Perturbative Unitarity in the Dark Sector

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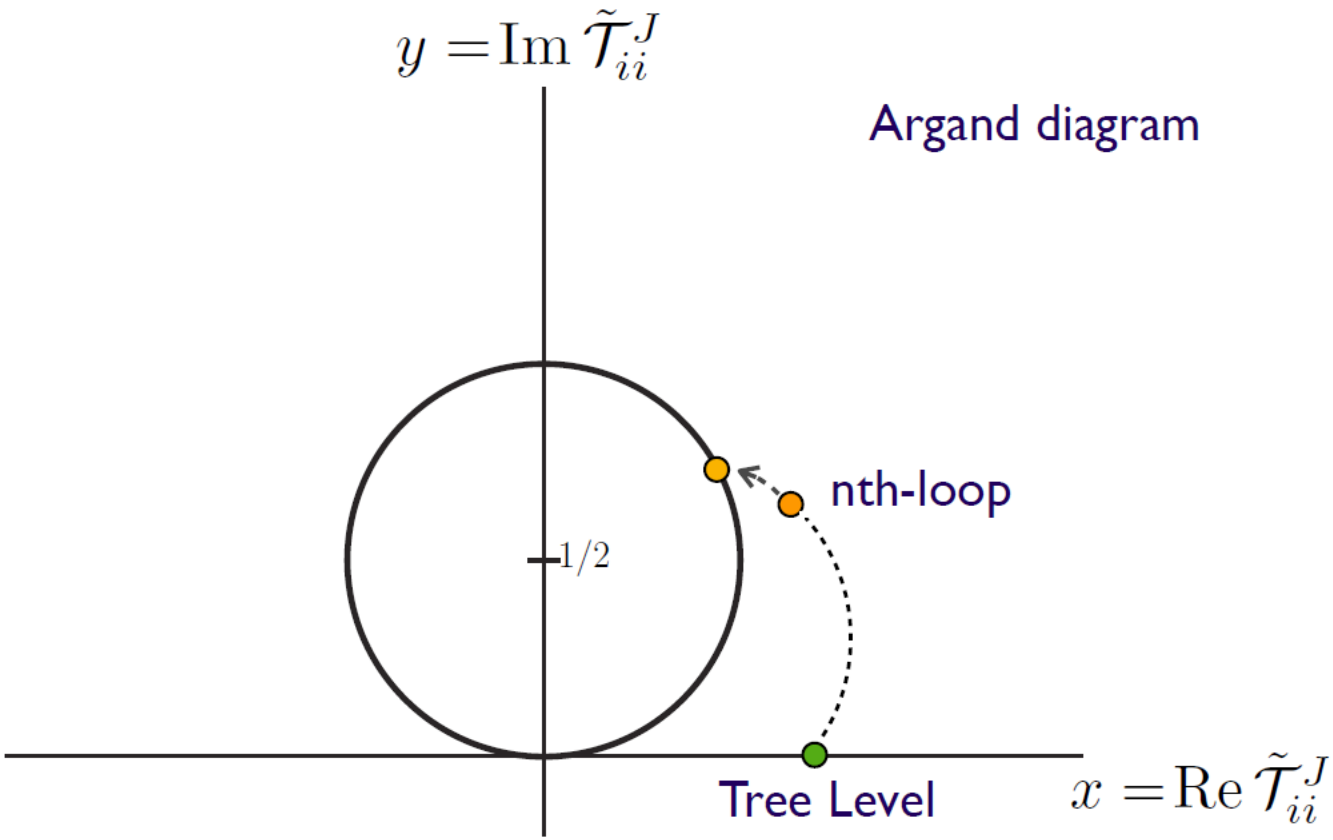
The Niels Bohr International Academy

Based on 1412.5660, 1501.03153
and ongoing work
with Matthew Cahill-Rowley,
Sonia El-Hedri, and Devin Walker

