

# EDM constraints on flavored CP-violating phases



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- Outline

*I- Introduction: MFV and CP-violating phases*

*II- MFV in the slepton sector*

*III- EDM constraints*

*Conclusion*

# Introduction

## A. CP-violating phases in the MFV approach

MFV is based on the  $U(3)^5$  *flavor symmetry group* of the gauge sector.

Chivukula,  
Georgi '87

*Minimally broken*: such that quark and lepton masses/mixing are reproduced.

Technically, the Yukawas are treated as the only *spurions*.

All the *flavor-dependent couplings are hierarchical*, with their non-trivial structures inherited directly from those of the Yukawa couplings.

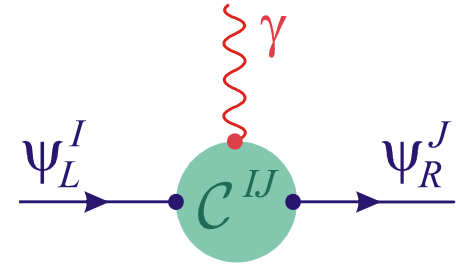
Hall, Randall '90, D'Ambrosio, Giudice, Isidori, Strumia '02

Does *this restrict CP-violating phases* only to those in the Yukawas? **No!**

- The  $U(3)^5$  does not say anything about phases (*free param. are complex*),
- There can be new CP-violating *phases in other sectors*,
- Requiring MFV not to introduce new CP-phases is a *fine-tuning*.

## B. Flavor transitions vs. flavor-diagonal observables

$$H_{eff} = e \frac{c^{IJ}}{\Lambda^2} \bar{\Psi}_R^I \sigma_{\mu\nu} \Psi_L^J F^{\mu\nu} H_d$$



*Flavor transitions*  $\sim c^{I \neq J}$  are severely constrained by MFV:

In the quark sector, all flavor changes tuned entirely by the hierarchical CKM.

In the lepton sector, such transitions are forbidden as long as  $m_\nu = 0$ .

But for *flavor-diagonal* operators  $\sim c^{II}$ , there is no restriction at all.

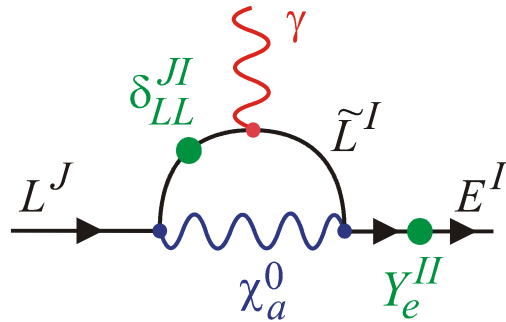
→ EDMs require very high New Physics scales?

### C. Situation in the MSSM leptonic sector

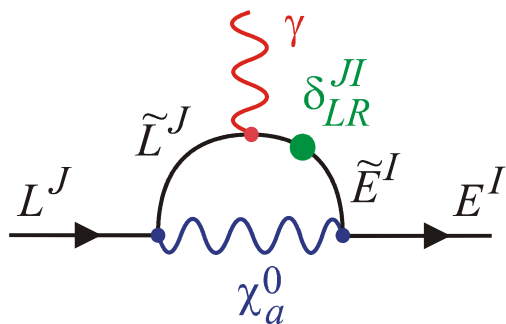
MFV implies expansions for the *soft-breaking couplings* in terms of Yukawa.

$$\mathcal{L}_{soft}^{RPC} \ni -\tilde{L}^\dagger m_L^2 \tilde{L} - \tilde{E} m_E^2 \tilde{E}^\dagger + \tilde{E} A_e (\tilde{L} H_d) + \dots$$

These can then *induce LFV transitions and EDMs*:



$$B(\ell^I \rightarrow \ell^J \gamma) \sim \frac{\alpha M_W^4 \tan^2 \beta}{M_{SUSY}^4} \left| \delta_{LL}^{JI} + \dots \right|^2$$



Beyond MFV

Correlations?

