FLAVOR PHYSICS AT COLLIDERS

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SLAC Summer Institute, Aug 25, 2016

FLAVOR AT COLLIDERS

- constraints on NP models from "low energy" precision observables
 - *B* physics programs at LHCb, ATLAS, CMS

see talks by V. Cirigliano, M. Sokoloff, H. Jawahery

- examples: *B_s* mixing, rare *B* decays, etc
- high *p*_T physics at ATLAS and CMS
 - nontrivial flavor structure modifies signatures
 - example: stop searches, $\tilde{t} \rightarrow c\chi^0$ instead of $\tilde{t} \rightarrow t\chi^0$
 - example: searches for vector-like quarks $B' \rightarrow tW$ vs. $B' \rightarrow uW$ see presentation by Team 3 in the afternoon
 - Higgs flavor structure (e.g., $h \rightarrow \tau \mu$)

LOW ENERGY PRECISION FLAVOR

HISTORIC VIEW

- most of on-shell discoveries in particle physics in the last ~50 years anticipated through a combination of
 - theoretical arguments
 - indirect experimental information
- GIM cancellation ⇒ NP@~GeV (charm quark)
- unitarization of Fermi theory \Rightarrow NP@~100GeV (W,Z)
- *B&L* accidental in the SM+ solar neutrino deficit ⇒ neutrino masses
- CPV in kaon sector \Rightarrow 3rd generation
- *B* mixing, EW fits \Rightarrow top quark@~170 GeV
- EW fits (WW unitarization) \Rightarrow Higgs@~100 GeV (NP <1TeV)

FACING THE FUTURE

- a number of open questions
 - origin/nature of dark matter
 - baryon asymmetry
 - cosmological constant
 - hierarchy problem (origin of EW scale)
 - strong CP problem
- unlike some of the historic examples none of the above uniquely fixes NP scale
 - *B* physics (flavor physics in general) can probe high NP scales

SENSITIVITY TO NEW PHYSICS

- sensitivity to NP from virtual corrections
 - e.g. $b \rightarrow sl^+l^-$
- NP contribs. scale as

 $\left[\delta C^{\rm NP} \propto \frac{\sin \theta_i \sin \theta_j}{M_{\rm NP}^2}\right]$

 need to know mix. angles and NP masses



rom talk by G. Hiller at The First Three years of LHC, Mainz, Mar 2013

SEARCHING FOR THE TAIL

• from observing the tail can deduce the existence of a whale



- in *B* (flavor) physics many observables
 - can reconstruct many features of the NP (whale)

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7

LOW ENERGY PRECISION BOUNDS

UTFit 0707.0636, 1411.7233

- an impressive progress on flavor bounds in last 10 years
- in D, B_s mixing
- also ~2x on NP scale from ε_K



LOW ENERGY PRECISION BOUNDS

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8

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9

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THE FUTURE: TREE PROCESSES @ BELLE 2



THE FUTURE: TREE PROCESSES @ BELLE 2



BELLE 2 RULE OF THUMB

- if NP gives dim-6 operators at low eng.
 - Br scale as $\sim \Lambda_{NP}^{-4}$

 $\frac{1}{\Lambda^2} (\bar{b}_L \gamma^\mu d_L) (\bar{b}_L \gamma_\mu d_L)$

- keeping NP couplings the same
 - increasing luminosity
 - 1ab⁻¹→50ab⁻¹ corresponds to an increase in energy scale by ~2.7x
 - like going from 8TeV LHC to 21TeV LHC

HIGGS AND FLAVOR

HIGGS BOSON IN THE STANDARD MODEL

- the Higgs has a dual role in the SM
- breaks EW symmetry and generates W, Z masses $D_{\mu}\phi = (\partial_{\mu}\phi - igT^{a}W_{\mu}^{a} - ig'YB_{\mu})\phi$ $\mathcal{L}_{\phi} = |D_{\mu}\phi|^{2} + \mu^{2}\phi^{\dagger}\phi - \lambda(\phi^{\dagger}\phi)^{2}$ $\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} \quad v = 246 \text{ GeV}$ $\mathcal{L}_{\phi} \supset \frac{1}{2} (\partial_{\mu}h)^{2} + \left[m_{W}^{2}W^{\mu}W_{\mu}^{-} + \frac{1}{2}m_{Z}^{2}Z^{\mu}Z_{\mu}\right] \left(1 + 2\frac{h}{v} + \frac{h^{2}}{v^{2}}\right)$

