

Overview of MATS detector at FAIR and Trap program in India

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At FAIR

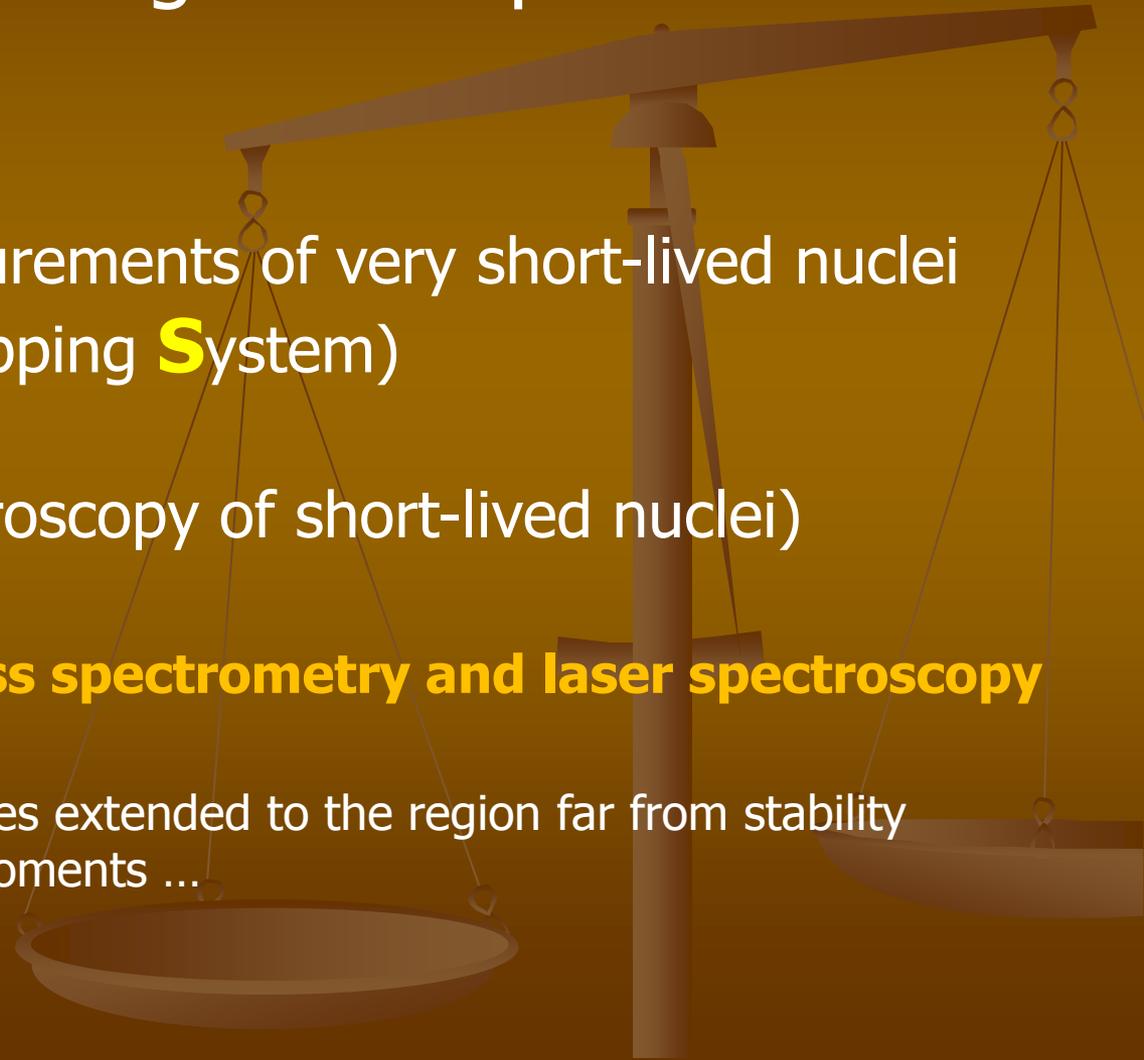
Low Energy Branch (LEB) of the Superconducting FRagment Separator (Super-FRS)

MATS (Precision **M**easurements of very short-lived nuclei using an **A**dvanced **T**rapping **S**ystem)

LaSpec (**L**aser **S**pectroscopy of short-lived nuclei)

Penning-trap based mass spectrometry and laser spectroscopy

Nuclear ground state properties extended to the region far from stability
mass, charge radii, spins, moments ...



MATS FACILITY

- A relative mass uncertainty of 10^{-9}
- ✓ highly-charged ions
- ✓ a non-destructive Fourier-Transform Ion-Cyclotron-Resonance (FT-ICR) detection technique
- ✓ single stored ions

(a) Isomer resolution

(b) Test of the conserved vector current hypothesis and the unitarity of the CKM matrix:

(c) Nuclear structure and the new masses:

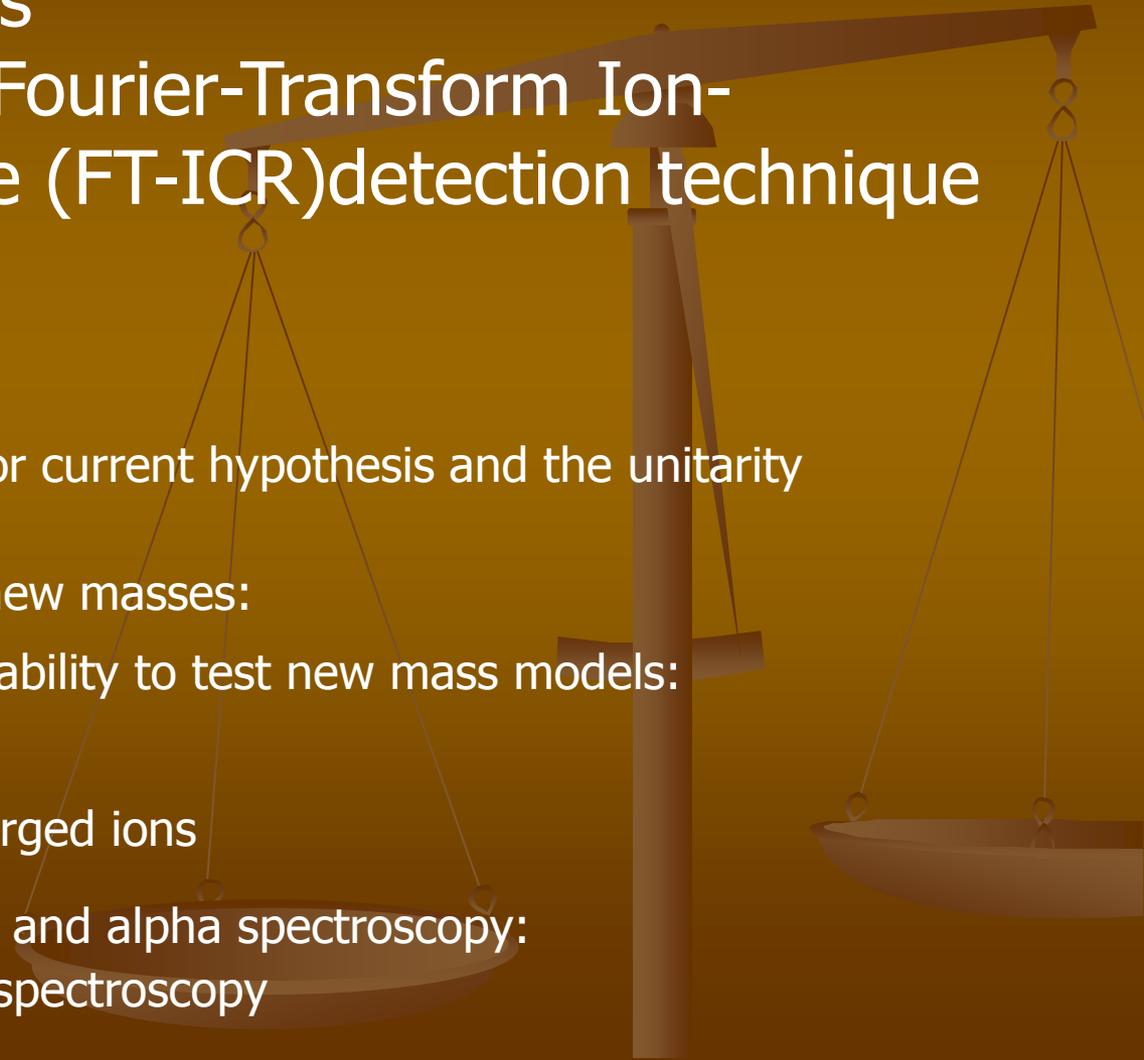
(d) Nuclear masses far from stability to test new mass models:

(e) Astrophysics

(f) Spectroscopy on highly-charged ions

(g) In-trap conversion electron and alpha spectroscopy:

(h) Trap-assisted and neutron spectroscopy



Review

MATS and LaSpec: High-precision experiments using ion traps and lasers at FAIR

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Advantages of using a TRAP

PROVIDES

An ENVIRONMENT FOR PRECISION MEASUREMENT

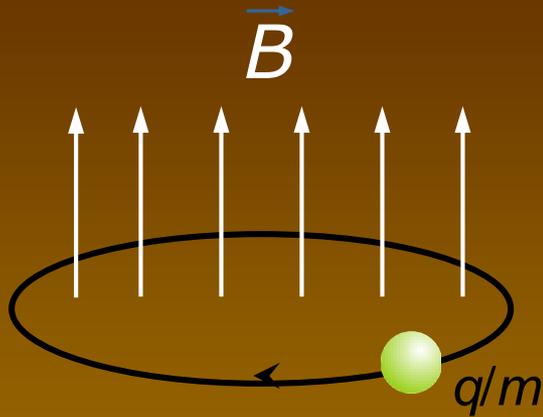
As in a trap there is...

- Well controlled environment*
- Small size and energy distribution of the source*
- Long and repeated observations possible*

So advantages of in TRAP studies

- β - decay studies :*** *No source scattering*
Recoil ion study possible
- Spectroscopic studies:*** *Isolation of a decay article*
Repeated measurement possible
- Angular Distribution of decay particles :*** *Source size small*

Principle of Penning Ion Trap working



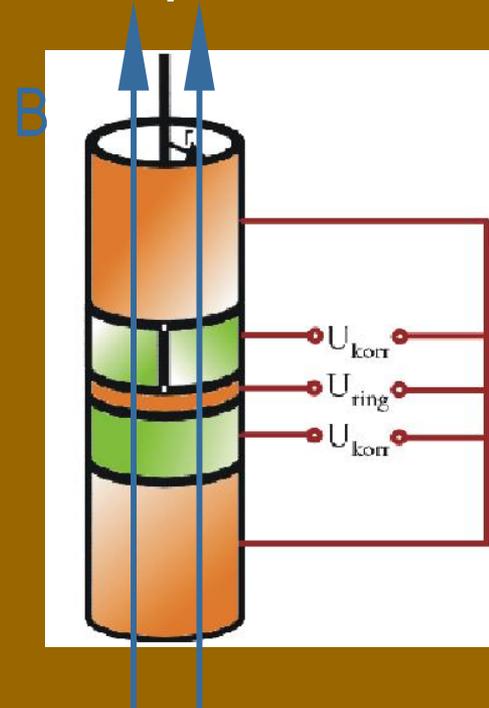
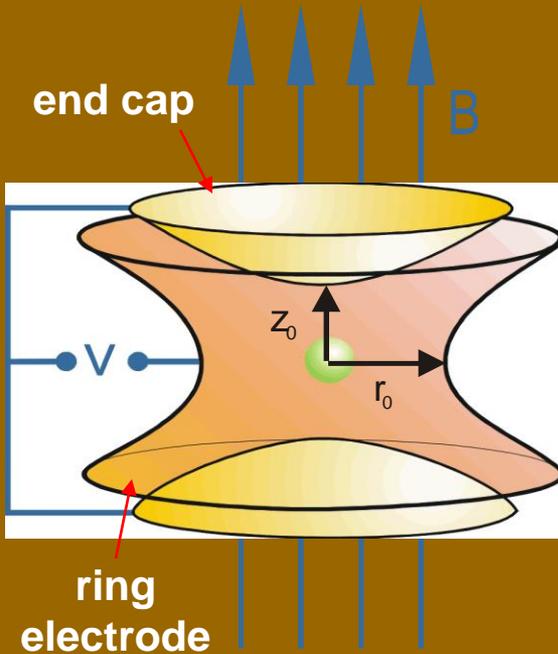
Cyclotron frequency:
$$f_c = \frac{1}{2\pi} \cdot \frac{q}{m} \cdot B$$

Hyperbolic

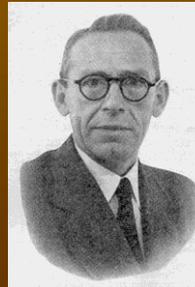
PENNING trap

- Strong homogeneous magnetic field
- Weak electric 3D quadrupole field

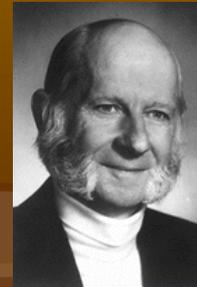
Cylindrical



Frans Michel Penning



Hans G. Dehmelt



Ion Motion in a Penning Trap

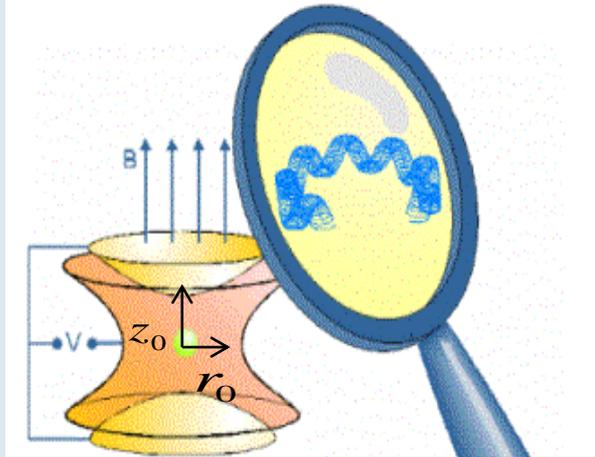
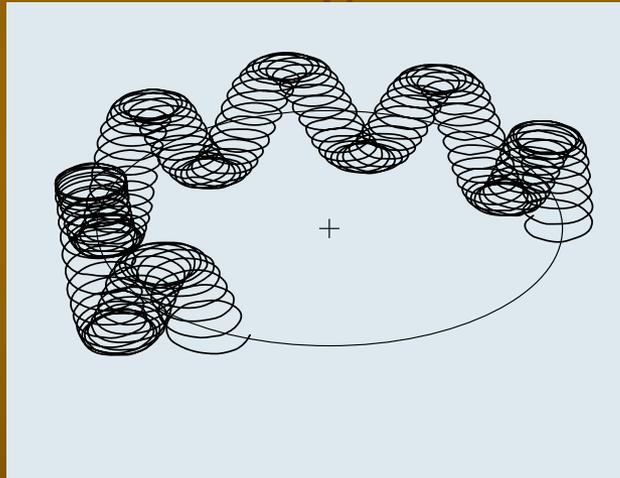
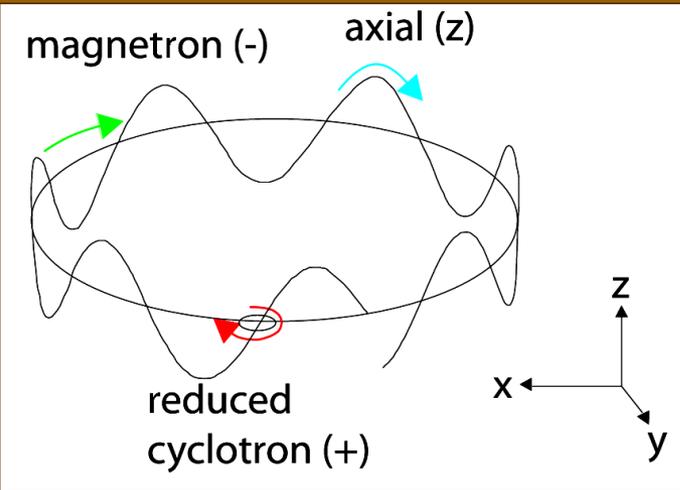


Motion of an ion is the superposition of three characteristic harmonic motions:

- axial motion (frequency ν_z)
- magnetron motion (frequency ν_-)
- modified cyclotron motion (frequency ν_+)

$$\nu_z = \frac{1}{2\pi} \sqrt{\frac{qV}{md^2}}$$

$$\nu_{\pm} = \frac{\nu_c}{2} \pm \sqrt{\frac{\nu_c^2}{4} - \frac{\nu_z^2}{2}}$$



The frequencies of the radial motions obey

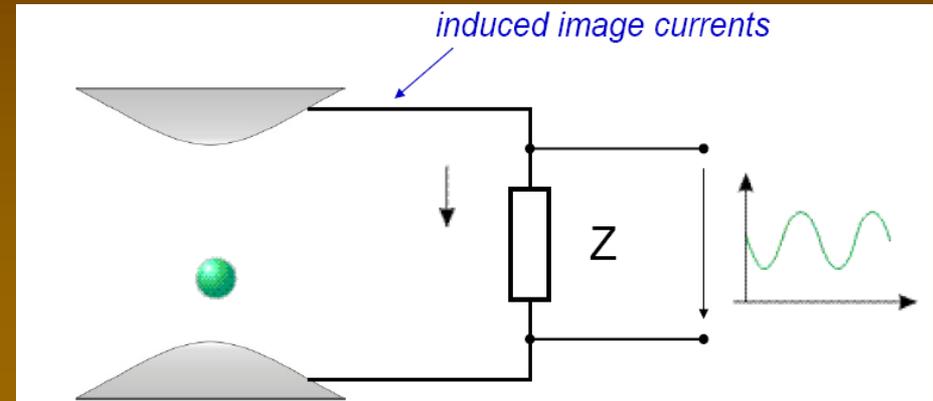
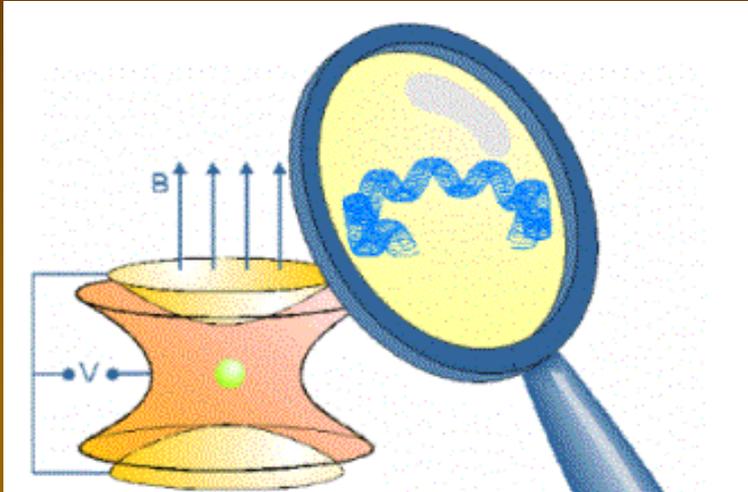
$$\nu_c = \nu_+ + \nu_-$$

$$\nu_c = \frac{1}{2\pi} \cdot \frac{q}{m} \cdot B$$

$$d^2 = \frac{1}{2} (z_0^2 + r_0^2)$$

Detection by Non destructive IMAGE CHARGE

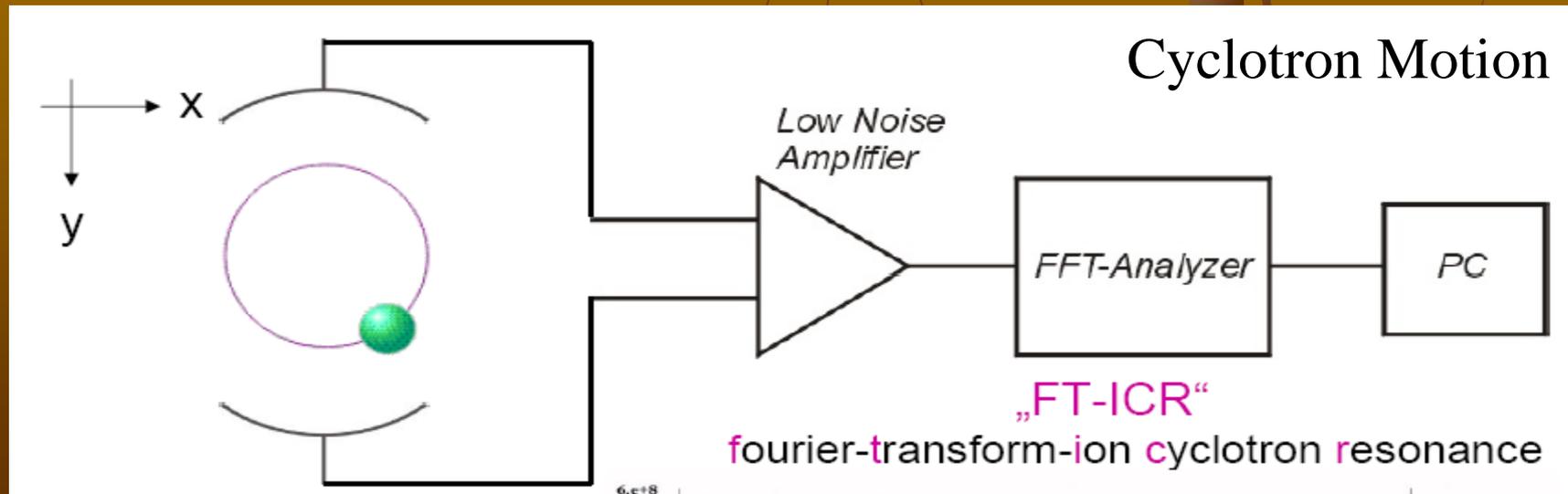
Broad band detection



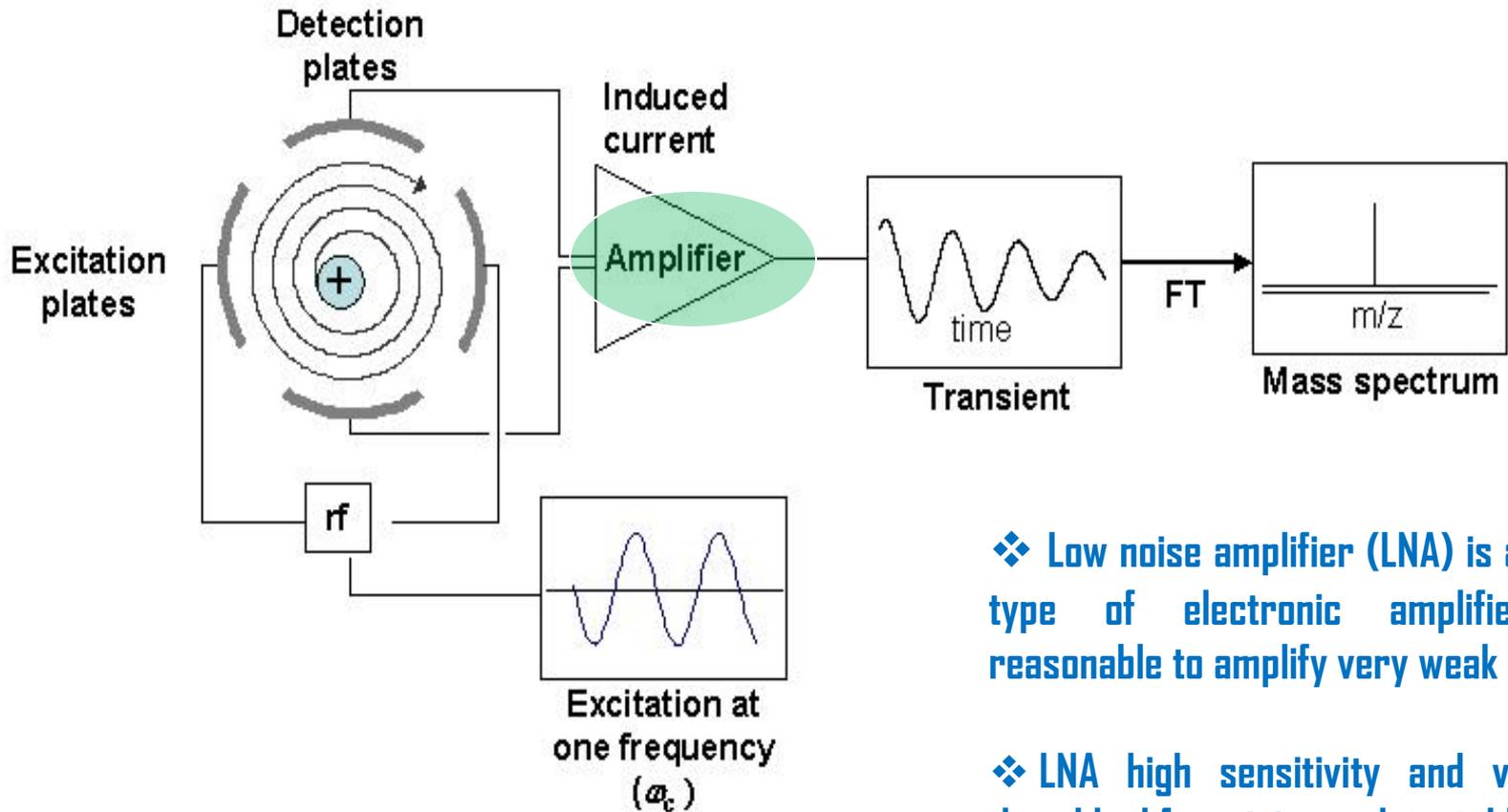
induced current:

$$I_{\text{eff}} = 1/\sqrt{2} \cdot r_{\text{ion}} / D \cdot \omega \cdot q$$

Cyclotron Motion

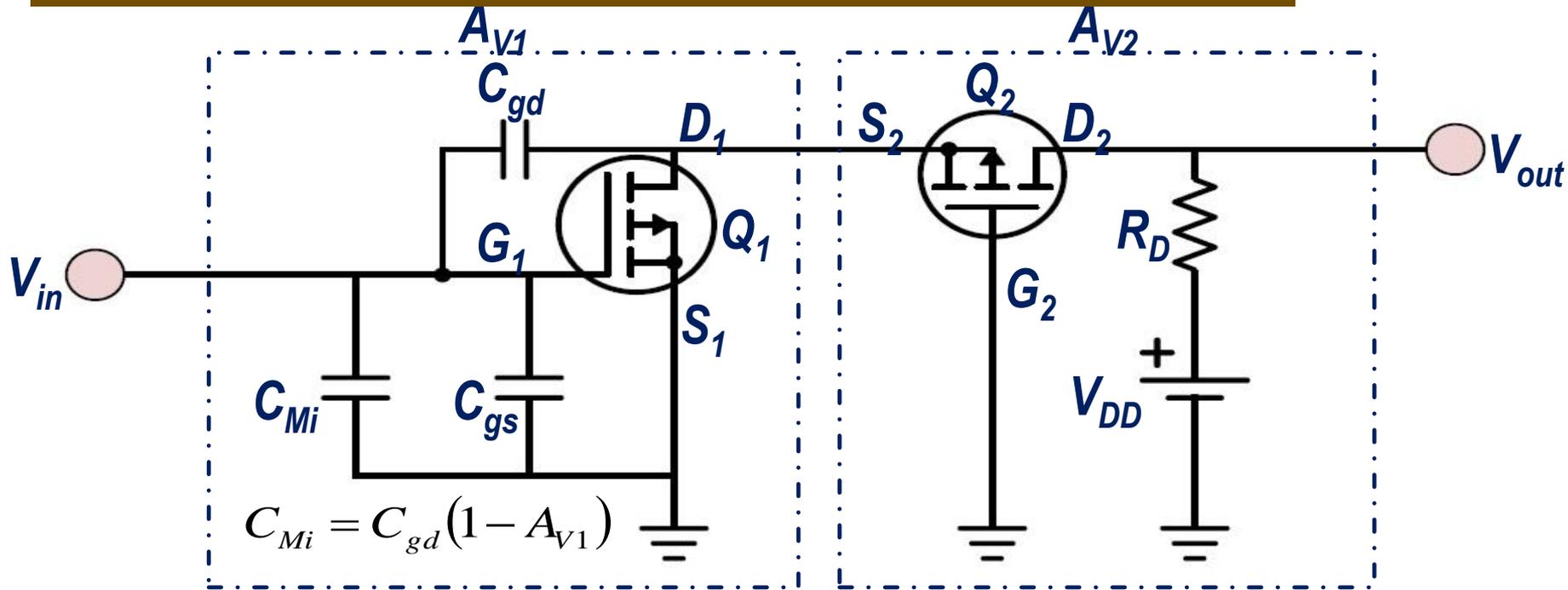


FTICR DETECTION TECHNIQUE



- ❖ Low noise amplifier (LNA) is a special type of electronic amplifier with reasonable to amplify very weak signals
- ❖ LNA high sensitivity and very low threshold for minimum detectable signal

Low Noise Amplifier with high input resistance



Cascode



Common Source

+

Common Gate

- Inverting Amplifier
- Miller effect increases input capacitance

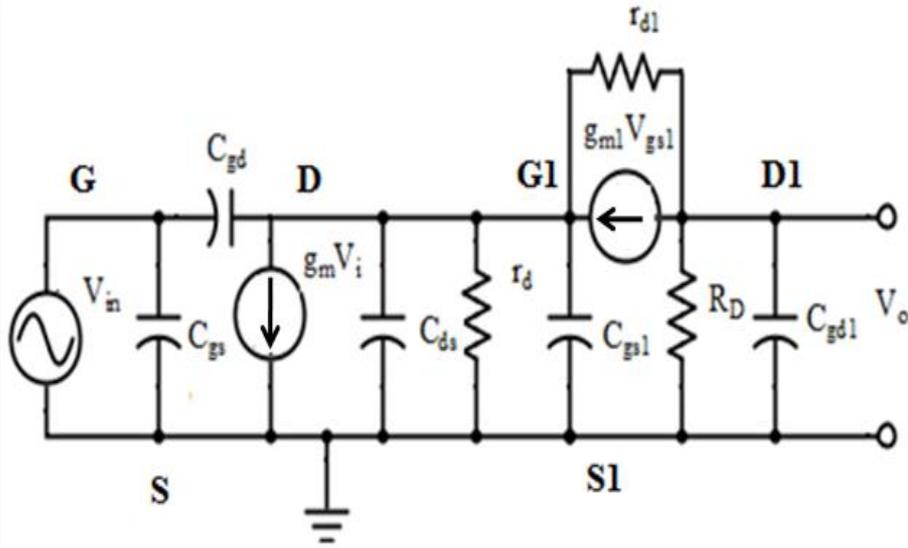
- Non-inverting Amplifier
- Low input impedance

A_{V1} decreases which reduces miller input capacitance (C_{Mi})

$$f_H = \frac{1}{2\pi R(C_{gs} + C_{Mi})}$$

- Better isolation between input and output
- Better frequency response
- Higher voltage gain

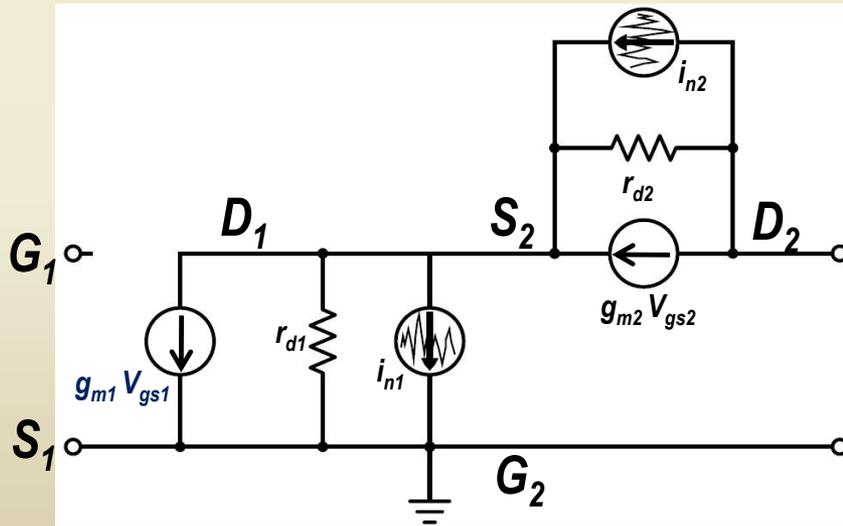
Voltage gain and noise for a cascode amplifier



High Frequency Model of Cascode Amplifier

Voltage gain

$$A_V = - \frac{g_m \left(g_{m1} + \frac{1}{r_{d1}} \right) r_{d1} R_D}{r_{d1} \left(g_{m1} + \frac{1}{r_{d1}} + \frac{1}{r_d} \right) + \frac{R_D}{r_d}}$$

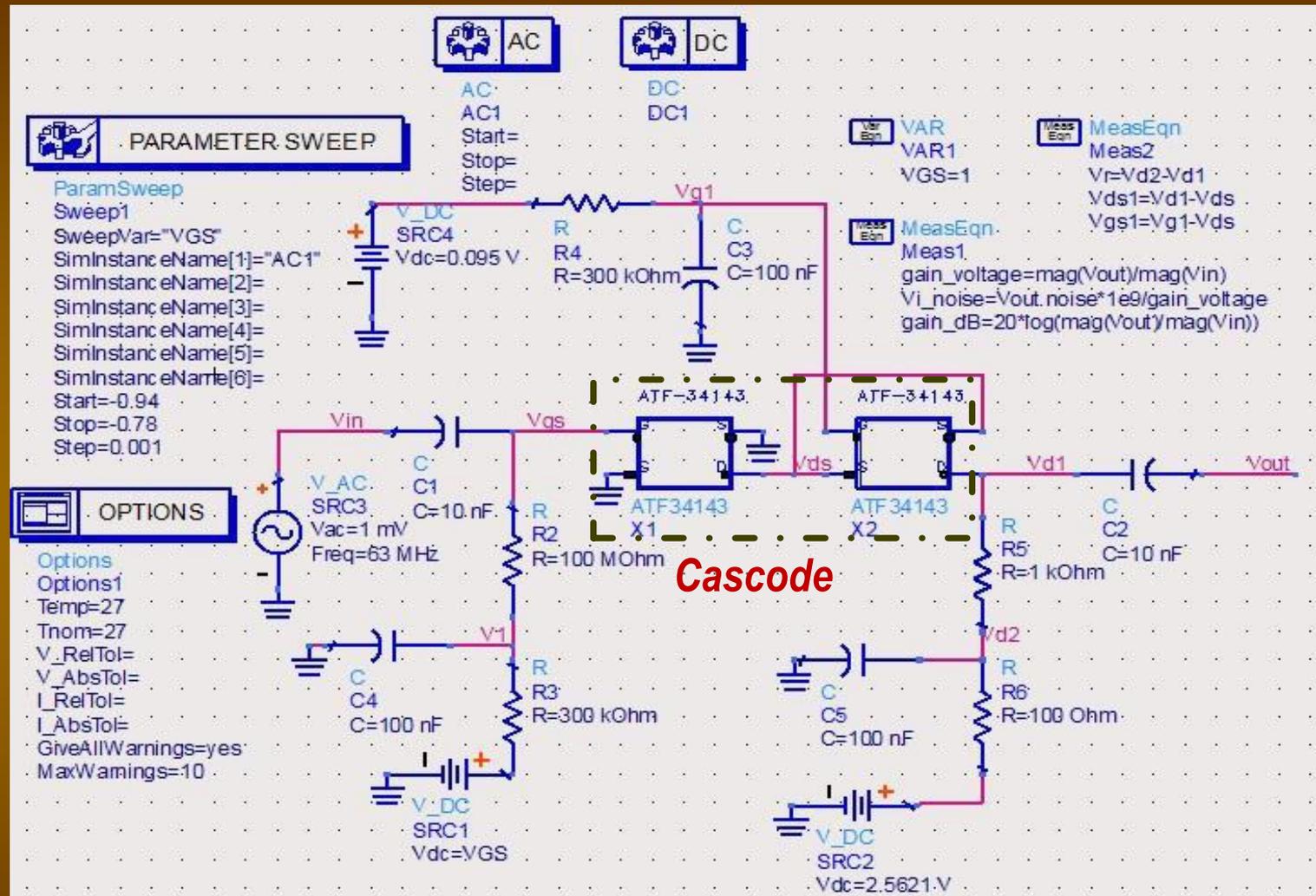


Thermal Noise Model of Cascode Amplifier

Input voltage noise density

$$v_n^2 = \frac{4kT\gamma}{g_{m1}} \left[1 + \left(\frac{g_{m2}}{g_{m1}} \right) \left(\frac{r_{d2}}{r_{d1}} \right)^2 \frac{1}{(g_{m2} r_{d2} + 1)^2} \right]$$