$$\frac{d_I}{e} \sim \frac{\alpha}{M_{SUSY}^3} \text{Im} \left( m_\ell^I \mu \tan \beta - v_d A_e^{*II} \right) + \dots$$

MFV in the slepton sector

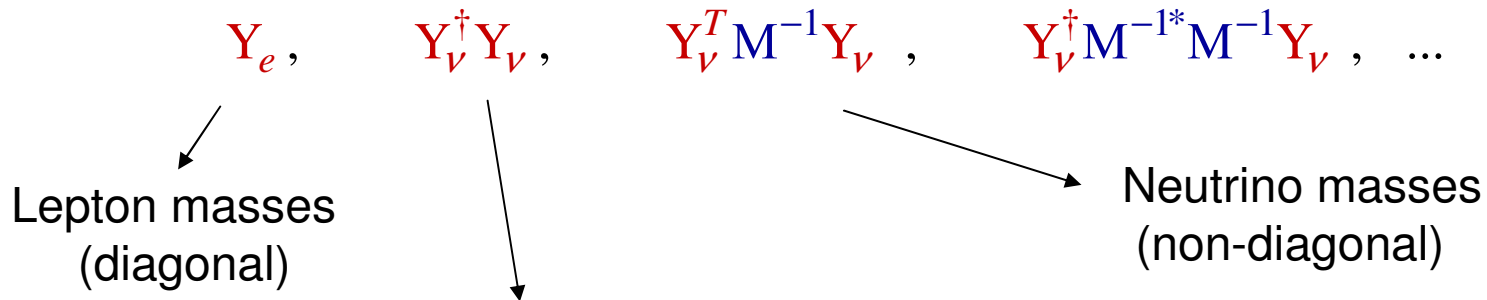
## A. Construction of the MFV expansions

**STEP 1:** Identify the spurions, i.e. the *minimal sources of flavor breaking* able to reproduce known fermion masses & mixings ( $\sim$  Yukawa).

Starting with  $\mathcal{W}_N = N\mathbf{M}N + N\mathbf{Y}_\nu(LH_u) - E\mathbf{Y}_e(LH_d)$ ,

*Cirigliano, Grinstein  
Isidori, Wise '05*

Integrating out the right-handed (s)neutrinos:



Not completely fixed (we take  $\mathbf{M} = M_R \mathbf{1}$ ):

$$\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu = \frac{M_R}{v_u} U^* m_\nu^{1/2} e^{2i\Phi} m_\nu^{1/2} U^\dagger, \quad \Phi^{IJ} = \varepsilon^{IJK} \phi_K$$

1 Dirac phase	→	6 CP-phases.
2 Majorana phases		
3 real $\phi_K$ parameters		



A. Construction of the MFV expansions

Nikolidakis, CS '07, Colangelo,  
Nikolidakis, CS '08, Mercolli, CS '09

STEP 2: Parametrize the *soft-breaking terms as expansions in the spurions*

- Most general expansions:  $m_L^2 = m_0^2 Q$ ,  $m_R^2 = m_0^2 (1 + Y_e Q Y_e^\dagger)$ ,  $A_e = A_0 Y_e Q$

$$\text{with } Q = \sum z_{lmn\dots} A^l B^m A^n \dots \quad A \equiv Y_e^\dagger Y_e, \quad B \equiv Y_\nu^\dagger Y_\nu$$

- Reduced to a *finite number of hermitian* terms using Cayley-Hamilton identity:

$$X^3 - \langle X \rangle X^2 + \frac{1}{2} X (\langle X \rangle^2 - \langle X^2 \rangle) = \frac{1}{3} \langle X^3 \rangle - \frac{1}{2} \langle X \rangle \langle X^2 \rangle + \frac{1}{6} \langle X \rangle^3$$

- Use the large *mass hierarchy* to set  $(Y_e^\dagger Y_e)^2 \sim Y_e^\dagger Y_e$ , leaving:

$$Q = x_1 \mathbf{1} + x_2 A + x_3 B + x_4 B^2 + x_5 \{A, B\} + x_6 BAB \\ + x_7 i[A, B] + x_8 i[A, B^2] + x_9 i(BAB^2 - B^2 AB)$$

If  $Q$  is hermitian:  $x_i \in \mathbb{R}$ , with  $x_{1-6}$  CP-conserving and  $x_{7,8,9}$  CP-violating,

If  $Q$  is complex:  $x_i \in \mathbb{C}$ , all CP-violating.

