

Hadronic Modelling in Geant4

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(on behalf of Geant4 Collaboration)

Used many slides from talks of Dennis Wright
at Hadronic Shower Simulation Workshop
FNAL, 6-8 September 2006

Overview

- Key characteristics of modelling
- A tour of key hadronic models
 - String Models $E > 5-10$ GeV
 - Cascades: ~ 150 MeV $< E < 3-10$ GeV
 - CHIPS
 - Pre-compound/Evaporation
- Latest developments, known limitations

- Can models be 'tuned' ?

Hadronic Inelastic Model Inventory

CHIPS

At rest
Absorption
 μ , π , K, anti-p

Hadron-nuclear CHIPS

Photo-nuclear, lepto-nuclear (CHIPS)

High precision neutron

Evaporation

Fermi breakup

Multifragment

γ de-excitation

Pre-
compound

Binary cascade

FTF String

QG String

Radioactive
Decay

Bertini cascade

INCL cascade

Fission

HEP

LEP

1 MeV

10 MeV

100 MeV

1 GeV

10 GeV

100 GeV

1 TeV

Survey of Hadronic Models

- **Three broad categories of models:**
 - tabulated: based on (large) databases
 - For neutrons ($E < 20$ MeV), photon de-excit.
 - parametrized: key aspects parameterised for speed
 - Parameters determined from fits to data
 - theory-based: based on (theoretical) models
 - Parameters chosen by comparing with thin-target data

'Theory-based' models

Phenomenology-based really.

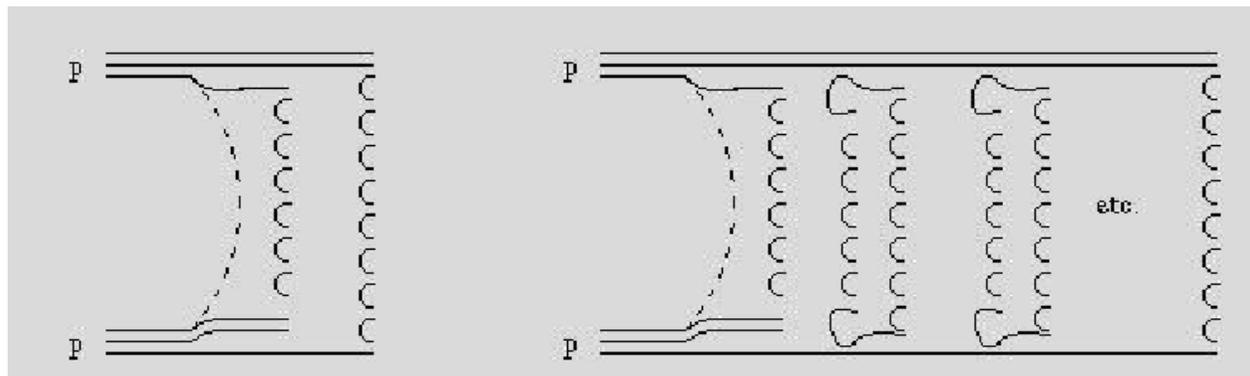
- Evaporation and pre-compound models
 - Use well-established recipes
- Cascade and CHIPS
 - Bertini-like
 - Binary Cascade
 - Chiral Invariant Phase Space
- Quark-Gluon String (QGS) model
 - Alternative FTF model, using Fritiof approach

Quark-Gluon String Model: Applicability

- Incident p, n, π, K
 - $\sim 20 \text{ GeV} < E < 50 \text{ TeV}$
- Also for high energy γ - nuclear
 - $\sim 5 \text{ GeV} < E < 50 \text{ TeV}$
- Model handles:
 - Selection of collision partners
 - Splitting of nucleons into quarks and diquarks
 - Formation and excitation of quark-gluon string
 - String hadronization

Quark Gluon String Model

- Two or more strings may be stretched between partons within hadrons
 - Strings from cut cylindrical Pomerons
- Parton interaction leads to color coupling of valence quarks
 - sea quarks included too
- Partons connected by quark gluon strings, which hadronize

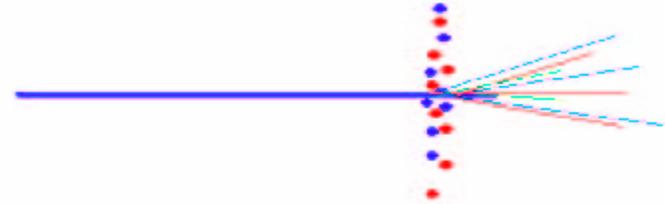


QGS Model

Options for 'back-end'

- Damaged nucleus handed to other Geant4 model
 - nuclear fragmentation and de-excitation
 - re-interaction of products (optional)
- Options for handling damaged nucleus:
 - pre-compound model (QGS/Preco – in QGSP)
 - CHIPS for nuclear fragmentation (QGS/Chips – labelled QGSC in physics lists naming)
 - Binary cascade reinteracts products (QGS/Binary in QGS_BIC)

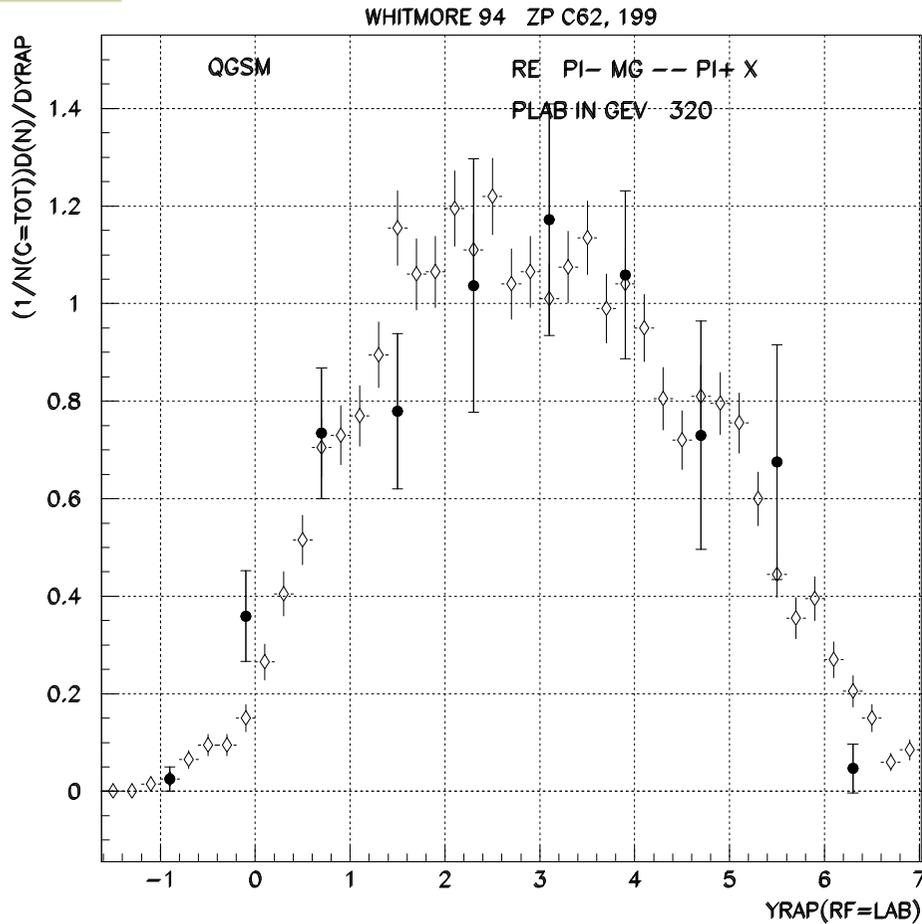
Quark Gluon String Model Algorithm



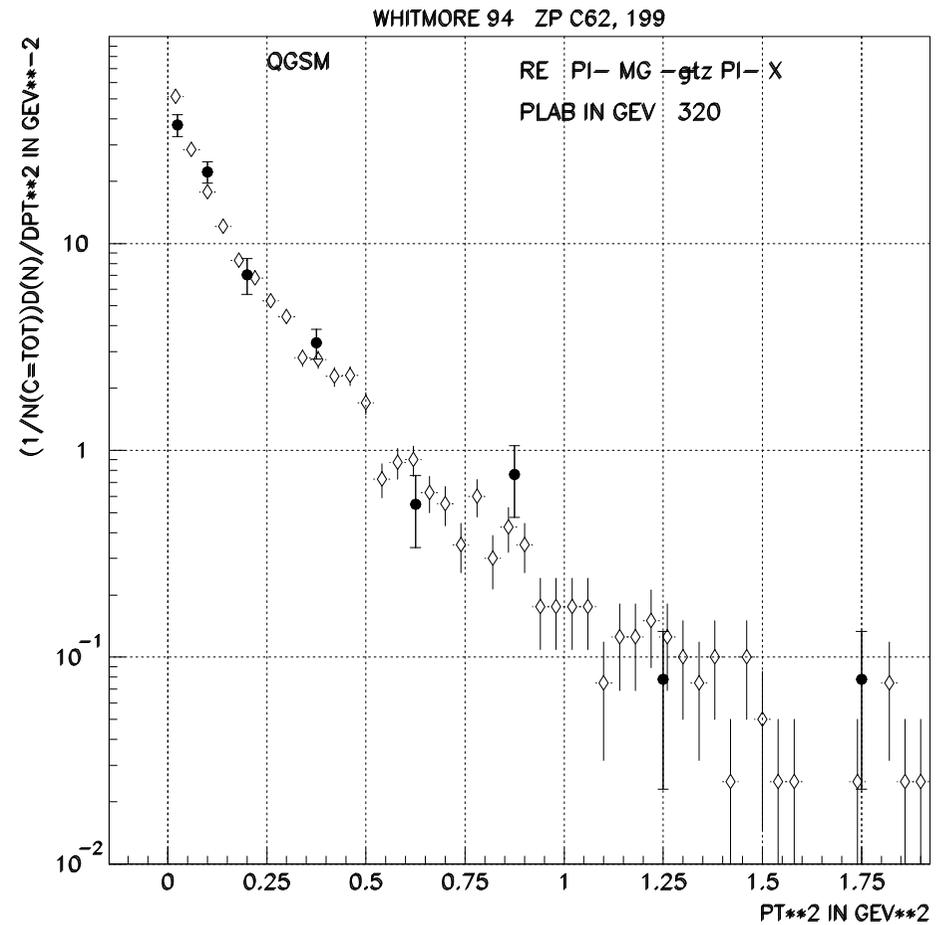
- Build up 3-dimensional model of nucleus
- Large γ -factor collapses nucleus to 2 dimensions
- Calculate impact parameter with all nucleons
- Calculate hadron-nucleon collision probabilities
 - based on quasi-eikonal model, using Gaussian density distributions for hadrons and nucleons
- Sample number of strings exchanged in each collision
- Unitarity cut, string formation and decay

QGSM - Results

$\pi^- \text{ Mg} \rightarrow \pi^+ X$, $P_{\text{lab}} 320 \text{ GeV}/c$ (Whitmore)

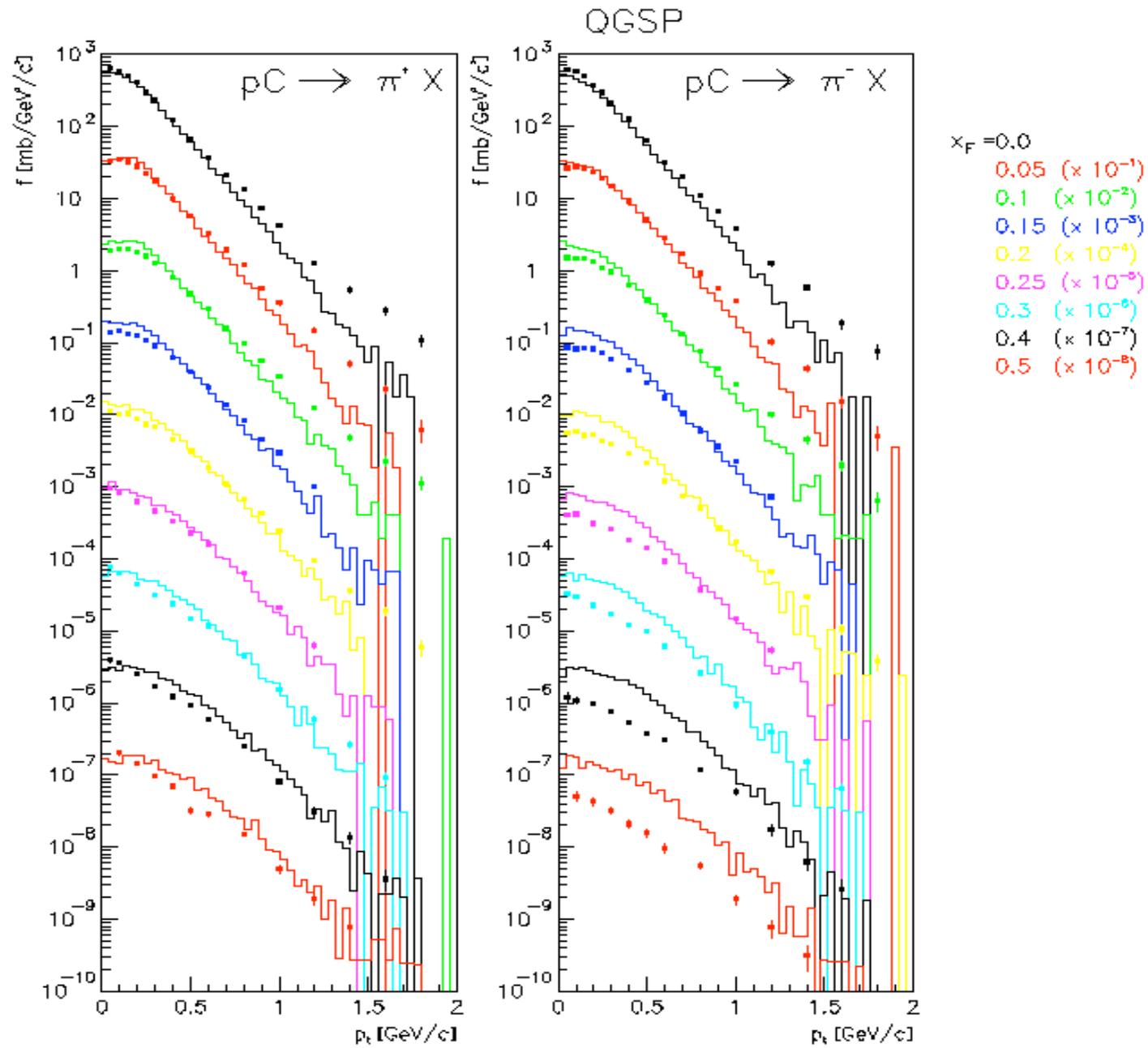


$$\text{Rapidity } \eta = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right)$$

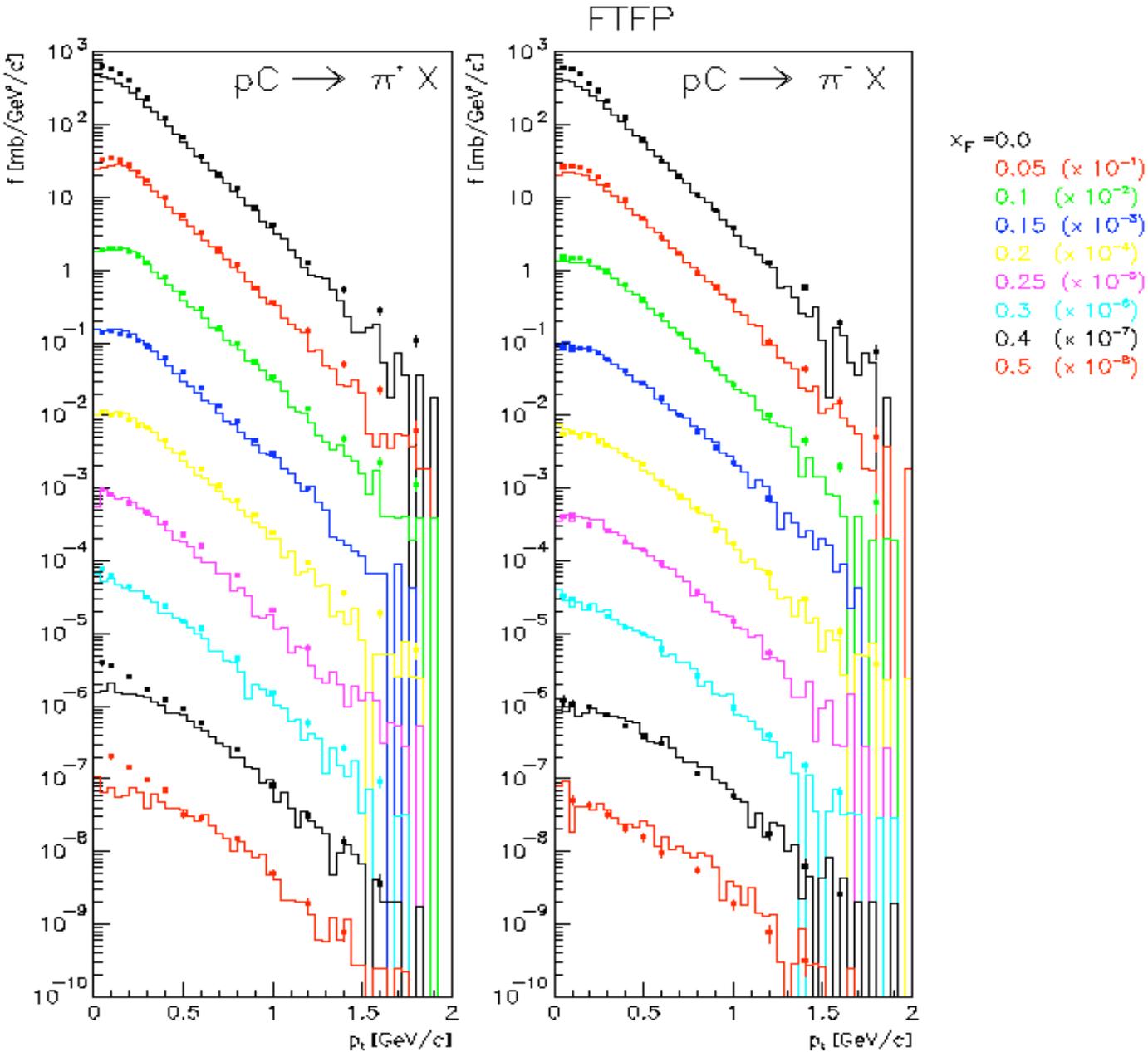


$$P_t^2 [\text{GeV}^2]$$

NA49 158 GeV/c (QGSP)

