

Model-Independent Constraints on New Physics: Minimal Flavour Violation (MFV)

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- *Outline* ---

- ① Model-Independent Analysis
 - ➡ Flavour Problem and MFV
- ② Present Constraints on MFV (*at large tan β*)
 - ➡ $\Delta F=2$ FCNC observables: $\Delta M_s, \dots$
 - ➡ $\Delta F=1$ FCNC observables: $B \rightarrow X_s \gamma, \dots$
 - ➡ $\Delta F=1$ Charged Current processes: $B \rightarrow D \tau \nu, \dots$

Model-independent Analysis: Flavour Problem

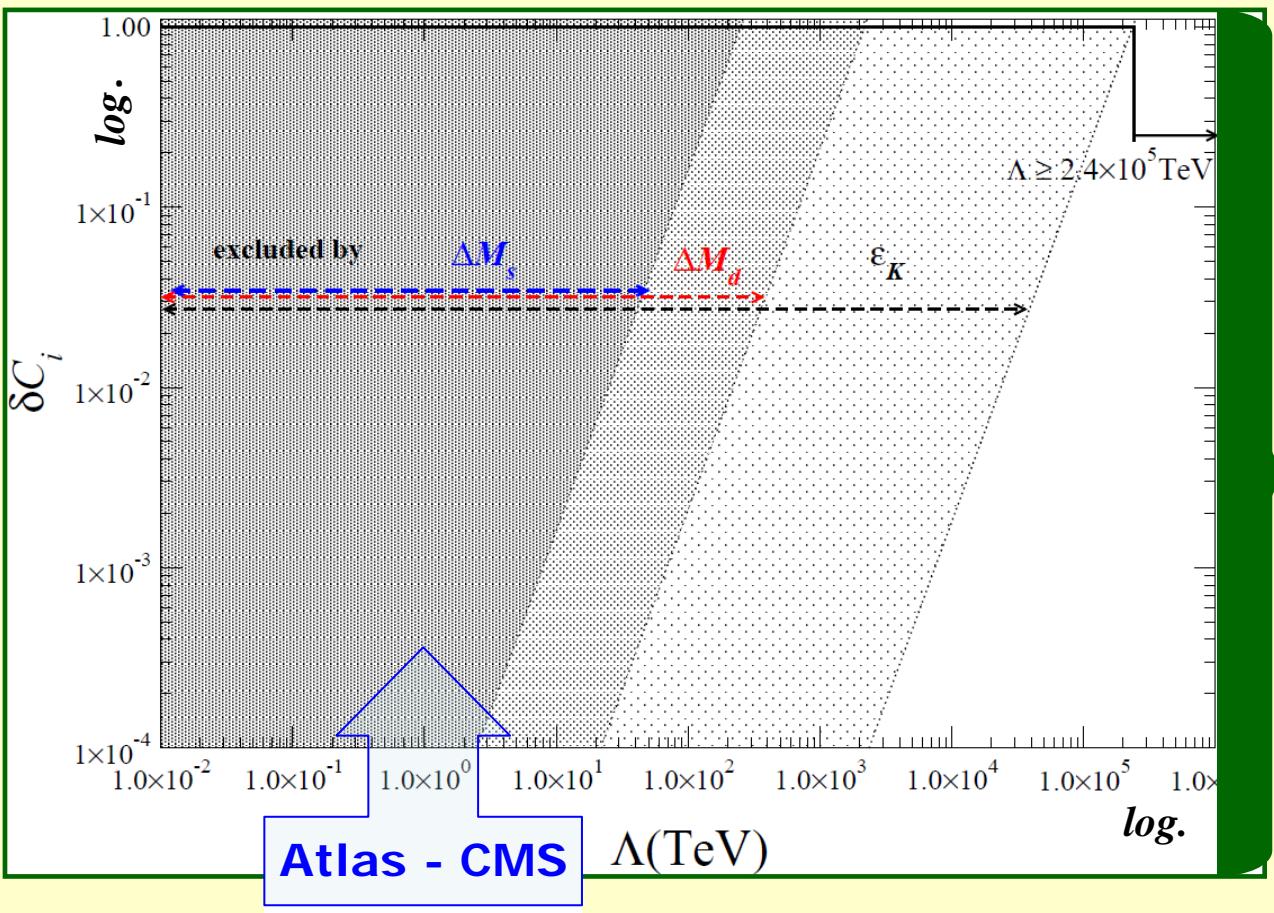
$$\mathcal{L}_{\text{eff}}(\mu \leq M_Z) = \mathcal{L}_{\text{SM}}(H, A_i, \psi_i) + \frac{\delta C_i}{\Lambda^2} \mathcal{O}_i^{(6)}$$

BSM contributions

for example,
for $\Delta F=2$ mixing:

$$\mathcal{O}_4^{(6)} = \bar{s}_R d_L \bar{s}_L d_R$$

$$\mathcal{O}_{SM}^{(6)} = \bar{s}_L \gamma^\mu d_L \bar{s}_L \gamma^\mu d_L ..$$



**Bounds for generic
flavour couplings**

⇒ $\delta C_i = 1$

$s \rightarrow d$: $\Lambda \geq 2.4 \times 10^5$ TeV ϵ_K

$b \rightarrow d$: $\Lambda \geq 2.2 \times 10^3$ TeV ΔM_d

$b \rightarrow s$: $\Lambda \geq 2.5 \times 10^2$ TeV ΔM_s

values from
UTfit 0707.0636

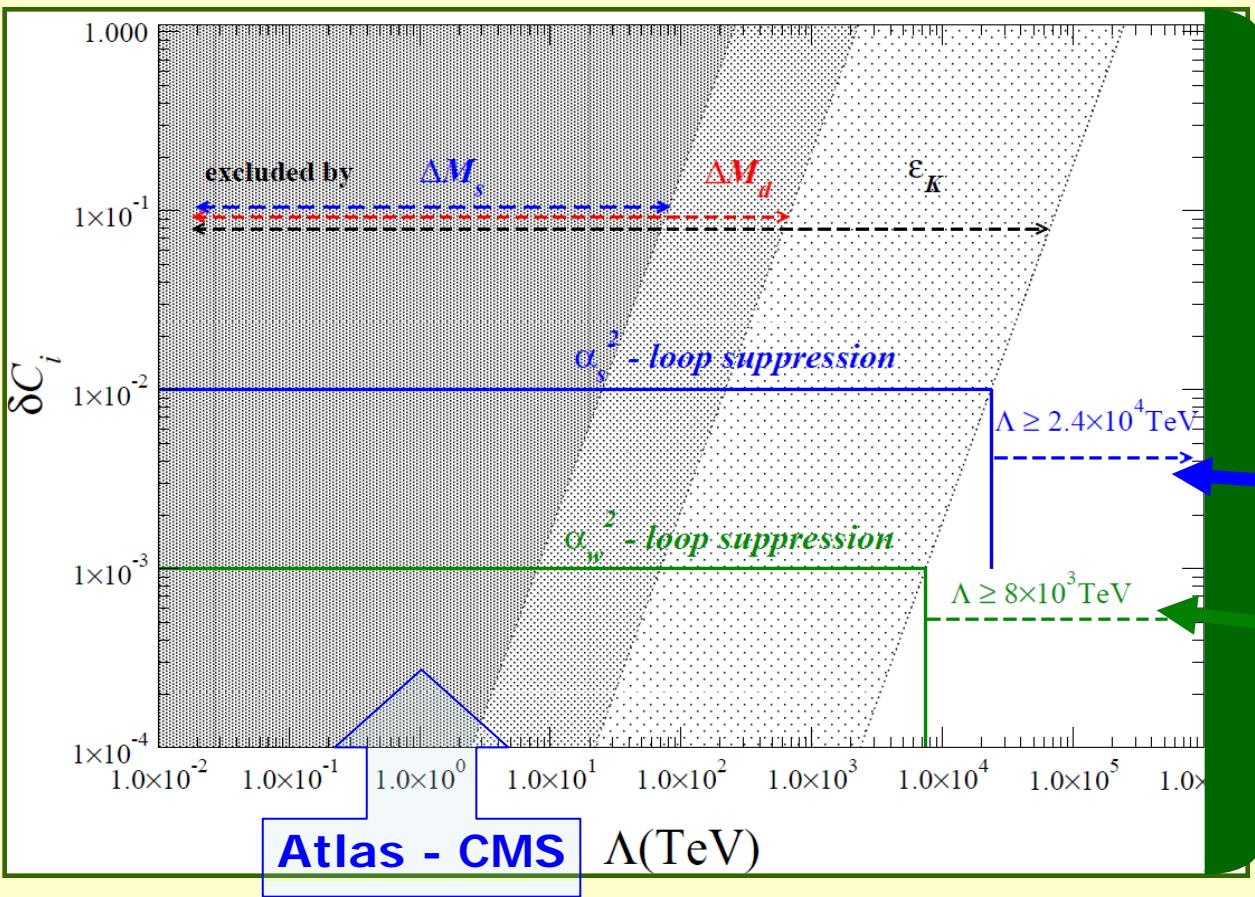
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$$\mathcal{O}_{SM}^{(6)} = \bar{s}_L \gamma^\mu d_L \bar{s}_L \gamma^\mu d_L \dots$$



