

$\psi(2S)$ production at energies available at LHC

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Outline

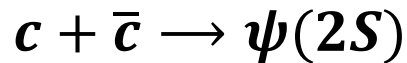
1. Introduce the time-dependent Schrodinger equation
2. Heavy quark potential at finite temperature
3. **$c\bar{c}$ dipole evolution in the Static medium**
 - 1). Testing codes
 - 2). A $c\bar{c}$ dipole evolution in the Static medium
 - 3). $R_{AA}(2S)/R_{AA}(1S)$ evolution in the Static medium
4. **Applying to Heavy ion collisions**
 - 1). Hydro profile: important for the transitions between Eigenstates
 - 2). The evolution of $c\bar{c}$ dipoles in heavy ion collisions
5. Summary

Experimental data

Strong enhancement of prompt $\psi(2S)$ production at middle p_T bin: $3 < p_T < 30$ GeV/c

X. Du, R. Rapp, 15'

(uncorrelated $c\bar{c}$)

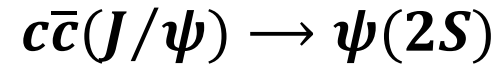


regeneration (Coalescence)

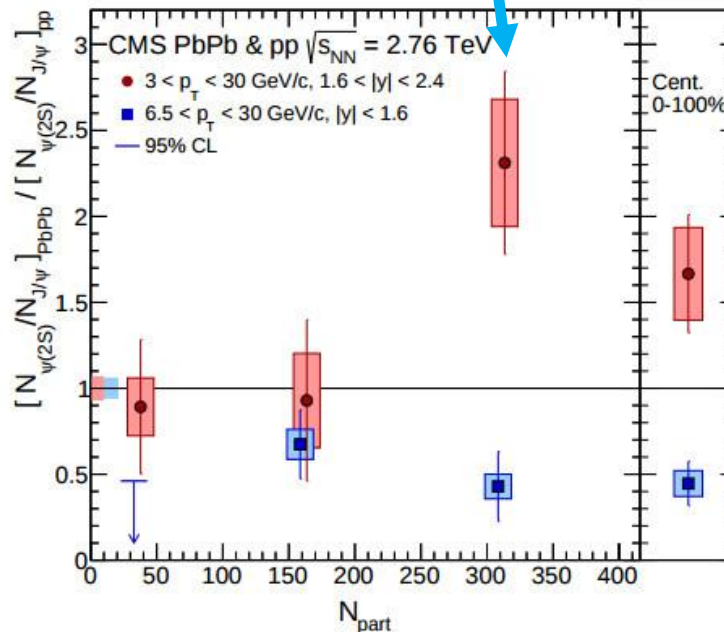
(Explain the data well)

?

(correlated $c\bar{c}$)



Formation process



$R_{AA}(2S)/R_{AA}(1S)$

CMS, PRL113 (2014)
no.26, 262301

Time-dependent Schrodinger equation

Radial Schrodinger equation:

$$i\hbar \frac{\partial}{\partial t} \psi(r, t) = \left[-\frac{\hbar^2}{2m_\mu} \nabla^2 + V(r, t) \right] \psi(r, t)$$

r : relative distance between c and \bar{c}

$m_\mu = m_c/2$: scaling mass

$$\frac{\psi(r, t)}{r} = \sum_m c_m(t) e^{-iE_m t} R_{mS}(r)$$

Wavefunction of eigenstates:

$$\Psi_{klm}(\vec{r}) = R_{kl}(r) Y_{lm}(\theta, \varphi)$$

Numerical form:

$$i \frac{\psi_j^{n+1} - \psi_j^n}{\Delta t} = \frac{1}{2} \left[-\frac{1}{2m_\mu} \frac{\psi_{j+1}^n - 2\psi_j^n + \psi_{j-1}^n}{(\Delta x)^2} + V_j^n \psi_j^n \right. \\ \left. - \frac{1}{2m_\mu} \frac{\psi_{j+1}^{n+1} - 2\psi_j^{n+1} + \psi_{j-1}^{n+1}}{(\Delta x)^2} + V_j^{n+1} \psi_j^{n+1} \right]$$

n : time point;

j : coordinate point;

$$t = t_0 + n \cdot \Delta t$$

$$r = r_0 + j \cdot \Delta r$$

Δt : step of the time

Δr : step of the radius

Time-dependent Schrodinger equation

Simplify the numerical form as:

$$\begin{pmatrix} \mathbf{T}_{0,0}^{n+1} & \mathbf{T}_{0,1}^{n+1} & 0 & 0 & \dots \\ \mathbf{T}_{1,0}^{n+1} & \mathbf{T}_{1,1}^{n+1} & \mathbf{T}_{1,2}^{n+1} & 0 & \dots \\ 0 & \mathbf{T}_{2,1}^{n+1} & \mathbf{T}_{2,2}^{n+1} & \mathbf{T}_{2,3}^{n+1} & \dots \\ \dots & \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots \end{pmatrix} \begin{pmatrix} \psi_0^{n+1} \\ \psi_1^{n+1} \\ \psi_2^{n+1} \\ \psi_3^{n+1} \\ \dots \end{pmatrix} = \begin{pmatrix} \Gamma_0^n \\ \Gamma_1^n \\ \Gamma_2^n \\ \Gamma_3^n \\ \dots \end{pmatrix}$$

Matrix elements:

$$\begin{aligned} \mathbf{T}_{j,j}^{n+1} &= 2 + 2a + bV_j^{n+1} & a &= i \Delta t / (2m_\mu (\Delta r)^2) \\ \mathbf{T}_{j,j+1}^{n+1} &= \mathbf{T}_{j+1,j}^{n+1} = -a & b &= i \Delta t \end{aligned}$$

Coefficient of each eigenstate:

$$c_{mS}(t) = \langle R_{mS}(r) | \frac{\psi(r,t)}{r} \rangle = \int R_{mS}(r) \psi(r,t) \cdot r dr$$

At each time step, the fraction of mS (m=0,1,..) eigenstate in a $c\bar{c}$ dipole = $|c_{mS}(t)|^2$

Initialization of $c\bar{c}$ wavefunction

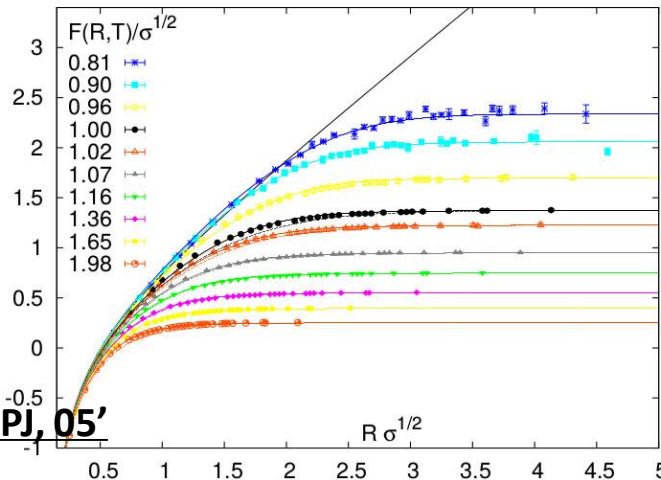
1) Gaussian wave: $\phi_0(r) = A e^{-\frac{r^2}{2\sigma_0^2}}$ $\int dr \cdot r^2 |\phi_0(r)|^2 = 1$

fixed by pp data

$$A = \frac{2}{\pi^{1/4} \sigma_0^{3/2}}$$

2) Heavy quark potential :