The Scale of New Physics

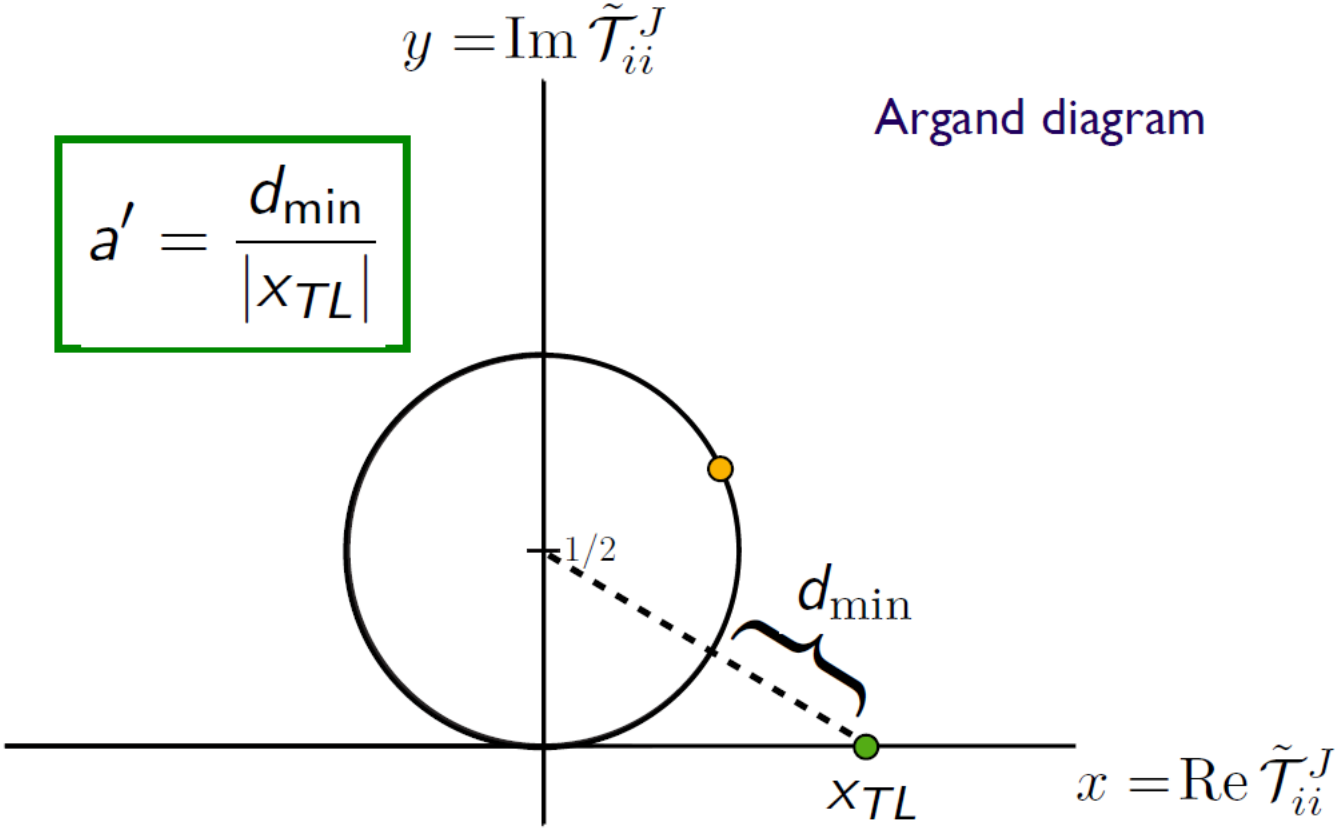
- Historically in HEP, we've often known where we were going
  - Fermi theory of weak decays needed new bosons
  - Precision measurements pointed to the top quark
  - Heavy bosons needed symmetry breaking
- After the Higgs discovery, we have no map
  - The Standard Model is stubbornly good
- Where are we going, and how far away is it?

A Picture of Unitarity



Schuessler and Zeppenfeld 0710.5175
Aydemir, Anber, Donoghue 1203.5153

A Picture of Unitarity



Schuessler and Zeppenfeld 0710.5175

Gauge Portal Dark Matter

- This model is characterized by the Lagrangian

$$\mathcal{L}_{DM} \supset g' \bar{\chi} \gamma^{\mu} \gamma_5 Z'_{\mu} \chi - \lambda_{\chi} \bar{\chi} \Phi \chi$$

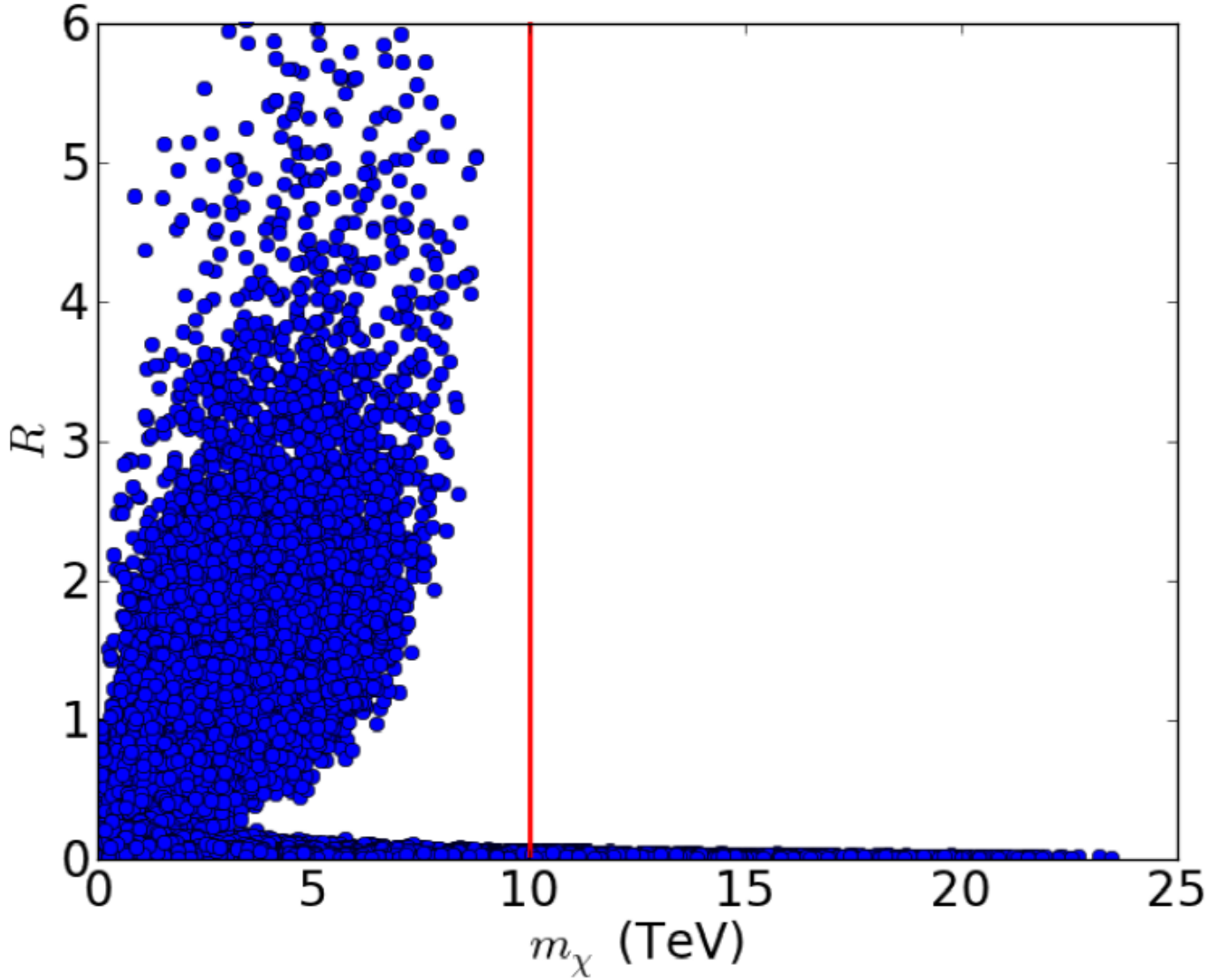
$$\mathcal{L}_{gauge} \supset -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + \frac{\sin\delta}{2} Z'_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{L}_{Higgs} \supset |D_{\mu}\Phi|^2 + V(H, \Phi; \lambda_1, \lambda_2, \lambda_3)$$