Dynamical hypothesis on δC_i :

• $\delta C_i \propto \alpha_S^2$
 $\Lambda \geq 2.4 \times 10^4 \text{ TeV}$

• $\delta C_i \propto \alpha_W^2$
 $\Lambda \geq 8 \times 10^3 \text{ TeV}$

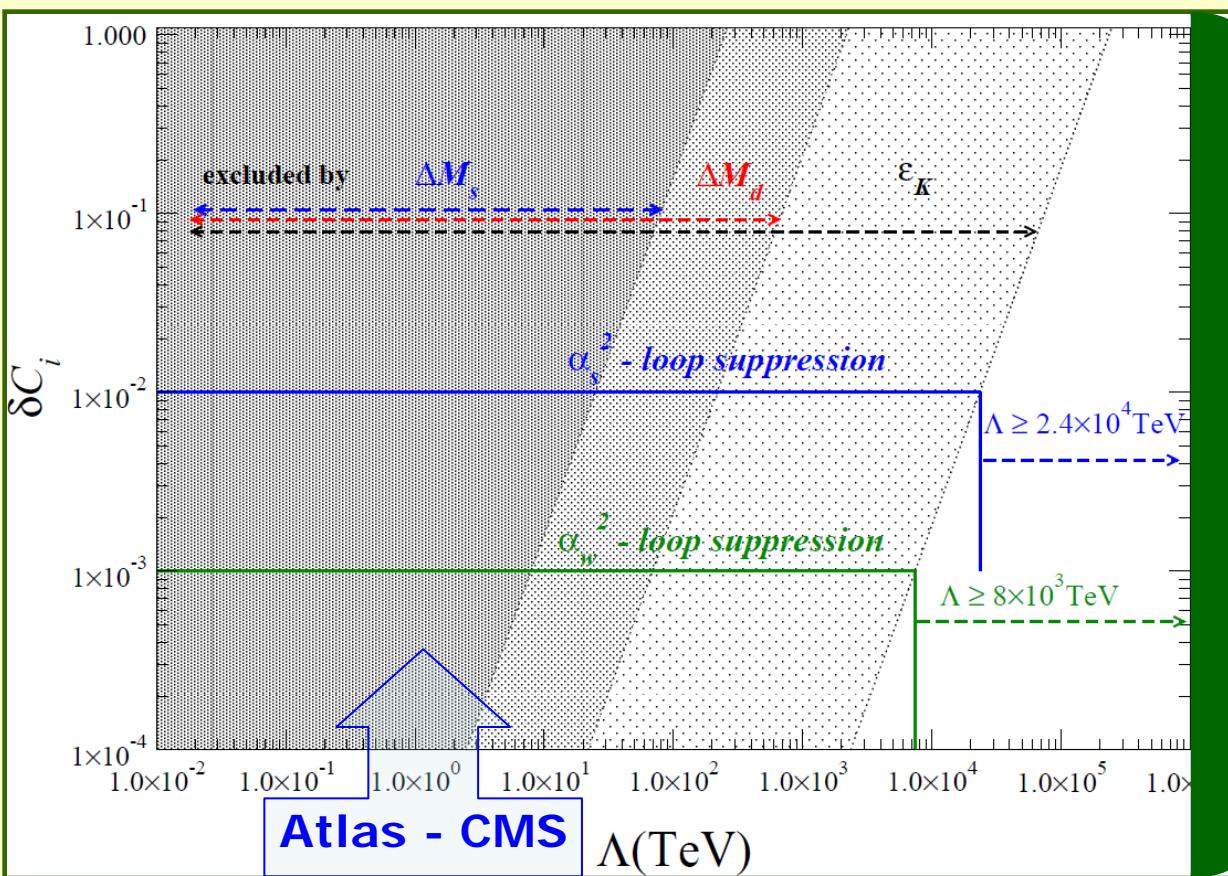
UTfit 0707.0636

does not help

Model-independent Analysis: Flavour Problem

$$\mathcal{L}_{\text{eff}}(\mu \leq M_Z) = \mathcal{L}_{\text{SM}}(H, A_i, \psi_i) + \frac{\delta C_i}{\Lambda^2} \mathcal{O}_i^{(6)}$$

$\delta C_i = 0$?
too strong restriction!



- at low energy, the minimal amount of flavour violation has been measured

$$Y_D = \hat{m}_D, Y_U = V_{CKM}^+ \hat{m}_U$$

- RGE potentially $\delta C_i \neq 0$

$$\text{" } g_{NP}^{FV} = g_{CKM}^{FV} \times \log \left(\frac{M_Z}{M_?} \right) \text{"}$$

MFV: δC_i small by symmetry!
accommodates both
flavour problem and RGE logs

Model-independent Analysis: MFV – Effective Theory (EFT)

Minimal Flavour Violation hypothesis:

[$\Lambda \sim O(1\text{TeV}) + \delta C_i$ natural small by additional symmetries]



The breaking of the flavour symmetry occurs at very high scales and is mediated at low energy only by terms proportional to SM Yukawa couplings preserving the $U(3)^5$ SM Flavour group.

EFT: D'Ambrosio, Giudice, Isidori & Strumia '02

$$\longrightarrow \delta C_i \propto (y_t^2 V_{tk}^* V_{tj})^2 \quad (\text{for FCNC with ext. } d\text{-type quark})$$

- Possibility of building a low-energy EFT: model-independent studies

Recently,

MFV in non-linear r.: Kagan, Perez, Zupan, Volansky '09; CPV: Mercolli & Smith '09

this afternoon

Smith '09

Wed. morning

RGE logs: Paradisi, Ratz, Schieren, Simonetto '08; Colangelo, Nikolaidakis, Smith '08;

earlier: Buras, Gambino, Gorbahn, Jager, L. Silvestrini '00

Chivukula & Georgi '86, J.L. Hall & L. Randall '90

Model-independent Analysis: $\Delta F=2$ constraints in MFV

EFT: D'Ambrosio, Giudice, Isidori & Strumia '02

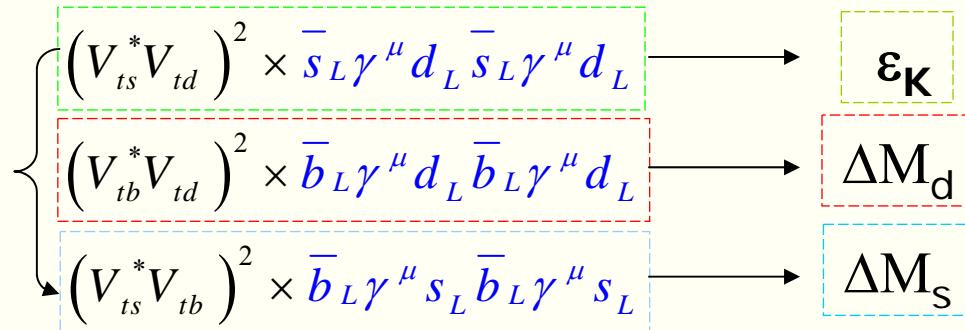
$$\mathcal{L}_{\text{eff}}^{\text{MFV}} = \sum_i \frac{\delta C_i}{\Lambda^2} \mathcal{O}_i^{(6)}$$

\mathcal{O} basis invariant under $SU(3)_{Q_L} \times SU(3)_{U_R} \times SU(3)_{D_R}$
 \mathcal{O} 's written in terms of $Y_U = \mathbf{3}_{Q_L} \times \mathbf{3}_{U_R}$, $Y_D = \mathbf{3}_{Q_L} \times \mathbf{3}_{D_R}$

- Due to the large top Y , $Y_U Y_U^+ \propto y_t^2 \sim O(1)$

$$1) \quad \mathcal{O}_{SM}^{(6)} = \bar{Q}_L Y_U Y_U^+ \gamma^\mu Q_L \cdot \bar{Q}_L Y_U Y_U^+ \gamma^\mu Q_L$$