→ 15 CP-phases.

## B. CP-violation in the MFV framework

$$Q = x_1 \mathbf{1} + x_2 \mathbf{A} + x_3 \mathbf{B} + x_4 \mathbf{B}^2 + x_5 \{ \mathbf{A}, \mathbf{B} \} + x_6 \mathbf{B} \mathbf{A} \mathbf{B} \\ + x_7 i [\mathbf{A}, \mathbf{B}] + x_8 i [\mathbf{A}, \mathbf{B}^2] + x_9 i (\mathbf{B} \mathbf{A} \mathbf{B}^2 - \mathbf{B}^2 \mathbf{A} \mathbf{B})$$

Can we set and maintain  $\text{Im } x_{1-6} = 0$ ,  $\text{Re } x_{7,8,9} = 0$  in a natural way?

When the spurions are CP-violating,  $\langle \mathbf{A}^l \mathbf{B}^m \mathbf{A}^n \dots \rangle$  can be complex:

- *Consistency*: Coefficients are understood to include spurion traces,
- *Choice of basis*: Coefficients differ by some spurion traces,
- *RGE effects*: Projecting back = absorbing spurion traces in the coefficients,

*CP cannot be defined* separately for the coefficients and for the spurions.

Forcing coefficients to conserve CP is *not protected by any symmetry*. Rather, it is, by definition, a *fine-tuning*.

## B. CP-violation in the MFV framework

1- But it is a “*stable fine-tuning*”:

When  $Y_\nu^\dagger Y_\nu$  &  $Y_e^\dagger Y_e$  are the only spurions, all complex traces  $\rightarrow$  Jarlskog:

$$J = \text{Im}\langle (Y_\nu^\dagger Y_\nu)^2 Y_e^\dagger Y_e Y_\nu^\dagger Y_\nu (Y_e^\dagger Y_e)^2 \rangle \quad \dots \text{which is very small.}$$

2- Same applies directly to the *quark sector*, with  $A \equiv Y_d^\dagger Y_d$ ,  $B \equiv Y_u^\dagger Y_u$ .

3- Possible *fine-tuning mechanism* does exist, at least in the quark sector:

RGE effects suppress CP-phases (but |coefficients| are then constrained)

*Paradisi, Ratz, Schieren, Simonetto '08, Colangelo, Nikolidakis, C.S. '08*

4- CP-violating coefficients needed in the presence of *new spurions*:

$$(Y_\nu^\dagger Y_\nu)^{IJ} \quad , \quad \sum_K Y_\nu^{\dagger IK} Y_\nu^{KJ} \log M_R^{KK}$$

*Ellis, Hisano, Raidal, Shimizu '08*

### C. Classification of the 6+15 CP-phases

Final expansions, with  $a_i, b_i \in \mathbb{R}$ ,  $c_i, d_i \in \mathbb{C}$  :

$$m_L^2 = m_0^2 (a_1 \mathbf{1} + a_2 \mathbf{A} + a_3 \mathbf{B} + a_5 \{ \mathbf{A}, \mathbf{B} \} + a_6 \mathbf{B} \mathbf{A} \mathbf{B} + b_1 i [ \mathbf{A}, \mathbf{B} ] + \mathcal{O}(\mathbf{A}^2, \mathbf{B}^2)),$$

$$m_R^2 = m_0^2 (a_7 \mathbf{1} + \mathbf{Y}_e (a_8 \mathbf{1} + a_9 \mathbf{B} + a_{11} \{ \mathbf{A}, \mathbf{B} \} + b_4 i [ \mathbf{A}, \mathbf{B} ])) \mathbf{Y}_e^\dagger + \mathcal{O}(\mathbf{A}^2, \mathbf{B}^2)),$$

$$\mathbf{A}_e = A_0 \mathbf{Y}_e (c_1 \mathbf{1} + c_2 \mathbf{A} + c_3 \mathbf{B} + c_5 \{ \mathbf{A}, \mathbf{B} \} + d_1 i [ \mathbf{A}, \mathbf{B} ] + \mathcal{O}(\mathbf{A}^2, \mathbf{B}^2))$$

