



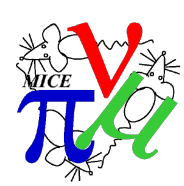
# MICE Step IV Lattice Optimization using GA

Ao Liu  
Fermilab



and also

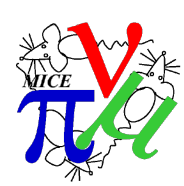
Cherenkov Light Yield



# Outline



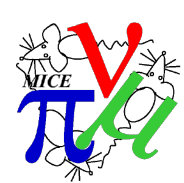
- Methodology of GA optimizations
- Results for Step IV lattice design
  - M1D off only
    - Minimum  $B_z$  of 2 T in the trackers;
    - Minimum  $B_z$  of 2.8 T in the trackers;
  - M1D and M2D both off
- Current Ckov light yield
- Discussion



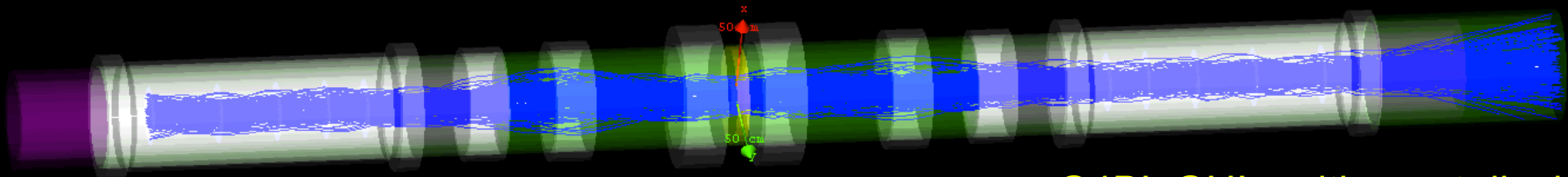
# Motivation



- MICE Step IV goals – demonstrate material physics properties
  - Measurement of the muon Multiple Coulomb Scattering (MCS) and energy loss in the materials;
  - Measurement of the transverse normalized emittance ( $\epsilon_{\perp}$ ) reduction
- In the absence of M1 coil downstream (M1D)
  - Lack of optics matching power;
  - Measurement of the MCS and energy loss are largely unaffected;
  - Can we still demonstrate  $\epsilon_{\perp}$  reduction?
  - Need: New lattice designs for all the run modes, which should have:
    - Decent transmission (good acceptance)
    - Maximized  $\epsilon_{\perp}$  reduction between the reference planes with minimum  $\epsilon_{\perp}$  growth, especially in the SSD.

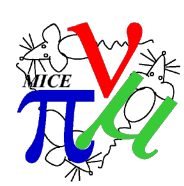


# Simulation setup – G4Beamline

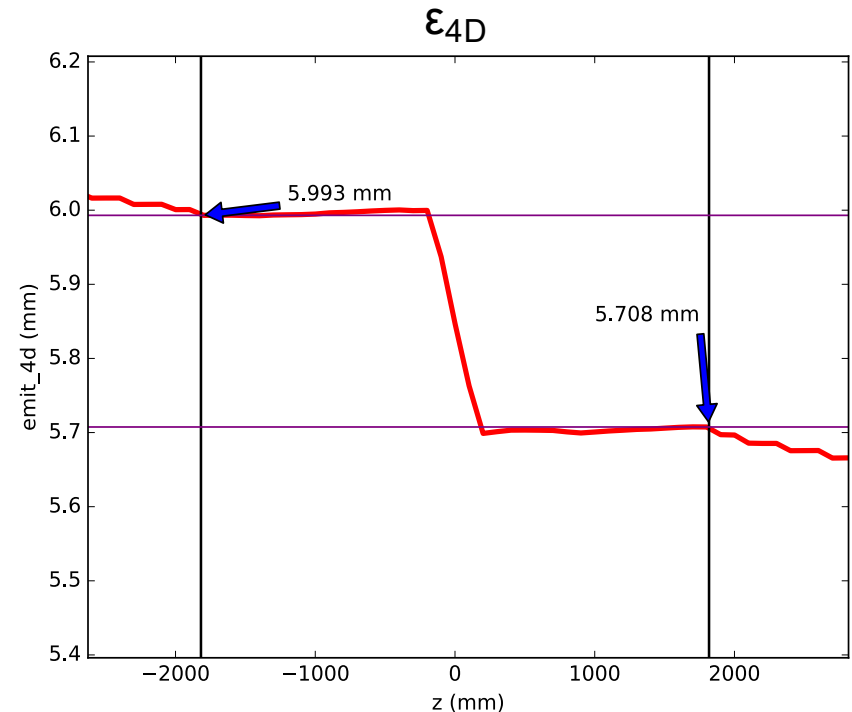
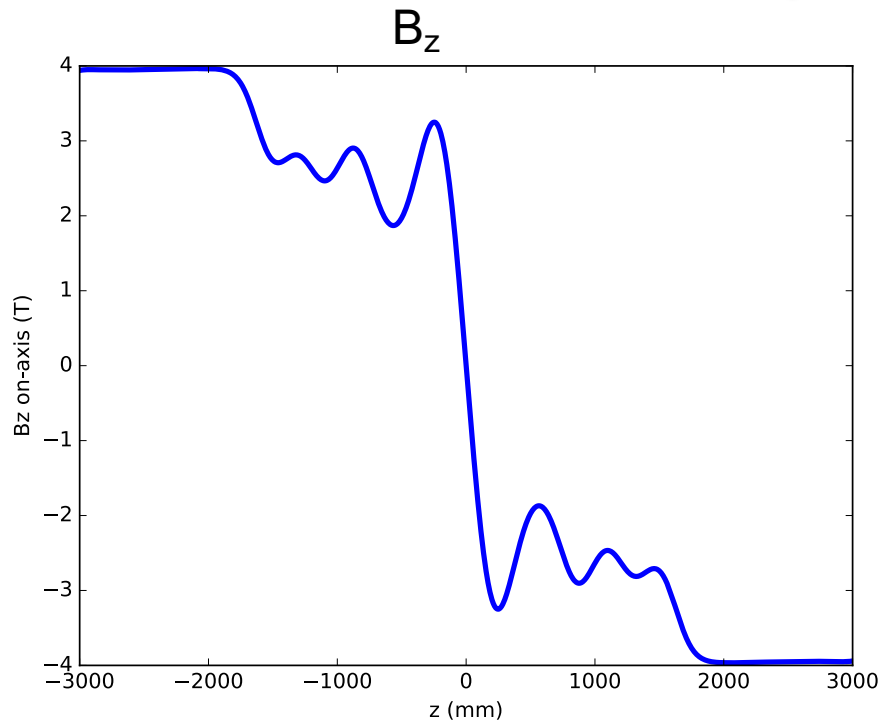