1 Higgs doublet, SM basis complete \rightarrow CMFV

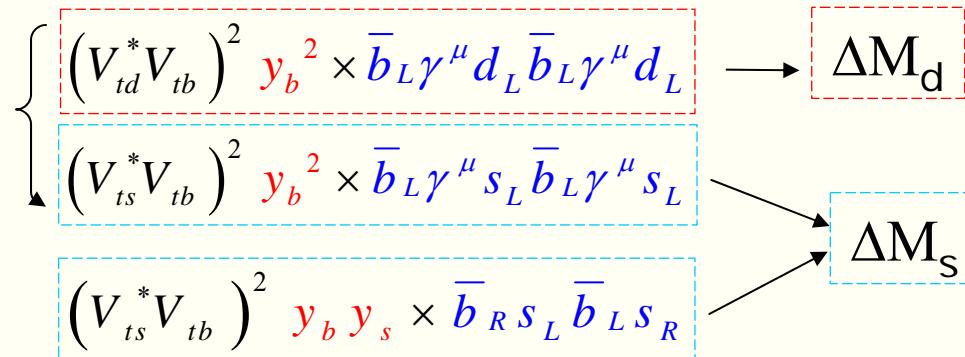


Buras, Gambino, Gorbahn, Jager, L. Silvestrini '00

- Adding Higgs doublets, $Y_D \propto m_b / m_t \frac{\langle H_U \rangle}{\langle H_D \rangle} \sim O(1)$ (*$\tan\beta$ enhancement of down-type YDs*)

$$2) \quad (\bar{Q}_L Y_D Y_D^+ Y_U Y_U^+ \gamma^\mu Q_L)^2$$

$$3) \quad \bar{D}_R Y_D^+ Y_U Y_U^+ Q_L \cdot \bar{Q}_L Y_U Y_U^+ Y_D D_R$$



A few extra $\mathcal{O}^{(6)}$'s in a clear pattern between $s \rightarrow d$ & $b \rightarrow d$, $b \rightarrow s$ transitions

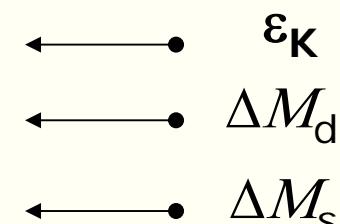
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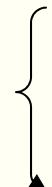


$$\left\{ \begin{array}{l} \Lambda \geq 5.5 \text{ TeV} \\ \Lambda \geq 0.5 \text{ TeV} \\ \text{loop-suppr} \end{array} \right.$$



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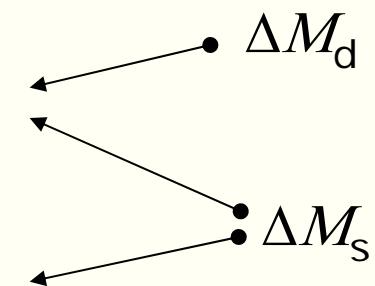
$$2) \quad \left(\bar{Q}_L Y_D Y_D^+ Y_U Y_U^+ \gamma^\mu Q_L \right)^2$$



$$\Lambda \geq 5.1 \text{ TeV}$$

$$3) \quad \bar{D}_R Y_D^+ Y_U Y_U^+ Q_L \cdot \bar{Q}_L Y_U Y_U^+ Y_D D_R$$

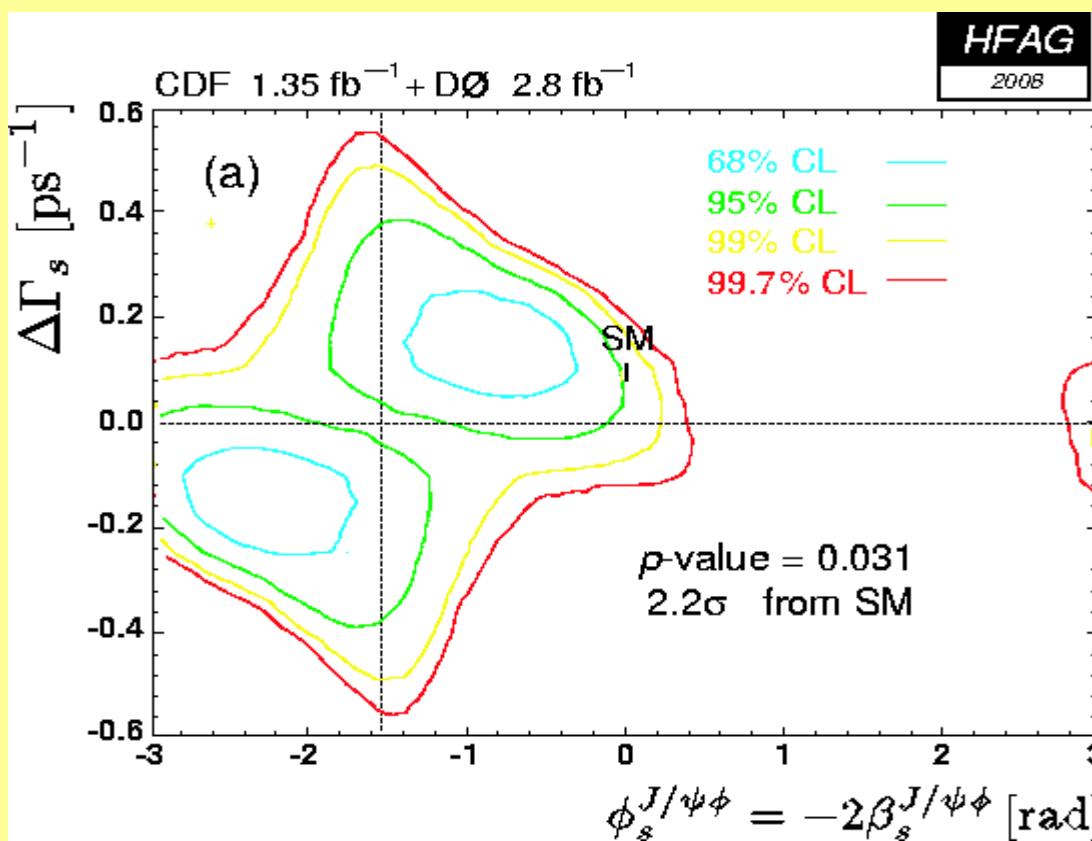
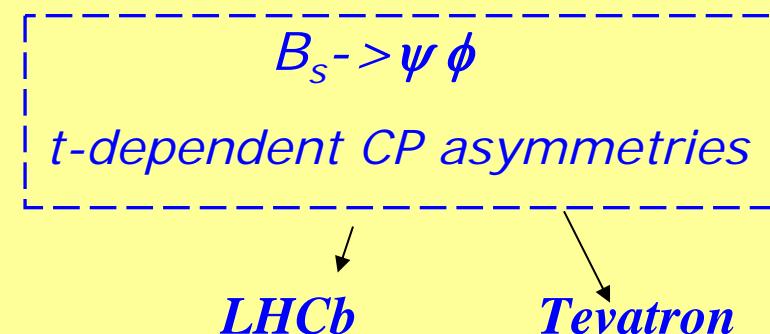
$$M_H \geq 5. \tan\beta/50 \text{ TeV}$$



Model-independent Analysis: $\Delta F=2$ constraints in MFV

❖ CPV signals in the B_s sector:

$$\beta_s^{MFV} \approx \beta_s^{SM}$$



$$\phi_s = -2\beta_s$$

UTfit 0803.0659

Model-independent Analysis: $\Delta F=1$ FCNC constraints in MFV

$$\mathcal{L}_{\text{eff}}^{\text{MFV}} = \sum_i \frac{\delta C_i}{\Lambda^2} \mathcal{O}_i^{(6)}$$

$$(\lambda_{\text{FC}})_{ij} = (Y_U Y_U^\dagger)_{ij}$$

- $\Delta F=1$ Higgs field:

$$\mathcal{O}_{H1} = i (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L) H_U^\dagger D_\mu H_U , \quad \mathcal{O}_{H2} = i (\bar{Q}_L \lambda_{\text{FC}} \tau^a \gamma_\mu Q_L) H_U^\dagger \tau^a D_\mu H_U ,$$

- $\Delta F=1$ gauge field:

$$\mathcal{O}_{G1} = H_D (\bar{Q}_L \lambda_{\text{FC}} \lambda_d \sigma_{\mu\nu} \bar{T}^a D_R) (g_s G_{\mu\nu}^a) , \quad \mathcal{O}_{G2} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu T^a Q_L) (g_s \bar{D}_\mu G_{\mu\nu}^a)$$

$$\mathcal{O}_{F1} = H_D (\bar{Q}_L \lambda_{\text{FC}} \lambda_d \sigma_{\mu\nu} D_R) (e F_{\mu\nu}) , \quad \mathcal{O}_{F2} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L) (e D_\mu F_{\mu\nu}) ,$$

- $\Delta F=1$ semileptonic field:

$$\mathcal{O}_{\ell 1} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L) (\bar{L}_L \gamma_\mu L_L) , \quad \mathcal{O}_{\ell 2} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu \tau^a Q_L) (\bar{L}_L \gamma_\mu \tau^a L_L) ,$$

$$\mathcal{O}_{\ell 3} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L) (\bar{E}_R \gamma_\mu E_R) ,$$

- $\Delta F=1$ scalar density: 2 Higgs doublets

$$\mathcal{O}_{S1} = (\bar{Q}_L \lambda_{\text{FC}} \lambda_d D_R) (\bar{E}_R \lambda_\ell L_L)$$