gives SM fermions their masses

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FERMION MASS GENERATION IN THE STANDARD MODEL

• in the SM fermion masses from Yukawa interactions with the Higgs

$$\mathcal{L}_{\text{Yuk}} = -(Y_d)_{ij} \bar{Q}_{L,i} d_{R,j} \phi - (Y_u)_{ij} \bar{Q}_{L,i} u_{R,j} \phi^c - (Y_\ell)_{ij} \bar{L}_{L,i} \ell_{R,j} \phi + \text{h.c.}$$

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0\\ v+h \end{pmatrix} \quad v = 246 \text{ GeV}$$
$$\mathcal{L}_f = -m_f \bar{f} f \left(1 + \frac{h}{v}\right) = m_f \bar{f} f - \frac{y_f}{\sqrt{2}} \bar{f} f h \qquad y_f = \sqrt{2} m_f / v$$

Higgs Yukawa couplings proportional to massesmasses and Yukawas diagonal in the same basis

SM HIGGS?

- Higgs boson discovery July 2012
- how closely does it resemble the SM Higgs?
- responsible for EWSB?
 - from couplings to $W, Z \Rightarrow$ yes, most of it
- fermion mass generation
 - does it couple to fermions?



• does it couple to fermions?

15

YUKAWA COUPLINGS : NONTRIVIAL FLAVOR STRUCTURE

- fermion masses are very hierarchical
- what is the origin of this?
 - this is the <u>SM flavor</u> <u>puzzle</u>
- in the SM

$$y_f = \sqrt{2}m_f/v$$

- implies Higgs has very hierarchical couplings to fermions
- how well have we tested this?



TESTING THE FLAVOR OF THE HIGGS

17

Nir, 1605.00433

- several questions
 - proportionality $y_{ii} \propto m_i$
 - factor of proportionality

$$y_{ii}/m_i = \sqrt{2}/v$$

 diagonality (flavor violation)

$$y_{ij} = 0, \quad i \neq j$$

• reality (CP violation) $Im(y_{ij}) = 0$

$$y_f^{\rm SM} = \sqrt{2}m_f/v$$



PROPORTIONALITY

- "proportionality" and "factor of proportionality" $y_{ii} \propto m_i$ $y_{ii}/m_i = \sqrt{2}/v$
- tested for 3rd generation fermions





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HIERARCHICAL COUPLINGS?

- does Higgs couple to the first two generations?
 - tough: couplings are small
- more modest question: can we show that the couplings are hierarchical?

• already known for charged leptons and up-quarks

direct	$\frac{y_{e(\mu)}^{\exp}}{y_{\tau}^{\exp}} < 0.22(0.28) ,$	$\frac{y_{u(c)}^{\exp}}{y_t^{\exp}} < 0.036 ,$	$\frac{y_{d(s)}^{\mathrm{exp}}}{y_b^{\mathrm{exp}}} < 5.6 . \label{eq:stars}$	global fit
measurements				

- can we establish this for down quarks?
- seems possible to establish $y_d < y_b$ at high luminosity LHC (~300 fb⁻¹)
 - from Higgs + jet
 p_T distributions







- seems possible to establish $y_d < y_h$ at high luminosity LHC (~300 fb⁻¹)
 - from Higgs + jet
 p_T distributions

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CPV AND FV HIGGS COUPLINGS TO SM FERMIONS

flavor violating couplings?

$$y_{ij} = 0, \quad i \neq j$$

- very sensitive indirect probes (from precise bounds on FCNCs, such at $\tau \rightarrow \mu \gamma$)
- from Higgs decays (e.g. $h \rightarrow \tau \mu$)
- CP violating couplings? $Im(y_{ij}) = 0$
 - severe bounds from precision measurements of CP violating observables (such as electric dipole moments, EDMs)

20

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PROBE OF NEW PHYSICS?