G4BL GUI multi-event display

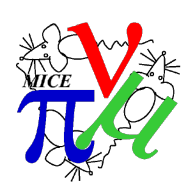
- Geometry ID 70 of MICE Step IV cooling channel
- Materials in channel to match MAUS as accurately as possible:
  - SciFi tracker planes (2 mm Polystyrene each), 65 mm LiH absorber;
  - TOF2 at the end of the channel (+4200 mm from the absorber);
  - Beam pipe to kill particles hitting it ( $r=258$  mm);
- Monte Carlo initial particle ensemble matched to the solenoid longitudinal field  $B_z$ 
  - Beam starts at  $z=-3000$  mm from the absorber (upstream tracker).
- G4BL chosen for its MPI feature and speed on the cluster



# Simulation setup – G4Beamline (cont'd)



Nominal 200 MeV/c flip mode;  
Transmission = 98% with  $\delta p/p$  in  $\pm 5\%$   
4.9% emit. Reduction between ref. planes  
G4BL is consistent with MAUS results – both Geant4 based



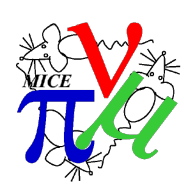
# Optimization setup – GA



- Single Objective Genetic Algorithm (SOGA):
  - Searches the parameter space thoroughly and finds the global optimum; The more variables, the more powerful;
- Objective function:

$$F = T^2 [(\epsilon_{ref,u} - \epsilon_{ref,d})/\epsilon_{ref,u} + (\epsilon_{bound,u} - \epsilon_{bound,d})/\epsilon_{bound,u}]$$

- $T$ : Transmission.  $T^2$  guarantees a good transmission and avoids bias from scraping particles with strong MCS
- $\epsilon_{ref,u}, \epsilon_{ref,d}$ : Transverse normalized emittance at the reference planes ( $\pm 1800$  mm from the absorber). The first term is what we measure;
- $\epsilon_{bound,u}, \epsilon_{bound,d}$ : Transverse normalized emittance at the boundaries of the upstream and downstream tracker ( $\pm 3000$  mm). The second term guarantees a regulated emittance in the trackers (especially downstream).



# Optimization setup – GA (for our case)



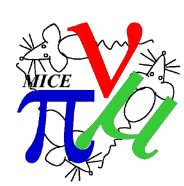
- A few more details:

- Optimization variables (and their ranges) and the corresponding coil current:

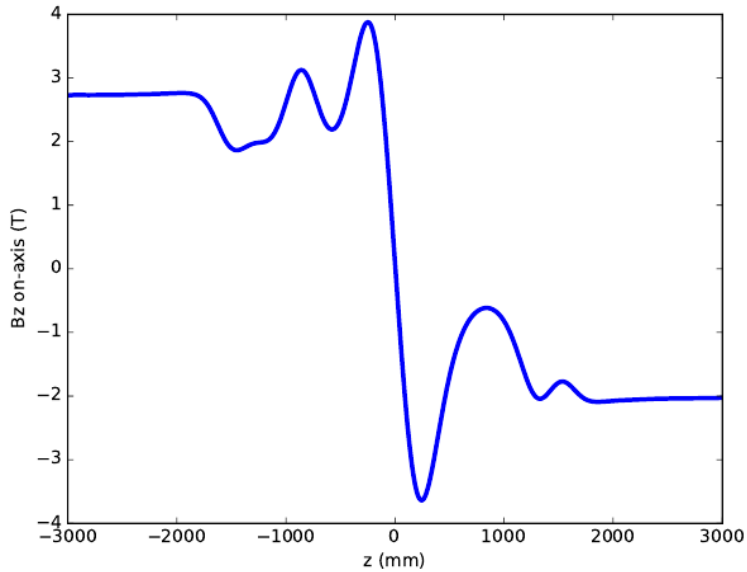
|     | Current (A)                     |                | Range                                      |
|-----|---------------------------------|----------------|--|
| E2U | $253.23 \times x_1$             |                |  |
| CU  | $277.98 \times x_1$             |                |  |
| E1U | $246.2 \times x_1$              | $x_1$          | [0.5, 0.95]                                |
| M2U | $x_2$                           | $x_2$          | [50, 253]                                  |
| M1U | $x_3$                           | $x_3$          | [50, 278]                                  |
| FCU | $x_4$                           | $x_4$          | [50, 225](flip); [50, 114](solenoid)       |
| FCD | $x_4$ (solenoid); $-x_4$ (flip) | $x_5$          | [-245, -50](flip, 200 or 240 MeV/c)        |
| M1D | 0                               | $x_5$ (cont'd) | [-214, -50](flip, 140 MeV/c)               |
| M2D | $x_5$                           | $x_5$ (cont'd) | (signs flipped for solenoid)               |
| E1D | $246.2 \times x_6$              | $x_6$          | [-0.89, -0.5](flip); [0.5, 0.89](solenoid) |
| CD  | $277.98 \times x_6$             |                |  |
| E2D | $253.23 \times x_6$             |                |  |

- Investigated both flip and solenoid modes at all three momentum: 140, 200 and 240 MeV/c

