

# Sparticle Parameters from the LHC and Their Impact on LFV

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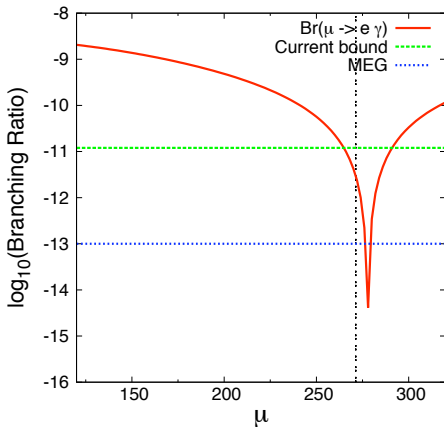
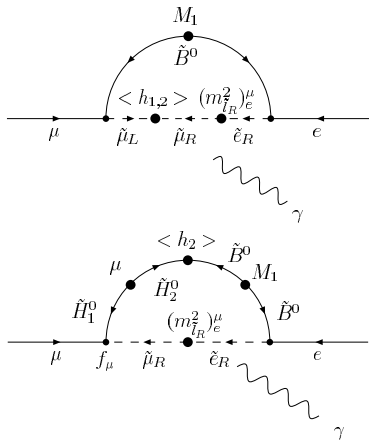
March 17, 2009

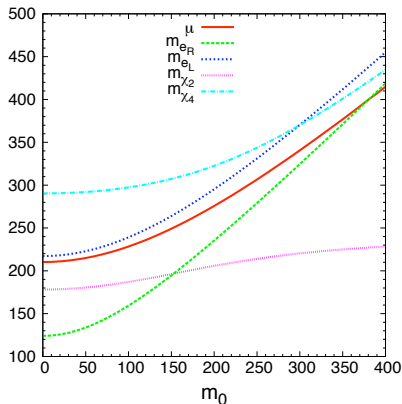
*In collaboration with J. Hisano and M. M. Nojiri, arXiv:0812.4496*

# Motivation

$$\mu \rightarrow e \gamma$$

Right-handed LFV  $\Rightarrow$  Cancellation among dominant diagrams





At the cancellation point,

$$\frac{1}{2m_{\tilde{l}_L}^2} - \frac{1}{m_{\tilde{l}_R}^2} f_1\left(\frac{\mu^2}{m_{\tilde{l}_R}^2}\right) \sim 0. \quad (1)$$

In the plot,

- i)  $m_{1/2} = 300$  GeV,  $\tan\beta = 10$
- ii) mSUGRA-like relations are assumed among  $M_1, M_2$ , and slepton masses
- iii)  $\mu$  is free (NUHM)

- ▶  $\mu \sim m_{\tilde{l}_L}$  along the cancellation line
- ▶  $\mu$  is smaller as  $m_0$  decreases  $\Rightarrow$  DM relic density is small and  $\tilde{\chi}_4^0 \rightarrow \tilde{e}_L$  and  $\tilde{\chi}_2^0 \rightarrow \tilde{e}_R$  are always kinematically allowed.

# Non-universal Higgs Mass Model (NUHM)

- H. Baer, A. Mustafayev, S. Profumo, A. Belyaev, X. Tata, Phys. Rev. D71, 095008 (2005).  
J. Ellis, K. A. Olive, Y. Santoso, Phys. Lett. B539, 107 (2002).  
M. Drees *et al.*, Phys. Rev. D63, 035008 (2001).  
J. Hisano, R. Kitano, M. M. Nojiri, Phys. Rev. D65:116002 (2002).

We took  $m_{H_U} > m_{H_D} = m_0$ , particularly with  $M_1 < M_2 < \mu \sim m_{1/2}$  and dark matter relic density consistent with observations.

Moreover, we took the choice  $m_{\tilde{\chi}_1^0} < m_{\tilde{e}_R} < m_{\tilde{\chi}_2^0} < m_{\tilde{e}_L} < m_{\tilde{\chi}_4^0}$  when both left- and right-handed sleptons can be directly produced via neutralino decay.

# LFV Model

J.L. Feng, C.G. Lester, Y. Nir, Y. Shadmi, arXiv:0712.0674

Consider a horizontal  $U(1) \times U(1)$  symmetry where each  $U(1)$  is explicitly broken by a scalar singlet spurion carrying the corresponding charge -1.