- discovery of a FV or CPV Higgs Yukawa coupling would mean New Physics
- how sensitive are these to New Physics?
- how precise are the experimental measurements?

see e.g., Falkowski, Straub, Vicente, 1312.5329

THE EFFECTS OF NEW PHYSICS

• an example: SM + 3 gen. of vectorlike leptons $L_i = (N_i, E_i), \tilde{E}_i$

 $\mathcal{L}_{F,c} = -M\left(\bar{L}C_LL + \bar{E}C_RE\right) - \left(\bar{L}_LY\tilde{E}_RH + \bar{L}_R\tilde{Y}\tilde{E}_LH + \text{h.c.}\right).$

 $\mathcal{L}_{\text{mix}} = M\left(\bar{l}_L \lambda_l L_R + \overline{\tilde{E}_L} \lambda_e e_R\right) + \text{h.c.}$

• imagine that the Higgs only couples to these but not the SM fermions

- the two contribs. have different flavor structure in general
- the Yukawas misaligned from the masses by $1/M^2$

 $y_f =$

 $\frac{\sqrt{2}}{m}m_f + \frac{v^2}{M^2}\lambda_\ell C_L^{-1}Y C_R^{-1}\tilde{Y} C_L^{-1}Y C_R^{-1}\lambda_e$

 $\propto (v^3 + 3v^2h + \cdots)$

EFFECTIVE FIELD THEORY DESCRIPTION

• this result is general - integrate heavy NP and obtain EFT description

11

$$\mathcal{L}_{\text{Yuk}} = -\left(Y_f\right)_{ij} \left(\bar{f}_L^i f_R^j\right) \phi + \text{h.c.} \qquad \Delta \mathcal{L}_{\text{Yuk}} = -\frac{\lambda_{ij}}{\Lambda^2} \left(\bar{f}_L^i f_R^j\right) \phi \left(\phi^{\dagger} \phi\right) + \text{h.c.} + \cdots$$

$$\sqrt{2}m_f = V_L \left(Y_f + \frac{v^2}{2\Lambda^2} \lambda'\right) V_R^{\dagger} v \qquad y_f = V_L \left(Y_f + 3\frac{v^2}{2\Lambda^2} \lambda'\right) V_R^{\dagger}$$

$$\left(y_f\right)_{ij} = \sqrt{2} \frac{m_i}{v} \delta_{ij} + \frac{v^2}{\Lambda^2} \left(V_L \lambda' V_R^{\dagger}\right)_{ij}$$

- important: SM Yukawa couplings small for the first two generations
 - Λ can be large but still have an effect for $\lambda' \sim O(1)$
- the effects different in different NP models of flavor
 - can learn about these from measured patterns

HOW LARGE?

 a useful rule of thumb for maximal FV
 do not want fine-tuned cancelations when diagonalizing mass matrix

$$y_{\tau\mu}y_{\mu\tau} \lesssim 2\frac{m_{\tau}m_{\mu}}{v^2}$$

• also what we would expect for $A \ge v$

MESON MIXING

in K⁰-K
⁰, B_d-B
_d, B_s-B
_s, D⁰-D
⁰ small mass splitting due to FV interactions