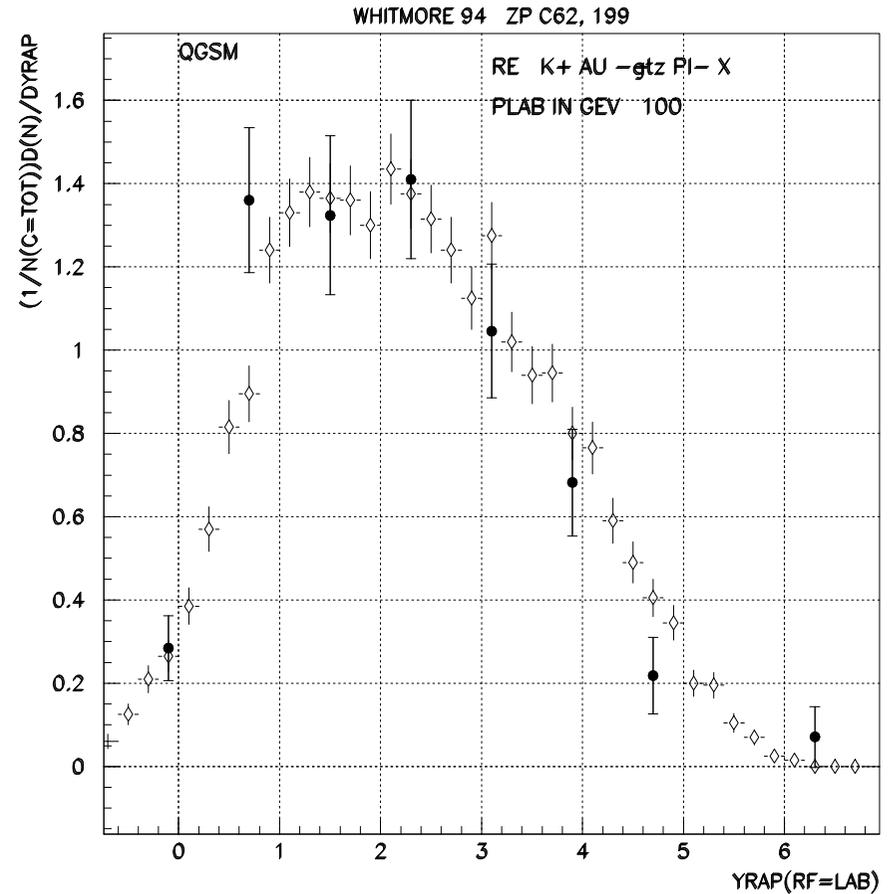
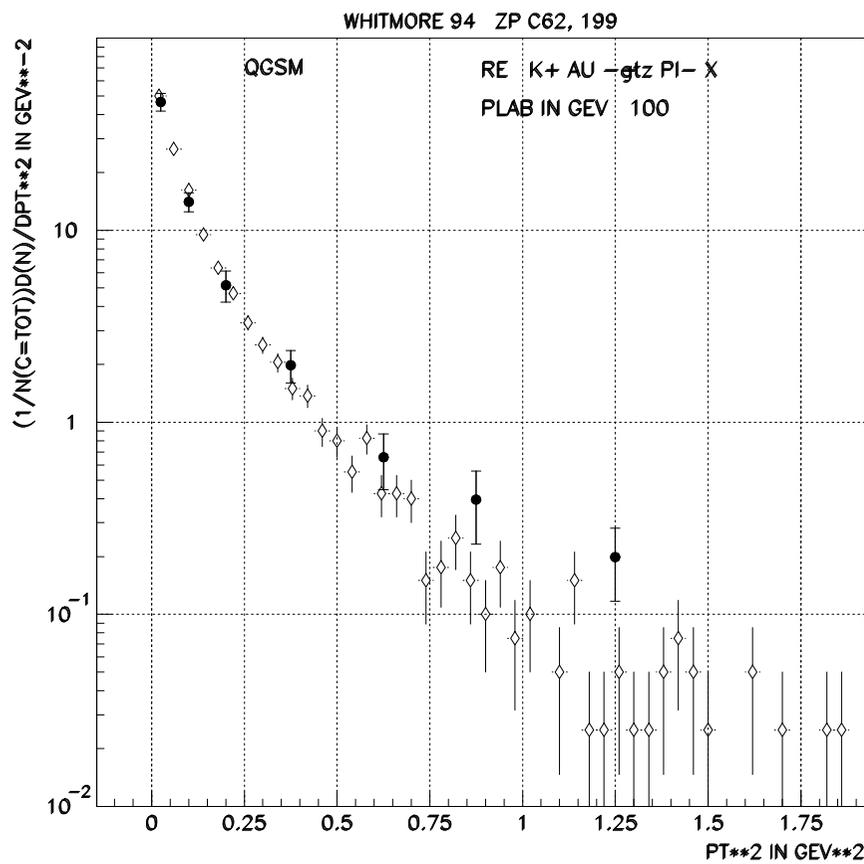


NA49 158 GeV/c (FTFP)



QGS Model Validation

K+ Scattering from Au (π^- inclusive)

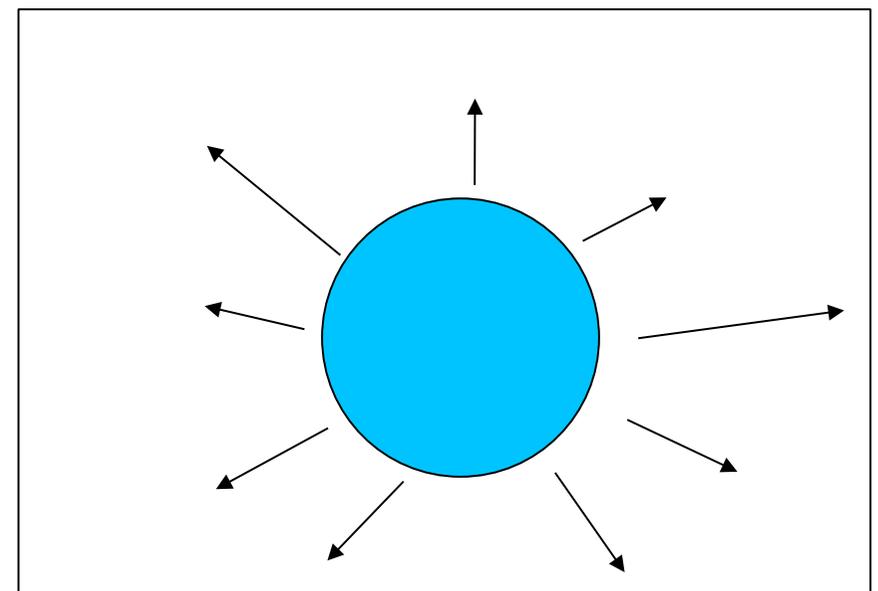
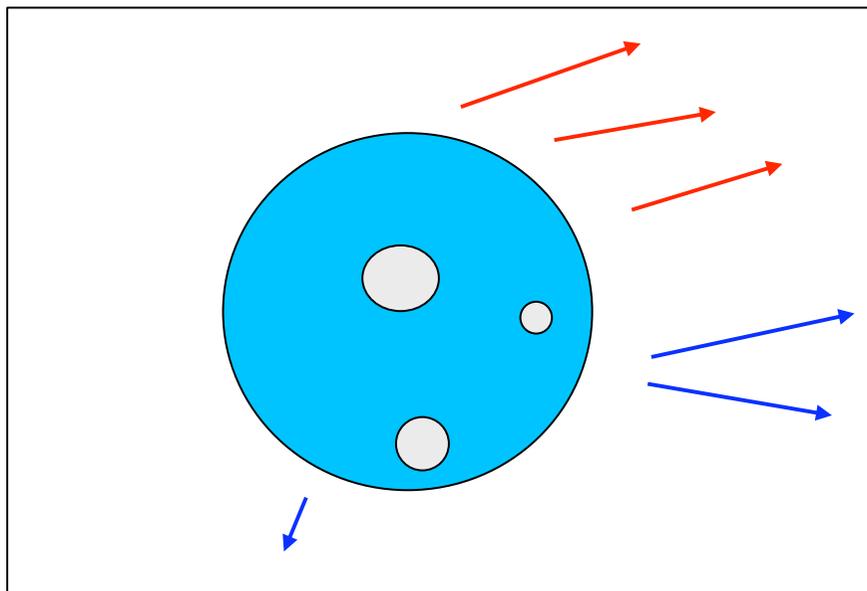
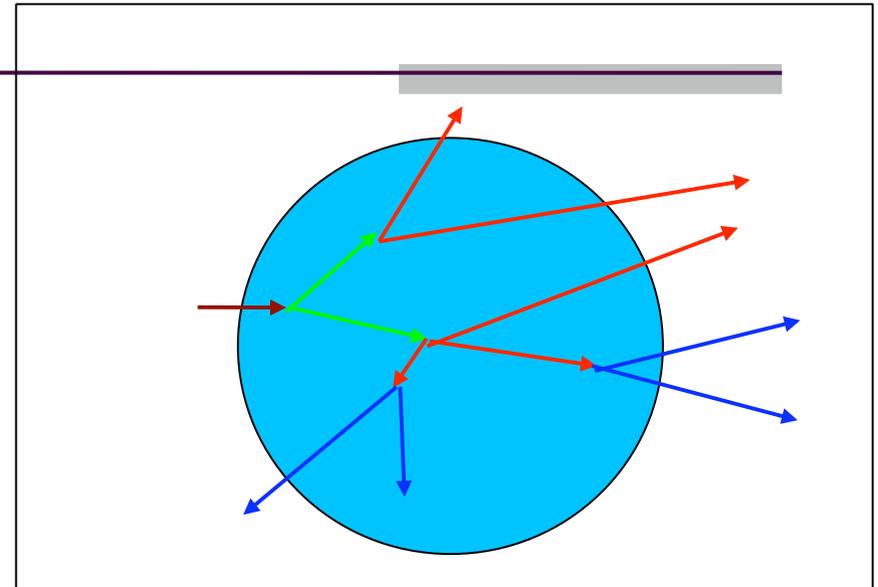
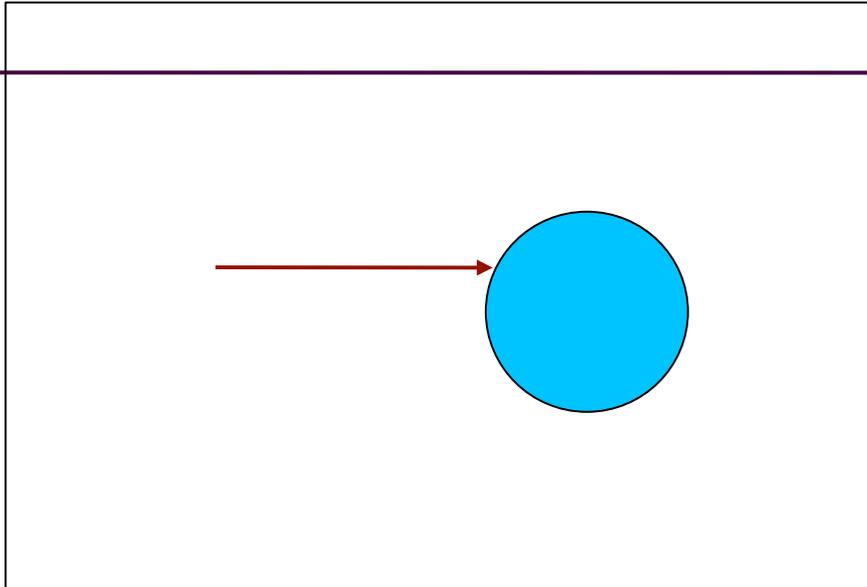


Solid dots: J.J.Whitmore et.al., Z.Phys.C62(1994)199

Description of High Energy Benchmarks

- [http:// geant4.fnal.gov/hadronic_validation/validation_plots.htm](http://geant4.fnal.gov/hadronic_validation/validation_plots.htm)
- 100 GeV/c (π^- , π^-X), (π^- , $\pi^+ X$) on Au
 - Whitmore, 1994
 - dN/dy vs y (rapidity)
- 158 GeV/c (p , πX) on C
 - NA49, 2007
 - Double differential cross section vs p_T , x_F
- 250 GeV/c (π^+ , charged) on Al, Au
 - NA22, 1991
 - Double particle density vs y
- 320 GeV/c (π^- , π^-X), (π^- , $\pi^+ X$) on Au
 - Whitmore, 1994
 - dN/dp_T vs p_T , dN/dy vs y
- 400 GeV/c (p , π^+X) on Ta
 - Bayukov, 1980
 - Invariant cross section vs kinetic energy

Cascade Modeling Concept



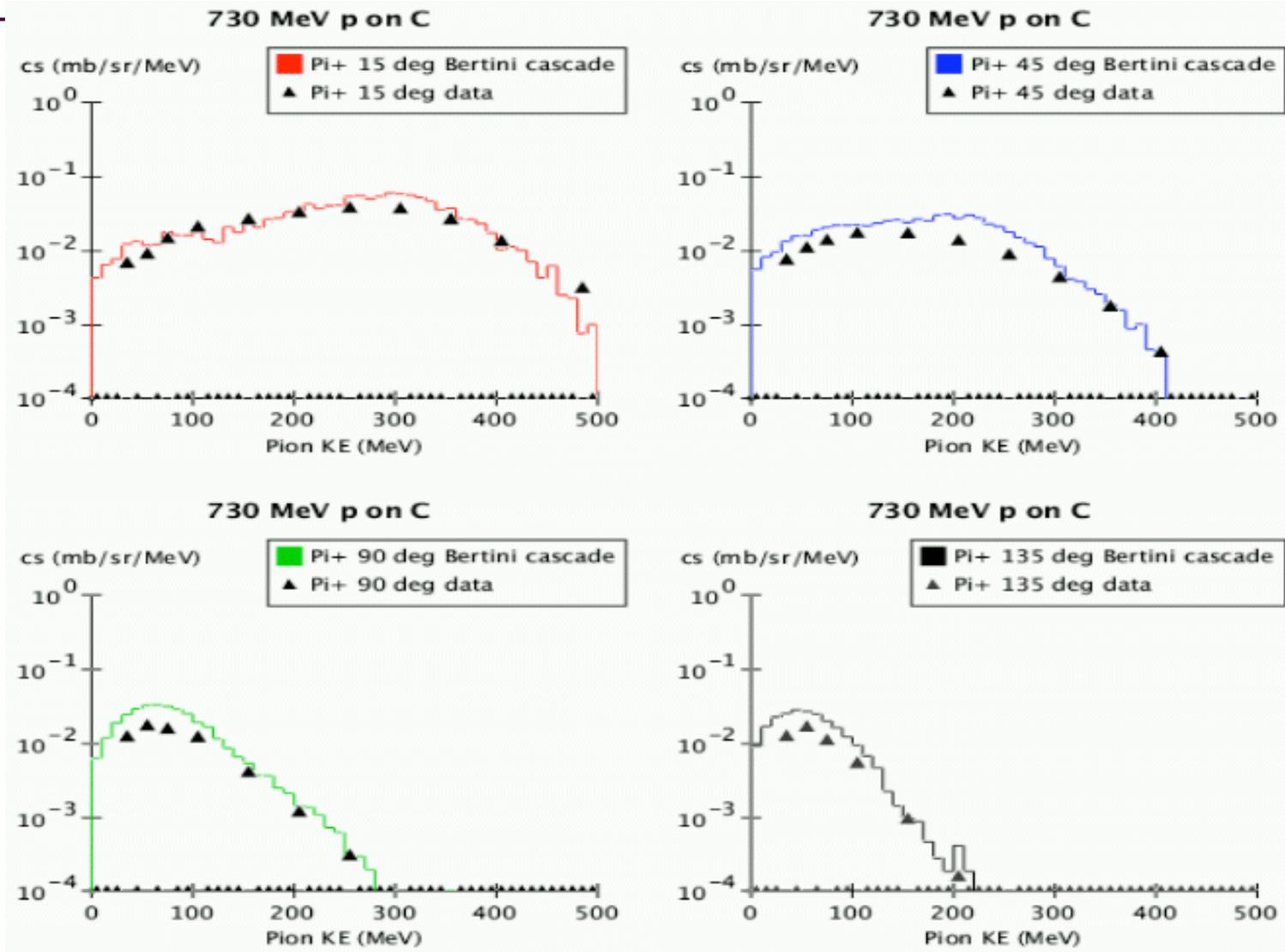
Applicability of the Bertini Cascade

- inelastic scattering of p , n , π , K , Λ , Σ , Ξ
- incident energies: $0 < E < 10$ GeV
 - upper limit determined by lack of partial final state cross sections and the end of the cascade validity region
 - lower limit due to inclusion of internal nuclear de-excitation models
- in principle, can be extended to:
 - anti-baryons
 - ion-ion collisions