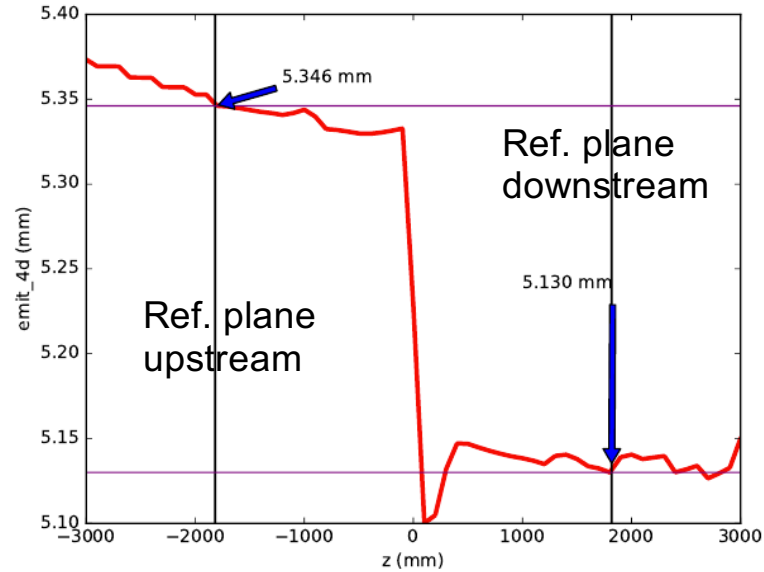




# Optimization result – 200 MeV/c

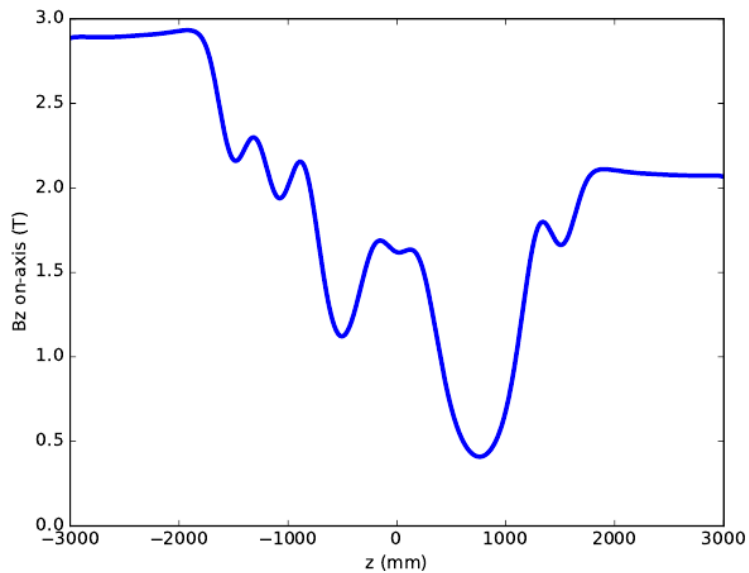


Flip

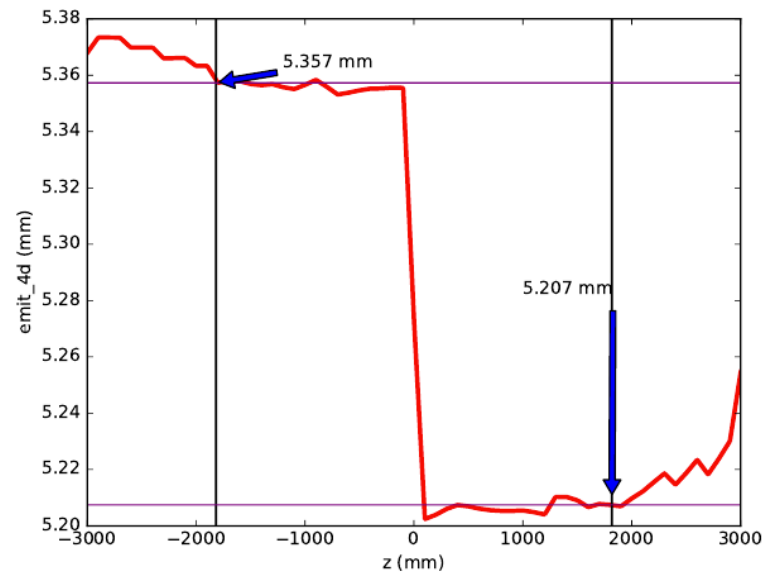


4 % reduction  
in  $\epsilon_{\perp}$

Transmission:  
93%

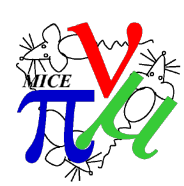


Sol

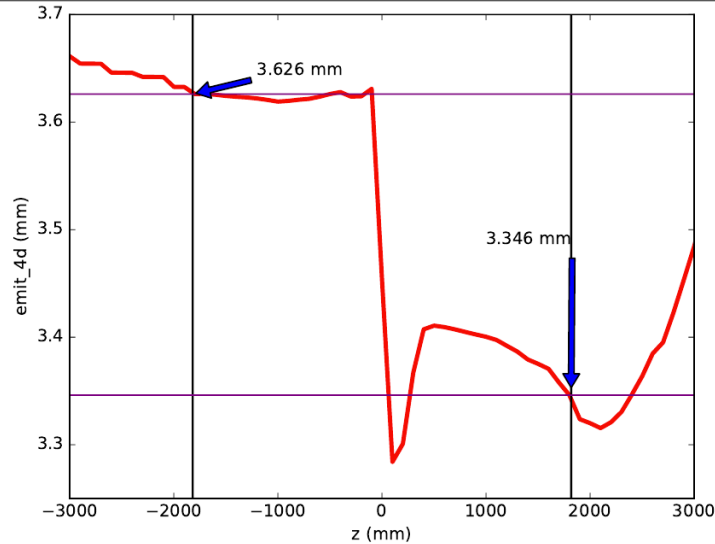
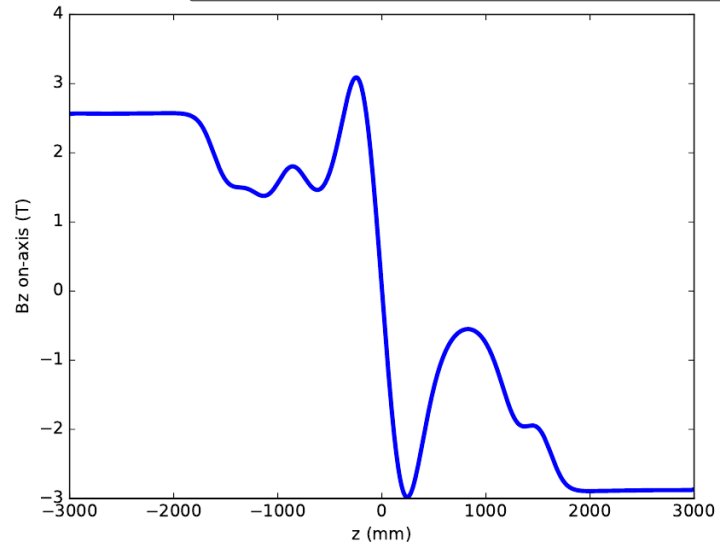