~ many $\Delta F=1$ operators
 $H_U \rightarrow H_D$ and/or $\lambda_{\text{FC}} \rightarrow Y_D Y_D^\dagger \lambda_{\text{FC}}$

after
ewsb

$$\mathcal{Q}_7 = \frac{e}{g^2} m_j \bar{d}_i \sigma_{\mu\nu} (1 + \gamma_5) d_j F_{\mu\nu} ,$$

$$\mathcal{Q}_8 = \frac{g_s}{g^2} m_j \bar{d}_i \sigma_{\mu\nu} T^a (1 + \gamma_5) d_j G_{\mu\nu}^a$$

$$\mathcal{Q}_9 = \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \sum_\ell \bar{\ell} \gamma_\mu \ell$$

$$\mathcal{Q}_{10} = \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \sum_\ell \bar{\ell} \gamma_\mu \gamma_5 \ell$$

$$\mathcal{Q}_{\nu\bar{\nu}} = \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \sum_\nu \bar{\nu} \gamma_\mu (1 - \gamma_5) \nu$$

$$\mathcal{Q}_S^\ell = \bar{d}_i (1 + \gamma_5) d_j \bar{\ell} (1 - \gamma_5) \ell$$

6 $\Delta F=1$ independent combinations after ewsb:
(as much as available $\Delta F=1$ "clean" observables)

Model-independent Analysis: $\Delta F=1$ FCNC constraints in MFV

$Br(B_d \rightarrow X_s \gamma)_{E_\gamma > 1.6 \text{ GeV}}$

th (7%): $(3.13 \pm 0.23) \times 10^{-4}$

exp (7%): $(3.52 \pm 0.24) \times 10^{-4}$

NNLO: Misiak et al '06

HFAG

$b \rightarrow s$

$s \rightarrow d$

$Br(B_d \rightarrow X_s l^+ l^-)$: 3 bins (out of r.)

exp (30%):

$[q^2 \in [0.04, 1.0] \text{ GeV}^2]$	$(0.6 \pm 0.5) \times 10^{-6}$
$[q^2 \in [1.0, 6.0] \text{ GeV}^2]$	$(1.6 \pm 0.5) \times 10^{-6}$
$[q^2 > 14.4 \text{ GeV}^2]$	$(4.4 \pm 1.3) \times 10^{-7}$

th (10-25%):

$(0.8 \pm 0.2) \times 10^{-6}$
$(1.6 \pm 0.1) \times 10^{-6}$
$(2.4 \pm 0.8) \times 10^{-7}$

$Br(B_s \rightarrow \mu^+ \mu^-)$:

Babar+Belle

NNLO: Bobeth et al. '01,
Asatrian et al., '02

th (20%): $(4.1 \pm 0.8) \times 10^{-9}$

Exp: $< 5.8 \times 10^{-8}$ (95% CL) CDF

$A_{FB}(B_d \rightarrow K^* l^+ l^-)$: 2 bins

exp (large): Babar+Belle '09

$[q^2 < 6.25 \text{ GeV}^2]$	$0.24^{+0.19}_{-0.24}$	-0.01 ± 0.02
$[q^2 > 10.24 \text{ GeV}^2]$	$0.76^{+0.53}_{-0.34}$	0.20 ± 0.08 [%]

$Br(K^+ \rightarrow \pi^+ \nu \bar{\nu})$:

BNL $(14.7^{+13.0}_{-8.9}) \times 10^{-11}$ **th** (10%):

$$Q_7 = \frac{e}{g^2} m_j \bar{d}_i \sigma_{\mu\nu} (1 + \gamma_5) d_j F_{\mu\nu},$$

$$Q_8 = \frac{g_s}{g^2} m_j \bar{d}_i \sigma_{\mu\nu} T^a (1 + \gamma_5) d_j G_{\mu\nu}^a$$

$$Q_9 = \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \sum_\ell \bar{\ell} \gamma_\mu \ell$$

$$Q_{10} = \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \sum_\ell \bar{\ell} \gamma_\mu \gamma_5 \ell$$

$$Q_{\nu\bar{\nu}} = \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \sum_\nu \bar{\nu} \gamma_\mu (1 - \gamma_5) \nu$$

$$Q_S^\ell = \bar{d}_i (1 + \gamma_5) d_j \bar{\ell} (1 - \gamma_5) \ell$$

6 $\Delta F=1$ independent combinations after ewsb:
(can now be constrained by $\Delta F=1$ observables)

Model-independent Analysis: $\Delta F=1$ FCNC constraints in MFV

Hurth, Isidori, Kamenik, F.M '08

$\delta C_i \star$	95% probability bound	Observables
δC_7	$[-0.14, 0.06] \cup [1.42, 1.62]$	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
δC_9	$[-2.8, 0.8]$	$B \rightarrow X_s \ell^+ \ell^-$
δC_{10}	$[-0.4, 2.3]$	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$\delta C_S^\mu/m_b$	$[-0.09, 0.09]/(4.2\text{GeV})$	$B_s \rightarrow \mu^+ \mu^-$
$\delta C_{\nu\bar{\nu}}$	$[-6.1, 2.0]$	$K^+ \rightarrow \pi^+ \nu\bar{\nu}$

available range for δC_i in MFV
=>predictions

$$Q_7 = \frac{e}{g^2} m_j \bar{d}_i \sigma_{\mu\nu} (1 + \gamma_5) d_j F_{\mu\nu},$$

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$$Q_S^\ell = \bar{d}_i (1 + \gamma_5) d_j \bar{\ell} (1 - \gamma_5) \ell$$

★ Mind: CKM couplings factorized out

$O(1\text{TeV})$ scale as much as
 $\Delta F=2$ constraints



Operator	$\Lambda_i @ 95\%$	Observables
$H_D^\dagger (\bar{D}_R \lambda_d \lambda_{FC} \sigma_{\mu\nu} Q_L) (e F_{\mu\nu})$	6.1	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$H_D^\dagger (\bar{D}_R \lambda_d \lambda_{FC} \sigma_{\mu\nu} T^a Q_L) (g_s G_{\mu\nu}^a)$	3.4	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$(\bar{Q}_L \lambda_{FC} \gamma_\mu Q_L) (e D_\mu F_{\mu\nu})$	1.5	$B \rightarrow X_s \ell^+ \ell^-$
$i (\bar{Q}_L \lambda_{FC} \gamma_\mu Q_L) H_U^\dagger D_\mu H_U$	1.1 ^a	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$i (\bar{Q}_L \lambda_{FC} \tau^a \gamma_\mu Q_L) H_U^\dagger \tau^a D_\mu H_U$	1.1 ^a	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$(\bar{Q}_L \lambda_{FC} \gamma_\mu Q_L) (\bar{L}_L \gamma_\mu L_L)$	1.7	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$(\bar{Q}_L \lambda_{FC} \gamma_\mu \tau^a Q_L) (\bar{L}_L \gamma_\mu \tau^a L_L)$	1.7	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$(\bar{Q}_L \lambda_{FC} \gamma_\mu Q_L) (\bar{E}_R \gamma_\mu E_R)$	2.7	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$

for CMFV: Bobeth, Bona, Buras, Ewerth, Pierini, Silvestrini Weiler '05

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available range for δC_i in MFV
=>predictions

1) Predictions in MFV: way to test and falsify MFV

Observable	Experiment	MFV bound	SM prediction
$R^{(\mu/e)}(B \rightarrow K \ell^+ \ell^-) - 1$	0.17 ± 0.28	$[-0.004, 0.14]$	$O(10^{-4})$ [64]
$R^{(\mu/e)}(B \rightarrow K^* \ell^+ \ell^-) - 1$	$0.37^{+0.53}_{-0.40} \pm 0.09$	$[-0.002, 0.01]$	$\lesssim 10^{-2}$
$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$	$< 1.8 \times 10^{-8}$	\star	$< 1.2 \times 10^{-9}$
$\mathcal{B}(B \rightarrow X_s \tau^+ \tau^-)$	–	\star	$< 5 \times 10^{-7}$
$\mathcal{B}(B \rightarrow K \nu\bar{\nu})$		\star	$(0.5 \pm 0.1) \times 10^{-5}$
$\mathcal{B}(B \rightarrow K^* \nu\bar{\nu})$		\star	$(0.68 \pm 0.10) \times 10^{-5}$
$\mathcal{B}(K_L \rightarrow \pi^0 \nu\bar{\nu})$		\star	$2.9(5) \times 10^{-11}$