Symmetry breaking parameter  $\epsilon \sim |V_{us}| \sim 0.2$

$$L_1(4, 0), \quad L_2(2, 2), \quad L_3(0, 4), \quad \bar{E}_1(1, 0), \quad \bar{E}_2(1, -2), \quad \bar{E}_3(0, -3)$$

$\Rightarrow$  Slepton masses:

$$M_L^2 = m_L^2 + \times m_0^2 X'_L, \quad M_{\bar{e}}^2 = m_{\bar{e}}^2 + \times m_0^2 X'_{\bar{e}}, \quad (2)$$

where

$$X'_L \sim \begin{pmatrix} 0 & \epsilon^4 & \epsilon^8 \\ \epsilon^4 & 0 & \epsilon^4 \\ \epsilon^8 & \epsilon^4 & 0 \end{pmatrix}, \quad X'_{\bar{e}} \sim \begin{pmatrix} 0 & \epsilon^2 & \epsilon^4 \\ \epsilon^2 & 0 & \epsilon^2 \\ \epsilon^4 & \epsilon^2 & 0 \end{pmatrix} \quad (3)$$

## Contents

1. A model point near the cancellation point with correct DM relic density
2. Sparticle masses and parameters determination from endpoint information
3. Flipping solution exercises

Key observables:

- ▶ 2 jets + missing  $E_T$
  - ▶ relative edge heights
  - ▶ charge asymmetry
4. LFV and DM density

## MC Study

ISAJET v7.75 + HERWIG 6.5 + AcerDet

# of generated events =  $5 \times 10^6 \rightarrow \sim 300 \text{ fb}^{-1}$  of integrated luminosity

point A:

$m_0$	100	$m_{1/2}$	300
$m_{H_D}$	100	$m_{H_U}$	380
$A_0$	0	$\tan \beta$	10

$\Rightarrow \mu = 271 \text{ GeV}$   
 $\Omega_{\text{DM}} h^2 = 0.1179$

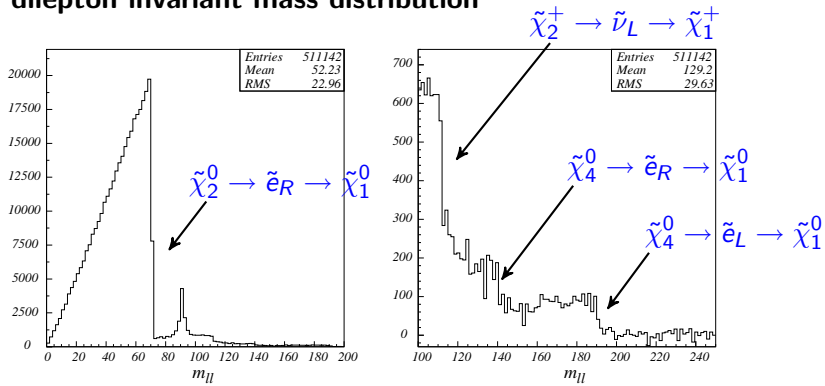
	A	mSUGRA		A	mSUGRA
$\tilde{u}_L \rightarrow \tilde{\chi}_2^0$	25.4	31.6	$\tilde{\chi}_2^0 \rightarrow \tilde{e}_R$	13.5	3.1
$\tilde{u}_L \rightarrow \tilde{\chi}_4^0$	7.8	1.3	$\tilde{\chi}_4^0 \rightarrow \tilde{e}_R$	0.7	0.3
$\tilde{u}_L \rightarrow \tilde{\chi}_2^+$	13.1	1.8	$\tilde{\chi}_4^0 \rightarrow \tilde{e}_L$	2.3	1.0
			$\tilde{\chi}_2^+ \rightarrow \tilde{\nu}_L$	7.4	2.1

( $\mu = 397.3 \text{ GeV}$  for mSUGRA point)

$\Rightarrow$  For point A,  $\tilde{\chi}_4^0$  and  $\tilde{\chi}_2^+$  have more Wino component.

$\Rightarrow$  Enhancement in  $Br(\tilde{u}_L \rightarrow \tilde{\chi}_4^0/\tilde{\chi}_2^+)$  by at least factor 6.