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*Flavor-blind phase:*  $\text{Im } c_1$  (remember  $d_I \sim \text{Im } \mathbf{A}_e^{*II} \sim \text{Im } c_1$ )

Defined relative to the flavor-blind parameters of the MSSM ( $\mu, M_1, M_2, \dots$ )

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*Flavor-blind phase:*  $\text{Im } c_1$

Defined relative to the flavor-blind parameters of the MSSM ( $\mu, M_1, M_2, \dots$ )

*Flavor-diagonal phases:*  $\text{Im } c_{2-6}$  (remember  $d_I \sim \text{Im } A_e^{*II} \sim \text{Im } c_{2-6}$ )

Contribute to EDMs at leading order in the MIA.

### C. Classification of the 6+15 CP-phases

Final expansions, with  $a_i, b_i \in \mathbb{R}$ ,  $c_i, d_i \in \mathbb{C}$  :

$$m_L^2 = m_0^2 (a_1 \mathbf{1} + a_2 \mathbf{A} + a_3 \mathbf{B} + a_5 \{A, B\} + a_6 \mathbf{BAB} + b_1 i[A, B] + \mathcal{O}(A^2, B^2)),$$

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*Flavor-blind phase:*  $\text{Im } c_1$

Defined relative to the flavor-blind parameters of the MSSM ( $\mu, M_1, M_2, \dots$ )

*Flavor-diagonal phases:*  $\text{Im } c_{2-6}$

Contribute to EDMs at leading order in the MIA.

*Flavor off-diagonal phases:*  $b_i, \text{Re } d_i$ , six phases of  $\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu$   $\leftarrow$  (hermitian op.)

Start to contribute to EDMs at 2<sup>nd</sup> order in the MIA ( $d_I \sim \text{Im}(\delta_{LL}^{IK} \delta_{LR}^{KI}) + \dots$ ).

**EDM constraints**



## A. Dominant operators

Only a single operator dominates for  $\mu \rightarrow e \gamma$  (coming from  $\delta_{LL}$ ):

$$B(\mu \rightarrow e \gamma) \sim \frac{\alpha M_W^4 \tan^2 \beta}{M_{SUSY}^4} \left| \frac{a_3}{a_1} (\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{12} \right|^2$$

Only a single operator per type of phases dominates for  $d_e$ :

$$\frac{d_e}{e} \sim \frac{\alpha m_e}{M_{SUSY}^2} \left( \frac{\text{Im } c_1}{a_1 a_7} + \frac{\text{Im } c_3}{a_1 a_7} \mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu - \frac{b_1 \text{Re } c_3}{a_1^2 a_7} [\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu, \mathbf{Y}_e^\dagger \mathbf{Y}_e] \mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu + \dots \right)^{11}$$

Flavor-blind

Flavor-diagonal

Flavor off-diagonal  
( $\geq$  neutrino phases)

Remark:  $m_L^2 \approx m_0^2 a_1$ ,  $m_R^2 \approx m_0^2 a_7$

## A. Dominant operators

Only a single operator dominates for  $\mu \rightarrow e \gamma$  (coming from  $\delta_{LL}$ ):

$$B(\mu \rightarrow e \gamma) \sim \frac{\alpha M_W^4 \tan^2 \beta}{M_{SUSY}^4} \left| \frac{a_3}{a_1} \frac{M_R \Delta m_{21}}{v_u^2} \right|^2$$