Real part:
(Lattice)



S.Digal, et al, EPJ, 05'

imaginary part (HTL):

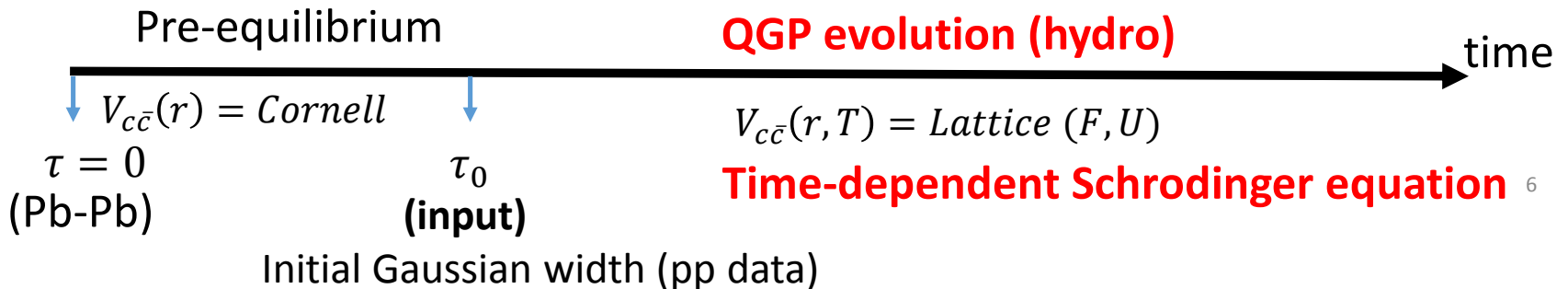
$$\text{Im}V(r) = -\frac{g^2 C_F T}{4\pi} \tilde{f}(\hat{r})$$

$$\tilde{f}(\hat{r}) = 2 \int_0^\infty dz \frac{z}{(z^2 + 1)^2} \left[1 - \frac{\sin(z\hat{r})}{z\hat{r}} \right]$$