Geant4 Bertini Cascade: Origin

- Employs standard INC methods from Bertini (1968)
 - using free particle-particle collisions within cascade
 - step-like nuclear density
- Core code:
 - elementary particle collider: uses free cross sections to generate secondaries
 - cascade in nuclear medium
 - pre-equilibrium and equilibrium decay of residual nucleus
 - nucleus modelled as three concentric spheres of different densities; density constant within sphere

Validation of the Bertini Cascade



Applicability of the Binary Cascade

- Incident p, n
 - $0 < E < \sim 3 \text{ GeV}$
- light ions
 - $0 < E < \sim 3 \text{ GeV/A}$
- π
 - $0 < E < \sim 1.5 \text{ GeV}$

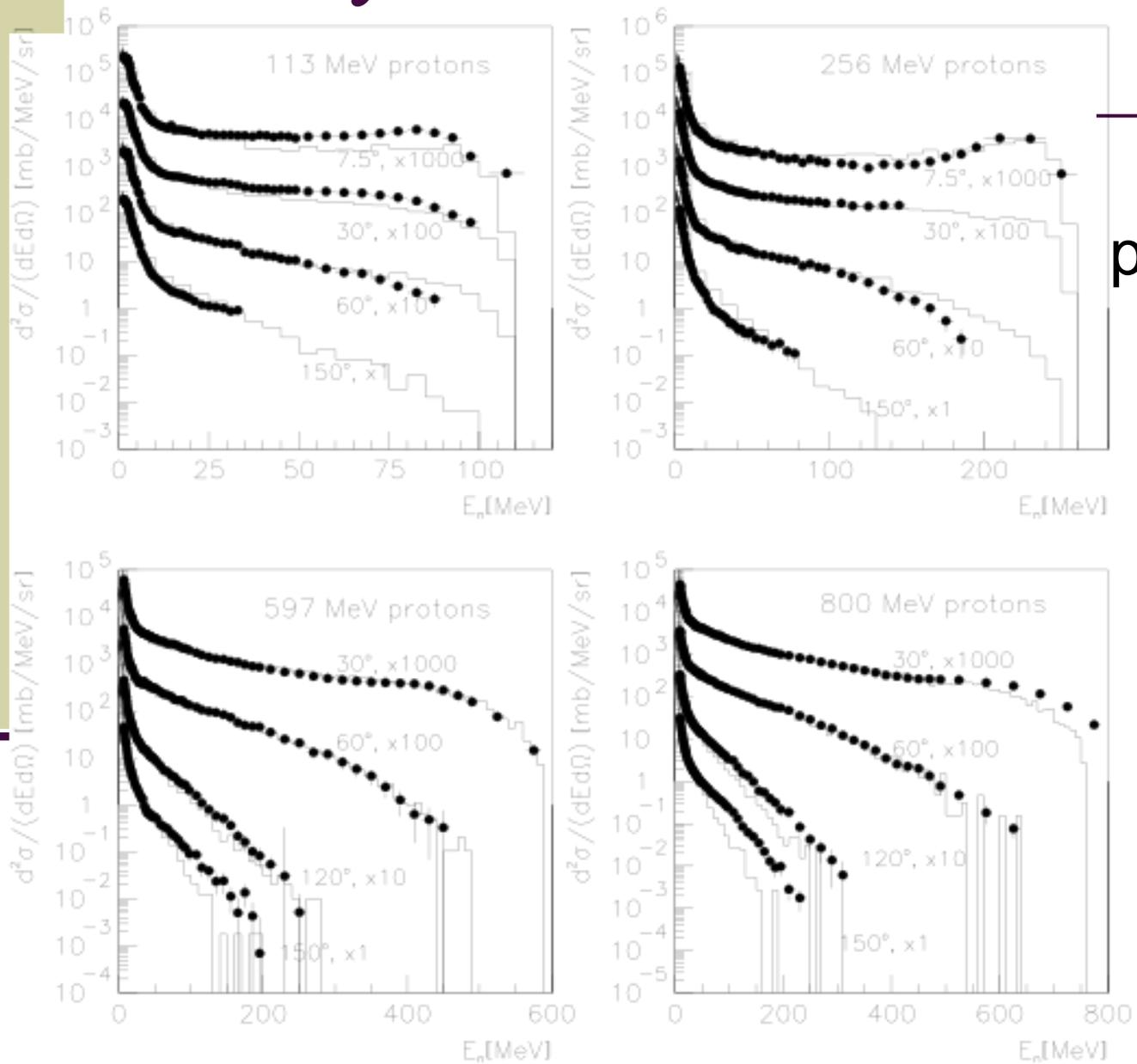
Binary Cascade

- Hybrid between classical cascade and full QMD model
- Detailed model of nucleus
 - nucleons placed in space according to nuclear density
 - nucleon momentum according to Fermi gas model
- Nucleon momentum taken into account when evaluating cross sections, collision probability
- Collective effect of nucleus on participant nucleons described by optical potential
 - numerically integrate equation of motion

Binary Cascade Modelling

- **Resonances** (to $\Delta 1950$, $N^* 2250$)
 - Created in NN scattering (t-channel) – use pp data σ
 - may interact or decay
- NN elastic scattering angular distributions
 - from Arndt phase shift analysis of exp. data
- Pauli blocking for final state nucleons
- Pion absorption on pseudo-deuterons
- Coulomb barrier present for charged hadrons
- Stop cascade when $\langle E \rangle$ below A-dependent cut

Binary Cascade - results

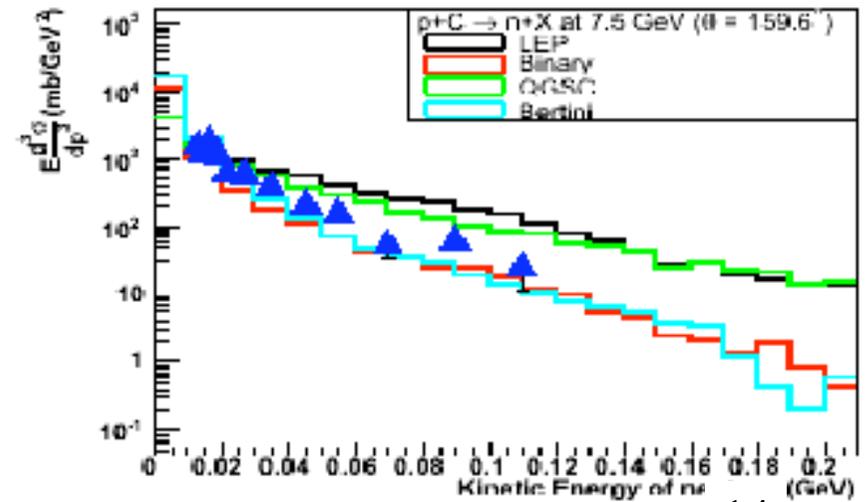
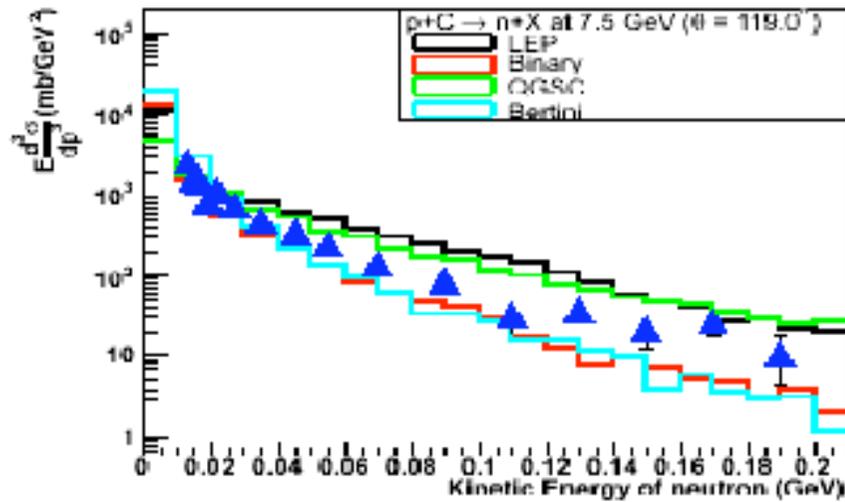
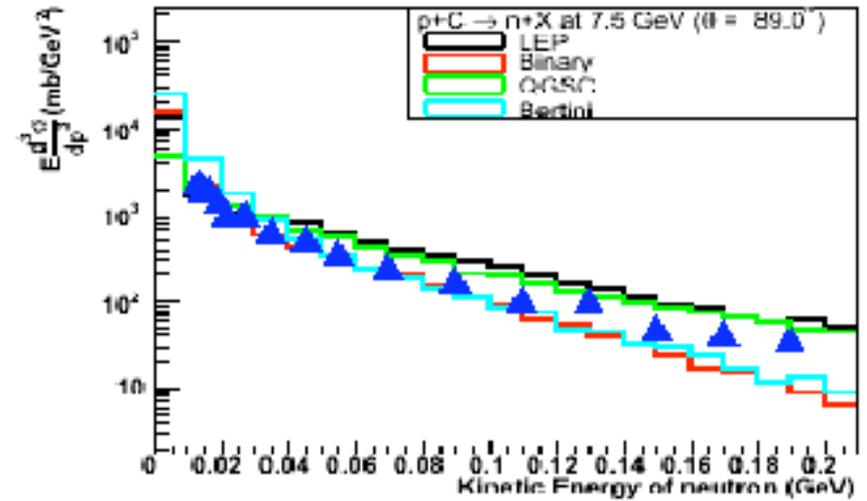
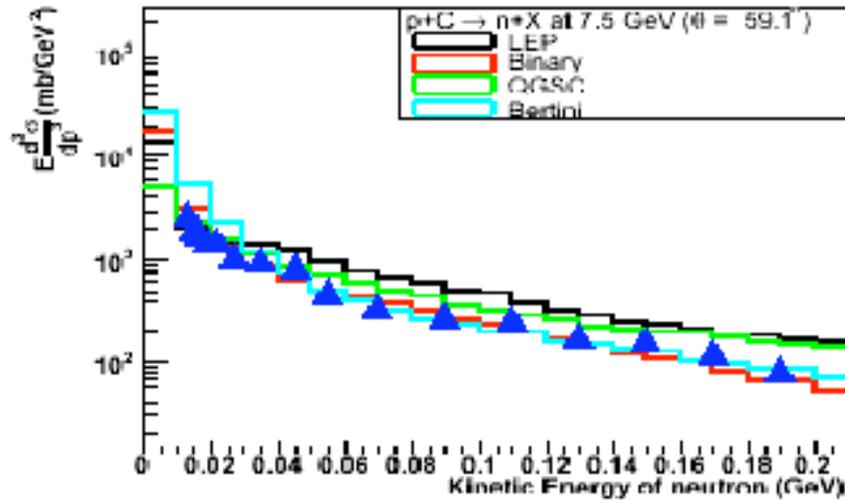


p Pb -> n X

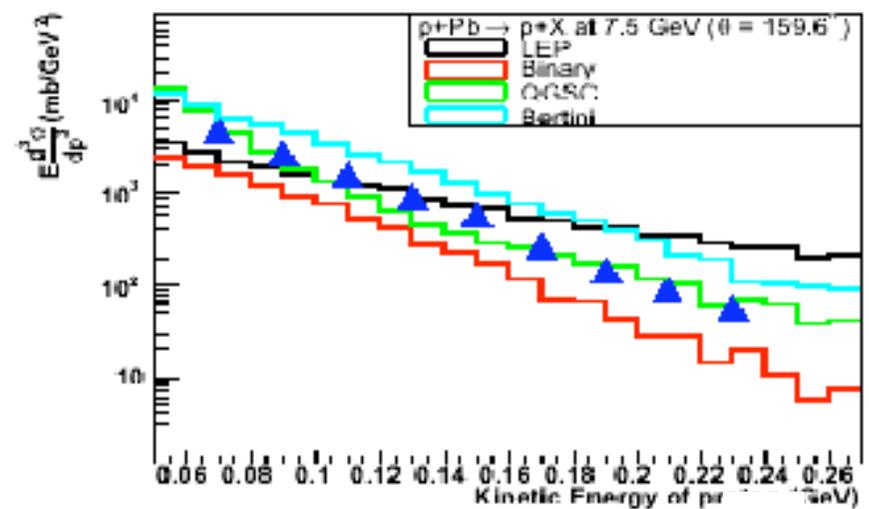
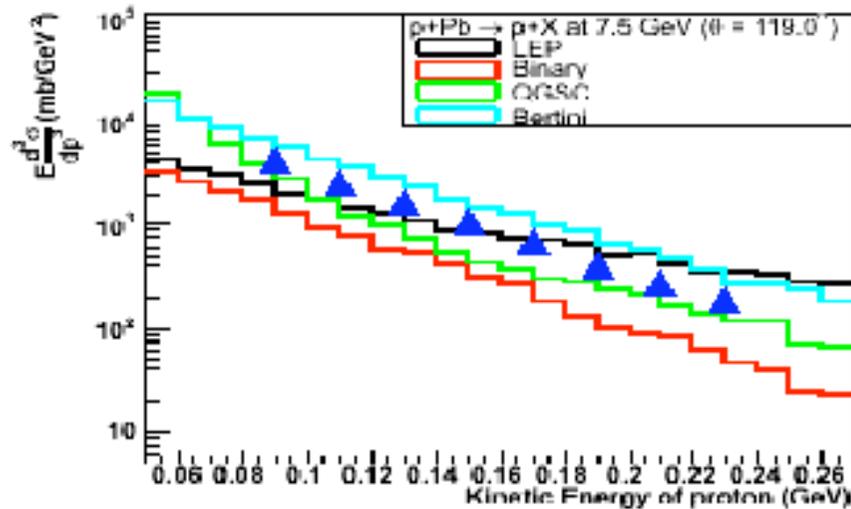
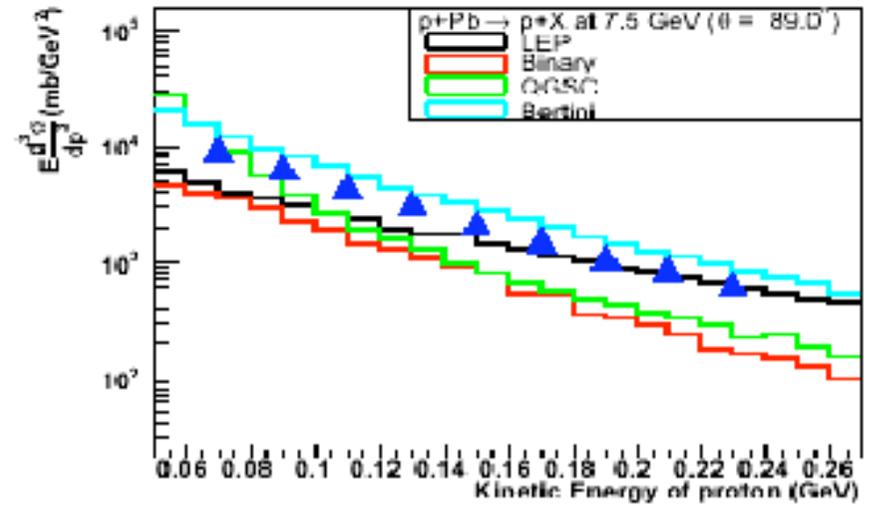
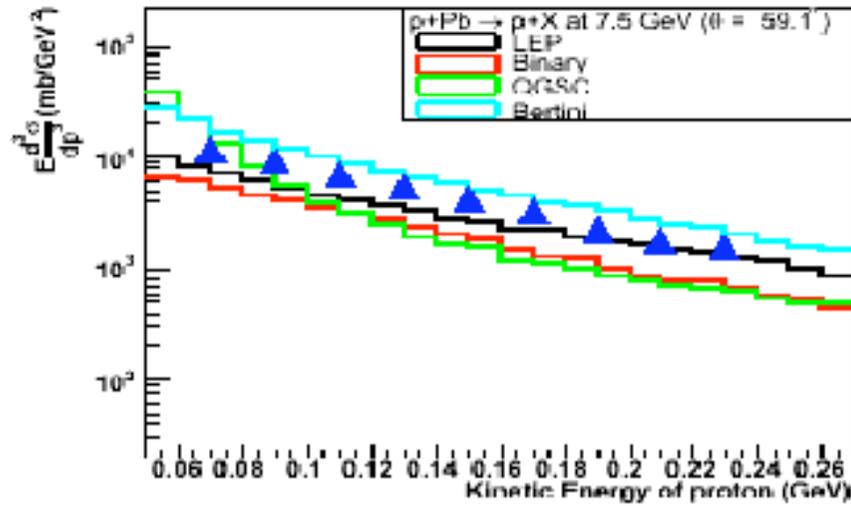
Overview of Medium Energy Benchmarks