Only a single operator per type of phase dominates for  $d_e$ :

$$\frac{d_e}{e} \sim \frac{\alpha m_e}{M_{SUSY}^2} \left( \frac{\text{Im } c_1}{a_1 a_7} + \frac{\text{Im } c_3}{a_1 a_7} \frac{M_R \Delta m_{21}}{v_u^2} - \frac{b_1 \text{Re } c_3}{a_1^2 a_7} \frac{m_\tau^2}{v_d^2} \left( \frac{M_R \Delta m_{21}}{v_u^2} \right)^2 + \dots \right)^{11}$$

Flavor-blind

$\gg$

Flavor-diagonal

$\gg$

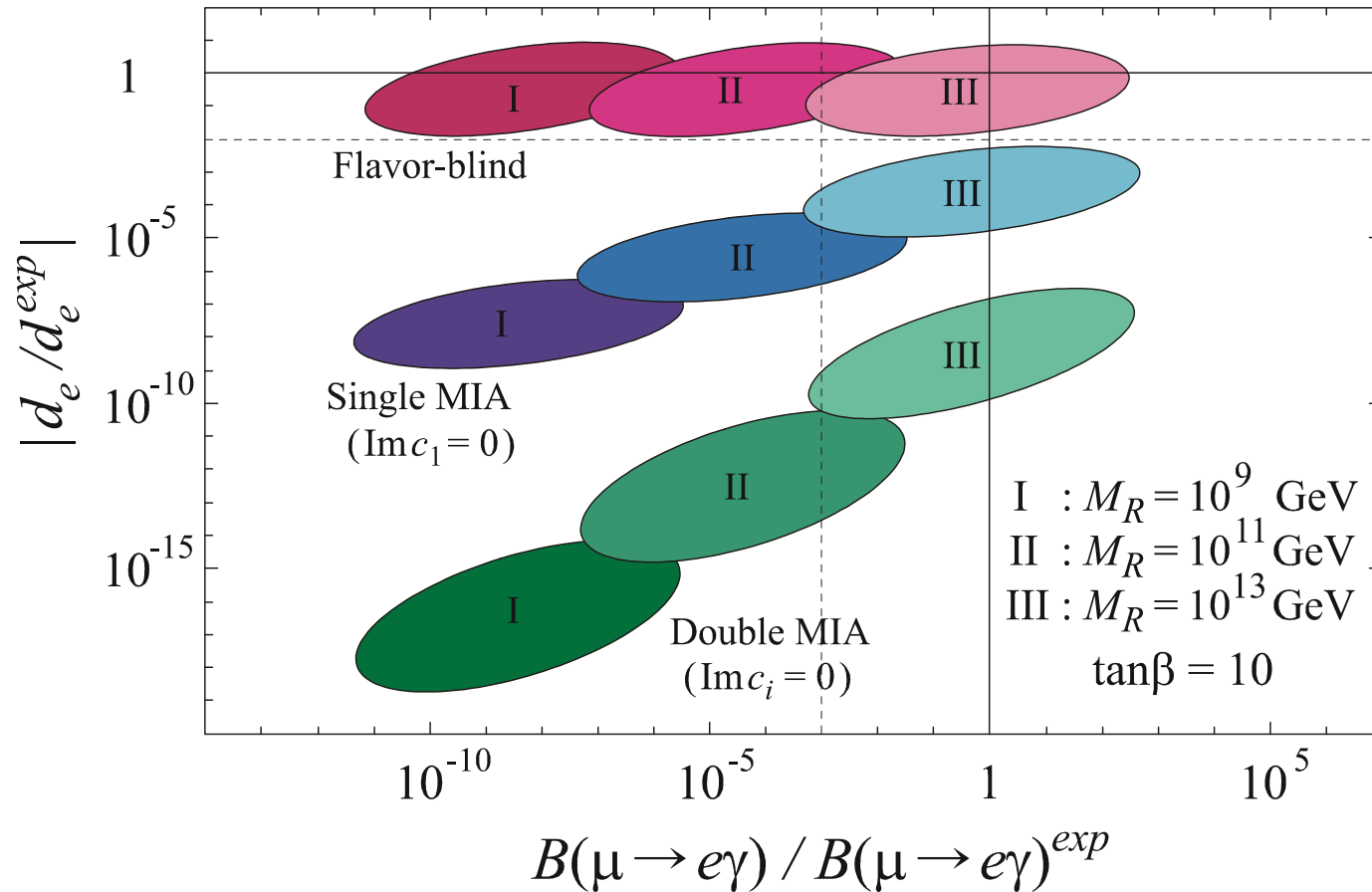
Flavor off-diagonal  
( $\geq$  neutrino phases)