M. Strickland, PRD, 09'

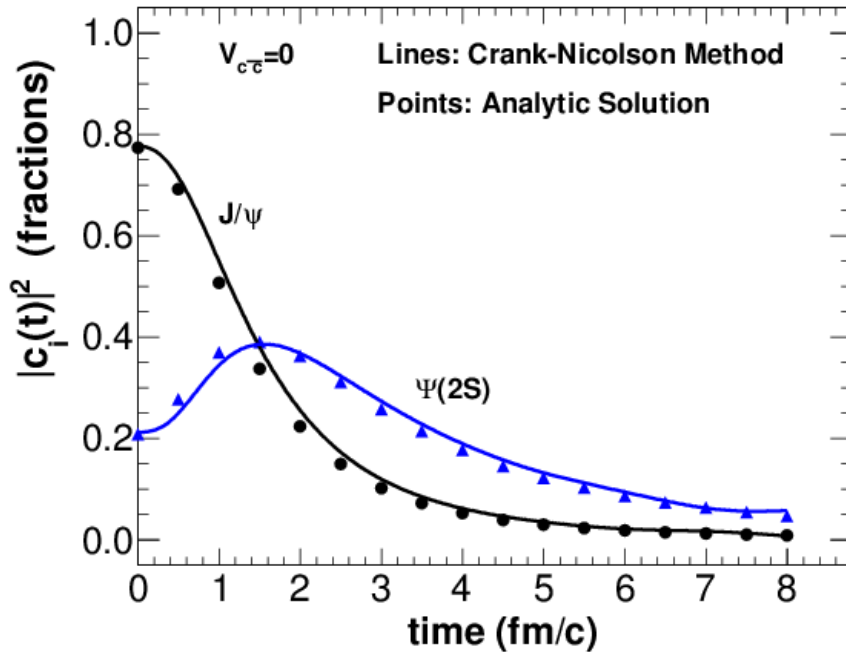
$$V = F$$

$$V = U = F + T(-\partial F / \partial T)$$

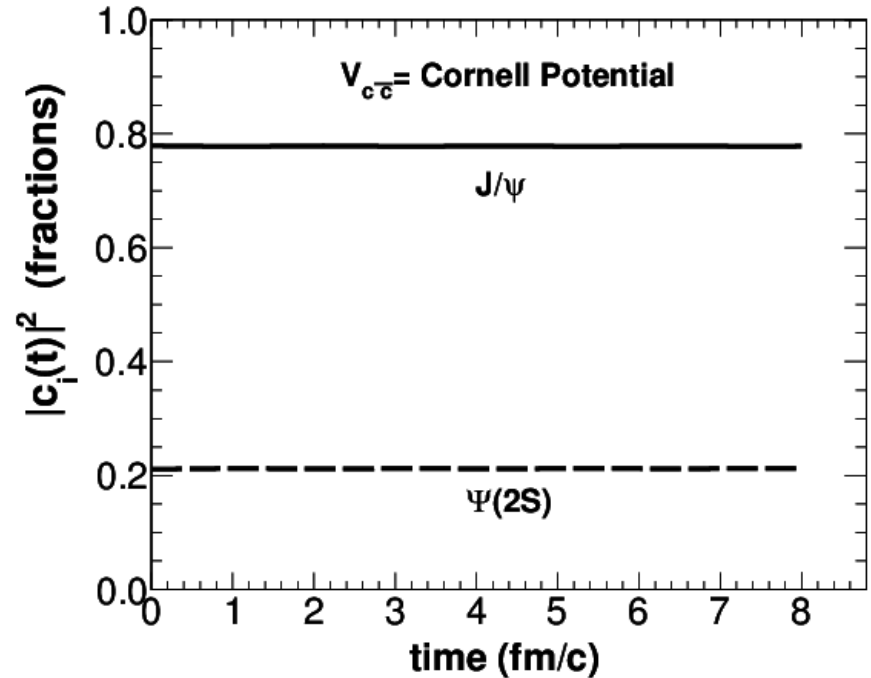


Testing codes

Evolutions of one $c\bar{c}$ with different potential



$$V_{c\bar{c}}(r) = 0$$

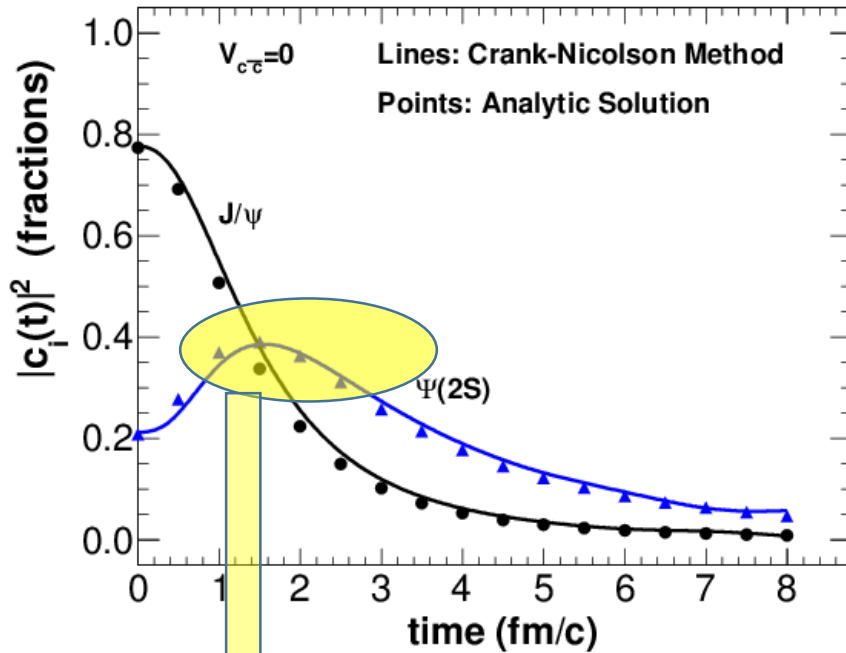


$$V_{c\bar{c}}(r) = \text{Cornell Potential}$$

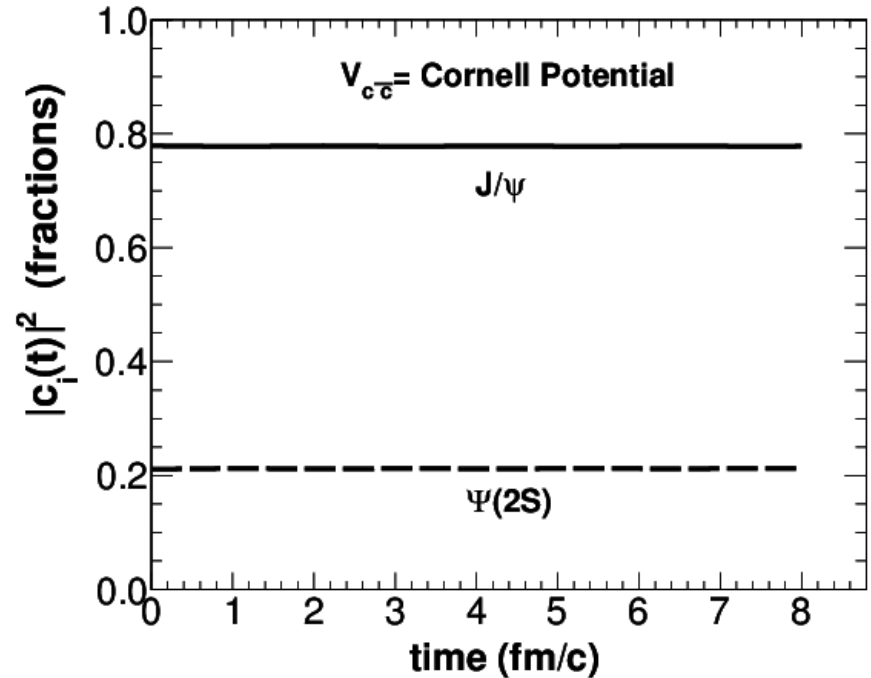
Numerical evolutions are reliable.

Testing codes

Evolutions of one $c\bar{c}$ with different potential



$$V_{c\bar{c}}(r) = 0$$



$$V_{c\bar{c}}(r) = \text{Cornell Potential}$$

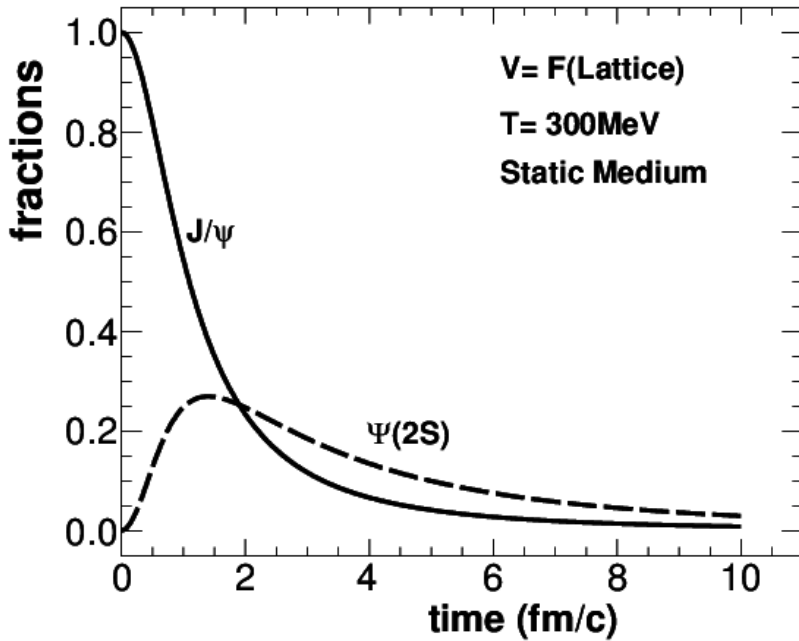
With weak potential, the $c\bar{c}$ dipole becomes a loosely bound dipole, its wavefunction expands outside.

→ the overlap between $\psi_{c\bar{c}}(r, t)$ and $\Psi(2S)$ increase at first, then decrease

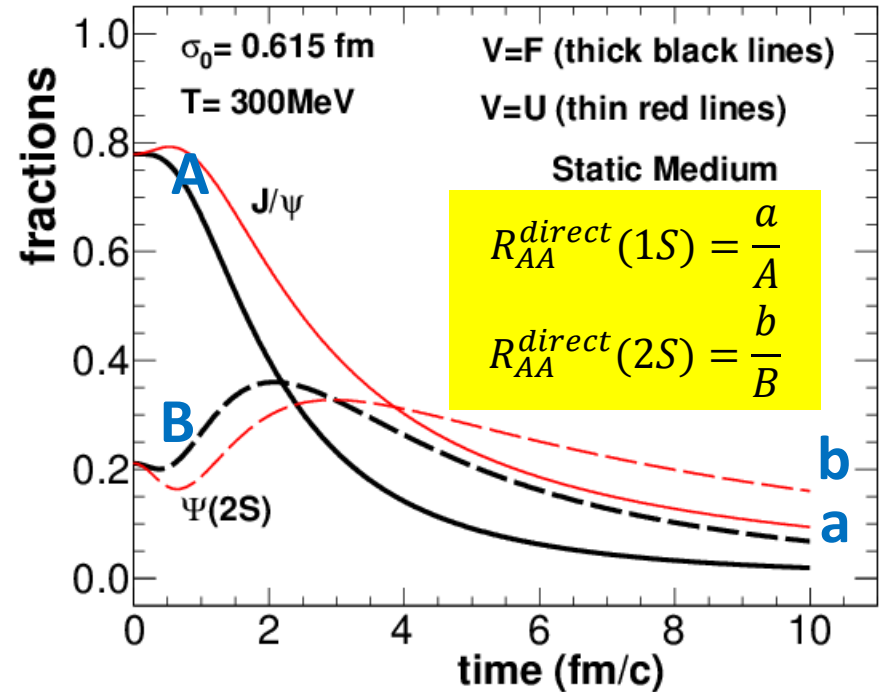
This behavior depends on the initial shape of the $c\bar{c}$ dipole

