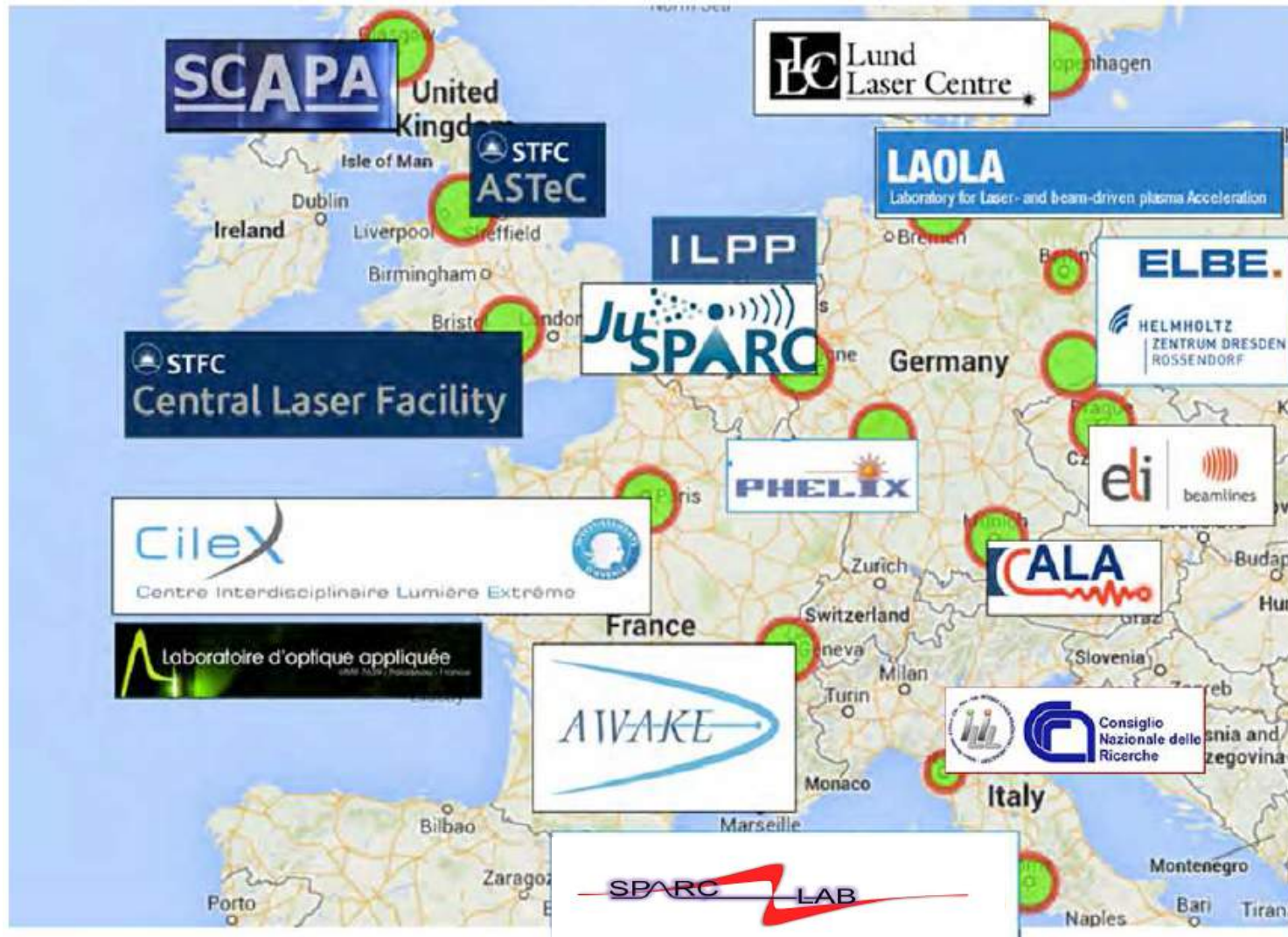
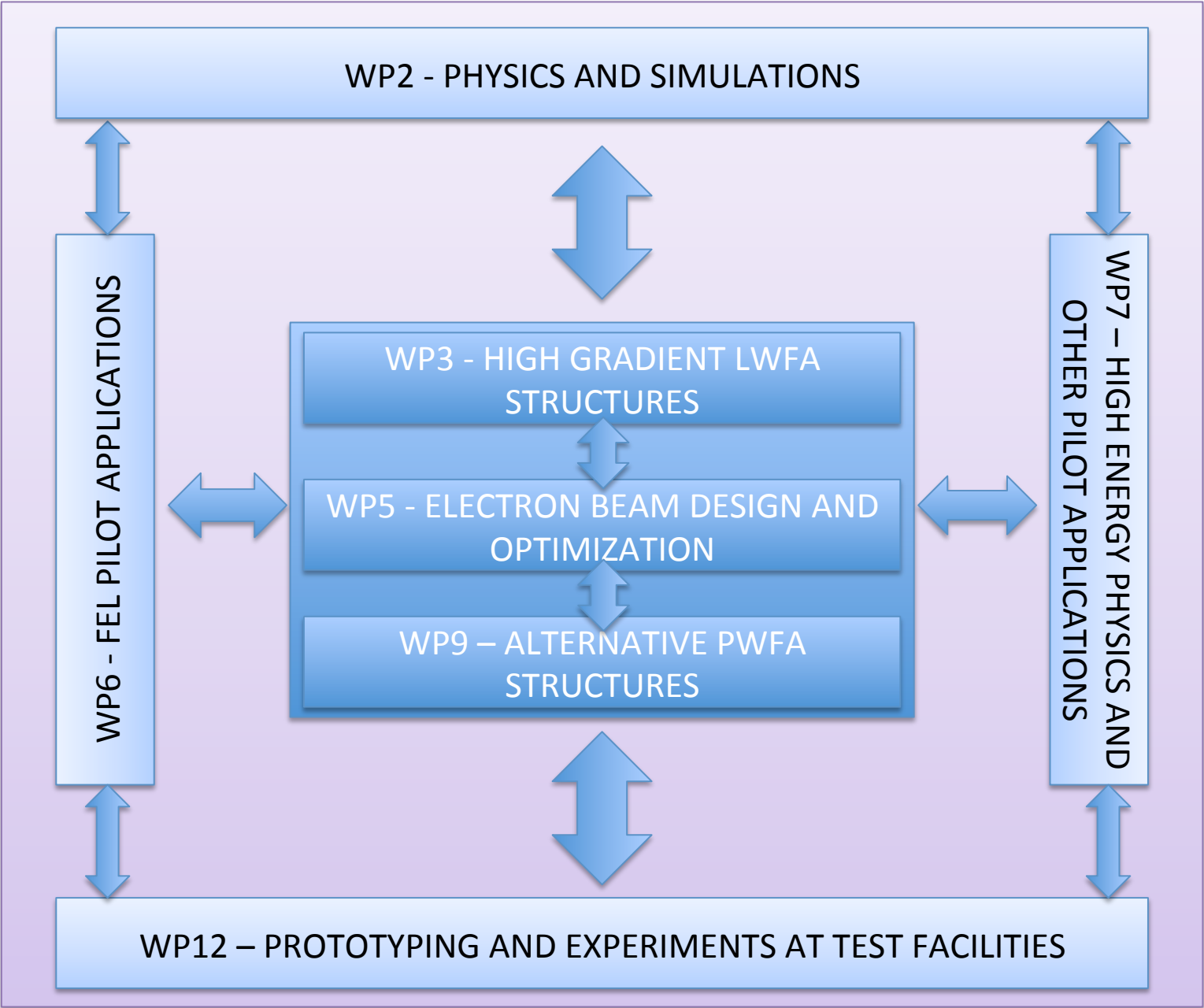