# OSSF dilepton invariant mass distribution



- ▶ Including  $m_{jll}^{max}$ ,  $m_{jl}^{max}$ ,  $m_{jl}^{min}$ , one can resolve  $m_{\tilde{q}_L}$ ,  $m_{\tilde{\chi}_4^0}$ ,  $m_{\tilde{\chi}_2^0}$ ,  $m_{\tilde{\chi}_1^0}$ ,  $m_{\tilde{e}_L}$ ,  $m_{\tilde{e}_R}$ .
- ▶ A study of four-lepton (2OSSF) events reveals  $m_{ll}^{max}(\tilde{\chi}_4^0 \rightarrow \tilde{e}_L \rightarrow \tilde{\chi}_1^0)$ .
- ▶  $m_{\tilde{e}_L} - m_{\tilde{\chi}_1^0} = 124.92^{+0.65}_{-0.65}$  GeV,  $m_{\tilde{e}_R} - m_{\tilde{\chi}_1^0} = 15.68^{+0.45}_{-0.49}$  GeV



## Flipping Solutions

- |                                  |  |
|----------------------------------|--|
| (1) $M_1 < M_2 < \mu$ (point A)  | } $m_{\tilde{u}_L}, m_{\tilde{\chi}_4^0}, m_{\tilde{\chi}_2^0} (m_{\tilde{\chi}_3^0} \text{ for A3}), m_{\tilde{\chi}_1^0}, m_{\tilde{e}_L}, m_{\tilde{e}_R}$<br>are degenerate between three points<br>$\Rightarrow$ endpoints from their cascade decay<br>will be the same |
| (2) $M_1 < \mu < M_2$ (point A2) |  |
| (3) $\mu < M_1 < M_2$ (point A3) |  |

We investigate whether three solutions can be discriminated @ the LHC.

For point A2,

- ▶  $\tilde{\chi}_4^0$  and  $\tilde{\chi}_2^+$  have more Wino component  $\Leftarrow$  Branching ratios
- ▶  $\tilde{\chi}_2^0$  has less Wino component  $\Leftarrow$  Charge asymmetry

For point A3,

- ▶  $\tilde{\chi}_1^0$  is Higgsino-like  $\Leftarrow$  2 jets + missing  $E_T$

## 2 jets + missing $E_T$

C. G. Lester and D. J. Summers, Phys. Lett. B463, 99 (1999)  
 A. Barr, C. Lester and P. Stephens, J. Phys. G29, 2343 (2003)

$$Br(\tilde{q}_R \rightarrow \tilde{\chi}_1^0) = \begin{cases} 0.94 & \text{point A} \\ 0.89 & \text{point A2} \\ 0.16 & \text{point A3} \end{cases}$$

For  $pp \rightarrow \tilde{q}_R \tilde{q}_R \rightarrow q \tilde{\chi}_1^0 q \tilde{\chi}_1^0$  events, their signature is two high- $p_T$  jets + large  $E_T$ .

$$m_{T2}(\mathbf{p}_T^j, \mathbf{p}_T^j, \mathbf{p}_T^{\text{miss}}; m_{\text{test}}) \equiv \min_{\mathbf{p}_T^\alpha + \mathbf{p}_T^\beta = \mathbf{p}_T^{\text{miss}}} \left[ \max \left\{ m_T(\mathbf{p}_T^j, \mathbf{p}_T^\alpha; m_{\text{test}}), m_T(\mathbf{p}_T^j, \mathbf{p}_T^\beta; m_{\text{test}}) \right\} \right]$$

$$m_T^2(\mathbf{p}_T^j, \mathbf{p}_T^\alpha; m_{\text{test}}) \equiv m_j^2 + m_{\text{test}}^2 + 2 \left( E_T^j E_T^\alpha - \mathbf{p}_T^j \cdot \mathbf{p}_T^\alpha \right).$$

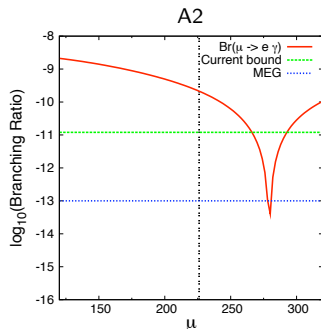
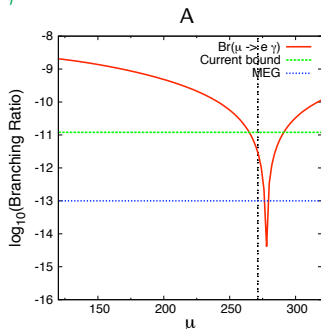
$$m_{T2}(m_{\text{test}} = m_{\tilde{\chi}_1^0}) \leq m_{\tilde{q}_R}$$

Point	No. of Signal	No. of SM Background	S/ $B_{SM}$	S/ $\sqrt{B_{SM}}$
A	1341	180	7.5	100.0
A3	133	180	0.7	9.9