Evolutions of $c\bar{c}$ in the Static Medium

Prompt yield: direct yield(60%) + decay from excited states(1P:30%, 2S:10%)



J/ψ survival probability



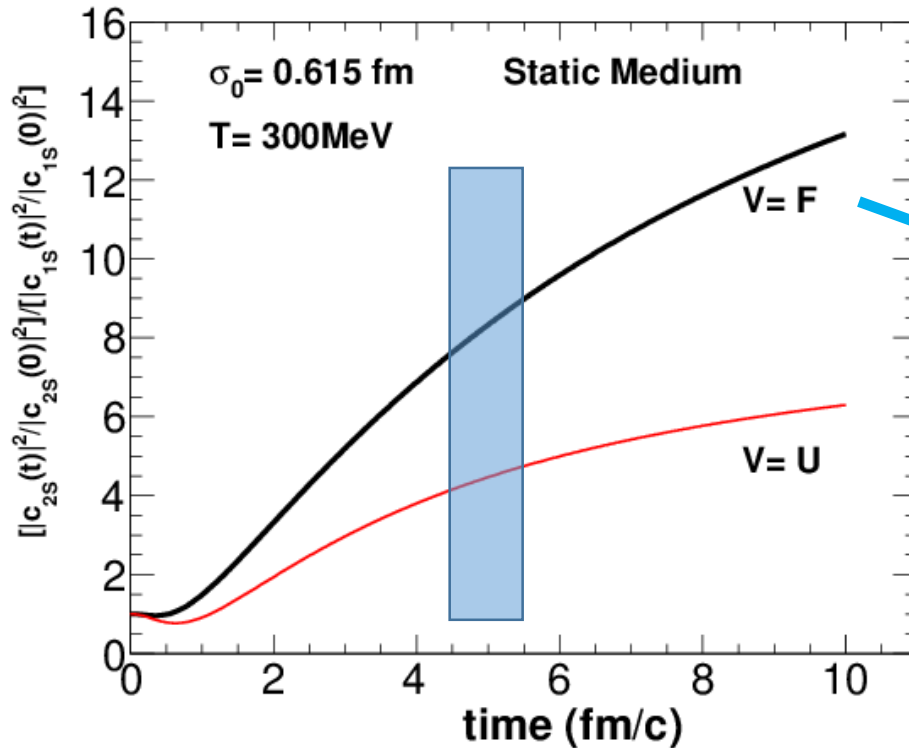
Fit the ratio of charmonium yields in pp collisions:

$$N_{2S}^{direct} / N_{1S}^{direct} = 0.6 / (0.1 / f^{2S \rightarrow 1S})$$

Initial Gaussian width $\longrightarrow \sigma_0 = 0.615 \text{ fm}$

Evolutions of $c\bar{c}$ in the Static Medium

Double ratio in the static medium, with Lattice potential.



$$\frac{R_{AA}^{direct}(2S)}{R_{AA}^{direct}(1S)}$$

- With weaker potential, the wavefunction of $c\bar{c}$ dipole expand outside more easily.
- Color screening effect enhance the RAA of 2S and the double ratio

Considering the size of QGP, and the velocity of $c\bar{c}$ dipoles, most of $c\bar{c}$ dipoles can move out of QGP at $\tau \sim 5 \text{ fm}/c$

Stay longer in QGP → Smaller RAA of 1S, Larger double ratio (2S/1S)

Generating $c\bar{c}$ dipoles in Pb-Pb

1. Generating $c\bar{c}$ dipoles in momentum space,

Assuming that the momentum distribution of the center of $c\bar{c}$ dipoles is similar to the momentum distribution of J/ψ , then we can generate the $c\bar{c}$ dipoles based on the relative probabilities ,

$$F_{c\bar{c}}^{pp}(p_T, y) = p_T f_{\Psi}^{\text{Norm}}(p_T|y) \cdot \frac{d\sigma_{\Psi}^{pp}/dy(y)}{d\sigma_{\Psi}^{pp}/dy(y=0)}$$

2. Generating $c\bar{c}$ dipoles in coordinate space,

$$F_{c\bar{c}}^{PbPb}(\mathbf{x}_T|\mathbf{b}) = \frac{T_{Pb}(\mathbf{x}_T)T_{Pb}(\mathbf{x}_T - \mathbf{b})}{T_{Pb}(0)T_{Pb}(0)}$$

The distribution of $c\bar{c}$ dipoles in full space,

$$n_{c\bar{c}}(\mathbf{x}_T, p_T|\mathbf{b}, y) = n_0 \times F_{c\bar{c}}^{PbPb}(\mathbf{x}_T|\mathbf{b}) \times F_{c\bar{c}}^{pp}(p_T, y) \\ \times \mathcal{R}^{Pb}(x_1, Q^2, \mathbf{x}_T) \mathcal{R}^{Pb}(x_2, Q^2, \mathbf{x}_T - \mathbf{b})$$

n_0 : constant
($c\bar{c}$ events)

Generating $c\bar{c}$ dipoles in Pb-Pb

The initial yields of charmonium eigenstates

$$n_{mS}^{t=0}(\mathbf{x}_T, p_T | \mathbf{b}, y) = n_{c\bar{c}}(\mathbf{x}_T, p_T | \mathbf{b}) \times |\langle R_{mS}(r) | \phi_0(r) \rangle|^2$$

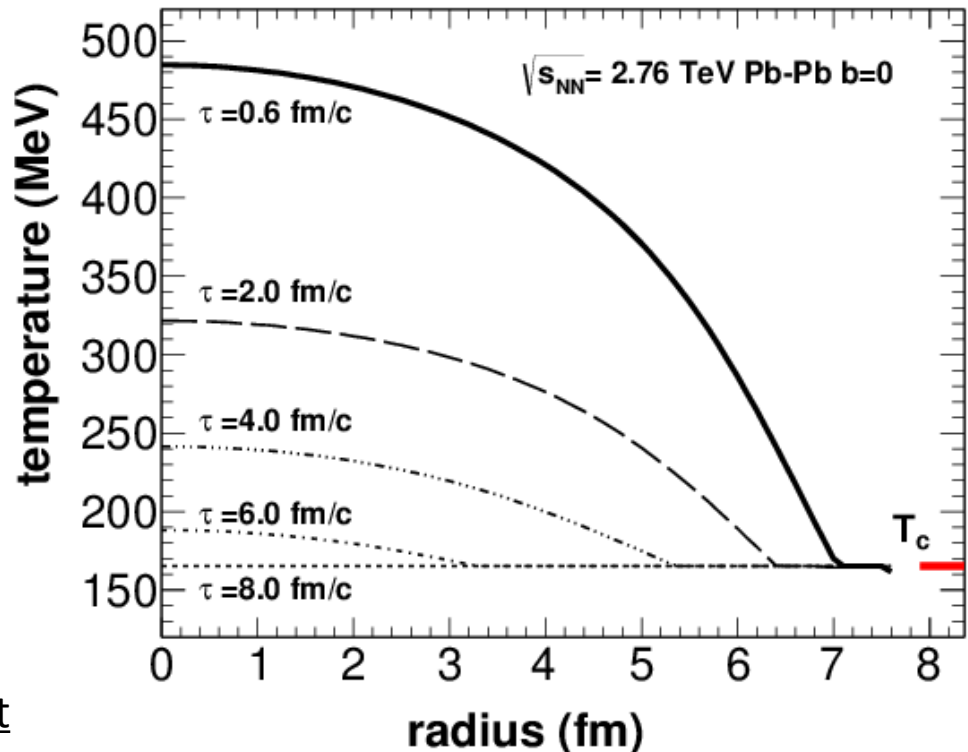
$$|c_{mS}(t=0 | \mathbf{b})|^2 = \int d\mathbf{x}_T \int_{p_{T1}}^{p_{T2}} dp_T n_{mS}(\mathbf{x}_T, p_T | \mathbf{b})$$