- [http:// geant4.fnal.gov/hadronic_validation/validation_plots.htm](http://geant4.fnal.gov/hadronic_validation/validation_plots.htm)
- 1.4 – 9.0 GeV (p,pX) on Be, C, Cu, Pb, U
 - Bayukov, 1985
 - Invariant cross section vs kinetic energy
- 1.4 – 5.0 GeV (π^+ ,p), (π^+ ,n) on Be, C, Cu, Pb, U
 - Bayukov, 1985
 - Invariant cross section vs kinetic energy
- 14.6 GeV/c (p, π^+ X), (p, π^- X) on Be, Al, Cu, Au
 - Abbot, 1992
 - Invariant cross section vs transverse mass
- 14.6 GeV/c (p,pX) on Cu
 - Abbot, 1992
 - Invariant cross section vs transverse mass

7.5 GeV (p,nX) on C



7.5 GeV (p,pX) on Pb



Chiral Invariant Phase Space (CHIPS)

- **Origin: M.V. Kosov (CERN, ITEP)**
 - Manual for the CHIPS event generator, KEK internal report 2000-17, Feb. 2001 H/R.
- **Use:**
 - capture of negatively charged hadrons at rest
 - anti-baryon nuclear interactions
 - gamma- and lepto-nuclear reactions
 - back end (nuclear fragmentation part) of QGSC model

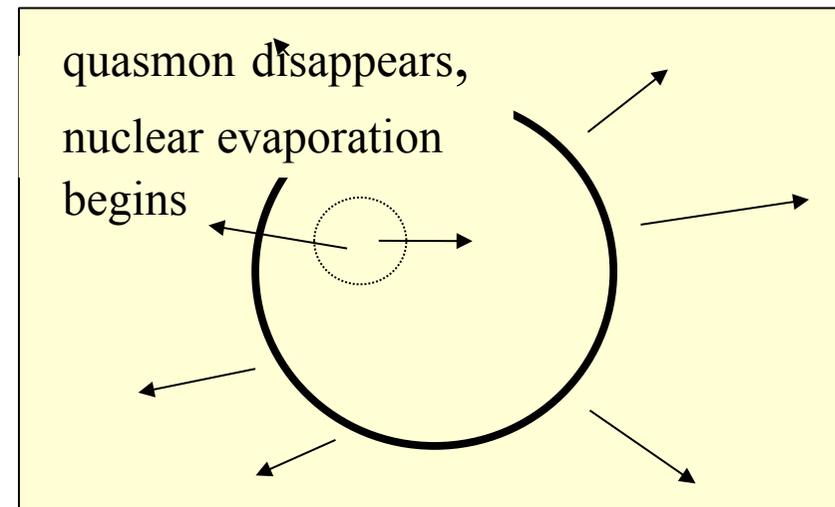
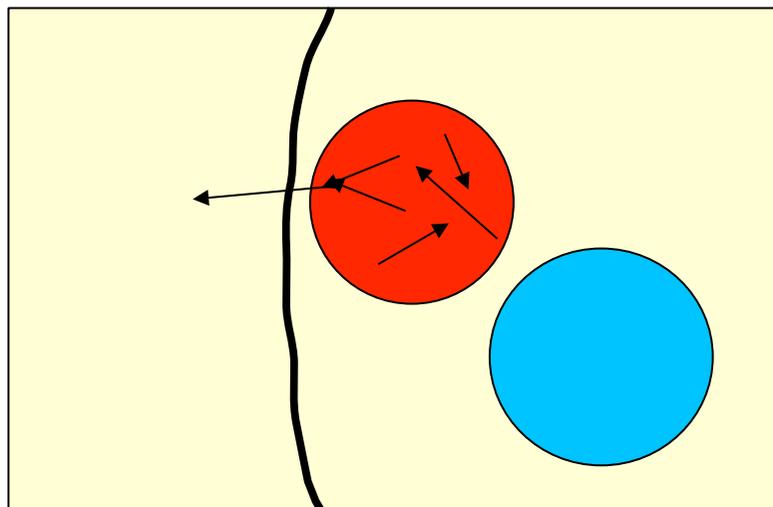
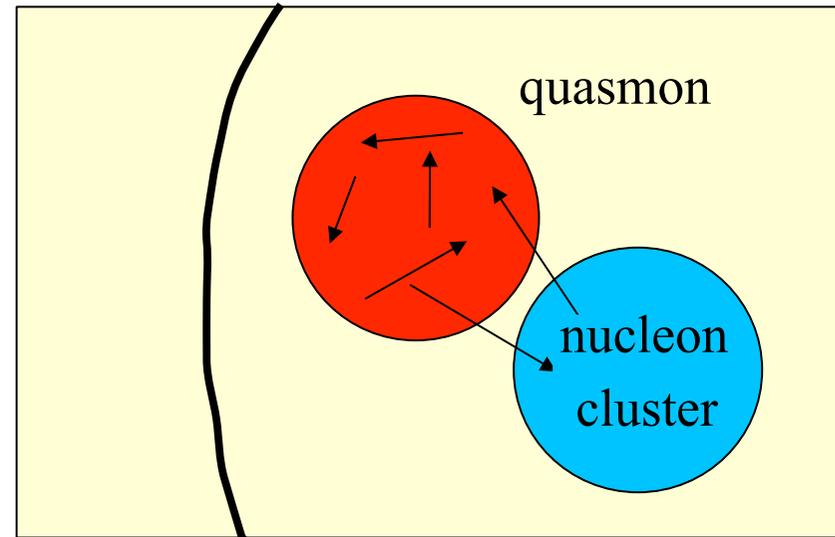
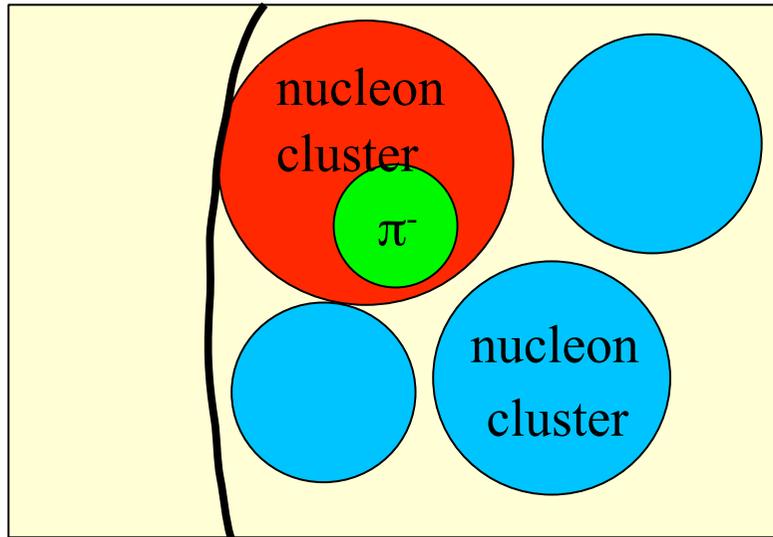
CHIPS Fundamental Concepts

- **Quasmon**: an ensemble of massless partons uniformly distributed in invariant phase space
 - a 3D bubble of quark-parton plasma
 - can be any excited hadron system or ground state hadron
- **Critical temperature T_c** : model parameter which relates the quasmon mass to the number of its partons:
 - $M_Q^2 = 4n(n-1)T_c^2 \Rightarrow M_Q \sim 2nT_c$
 - $T_c = 180 - 200 \text{ MeV}$
- **Quark fusion hadronization**: two quark-partons may combine to form an on-mass-shell hadron
- **Quark exchange hadronization**: quarks from quasmon and neighbouring nucleon may trade places

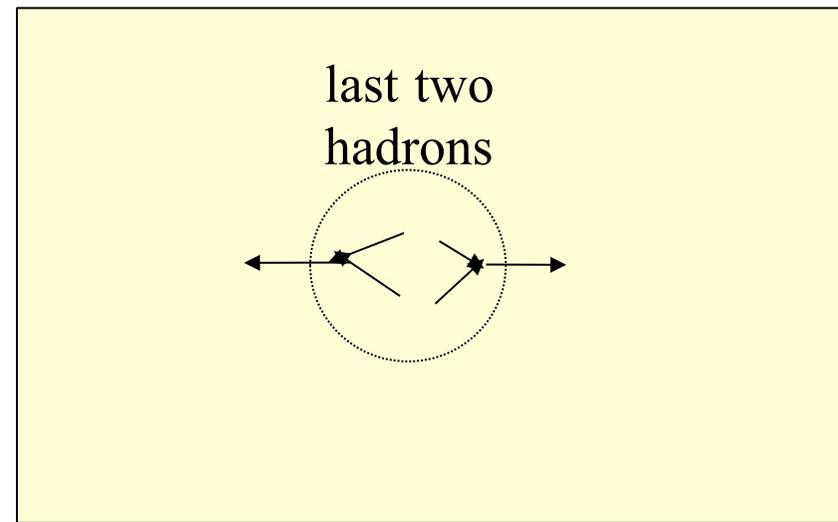
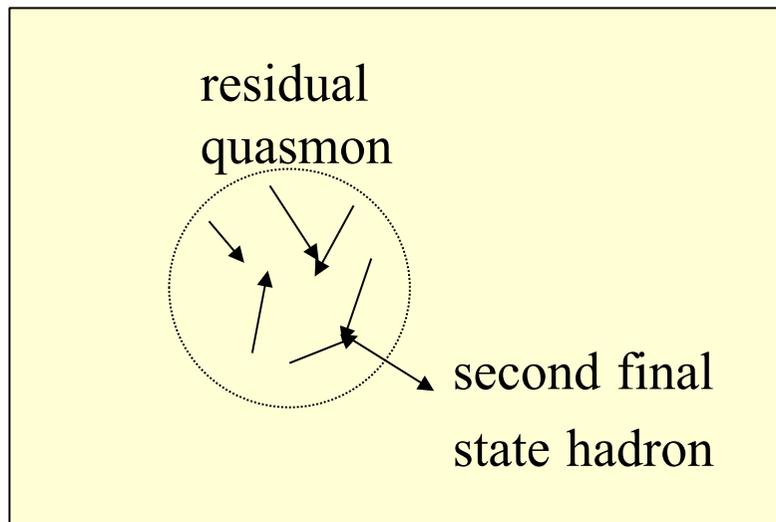
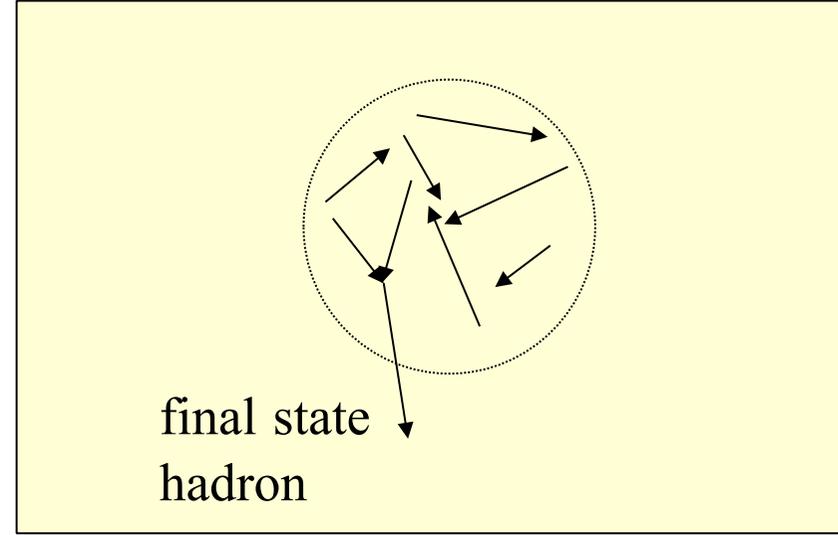
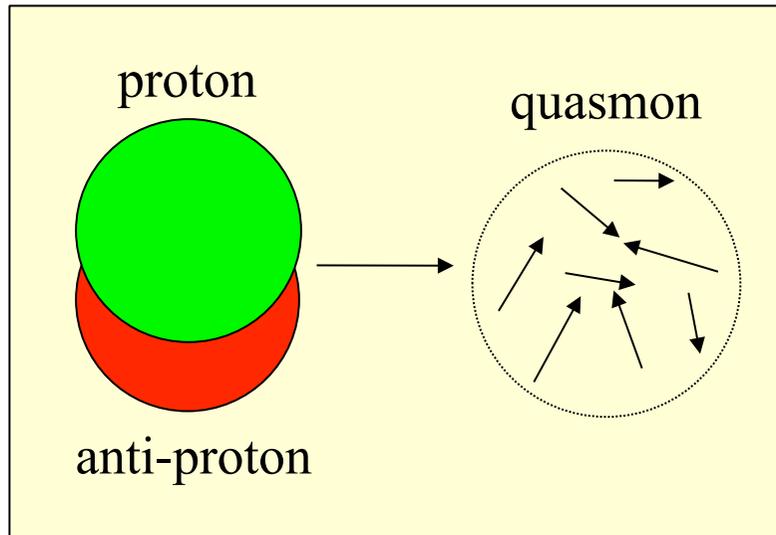
CHIPS Applications

- u,d,s quarks treated symmetrically (all massless)
 - model can produce kaons, but s suppression parameter is needed, η suppression parameter also required
 - real s-quark mass is taken into account by using masses of strange hadrons
- CHIPS is a universal method for fragmentation of excited nuclei (containing quasmons).
- Unique, initial interactions were developed for:
 - interactions at rest such as π^- capture, $p\bar{p}$ annihilation
 - gamma- and lepto-nuclear reactions
 - hadron-nuclear interaction in-flight are in progress
- Anti-proton annihilation on p and π^- capture at rest in a nucleus illustrate two CHIPS modelling sequences

