



# Cascade $c\bar{c}$ and $b\bar{b}$ Production

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- Full simulation implementation strategy
- $c\bar{c}$
- $b\bar{b}$
- HNL acceptances
- Background
- What about  $J/\psi$ ?
- Conclusions



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## Heavy Flavour Cascade Production in a Beam Dump

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CERN

### Abstract

SHiP will use a 400 GeV/c proton beam impinging on a several interaction length long Molybdenum target. Heavy flavour hadrons produced in the dump can decay semi-leptonically, which can produce both the Heavy Neutral Leptons as signal, but also potential background from muons and neutrinos. The absolute rate of heavy flavour production is taken from measurements. Pythia is used to predict the phase space distribution of the charm and beauty hadrons which are produced both in the primary interaction of the 400 GeV/c proton and in interactions of the secondaries produced in the cascade. The full cascade production of both HNL and background is compared to that reported in the SHiP Technical Proposal, where only the primary  $pN$  interactions were taken into account.

H.Dijkstra





# Heavy Flavour production on Mo target

- $\chi_{c\bar{c}(b\bar{b})} = \frac{\sigma(pp \rightarrow c\bar{c}(b\bar{b})X)}{\sigma_{\text{Total} \rightarrow Y}}$
- In TP used the following numbers:
  - pN(p):  $\chi_{c\bar{c}} = 18 \mu\text{b}/40 \text{ mb} = 0.45 \times 10^{-3}$
  - pN(p):  $\chi_{b\bar{b}} = 0.43 \times 10^{-7}$
  - pN(Mo):  $\chi_{c\bar{c}} = 18 \mu\text{b}/10.7 \text{ mb} = 1.7 \times 10^{-3}$
  - pN(Mo):  $\chi_{b\bar{b}} = 1.6 \times 10^{-7}$
  - Used  $\sigma_{\text{Total}}$ :  $\frac{\sigma_{\text{elastic}}}{\sigma_{\text{Total}}} = 0.17$ , hence “very conservative”
- Cascade production:
  - A secondary particle will interact, and can produce another  $c\bar{c}(b\bar{b})$ -pair.  
Hence: need to get p,n, $\pi$ ,K+N  $\rightarrow c\bar{c}(b\bar{b})$  cross-sections as a function of “beam” momentum.
  - Note:  $\pi$ N:  $\sigma_{\text{Total}} \approx 25 \text{ mb}$ ,  $1.6 \times$  smaller than for pN interactions.  
Hence: need to get  $\sigma_{\text{Total}}$  also as function of “beam” momentum.



# Implementation in Simulation

Used Pythia 6 as implemented in FairShip (need FORTRAN version, since Pythia 8 init takes too long, and we need an init for every secondary particle)

Following steps in FairShip/macro/makeCascade.py:

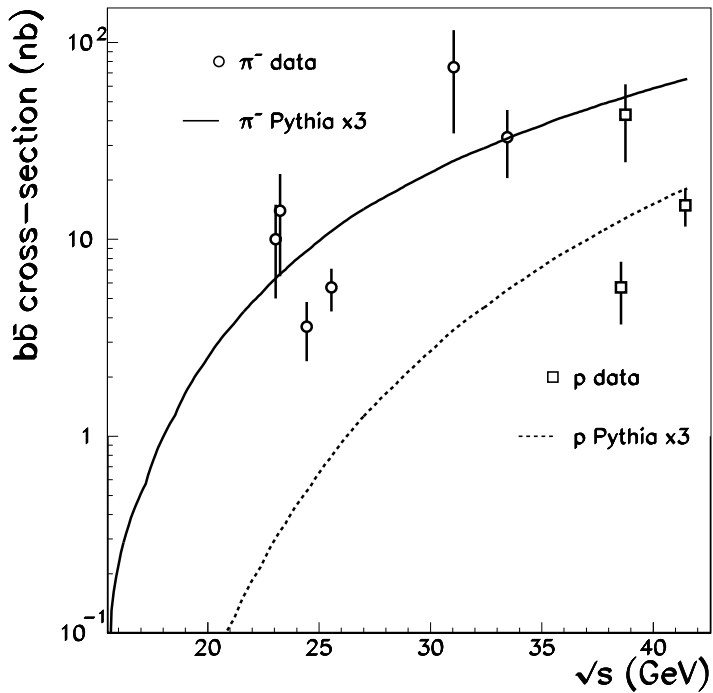
- 1 use Pythia to get the cross-sections vs momentum for p,n, $\pi$ ,K
- 2 calculate  $\chi_{\text{norm}}$  values for all “beams” and all momenta:  $\chi_{\text{norm}} = \frac{\chi}{\chi_{400\text{GeV}}^{\text{max}}}$
- 3 Put 400 GeV proton on the “beam-stack”.
- 4 While particles on “beam-stack”:
  - if  $\text{random}(0-1) < \chi_{\text{norm}}$ : produce a signal  $c\bar{c}(b\bar{b}) \rightarrow \text{ntuple}$
  - Produce total cross-section event, and add new stable particles with  $p > \text{threshold}$  on the “beam-stack”
  - Remove used particle from “beam-stack”
- 5 Goto 3

- Ntuple will contain correct mix of D(B)-mesons.
- Use Ntuple as input to generate semileptonic signal decays to f.i. HNL using Pythia.



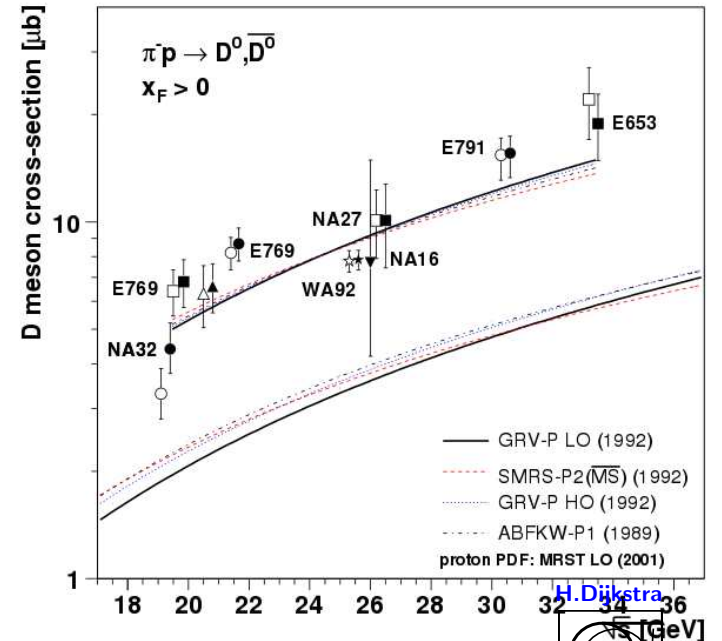
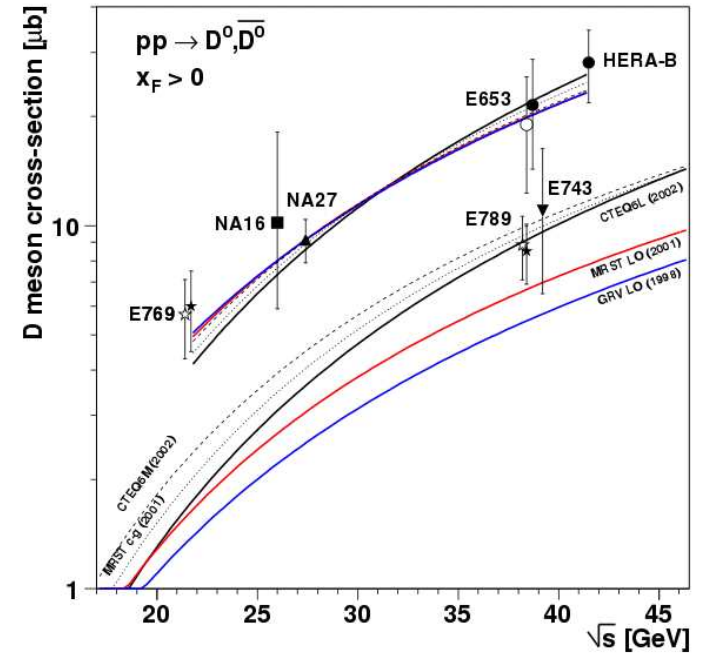
# Validate Pythia for $\chi_{\text{norm}}$ Determination

- Reproduce from <http://arxiv.org/pdf/hep-ph/0609101v1.pdf>
- $c\bar{c}$  dominated by  $gg$ -fusion  $\rightarrow \sigma(pp) \approx \sigma(\pi p)$
- $b\bar{b}$  dominated by  $q\bar{q}$ -annihilation  $\rightarrow \sigma(pp) \ll \sigma(\pi p)$



- $b\bar{b}$  curves from makeCascade.py
- K-factors arbitrary, just the  $\sqrt{s}$  dependence counts.

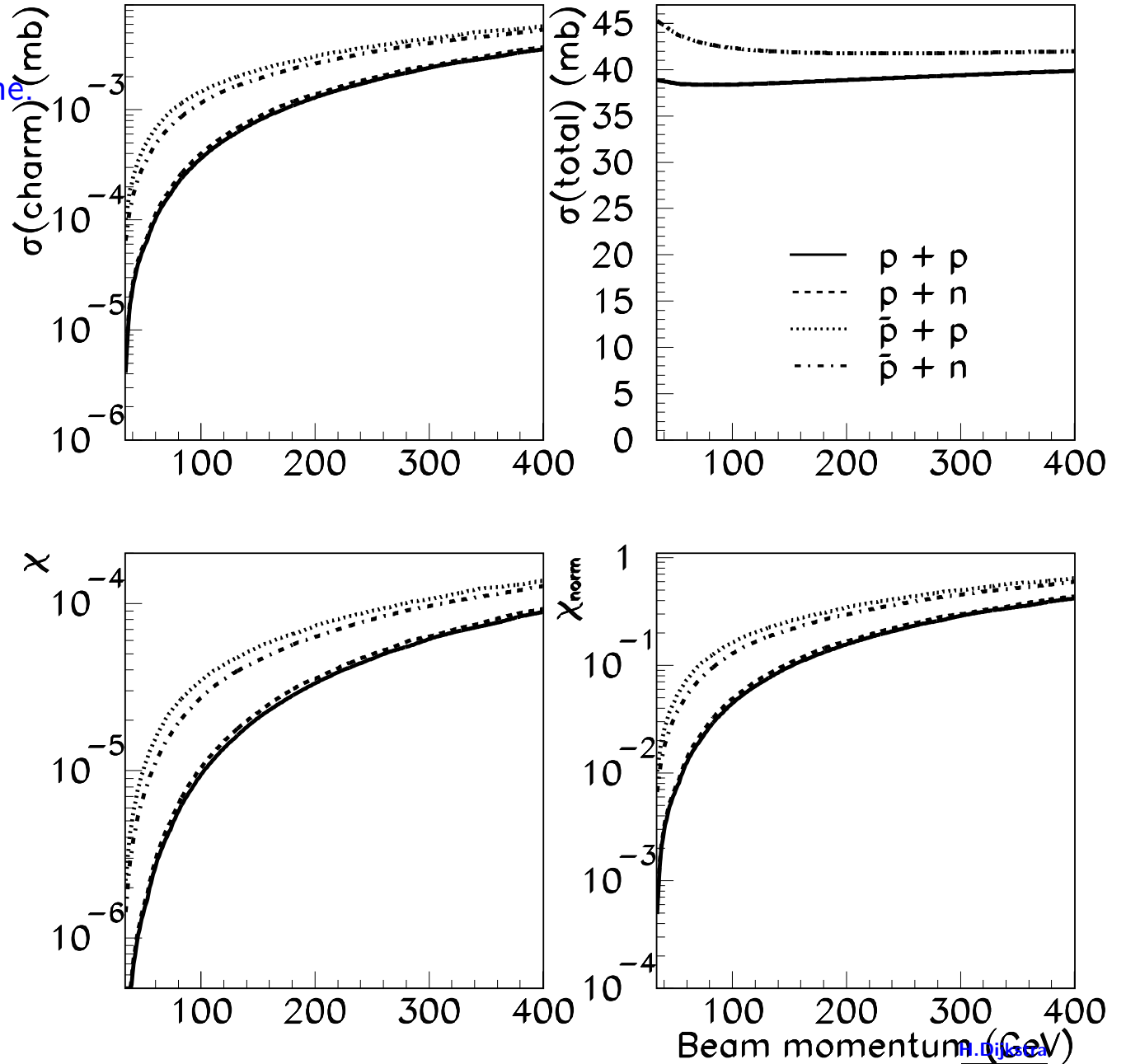
Pythia seems reasonable!