★ room for NP contributions

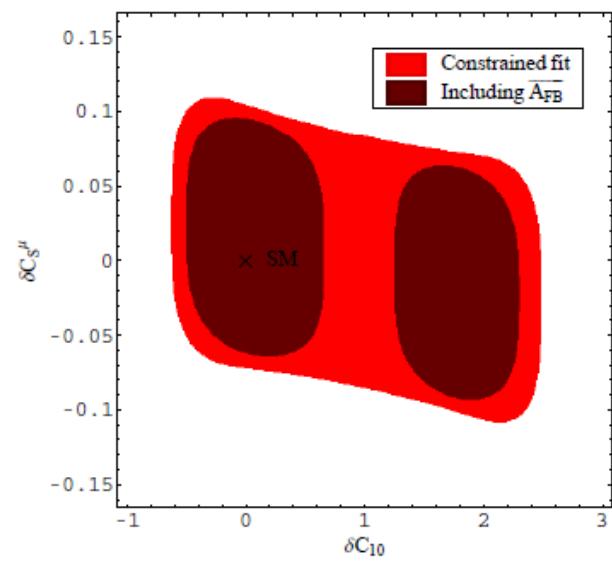
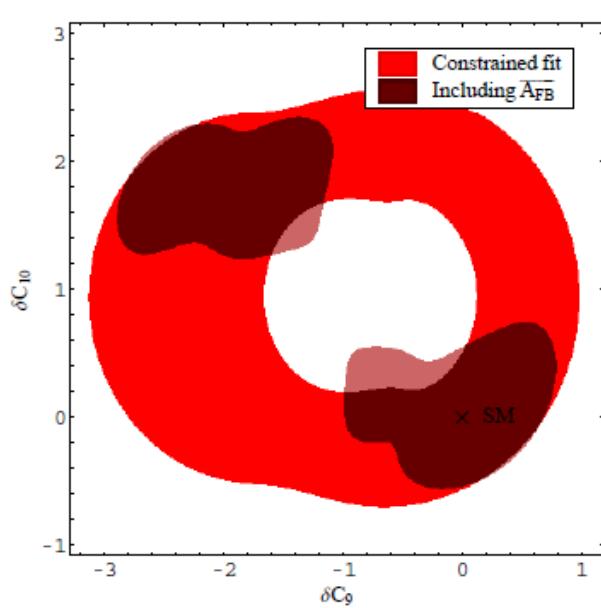
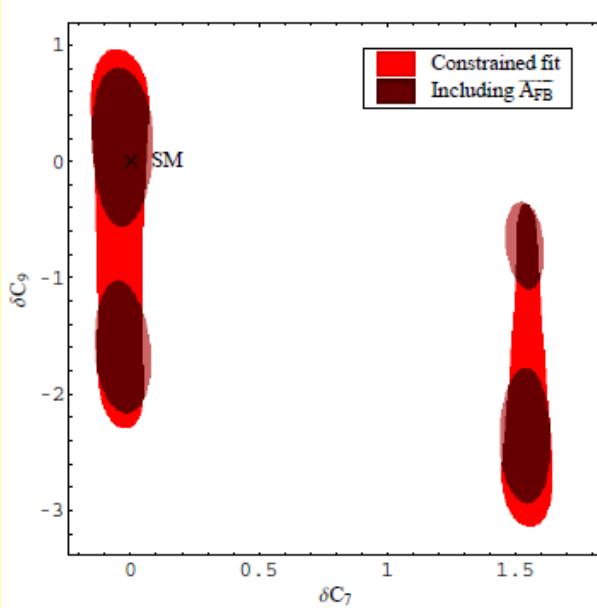
for $B \rightarrow K(*) \nu\bar{\nu}$, recently
Altmannshofer, Buras, Straub Wick '09

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Hurth, Isidori, Kamenik, F.M '08

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available range for δC_i in MFV
=>predictions



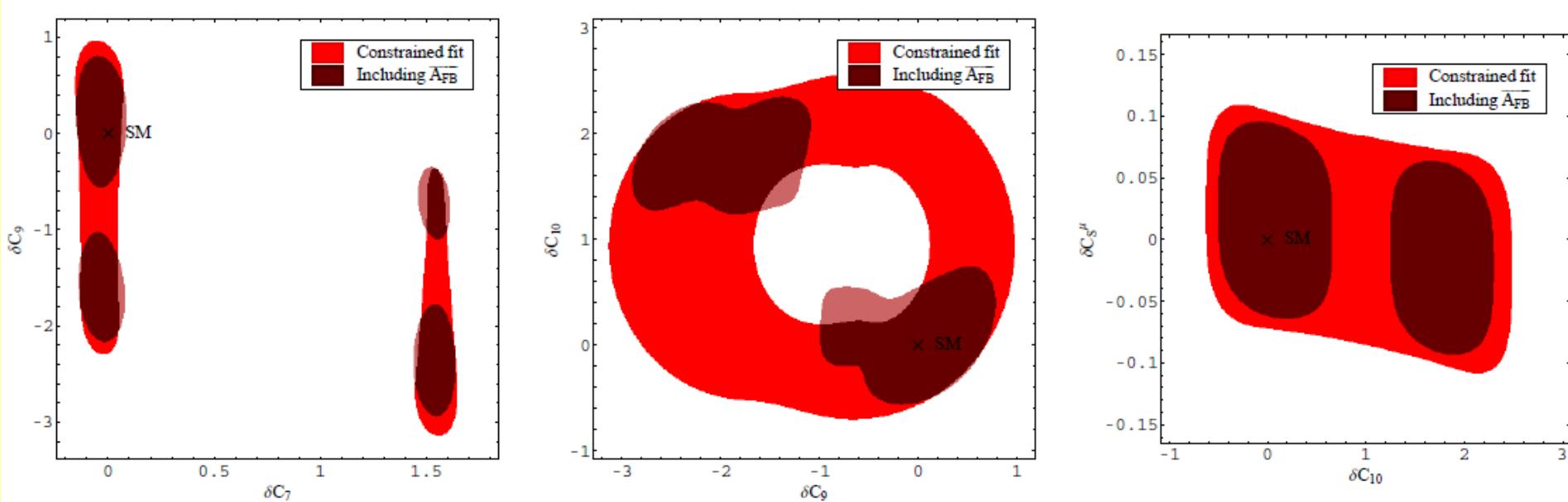
$A_{FB}(B_d \rightarrow K^* l^+ l^-)$, plays a special role: large exp err. but sensitive to independent δC_i

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Hurth, Isidori, Kamenik, F.M '08

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available range for δC_i in MFV
=>predictions



$B_d \rightarrow K^* l^+ l^-$: in future, full angular analysis gives access to other th. clean obs: LHCb, SFF

recent refs: Egede et al. '08, Altmannshofer et al. '08

Model-independent Analysis: $\Delta F=1$ FCNC constraints in MFV

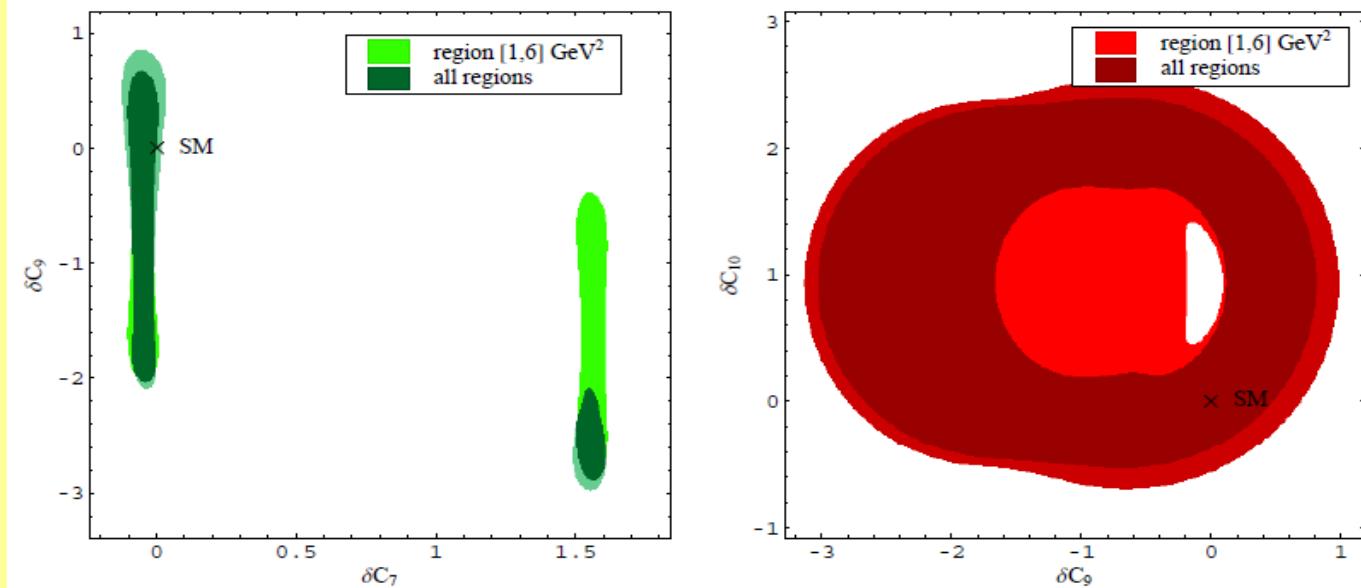
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δC_{10}	$[-0.4, 2.3]$	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$\delta C_S^\mu/m_b$	$[-0.09, 0.09]/(4.2 \text{ GeV})$	$B_s \rightarrow \mu^+ \mu^-$
$\delta C_{\nu\bar{\nu}}$	$[-6.1, 2.0]$	$K^+ \rightarrow \pi^+ \nu\bar{\nu}$

available range for δC_i in MFV
=>predictions

$B_d \rightarrow X_s l^+ l^-$: interesting information from low and high q^2 bin

$[q^2 \in [0.04, 1.0] \text{ GeV}^2]$
 $[q^2 \in [1.0, 6.0] \text{ GeV}^2]$
 $[q^2 > 14.4 \text{ GeV}^2]$