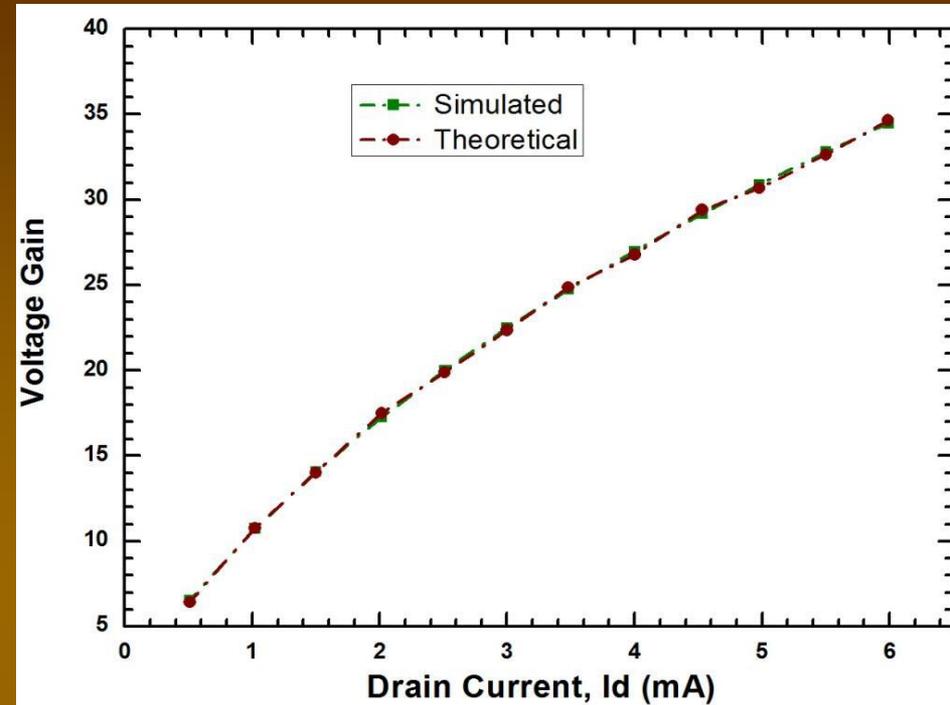
Cascode LNA Simulation



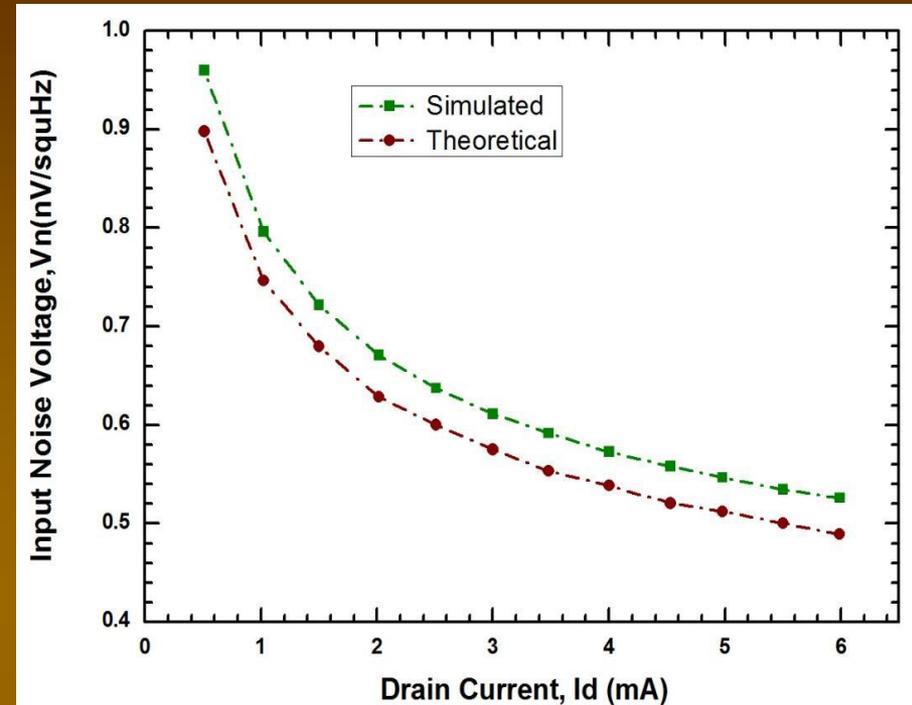
Advanced Design System (ADS)

:An electronic design automation software produced by Agilent

Simulation of voltage gain and input voltage noise with different drain current



Voltage gain Vs drain current



Input voltage noise density Vs drain current for cascode amplifier

- ❑ The simulated voltage gain is very close to the theoretical value.
- ❑ The input voltage noise density simulated in ADS is slightly higher than the theoretical value of channel thermal noise

Device selection

- **VECC Penning trap is a cryogenic facility which will operate at 4K. So, GaAs devices has been chosen considering its low noise characteristics and its ability to operate at very low temperature.**

Common source stage



Avago GaAs FET (ATF-34143)

- **Very low noise figure ~ 0.5 dB**
- **Gain ~ 17.5 dB**
- **Typical transconductance ~ 230 mS**
- **Very low input capacitance ~ 0.8 pF**
- **Very low gate-drain feedback capacitance ~ 0.16 pF**

Common gate stage



Toshiba GaAs FET (3SK-240)

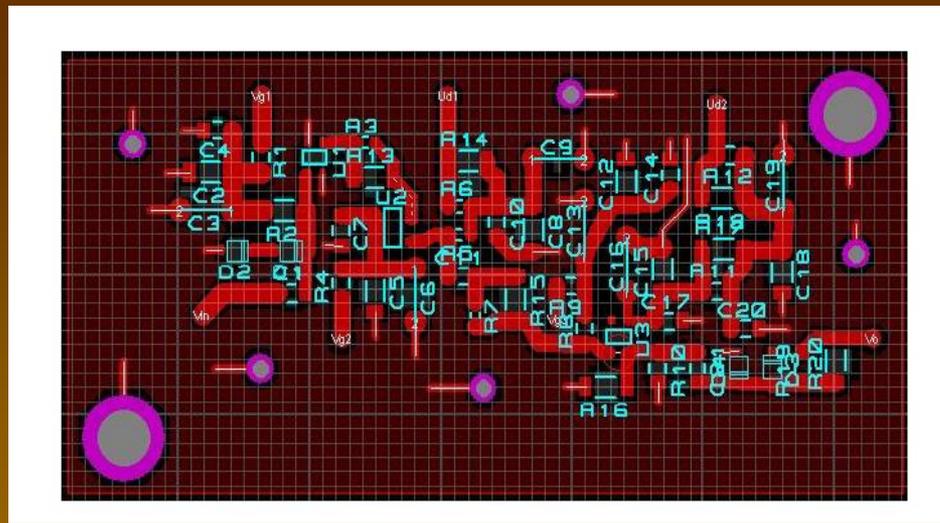
- **Low noise figure ~ 1 dB**
- **Gain ~ 20.5 dB**
- **Transconductance ~ 19 mS**
- **Very low input capacitance ~ 0.6 pF**
- **Very low gate-drain feedback capacitance ~ 0.013 pF**

Impedance matching stage

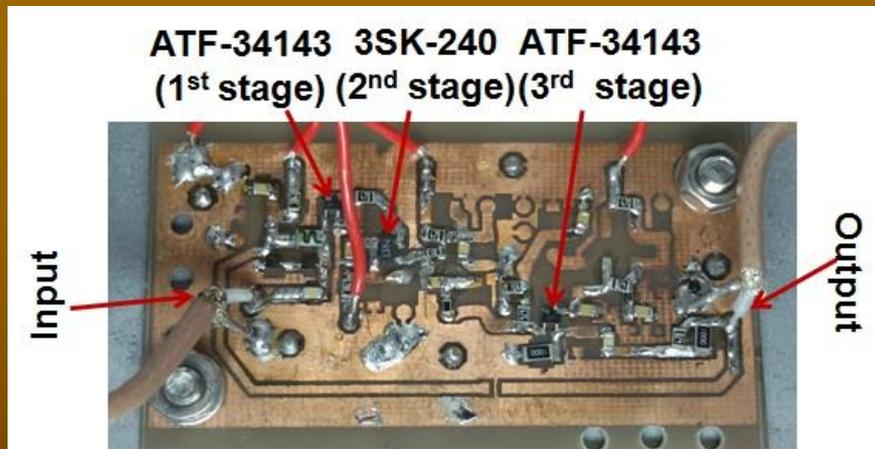


Avago GaAs FET (ATF-34143)

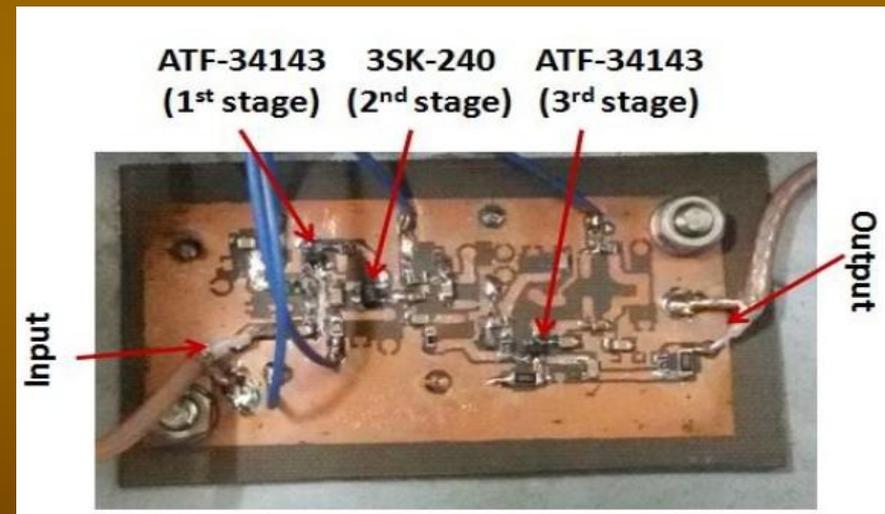
LNA CIRCUIT FABRICATED



LNA circuit layout built on ARES

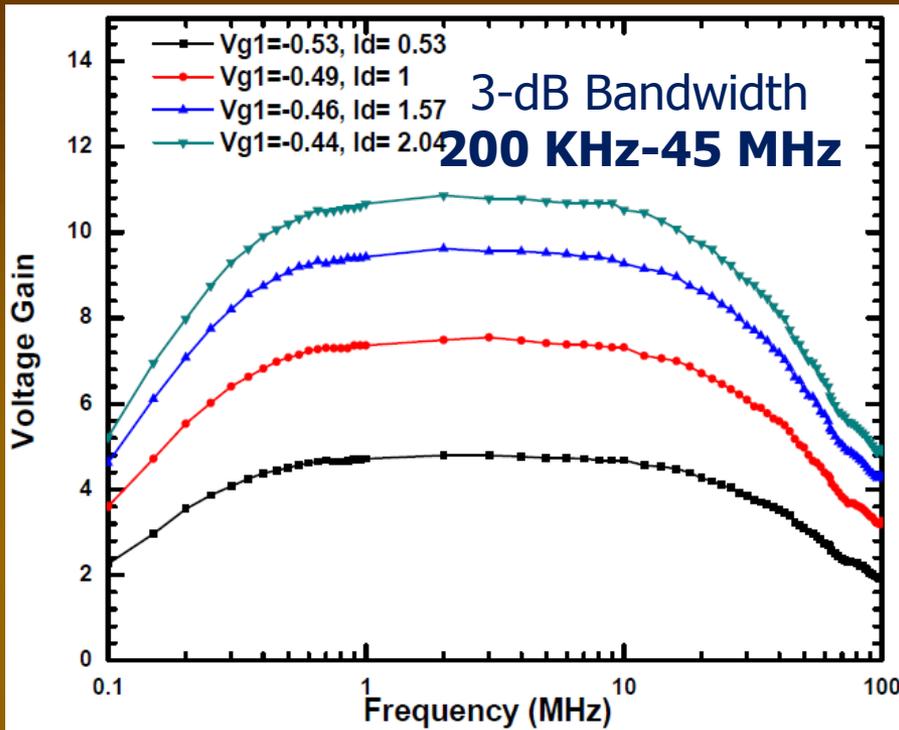


LNA circuit fabricated on FR4 PCB

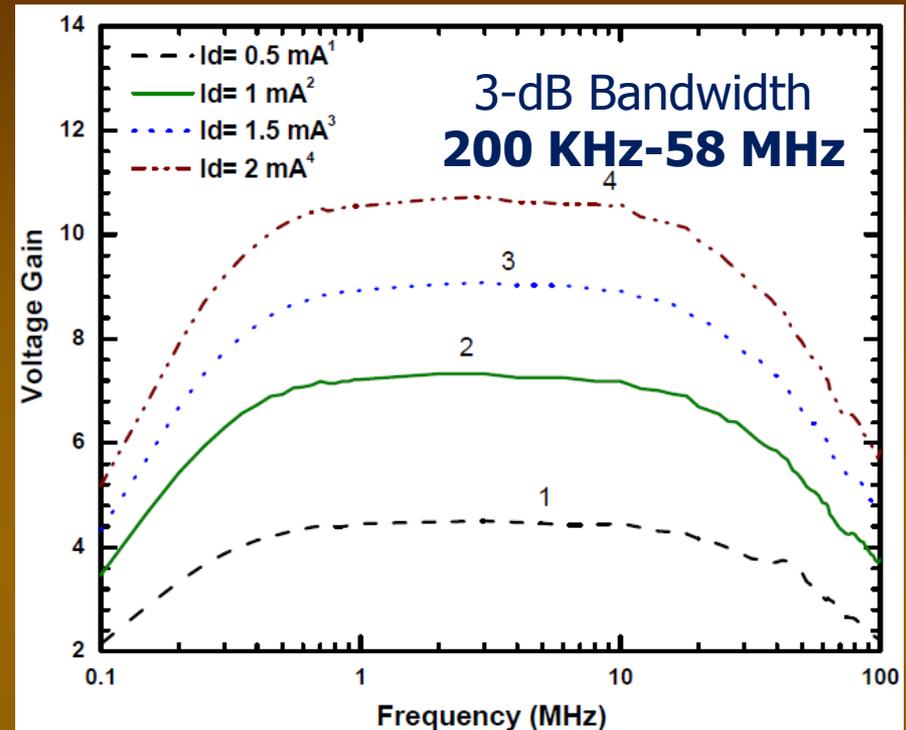


LNA circuit fabricated on Teflon PCB

Voltage Gain of LNA

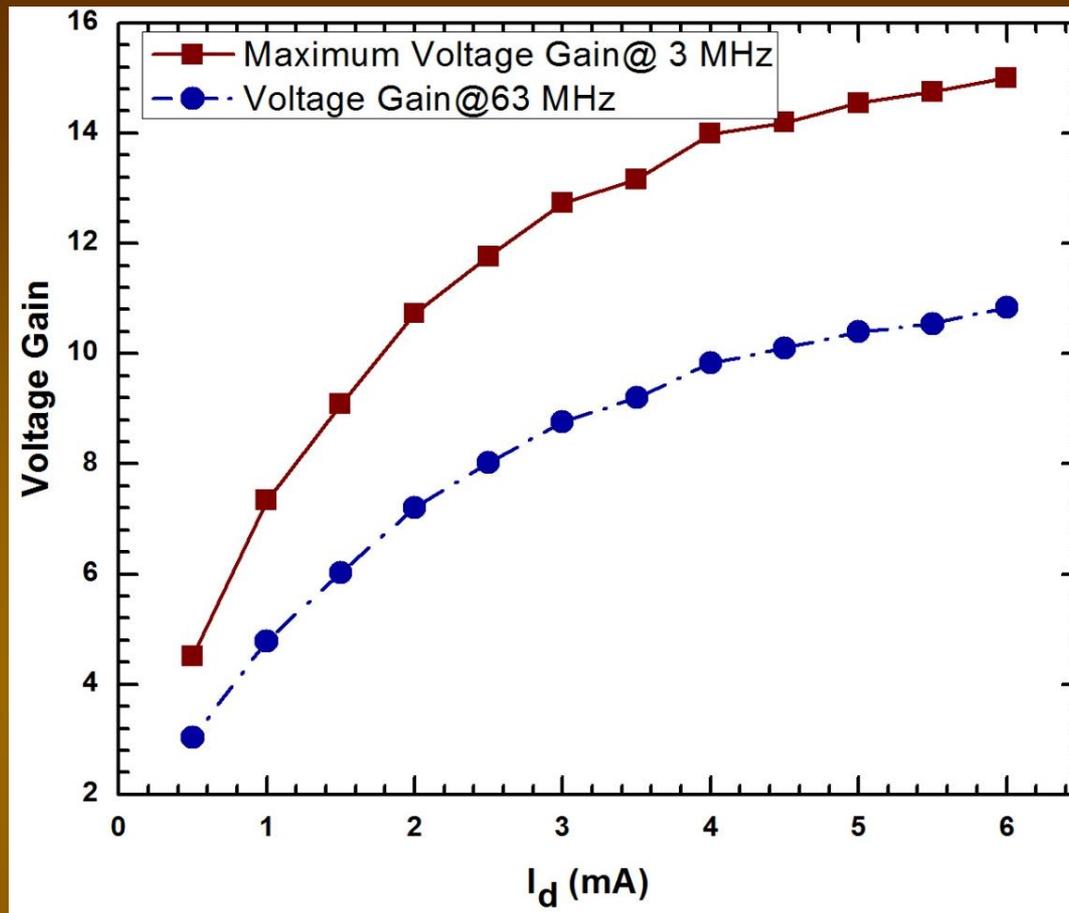


Frequency response with FR4 substrate



Frequency response with Teflon substrate

□ The higher cut-off frequency with teflon substrate is $\approx 58 \text{ MHz}$ compared to FR4 substrate where higher cut-off frequency is $\approx 45 \text{ MHz}$



Voltage gain vs drain current

- ❑ Voltage gain of the LNA decreases at 63 MHz due to roll-off of voltage gain at higher frequency