Technique	Coupling	Constraint	Norm. Constr.
D^0 oscill. [48]	$ y_{uc} ^2, y_{cu} ^2$	$< 1.0 \times 10^{-8}$	$<(0.5)^2 y_u^{\rm SM} y_c^{\rm SM}$
	$\left y_{uc}y_{cu} ight $	$< 1.5 \times 10^{-9}$	$<(0.2)^2 y_u^{\rm SM} y_c^{\rm SM}$
B_d^0 oscill. [48]	$ y_{db} ^2, y_{bd} ^2$	$<4.6\times10^{-8}$	$<(0.4)^2 y_d^{\rm SM} y_b^{\rm SM}$
	$ y_{db}y_{bd} $	$< 6.6 \times 10^{-9}$	$<(0.15)^2y_d^{\rm SM}y_b^{\rm SM}$
B_s^0 oscill. [48]	$ y_{sb} ^2, y_{bs} ^2$	$< 3.6 \times 10^{-6}$	$<(0.8)^2y_s^{\rm SM}y_b^{\rm SM}$
	$ y_{sb}y_{bs} $	$< 5.0 \times 10^{-7}$	$<(0.3)^2 y_s^{\rm SM} y_b^{\rm SM}$
K^0 oscill. [48]	$\operatorname{Re}(y_{ds}^2), \operatorname{Re}(y_{sd}^2)$	$[-1.21.2] \times 10^{-9}$	$<(0.4)^2y_d^{\rm SM}y_s^{\rm SM}$
	$\operatorname{Im}(y_{ds}^2), \operatorname{Im}(y_{sd}^2)$	$[-5.83.2] \times 10^{-12}$	$<(0.03)^2 y_d^{\rm SM} y_s^{\rm SM}$
	$\operatorname{Re}(y_{ds}^*y_{sd})$	$[-1.1 \dots 1.1] \times 10^{-10}$	$<(0.13)^2 y_d^{\rm SM} y_s^{\rm SM}$
	${ m Im}(y^*_{ds}y_{sd})$	$[-2.8\dots 5.6] imes 10^{-13}$	$<(0.01)^2 y_d^{\rm SM} y_s^{\rm SM}$
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			(a)
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DIPOLE TRANSITIONS

- severe exp. bounds on dipole transitions BaBar, 0908.2381 MEG, 1605.05081 Br($\tau \rightarrow \mu \gamma$) < 4.4 · 10⁻⁸ Br($\tau \rightarrow e \gamma$) < 3.3 · 10⁻⁸ Br($\mu \rightarrow e \gamma$) < 4.2 · 10⁻¹³
 - same NP diagrams that give $h \rightarrow \tau \mu$ generically also give $\tau \rightarrow \mu \gamma$ at 1-loop



• NDA estimate for the EM dipole operators

$$y_{\tau\mu} \sim \frac{v^2}{\Lambda^2} \lambda'_{\tau\mu}$$

$$c_{L,R} \sim \frac{v}{m_{\tau}\Lambda^2} \lambda'_{\tau\mu,\mu\tau} \sim \frac{1}{m_{\tau}v} y_{\tau\mu,\mu\tau}$$

$$\mathcal{L}_{\text{eff}} = c_{L,R} \, m_\tau \frac{e}{8\pi^2} \left(\bar{\mu}_{R,L} \sigma^{\mu\nu} \tau_{L,R} \right) F_{\mu\nu}$$

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26

$h \rightarrow \tau \mu \exp. info$

• hint of a signal in $h \rightarrow \tau \mu$ still there?

CMS-HIG-14-005

- CMS: $Br(h \rightarrow \tau \mu) = (0.89 \pm 0.39)\%$
- ATLAS: $Br(h \rightarrow \mu \tau) = (0.53 \pm 0.51)\%$

ATLAS, 1508.03372; 1604.07730

• first 13 TeV result

CMS-PAS-HIG-16-005

 CMS @ 13 TeV, 2.3 fb⁻¹: no excess, Br(H→τµ)<1.20% (1.62% expected)

EXCLUDED?

- if Higgs the only^{*} source of ferm. mass $\Rightarrow Br(\tau \rightarrow \mu \gamma)$ too large by <u>4 orders</u> of magnitude
 - *and no tunings for tuned MSSM example see e.g., Aloni, Nir, Stamou, 1511.00979
- alternatively one could do EFT analysis of low energy constraints with the Lagrangian after EWSB

$$\mathcal{L}_Y = -m_i \bar{f}_L^i f_R^i - Y_{ij} (\bar{f}_L^i f_R^j) h + h.c. + \cdots,$$

- does not care whether Higgs is part of a doublet
- or if there are other EWSB sources







LARGE FV HIGGS DECAYS?

- Can one have large flavor violating Higgs decays in reasonable NP models?
- What is so special about type III 2HDM?