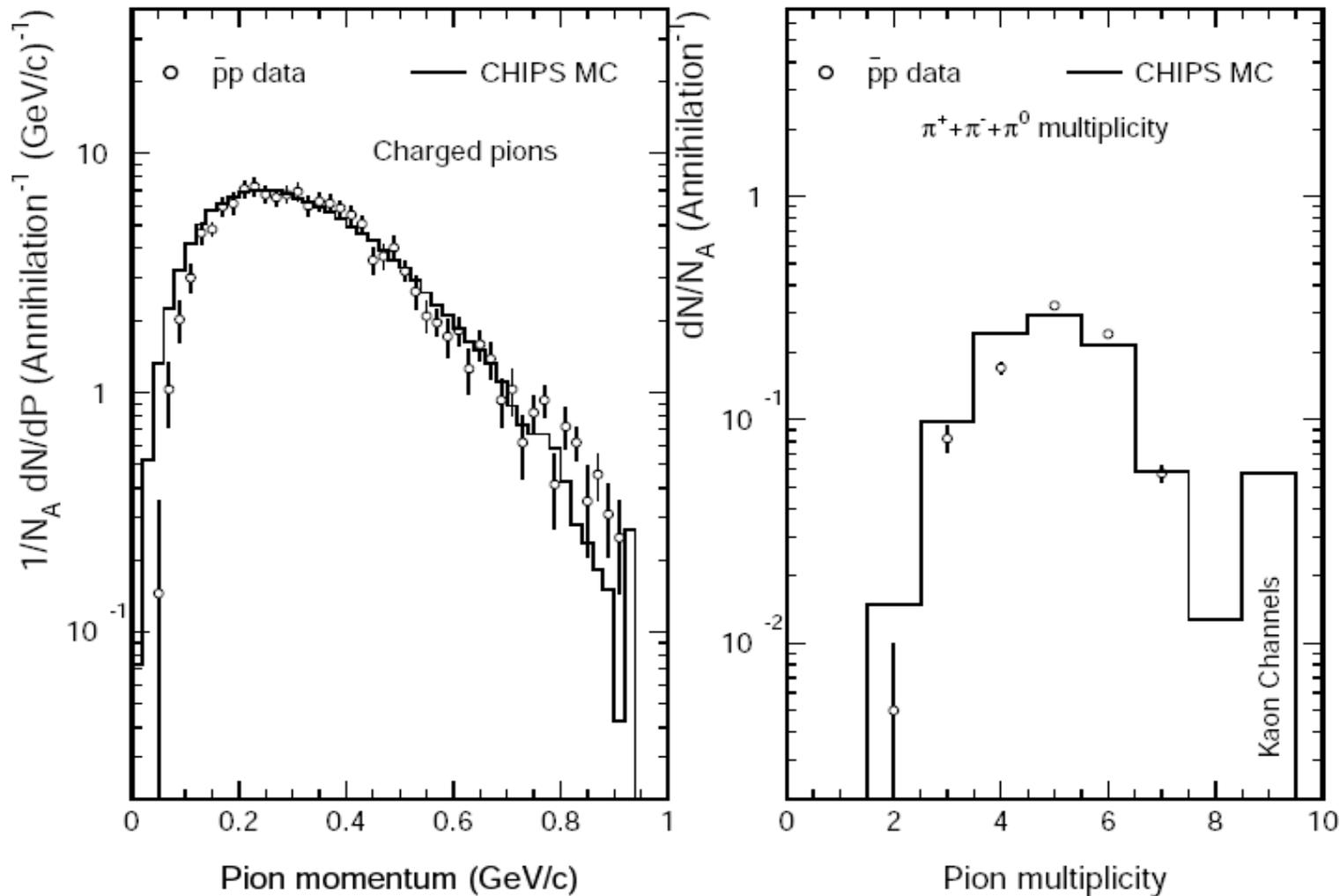
Modeling Sequence for π^- Capture at Rest in a Nucleus



Modeling Sequence for Proton – antiproton Annihilation



Validation of CHIPS for Proton Anti-Proton Annihilation





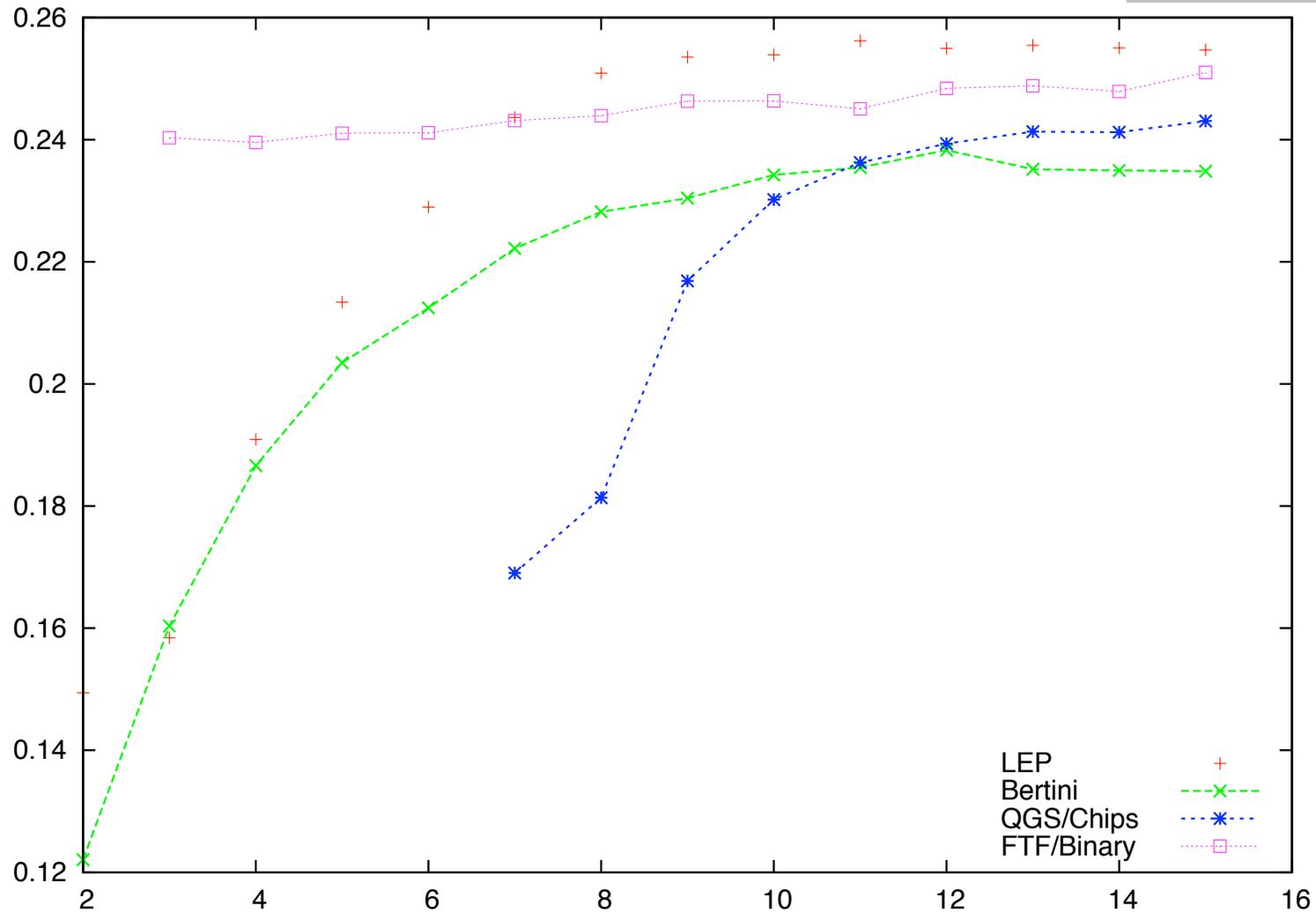
(Personal perspective)

LATEST

Known issues; challenges

- ‘Discontinuity’ in energy deposition in transition between Bertini and LEP QGSP_BERT
 - Reported by CMS, ATLAS
- Deficiencies of LEP model
 - Conservation laws
 - Spectra
- Gap between ‘applicability’ of cascades and string models (general issue for MCs)
 - Bertini validated up to ~ 5 GeV
 - Binary limited to ~ 2.5 GeV (protons), ~ 1.5 GeV (pions)
 - QGS validated from $E > \sim 13/15$ GeV
 - FTF potential to fill the gap (under validation 3+ GeV)

π^- on Fe: Energy fraction in π^0



Sum E tot /
E_{beam}

LEP
Bertini
QGS/Chips
FTF/Binary

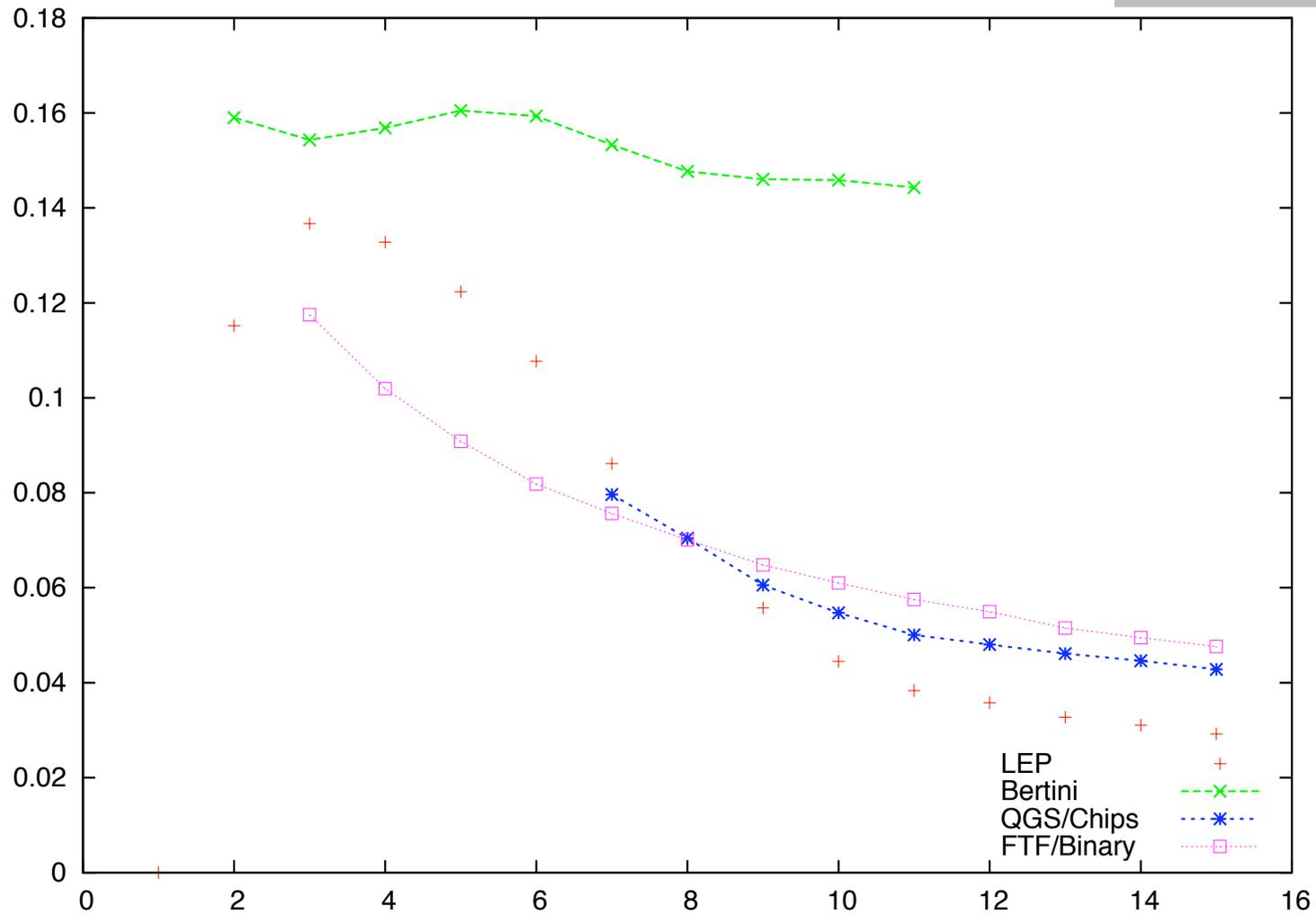
+

x

*

□

π^- on Fe: Energy fraction in protons



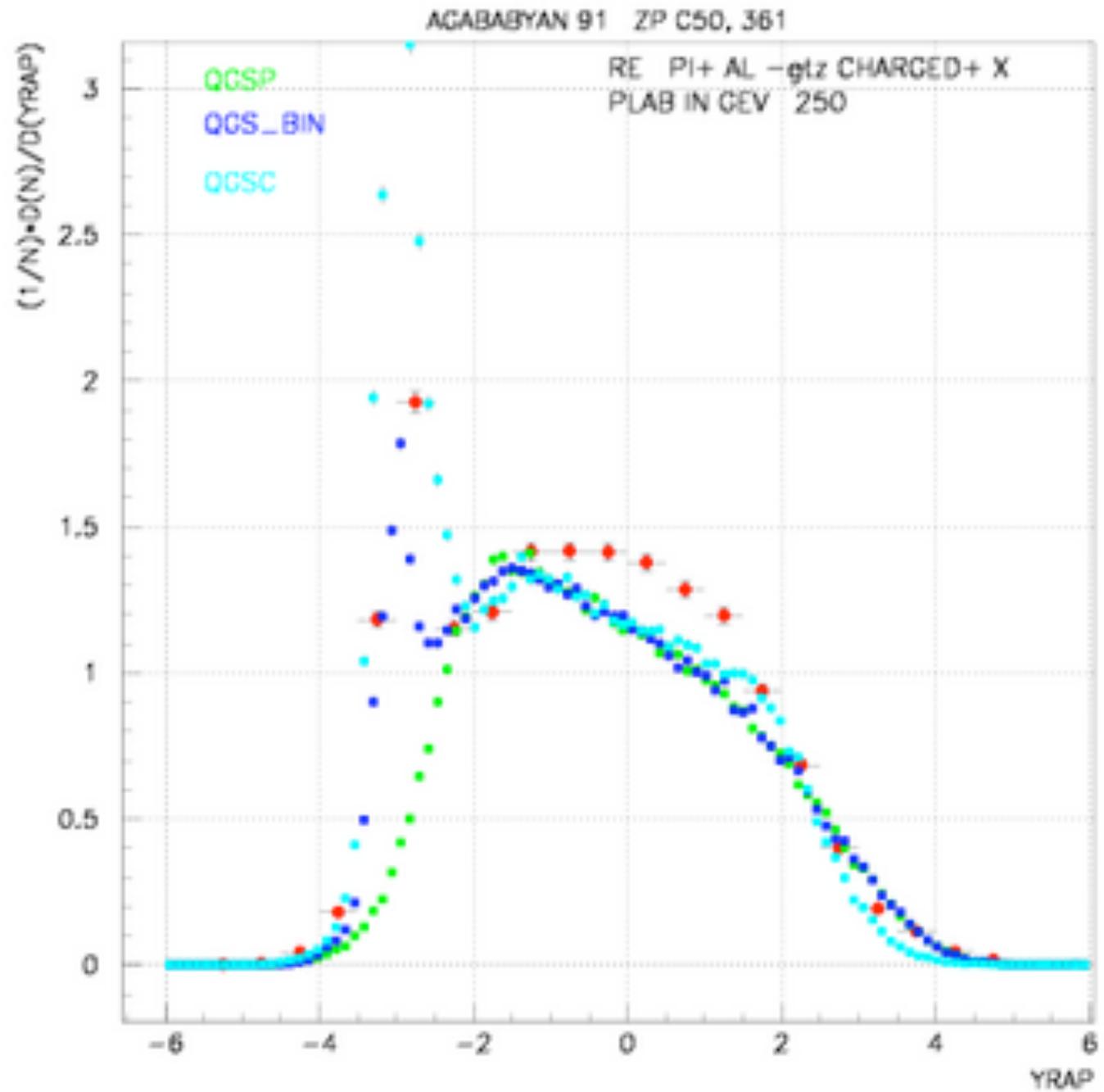
Description of QGSP_BERT

- Elastic n/p from M. Kosov
- Uses BERTini up to about 9.7 GeV for p/n/pi
- Uses LEP for most interactions $9.7 < E < 18$ GeV
 - And for hyperons
- QGS for most interactions $E > 18$ GeV
 - Links with Precompound for de-Excitation
 - Underestimates target fragmentation
- Neutron capture from LEP model
 - Significant limitations
 - alternative HP can be used via QGSP_BERT_HP)

Underway

- Expansion of validation
 - Status for 5-20 GeV [presented at CHEP 2009](#)
 - Additional comparisons being prepared & sought
 - Future 25-70+ GeV
- Linking of cascade to string model(s)
 - To model [re-interaction](#) of low-energy products
- Study of transitions between models
 - Multiplicity, energy moments of products
- Trial physics lists
 - FTF in place of LEP and QGS
 - Others without LEP models

- Effect of reinter-action



Transitions between models

- Transitions in existing physics lists
 - QGSP_BERT: Between Bertini, LEP and QGS/P
 - Bertini $E < 9.9$; LEP: $9.5 < E < 25$; QGS/Preco: $E > 12.5$
- Studying
 - Energy in π^0 , π^+/π^- (total), in p, n, light ions (kinetic)
 - Multiplicities, spectra (to do)
- Future
 - Identifying best criteria for transitioning between models

Potential production physics lists

- Old: LHEP, QGSP
 - QGSP: uses QGS/Preco phased in over interval 12-25 GeV)
 - Alternative: QGSC (CHIPS as de-excitation, QGS 8-25)
- 'Production' at LHC: QGSP_BERT
- Emerging: Featuring FTF in place of LEP and QGS
 - FTF_BERT: transition from BERTinit to FTF at 4-5 GeV
 - QGS not used at all
- New: Linking of cascade to string model(s)
 - To model re-interaction of low-energy products
 - Improve target fragmentation
 - FTF_BIC and QGS_BIC

Development / Trial physics lists

- Others without LEP models
 - QBBC: Binary for p/n, BERTini for pions
- Experimental combinations
 - Chosen guided by the studies of Energy per particle type
 - QGSP_FTFP_BERT
 - replaces LEP in QGSP_BERT; transition BERT/FTF 7-9GeV
 - FTFP_BERT_TRV
 - Changes BERT/FTF transition to 6-8 GeV – not 4-5 FTFP_BERT
 - Not yet searched for ‘ideal’ transition point
- Exposure to new models
 - QGSC_CHIPS
 - Direct use of CHIPS for p (soon n) $E < 300$ MeV, soon higher

Physics Model: Strengths and Limitations

- Cascades created for 200 MeV – 3 GeV
 - Based on nuclear models, p-p data
 - Strength: Pion creation
 - Do not include ‘formation time’ (yet)
 - needed above ~ 4 GeV to reduce reinteraction and nucleon emission
 - Binary based on resonances
 - creates, transports, interacts, decays them
 - give correlations
 - Resonances are not resolved above ~ 2.5 GeV; for p-incident 1.5 GeV is ‘strict’ limit

Strengths and weaknesses

- INUCL Bertini
 - Based on hadron-nucleus data
 - Extended above 5 GeV (but missing formation time)
 - Production of 6+ secondaries not well measured
 - Not yet able to transport products of high energy collision (reinteraction after QGS or FTF)
- LEP
 - Problems with energy partitioning at $E < \sim 20$ GeV
 - Spectra have several unphysical features
- QGS
 - Assumptions of high energy limit ($E > 20-50$ GeV)
 - Stretches down to 12-15 GeV, but breaks between 8-10 GeV

Transitions between models

- Choice made for transition points
 - Stretching model on each side if needed
 - Looking at validation, strengths and limitations
 - By trial and error
- QGSP_BERT: started from QGSP (LEP and QGSP)
 - BERT has better behaviour than LEP: push BERT to 9.5-9.9 GeV
 - Trial transition at 5 GeV (QGSP_BERT_TRV) not better (ATLAS studies ca 2007)
 - Transition LEP to QGS (12-25 GeV) unchanged

Known Problems and Improvements (1)

■ QGS:

- gaussian sampling of p_T too simple => incorrect diffraction, not enough π^- suppression in p scattering
- internal cross sections being improved

■ Medium energy (~5 GeV - 20 GeV):

- too low for QGS, HEP models
- too high for cascades, LEP models
- FTF model developed, being improved

- improved parameterized model will be developed (2010?)