Noise Measurement

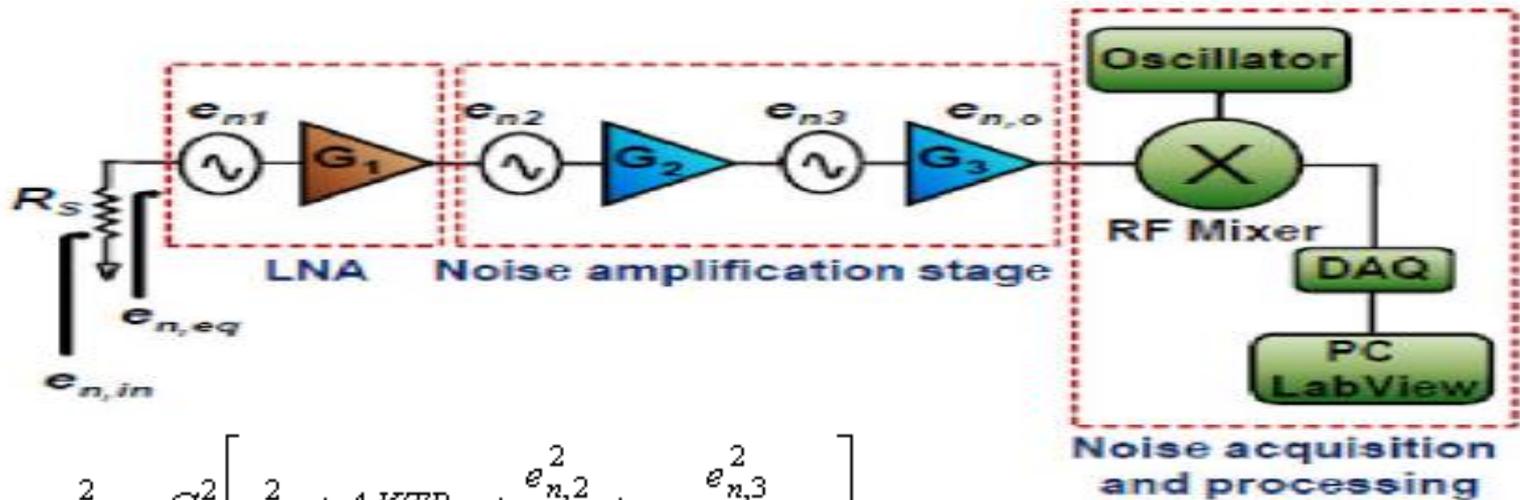
One can measure the noise performance of a low noise amplifier using a spectrum analyzer/network analyzer or noise figure meter

Above noise measurement devices are very costly and not easily available so we have tried an alternate method of noise measurement

NOISE MEASUREMENT USING DAQ (NI-PCI 4472)

- Here, we have integrated a low frequency data acquisition card (DAQ) using Labview 8.5 to measure the input voltage noise density of an amplifier.**
- This DAQ card can acquire an input signal from DC - 49.8 KHz. So we need to downconvert the actual signal to the frequency range acceptable DAQ card to measure the noise of amplifier at high frequency**

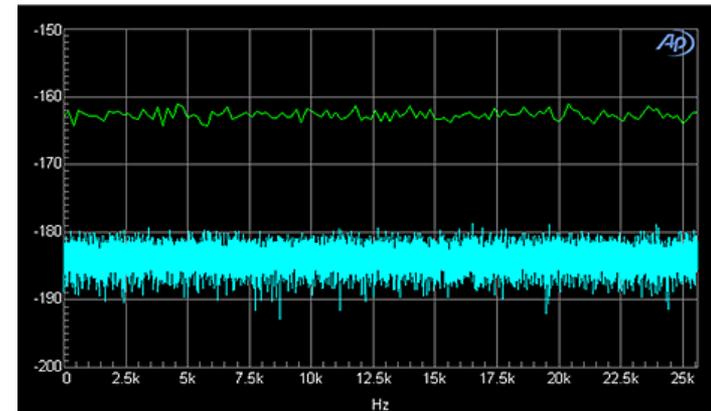
Noise measurement Scheme



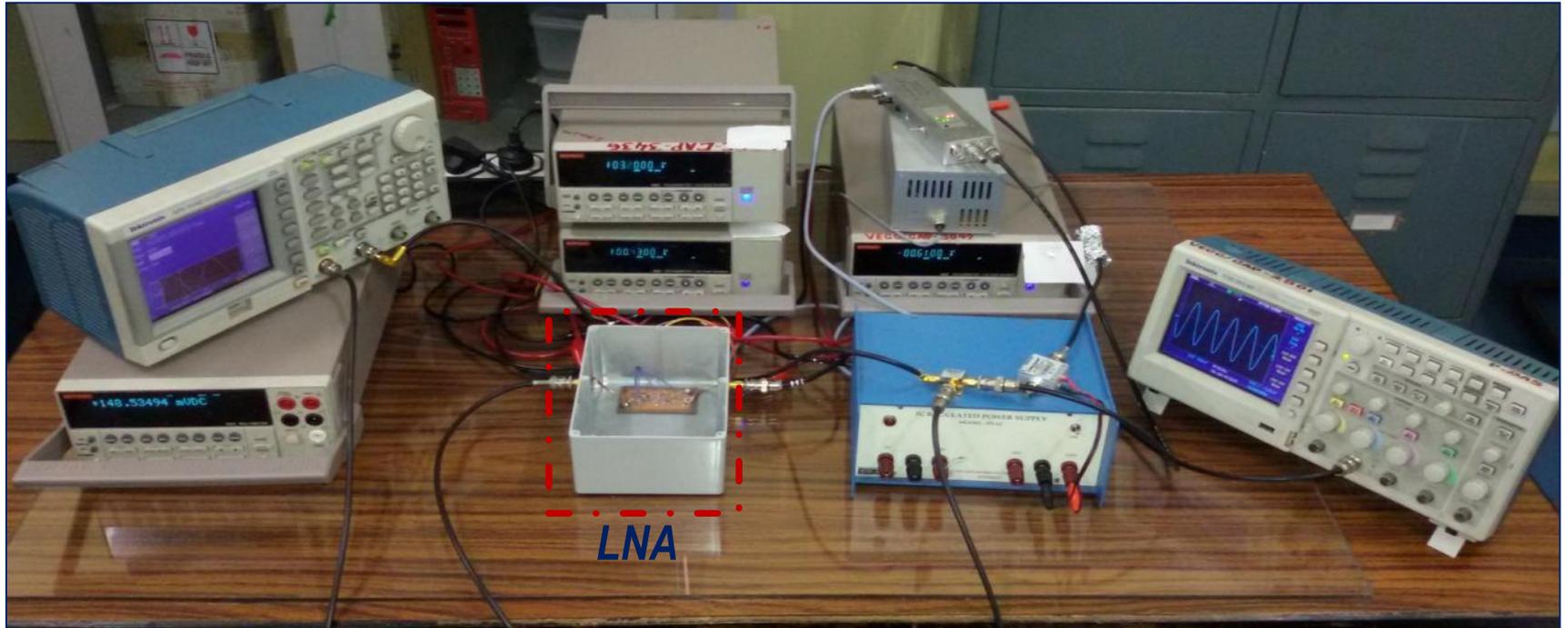
$$e_{n,o}^2 = G^2 \left[e_{n,1}^2 + 4KTR_S + \frac{e_{n,2}^2}{G_1^2} + \frac{e_{n,3}^2}{(G_1^2 \cdot G_2^2)^2} \right]$$

$$V_{n,eq} = \sqrt{V_{n,in}^2 - 4KTR_S} = \sqrt{\left(\frac{V_{n,0}}{G} \right)^2 - 4KTR_S}$$

$$V_{n,eq} = \sqrt{V_{n,1}^2 + \frac{1}{G_1^2} V_{n,2}^2 + \frac{1}{(G_1 \cdot G_2)^2} V_{n,3}^2}$$



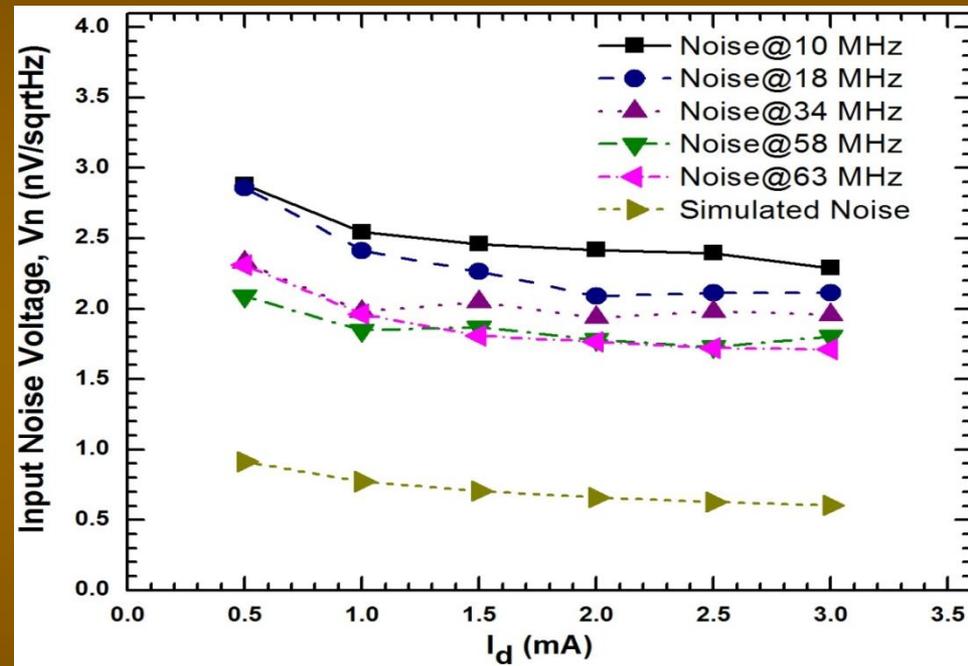
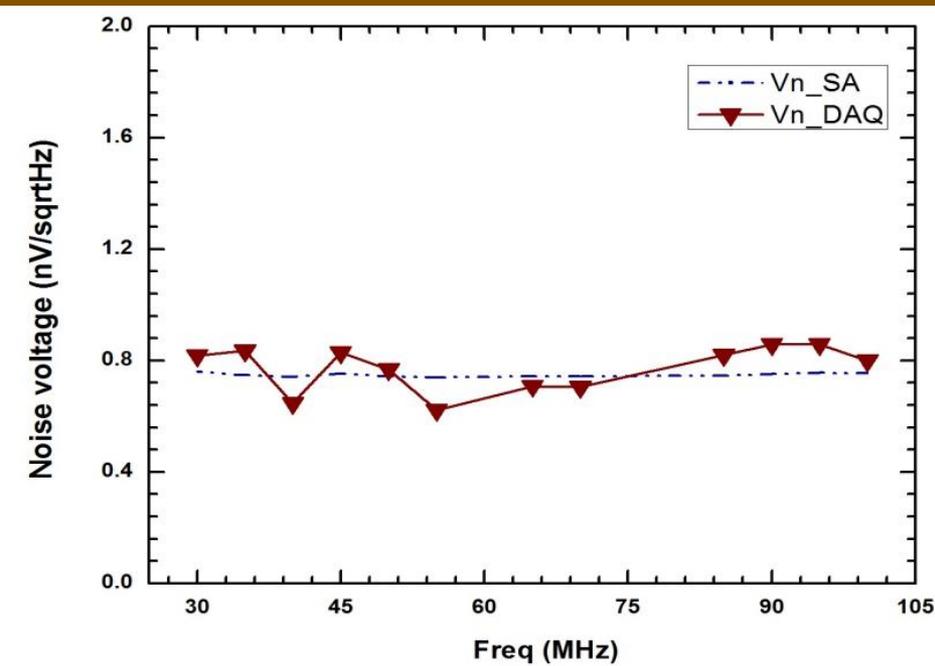
- If the 2nd and 3rd stage amplifier has a low noise characteristics then the $V_{n,eq}$ will be close to the input voltage noise density V_{n1} of the LNA.



Experimental setup for amplifier testing

Comparison of noise measurement of ZFL-500LN using spectrum analyzer and DAQ card

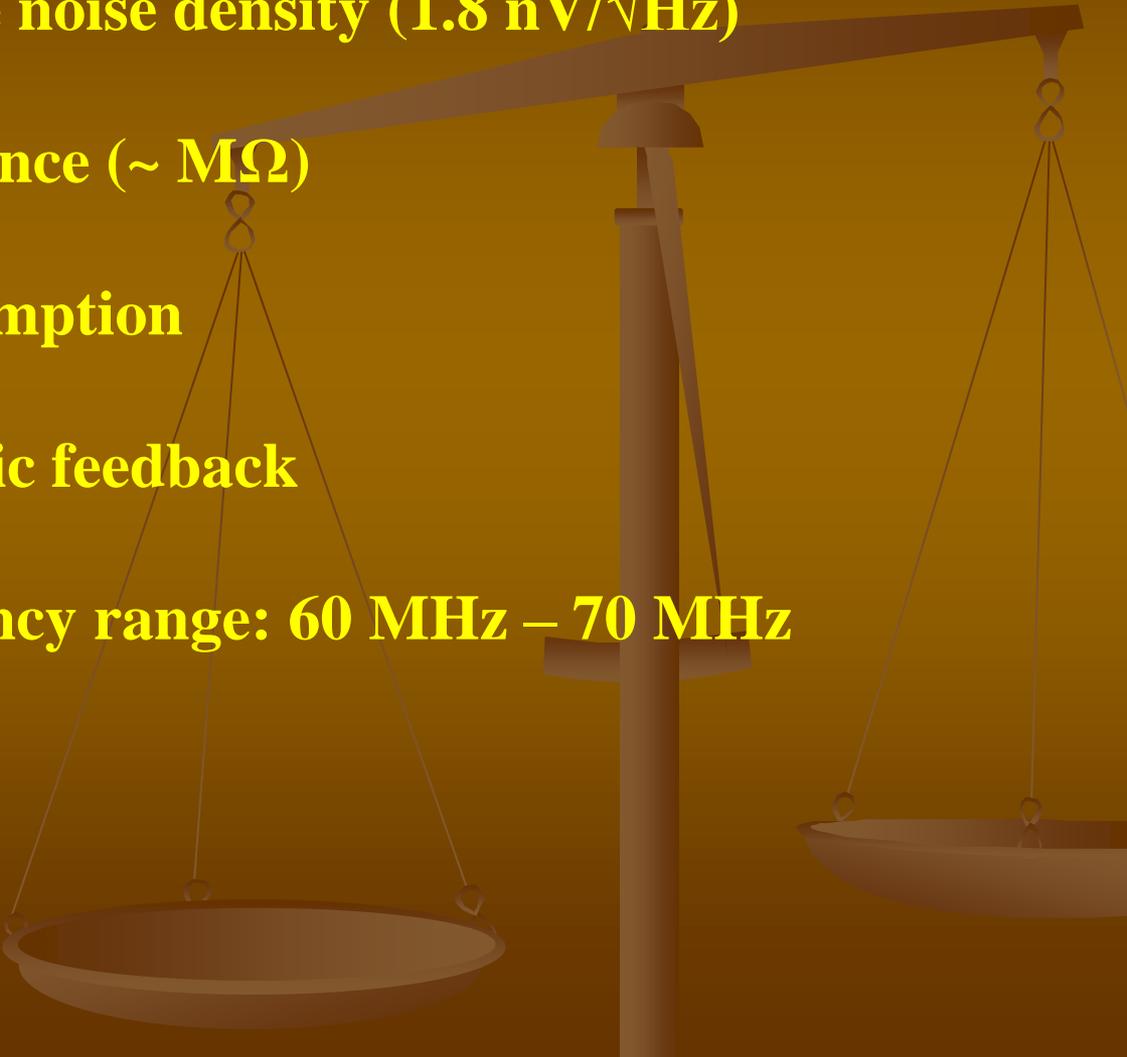
Noise performance of LNA under different operating condition



Input noise voltage vs drain current with teflon substrate

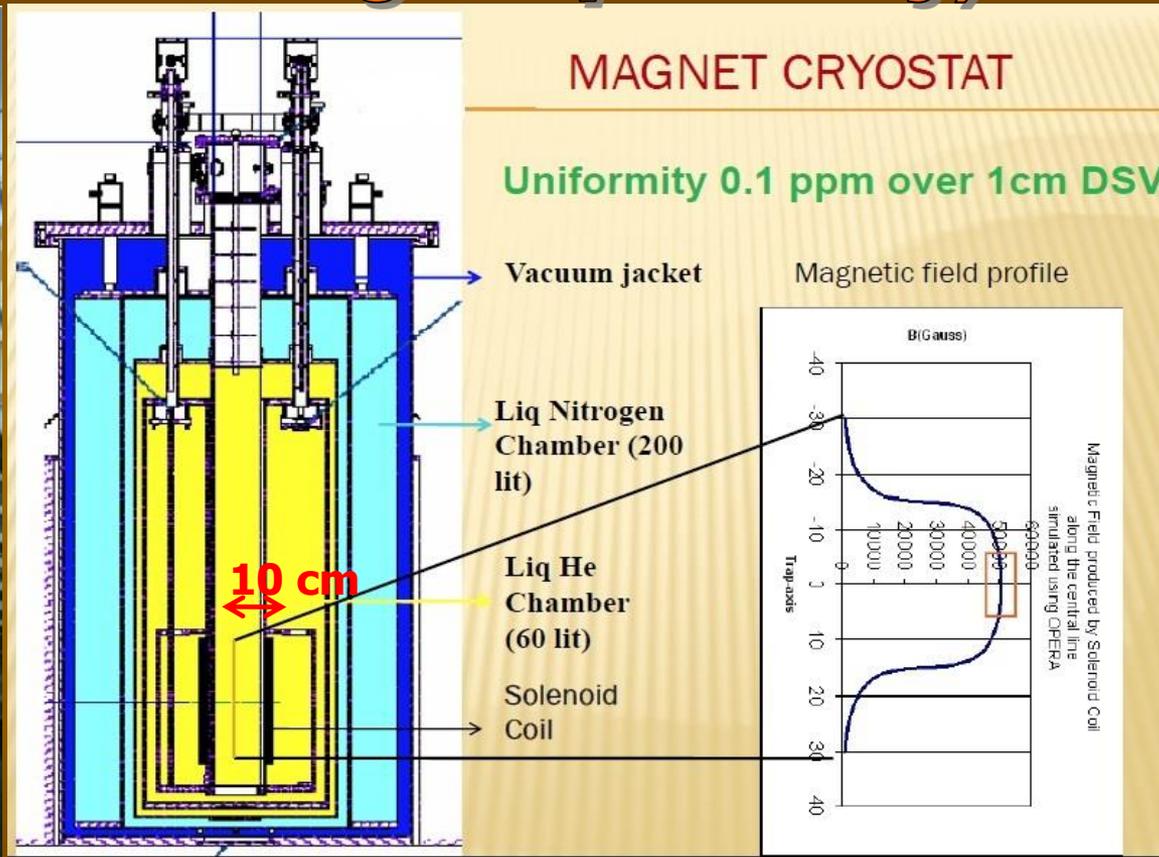
The input voltage noise density at 63 MHz with FR4 substrate was found to be $\approx 2.7 \text{ nV}/\sqrt{\text{Hz}}$ with a drain current of 1 mA while it improves to $\approx 1.8 \text{ nV}/\sqrt{\text{Hz}}$ with teflon substrate.