30

VIABLE MODELS: SEQUESTERED MASS GENERATION

Altmannshofer, Gori, Kagan, Silvestrini, JZ, 1507.07927

- a family of viable new physics models
 - lepton mass matrix of the form

$$\mathcal{M}^{\ell} = \mathcal{M}^{\ell}_0 + \Delta \mathcal{M}^{\ell},$$

rank 1 matrix, from ϕ rank 2 or 3 matrix

- scalar ϕ the primary component of the Higgs
 - accounts for the bulk of m_{τ}
- ΔM_1 due to an additional source of EWSB

• accounts for m_e and m_μ

2HDM

- two Higgs doublets, neutral compts: ϕ , ϕ' , vevs v, v'
 - ϕ couples to 3rd family, ϕ' to all three





- a hierarchy of vevs $v \gg v'$ can explain $m_{\tau} \gg m_{\mu}$
- can saturate $Br(h \rightarrow \tau \mu)$
- $Br(\tau \rightarrow \mu \gamma)$ parametrically suppressed (there is an extra y_{τ} insertion)
- predicts modified phenomenology of heavy Higgses

32

CONCLUSIONS

- flavor physics can probe NP scales well above LHC
- flavor violating Higgs decays a window to fermion mass generation

BACKUP SLIDES

DIFFERENT PROBES

- several probes of 1st and 2nd generation Higgs yukawas proposed
 - using charm tagging for h→cc̄ inclusive Perez, Soreq, Stamou, Tobioka, 1503.00290 decays
 - exclusive decays: $h \rightarrow \Upsilon \gamma (y_b)$, $h \rightarrow J/\psi \gamma (y_c), h \rightarrow \phi \gamma (y_s)_{\text{Kagan, Perez, Petriello, Soreq, Stoynev, JZ, 1406.1722}$
 - isotopic shift measurements
 - Delaunay, Ozeri, Perez, Soreq, 1601.05087

Bodwin, Petriello, Stoynev, Velasco, 1306.5770

• Higgs *p*_T distributions

Bishara, Haisch, Monni, Re, 1606.09253 Soreq, Zhu, JZ, 1606.09621

35

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$$h \rightarrow \phi \gamma$$

- for s Yukawa $h \rightarrow \phi \gamma$ (where $\phi \sim \bar{s}s$; $J^{PC} = 1^-$; $m_{\phi} = 1.02 \text{GeV}$)
- two amplitudes, direct is subleading



• prediction at NLO

$$\frac{\mathrm{BR}_{h\to\phi\gamma}}{\mathrm{BR}_{h\to b\bar{b}}} = \frac{\kappa_{\gamma}[(2.3\pm0.1)\kappa_{\gamma}-0.43\bar{\kappa}_s]\cdot10^{-6}}{0.57\bar{\kappa}_b^2}$$

$$Y_{ss} = ar\kappa_s m_b / v$$

Kagan, Perez, Petriello, Soreq, Stoynev, JZ, 1406.1722 Konig, Neubert, 1505.03870

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ATLAS MEASUREMENT



CHARM YUKAWA

• similarly Y_c from $h \rightarrow J/\psi\gamma$ Bodwin, Petriello, Stoynev, Velasco, 1306.5770 Konig, Neubert, 1505.03870 $\frac{\mathrm{BR}_{h\to J/\psi\gamma}}{\mathrm{BR}_{h\to b\bar{b}}} = \frac{\kappa_{\gamma}[(3.0\pm0.15)\kappa_{\gamma}-0.56\bar{\kappa}_c]\cdot10^{-6}}{0.57\bar{\kappa}_b^2}$ ATLAS, 1501.03276 • projecting the ATLAS bound to 100TeV, 2x3ab⁻¹, same S/B: $\bar{\kappa}_c < 4$ Perez, Soreq, Stamou, Tobioka, 1505.06689 • from inclusive, Unboosted Higgs at a 100 TeV pp collider 1.6med. b-tag+c-tag II using charm $-2 \times 3000 \, \text{fb}^{-1}$ 1.4tagging $\kappa_b 1.2$ 1.0Profiling @ 95% CL $\bar{\kappa}_c = 0.6$ $\begin{array}{l} \kappa_b \in [0.9, 1.1] \\ \kappa_c < 2.1 \end{array}$ 0.80 1 3 4 κ_c J. Zupan Flavor Physics at Colliders SLAC, Aug 23 2016