2.8 % reduction  
in  $\epsilon_{\perp}$

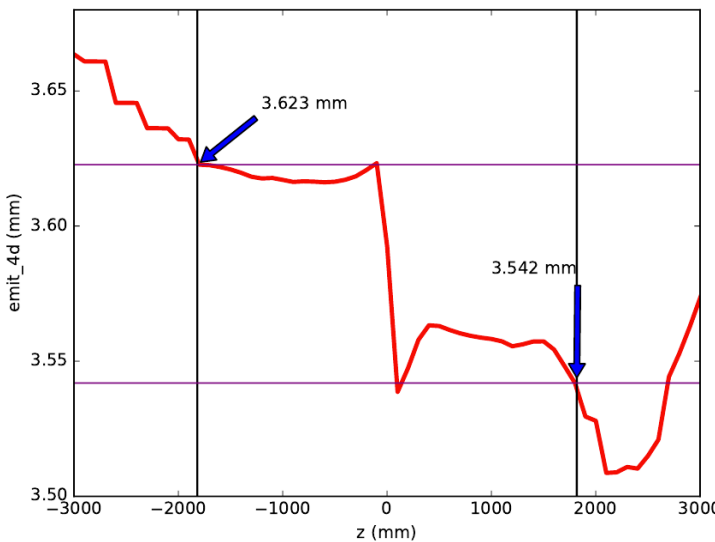
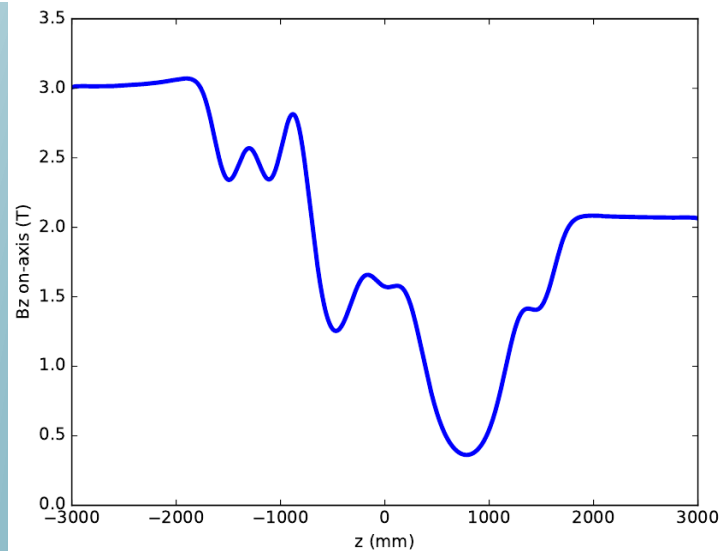
Transmission:  
92%



# Optimization result – 140 MeV/c

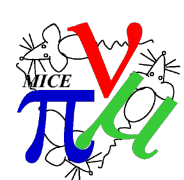


140 MeV/c  
flip  
 $T=93\%$   
 $\epsilon_{\perp}$  reduction:  
7.7%

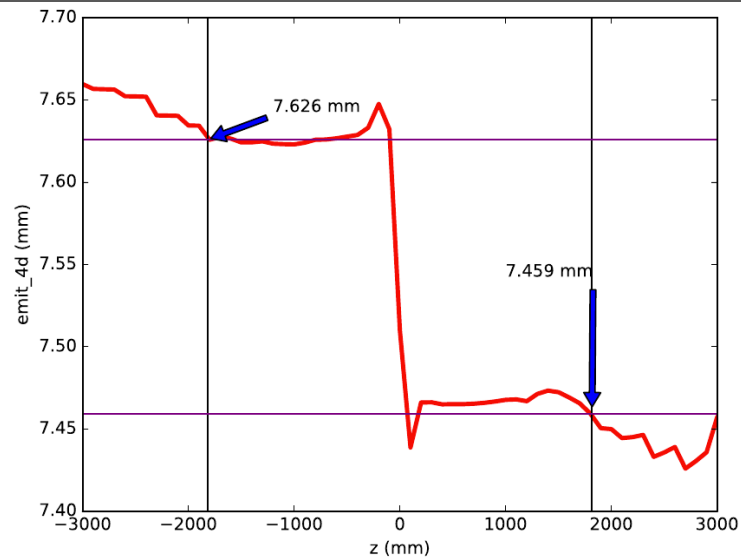
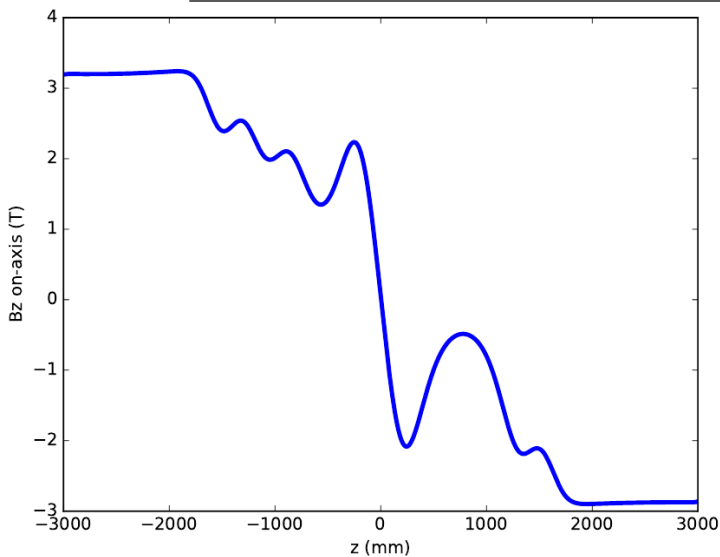