LNA SPECIFICATIONS

- **Low input voltage noise density (1.8 nV/ $\sqrt{\text{Hz}}$)**
 - **High input resistance ($\sim \text{M}\Omega$)**
 - **Low power consumption**
 - **Minimum parasitic feedback**
 - **Operating frequency range: 60 MHz – 70 MHz**
- 

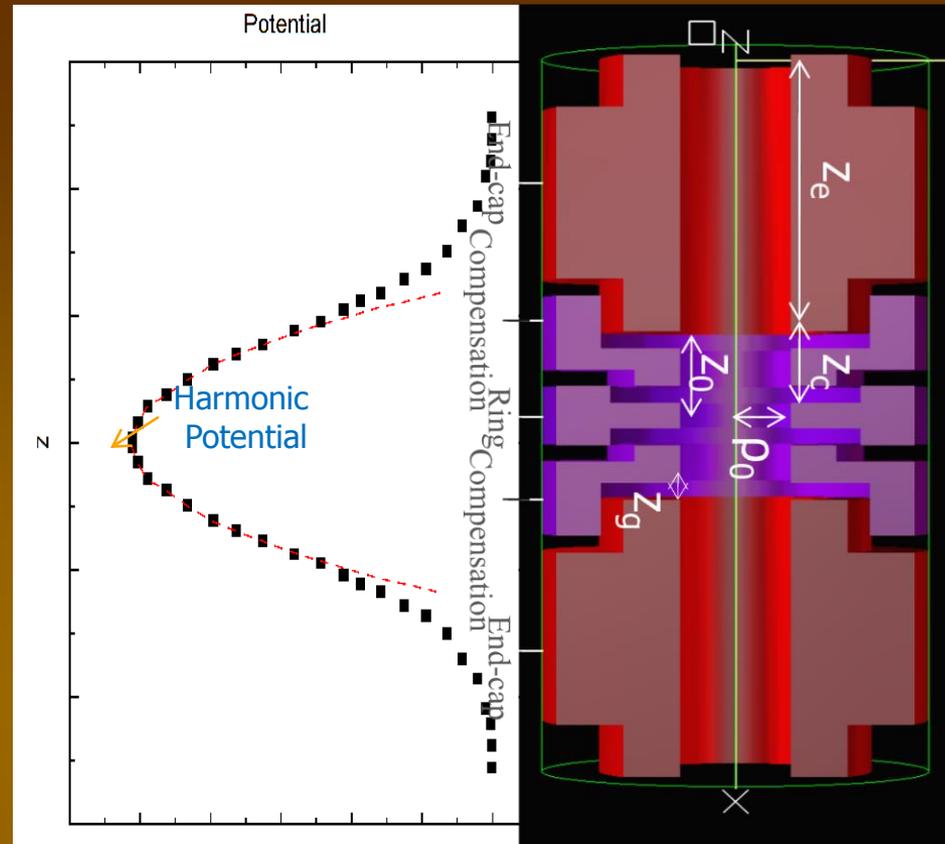
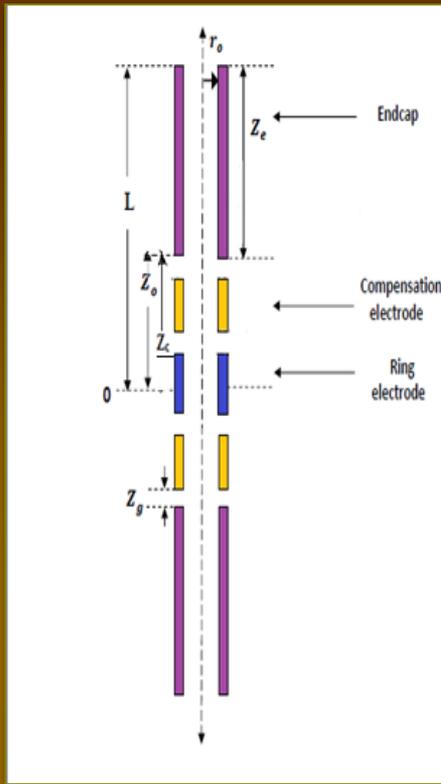
VEC TRAP

(A cryogenic Penning Trap facility)



*5 Tesla superconducting persistent mode magnet cryostat for Penning ion trap
Temporal stability ~1ppb/hr, A magnetic shielding circuit provides flux stabilization*

MAGNET COMMISSIONED



$r_o = 3.29mm$
 $Z_o = 3.04mm$
 $Z_c = 2.58mm$
 $Z_g = 0.6mm$
 $d = 2.707mm$

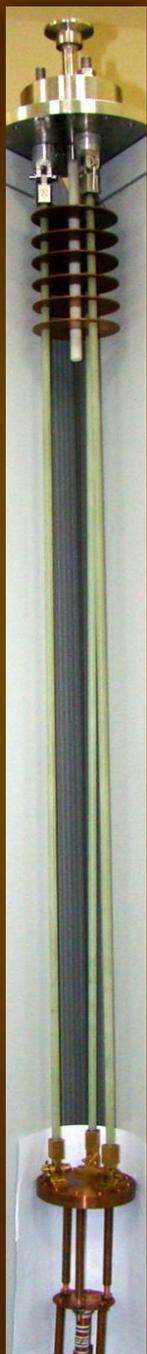
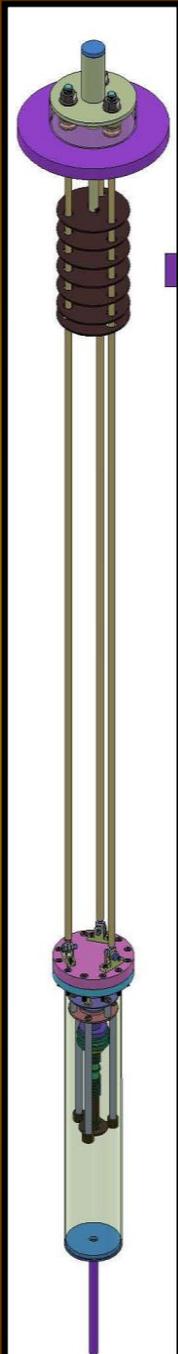
The most general solution to Laplace equation

$$V(r, \theta) = \frac{1}{2}V_0 \sum_{\substack{k=0 \\ \text{even}}}^{\infty} C_k \left(\frac{r}{d}\right)^k P_k(\cos \theta).$$

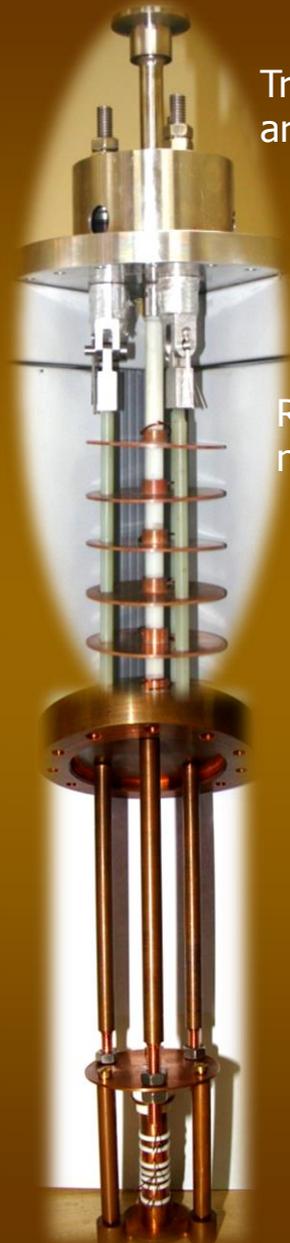
where $d^2 = ((r_o^2/2) + z_o^2)/2$

Dimensional (mm)		Potential parameter	
ρ_0	3.29	V_0	10
Z_0	3.04	V_c	4.9874
d	2.7068	C_0	0.57463
Z_r	0.92	C_2	0.65202
Z_c	1.38	C_4	1.17E-4
Z_e	10.00	C_6	0.0668
Z_g	0.60	C_8	-0.00934

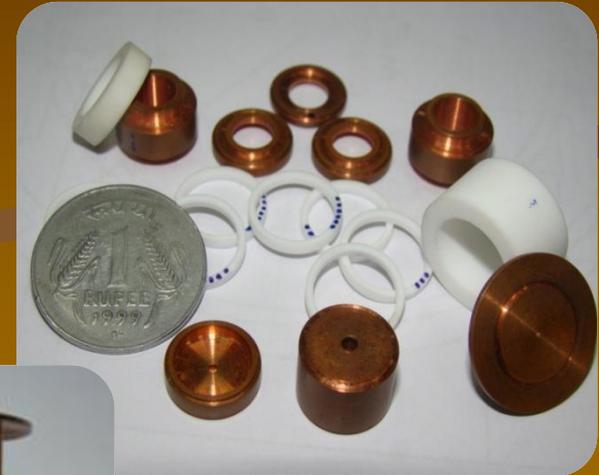
**TRAP ELECTRODES FABRICATED
AT VECC WORKSHOP
within 40 micron tolerance**



Trap positioning arrangement



Radiation baffle



OFHC PIN Laser Welded at RRCAT for connection



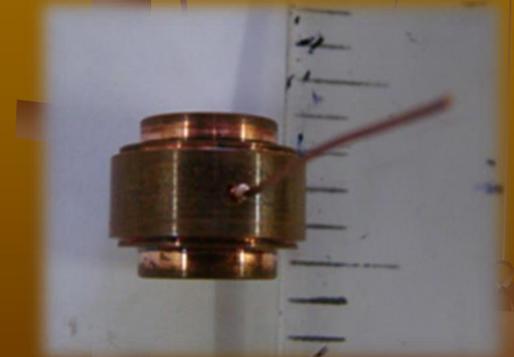
Axial frequency,

$$f_z = \frac{1}{2\pi} \sqrt{\frac{qU_{dc}}{md^2}} C_2 =$$

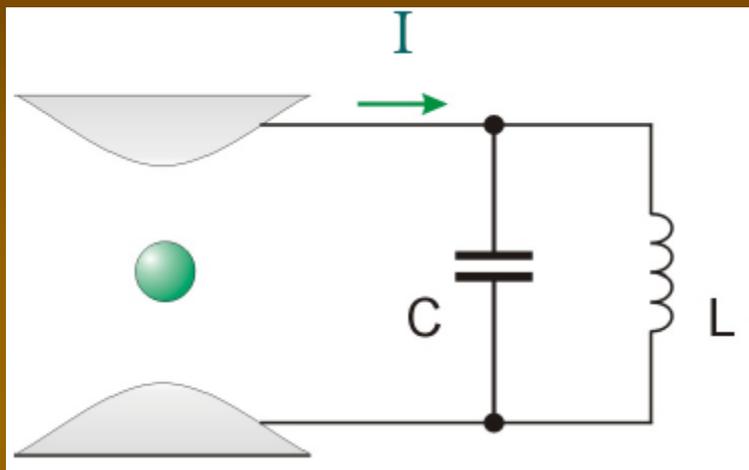
63 MHz

$U_{dc} = 10V$

$C_2 = 0.65202$



Resonant instead of broadband detection



measured signal:

$$U = Z \cdot I$$

$$Z_{LC} = Q_{LC} \cdot |Z_{C,parasitic}|$$

$$\omega_{ion} = \omega_{LC} = 1/\sqrt{LC}$$

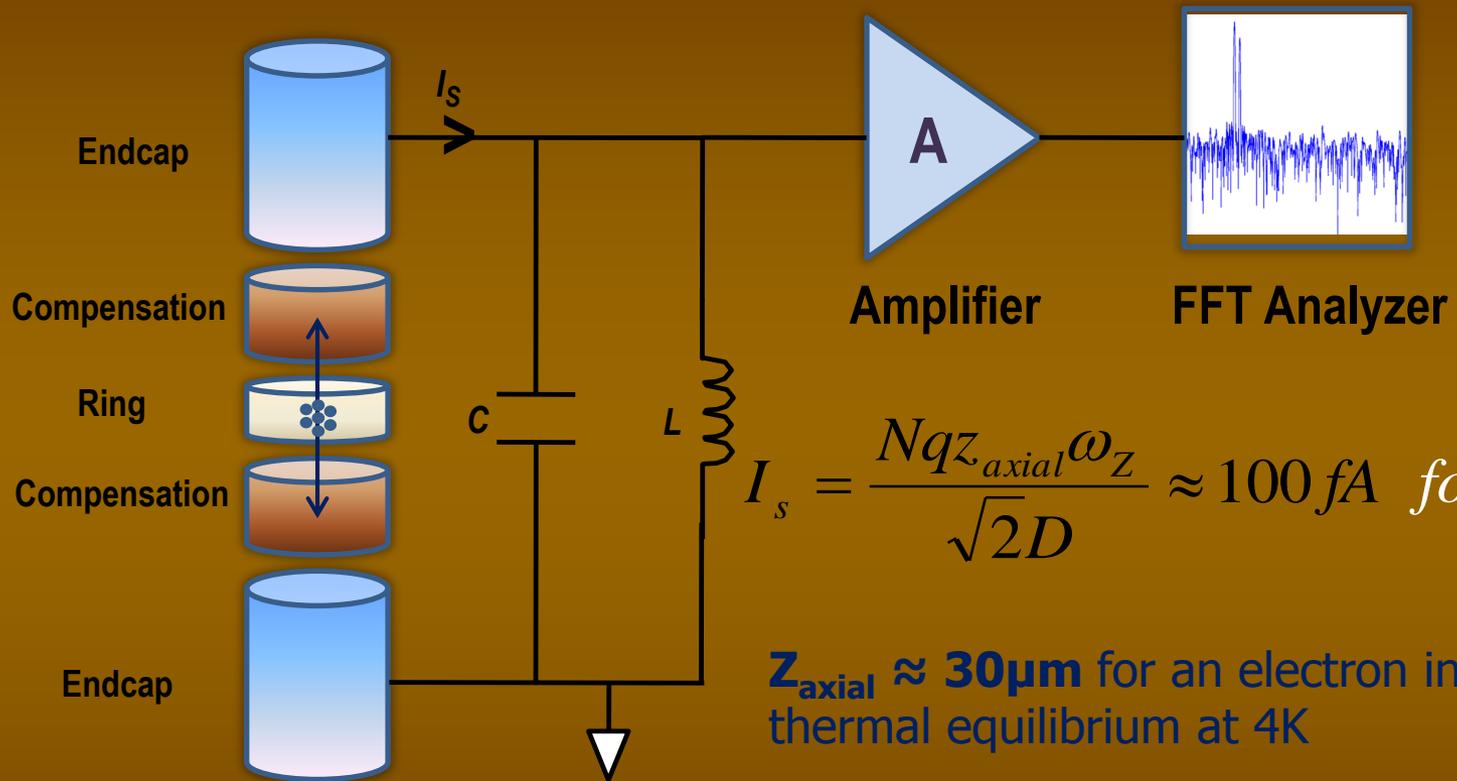
$$\frac{S}{N} = \frac{\sqrt{\pi}}{2} \frac{r_{ion}}{D} q \sqrt{\frac{\nu}{\Delta\nu}} \sqrt{\frac{Q}{kTC}}$$

enhancement factor

~100 (T=300K)

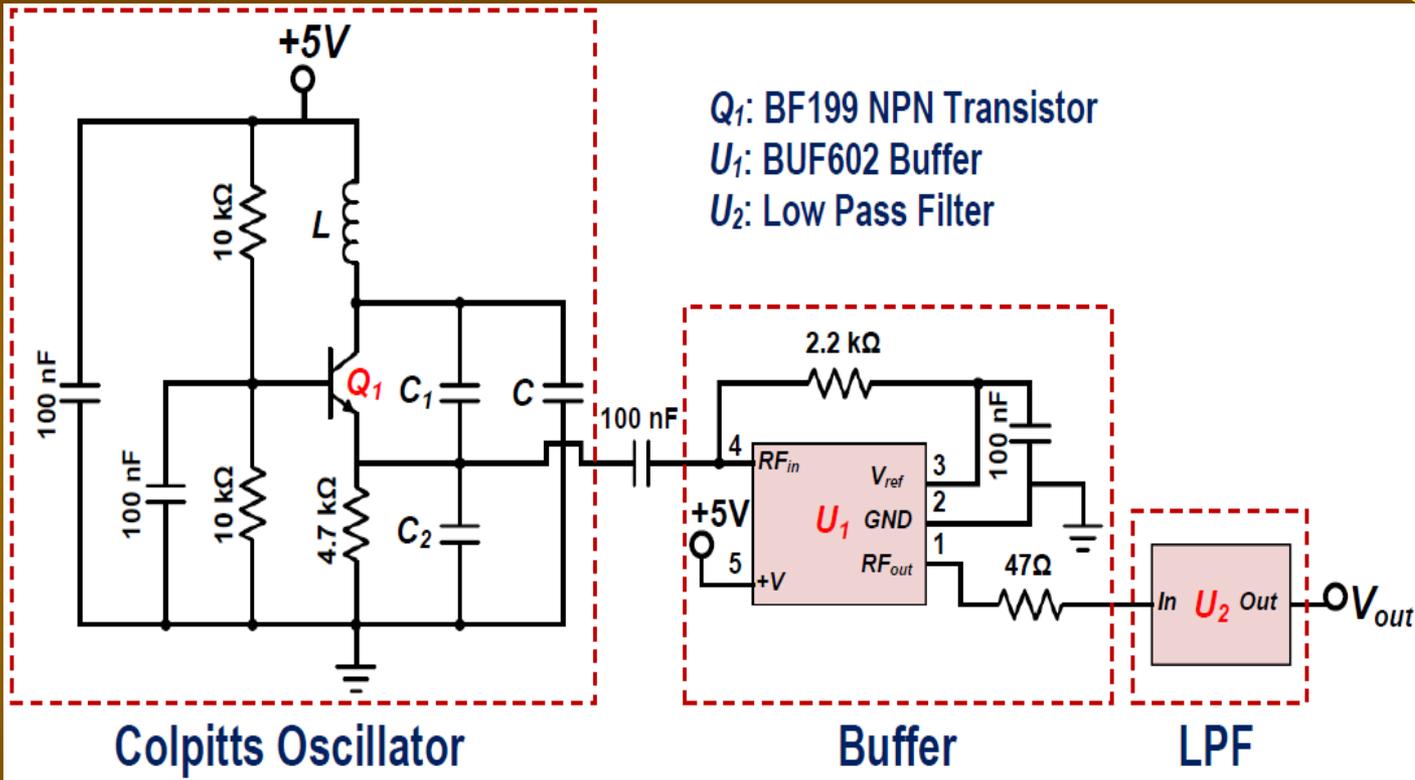
~2000 (T = 4K)