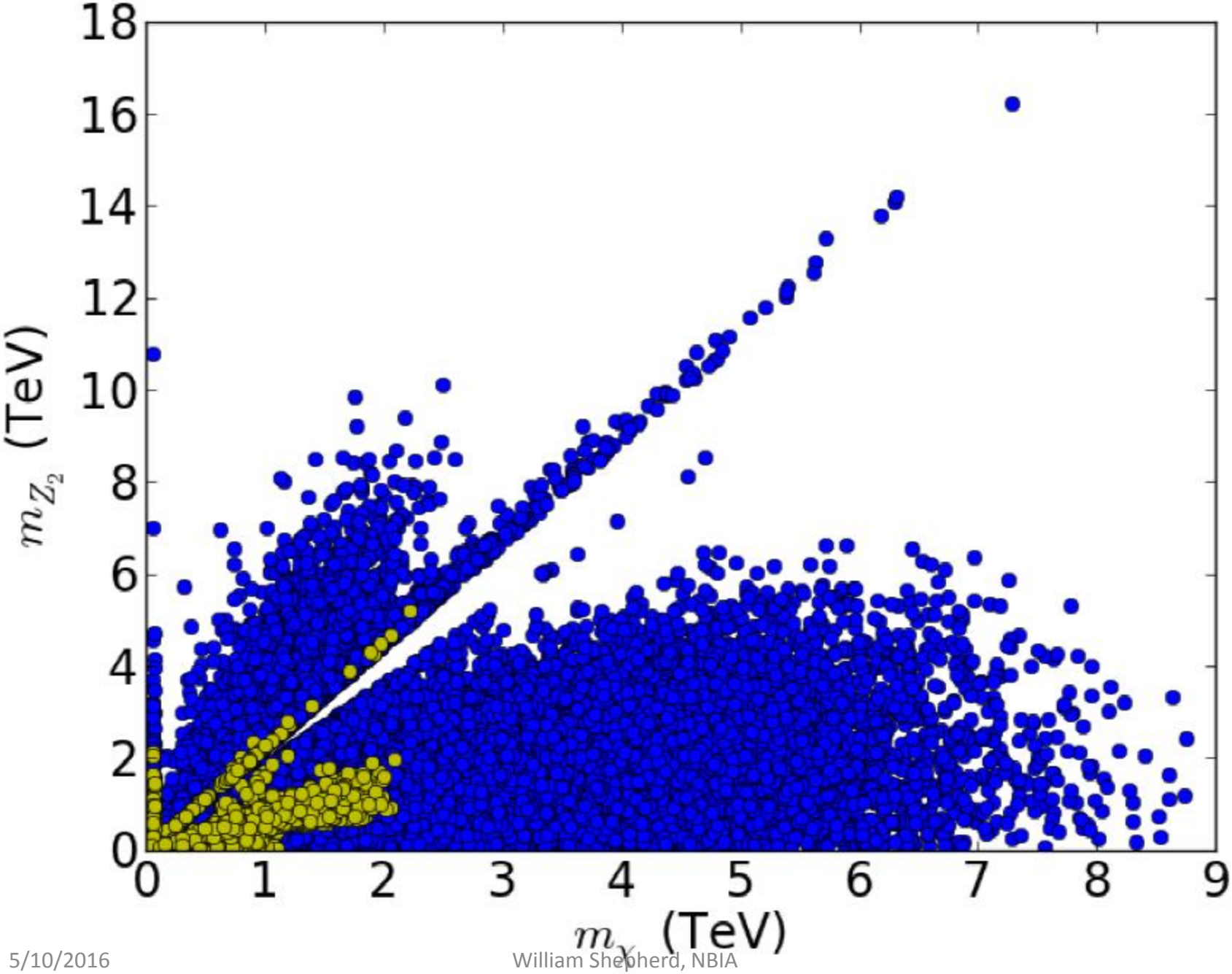
- With breaking of the new symmetry by

$$\Phi = \frac{1}{\sqrt{2}}(\mathbf{u} + \phi^0)$$

Babu, Kolda, March-Russell hep-ph/9710441



$$R = \min\left\{\frac{|2m_\chi - m_{Z'}|}{m_\chi}, \frac{|2m_\chi - m_{\phi^0}|}{m_\chi}\right\}$$


18
16
14
12
10
8
6
4
2
0
0
1
2
3
4
5
6
7
8
9
m_{Z_2} (TeV)
m_χ (TeV)