140 MeV/c  
Sol  
 $T=91\%$   
 $\epsilon_{\perp}$  reduction:  
2.2%

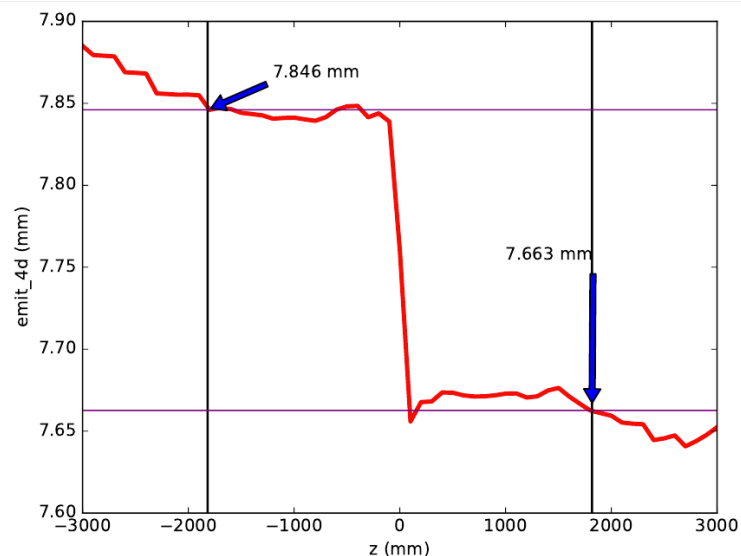
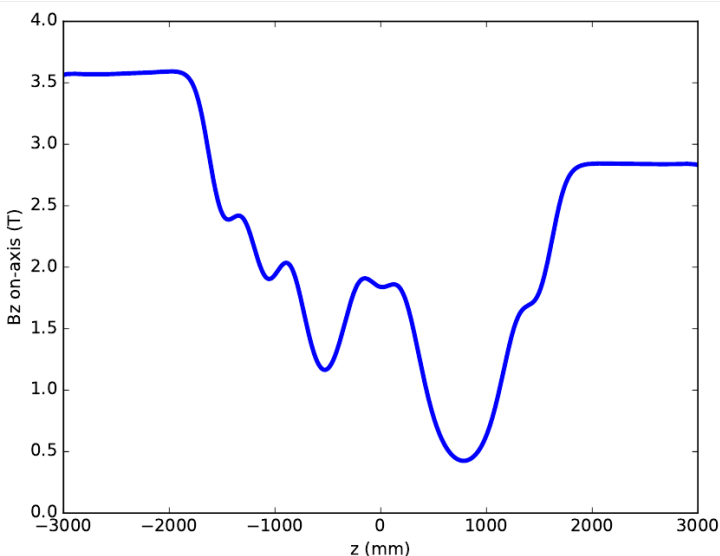
Left: flip mode; right: solenoid mode



# Optimization result – 240 MeV/c

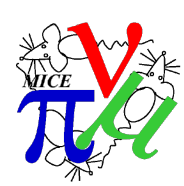


240 MeV/c  
flip  
 $T=90\%$   
 $\epsilon_{\perp}$  reduction:  
2.2%



240 MeV/c  
Sol  
 $T=90\%$   
 $\epsilon_{\perp}$  reduction:  
2.1%

Left: flip mode; right: solenoid mode



# Optimization result - Continued

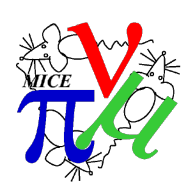


- Variable values corresponding to the previous results:

| variable                    | flip, 140 | flip, 200 | flip, 240 | sole, 140 | sole, 200 | sole, 240 |
|-----------------------------|-----------|-----------|-----------|-----------|-----------|-----------|
| $x_1$                       | 0.64      | 0.68      | 0.80      | 0.75      | 0.72      | 0.89      |
| $x_2$                       | 116.40    | 150.40    | 251.62    | 241.14    | 219.81    | 222.69    |
| $x_3$                       | 133.01    | 253.18    | 150.98    | 225.42    | 162.66    | 146.06    |
| $x_4$                       | 181.21    | 222.94    | 126.80    | 53.52     | 55.95     | 64.09     |
| $x_5$                       | -205.95   | -242.47   | -244.00   | 147.05    | 205.66    | 161.48    |
| $x_6$                       | -0.71     | -0.5      | -0.70     | 0.51      | 0.51      | 0.70      |
| $\Delta\epsilon/\epsilon_i$ | -7.7%     | -4.0%     | -2.2%     | -2.2%     | -2.8%     | -2.3%     |
| $T$                         | 93%       | 93%       | 90%       | 91%       | 92%       | 90%       |

|     | Current (A)                     |
|-----|---------------------------------|
| E2U | $253.23 \times x_1$             |
| CU  | $277.98 \times x_1$             |
| E1U | $246.2 \times x_1$              |
| M2U | $x_2$                           |
| M1U | $x_3$                           |
| FCU | $x_4$                           |
| FCD | $x_4$ (solenoid); $-x_4$ (flip) |
| M1D | 0                               |
| M2D | $x_5$                           |
| E1D | $246.2 \times x_6$              |
| CD  | $277.98 \times x_6$             |
| E2D | $253.23 \times x_6$             |

- In each run mode, we are able to deliver an ensemble of particles that can be cooled in the MICE Step IV lattice, with at least 90% transmission to the TOF2 without M1D. In most of them, the normalized transverse emit. reduction is more than 3%;



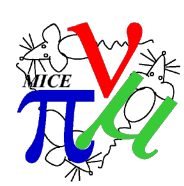
# You may have noticed that



- AFC module with LiH can not run above 185 A.