Signal Detection using resonant technique



$$f_Z = \frac{1}{2\pi} \sqrt{\frac{qU_{dc}}{md^2} C_2} = \mathbf{63 \text{ MHz}}$$

COLPITTS OSCILLATOR DESIGN



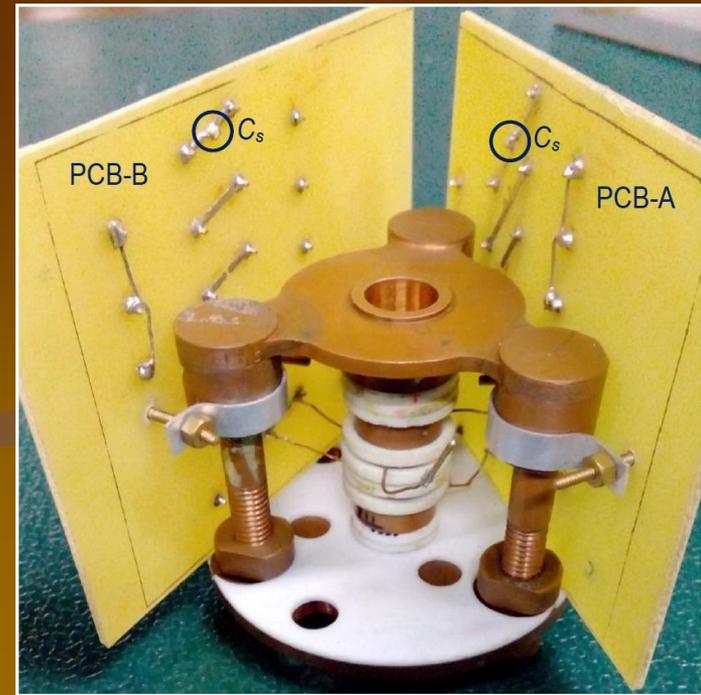
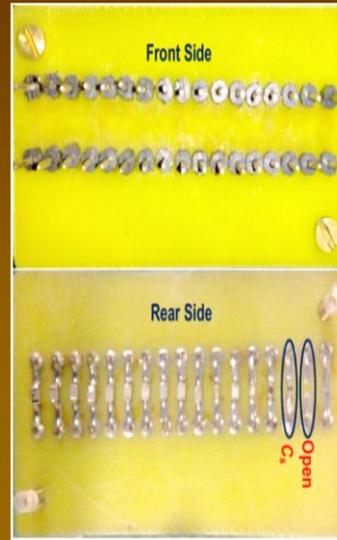
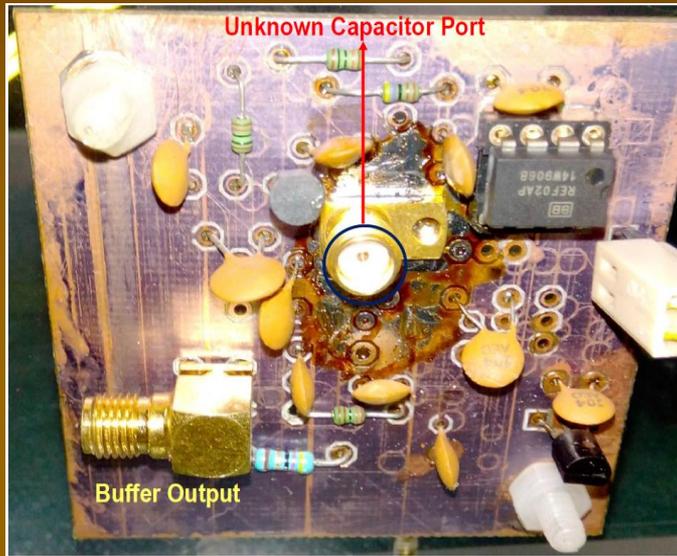
High frequency Osc
 Q1: Common base
 non inverting

Buffer stage
 Impedance
 High input
 Low output
 Improves
 Frequency stability

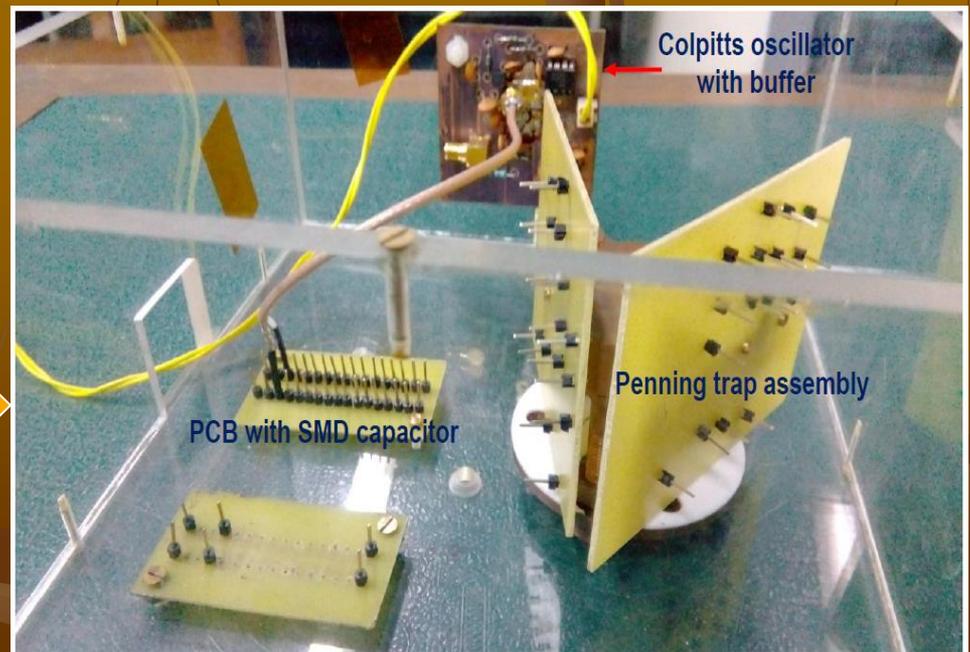
$$f_1 = \frac{1}{2\pi\sqrt{LC_{eq}}}, f_2 = \frac{1}{2\pi\sqrt{L(C_{eq} + C)}}$$

$$C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

COLPITTS OSCILATOR CIRCUIT FABRICATED



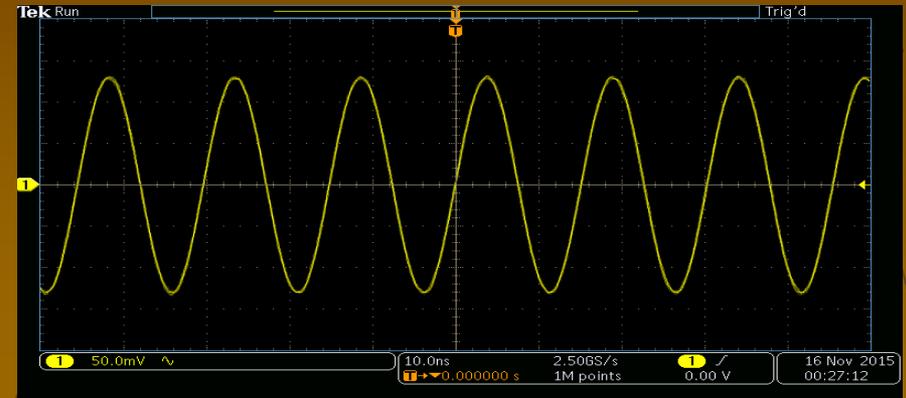
Trap Capacitance
Measurement set up



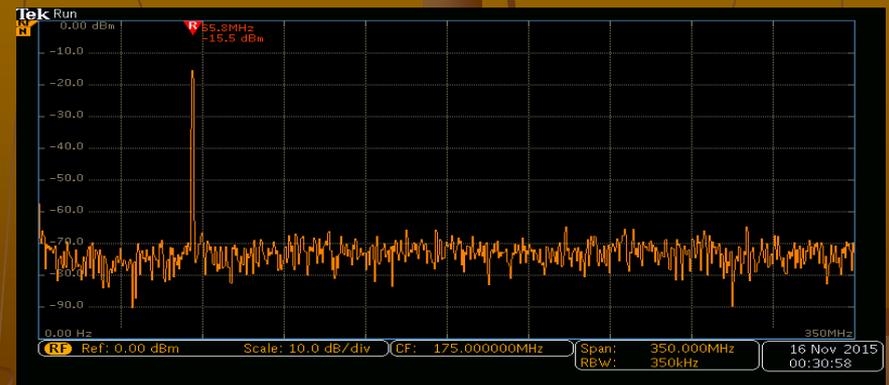
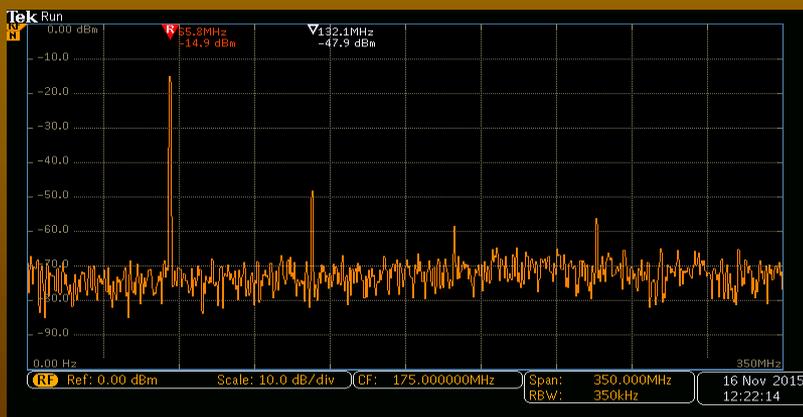
Colpitts oscillator output Buffer stage



Output signal with filter

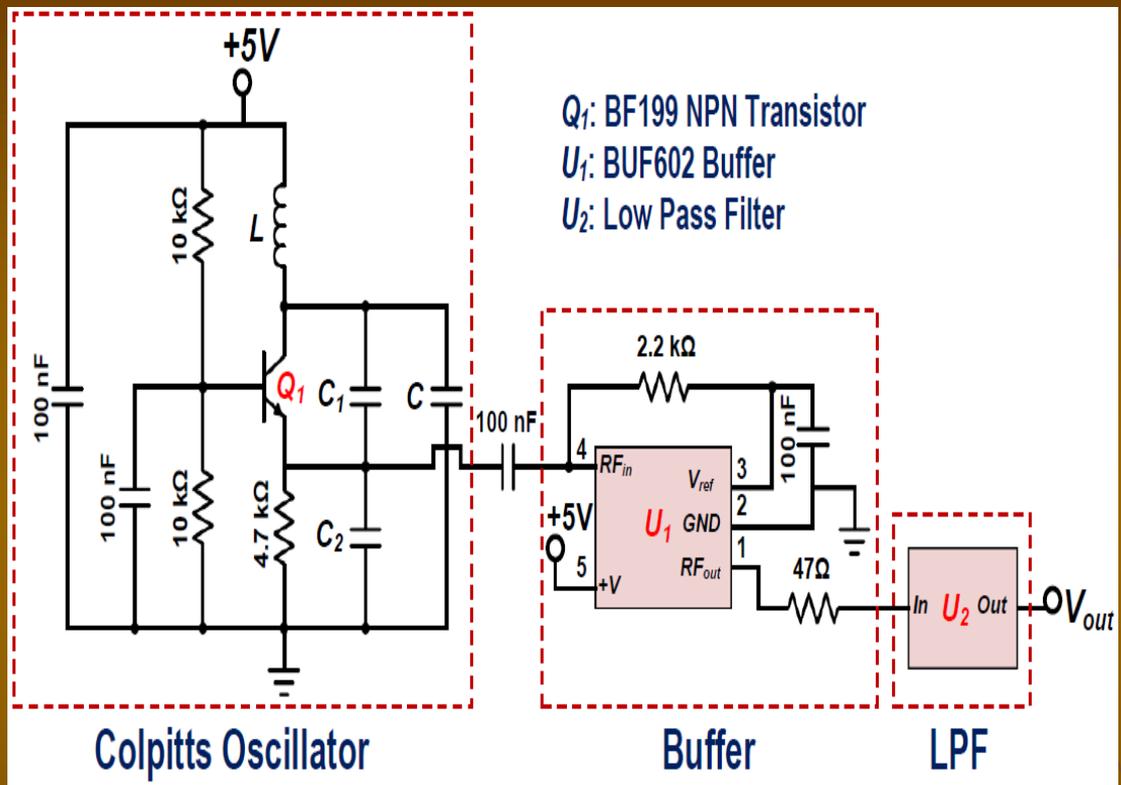


time domain output signal



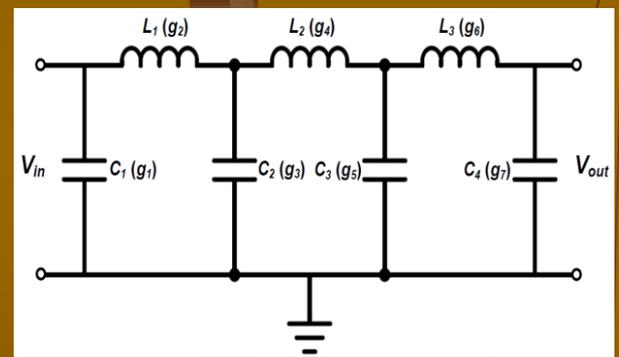
FFT of the output signal

Third stage of Colpitts oscillator : Low Pass Filter



- (a) Cut-off frequency (f_c): 75 MHz
- (b) Minimum stopband attenuation (L_{AS}): 30 dB
- (c) Minimum stopband attenuation frequency (f_s): 126 MHz

7th order filter



A Butterworth low pass filter
FR4 PCB

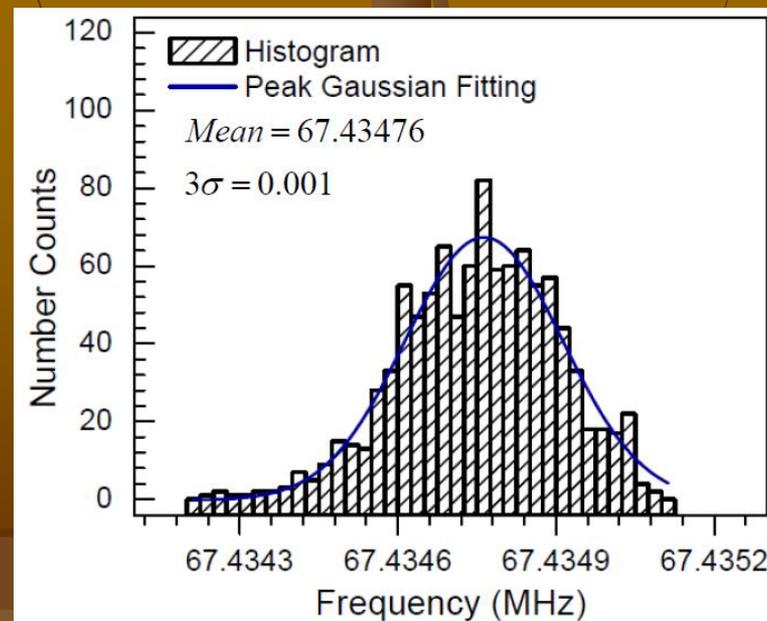
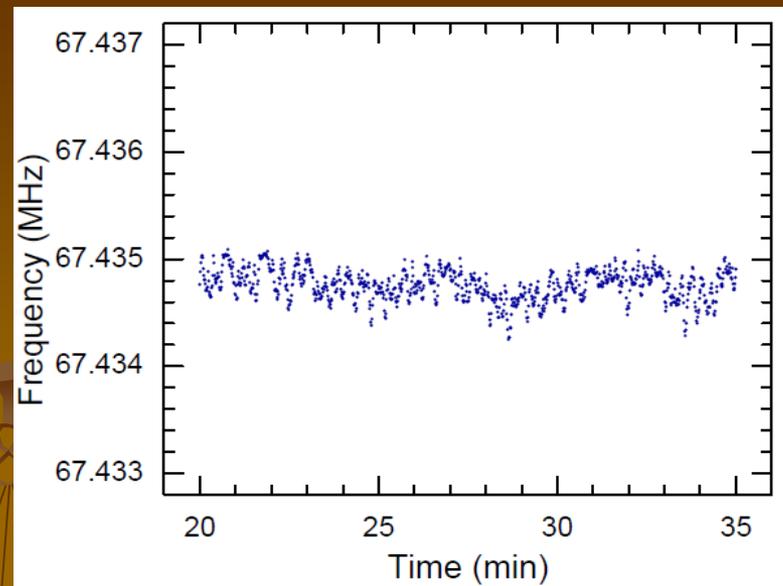
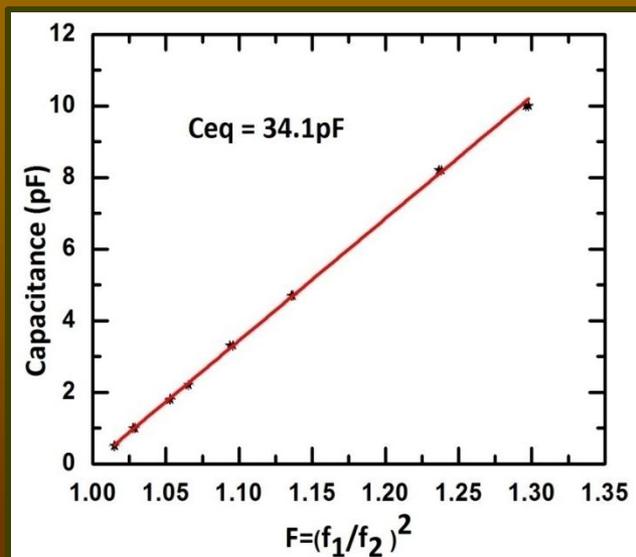