1). $c\bar{c}$ dipoles move inside QGP,

$$\mathbf{R}_{c\bar{c}}(\tau + \Delta\tau) = \mathbf{R}_{c\bar{c}} + \mathbf{v}_{c\bar{c}} \cdot \Delta\tau$$

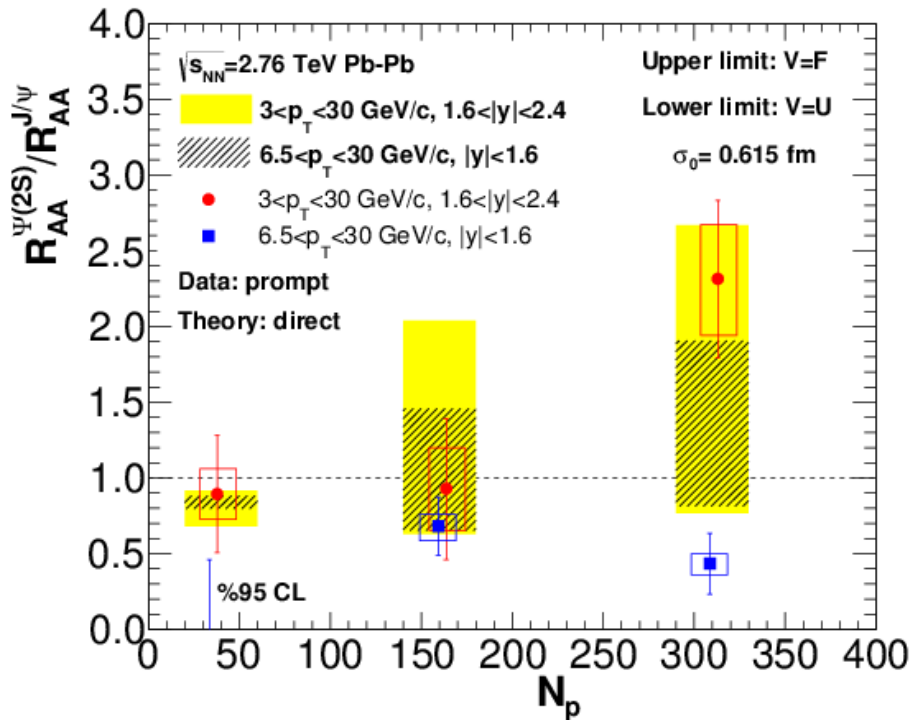
2). During each time step, wavefunctions of $c\bar{c}$ dipoles are evolved with the Schrodinger equation.

At different $(\tau, R_{c\bar{c}})$,
the temperature of QGP is different



$R_{AA}(2S)/R_{AA}(1S)$ in Pb-Pb

Double ratio of direct 1S and 2S states,



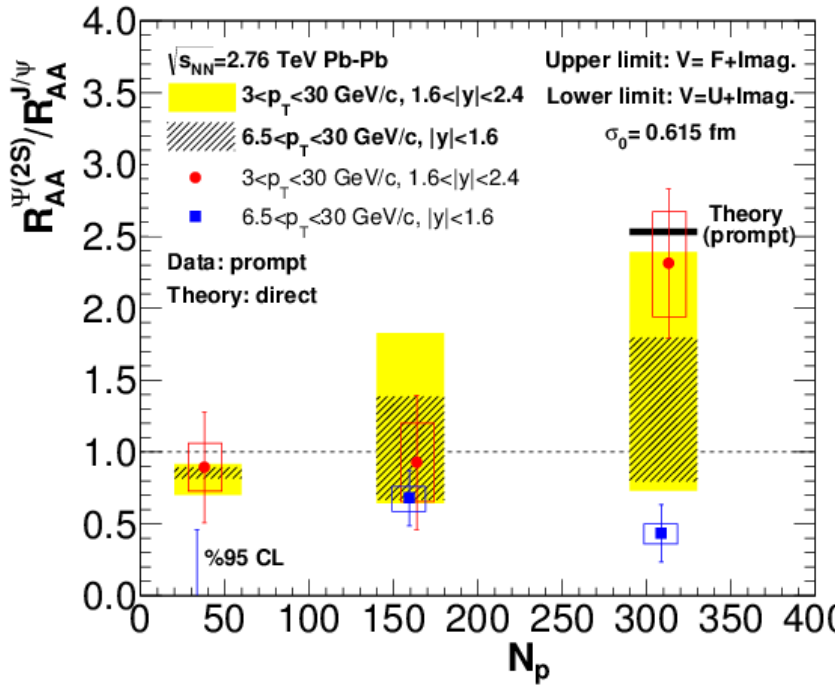
Real potential
(without imaginary part)

- Yellow region → red data points (3 < pT < 30 GeV/c)
- Shadowing region → blue data points (6.5 < pT < 30 GeV/c)

- **High pt region:** move out of QGP quickly.
- **Middle pt region:** stay longer in QGP
- **Low pt region:** regeneration will increase the yield of J/psi by ~10 times.
regeneration of J/psi pull down the double ratio,
color screening effect increases the double ratio.
→ difficult to draw a conclusion at this pT bin