Model-independent Analysis: $\Delta F=1$ FCNC constraints in MFV

δC_i	95% probability bound	Observables
δC_7	$[-0.14, 0.06] \cup [1.42, 1.62]$	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
δC_9	$[-2.8, 0.8]$	$B \rightarrow X_s \ell^+ \ell^-$
δC_{10}	$[-0.4, 2.3]$	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$\delta C_S^\mu/m_b$	$[-0.09, 0.09]/(4.2\text{GeV})$	$B_s \rightarrow \mu^+ \mu^-$
$\delta C_{\nu\bar{\nu}}$	$[-6.1, 2.0]$	$K^+ \rightarrow \pi^+ \nu\bar{\nu}$

available range for δC_i in MFV
 \Rightarrow predictions

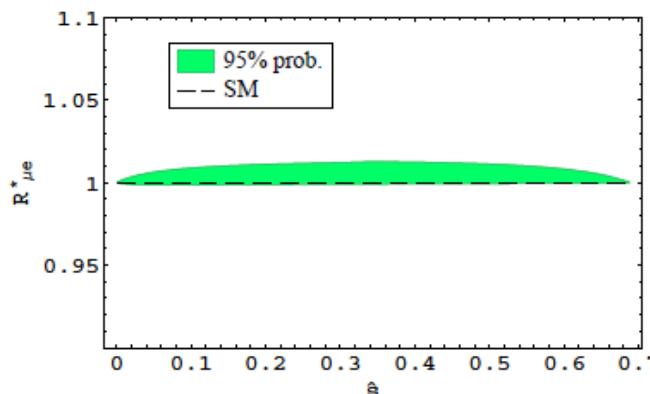
2) Predictions in MFV: way to test and falsify MFV

- Predictive relations between observables linked by CKM factors

$$\frac{\Gamma(B_s \rightarrow \ell^+ \ell^-)}{\Gamma(B_d \rightarrow \ell^+ \ell^-)} \approx \frac{f_{B_s} m_{B_s}}{f_{B_d} m_{B_d}} \left| \frac{V_{ts}}{V_{td}} \right|^2 .$$

valid at both small and large $\tan \beta$!

- $R_{K^*} \equiv \Gamma(B \rightarrow K^* \mu^+ \mu^-)/\Gamma(B \rightarrow K^* e^+ e^-)$ close to SM values even at large $\tan \beta$



Hurth, Isidori, Kamenik, F.M '08

Hiller & Kruger '03

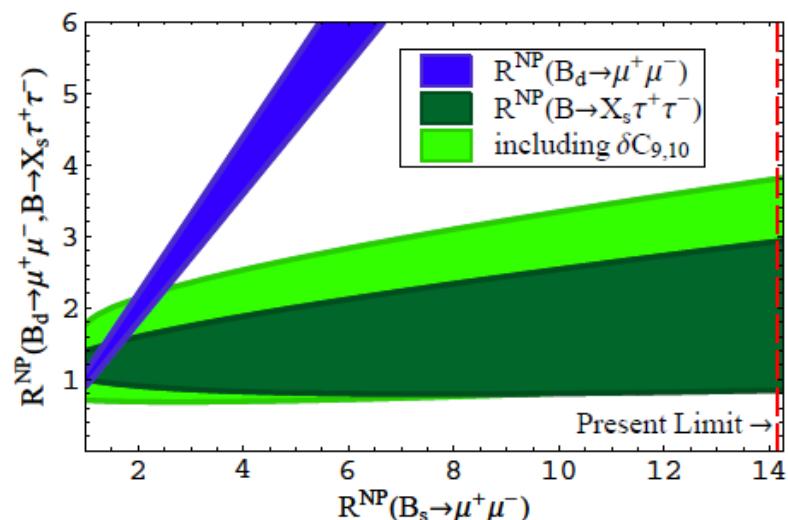
Model-independent Analysis: $\Delta F=1$ FCNC constraints in MFV

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$\delta C_{\nu\bar{\nu}}$	$[-6.1, 2.0]$	$K^+ \rightarrow \pi^+ \nu\bar{\nu}$

available range for δC_i in MFV
=>predictions

3) Predictions in MFV: way to test and falsify MFV

- $B \rightarrow X_s \tau^+ \tau^-$ - room for density operator contributions: m_τ / m_μ relative enhancement - (SM $\times 3$ contributions to Br still allowed)



$\tan\beta$ enhancement at work

Hurth, Isidori, Kamenik, F.M '08

Model-independent Analysis:

Flavour Changing Neutral Current constraints in MFV

- Bounds can be set on the complete set of MFV contributions at both small and large $\tan\beta$

extra operators

- Bounds on NP contributions from $\Delta F=2$ obs very constraining

$$\Lambda \geq 5 \text{ TeV}$$

- in $\Delta F=1$ processes,
 - mainly $\delta C_{7\gamma}$ very constraining
 - not all ambiguities can be resolved

$$\Lambda \geq 6 \text{ TeV}$$

Tree level NP d.o.f: $\Lambda \geq 6 \text{ TeV}$

Loop-suppressed NP d.o.f: $\Lambda \geq 0.6 \text{ TeV}$

$\Delta F=1$ Charged Current Processes: H^+ bounds

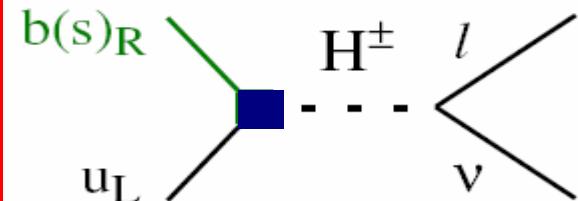
$$\mathcal{L}_{\text{eff}}^{\text{CC}} = \frac{4G_F}{\sqrt{2}} V_{qb} \sum_{\substack{\ell=e,\mu,\tau \\ U=u,c}} \left(\bar{U} \gamma^\mu b \bar{\ell}_L \gamma^\mu v_L + C_{NP}^{\ell} \bar{U}_L b_R \bar{\ell}_R v_L \right)$$

In MFV

$$C_{NP}^{\tau} = -\frac{m_b m_{\tau}}{M_{H^+}^2} \frac{\tan^2 \beta}{1 + \varepsilon_0 \tan \beta}$$

- *$\tan \beta$ enhancement of down-type Ys: competitive to $W^{\pm}_{||}$ tree-level exchange*
- *the sign of C_{NP}^{ℓ} fixed in MFV: destructive interference with SM*
- *$\varepsilon_0 \tan \beta$ resumes $U(1)_{PQ}$ breaking corrections*
 $=> 2\text{HDM} \rightarrow \varepsilon_0 \sim 0.00$ and $SUSY \rightarrow \varepsilon_0 \sim 0.01 \times f(M_{\text{Susy}})$

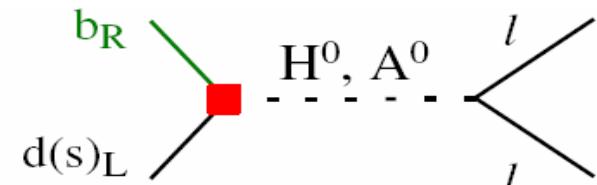
Tree-level H^+ exchange



CC

$$\begin{aligned} B^{\pm} &\rightarrow \tau^{\pm} \nu \\ B^{\pm} &\rightarrow D \tau^{\pm} \nu \\ (K^{\pm} \rightarrow \mu^{\pm} \nu) \end{aligned}$$

Complementary to H^0 searches



FCNC

$$B_{s,d} \rightarrow l^+ l^-$$

$\Delta F=1$ Charged Current Processes: H^+ bounds

$$C_{NP}^\tau = -\frac{m_b m_\tau}{M_{H^+}^2} \frac{\tan^2 \beta}{1 + \varepsilon_0 \tan \beta} \quad (\text{MFV})$$

$B^\pm \rightarrow \tau^\pm \nu$

$$Br(B \rightarrow \tau \nu) \propto |V_{ub}|^2 f_B^2 m_B m_\tau^2 \times \left(1 + \frac{m_B^2}{m_B m_\tau} C_{NP}^\tau\right)^2$$

1. helicity suppressed in the SM, m_τ

2. hadronic uncertainty in f_B :