Colored Scalars and Dark Matter

- In a SUSY-inspired model, we add

$$\tilde{u}_R = (\tilde{u}_R, \tilde{c}_R, \tilde{t}_R)$$

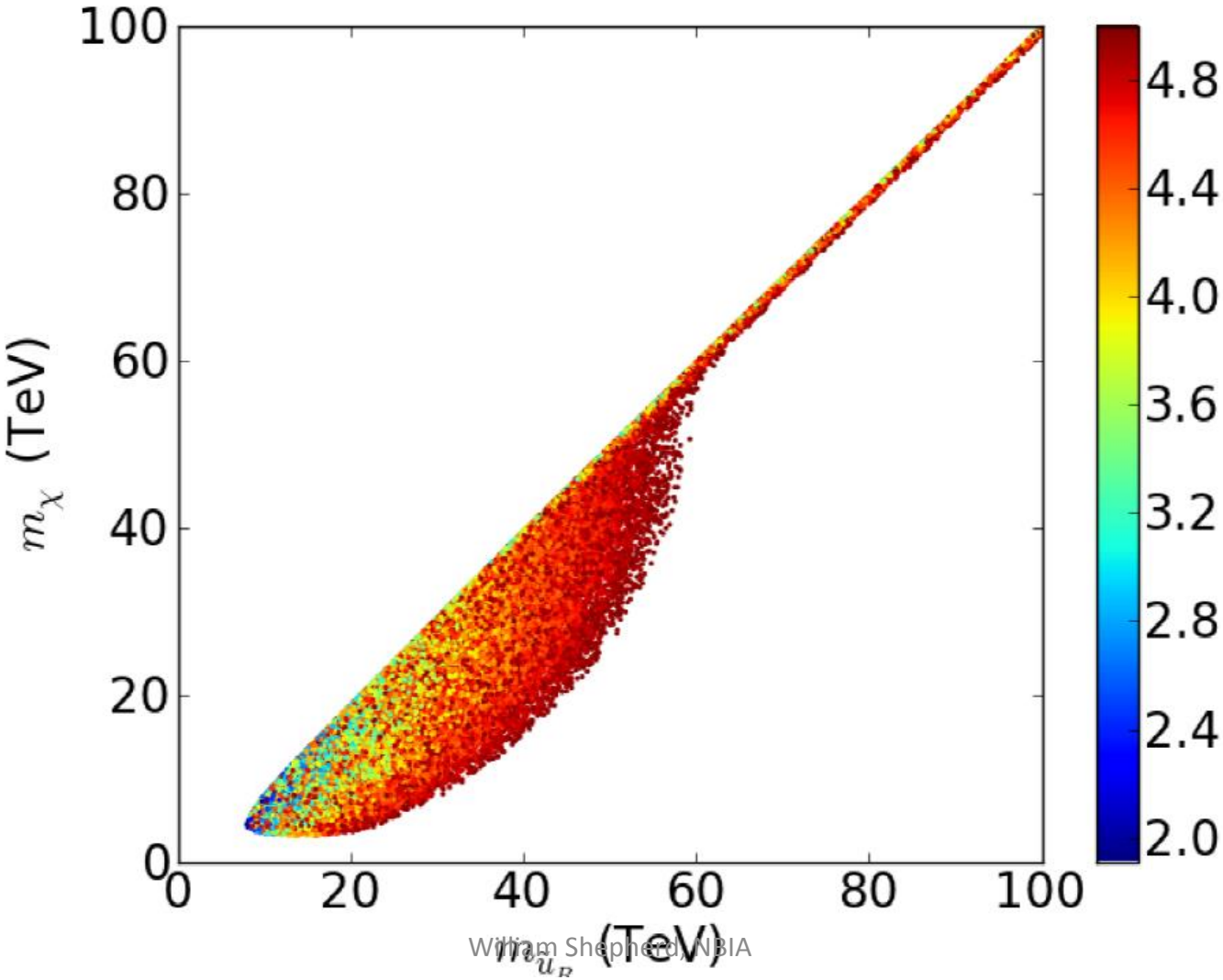
- And the Lagrangian terms

$$\mathcal{L} \supset \frac{1}{2} M_\chi \bar{\chi}\chi + \frac{1}{2} {M_{\tilde{u}}}^2 \tilde{u}^* u + \lambda_{\text{dark}} \tilde{u}^* \bar{\chi} P_R u$$