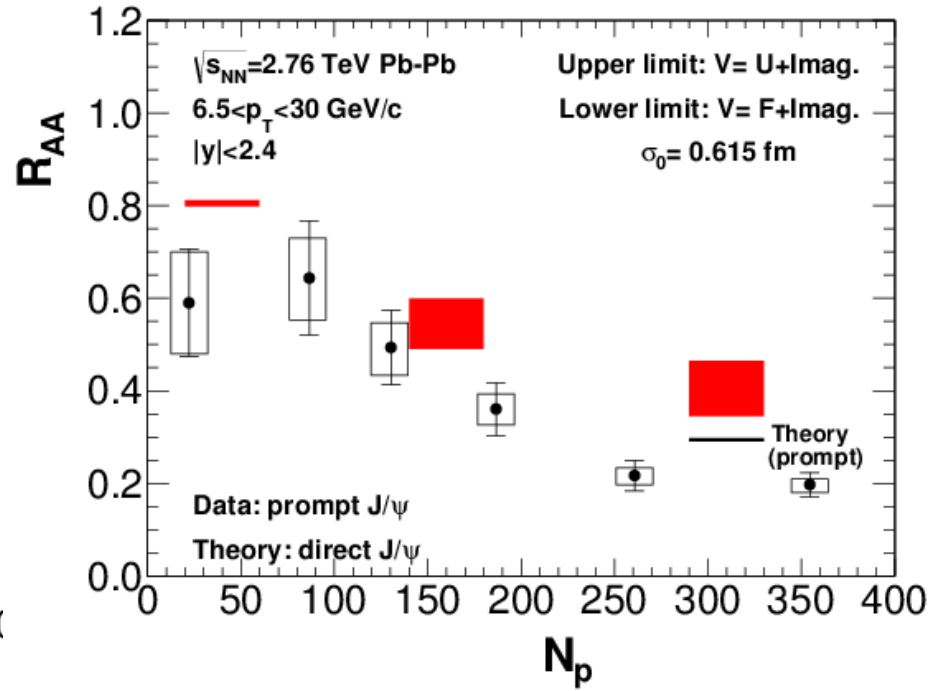
$R_{AA}(2S)/R_{AA}(1S)$ in Pb-Pb

Double ratio,



$6.5 < p_T < 30$ GeV/c
 $3.0 < p_T < 30$ GeV/c

RAA (1S)



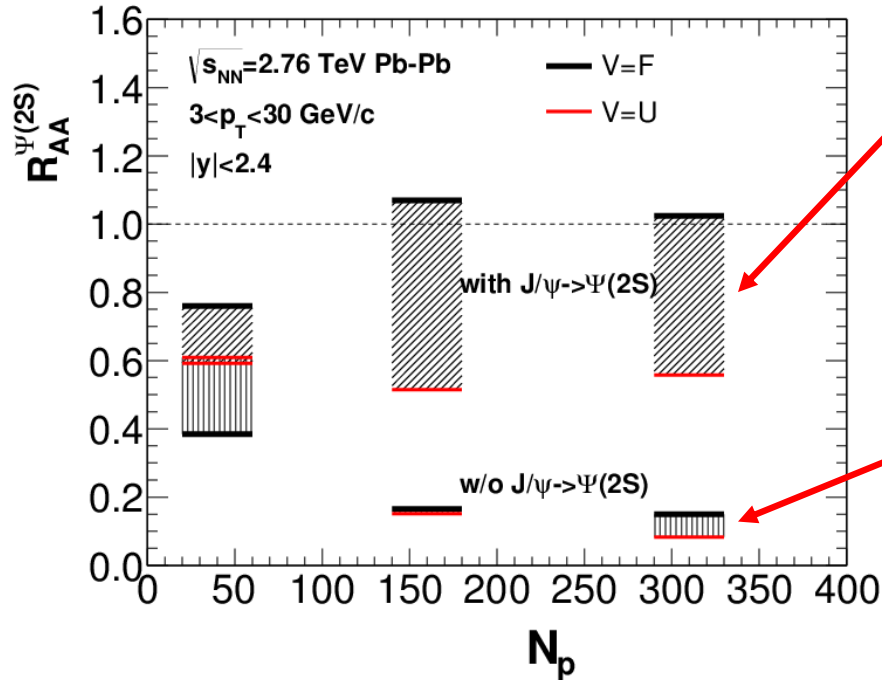
$6.5 < p_T < 30$ GeV/c

Both: Complex potential

Black solid line: estimation of prompt value

Estimate prompt RAA

Nuclear modification factor of 2S



Initialize the wavefunction of $c\bar{c}$ dipole with **Gaussian function** (contains both 1S and 2S fractions)

Initialize the wavefunction of $c\bar{c}$ dipole with **2S eigenstate**

➤ **Estimate prompt value** at $N_p=320$, (at pt: 3-30 GeV/c):

$$R_{AA}^{\text{prompt}}(J/\psi) = R_{AA}^{\text{direct}}(J/\psi) \times 0.6 + R_{AA}^{\text{direct}}(\chi_c) \times 0.3 + R_{AA}^{\text{direct}}(\Psi(2S)) \times 0.1$$

(We assume that the suppression of **1P eigenstates** is similar to **2S eigenstate**.)

Summary

- In QGP, color screening effect makes $c\bar{c}$ become a loosely bound dipole. This changes the yields of charmonium 1S and 2S states.

The formation process is important for charmonium 2S eigenstate in heavy ion collisions.

- Predictions:

Upsilon is a tightly bound state,
at FCC (39TeV), the temperature of QGP is very high.

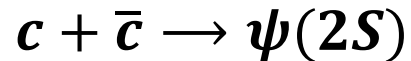
Is there a similar phenomena for upilon observables (1S,2S,3S) at FCC ? We are already working on this.

part 2

part 2

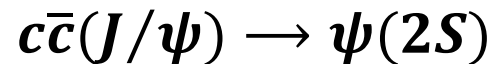
How to distinguish two mechanisms of $\psi(2S)$ production ?

(uncorrelated $c\bar{c}$)



regeneration (Coalescence)

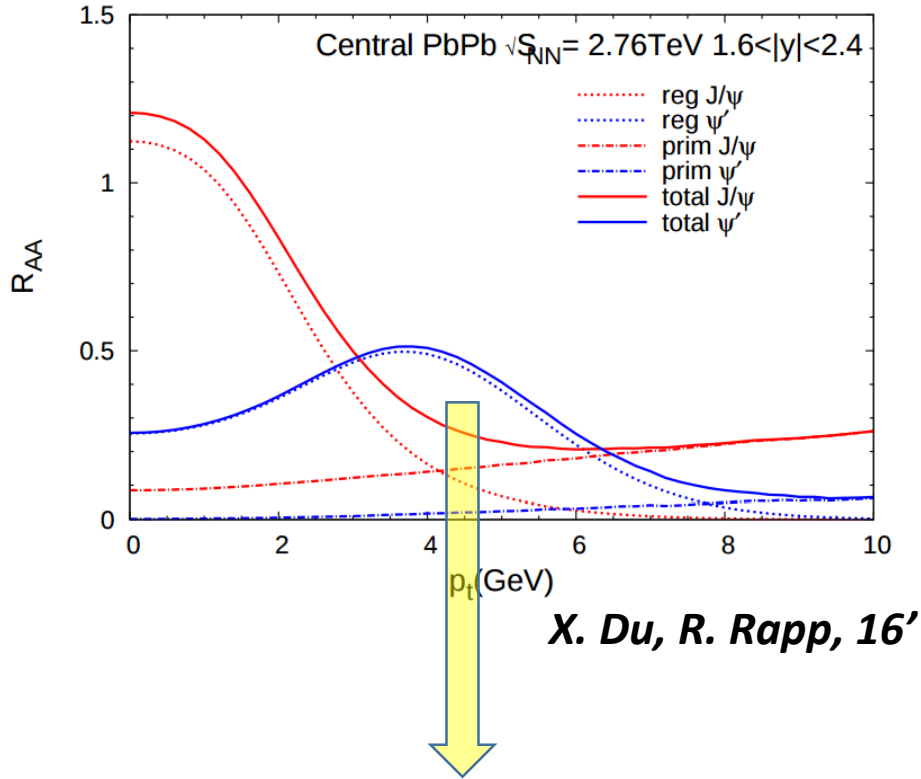
(correlated $c\bar{c}$)



transition (formation)

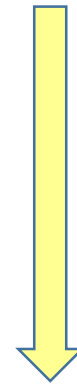
$v_2^{\psi(2S)}$ (p_T) may be a sensitive probe for the $\psi(2S)$ production mechanisms.