■ Cascades:

- no Coulomb barrier in Bertini

Known Issues and Improvements (2)

■ CHIPS:

- originally designed only as final state generator, not intended for projectile interaction with nucleus
- neutrino scattering added 2006
- extension underway for nucleon inelastic scattering
 - Available: protons ($E < 300$ MeV), shortly neutrons (ditto)
 - Extension to higher energies during next months.
-

Can G4 models be ‘tuned’?

- Can (individual) physics models be tuned with LHC experiment data ?
 - Tuning is constrained by some data
 - tuning of parameters is done against thin-target data
 - where the results of single microscopic interactions is directly comparable.
 - These constraint the model parameters where measured data exists
 - there are regions where comparisons are not possible or have not been undertaken yet.
 - A few parameters are simpler to change:
 - P_t in the QGS model
 - Partial cross sections in Bertini cascade
 - Fragmentation time (FTF)

Model tuning

- G4 model parameters
 - Are not like Event Generator parameters
 - In many cases are constrained by data
 - In others either no data exists or a comparison is pending
- Changing model parameters is complicated
 - Needs collaboration with authors, preparation
 - If it is to be attempted

Other tuning

- The choice of models (choosing physics list)
- The transition points between physics models
 - is a parameter for which there are indications but not yet clear optimal values.
- The choice of cross sections
- The choice of de-excitation model for the high energy interaction.

Varying the Transition points between models

- Example: choices for QGSP_BERT
 - The interval for the transition between the Bertini and LEP model in was chosen as [9.5, 9.9] GeV.
 - A trial to bring this to the region of 5 GeV did not improve physics results.
 - Between these extremes the values for the upper and lower limits of the transition can be seen as tunable parameters.
 - The transition between the LEP model and the QGSP model is currently undertaken between [12, 25] GeV.

Choice of de-excitation

- QGSP: This is chosen as the Pre-Compound model (the P in QGSP).
 - Alternatives include CHIPS (QGSC) and Binary-cascade (QGS_BIC).
 - Seen improvements in
 - the emission of light ions (CHIPS) and
 - Extra low momentum outgoing hadrons (rescater using Binary – ie BIC).
- Until now, the visible energy has not been shown to be significantly different in setups tested
 - but the number of secondary nucleons and light ions are increased.



Recent Improvements – 2008/9

Improvements in hadronic processes in
Release 9.2 (Dec 2008) and its patch 1

Selected from G. Cosmo's talk at
[March 9th Geant4 Technical Forum](#)
meeting

Hadronics: the Improved and New

Improved (9.2, Dec. 2008) :

- ✧ Corrections & tuning in **pre-compound** and **de-excitation** code
 - ✧ affecting results for low-energy secondaries in Binary cascade
- ✧ Revised string fragmentation and tuned parameters in **FTF** model
 - ✧ For p_i+p and $pion-nucleon$ interactions
 - ✧ Implemented quasi-elastic hadron-nucleus scattering and formation time
- ✧ Enabled/added Coulomb barrier penetration in **Bertini** cascade

New:

- ✧ **INCL** cascade and **ABLA** evaporation model officially released
 - ✧ Can be used for incident p , n , d , t , $3He$, $alpha$ and $pions$ from 200 MeV up to 3 GeV, on nuclei ranging from carbon to uranium
- ✧ *Beta* release of *new* quantum molecular dynamics (**QMD**) model
 - ✧ For nucleus-nucleus collisions; valid from 50 MeV to 5 GeV

Hadronic processes: major fixes

- ✧ Bug fix in the final state multiplicity sampling in **Bertini** cascade
 - ✧ Fixes observed problem of quasi-elastic peak in energy spectra
- ✧ Corrections to the **multi-fragmentation** model to ensure it conforms with the original SMM model (from its authors)
- ✧ Improved energy and angular distributions for both scattered neutron and recoil targets in the **hp_neutron** model
- ✧ Code review and performance improvements to **Bertini** code
 - ✧ Measured ~25% CPU time boost for QGSP_BERT for 50 GeV π^-
- ✧ Tuned absorption coefficient in Bertini cascade
 - ✧ Changed pion absorption coefficient from 0.2 to 1.0



OTHER / BACKUP

New Features – physics - 2

✧ Standard Electromagnetic processes

- ✧ Enabled by default Cubic Spline interpolation of `dedx` and cross section tables
- ✧ New multiple-scattering process and model
 - ✧ `G4eMultipleScattering`, specialized for simulation of e^+ and e^-
 - ✧ `G4WentzelVIModel` for multiple scattering of muons and hadrons
- ✧ New Bremsstrahlung model, `G4eBremsstrahlungRelModel`, including advanced description of LPM effect
- ✧ New utility classes
 - ✧ `G4EmSaturation` for sampling of Birks saturation; `G4ElectronIonPair` based on the ICRU'31 report for sampling electron/ion pairs in sensitive detectors; `G4EmConfigurator` for configuration of models in physics lists
- ✧ Initialization of `SubType` added for all processes

Major fixes – physics - 1

✧ Electromagnetic processes

- ✧ Improved implementation of the `G4LogLogInterpolation` class
 - ✧ Providing visible CPU improvement in low-energy physics processes
- ✧ More precise multiple scattering model for e^- and e^+
 - ✧ Providing wider shower (about 0.5% measured for the CMS calorimeter)
 - ✧ Increase of visible energy in sampling calorimeters (due also to Spline approx)
- ✧ Fixed cases of string comparison when computing transport cross-sections in MSC models, compare masses instead
- ✧ Speedup run-time computations in e-Coulomb scattering model
 - ✧ Using pre-computed nuclear form-factors per element
- ✧ Added scintillation with Birk's law and modified sampling of the Cerenkov photon origins

Improved in 2008: De-excitation

- De-excitation reviewed & corrected
 - Many components improved
 - Pre-compound model (JM Quesada)
 - Evaporation (A Howard, JM Q)
 - Multi-fragmentation (donated by SMM authors)



**DETAILS OF MODELING
(BACKUP SLIDES 1)**



QGS MODEL

The Nuclear Model

- Nucleon momenta are sampled assuming Fermi gas model
- Nuclear density
 - harmonic oscillator shape for $A < 17$
 - Woods-Saxon for others
- Sampling is done in a correlated manner:
 - local phase-space densities are constrained by Pauli principle
 - sum of all nucleon momenta must equal zero

Collision Criterion

- In the Regge-Gribov approach, the probability of an inelastic collision with nucleon i can be written as

$$p_i(b_i, s) = (1/c)(1 - \exp[-2u(b_i, s)]) = \sum_{n=1}^{\infty} p_{i^{(n)}}(b_i, s)$$

- where

$$p_{i^{(n)}}(b_i, s) = (1/c) \exp[-2u(b_i, s)] \frac{[2u(b_i, s)]^n}{n!}$$

is the probability of finding n cut pomerons in the collision

$$u(b_i, s) = \frac{z(s)}{2} \exp(b_i^2/4L(s))$$

is the eikonal amplitude for hadron-nucleon elastic scattering with pomeron exchange

Pomeron Parameters

- The functions $z(s)$ and $L(s)$ contain the pomeron parameters:
 - fitted to N-N, π -N, K-N collision data (elastic, total, single diffraction cross sections)
 - pomeron trajectory: $\alpha_p' = 0.25 \text{ GeV}^{-2}$, $\alpha_p(0) = 1.0808$ for π , K, 0.9808 for N
- Other parameters:
 - energy scale $s_0 = 3.0 \text{ GeV}^2$ for N, 1.5 GeV^2 for π , 2.3 GeV^2 for K
 - Pomeron-hadron vertex parameters also included:
 - coupling: $\gamma_p^N = 6.56 \text{ GeV}^{-2}$
 - radius of interaction: $R_p^{2N} = 3.56 \text{ GeV}^{-2}$

Diffractive Dissociation

- Need to sample the probability of diffraction
 - get it from difference of total and inelastic collision probabilities

$$p_{ij}^{diff}(b_{ij}, s) = \frac{c-1}{c} (p_{ij}^{tot}(b_{ij}, s) - p_{ij}(b_{ij}, s))$$

- where c is the “shower enhancement” coefficient
 - $c = 1.4$ for nucleons, 1.8 for pions
- Splitting off diffraction probabilities with parameter c follows method of Baker 1976

String Formation

- Cutting the pomeron yields two strings
- String formation is done by parton exchange (Capella 94, Kaidalov 82)
 - for each participating hadron, parton densities are sampled
 - requires quark structure function of hadron
 - parton pairs combined into color singlets
 - sea quarks included with $u:d:s = 1: 1: 0.27$

Longitudinal String Fragmentation

- String extends between constituents
- Break string by inserting q-qbar pair according to
 - $u : d : s : qq = 1 : 1 : 0.27 : 0.1$
- At break -> new string + hadron
- Gaussian P_t , $\langle P_t^2 \rangle = 0.5 \text{ GeV}$
- Created hadron gets longitudinal momentum from sampling QGSM fragmentation functions
 - Lund functions also available



BERTINI CASCADE

Bertini Cascade Modeling Sequence (1)

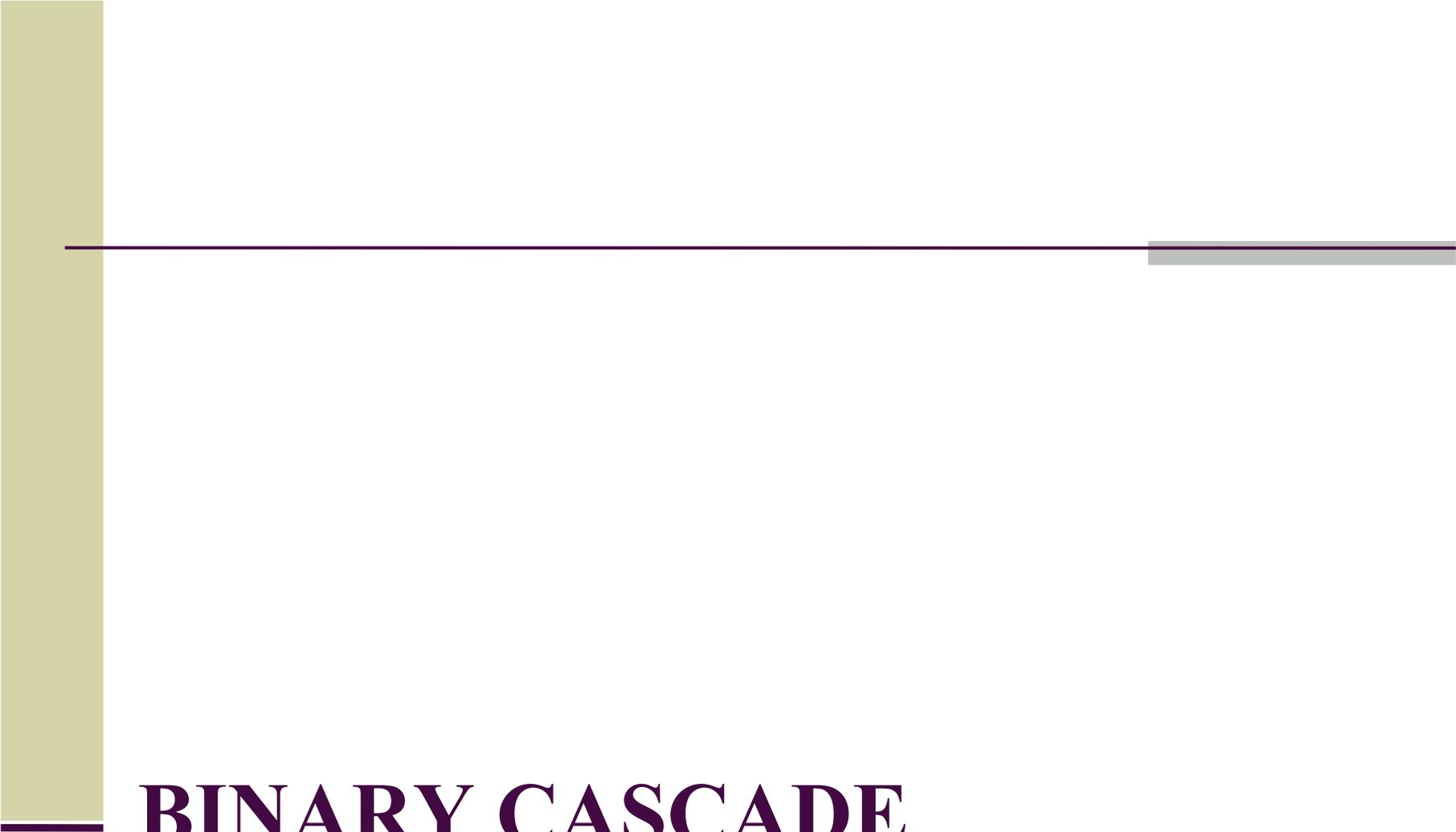
- Nuclear entry point sampled over projected area of nucleus
- Incident particle is transported in nuclear medium
 - mean free path from total particle-particle cross sections
 - nucleus modeled as 3 concentric, constant-density shells
 - nucleons have Fermi gas momentum distribution
 - Pauli exclusion invoked
- Projectile interacts with a single nucleon
 - hadron-nucleon interactions based on free cross sections and angular distributions
 - pions can be absorbed on quasi-deuterons

Bertini Cascade Modeling Sequence (2)

- Each secondary from initial interaction is propagated in nuclear potential until it interacts or leaves nucleus
 - can have reflection from density shell boundaries
 - Coulomb barrier applied for emission of positives (2008)
- As cascade collisions occur, exciton states are built up, leading to equilibrated nucleus
 - selection rules for p-h state formation: $\Delta p = 0, +/-1,$
 $\Delta h = 0, +/-1, \Delta n = 0, +/-2$
- Model uses its own exciton routine based on that of Griffin
 - Kalbach matrix elements used
 - level densities parametrized vs. Z and A

Bertini Cascade Modeling Sequence (3)

- Cascade ends and exciton model takes over when secondary KE drops below 20% of its original value or 7 X nuclear binding energy
- Nuclear evaporation follows for most nuclei
 - emission continues as long as excitation is large enough to remove a neutron or α
 - γ emission below 0.1 MeV
- For light, highly excited nuclei, Fermi breakup
- Fission also possible



BINARY CASCADE

Binary Cascade Modeling (1)

- Nucleon-nucleon scattering (t-channel) resonance excitation cross-sections are derived from p-p scattering using isospin invariance, and the corresponding Clebsch-Gordan coefficients
 - elastic N-N scattering included
- Meson-nucleon inelastic (except true absorption) scattering modelled as s-channel resonance excitation. Breit-Wigner form used for cross section.
- Resonances may interact or decay
 - nominal PDG branching ratios used for resonance decay
 - masses sampled from Breit-Wigner form