Test Facilities





SASE FEL at short wavelengths require a very high quality beam

- FEL Parameter

$$\rho \approx \frac{1}{4} \left(\frac{1}{2\pi^2} \frac{I_{pk}}{I_A} \frac{\lambda_u^2}{\beta \epsilon_N} \left(\frac{K}{\gamma} \right)^2 \right)^{1/3}$$

- Exponential growth

$$P(z) = \frac{P_0}{9} \exp\left(\frac{z}{L_G}\right)$$

- Gain Length

$$L_G = \frac{\lambda_u}{4\pi\sqrt{3}\rho}$$

- Saturation power

$$P_{sat} = \rho P_{beam} \propto N_e^{4/3}$$

- Constraint on emittance

$$\epsilon_n < \frac{\gamma \lambda_r}{4\pi}$$

- Constraint on energy spread

$$\Delta\gamma/\gamma < \rho$$

- Relative bandwidth

$$\frac{\Delta\omega}{\omega} = \sqrt{\frac{\rho}{N_u}}$$

$$\varepsilon_n^2 = \langle \gamma \rangle^2 \left(\sigma_E^2 \sigma_x^2 \sigma_{x'}^2 + \varepsilon^2 \right) \quad \text{General formula}$$

Emittance dominated beam drifting in vacuum

$$\varepsilon_n^2 = \langle \gamma \rangle^2 \left(s^2 \sigma_E^2 \sigma_{x'}^4 + \varepsilon^2 \right)$$