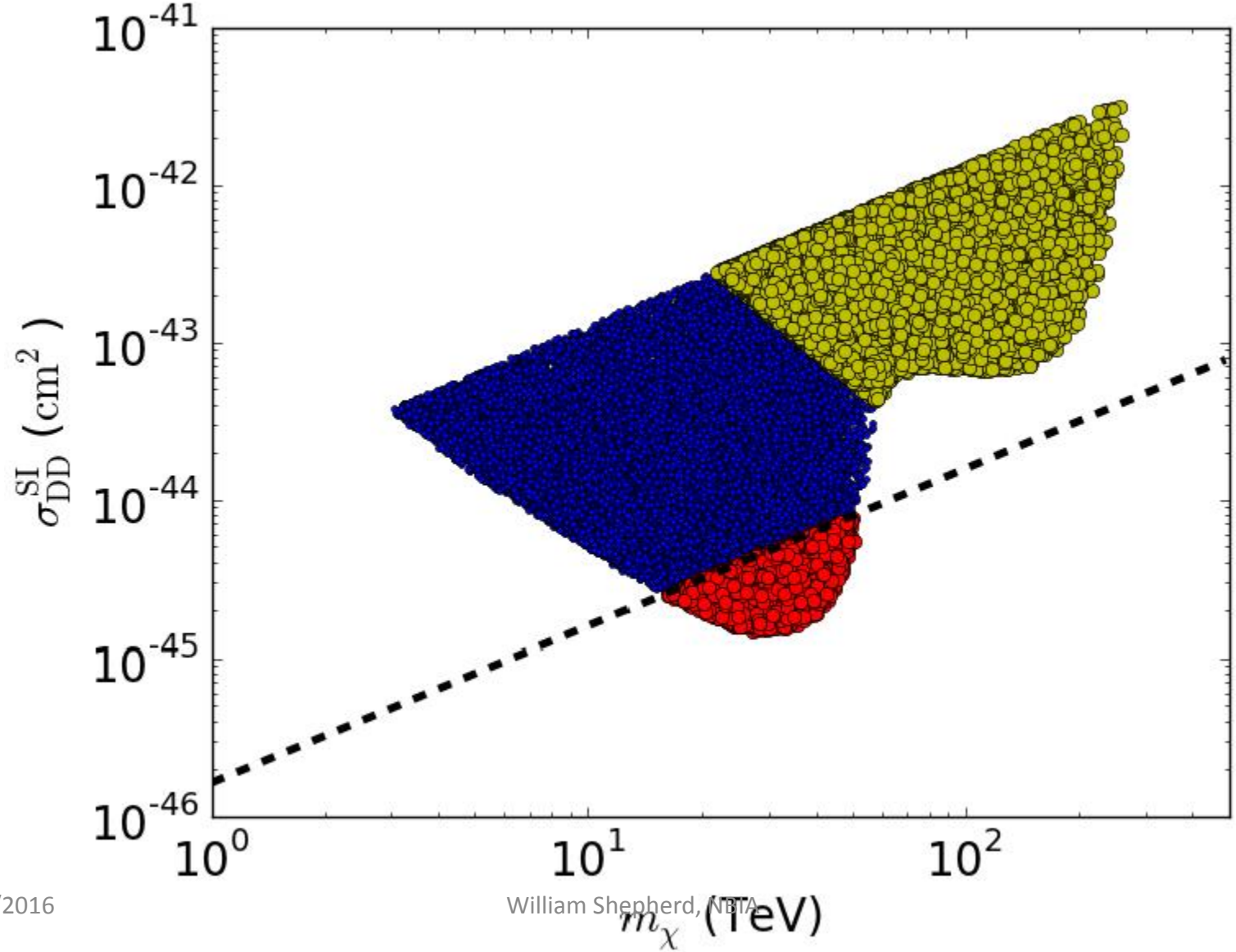
- This introduces the new parameter and scales