Binary Cascade Modeling (2)

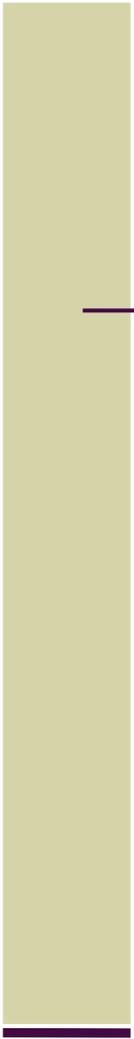
- Calculate imaginary part of the R-matrix using free 2-body cross-sections from experimental data and parametrizations
- For resonance re-scattering, the solution of an in-medium BUU equation is used.
 - The Binary Cascade at present takes the following strong resonances into account:
 - The delta resonances with masses 1232, 1600, 1620, 1700, 1900, 1905, 1910, 1920, 1930, and 1950 MeV
 - Excited nucleons with masses 1440, 1520, 1535, 1650, 1675, 1680, 1700, 1710, 1720, 1900, 1990, 2090, 2190, 2220, and 2250 MeV

Binary Cascade Modeling (3)

- Resonances may interact or decay
- Nucleon-nucleon elastic scattering angular distributions taken from Arndt phase shift analysis of experimental data
- Pauli blocking implemented in its classical form
 - finals state nucleons occupy only states above Fermi momentum
- Pion absorption modelled as s-wave absorption on quasi-deuterons
- Coulomb barrier present for charged hadrons

Binary Cascade Modeling (4)

- Cascade stops when mean energy of all scattered particles is below A -dependent cut
 - varies from 18 to 9 MeV
 - if primary below 45 MeV, no cascade, just precompound
- When cascade stops
 - the properties of the residual exciton system and nucleus are evaluated, and
 - passed to a pre-equilibrium decay code for nuclear de-excitation



CHIPS



Modeling Sequence for Proton - antiproton Annihilation (2)

- anti-proton and proton form a quasmon in vacuum
 - no quark exchange with neighboring nucleons
 - $n = M/2T_c$ quark-partons uniformly distributed over phase space with spectrum $dW/kdk \propto (1 - 2k/M)^{n-3}$
- quark fusion occurs
 - calculate probability of two quark-partons in the quasmon to combine to produce effective mass of outgoing hadron:
 - sample k in 3 dimensions
 - second quark momentum q from spectrum of $n-1$ quarks
 - integrate over vector q with mass shell constraint for outgoing hadron

Modeling Sequence for Proton - antiproton Annihilation (3)

- determine type of final state hadron to be produced
 - probability that hadron of given spin and quark content is produced: $P = (2s_h + 1) z^{N-3} C_Q$
 - C_Q is the number of ways a hadron h can be made from the choice of quarks in the quasmon
 - z^{N-3} is a kinematic factor from the previous momentum selection
- first hadron is produced, escapes quasmon
- randomly sample residual quasmon mass, based on original mass M and emitted hadron mass

Modeling Sequence for Proton - antiproton Annihilation (4)

- Repeat quark fusion with reduced quasmon mass and quark-parton content
- hadronization process ends when minimum quasmon mass m_{\min} is reached
 - m_{\min} is determined by quasmon quark content at final step
 - depending on quark content, final quasmon decays to two hadrons or a hadron and a resonance
 - kaon multiplicity regulated by the s-suppression parameter ($s/u = 0.1$)
 - η/η' suppression regulated by η -suppression parameter (0.3)

Modeling Sequence for π^- Capture at Rest in a Nucleus (2)

- pion captures on a subset or **cluster** of nucleons
 - resulting quasmon has a large mass, many partons
 - capture probability is proportional to number of clusters in nucleus
 - 3 clusterization parameters determine number of clusters
- both quark exchange and quark fusion occurs
 - only quarks and diquarks can fuse
 - mesons cannot be produced, so quark-anti-quark cannot fuse as in vacuum case (p-pbar)
 - because q-qbar fusion is suppressed, quarks in quasmon exchange with neighboring nucleon or cluster
 - produces correlation of final state hadrons

Modeling Sequence for π^- Capture at Rest in a Nucleus (3)

- some final state hadrons escape nucleus, others are stopped by Coulomb barrier or by over-barrier reflection
- as in vacuum, hadronization continues until quasimon mass reaches lower limit m_{\min}
 - in nuclear matter, at this point nuclear evaporation begins
 - if residual nucleus is far from stability, a fast emission of p , n , α is made to avoid short-lived isotopes



**RECENT
FIXES, IMPROVEMENTS**

Hadronics: the Improved and New

Improved:

- ✧ Corrections & tuning in **pre-compound** and **de-excitation** code
 - ✧ affecting results for low-energy secondaries in Binary cascade
- ✧ Revised string fragmentation and tuned parameters in **FTF** model
 - ✧ For **p_i+p** and **pion-nucleon** interactions
 - ✧ Implemented quasi-elastic hadron-nucleus scattering and formation time
- ✧ Enabled/added barrier penetration for the Coulomb barrier in **Bertini** cascade

New:

- ✧ **INCL** cascade and **ABLA** evaporation model officially released
 - ✧ Can be used for incident **p, n, d, t, ³He, alpha** and **pions** from **200 MeV** up to **3 GeV**, on nuclei ranging from carbon to uranium
- ✧ *Beta* release of *new* quantum molecular dynamics (**QMD**) model
 - ✧ For nucleus-nucleus collisions; valid from **50 MeV** to **5 GeV**

Hadronic processes: major fixes

- ✧ Bug fix in the final state multiplicity sampling in **Bertini** cascade
 - ✧ Fixes observed problem of quasi-elastic peak in energy spectra
- ✧ Corrections to the **multi-fragmentation** model to ensure it conforms with the original SMM model (from its authors)
- ✧ Improved energy and angular distributions for both scattered neutron and recoil targets in the **hp_neutron** model
- ✧ Code review and performance improvements to **Bertini** code
 - ✧ Measured ~25% CPU time boost for QGSP_BERT for 50 GeV π^-
- ✧ Technical
 - ✧ Rationalised usage of the nuclear mass tables

Latest Hadronic fixes – 9.2.p01

- ✧ Corrected light ion emission in pre-compound/de-excitation
 - ✧ Probability of emission in pre-compound
 - ✧ Implementation of the emission probability in de_excitation model
 - ✧ Added smearing of Coulomb barriers for **d**, **t**, **he3** and **alpha**
- ✧ Tuned absorption coefficient in Bertini cascade
 - ✧ Changed pion absorption coefficient from 0.2 to 1.0
- ✧ Technical
 - ✧ Activate proper deletion of processes, models and cross-sections at job closure



FURTHER INFORMATION

String Formation

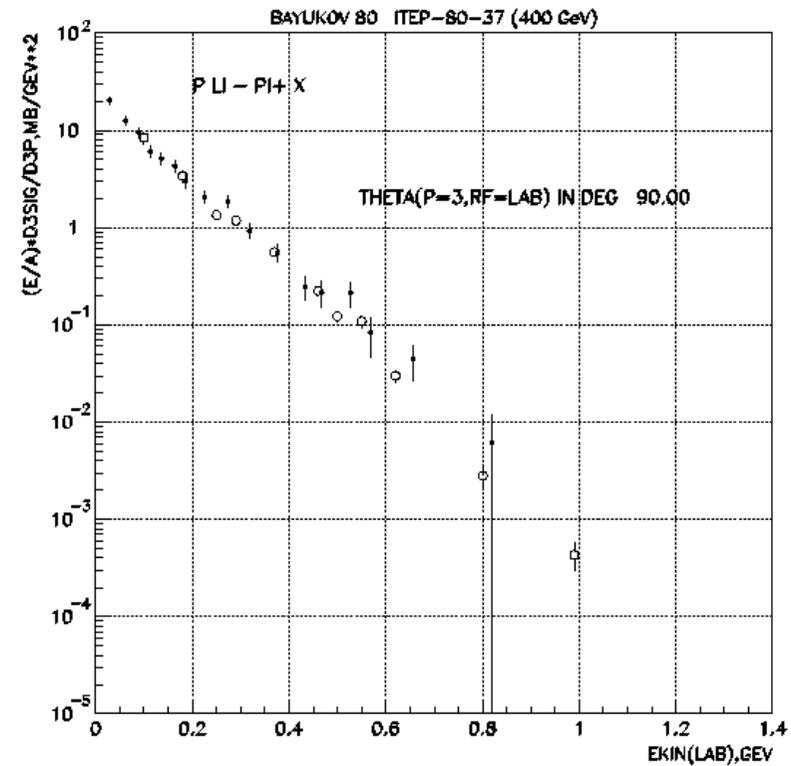
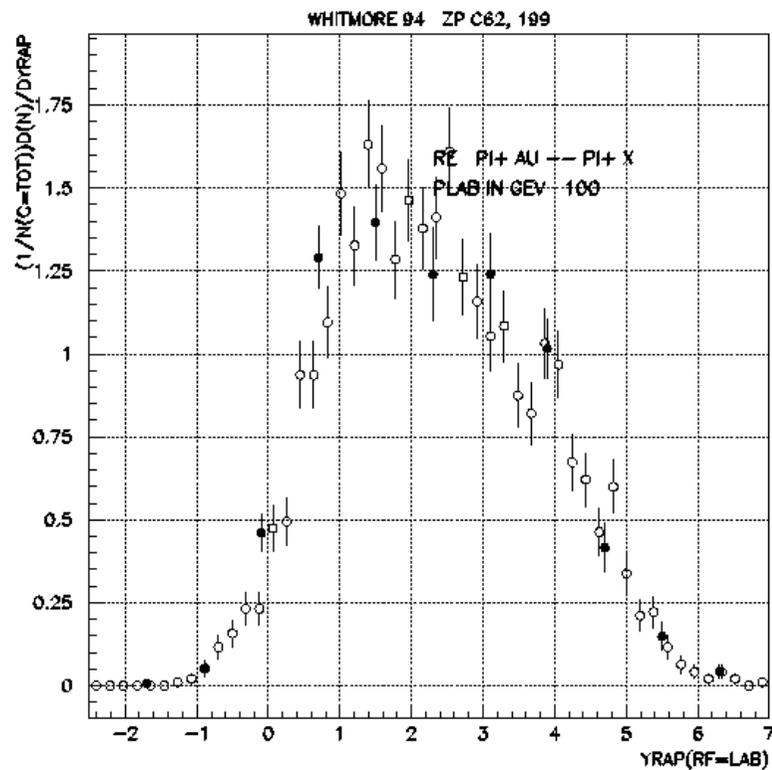
- Cutting the pomeron yields two strings
- String formation is done by parton exchange (Capella 94, Kaidalov 82)
 - for each participating hadron h , parton densities are sampled

$$f^h(x_1, x_2, \dots, x_{2n-1}, x_{2n}) = f_0 \prod_{i=1}^{2n} u_{p_i}^h(x_i) \delta(1 - \sum_{i=1}^{2n} x_i)$$

- parton pairs combined to form color singlets
- u is quark structure function of hadron h
- sea quarks included with $u:d:s = 1: 1: 0.27$

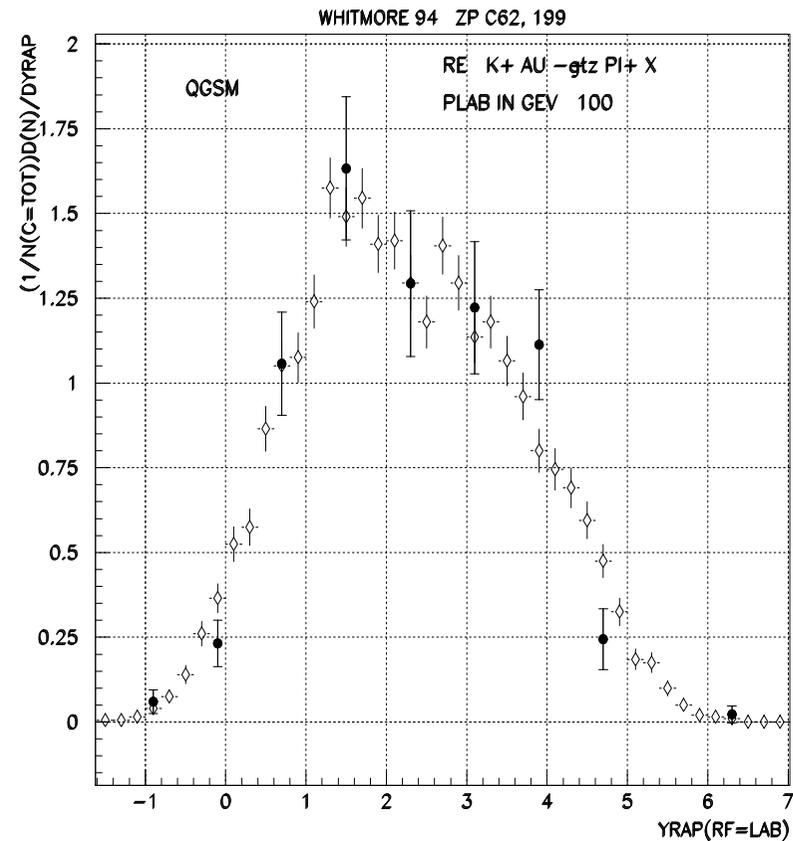
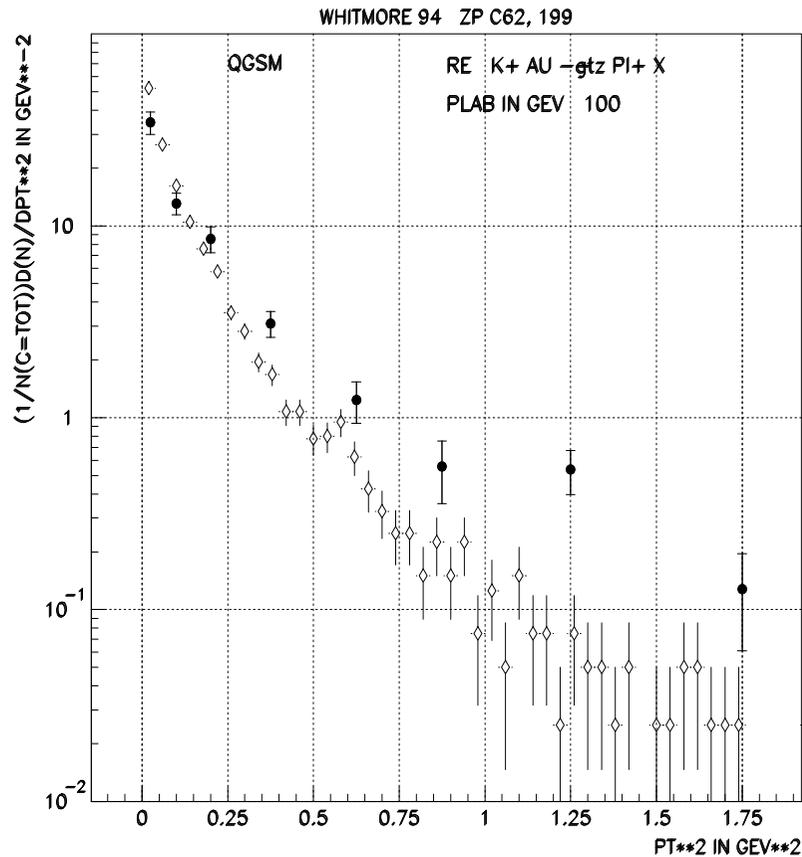
QGS Model