~20% accuracy from Lattice

(use $\Delta m_d \propto f_B^2$ for Δm_d NP free,
like in MFV-MSSM)

$Br = (1.41 \pm 0.43) \times 10^{-4}$ [Belle-Babar]

Best for indirect H^+ searches
but only feasible at • SuperB

Isidori & Paradisi '06;
earlier: Hou '93; Akeroyd & Recksiegel '03

$B^\pm \rightarrow D^- \tau^+ \nu$

$$\begin{aligned} \frac{d\Gamma(B \rightarrow D \tau \nu)}{dq^2} \propto & |V_{cb}|^2 \rho_V(q^2) \\ & \times \left(1 - \left| \frac{m_\tau^2}{m_B^2} \left(1 + \frac{t(w)}{(m_b - m_c)m_\tau}\right)^2 \rho_S(q^2) \right|^2 \right) \end{aligned}$$

1. ρ_V : vector component (~ 0.5 Br) $\rightarrow W^\pm$
 $=>$ from exp. $B \rightarrow D \tau \nu$ spectrum & Lattice

2. ρ_S : scalar component (~ 0.5 Br) $\rightarrow W^\pm, H^\pm$
 $=>$ helicity suppressed m_τ

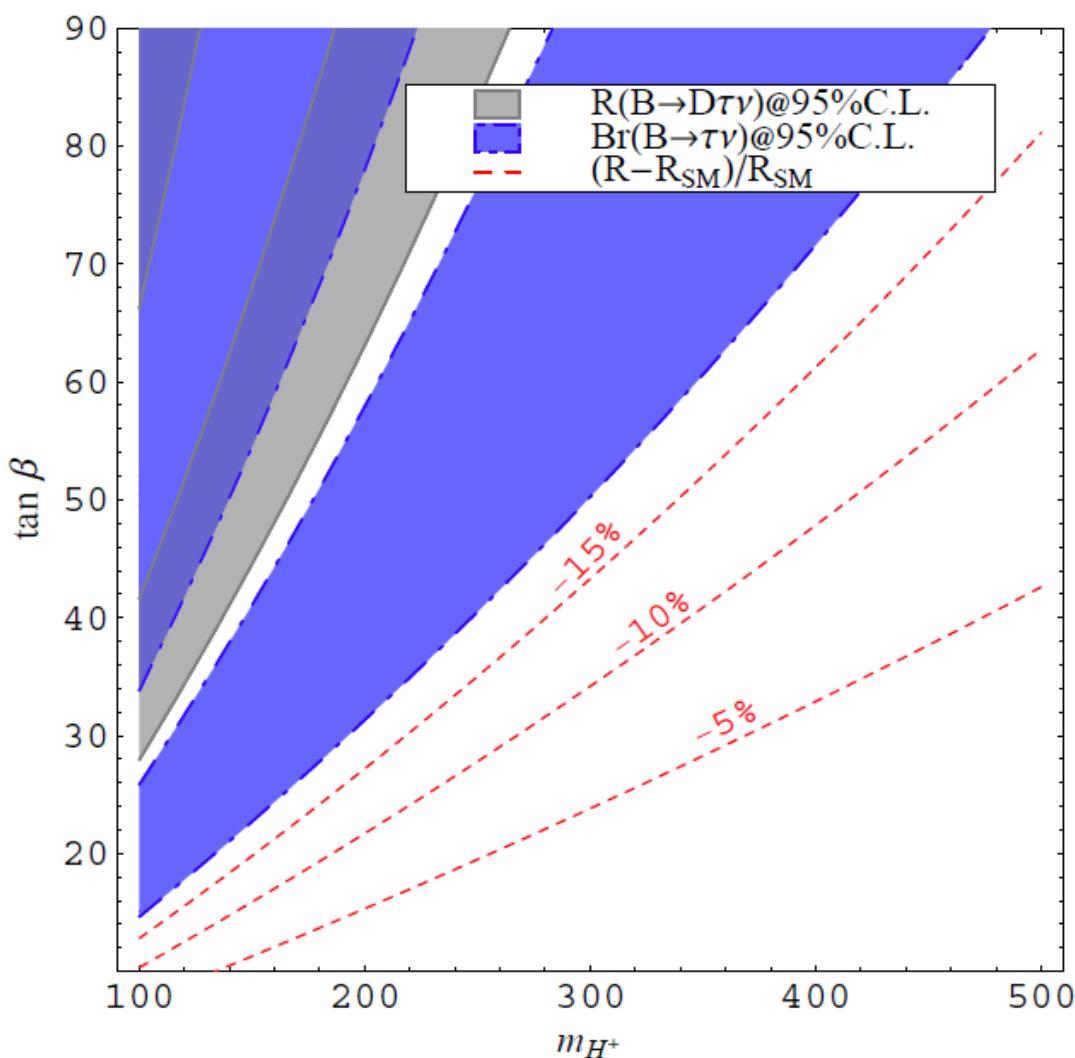
$Br = (0.86 \pm 0.30) \times 10^{-2}$ [Babar]

Only scalar component sensitivity
to H^+ but opportunity for Lhcb

Kamenik & F.M '08; Nierste, Trine, Westhoff '08,
Trine ICHEP08. earlier: Hou '93; Kiers & Soni '97

$\Delta F=1$ Charged Current Processes: H^+ bounds

$$C_{NP}^\tau = -\frac{m_b m_\tau}{M_{H^+}^2} \frac{\tan^2 \beta}{1 + \varepsilon_0 \tan \beta} \quad (\text{MFV})$$



To reduce hadronic uncertainty it is useful to consider the ratio
 $R = \text{Br}(B \rightarrow D\tau\nu) / \text{Br}(B \rightarrow D\bar{e}\nu)$

in the SM, uncertainty of $\text{Br}(B \rightarrow D\tau\nu) / \text{Br}(B \rightarrow D\bar{e}\nu) \sim 6\%$

H^+ bounds with $R(B \rightarrow D\tau\nu)$:
not as sensitive as $\text{Br}(B \rightarrow \tau\nu)$,
but competitive thanks
different exp. & theory
prospects

Kamenik & F.M '08:
Nierste, Trine, Westhoff '08

updates on, Trine ICHEP'08

Conclusions:

The MFV allows us for a bottom -> up approach:

- ⇒ testable and model-independent predictions

① $\beta_s^{MFV} \approx \beta_s^{SM}$

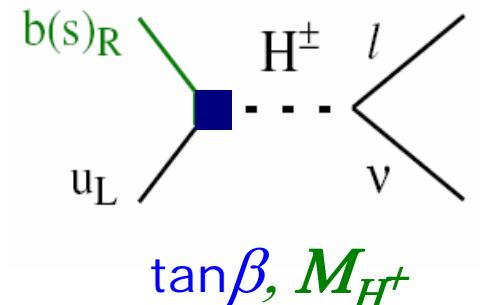
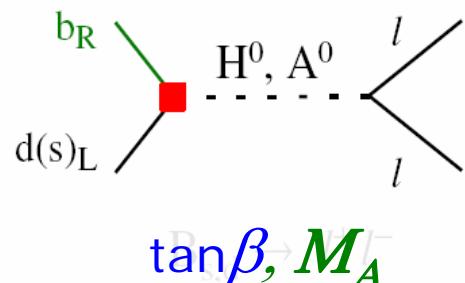
②

$$\frac{\Gamma(B_s \rightarrow \ell^+ \ell^-)}{\Gamma(B_d \rightarrow \ell^+ \ell^-)} \approx \frac{f_{B_s} m_{B_s}}{f_{B_d} m_{B_d}} \left| \frac{V_{ts}}{V_{td}} \right|^2$$

- ⇒ powerful tool to analyse future precise data on Flavour Physics
- ⇒ with the flavour constraints embedded in MFV, the residual info directly points to Atlas-CMS searches (**masses and FC couplings**):

interplay

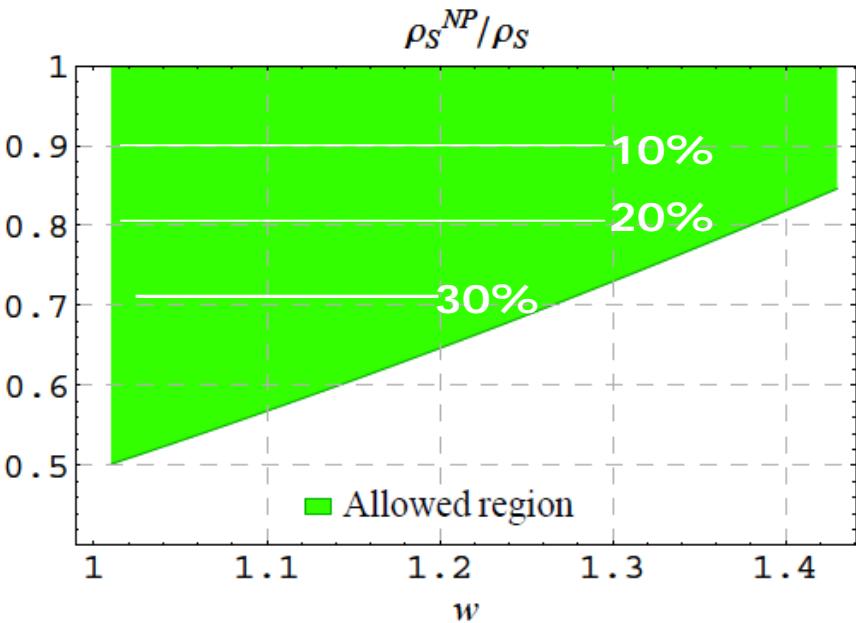
$\Lambda \geq 6 \text{ TeV}$,



$\Delta F=1$ Charged Current Processes: H^+ bounds

$$C_{NP}^\tau = -\frac{m_b m_\tau}{M_{H^+}^2} \frac{\tan^2 \beta}{1 + \varepsilon_0 \tan \beta} \quad (\text{MFV})$$

$$\rho_S^{NP}(w) = \left| 1 + \frac{t(w)}{(m_b - m_c)m_\tau} C_{NP}^\tau \right|^2 \rho_S(w)$$