$$M_{SUSY} \approx 500 \text{ GeV}$$

$$\Delta m_{21} \approx \sqrt{\Delta m_{\odot}^2} \approx 10^{-9} - 10^{-11} \text{ GeV}$$

$$\Rightarrow M_R \leq 10^{13} \text{ GeV}$$

## A. Dominant operators



$$M_2 = \pm\mu = 2M_1 = \frac{2}{3}m_0 = A_0 = 400 \text{ GeV}, \quad a_i, b_i, c_i, d_i \in \pm[0.1, 8]$$

## B. Comparison with the model-independent approach

MSSM-inspired parametrization: 
$$H_{eff} = e \frac{\alpha}{4\pi} \frac{(\mathbf{Y}_e \mathbf{Q})^{IJ}}{\Lambda^2} \bar{\Psi}_R^I \sigma_{\mu\nu} \Psi_L^J F^{\mu\nu} H_d$$

where: 
$$\begin{aligned} \mathbf{Q} = & h_1 \mathbf{1} + h_2 \mathbf{A} + h_3 \mathbf{B} + h_4 \mathbf{B}^2 + h_5 \{\mathbf{A}, \mathbf{B}\} + h_6 \mathbf{B} \mathbf{A} \mathbf{B} \\ & + g_1 i[\mathbf{A}, \mathbf{B}] + g_2 i[\mathbf{A}, \mathbf{B}^2] + g_3 i(\mathbf{B} \mathbf{A} \mathbf{B}^2 - \mathbf{B}^2 \mathbf{A} \mathbf{B}) \end{aligned}$$

$(\mathbf{A} \equiv \mathbf{Y}_e^\dagger \mathbf{Y}_e, \mathbf{B} \equiv \mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)$

*Flavor-blind:*  $\text{Im } h_1$ , for all flavor-blind parameters, including  $\mu, M_1, M_2, \dots$

*Flavor-diagonal:*  $\text{Im } h_{2-6}$ , dominated by  $\text{Im } h_3$ , LFV and EDM correlated.

*Flavor off-diagonal:* Do not contribute,  $\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu$  phases have no impact.

*Same general features*, though  $\Lambda \approx M_{SUSY}$  only up to a factor of  $\sim 5-10$ .

### C. What about the general MSSM?

$$Q = x_1 1 + x_2 A + x_3 B + x_4 B^2 + x_5 \{A, B\} + x_6 BAB \\ + x_7 i[A, B] + x_8 i[A, B^2] + x_9 i(BAB^2 - B^2 AB)$$

The MFV operators form a *complete basis* for soft-breaking terms.

Allowing the coefficients to take any value  $\rightarrow$  *full MSSM*.

Experimental data  $\Rightarrow$  *bounds on the coefficients*.

Turning on an operator  $\Leftrightarrow$  Turning on a *whole set of mass insertions*, but with a *definite pattern*, originating from those of the spurions.



Permits to test the *naturality* of soft-breaking terms.