$$\lambda_{\text{dark}},\ M_\chi,\ M_{\tilde{u}}$$

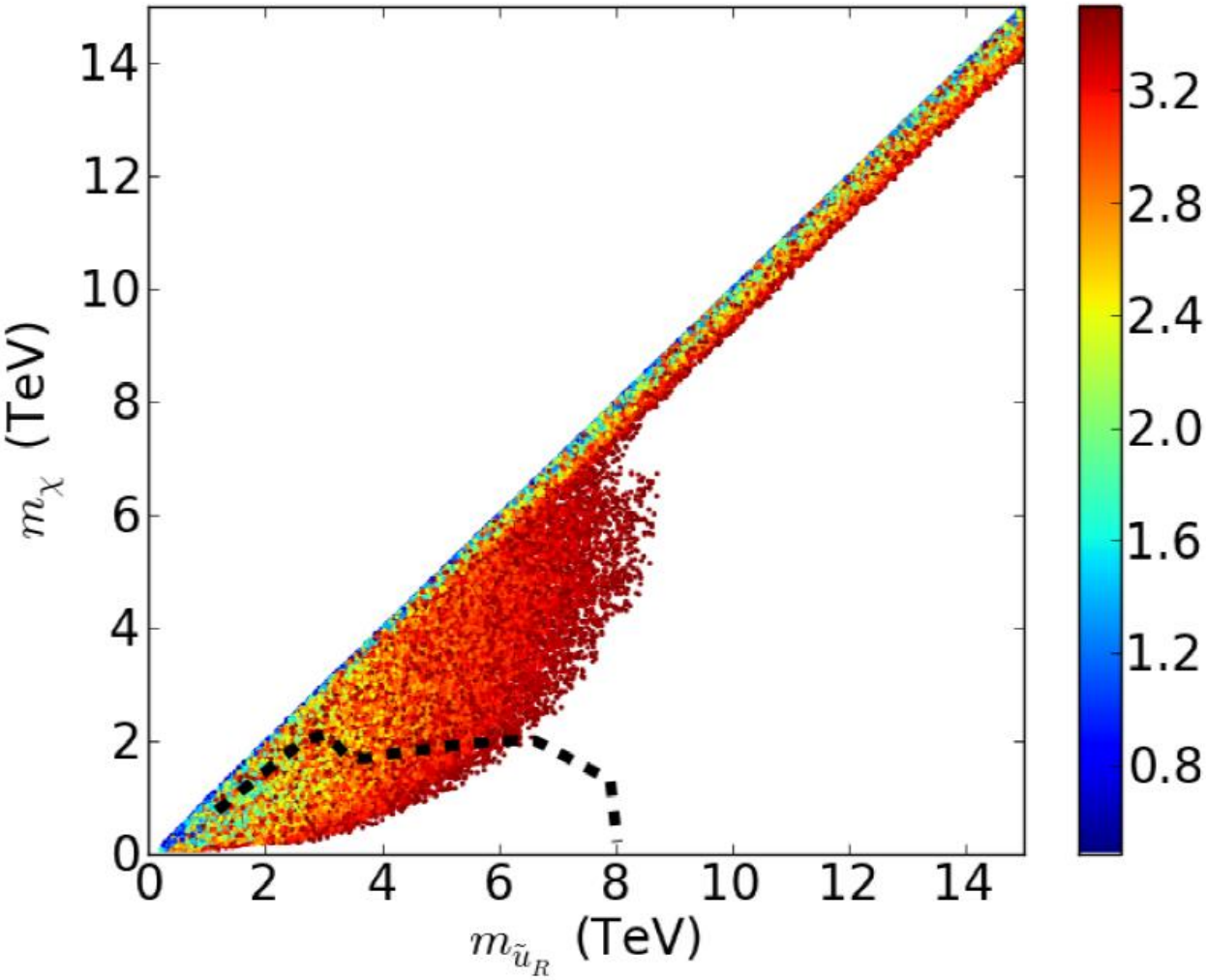
Dirac Dark Matter



Direct Detection

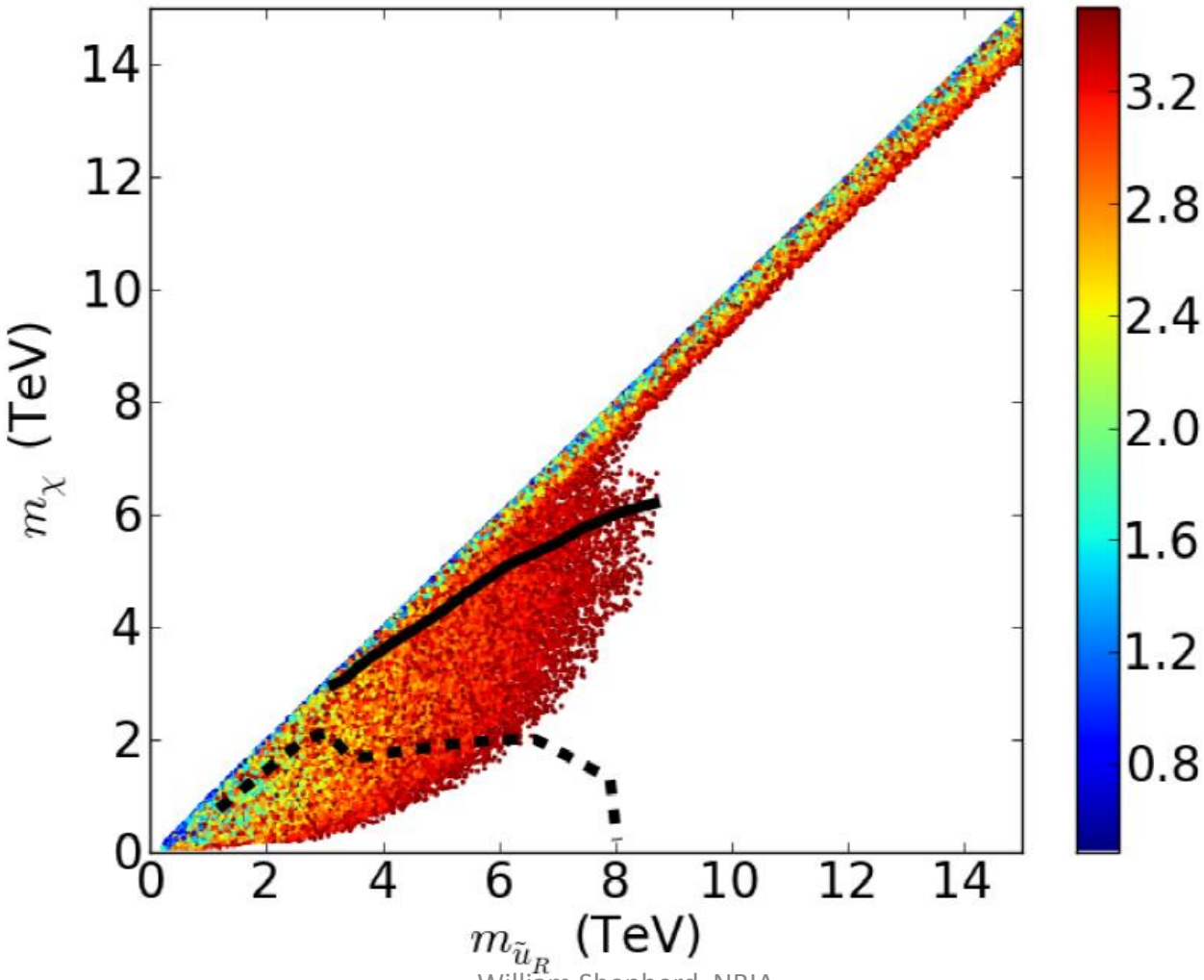


Majorana Dark Matter



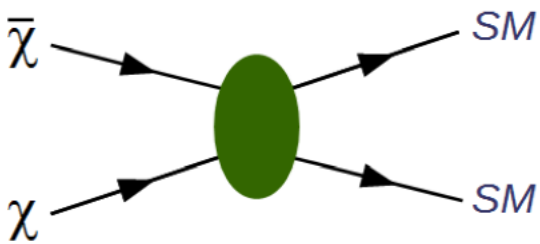
Cohen, Golling, Hance, Henrichs, Howe, Loyal, Padhi, Wacker [arXiv:1311.6480]