EXAMPLE: RF gun

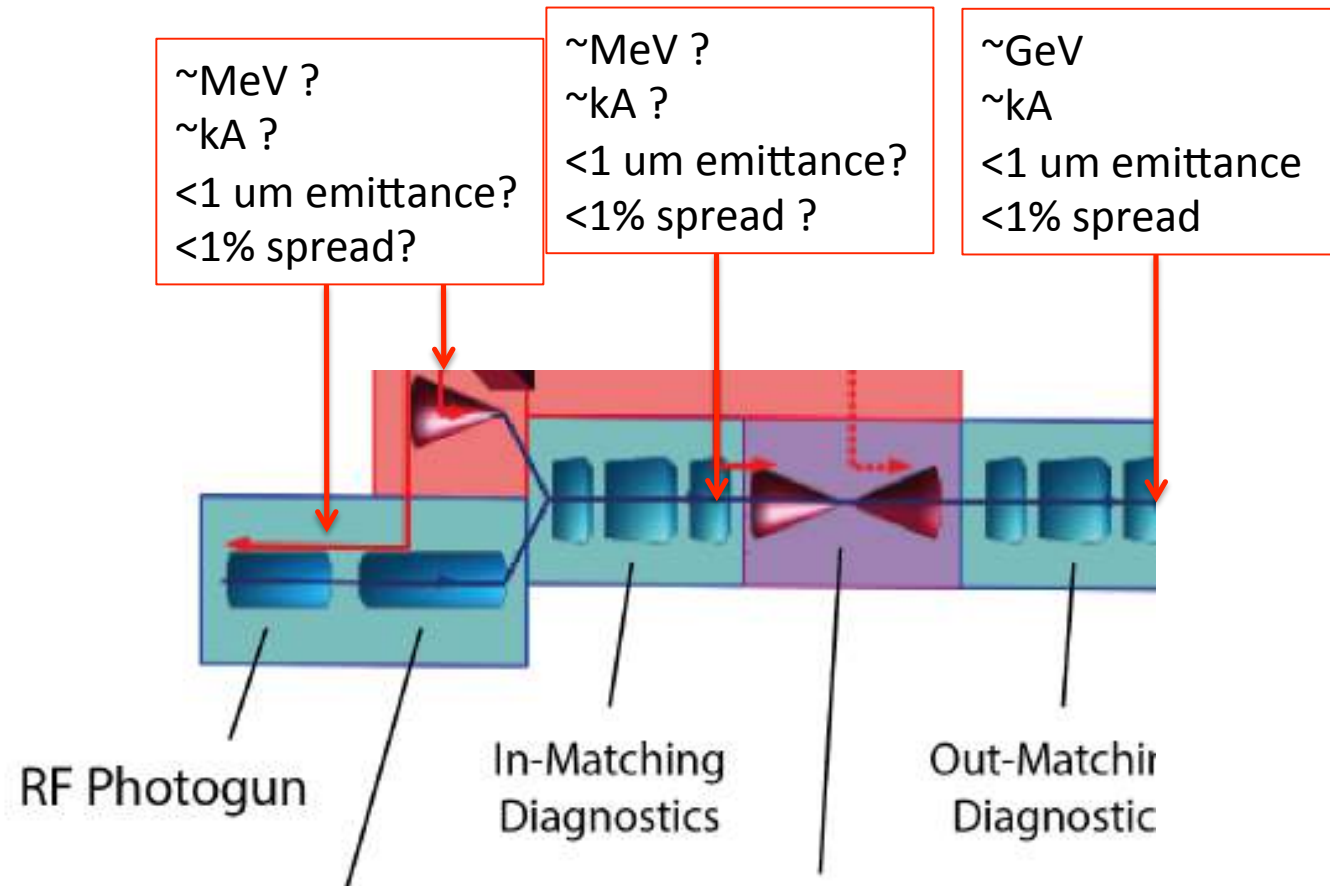
$\langle \gamma \rangle$	σ_E	σ_x	$\sigma_{x'}$	s	$s \sigma_E \sigma_{x'}^2$	$\gamma \varepsilon$	ε_n
12	9×10^{-3}	780 μm	1.1×10^{-4}	1 m	10 nm	1.01 μm	1.02 μm

EXAMPLE: GeV class beam from SELF INJECTION

$\langle \gamma \rangle$	$\sigma_E^{(0)}$	$\sigma_x^{(0)}$	$\sigma_{x'}^{(0)}$	s	$s \sigma_E \sigma_{x'}^2$	$\gamma \varepsilon$	ε_n
1800	6.4×10^{-2}	0.49 μm	2.9×10^{-2}	1 m	0.94 mm	2.5 μm	~ 1 mm

- K. Floettmann, *Some basic features of beam emittance*, Phys. Rev. STAB **6**, 034202 (2003).
- T. Mehrling *et al.*, *Transverse growth in staged-wakefield acceleration*, Phys. Rev. STAB **15**, 111303 (2012).
- P. Antici *et al.*, *Laser-driven electron beamlines generated by coupling laser-plasma sources with conventional transport systems*, J. App. Phys. **112**, 044902 (2012).
- M. Migliorati *et al.*, *Intrinsic normalized emittance growth in laser-driven electron accelerators*, Phys. Rev. STAB **16**, 011302 (2013).

