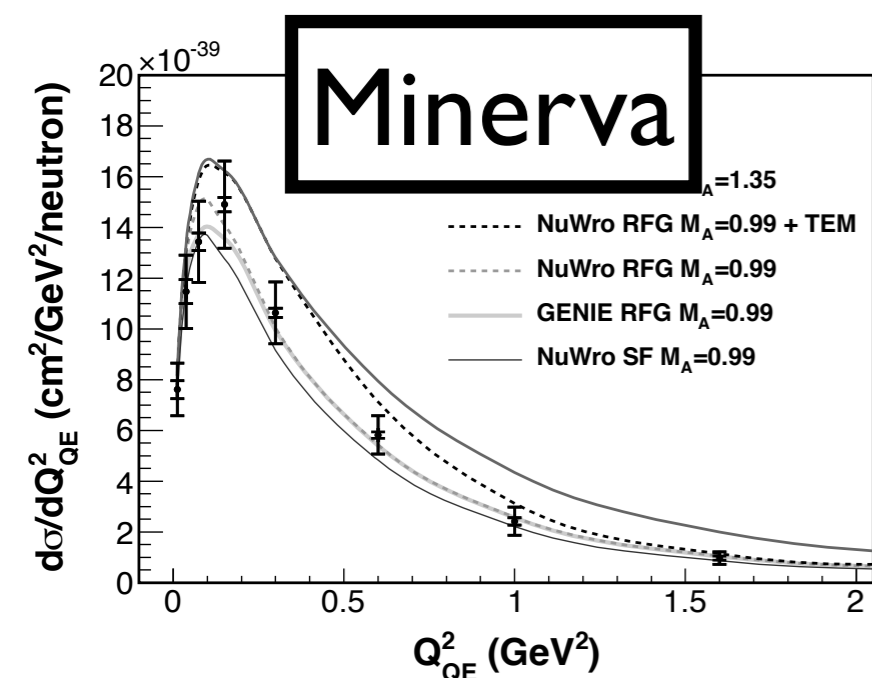
Can we constrain a simple nuclear model for two-body contributions ?

$$\sigma = \sigma_{1\text{-body}} + f \sigma_{2\text{-body}}$$

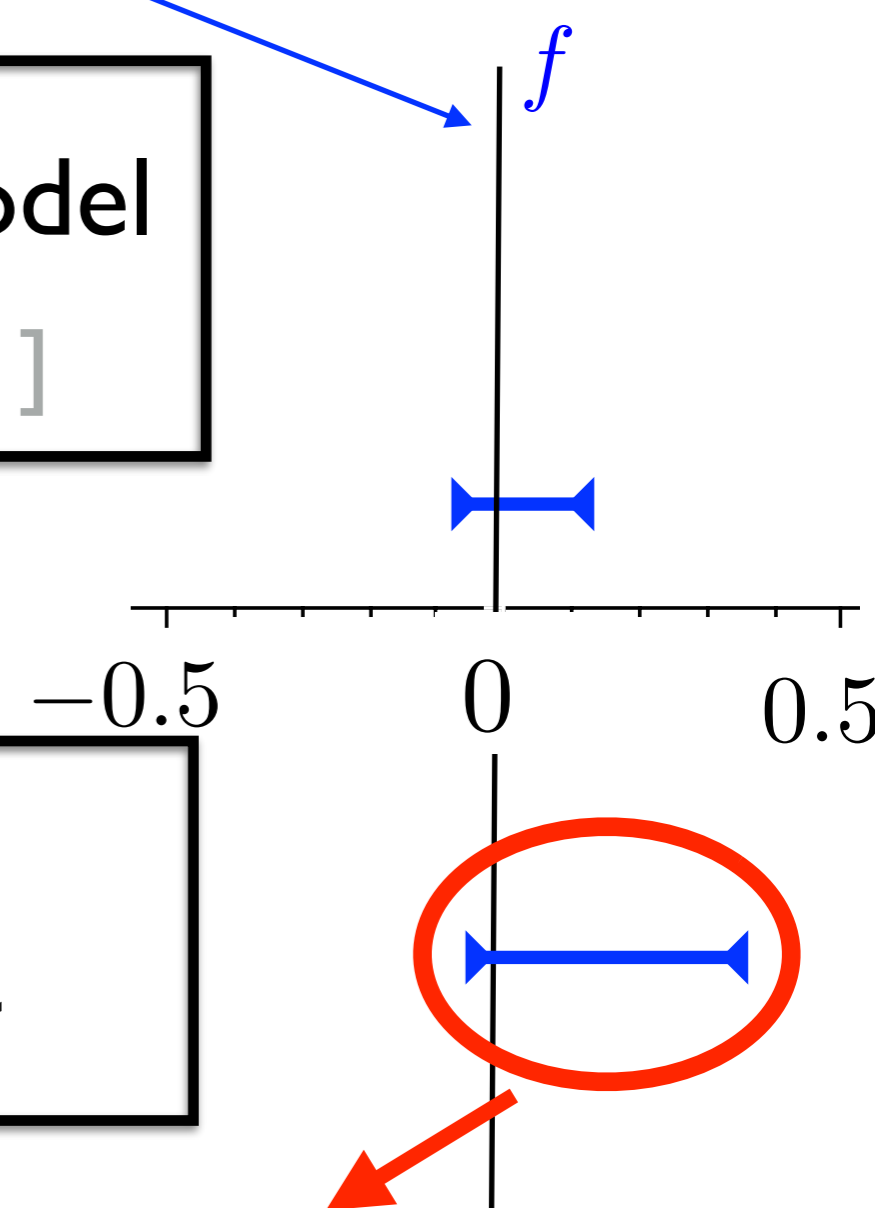
(GENIE MEC model)