Different mechanisms



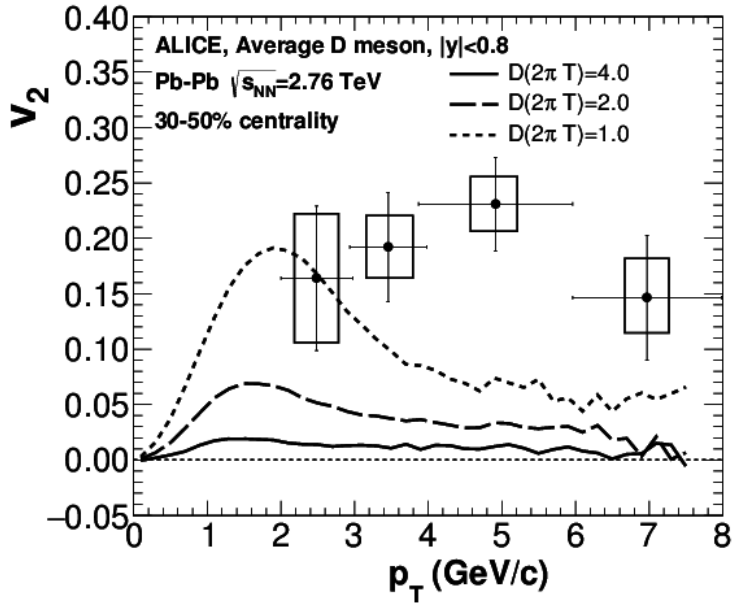
Sequential regeneration:
 almost all of the final $\psi(2S)$ are
 from the regeneration at $T \sim T_c$.

$$c\bar{c}(J/\psi) \rightarrow \psi(2S)$$

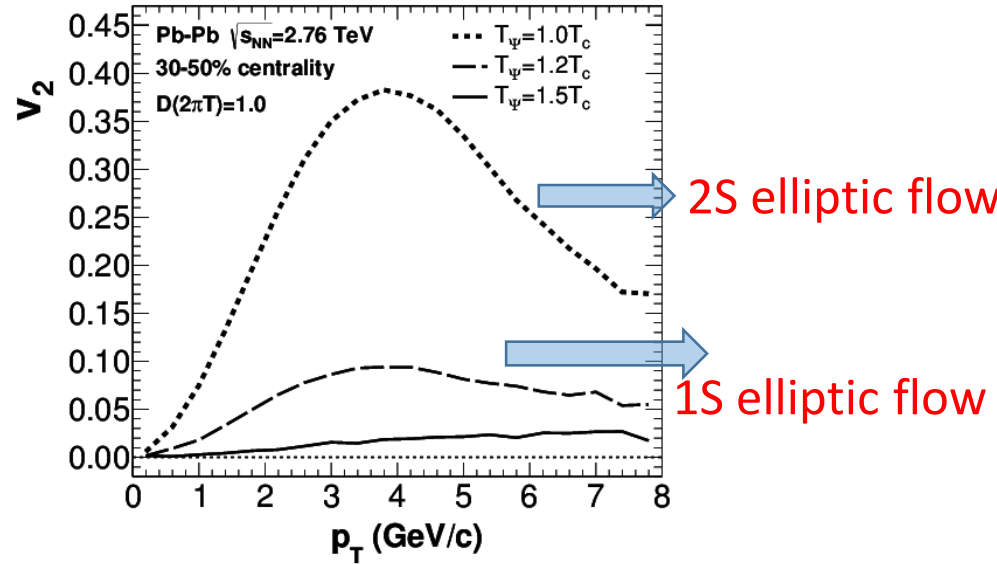


$\psi(2S)$ are mainly from the
 initially produced $c\bar{c}$ dipole

Charm elliptic flow



Charm quarks



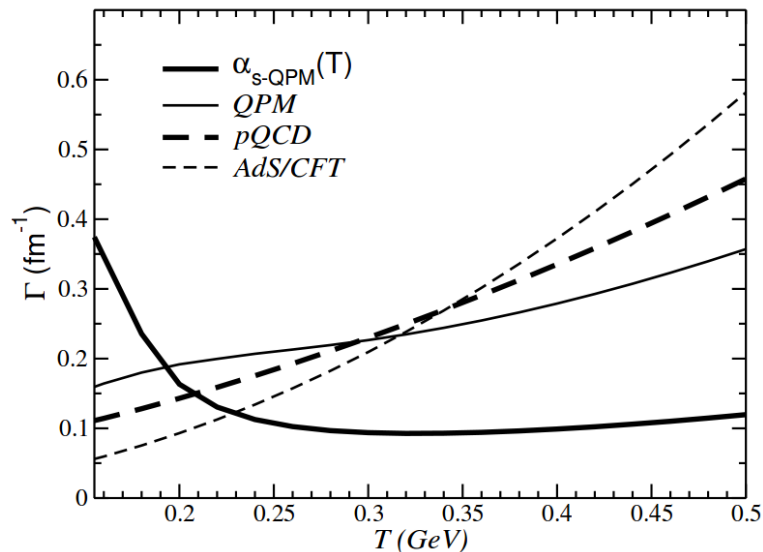
Regenerated charmonium

Quark number scaling: $v_2^\psi(pT) = 2v_2^c(pT/2)$

- Elliptic flow of charm quarks are mainly developed at the Later stage of QGP evolution. Charmonium produced at later stage will carry larger v_2 .
- Coalescence or fragmentation process will change the v_2 of charm quarks by 20% around.