# Steps 1&2) Get $\chi_{\text{norm}}$

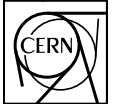
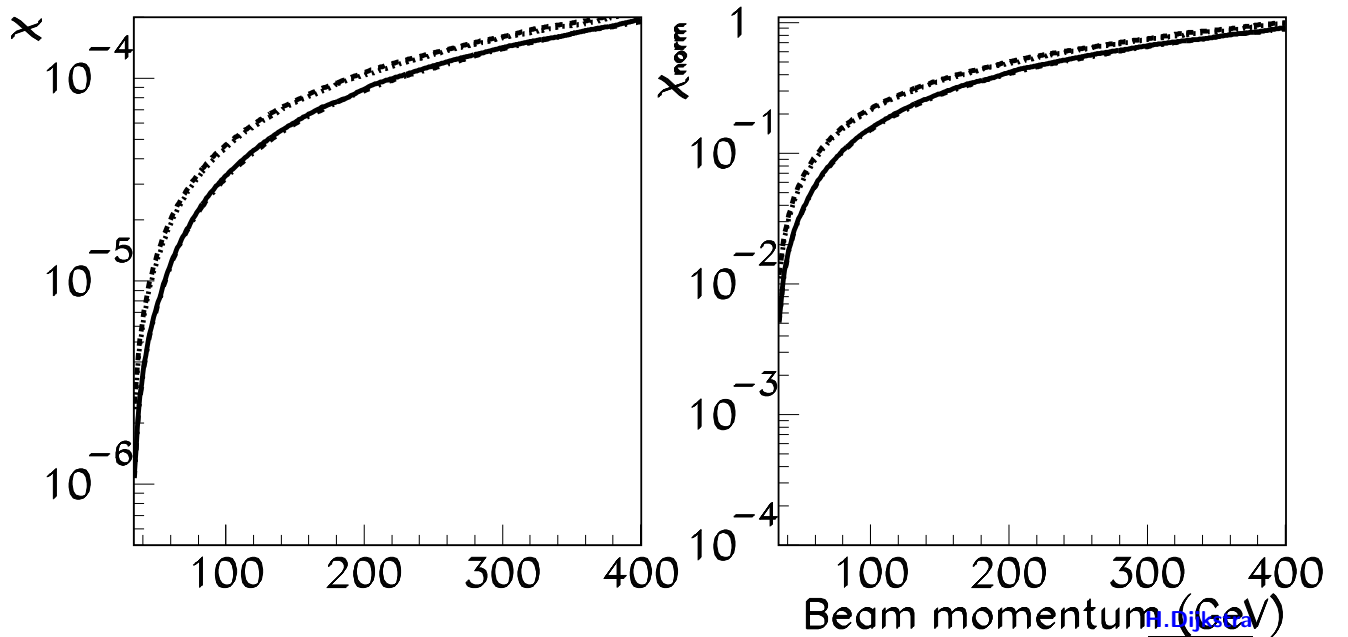
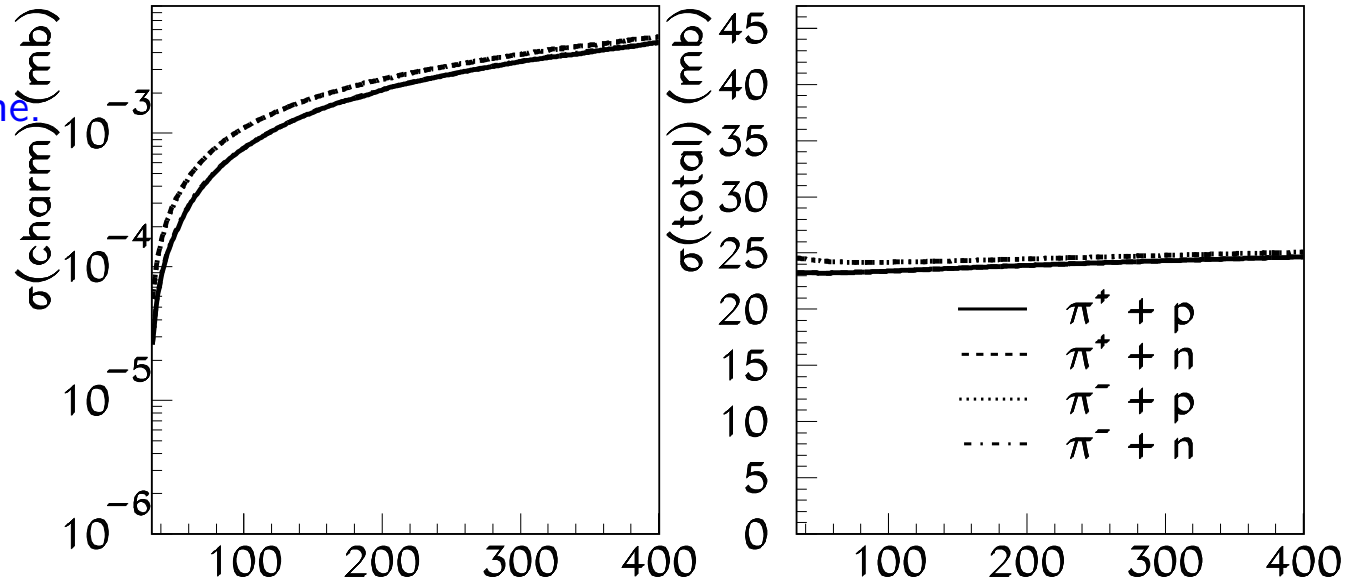
- Use Pythia to get  $\sigma$  at 20 points, interpolated with straight line.
- Target: mix p and n, hence get  $\sigma$  for both independently.





# Steps 1&2) Get $\chi_{\text{norm}}$

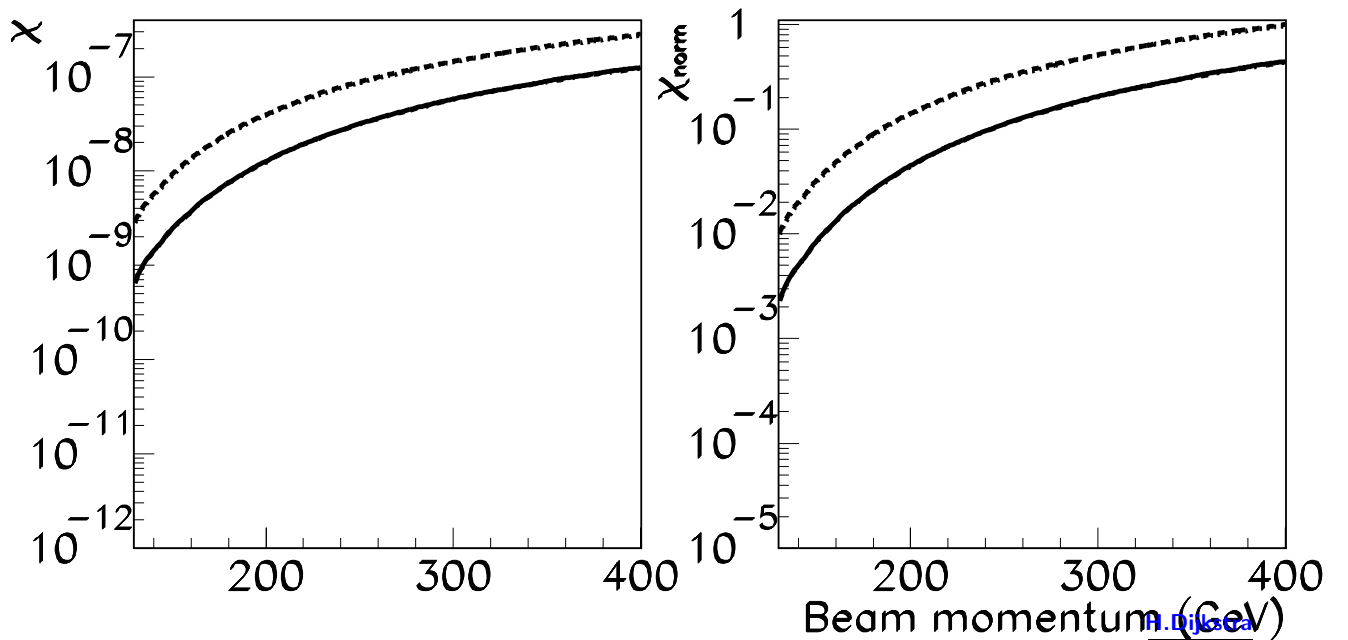
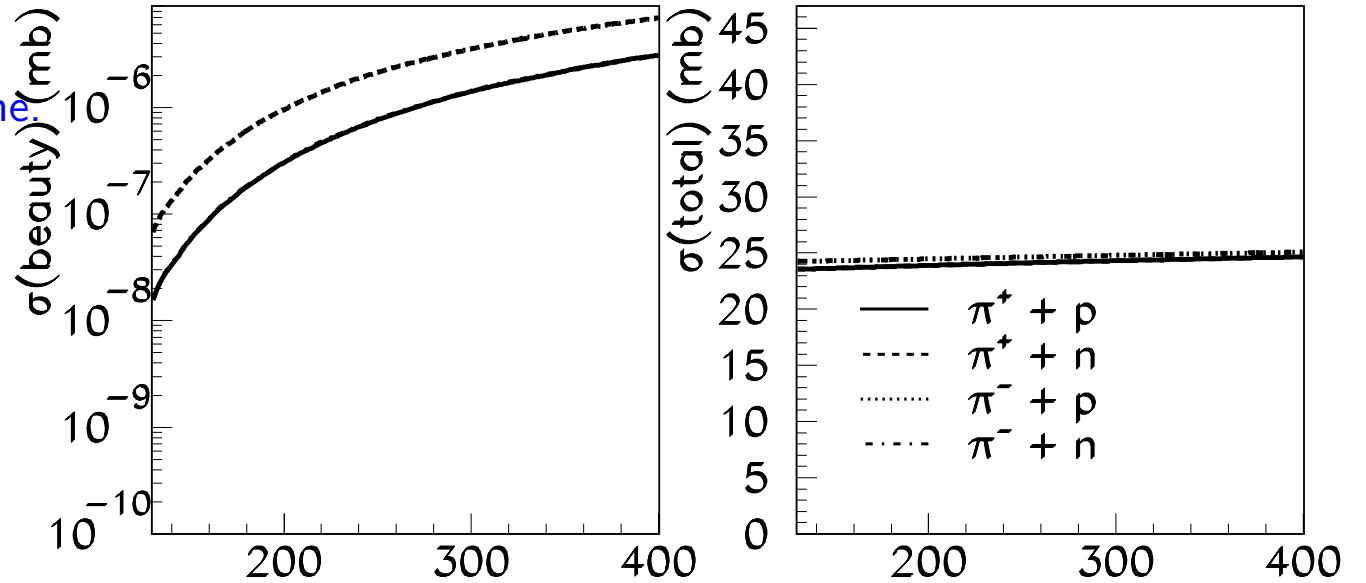
- Use Pythia to get  $\sigma$  at 20 points, interpolated with straight line.
- Target: mix p and n, hence get  $\sigma$  for both independently.
- $\chi_{400\text{GeV}}^{\text{max}}$ :  
 $\pi^+(400\text{GeV}) + n \rightarrow c\bar{c} + X$