$B^\pm \rightarrow D \tau^\pm \nu$

$$\frac{d\Gamma(B \rightarrow D \tau \nu)}{dw} \propto |V_{cb}|^2 \rho_\nu(w)$$

$$\times \left(1 - \frac{m_\tau^2}{m_B^2} \left| 1 + \frac{t(w)}{(m_b - m_c)m_\tau} C_{NP}^\tau \right|^2 \rho_S(w) \right)$$

2. ρ_S : scalar component (~ 0.5 Br) $\rightarrow W^\pm, H^\pm$



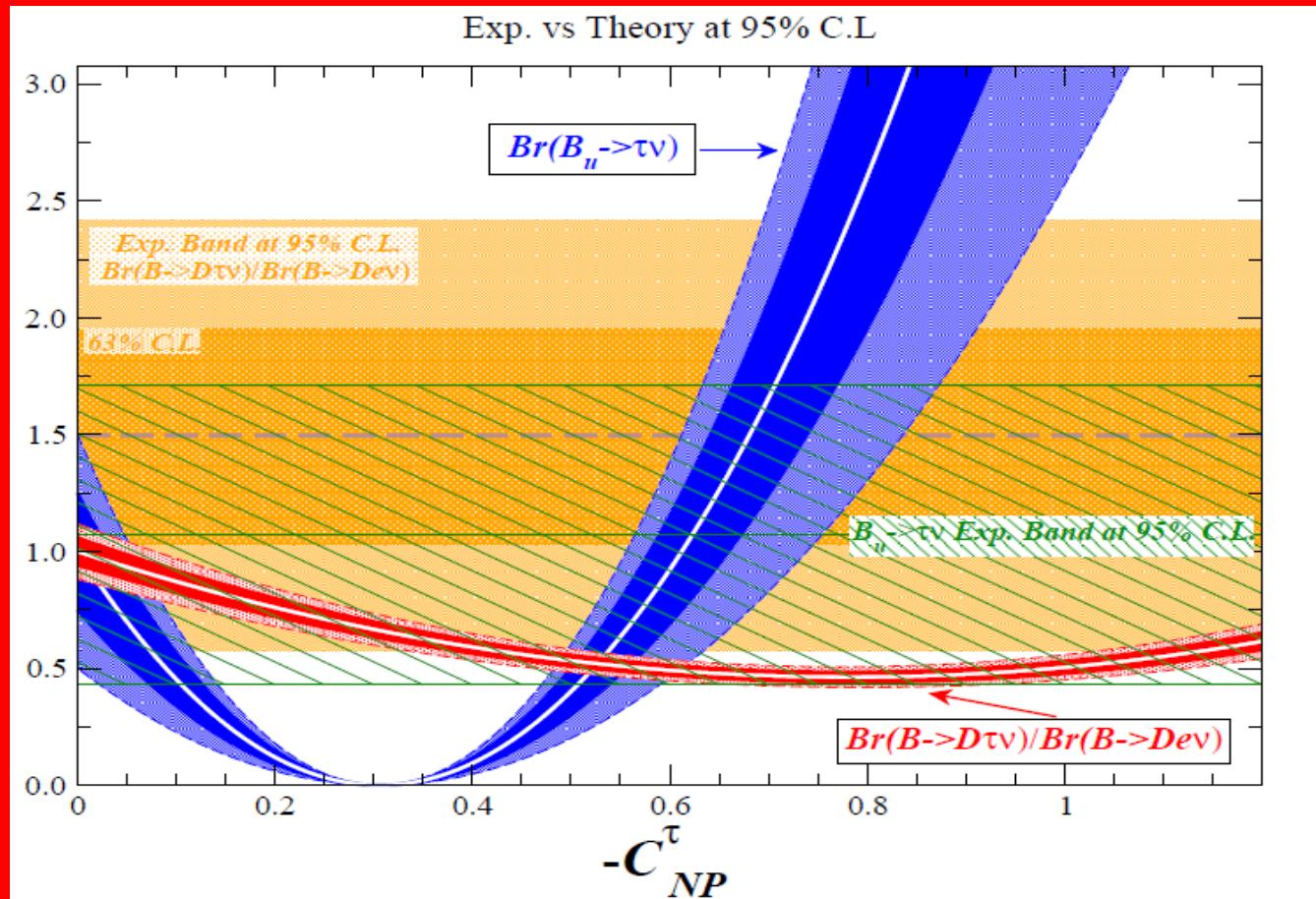
=> elicity suppresses m_τ

$\Delta F=1$ Charged Current Processes: H^+ bounds

$$C_{NP}^\tau = -\frac{m_b m_\tau}{M_{H^+}^2} \frac{\tan^2 \beta}{1 + \varepsilon_0 \tan \beta} \quad (\text{MFV})$$

$B^\pm \rightarrow \tau^\pm \nu$

$B^\pm \rightarrow D \tau^\pm \nu$

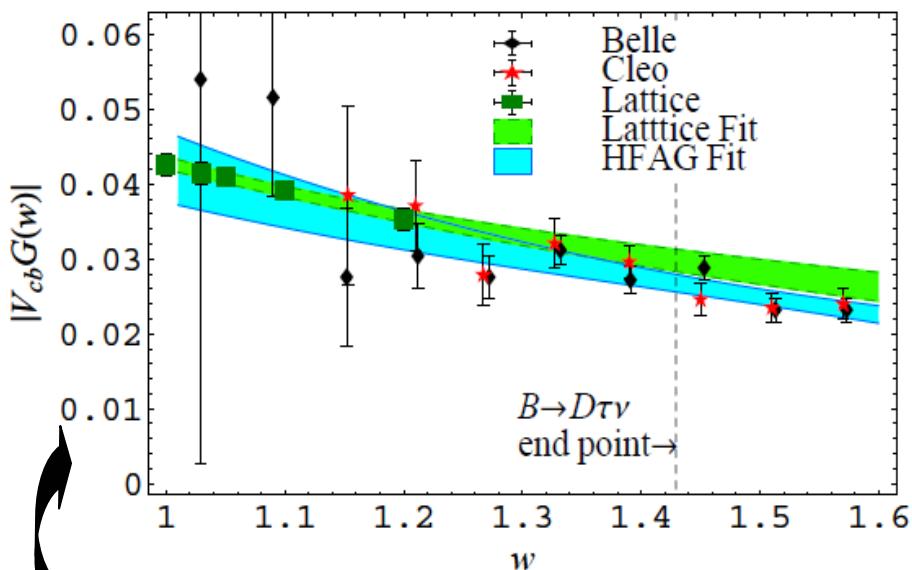


$\Delta F=1$ Charged Current Processes: H^+ bounds

HFAG'08:

De Divitiis, Petronzio and Tantalo '07'08

$B \rightarrow D\bar{v}$ spectrum



ρ_V :

- under control by the exp. $B \rightarrow D\bar{v}$ spectrum &/or Lattice: ~5%
-> can be improved by Belle!
- partially cancels in the ratio $B \rightarrow D\tau\nu/B \rightarrow D\bar{v}$*

ρ_s : from Lattice => ratio of ffs and symmetry at work

$B^\pm \rightarrow D \tau^\pm \nu$

$$\frac{d\Gamma(B \rightarrow D\tau\nu)}{dw} \propto |V_{cb}|^2 \rho_V(w)$$

$$\times \left(1 - \frac{m_\tau^2}{m_B^2} \left| 1 + \frac{t(w)}{(m_b - m_c)m_\tau} C_{NP}^\tau \right|^2 \rho_s(w) \right)$$

1. ρ_V : vector component (~0.5 Br) $\rightarrow W^\pm$

Kamenik & F.M '08:Nierste, Trine, Westhoff '08