| variable                    | flip, 140 | flip, 200 | flip, 200 ( $x_4 \leq 185$ ) | flip, 240 | sol, 140 | sol, 200 | sol, 240 |
|-----------------------------|-----------|-----------|------------------------------|-----------|----------|----------|----------|
| $x_1$                       | 0.64      | 0.68      | 0.63                         | 0.80      | 0.75     | 0.72     | 0.89     |
| $x_2$                       | 116.40    | 150.40    | 231.91                       | 251.62    | 241.14   | 219.81   | 222.69   |
| $x_3$                       | 133.01    | 253.18    | 268.11                       | 150.98    | 225.42   | 162.66   | 146.06   |
| $x_4$                       | 181.21    | 222.94    | 184.73                       | 126.80    | 53.52    | 55.95    | 64.09    |
| $x_5$                       | -205.95   | -242.47   | -234.35                      | -244.00   | 147.05   | 205.66   | 161.48   |
| $x_6$                       | -0.71     | -0.5      | -0.51                        | -0.70     | 0.51     | 0.51     | 0.70     |
| $\Delta\epsilon/\epsilon_i$ | -7.7%     | -4.0%     | -3.7%                        | -2.2%     | -2.2%    | -2.8%    | -2.3%    |
| $T$                         | 93%       | 93%       | 93%                          | 90%       | 91%      | 92%      | 90%      |

From Flip, 200 with and without the constraint on FC current:  
Performance not as good when constrained;  
Showed a preference of higher FC current  
Still doable



# You may have worried that

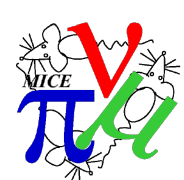


- Tracker resolution becomes a problem with  $B_z \sim 2T$

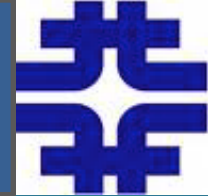
| variable                    | flip, 140 | flip, 200 | flip, 200 ( $x_4 \leq 185$ ) | flip, 240 | sol, 140 | sol, 200 | sol, 240 |
|-----------------------------|-----------|-----------|------------------------------|-----------|----------|----------|----------|
| $x_1$                       | 0.83      | 0.72      | 0.72                         | 0.80      | 0.80     | 0.77     | 0.89     |
| $x_2$                       | 142.56    | 168.13    | 233.49                       | 251.62    | 132.76   | 249.89   | 222.69   |
| $x_3$                       | 125.55    | 261.81    | 262.59                       | 150.98    | 205.79   | 276.14   | 146.06   |
| $x_4$                       | 180.83    | 221.55    | 184.91                       | 126.80    | 65.21    | 86.61    | 64.09    |
| $x_5$                       | -191.34   | -233.37   | -237.68                      | -244.00   | 223.01   | 208.29   | 161.48   |
| $x_6$                       | -0.73     | -0.74     | -0.74                        | -0.70     | 0.73     | 0.74     | 0.70     |
| $\Delta\epsilon/\epsilon_i$ | -7.4%     | -4.0%     | -3.5%                        | -2.2%     | -4.6%    | -3.5%    | -2.3%    |
| $T$                         | 92%       | 92%       | 93%                          | 90%       | 91%      | 92%      | 90%      |

New constraint applied: minimum  $B_z$   
in trackers = 2.8 T  
Results slightly worse but still  
doable.

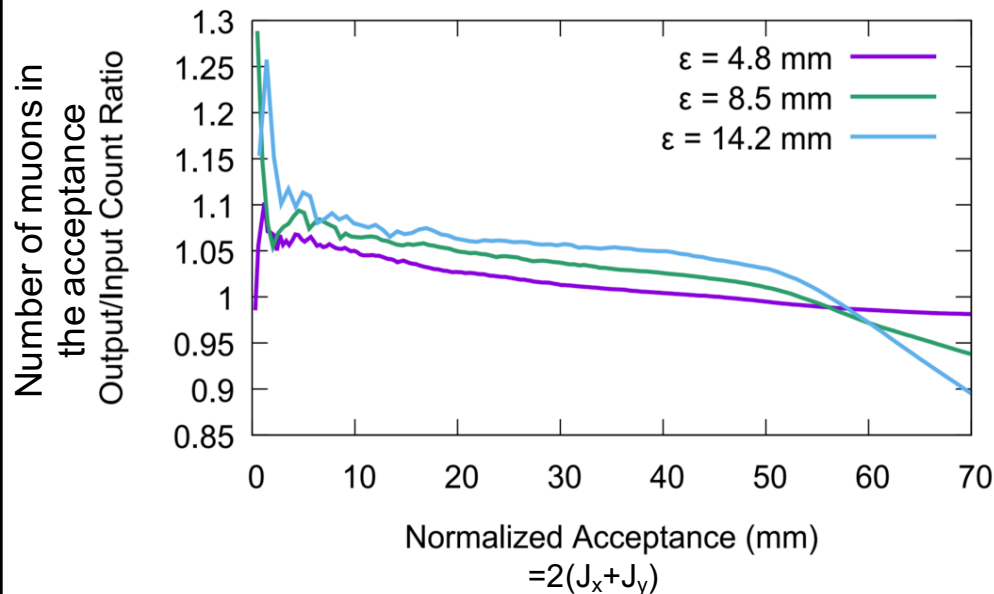
More emit. reduction between  
ref. planes but stronger emit.  
growth after ref. plane in SSD.  
Objective fitness was ~ same.



# 200 MeV/c flip mode – from the above-shown optimization result



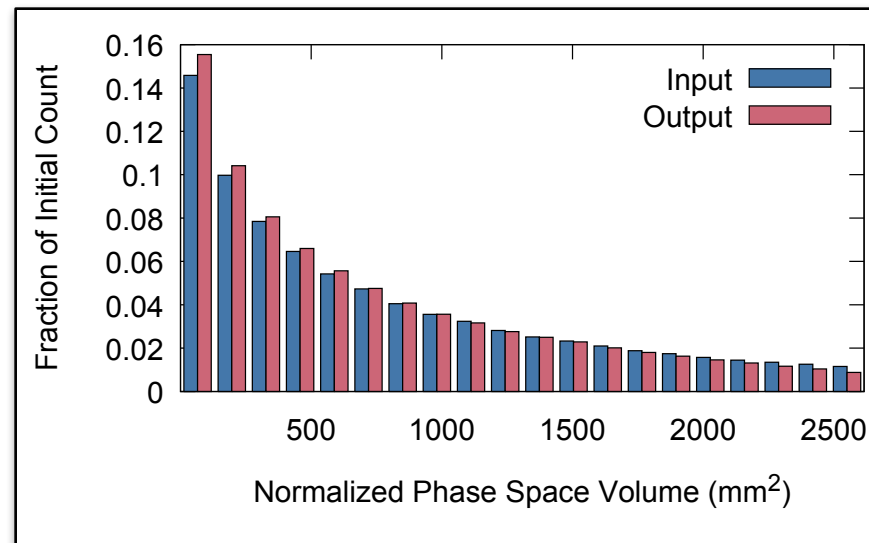
- Check the phase space density at the two ref. planes:

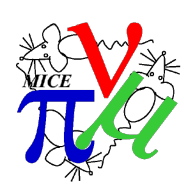


A ratio that is larger than 1 shows cooling in that acceptance;

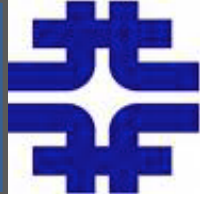
Courtesy of J. Scott Berg, BNL.

Loss taken into account – not fooled by losing only muons with more MCS to reduce RMS normalized emit.





# Optimization result – no M1D nor M2D



| variable                    | flip, 140<br>(low T) | flip, 140<br>(high T) | flip, 200<br>(low T) | flip, 200<br>(high T,<br>low $x_4$ ) | sol, 140<br>(low T,<br>no high T) | sol, 200<br>(high T) | sol, 240<br>(high T) |
|-----------------------------|----------------------|-----------------------|----------------------|--------------------------------------|-----------------------------------|----------------------|----------------------|
| $x_1$                       | 0.71                 | 0.77                  | 0.89                 | 0.70                                 | 0.65                              | 0.76                 | 0.65                 |
| $x_2$                       | 80.00                | 169.49                | 153.19               | 125.73                               | 172.39                            | 236.83               | 158.43               |
| $x_3$                       | 158.14               | 208.96                | 251.15               | 133.93                               | 242.20                            | 135.21               | 132.32               |
| $x_4$                       | 172.05               | 118.23                | 224.99               | 88.85                                | 56.15                             | 55.98                | 64.11                |
| $x_5$                       | 0                    | 0                     | 0                    | 0                                    | 0                                 | 0                    | 0                    |
| $x_6$                       | -0.56                | -0.53                 | -0.5                 | -0.51                                | 0.57                              | 0.54                 | 0.57                 |
| $\Delta\epsilon/\epsilon_i$ | 12.8%                | 6.8%                  | 6.3%                 | 1%                                   | 8.2%                              | 2.6%                 | 2.7%                 |
| $T$                         | 72%                  | 80%                   | 74%                  | 85%                                  | 73%                               | 82%                  | 80%                  |

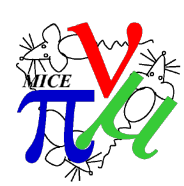
It is possible but more difficult to pursue Step IV with M2D off:

1. Requires (obviously) low ECE current downstream;
2. Challenges are data collection inefficiency and understanding the outcome from the big loss
3. More MC analyses are needed to be affirmative





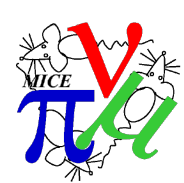
# Ckov Light Yield



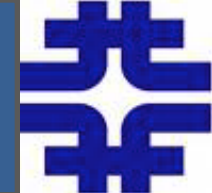
# Redone the analyses



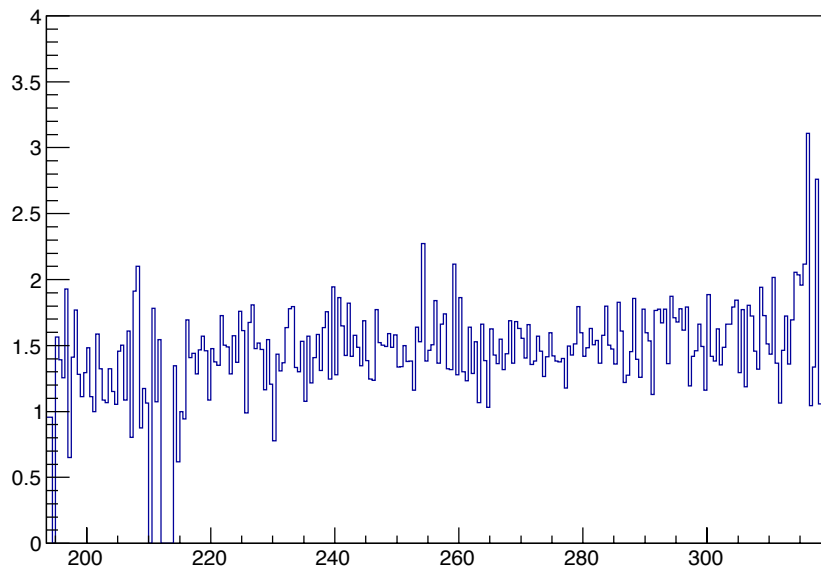
- Previous: calculated the TOF based on the distance in the geometry
  - Approximation turned out to be not good enough
- Redo:
  - Use the electron TOF;
  - Consider that D1 and D2 select the same momentum, optics should be the same for pi, mu, e, therefore same path lengths