# Steps 1&2) Get $\chi_{\text{norm}}$

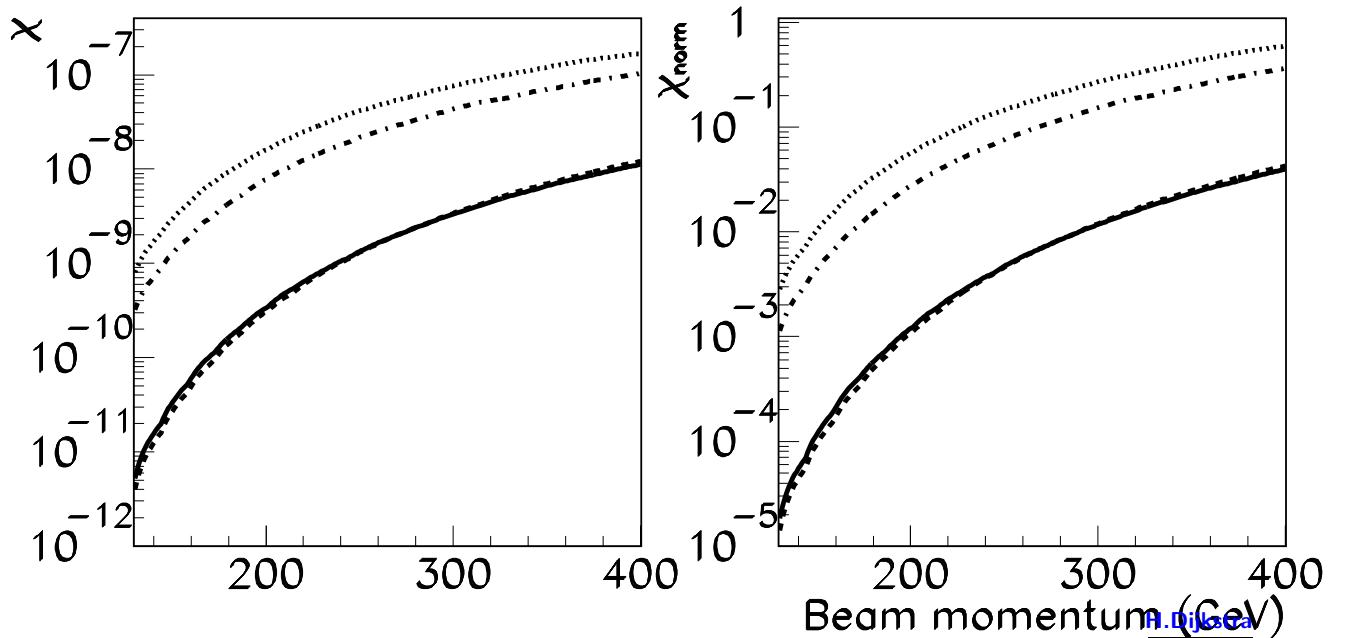
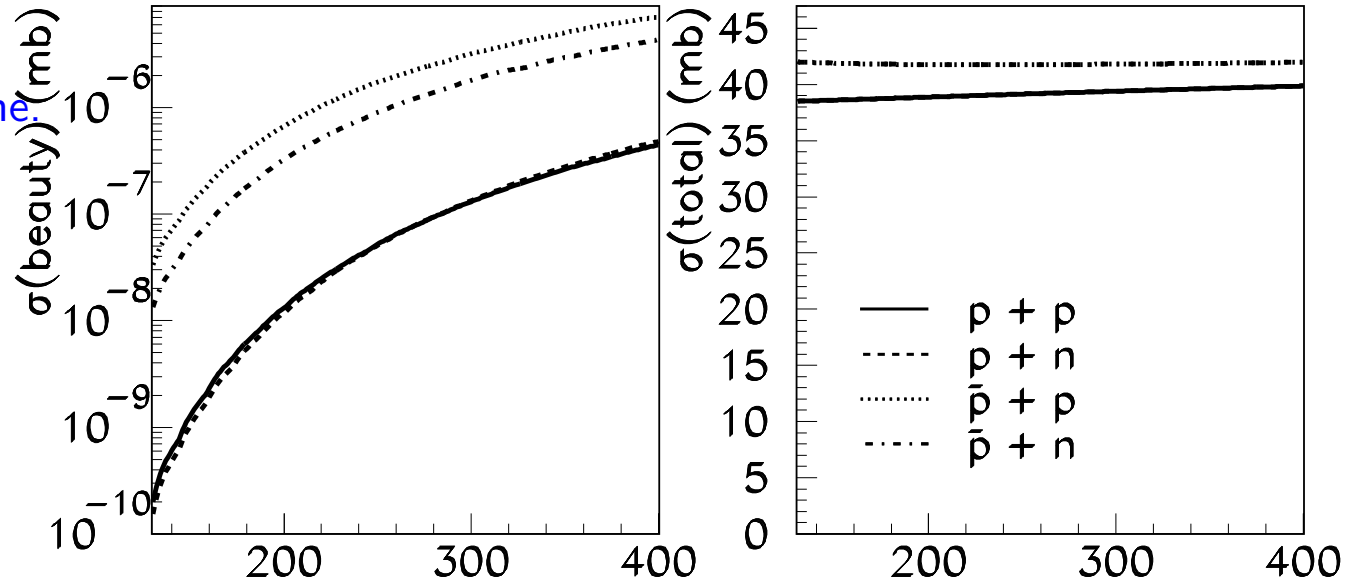
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# Steps 1&2) Get $\chi_{\text{norm}}$

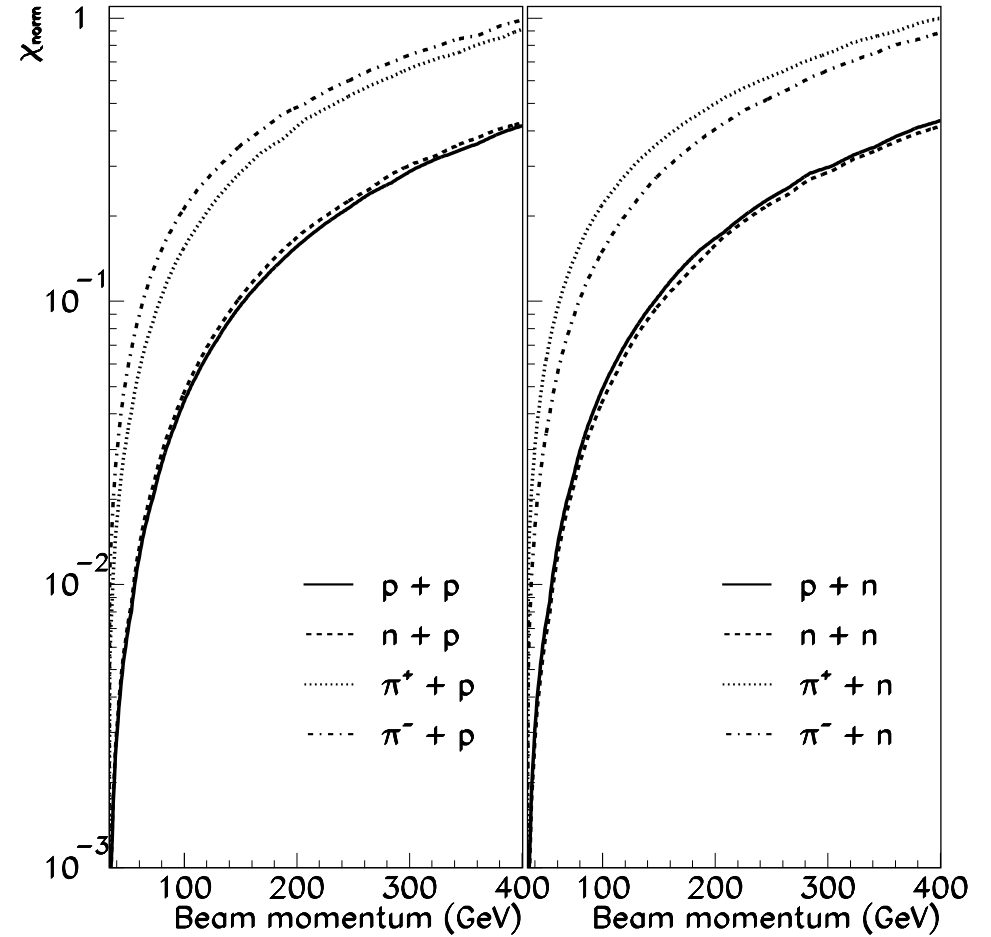
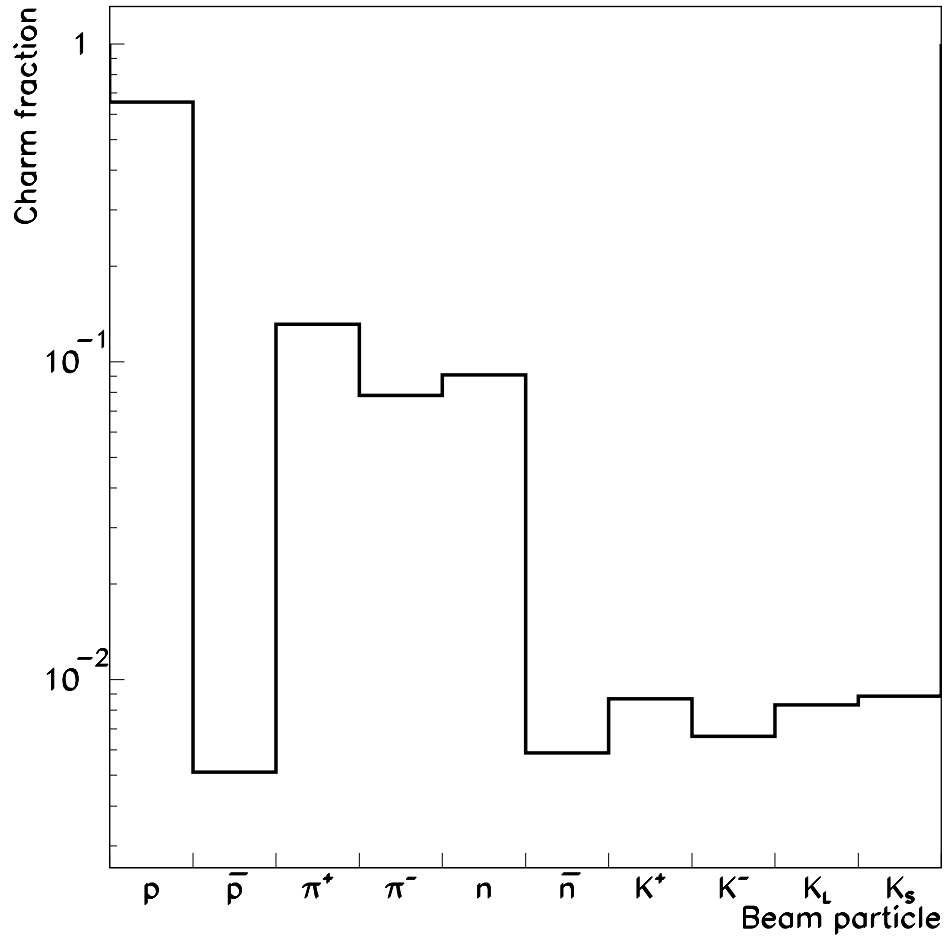
- Use Pythia to get  $\sigma$  at 20 points, interpolated with straight line.
- Target: mix p and n, hence get  $\sigma$  for both independently.
- $\chi_{400\text{GeV}}^{\text{max}}$ :  
 $\pi^+(400\text{GeV}) + n \rightarrow b\bar{b} + X$
- Hence:  $\chi_{\text{norm}}$ :  
 $p(400\text{GeV}) + p \rightarrow b\bar{b} + X = 0.04$