+  $F_A = \text{dipole model}$   
[  $m_A=1.01(2)$  ]



+  $F_A = \text{model-independent}$



**large nucleon-level uncertainties**



# Addressing energy reconstruction biases

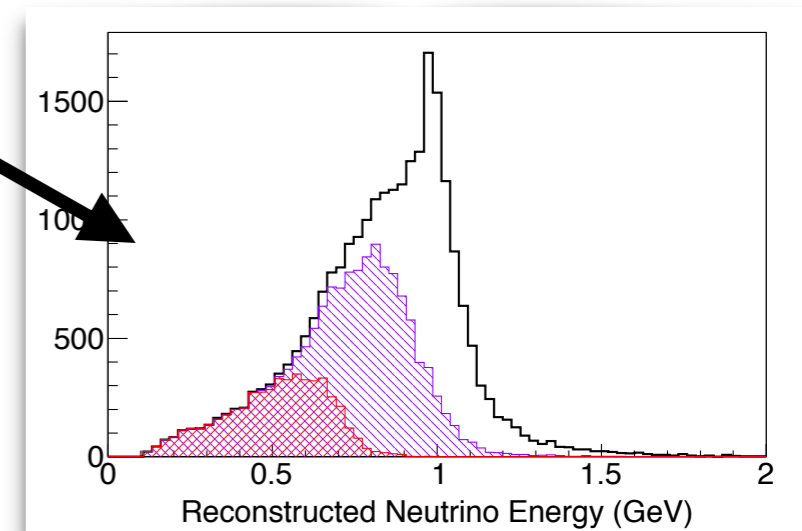
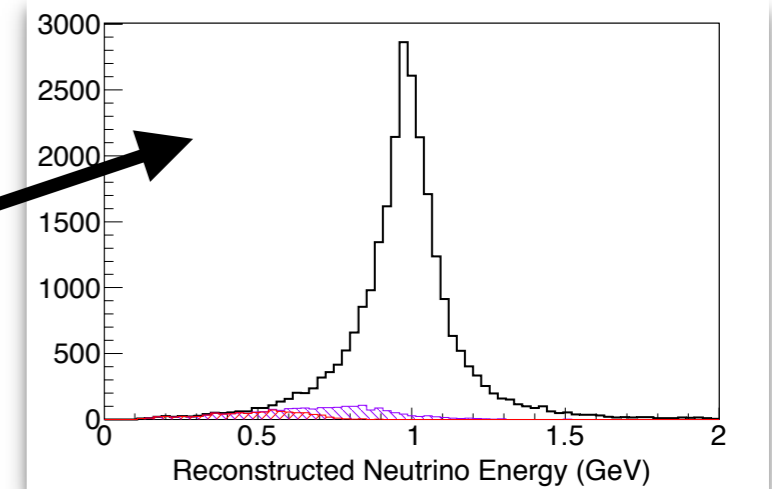
cf. colliders: define event classes to isolate underlying parton mechanisms (vector boson fusion, gluon fusion,...)

for neutrinos: define event classes with (in)sensitivity to underlying nucleon-level mechanisms (multinucleon processes,...)

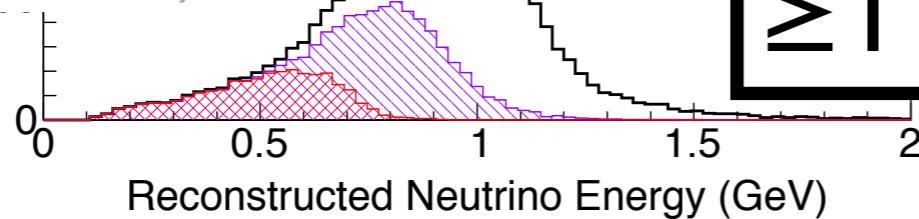
1 GeV neutrino events,  
0 pions, reconstructed  
as quasielastic

0 neutron

$\geq 1$  neutron



(GENIE, +30% MEC)



*C. Blanco, M. Wetstein, RJH*

Capitalize on new detector technologies

- final state protons in LArTPC
- final state neutrons (ANNIE)
- simple flux (stored muons); multiple fluxes (“nuPRISM”), ...