# Ckov A

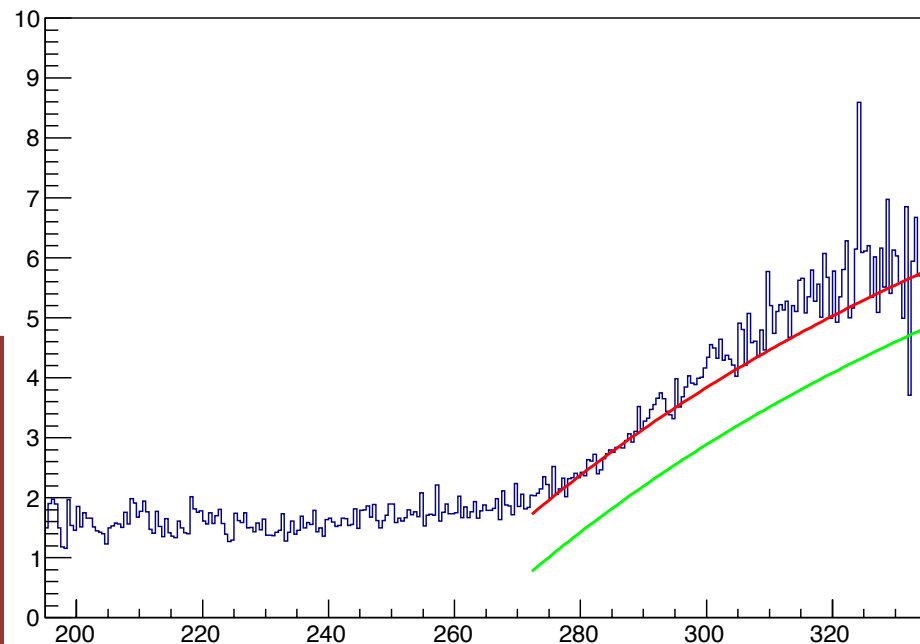


Avg\_#\_of\_CkovA\_pes\_v.s.\_momentum\_PID=211

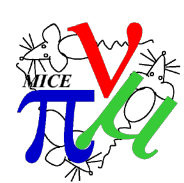


Compare with the light yield formula in note 473:  $f = 0.75 + 12 \times [1 - (272/p)^2]$   
Background light yield was observed to be higher: (Red:  $f+0.95$ )

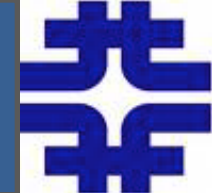
Avg\_#\_of\_CkovA\_pes\_v.s.\_momentum\_PID=-13



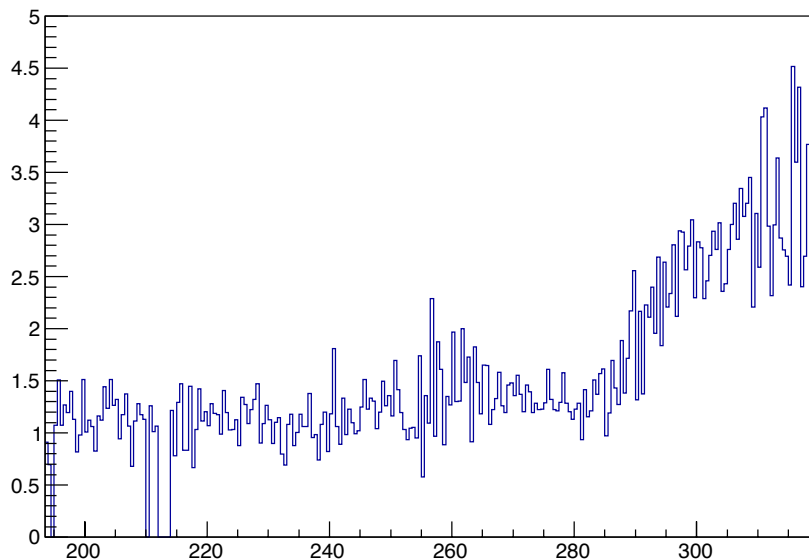
Note 473:  
367.9 MeV/c for pions;  
280.5 MeV/c for muons, but from the formula should be around 272 MeV/c, which was consistent with the scan;



# Ckov B

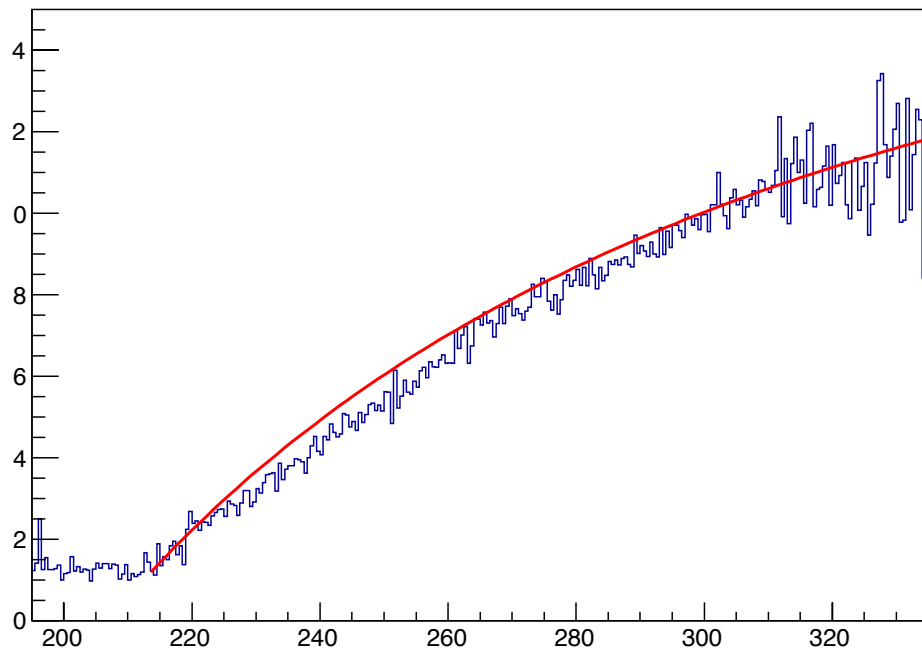


Avg\_#\_of\_CkovB\_pes\_v.s.\_momentum\_PID=211

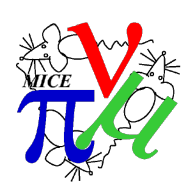


Compare with the light yield formula in note 473:  $f = 1.1 + 18 \times [1 - (213/p)^2]$   
Consistent results

Avg\_#\_of\_CkovB\_pes\_v.s.\_momentum\_PID=-13



Note 473:  
285.8 MeV/c for pions;  
217.9 MeV/c for muons;



# Lack of data and action



- Lack of data at high momentum;
- Lack of pion data
  - For the last Ckov scan runs, DS was fixed and was running as a high current;
  - If we could get some pion runs to fill the data we probably could see the Ckov A turns on at higher momentum
- Waiting for a designated but short momentum scan run.