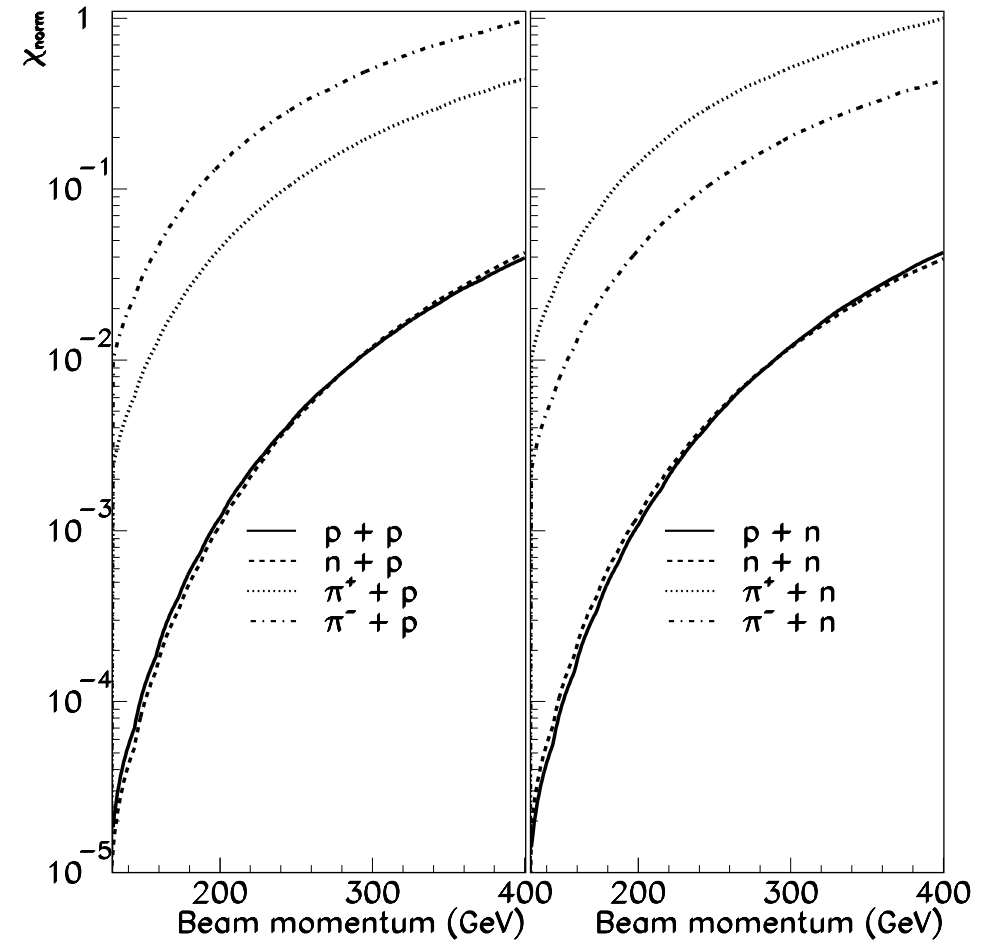
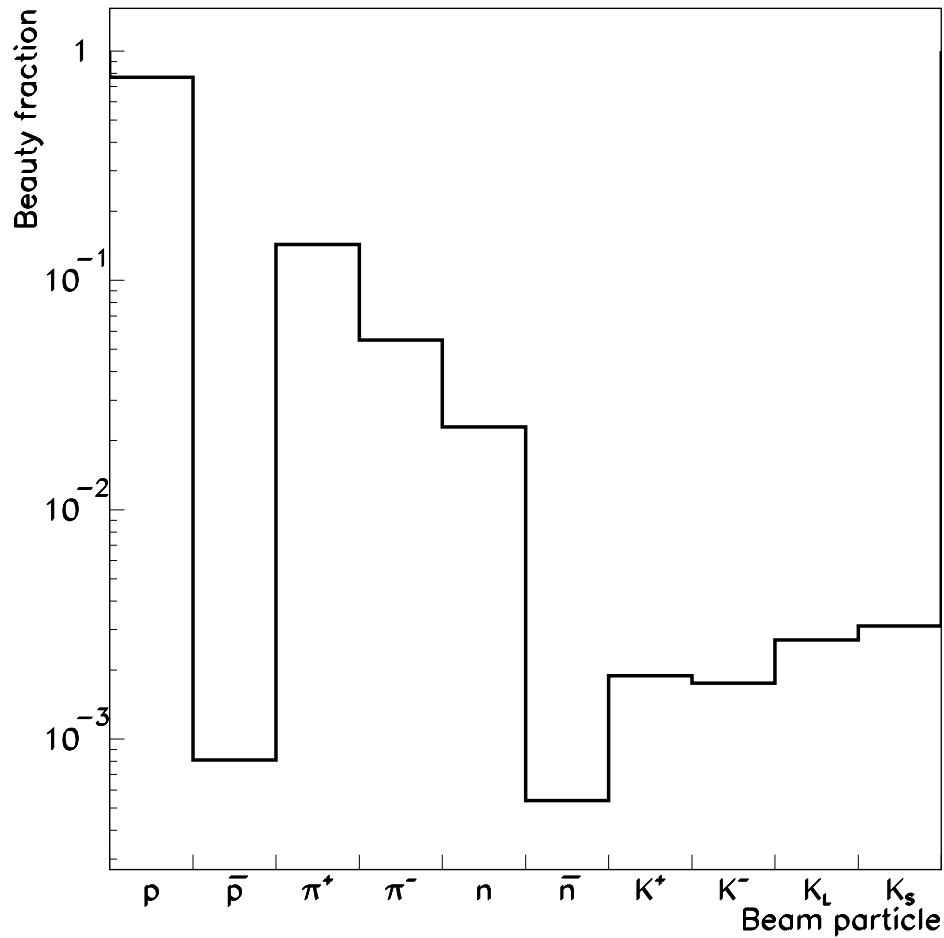
# Step 4) Produce $c\bar{c}$

- $p + \pi^\pm + n = 65 + 21 + 9 = 95$  % main contributors to signal production.
- Molybdenum: 43% of nucleons is proton, generate with correct mix.



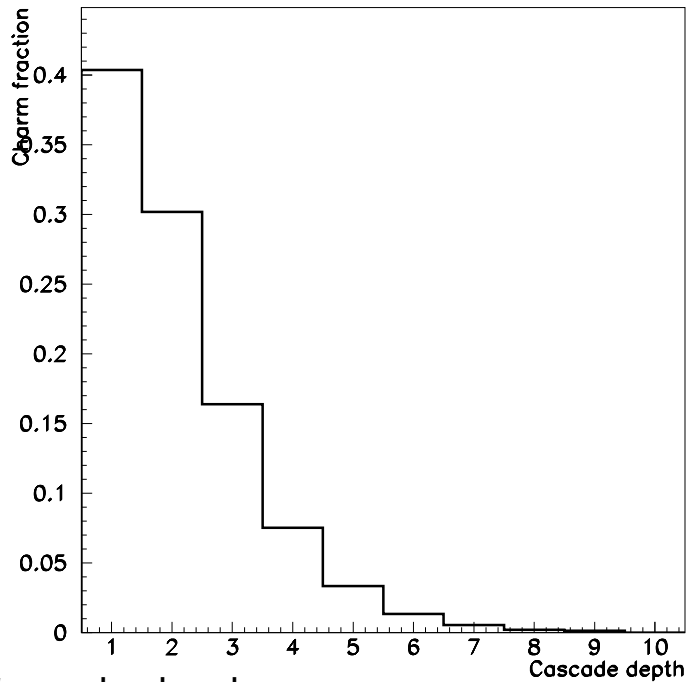
# Step 4) Produce $b\bar{b}$

- $p + \pi^\pm + n = 77 + 20 + 2 = 99\%$  main contributors to signal production.
- Molybdenum: 43% of nucleons is proton, generate with correct mix.



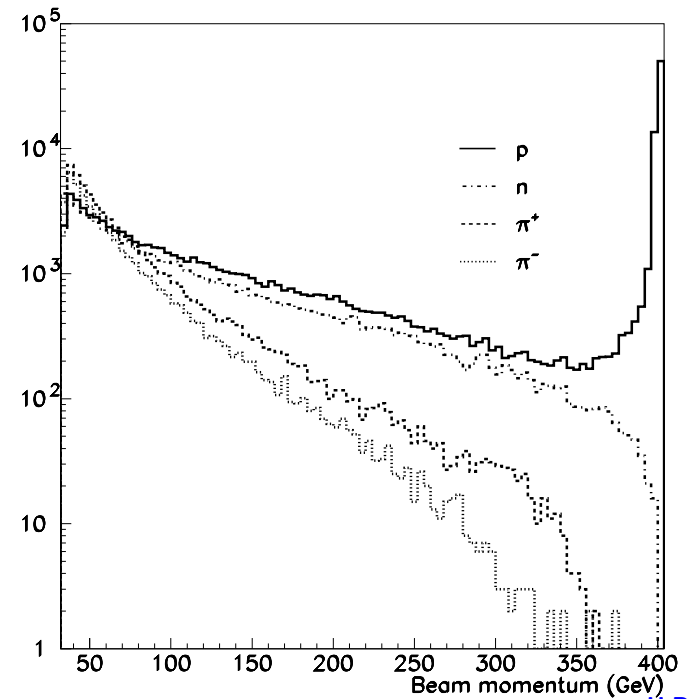
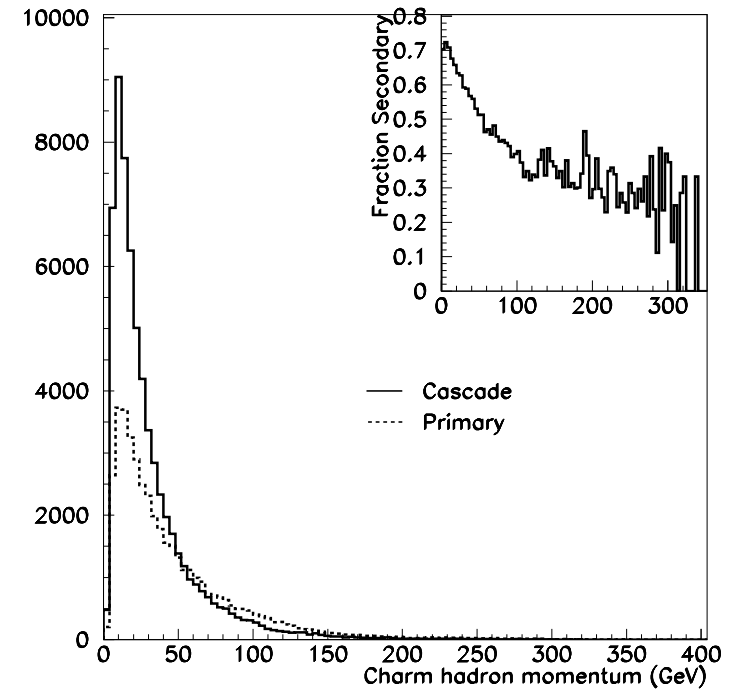
# Steps 4) Charm plots

- TP addendum: only first cascade  $\frac{\text{Total}}{\text{Primary}} = 1.61$
- Now: all cascade till kinematic limit.
- Full cascade  $\frac{\text{Total}}{\text{Primary}} = 2.31$



Cascade depth:

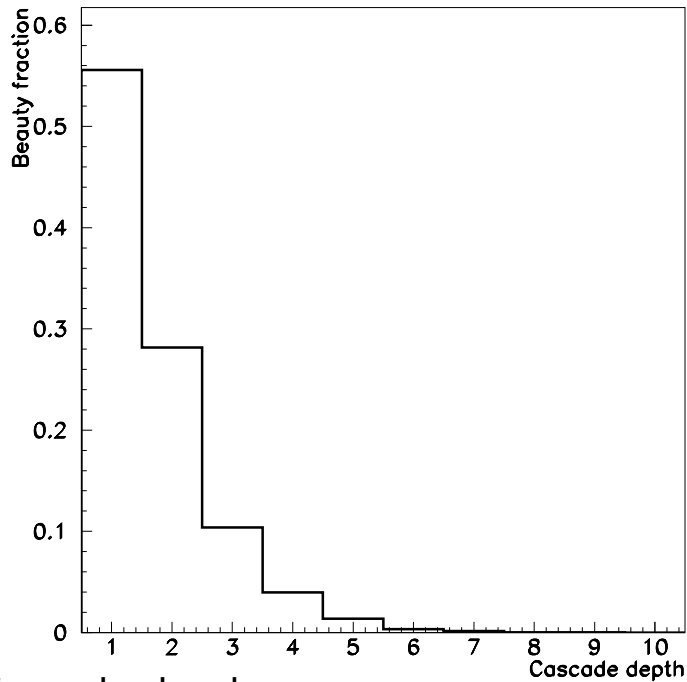
1. 400 GeV pN
2. Products of 1
3. Products of 2 etc..