Capacitance measurement scheme

$$f_o = \frac{1}{2\pi\sqrt{L_{eff}C_{eff}}}$$

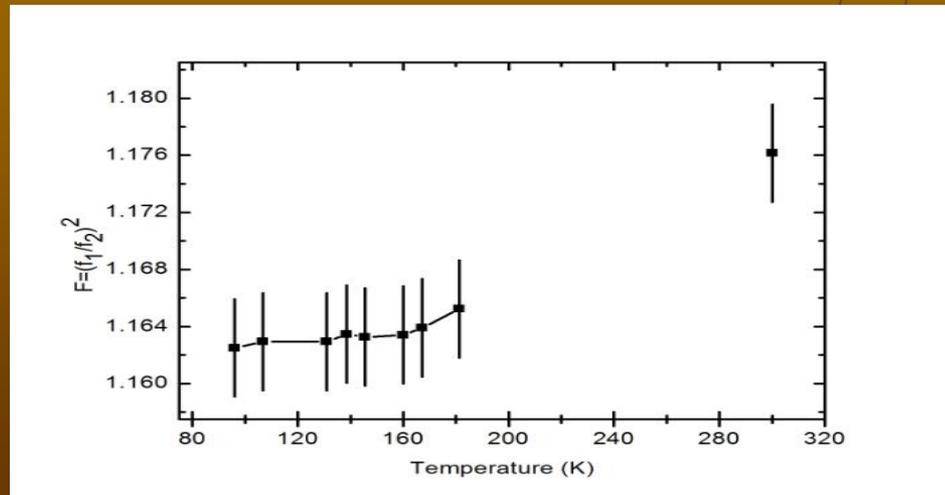
$$f_s = \frac{1}{2\pi\sqrt{L_{eff}(C_{eff} + C_s)}}$$

$$C_u = C_{eff} \left[\left(\frac{f_o}{f_u} \right)^2 - 1 \right]$$

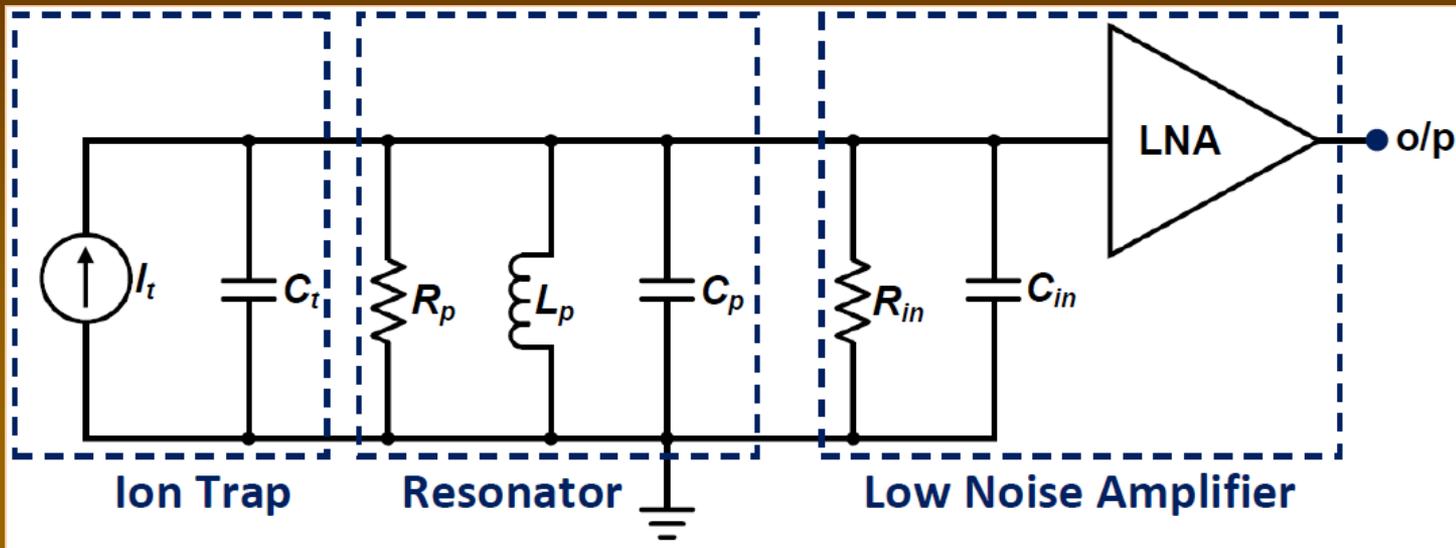


Capacitance measurement using Resonant technique

Capacitors (pF)	Measured (pF) (Helical Resonator)	Measured (pF) (Colpitts Oscillator)
0.5	0.494	0.474
1.0	1.018	0.96
3.3	3.28	3.39
Trap (UE-LE)	2.23	2.15
Trap (UC-R)	4	4



Design of a Helical Resonator with capacitive loading



- Capacitive loading contributed from trap, LNA and connecting wire is roughly estimated to be of the order of 12 to 15 pF.
- The resonator should be designed in such a way that it will resonate at a frequency range of (60-70) MHz after a capacitive loading of 15pF.

Design parameter of 160 MHz helical resonator

f_o (MHz)	C_e (pF)	C_l (pF)	f_l (MHz)
100	2.822	15	39.8
120	2.897	15	48.3
140	2.961	15	56.8
160	3.042	15	65.7
180	3.140	15	74.9

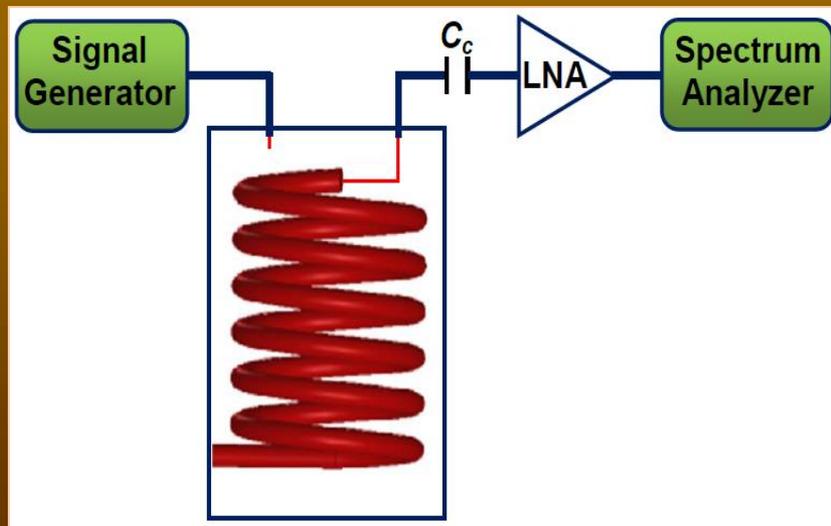
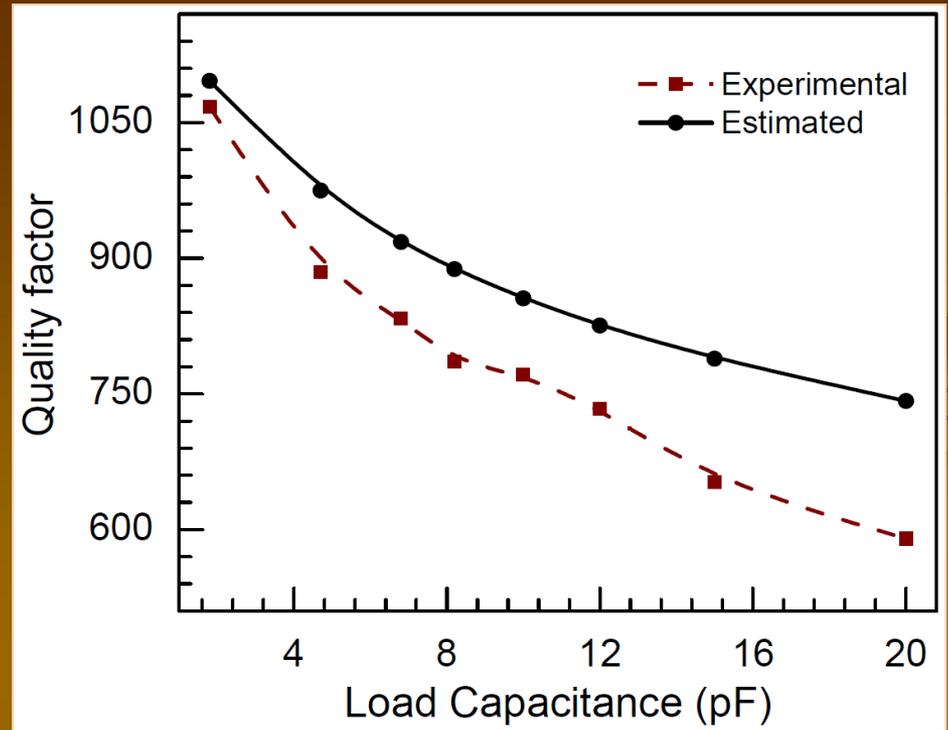
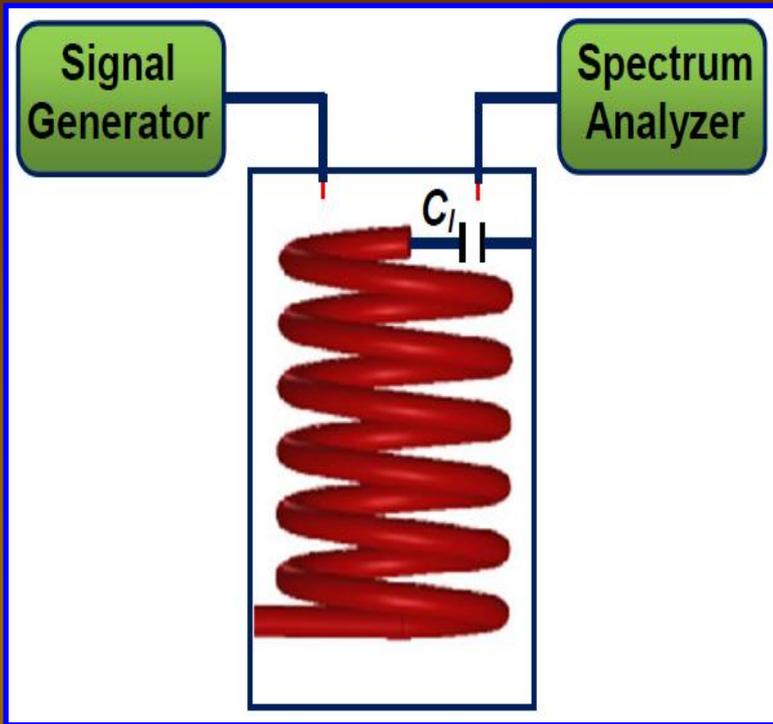
Design parameters	Values
Design frequency	160 MHz
Outer shield diameter	50 mm
Helix core diameter	27.52 mm
Helix length	41.28 mm
Outer shield height	66.3 mm
Number of turns	6
Helix wire diameter	3 mm

Helical resonator is designed for 160 MHz, we can expect a loaded resonant frequency within (60-70) MHz with a capacitive loading of 15 pF.

High Frequency Structure Simulation (HFSS)

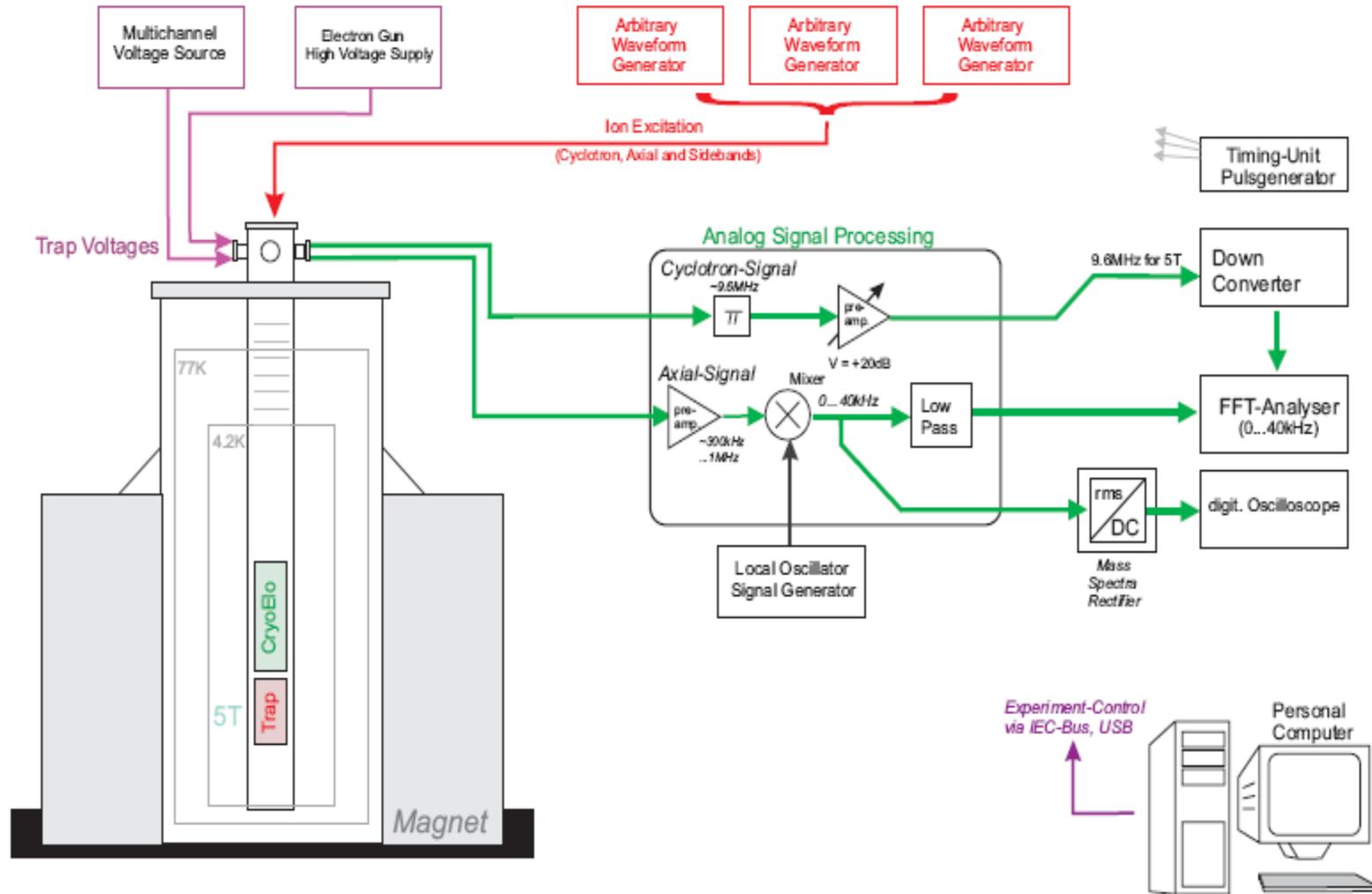


Fabricated helical resonator
 $f_o = 155.11$ MHz, $Q_o = 1231$



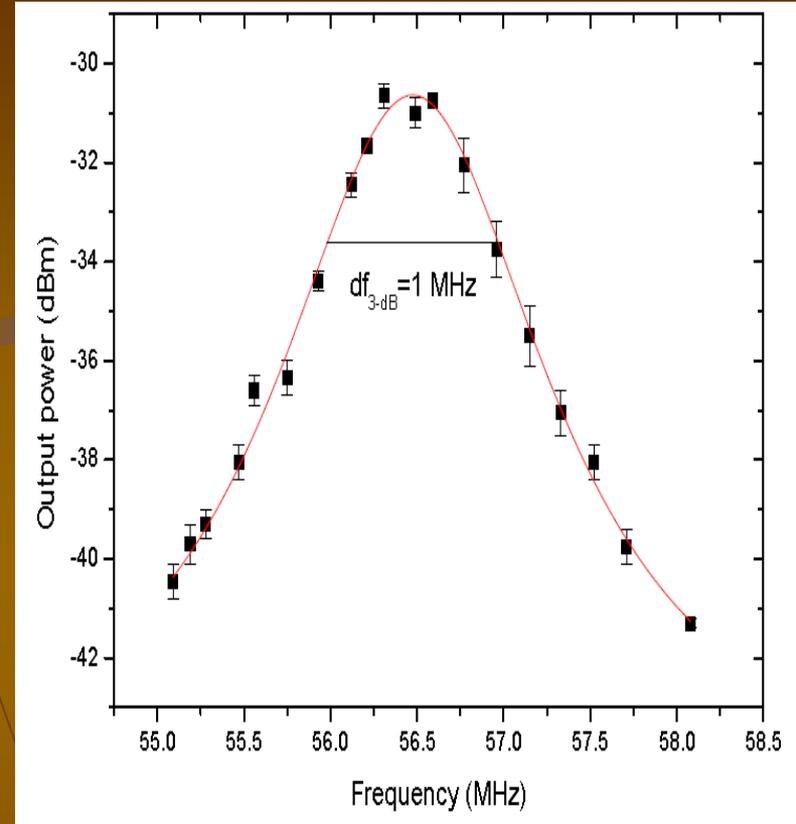
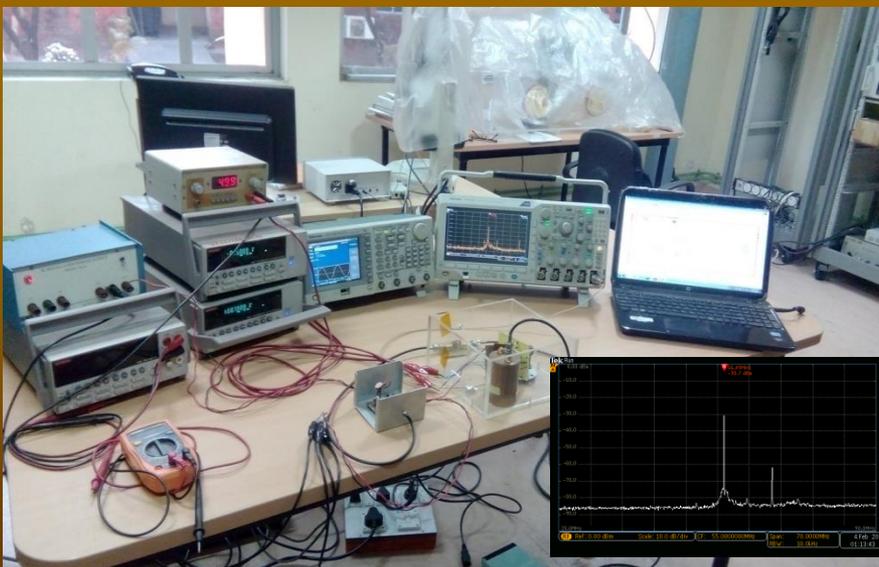
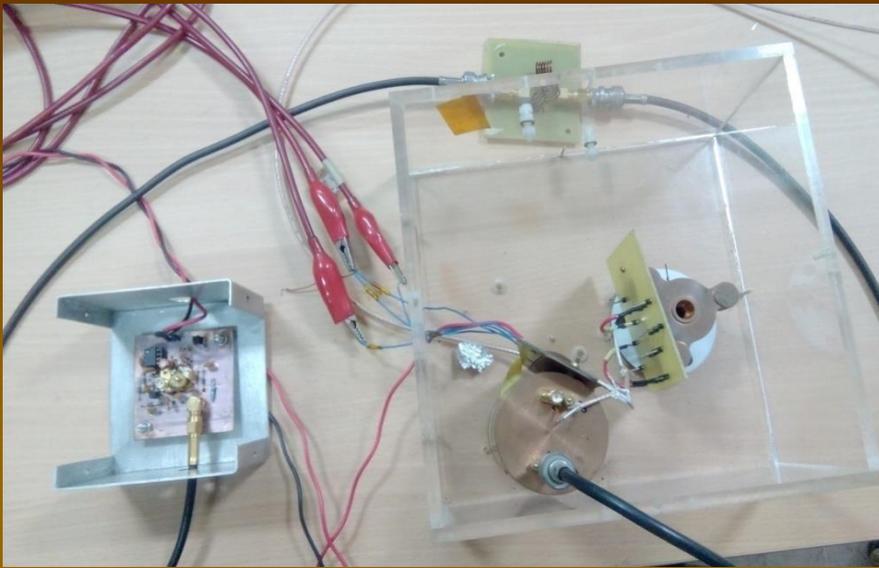
With a coupling capacitor of 1.8 pF, a quality factor of 323 is obtained at a resonant frequency of 61.45 MHz.