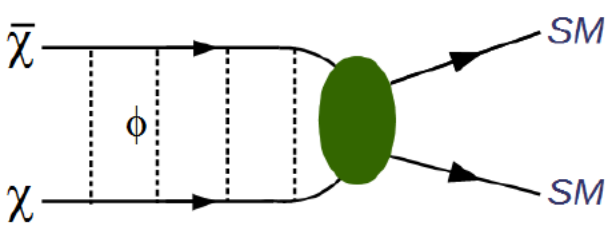
True FCC Reach



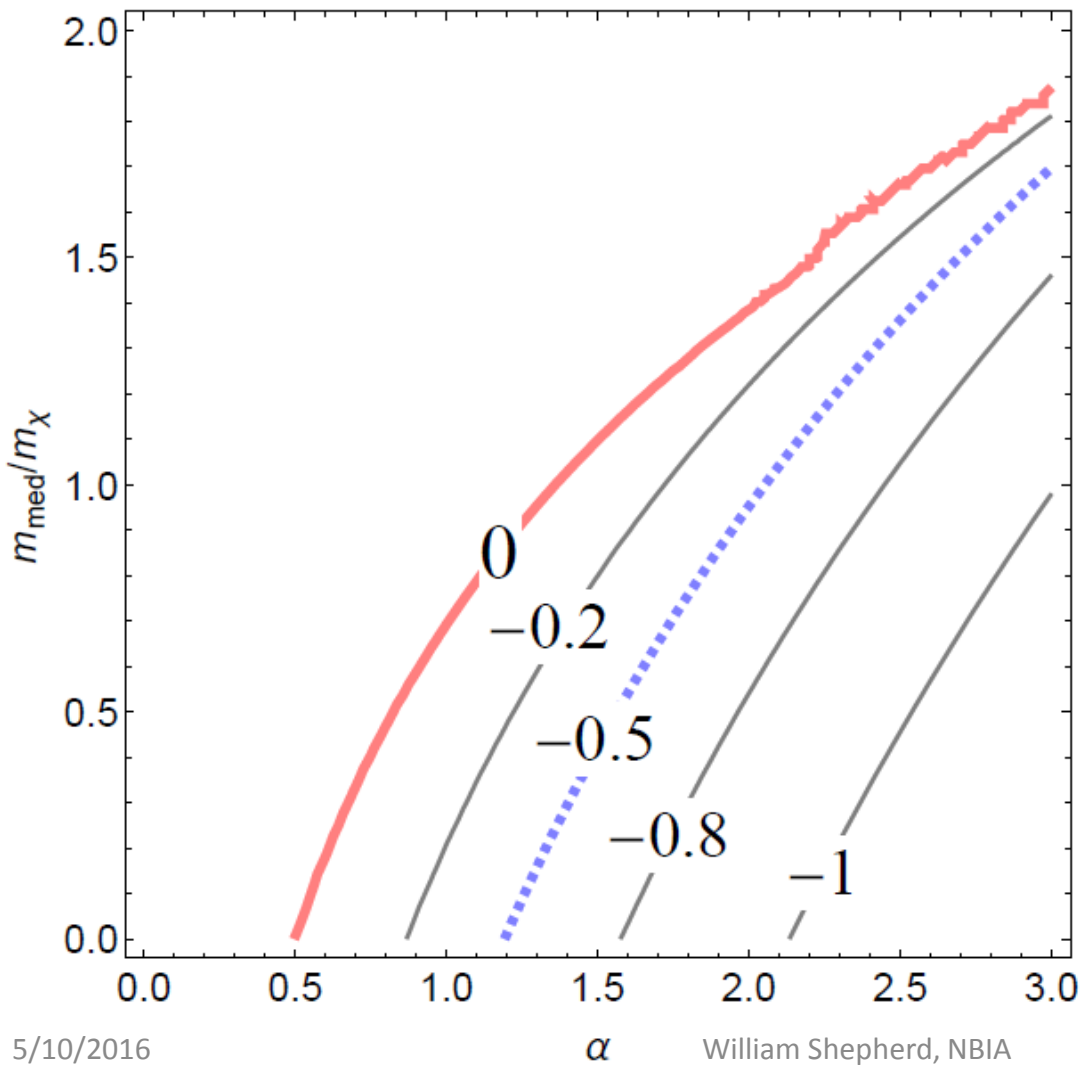
Strong Couplings and Bound States

- All of this analysis has focused on the case of very strong couplings to get high allowed mass
- These large couplings can also lead to other effects that may be important
  - Sommerfeld enhancements
  - Dark matter bound states