H.Dijkstra

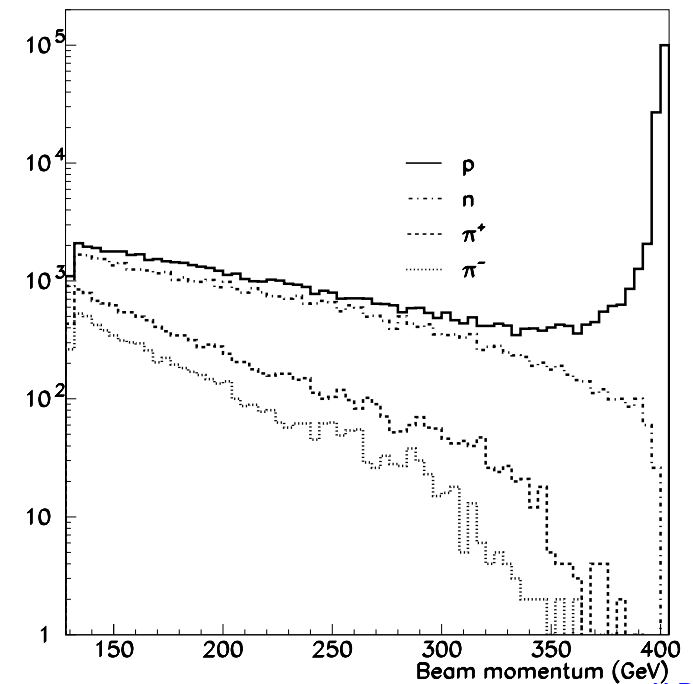
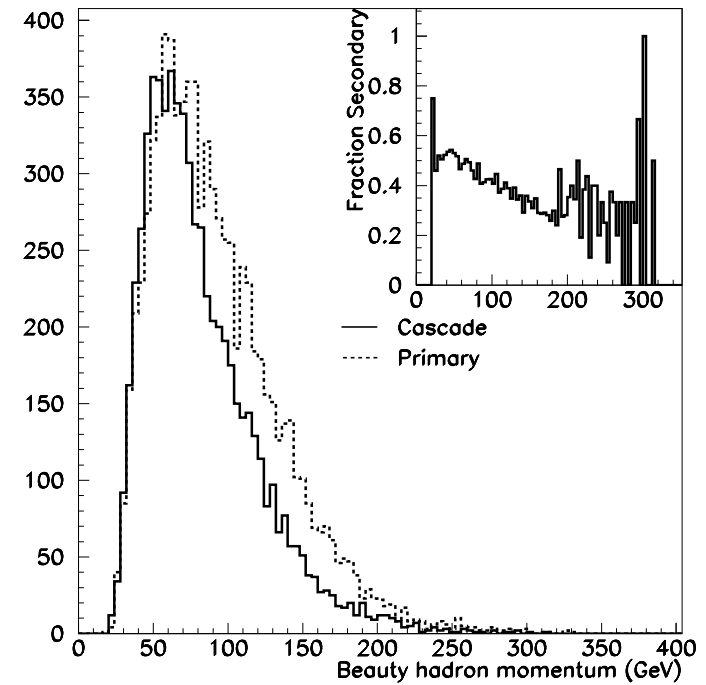
# Steps 4) Beauty plots

- TP addendum: only first cascade  $\frac{\text{Total}}{\text{Primary}} = 1.54$
- Now: all cascade till kinematic limit.
- Full cascade  $\frac{\text{Total}}{\text{Primary}} = 1.74$



Cascade depth:

1. 400 GeV pN
2. Products of 1
3. Products of 2 etc..



H.Dijkstra

# Cascade and HNL Acceptance

Or: what is the correct Pythia tune?

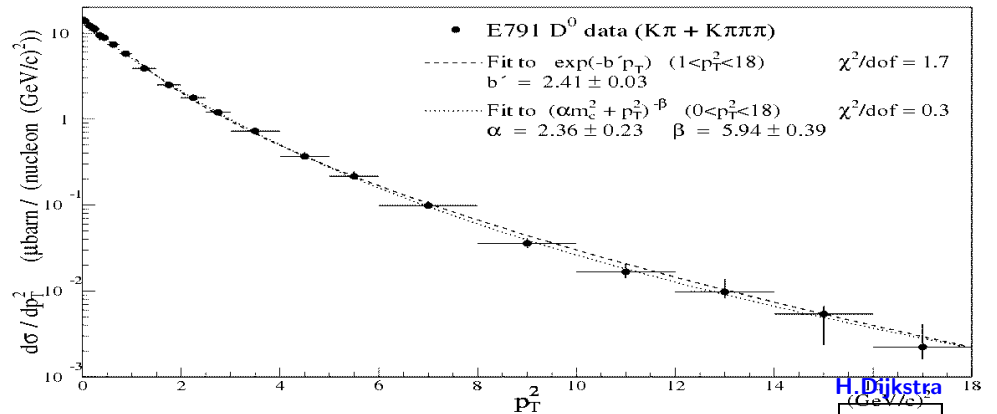
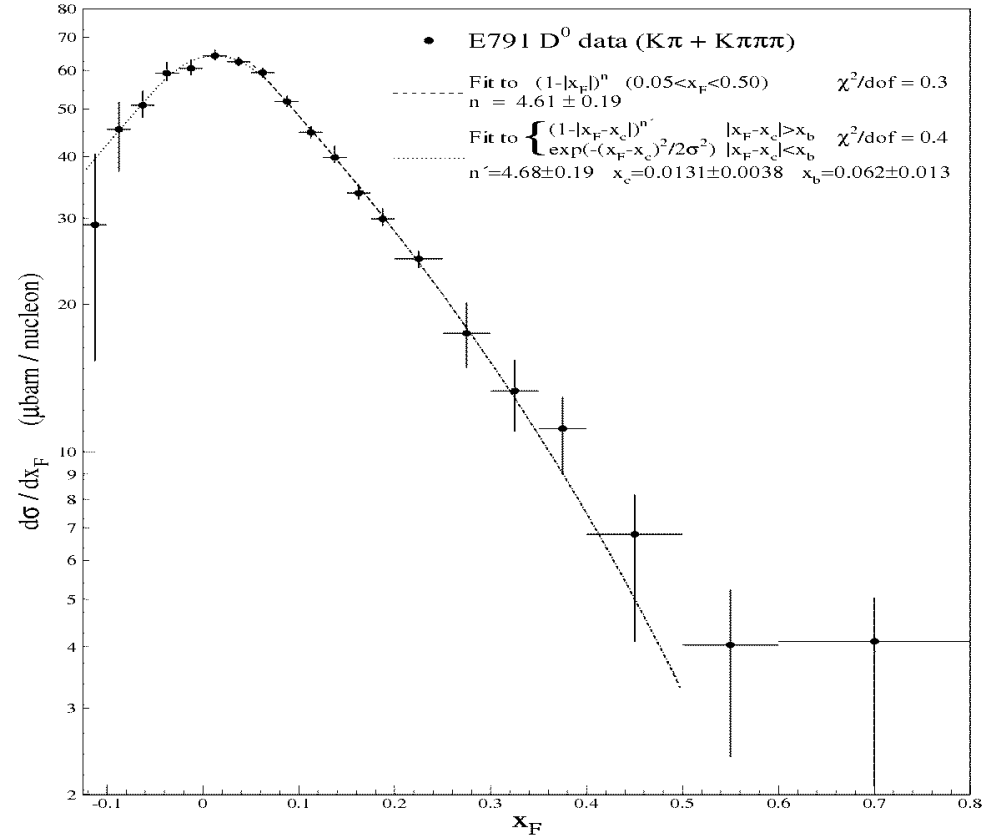
## Chronology of Cascade sim:

- First written in FORTRAN, and used default Pythia 6.205 (cernlib linux version). This produced  $\langle p_T^{D^0} \rangle = 0.84$  GeV
- Charm in the TP was produced with Pythia 8.1, This produced  $\langle p_T^{D^0} \rangle = 1.29$  GeV
- The FORTRAN Pythia in FairShip has version 6.4. This produced  $\langle p_T^{D^0} \rangle = 1.21$  GeV

Resulted in a very different (larger) HNL acceptance from Pythia 6.205 charm, and completely confused us.

## Which Pythia tuning is correct? Literature:

- E791: 90 k  $D^0 + \bar{D}^0$  in 500 GeV  $\pi^- + C$ .
- <http://arxiv.org/pdf/hep-ex/9906034.pdf>
- Published nice differential  $p_T^2$ ,  $X_F$  distributions.
- $\langle p_T^{D^0} \rangle = 1.0$  GeV



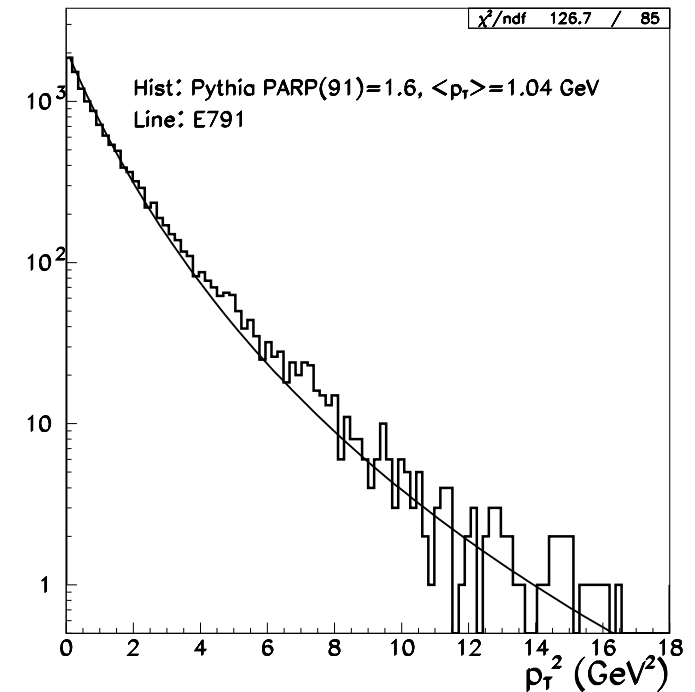
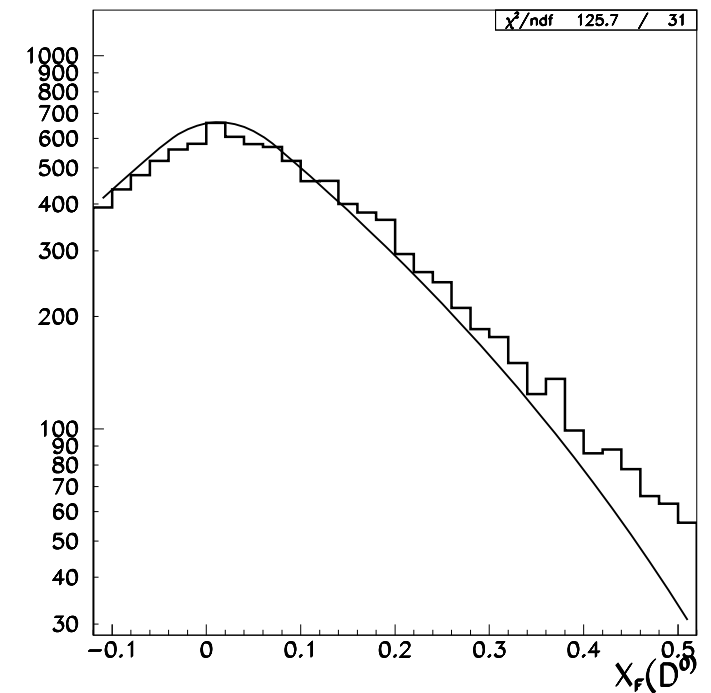


# First Pythia Tune Attempt

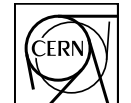
- Pythia 6: PARP(91) varies  $p_T$ .
- PARP(91)=1.6:  $p_T$  is OK, but  $X_F$  is too large.
- Feeling for HNL acceptance systematic:
  - Pythia: generate  $D^0$  with 500 GeV  $\pi^- + p$
  - E791: generate  $D^0$  according to  $p_T^2$ ,  $X_F$  distributions.
  - Then for both:  $D^0 \rightarrow \text{HNL}(1 \text{ GeV}) + X$ ,  $\text{HNL} \rightarrow \mu\pi$
  - SHiP-HNL acceptance: E791/Pythia=78 %.
- Hence: this Pythia tune is too optimistic?