Non destructive Detection of a cloud of Li/Be ions in a VEC Cryogenic Penning trap



$$Q = f_0 / \Delta f$$

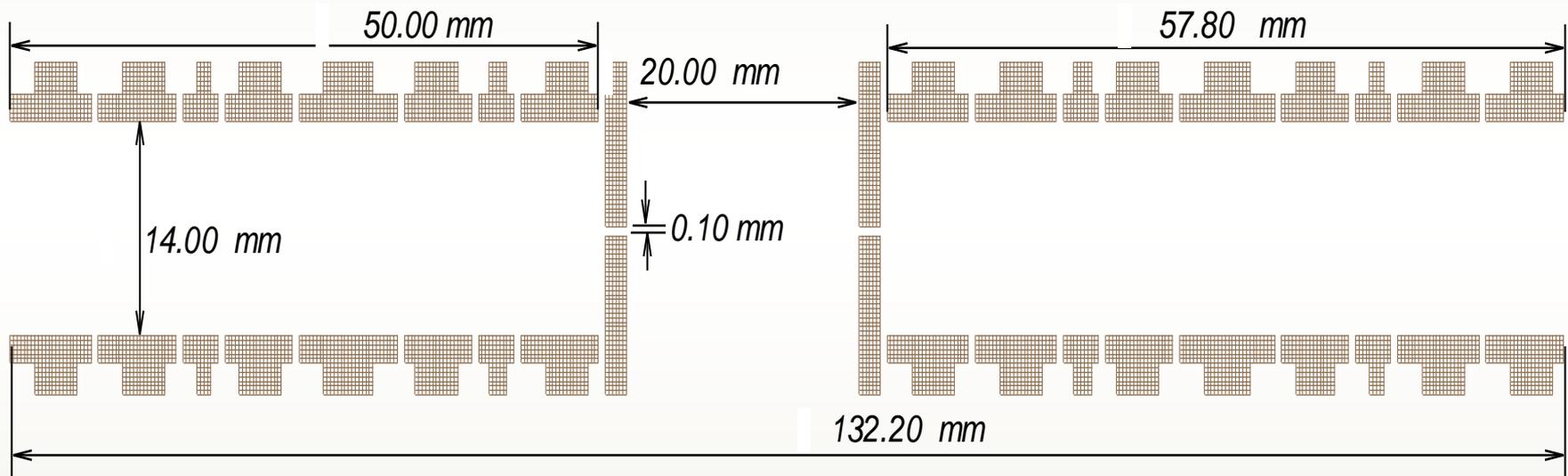
DETECTION SET UP FOR TRAPPED IONS



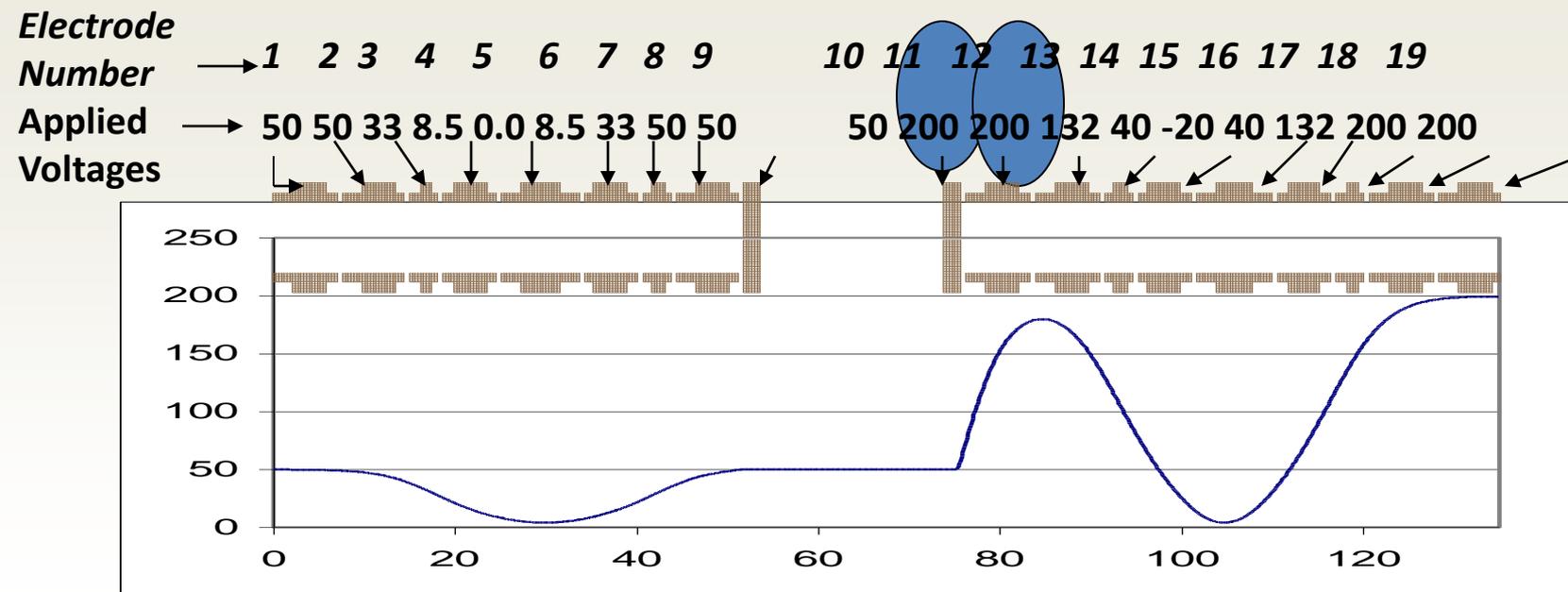
Resonant frequency (f_0)	3-dB bandwidth (Δf)	Quality factor (Q)
56.47 MHz	1 MHz	56.47

PROPOSAL AT FAIR

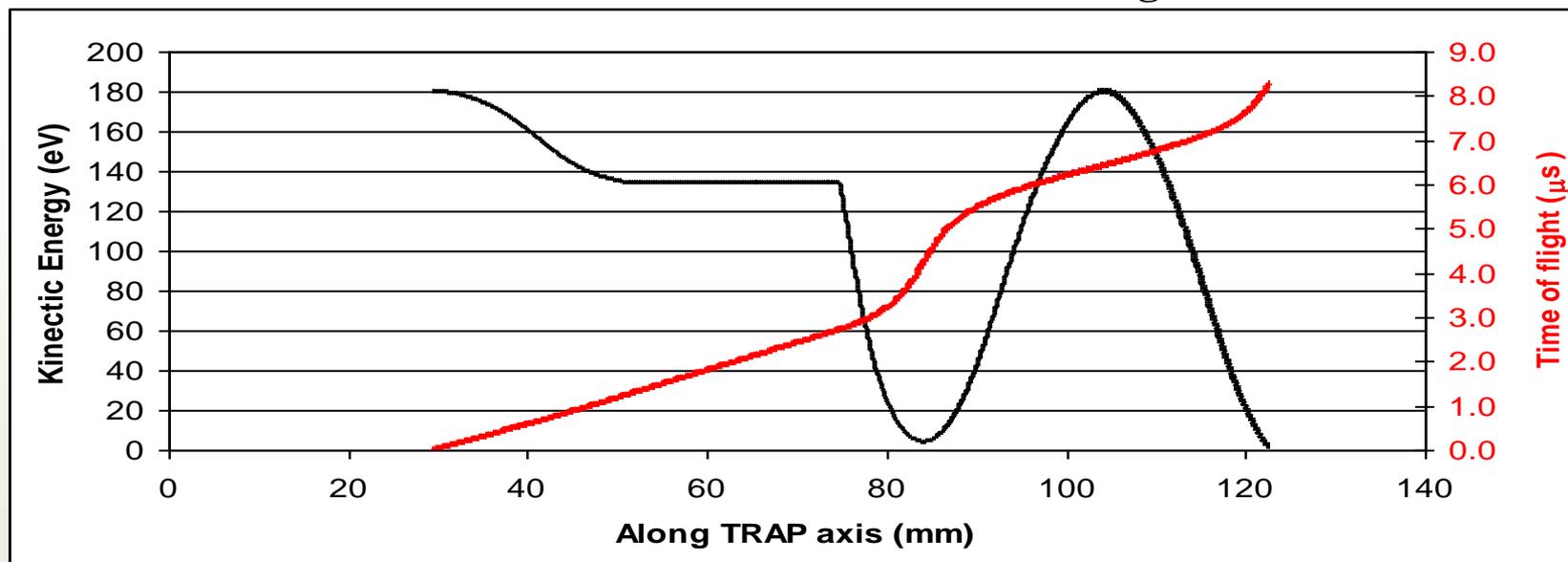
High precision Q-value measurement



19 Electrode TRAP Assembly



Simulation Result for Ion of mass 100 amu recoiling with with 180 eV



COLLABORATORS
DR AMLAN RAY
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Contributors

*Prof. Kumardeb Banerjee
(Jadavpur Unniversity)*

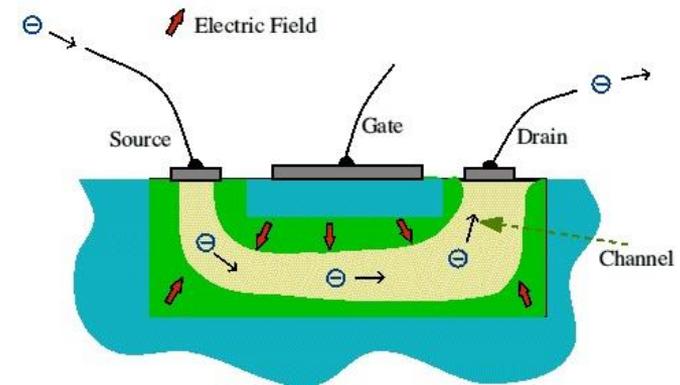
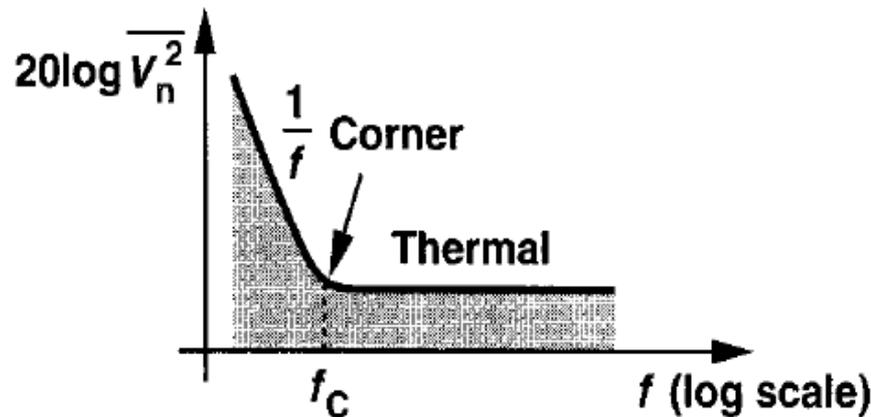
Ashif Reza, DGFS-PhD fellow

Dr Pushpa Rao (BARC)

Thank you

Noise Sources in FET

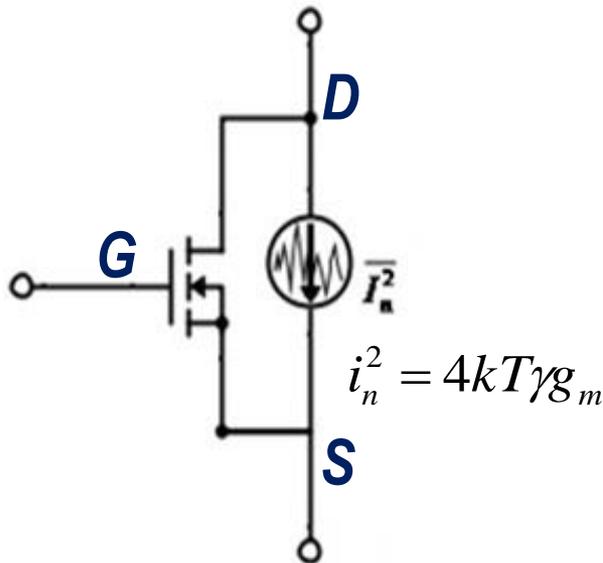
- Frequency independent thermal noise in the drain-source channel
- Gate noise induced by the channel thermal noise via Gate-Drain capacitance
- Flicker noise ($1/f$ noise) due to the fluctuations in generation and recombination rate of charge carriers in the depletion region of the FET
- Shot noise due to the leakage current flowing from gate to channel



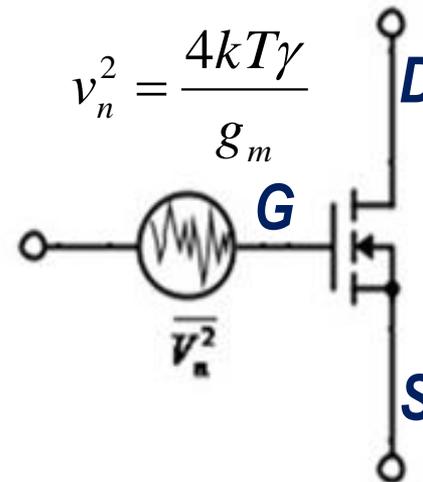
For frequencies in excess of 10 MHz the channel thermal noise is the dominant noise contribution.

Channel Thermal Noise in FET

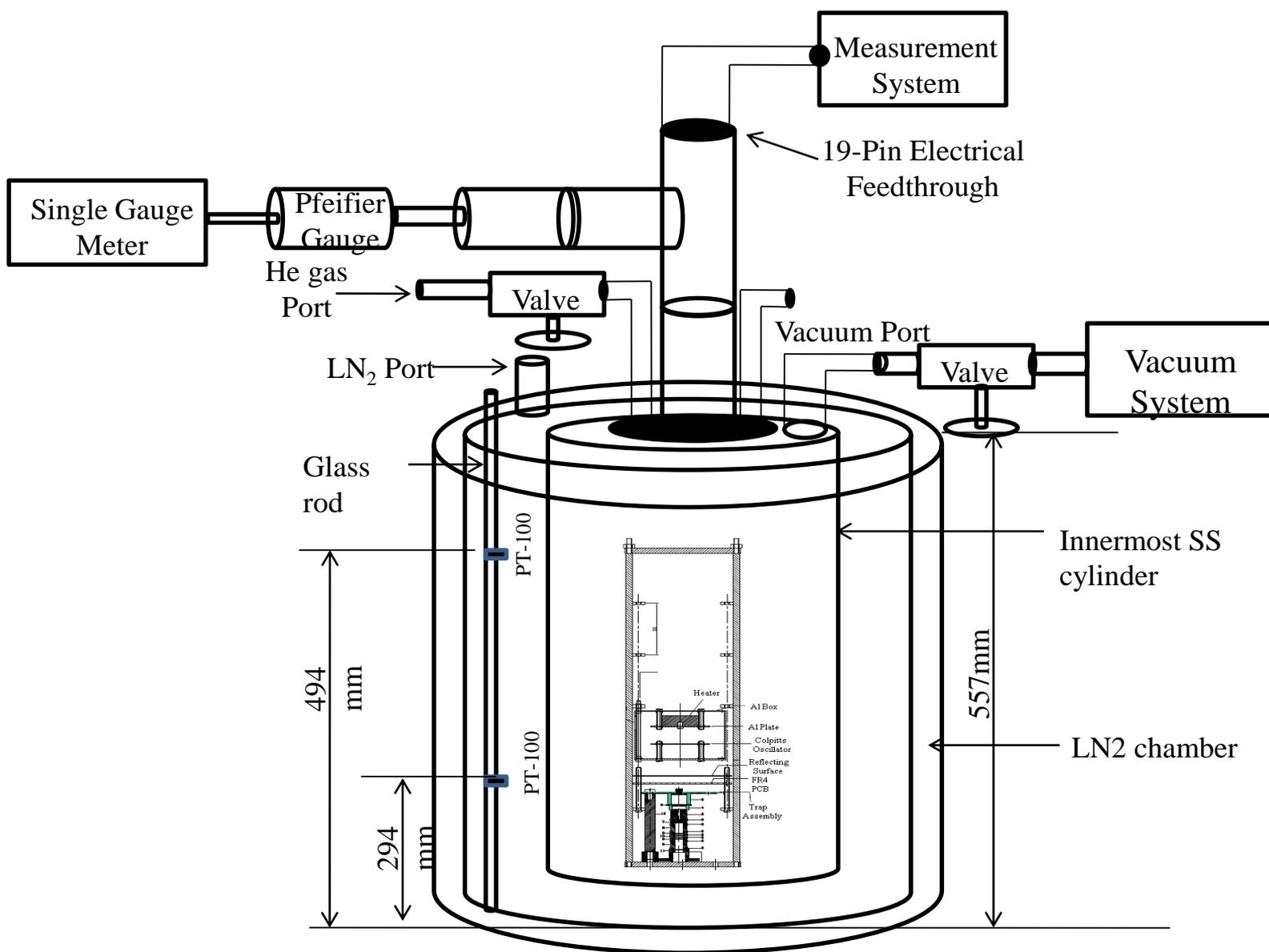
- In a FET, the conducting drain-source channel has an effective resistance that causes thermal noise



FET current noise model



FET voltage noise model



The setup holding assembly within LN₂ cryostat

Helical Resonator Simulation

High Frequency Structure Simulation (HFSS)

- **A high performance full-wave electromagnetic field simulator**
- **Employs finite element method solver for electromagnetic structures**
- **Solves a wide range of microwave, RF and high speed digital applications**
- **Calculate parameters of a geometrical structure such as S-parameters, resonant frequency and quality factor etc.**
- **Geometrical model is automatically divided into an efficient and accurate tetrahedral mesh for the simulation**