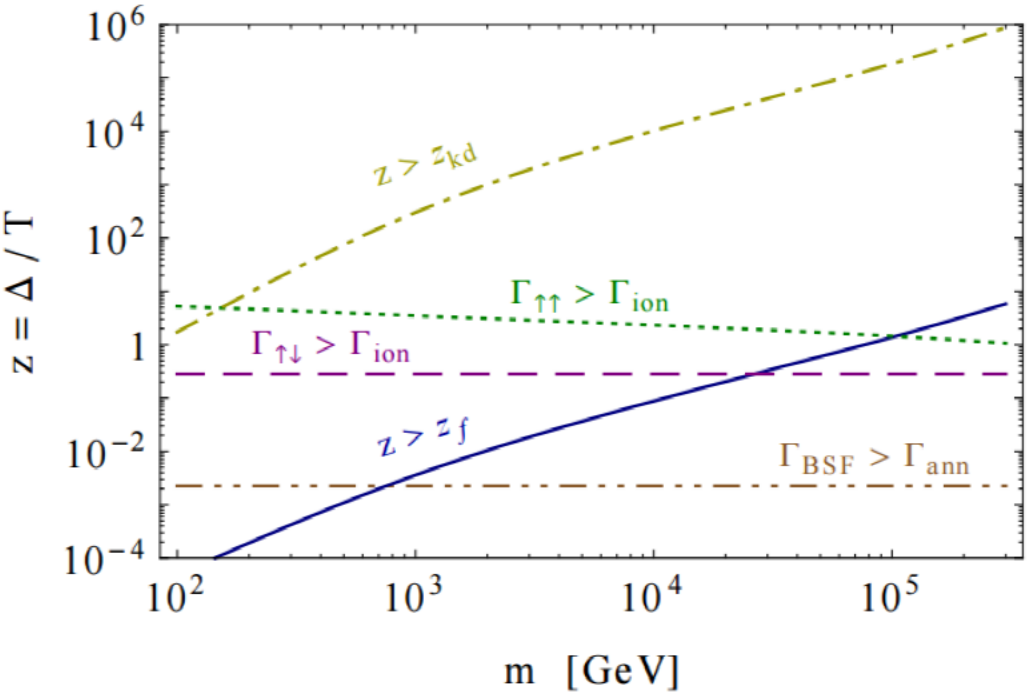
Yukawa Potential Bound States



$$V(r) = \alpha \frac{e^{-m_{\rm med} r}}{r}$$

$$T_{freeze} \sim \frac{m_\chi}{20}$$

Cosmological Rates



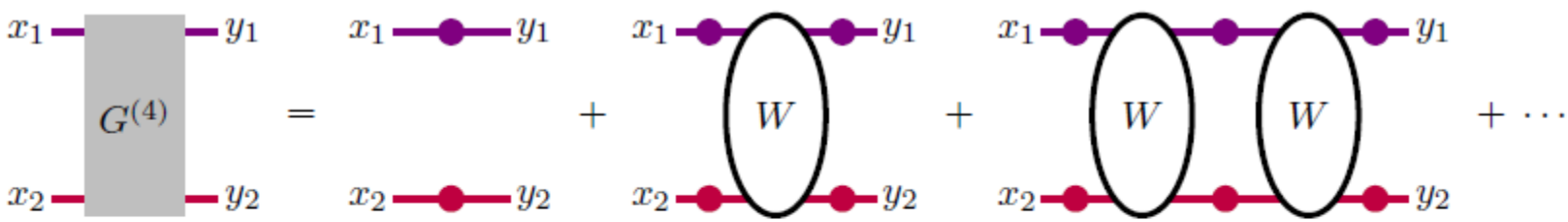
$$\Delta = \frac{m\alpha^2}{4}$$

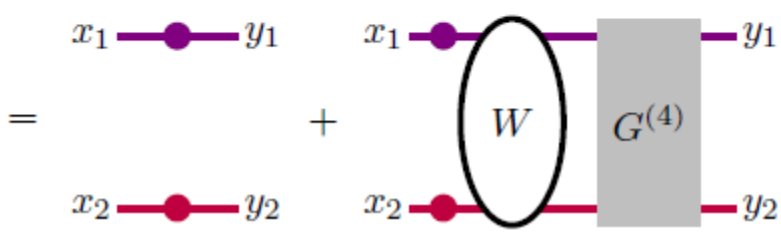
$\uparrow\downarrow$ and $\uparrow\uparrow$ bound states

von Harling and Petraki, 1407.7874

Bethe-Salpeter Equation

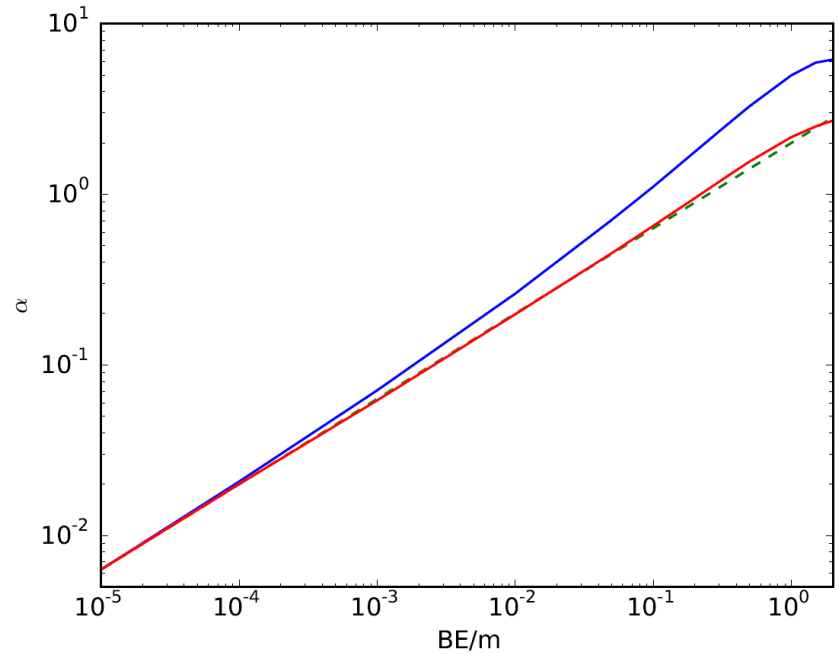
- States that are strongly bound enough to matter will have momenta high enough to require relativistic treatment
- If ladder diagrams are the dominant contribution to the binding the Bethe-Salpeter equation describes the physics





Relativistic Corrections

- States with binding energies of M/10 or larger require relativistic corrections to the coupling of a factor of 2 or more
- This will be an important shift in the cosmological implications of strong coupling



Outlook

- Perturbativity arguments can be made fully rigorous through unitarity considerations
- These unitarity bounds provide strong constraints on dark matter dynamics
- Combined with collider searches we will be able to place strong limits on WIMPs
- Models with strong coupling like these may already be affected by new phenomena due to bound state formation
  - Investigations of cosmological impact of bound state dynamics are in progress