### C. What about the general MSSM?

$m_L^2$	$(x_i / a_1)$	$m_R^2$	$(x_i / a_7)$	$\text{Re } A_e$	$(x_i / a_1 a_7)$	$\text{Im } A_e$	$(x_i / a_1 a_7)$
$a_1$	<i>free</i>	$a_7$	<i>free</i>	$\text{Re } c_1 \leq 10^2$	<i>stab.</i>	$\text{Im } c_1 \leq 2$	$d_e$
$a_2 \leq 10^3$	<i>masses</i>	$a_8 \leq 10^3$	<i>masses</i>	$\text{Re } c_2 \leq 10^3$	<i>stab.</i>	$\text{Im } c_2 \leq 10^3$	<i>stab.</i>
$a_3 \leq 10$	$\mu \rightarrow e\gamma$	$a_9 \leq 10^6$	$\tau \rightarrow \mu\gamma$	$\text{Re } c_3 \leq 10^3$	$\mu \rightarrow e\gamma$	$\text{Im } c_3 \leq 10^3$	$\mu \rightarrow e\gamma$
$a_4 \leq 10^4$	$\mu \rightarrow e\gamma$	$a_{10} \leq 10^9$	$\tau \rightarrow \mu\gamma$	$\text{Re } c_4 \leq 10^6$	$\mu \rightarrow e\gamma$	$\text{Im } c_4 \leq 10^6$	$\mu \rightarrow e\gamma$
$a_5 \leq 10^3$	$\tau \rightarrow \mu\gamma$	$a_{11} \leq 10^7$	$\tau \rightarrow \mu\gamma$	$\text{Re } c_5 \leq 10^5$	$\tau \rightarrow \mu\gamma$	$\text{Im } c_5 \leq 10^5$	$\tau \rightarrow \mu\gamma$
$a_6 \leq 10^4$	$\mu \rightarrow e\gamma$	$a_{12} \leq 10^{11}$	$\tau \rightarrow \mu\gamma$	$\text{Re } c_6 \leq 10^7$	$\mu \rightarrow e\gamma$	$\text{Im } c_6 \leq 10^7$	$\mu \rightarrow e\gamma$
$b_1 \leq 10^3$	$\tau \rightarrow \mu\gamma$	$b_4 \leq 10^7$	$\tau \rightarrow \mu\gamma$	$\text{Re } d_1 \leq 10^5$	$\tau \rightarrow \mu\gamma$	$\text{Im } d_1 \leq 10^5$	$\tau \rightarrow \mu\gamma$
$b_2 \leq 10^6$	$\tau \rightarrow \mu\gamma$	$b_5 \leq 10^{10}$	$\tau \rightarrow \mu\gamma$	$\text{Re } d_2 \leq 10^8$	$\tau \rightarrow \mu\gamma$	$\text{Im } d_2 \leq 10^8$	$\tau \rightarrow \mu\gamma$
$b_3 \leq 10^8$	$\mu \rightarrow e\gamma$	$b_6 \leq 10^{13}$	$\tau \rightarrow \mu\gamma$	$\text{Re } d_3 \leq 10^{10}$	$\mu \rightarrow e\gamma$	$\text{Im } d_3 \leq 10^{10}$	$\mu \rightarrow e\gamma$

$$M_{SUSY} \approx 500 \text{ GeV}, \tan \beta = 20, M_R = 10^{12} \text{ GeV}, m_{L,R} \leq 4 \text{ TeV}$$

**Compared to MIA:** If a coefficient must be  $x_i \gg 1 \Rightarrow$  *New flavor structures*

If a coefficient must be  $x_i \ll 1 \Rightarrow$  *Fine-tuning problem is back*

If all coefficients are  $x_i \approx 1 \Rightarrow$  *MFV*

Conclusion

*MFV does introduce (many) CP-violating phases* beyond those of the SM.

*Rich CPV phenomenology*, especially when two spurions are competitive.

*Extension to the quark sector* needs to be completed.

Is the “non-MFV” phase observed really beyond MFV?

*Application to R-parity violating MFV:*

Moderate  $M_R$  implied by  $\mu \rightarrow e \gamma \Rightarrow$  Proton decay bounds easier to pass.

The only significant coupling,  $\lambda''_{312}(t-s-d)$ , is complex. Phenomenology?

*Application to leptogenesis:* Whole series of new CP-phase within MFV.