CHARM QUARK

39

- Higgs *p_T* also sensitive to charm quark, if enhanced Yukawa
- sensitivity from the charm loop in gluon fusion
- log enhanced

$$\kappa_Q \; \frac{m_Q^2}{m_h^2} \; \ln^2\left(\frac{p_\perp^2}{m_Q^2}\right)$$



DIAGONAL YUKAWAS



PHENOMENOLOGICAL IMPLICATIONS

- $B_s \rightarrow \mu \mu$ can be modified by O(1)
- sizable $B_s \rightarrow \tau \mu$, $B \rightarrow K \tau \mu$, $B \rightarrow K^* \tau \mu$
- anomalies could be seen in B_s mixing, $\tau \rightarrow \mu \gamma$, $b \rightarrow s \gamma$
- leptonic heavy Higgs (*H*) decays to $\mu\mu$ dominate over $\tau\tau$
 - opposite to Type-II 2HDMs
- $t \rightarrow hc$ potentially sizable
- a general sum rule

$$\hat{y}_{\mu}\hat{y}_{\tau} - \hat{y}_{\tau\mu}\hat{y}_{\mu\tau} = \hat{y}_{t,b}(\hat{y}_{\mu} + \hat{y}_{\tau} - \hat{y}_{t,b})$$
 $\hat{y}_{ij} \equiv Y_{ij}/Y_{ii}^{\mathrm{SM}}$

- valid to the extent that both $\Delta M'$ and ΔM_0 are rank 1
- is explicitly true in our TC example 41
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ELECTRON YUKAWA

• $\tilde{\kappa}_e \neq 0$ induces electron EDM

Altmannshofer, Brod, Schmaltz, 1503.04830





- analytic results with an internal Z boson are new
- experimental bound ACME coll., 1310.7534

$$\left|\frac{d_e}{e}\right|_{\rm exp} < 8.7 \times 10^{-29} \ {\rm cm} \ @ 90\% \ {\rm C.L.} \,,$$

$$|\tilde{\kappa}_e| < 1.7 \times 10^{-2}$$

SUMMARY OF MODELS

an example: higgs couplings to 2nd&3rd gen. charged leptons

adapted from Dery, Efrati, Hochberg, Nir, 1302.3229 and extended; see also Bishara, Brod, Uttayarat, JZ, 1504.04022

Model	$\hat{\mu}_{ au au}$	$(\hat{\mu}_{\mu\mu}/\hat{\mu}_{ au au})/(m_{\mu}^2/m_{ au}^2)$	$\hat{\mu}_{\mu au}/\hat{\mu}_{ au au}$
\mathbf{SM}	1	1	0
NFC	$(V_{h\ell}^*v/v_\ell)^2$	1	0
MSSM	$(\sin \alpha / \cos \beta)^2$	1	0
${ m MFV}$	$1+2av^2/\Lambda^2$	$1-4bm_{ au}^2/\Lambda^2$	0
\mathbf{FN}	$1 + \mathcal{O}(v^2/\Lambda^2)$	$1 + \mathcal{O}(v^2/\Lambda^2)$	$\mathcal{O}(U_{23} ^2 v^4/\Lambda^4)$
GL	9	25/9	${\cal O}(\hat{\mu}_{\mu\mu}/\hat{\mu}_{ au au})$
$\mathrm{RS}~(i)$	$1 + \mathcal{O}(\bar{Y}^2 v^2 / m_{KK}^2)$	$1 + \mathcal{O}(\bar{Y}^2 v^2 / m_{KK}^2)$	$\mathcal{O}(ar{Y}^2 v^2/m_{KK}^2)\sqrt{m_{ au}/m_{\mu}}$
RS(ii)	$1 + \mathcal{O}(\bar{Y}^2 v^2 / m_{KK}^2)$	$1 + \mathcal{O}(\bar{Y}^2 v^2 / m_{KK}^2)$	$\mathcal{O}(\bar{Y}^2 v^2 / m_{KK}^2)$
PGB (1 rep.)	$1 - v^2/f^2$ min	1	0

43

TECHNICOLOR EXAMPLE

- ΔM_l due to technicolor strong dynamics
 - UV completion is bosonic TC
- Higgs: elementary ϕ + composite heavy scalar σ_{TC}
- ΔM^{l} from TC condensate, rank 1