Pion and proton scattering



QGS Model

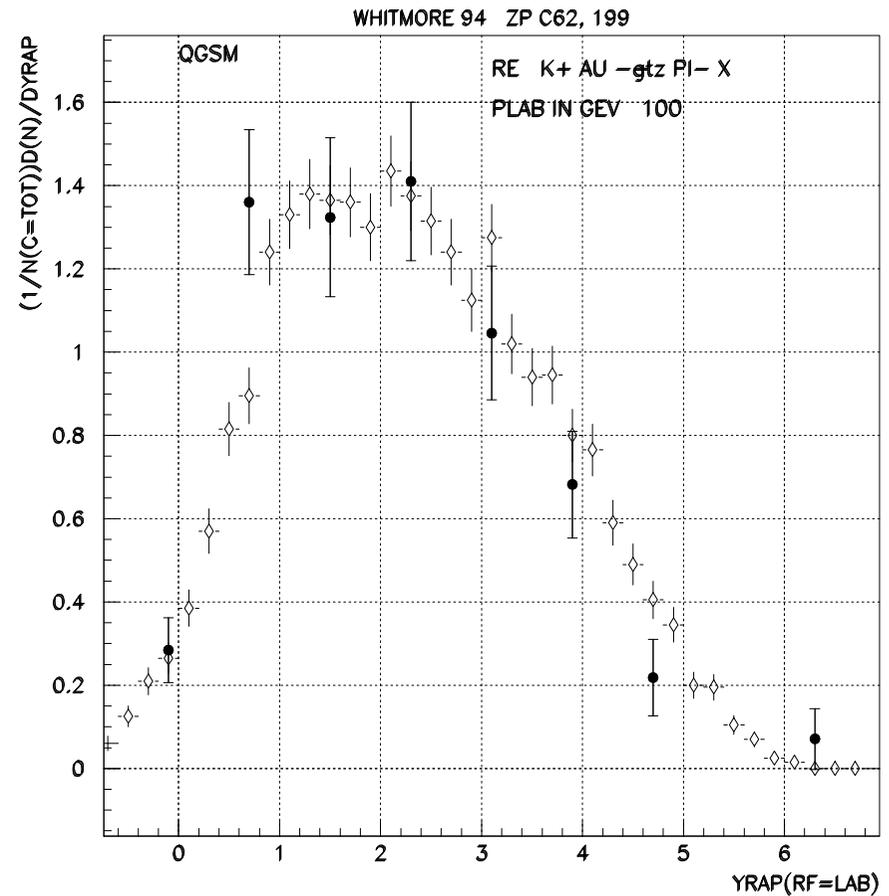
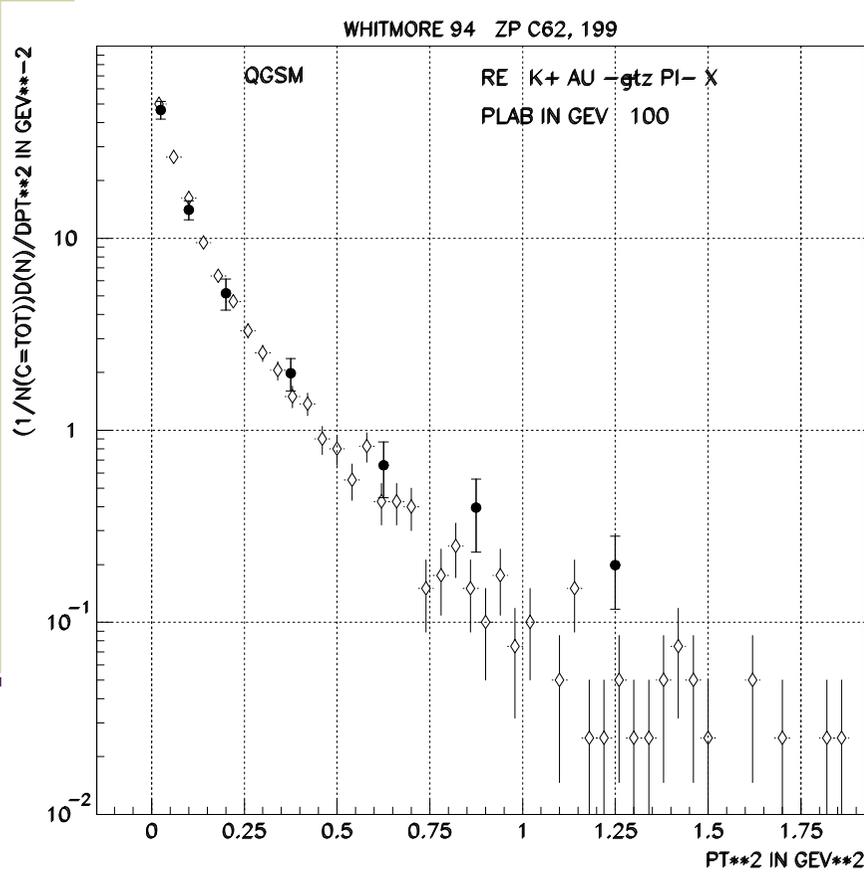
K⁺ Scattering from Au (π^+ inclusive)



Solid dots: J.J.Whitmore et.al., Z.Phys.C62(1994)199

QGS Model

K⁺ Scattering from Au (π^- inclusive)



Solid dots: J.J.Whitmore et.al., Z.Phys.C62(1994)199

Chiral Invariant Phase Space (CHIPS)

- Hadron spectra reflect spectra of quark-partons within quasmon

- 1-D quark exchange:

$$k + M = q + E, \quad k = p - q \quad \Rightarrow \quad k = (E - M + p)/2$$

- 1-D quark fusion:

$$k + q = E, \quad k - q = p \quad \Rightarrow \quad k = (E + p)/2$$

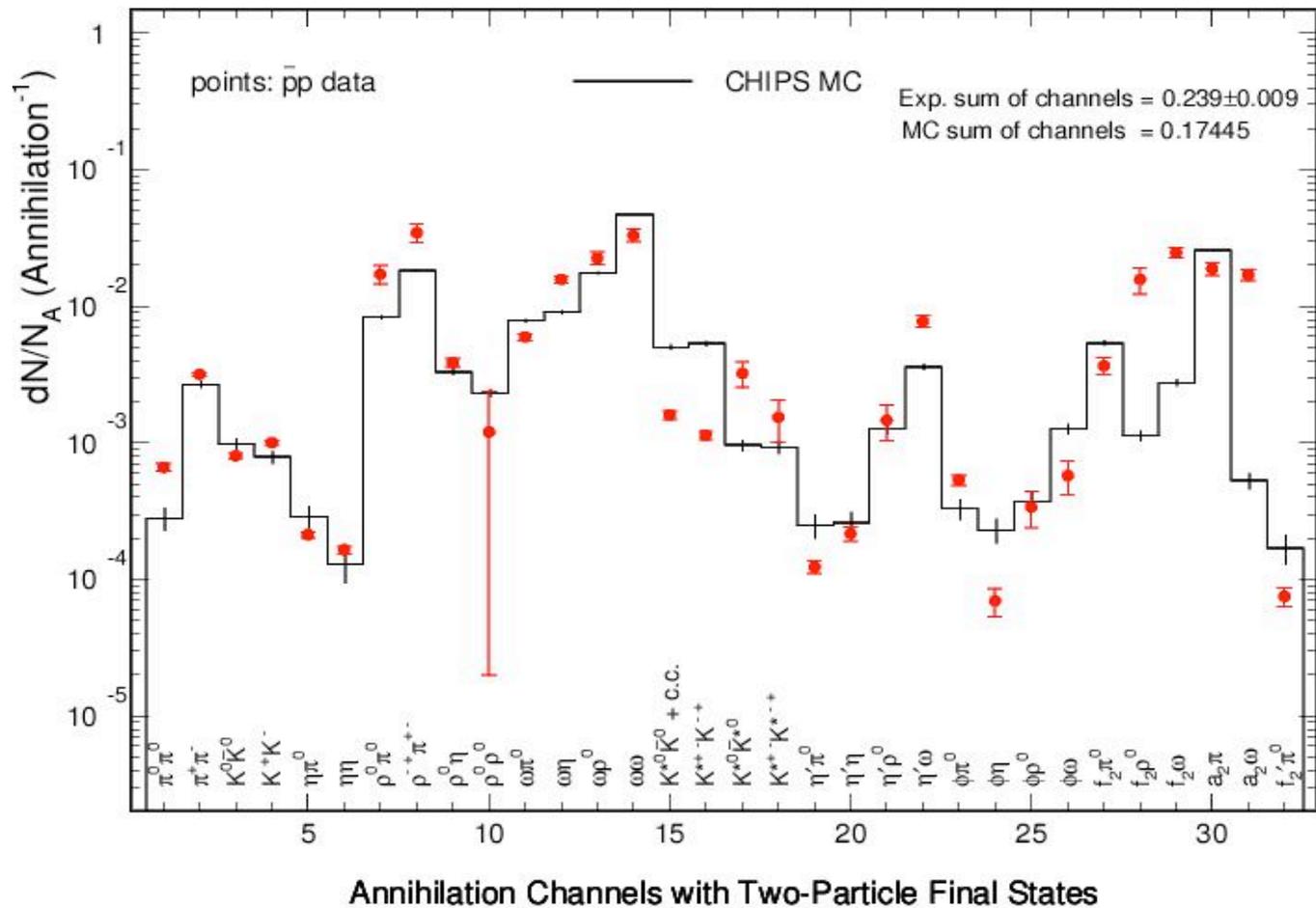
Currently Implemented Mechanisms (1)

- Negative meson captured by nucleon or nucleon cluster:
 - $dE_{\pi} = m_{\pi}$, $dE_K = m_K + m_N - m_{\Lambda}$
- Negative hyperon captured by nucleon or nucleon cluster:
 - $dE_{\Sigma^-} = m_{\Sigma^-} - m_{\Lambda}$, $dE_{\Xi^-} = m_{\Xi^-} + m_N - 2m_{\Lambda}$, $dE_{\Omega} = m_{\Omega} + 2m_N - 3m_{\Lambda}$
- Nuclear capture of anti-baryon:
 - annihilation happens on nuclear periphery
 - 4π explosion of mesons irradiates residual nucleus
 - secondary mesons interacting with residual nucleus create more quasimons in nuclear matter
 - large excitation: $dE = m_{\text{antibaryon}} + m_N$

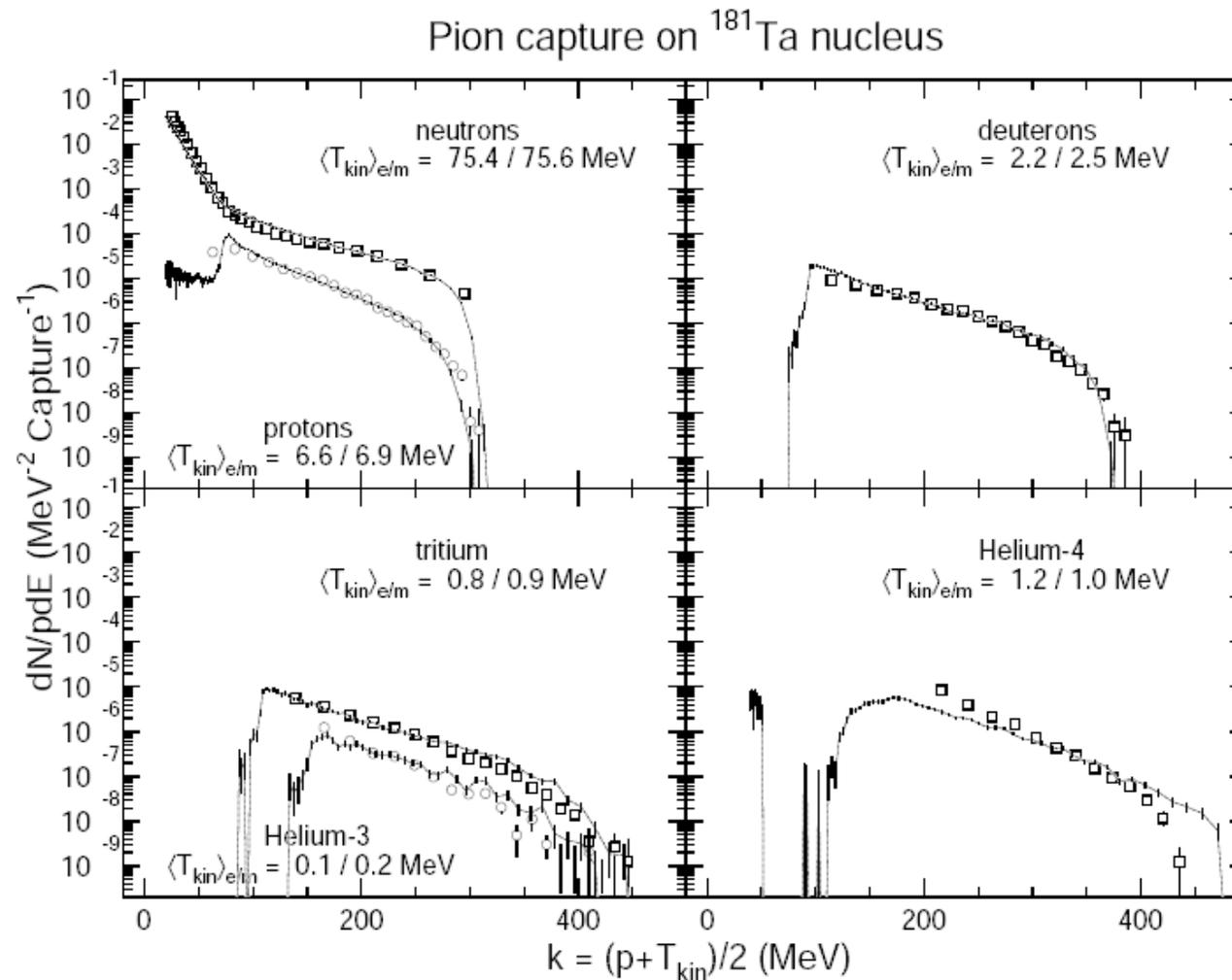
Currently Implemented Mechanisms (2)

- In photo-nuclear reactions γ is absorbed by a quark-parton
 - $dE_\gamma = E_\gamma$
- In back-end of string-hadronization (QGSC model) soft part of string is absorbed:
 - $dE_{\text{QGSC}} = 1 \text{ GeV/fm}$
- lepto-nuclear reactions γ^* , W^* are absorbed by quark-parton:
 - $dE_l = E_{\gamma^*}$, $\cos(\theta_k) = (2k/v - Q^2)/2kq$, $Q^2 = q^2 - v^2$
 - with $k < M/2$, if $q - v < m_N$, virtual γ cannot be captured by one nucleon

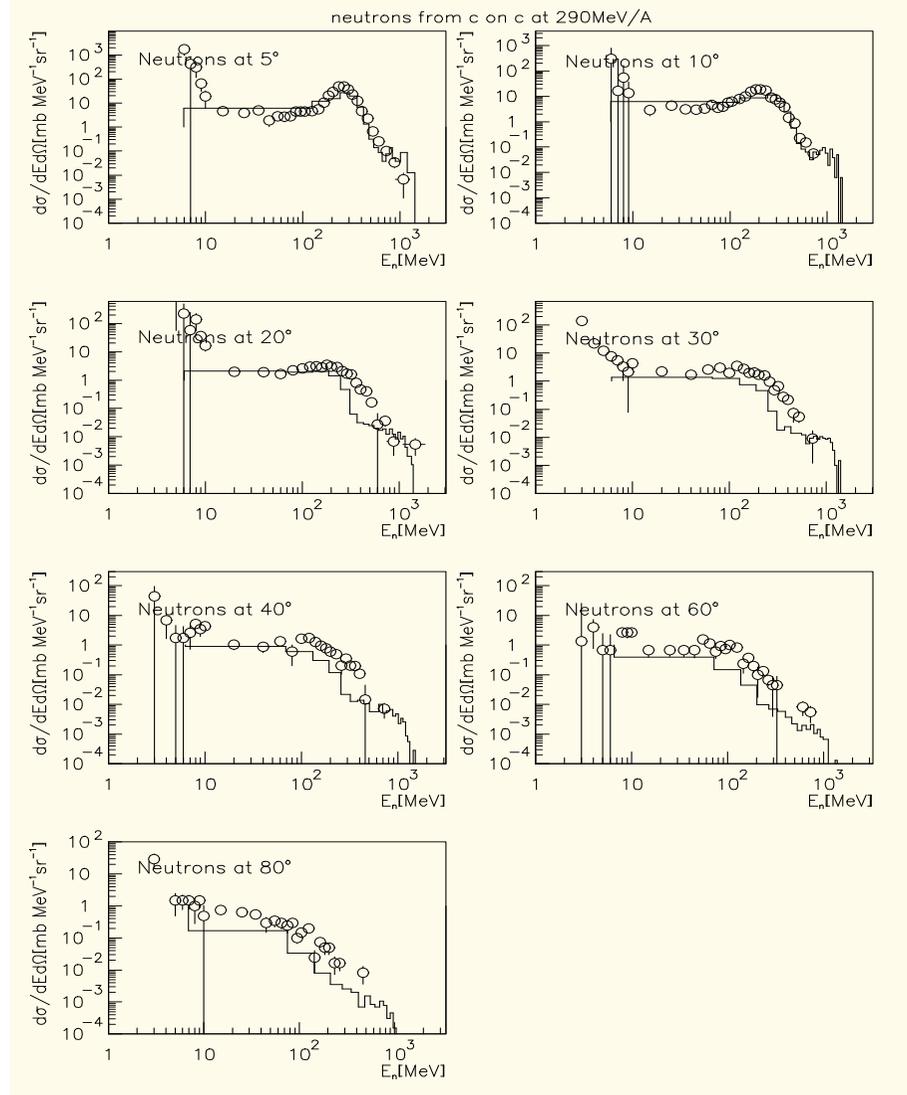
P-pbar Annihilation into Two Body Final States



Validation of CHIPS Model for Pion Capture at Rest on Tantalum



Neutrons from C on C at 290 MeV/c



p+Ta=h+X, 400 GeV, 90°