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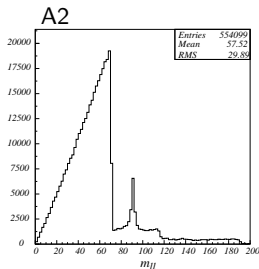
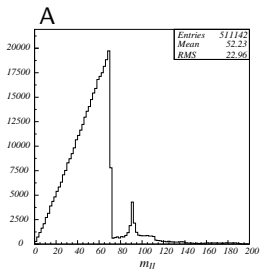
$\mu \rightarrow e\gamma$

$x = 0.3$



- ▶ Point A and A2 have  $Br(\mu \rightarrow e\gamma)$  differ by two orders of magnitude.
- ▶ Only point A is in the cancellation region and then gives  $Br(\mu \rightarrow e\gamma)$  below the current experimental upper bound.
- ▶ A precise determination of  $\mu$  parameter is important for determination of flavor mixing parameter.

# OSSF Dilepton Invariant Mass Distribution



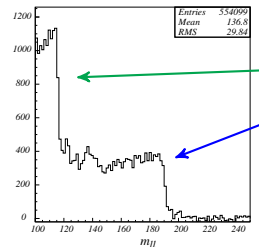
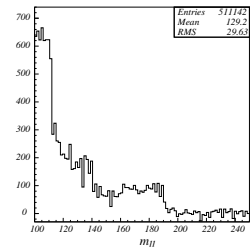
A2:  $\tilde{\chi}_4^0$  and  $\tilde{\chi}_2^+$  have more Wino component

⇒ Enhancement in edges from

$\tilde{\chi}_2^+ \rightarrow \tilde{\nu}_L \rightarrow \tilde{\chi}_1^0$  (factor 2)  
and

$\tilde{\chi}_4^0 \rightarrow \tilde{e}_L \rightarrow \tilde{\chi}_1^0$  (factor 4)

relative to edge of  
 $\tilde{\chi}_2^0 \rightarrow \tilde{e}_R \rightarrow \tilde{\chi}_1^0$



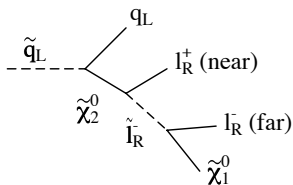
# Charge Asymmetry

A. J. Barr, Phys. Lett. B596, 205 (2004)

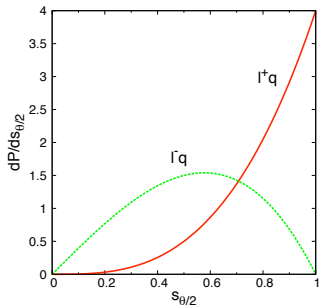
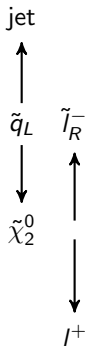
T. Goto, K. Kawagoe, M. M. Nojiri, Phys. Rev. D70, 075016 (2004)

J. M. Smillie, B. R. Webber, JHEP 0510:069,2005.

## Example

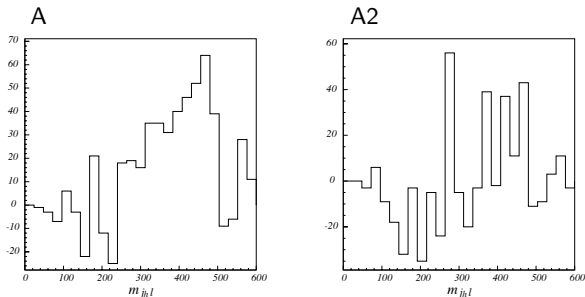


$\theta$  = angle between quark and lepton in the  $\tilde{\chi}_2^0$  rest frame



$\Rightarrow$  positive charge asymmetry

## Spin correlation in Herwig, G. Corcella *et al*, arXiv:hep-ph/0011363v3.



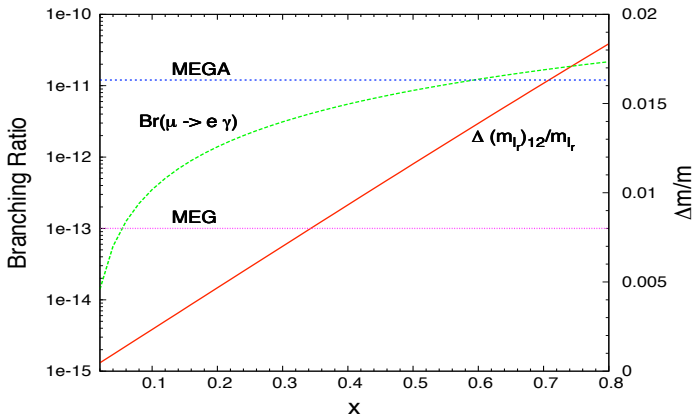
The difference between  $m_{j_h l+}$  and  $m_{j_h l-}$  distributions as a function of  $m_{j_h l}$   
 $j_h$  is defined by  $m_{j_h ll} \equiv \max(m_{j_1 ll}, m_{j_2 ll})$