Anyway: use this Pythia tune to get a feeling:  
(Mario Campanelli offered to investigate better tune)

- 1 GeV HNL from charm:
  - Acceptance  $\frac{\text{Pythia6(primary)}}{\text{Pythia8(primary)}} = 1.4$
  - Acceptance  $\frac{\text{Pythia6(all)}}{\text{Pythia8(primary)}} = 2.6$
- 1(3) GeV HNL from beauty:
  - Acceptance  $\frac{\text{Pythia6(primary)}}{\text{Pythia8(primary)}} = 1.07(1.03)$
  - Acceptance  $\frac{\text{Pythia6(all)}}{\text{Pythia8(primary)}} = 1.7(1.9)$



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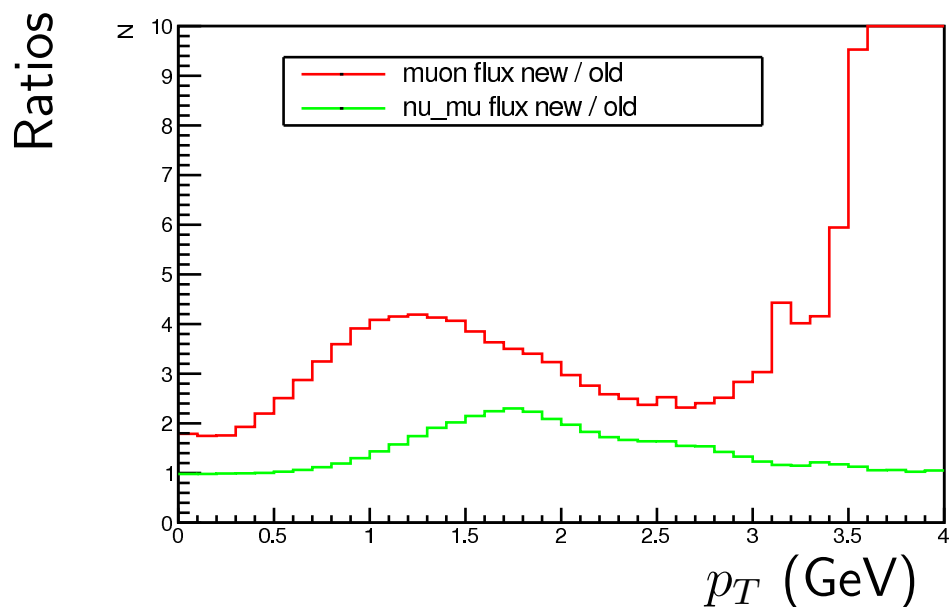
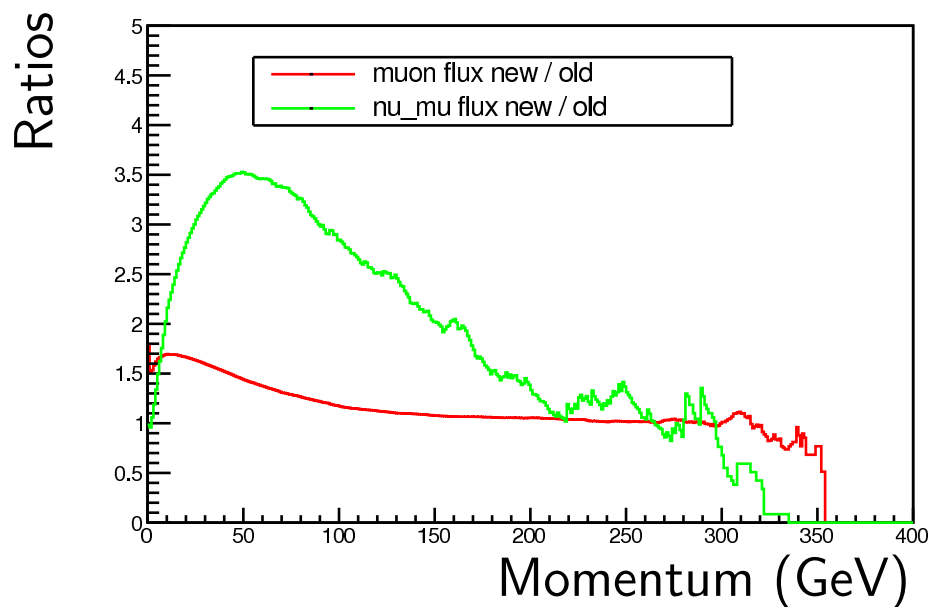


# $\mu, \nu$ Backgrounds

What about background?

- TP:  $pN(\text{Mo}): \chi_{c\bar{c}} = 18 \mu\text{b}/10.7 \text{ mb} = 1.7 \times 10^{-3}$
- But Pythia (pp, some version):  $\chi_{c\bar{c}} = 8.9 \times 10^{-5}$
- Hence: Pythia gives a factor 19 smaller  $\chi$ , in addition we now add Cascade charm.

Removed  $\nu, \mu$  from charm-decay from original files, and added in the new  $\nu, \mu$  from charm with the appropriate weight.

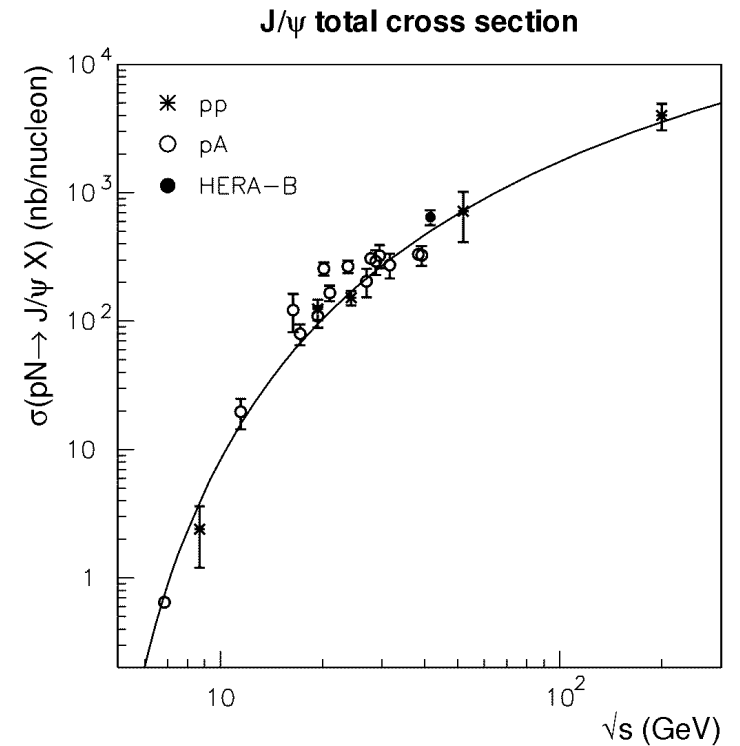


# $J/\psi$ production: Pythia vs data.

- $J/\psi$  rate produced by Pythia-8 is much larger than what is known experimentally.
- For a 400 GeV/c p  $\sigma(pMo \rightarrow J/\psi X) \approx 180$  nb/nucleon, assuming  $\sigma \propto A^{0.96}$ .
- $\chi(J/\psi) \approx 1.7 \times 10^{-5}$ . Pythia 8 produces  $\chi(J/\psi) = 4.2 \pm 0.1 \times 10^{-5}$ , hence more than twice what is expected from prompt  $J/\psi$  production.

This is even larger than what we expect taking the cascade production into account, albeit with a harder spectrum. Hence, it is proposed to not correct this rate with a separate production as used for charm and beauty.

- Hence, we have more than enough muons from  $J/\psi$ -decay in the sample.
- But do they have the correct spectrum???







# Summary

Produced charm(beauty) hadrons with full cascade:

- Charm: full cascade  $\frac{\text{Total}}{\text{Primary}} = 2.31$
- Beauty: full cascade  $\frac{\text{Total}}{\text{Primary}} = 1.74$
- Health Warning: we should first get a reliable Pythia tune, before we conclude on the signal gain the cascade gives us!

Backgrounds:

$\mu \sim 50\%$  more rate, but very  $p_T$  dependent!

$\nu$  Up to  $3.5\times$  more rate at low momenta!

- A lot more plots+how to use new background:

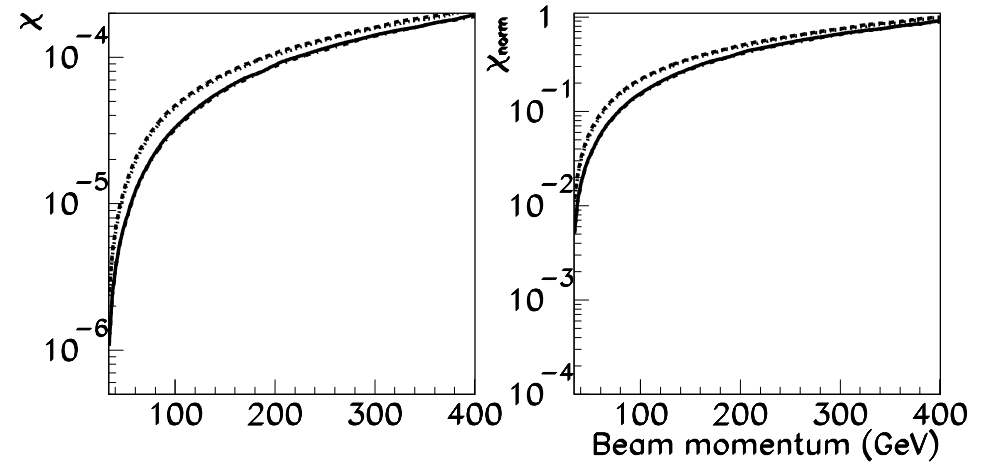
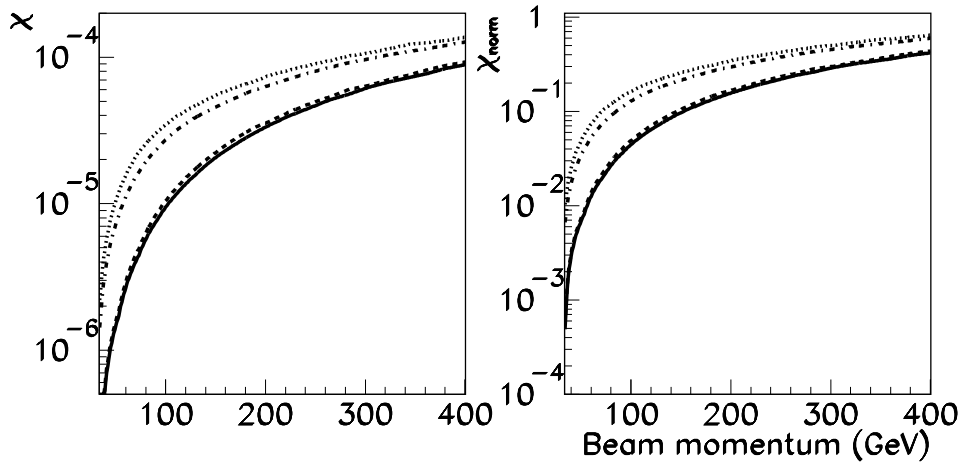
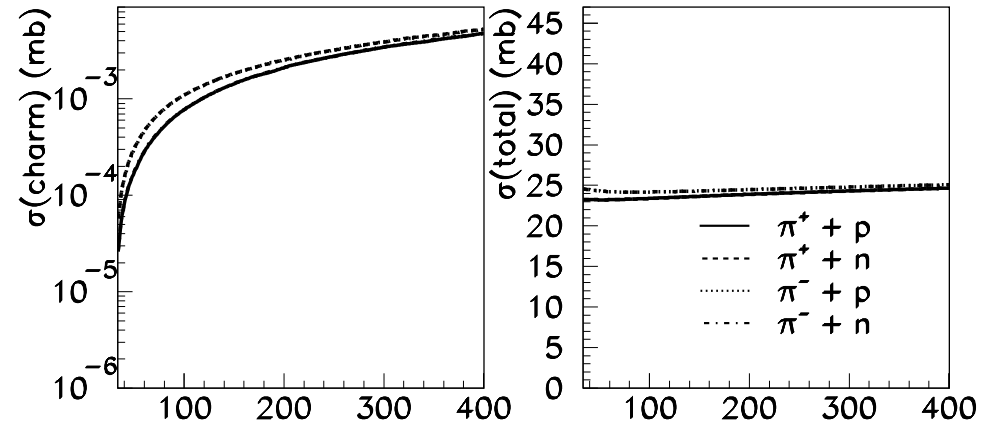
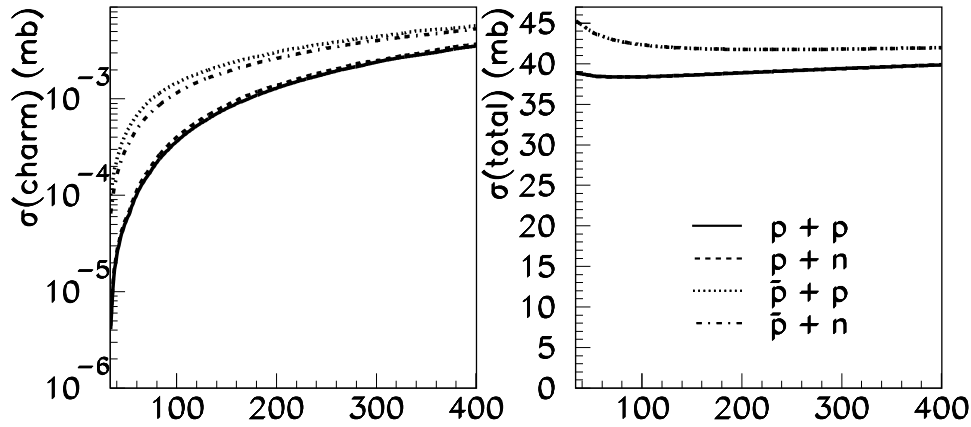
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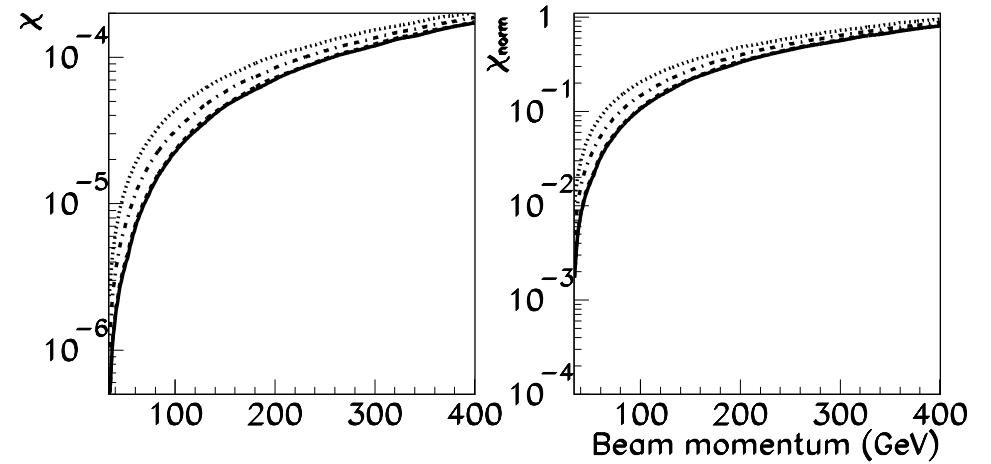
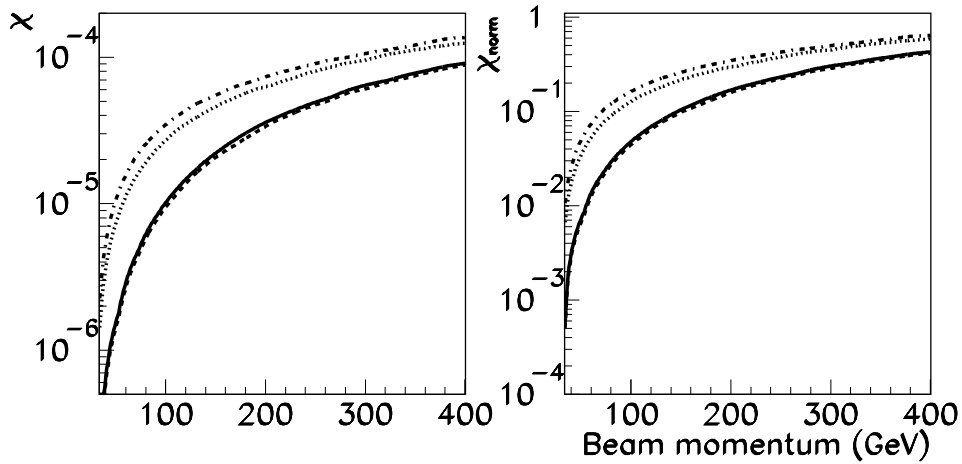
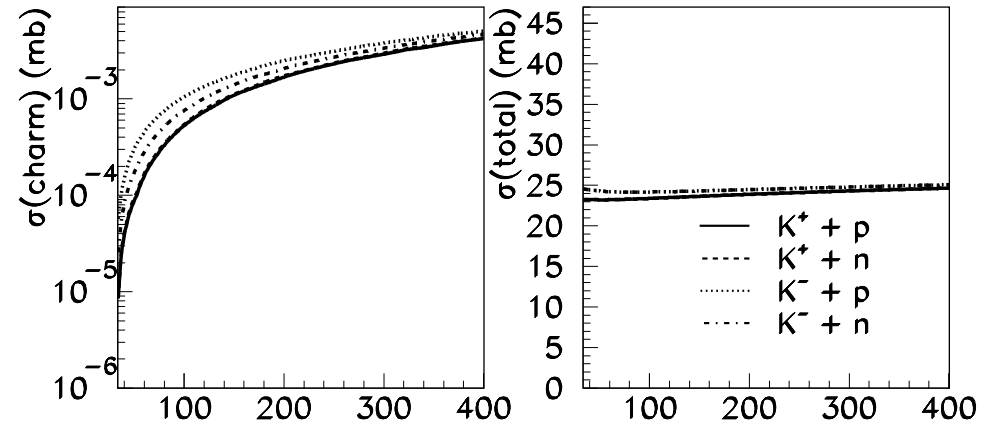
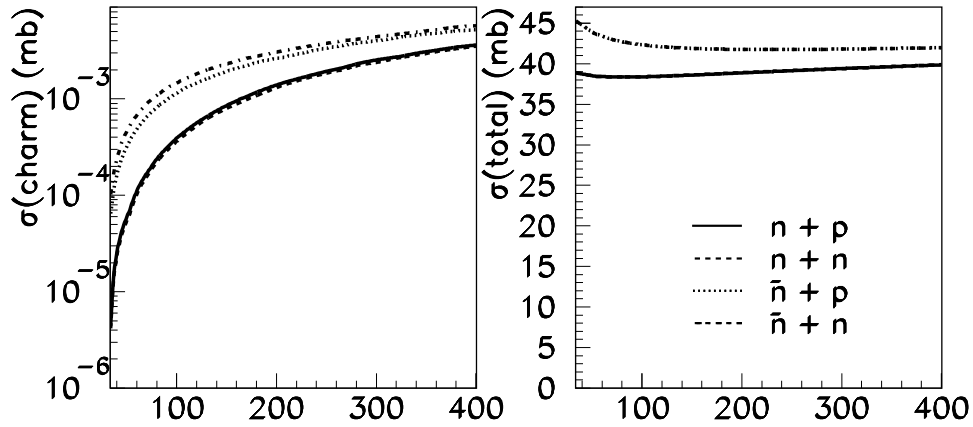
# BACKUP