Summary 2:

1. With different drag coefficient, the relation between elliptic flows of 1S and 2S do not change.



S.K Das et al, arXiv: 1502.03757

Different drag coefficient

backup

Cornell potential : $V_{\text{Cornell}}(r) = \begin{cases} -\frac{\alpha}{r} + \sigma r & r < r_{D\bar{D}} \\ 2m_D - 2m_c & r \geq r_{D\bar{D}} \end{cases}$

H. Satz, JPG 06'
 $\alpha = \pi/12$
 $\sigma = 0.2 \text{ GeV}^2$

➤ Estimate prompt value at $N_p=320$, (at pt: 3-30 GeV/c):

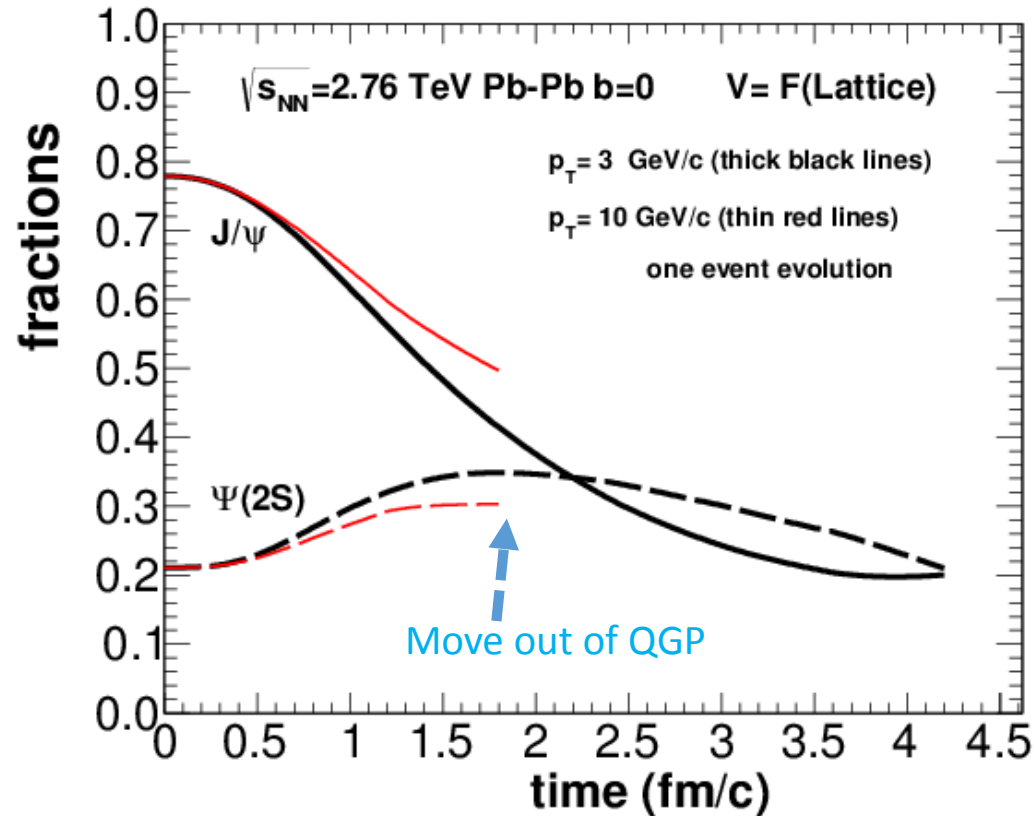
RAA(1S)(direct) = 0.16

RAA(2S)(direct) = 0.38

RAA(1p)(direct) = 0.056

One $c\bar{c}$ evolution in Pb-Pb

One $c\bar{c}$ dipole evolution in Pb-Pb, it is produced at the center of QGP



Expanding QGP

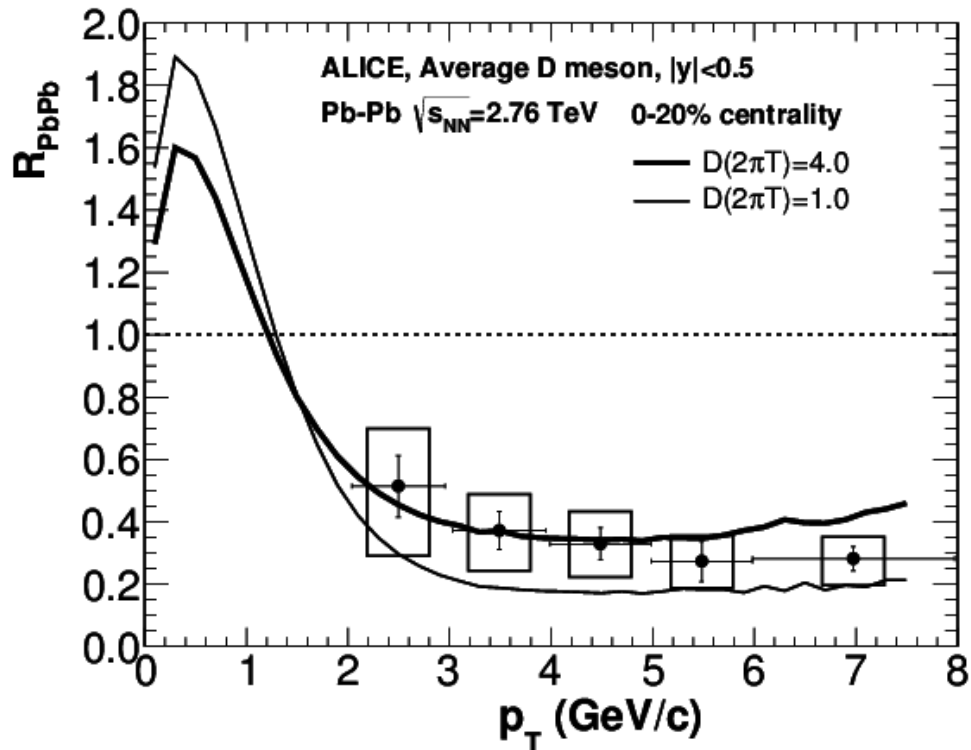
We want to explain the yields of 2S states in the momentum region:
3-30 GeV/c, and **6.5-30 GeV/c**.

We choose two typical values of momentum (the center of the $c\bar{c}$ dipole)

Charm evolution

$$\frac{d\vec{p}}{dt} = -\eta_D(p)\vec{p} + \vec{\xi}$$

$$\eta_D(p) = \frac{\kappa}{2TE}$$



$$\langle \xi^i(t) \xi^j(t') \rangle = \kappa \delta^{ij} \delta(t - t')$$

$$\eta_D(p) = \frac{\kappa}{2TE}$$

$$D = \frac{2T^2}{\kappa}$$


$$D = C/2\pi T$$

C: parameter,

Our values are similar to Guang-You Qing's

Initialization of $c\bar{c}$ wavefunction

Gaussian wave: $\phi_0(r) = A e^{-\frac{r^2}{2\sigma_0^2}}$ $\int dr \cdot r^2 |\phi_0(r)|^2 = 1$



 given by pp data

$$A = \frac{2}{\pi^{1/4} \sigma_0^{3/2}}$$

Heavy quark potential from Lattice Results:

Real part: $F(T, r) = -\frac{\alpha}{r} e^{-\mu r} - \frac{\sigma}{2^{3/4} \Gamma[3/4]} \left(\frac{r}{\mu}\right)^{1/2} K_{1/4}[(\mu r)^2]$

imaginary part:

(HTL results) $\text{Im}V(r) = -\frac{g^2 C_F T}{4\pi} \tilde{f}(\hat{r})$

$$\tilde{f}(\hat{r}) = 2 \int_0^\infty dz \frac{z}{(z^2 + 1)^2} \left[1 - \frac{\sin(z\hat{r})}{z\hat{r}}\right]$$

M. Strickland, PRD, 09'

The evolutions of $c\bar{c}$ dipoles with **real** and **complex** heavy quark potentials will be given respectively.