Assuming that L-R slepton mixing is negligible, the flatness of charge asymmetry distribution suggests the contribution from  $\tilde{q}_R \rightarrow \tilde{\chi}_2^0$  decay.

$\Rightarrow \tilde{\chi}_2^0$  for point A2 must have smaller Wino component.

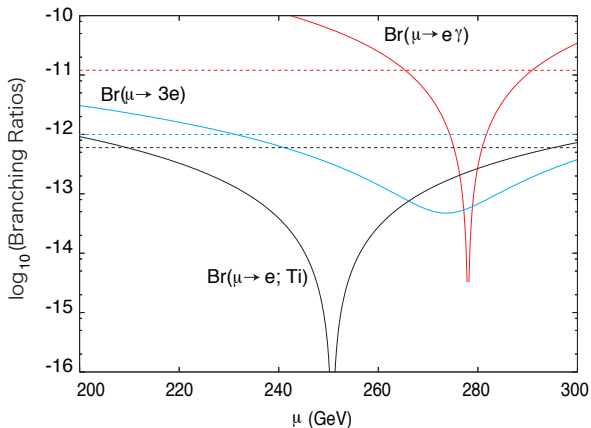
$\Rightarrow M_1 < \mu < M_2$

$\mu \rightarrow e \gamma$



Recall  $m_{\tilde{e}_L} - m_{\tilde{\chi}_1^0} = 124.92^{+0.65}_{-0.65}$  GeV,  $m_{\tilde{e}_R} - m_{\tilde{\chi}_1^0} = 15.68^{+0.45}_{-0.49}$  GeV.

- ▶ The mass difference of order one percent, corresponding to 1 ~ 2 GeV, is allowed by MEGA bound ( $Br(\mu \rightarrow e \gamma) < 1.2 \times 10^{-11}$ ).



- ▶ The  $\mu \rightarrow e$  conversion rate shows strong sensitivity to the SUSY parameters at different  $\mu$  values from  $Br(\mu \rightarrow e\gamma)$  and  $Br(\mu \rightarrow 3e)$ .
- ▶  $\mu = 271.33^{+6.89}_{-6.81}$  GeV



Finally, precise SUSY parameter determination is also important for the determination of DM density and DM scattering cross section.

	$\Omega_{\text{DM}} h^2$	$\sigma_{p\chi}^{SI} (10^{-8} \text{ pb})$
A	0.1179	1.6
A2	0.0817	3.2
A3	0.0096	17.5
observation/exp. upper bound	0.122 (WMAP & SDSS)	4.6 (CDMS)

Uncertainties in  $\sigma_{p\chi}^{SI}$ :

- ▶ nucleon matrix element of strange quark

- ▶  $\sigma_{p\chi}^{SI} |_{A\text{-exchange}} \propto \left( \frac{\tan^2 \beta}{m_A^4} \right)$

## Conclusions

- ▶ We studied the one-parameter-extended NUHM,  $m_{H_U} \neq m_{H_D} = m_0$ , particularly with  $M_1 < M_2 < \mu \sim m_{1/2}$  and dark matter relic density consistent with cosmological and astrophysical observations.
- ▶ We are also interested in the region where cancellation among leading contributions to  $Br(\mu \rightarrow e\gamma)$  occurs in the models with right-handed LFV masses. Therefore, we took the choice  $m_{\tilde{\chi}_1^0} < m_{\tilde{e}_R} < m_{\tilde{\chi}_2^0} < m_{\tilde{e}_L} < m_{\tilde{\chi}_4^0}$  when both left- and right-handed sleptons can be directly produced via neutralino decay.
- ▶ In the region when  $M_1 < M_2 < \mu \sim m_{1/2}$ ,  $\tilde{\chi}_4^0$  and  $\tilde{\chi}_2^+$  are a mixed states with rather large Wino component and their various decay patterns are expectable at the LHC.
- ▶ When the relation  $M_1 < M_2, \mu$  is kept, we showed three solutions with similar mass spectrum but different ordering of  $M_1, M_2$  and  $\mu$ . We showed that by looking into 2 jets + missing  $E_T$  signature, relative height of  $m_{II}$  edges and charge asymmetry, the degeneracy can be lifted.
- ▶ We emphasized that a precise  $\mu$  parameter determination is an important key for resolving cancellation point of LFV processes, determination of the LFV parameter and determination of DM density and DM scattering cross section.