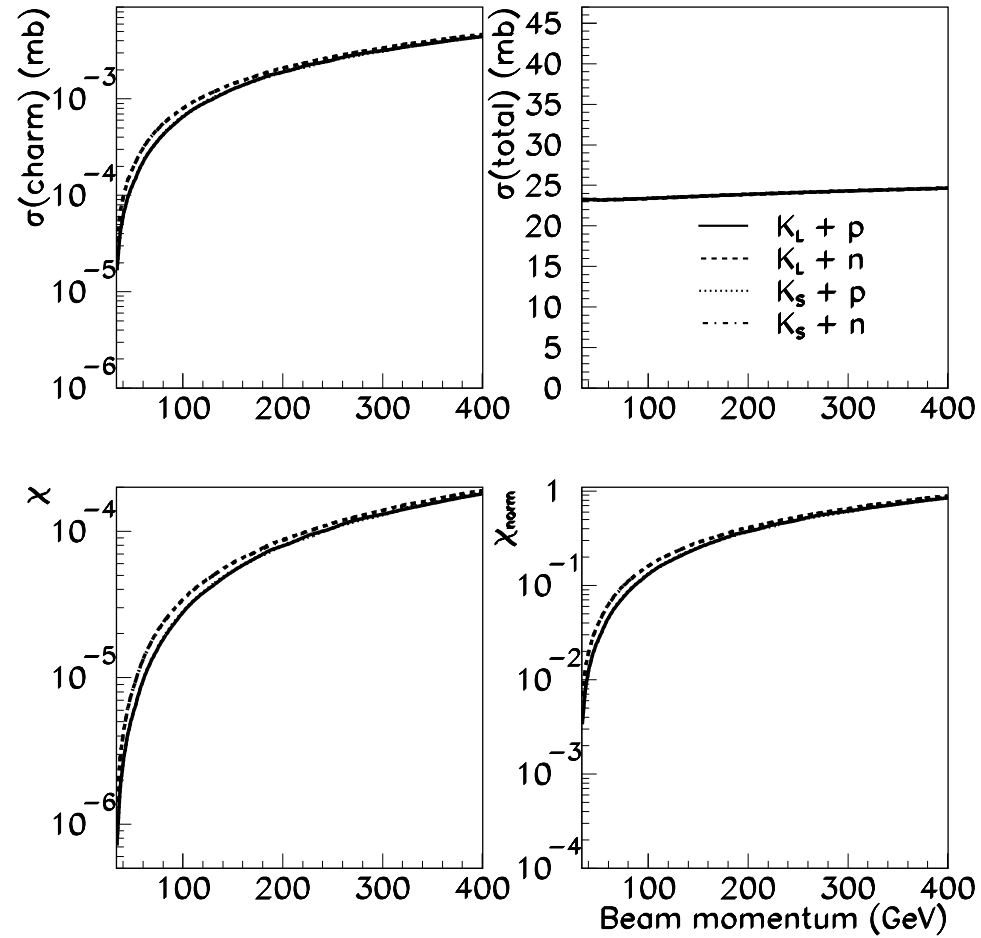
# Steps 1&2) Get $\chi_{\text{norm}}$



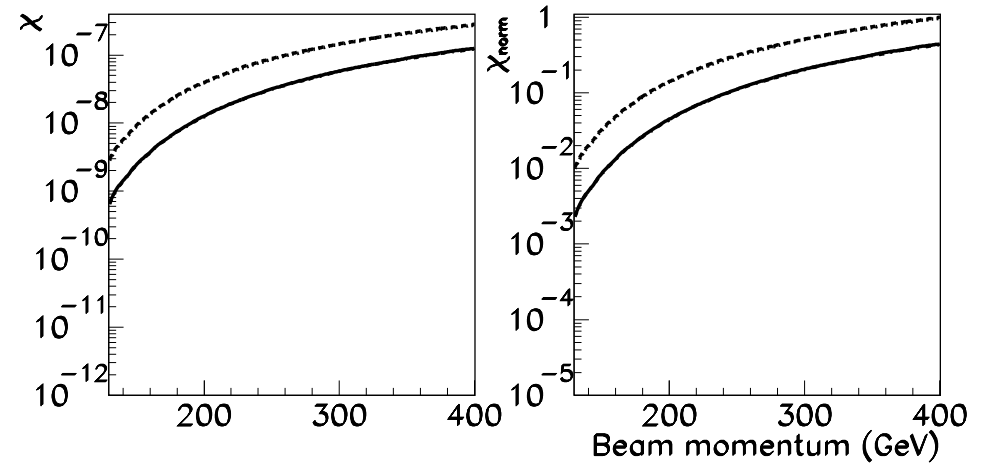
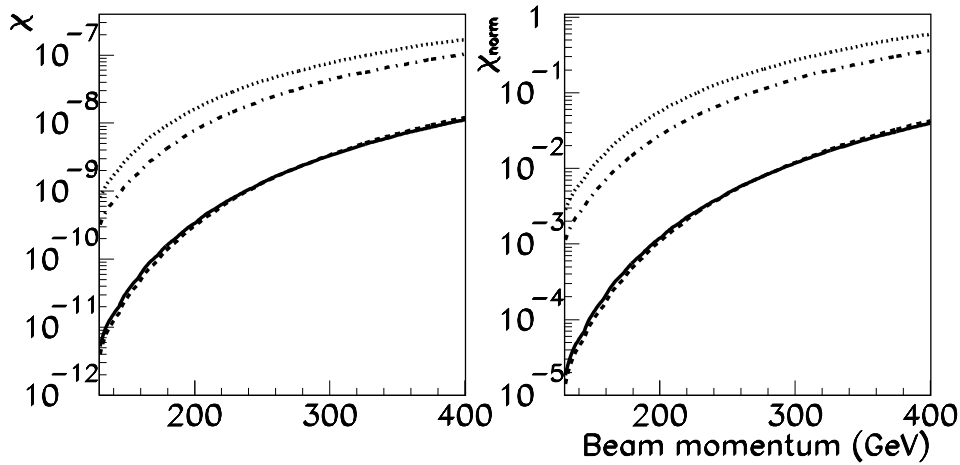
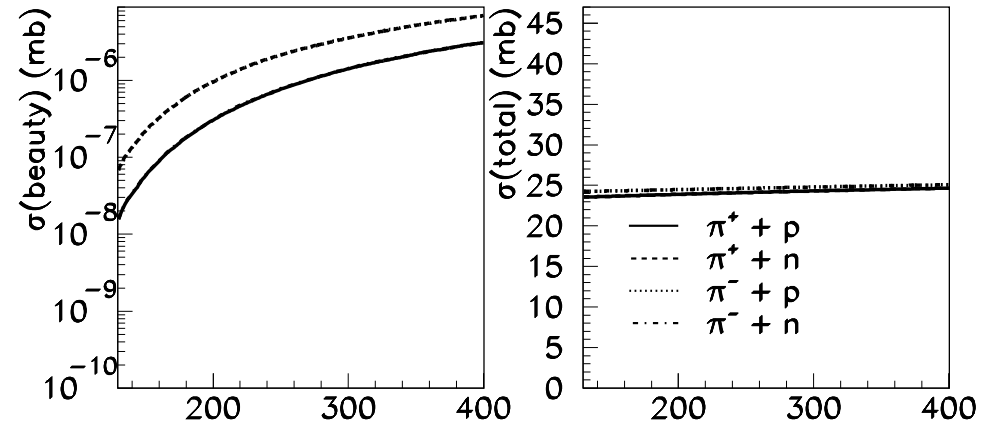
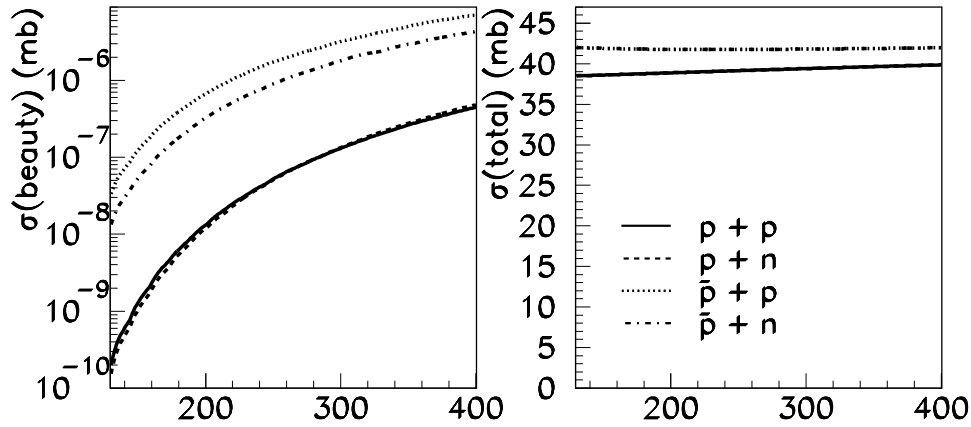
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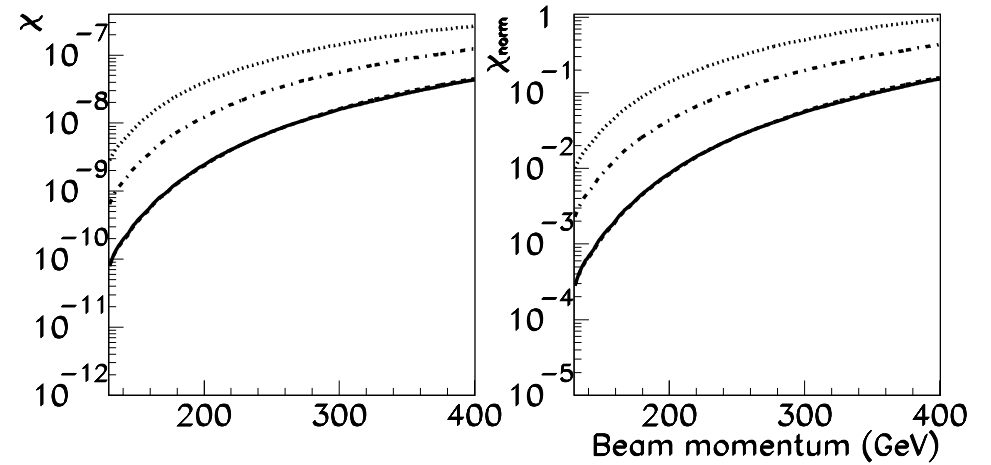
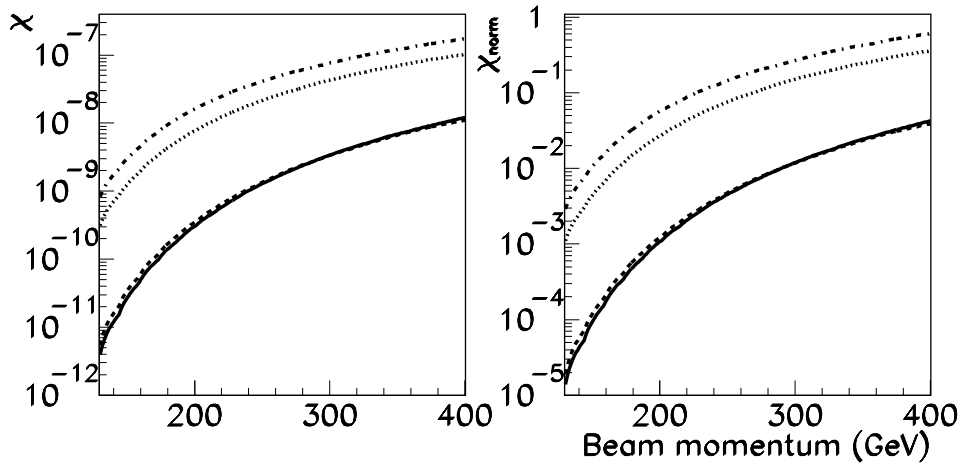
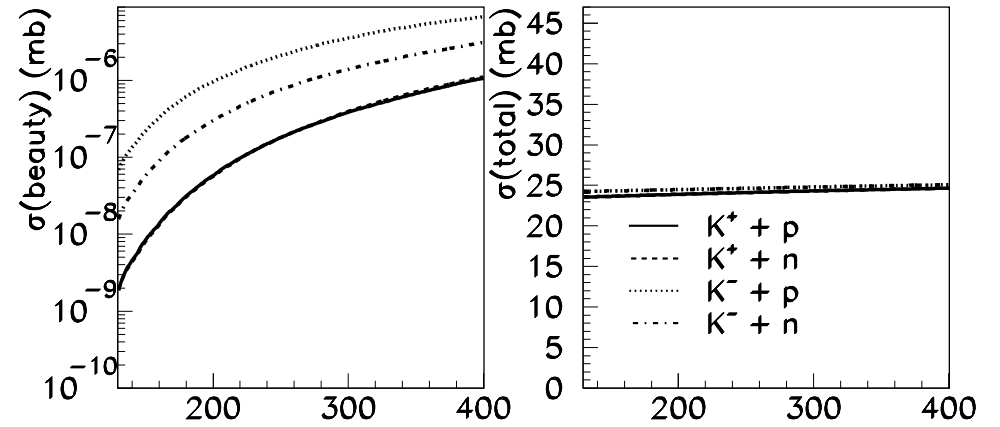
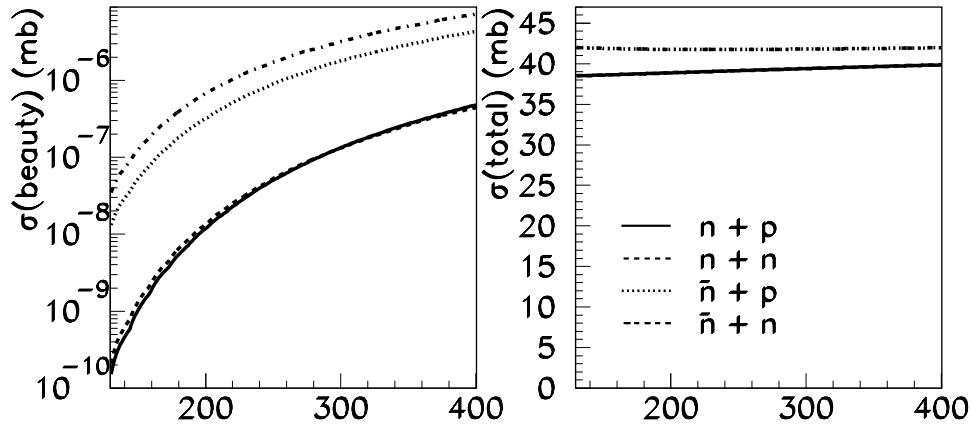
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