## Mass Spectrum (point A)

$m_{\tilde{g}}$	719.67	$m_{\tilde{\nu}}$	224.37	$m_{\tilde{\chi}_2^+}$	321.62
$m_{\tilde{u}_L}$	665.19	$m_{\tilde{e}_L}$	239.62	$m_{\tilde{\chi}_1^+}$	196.30
$m_{\tilde{d}_L}$	670.29	$m_{\tilde{e}_R}$	130.38	$m_{\tilde{\chi}_4^0}$	323.23
$m_{\tilde{u}_R}$	648.85	$m_{\tilde{\tau}_2}$	238.89	$m_{\tilde{\chi}_3^0}$	278.87
$m_{\tilde{d}_R}$	642.47	$m_{\tilde{\tau}_1}$	128.07	$m_{\tilde{\chi}_2^0}$	197.82
				$m_{\tilde{\chi}_1^0}$	114.70

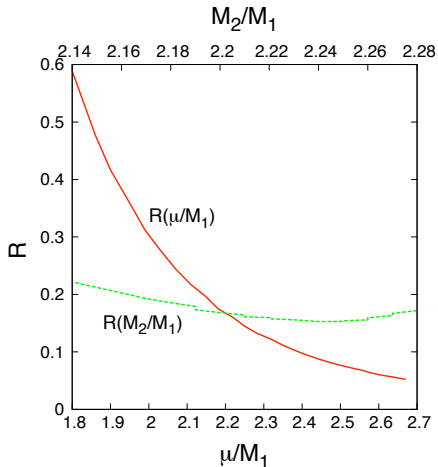
## Selection criteria:

- ▶ an OSSF dilepton pair where both leptons have  $p_T^l > 10$  GeV and  $|\eta| < 2.5$ .
- ▶ more than 4 jets with  $p_{T,1}^j > 100$  GeV,  $p_{T,2,3,4}^j > 50$  GeV.
- ▶  $M_{\text{eff}} \equiv p_{T,1} + p_{T,2} + p_{T,3} + p_{T,4} + \cancel{E}_T > 400$  GeV.
- ▶  $\cancel{E}_T > \max(100, 0.2M_{\text{eff}})$ .

## Estimated error of sparticle masses and SUSY parameters

Sparticle Mass	Central value	Estimated error ( $1-\sigma$ )
$m_{\tilde{\chi}_1^0}$	114.70	+6.7 -6.3
$m_{\tilde{e}_R} - m_{\tilde{\chi}_1^0}$	15.68	+0.45 -0.49
$m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}$	83.12	+0.75 -0.62
$m_{\tilde{e}_L} - m_{\tilde{\chi}_1^0}$	124.92	+0.65 -0.65
$m_{\tilde{\chi}_4^0} - m_{\tilde{\chi}_1^0}$	208.53	+0.77 -0.64
$m_{\tilde{q}_L} - m_{\tilde{\chi}_1^0}$	551.19	+4.64 -4.47
$m_{\tilde{e}_R} - m_{\tilde{\mu}_R}$	1.00	+0.04 -0.04
$m_{\tilde{e}_L} - m_{\tilde{\mu}_L}$	2.00	+0.48 -0.49

Parameter	Central value	Estimated error ( $1-\sigma$ )
$\mu$	271.33	+6.89 -6.81
$M_1$	122.49	+7.16 -7.17
$M_2$	230.89	+6.57 -6.54
$\mu/M_1$	2.215	+0.084 -0.078
$M_2/M_1$	1.885	+0.063 -0.057



$$R \equiv \frac{Br(\tilde{u}_R \rightarrow \tilde{\chi}_2^0)}{Br(\tilde{u}_L \rightarrow \tilde{\chi}_2^0)}$$

$\Rightarrow$  The ratio  $R$  depends on  $\mu/M_1$  stronger than on  $M_2/M_1$ .

$\Rightarrow$  As  $\mu/M_1$  is smaller, mixing between neutralino states is larger and the charge asymmetry receives more  $\tilde{q}_R$  contribution so that the distribution becomes flat.