Beam parameters



We need a baseline design supported by start to end simulations

- Define beam parameters and pulse shaping at injection (internal/external) => **wp2+wp3+wp5+wp9**

- Verify need of longitudinal Compression => **wp2+wp5+wp9**

- Transport and Match the beam to the accelerating modules (staging) => **wp2+wp3+wp5+wp9+wp12**

- Capture the beam at extraction => **wp2+wp3+wp5+wp9+wp12**

- Energy spread final correction => wp2+wp5+wp12
- Define proper plasma and single shot (non intercepting) beam diagnostics => wp3+wp5
- Provide suitable Synchronization => wp2+wp3+wp5

Coherent phase space matching for staging plasma and traditional accelerator using longitudinally tailored plasma structure

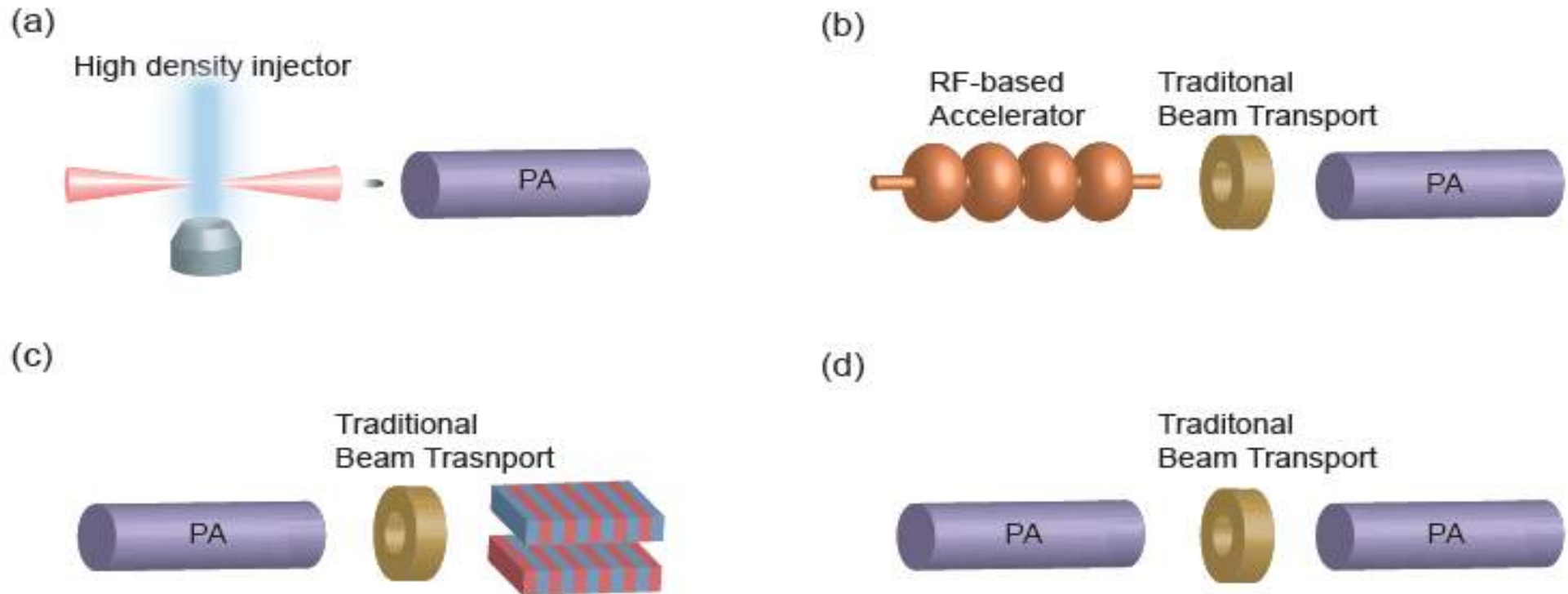
X. L. Xu,¹ Y. P. Wu,¹ C. J. Zhang,¹ F. Li,¹ Y. Wan,¹ J. F. Hua,¹ C.-H. Pai,¹ W. Lu,^{1,*} P. Yu,² W. An,² W. B. Mori,² C. Joshi,² and M. J. Hogan³

¹Department of Engineering Physics, Tsinghua University, Beijing 100084, China

²University of Los Angeles, Los Angeles, California 90095, USA

³SLAC National Accelerator Laboratory, Menlo Park, California 94025, USA

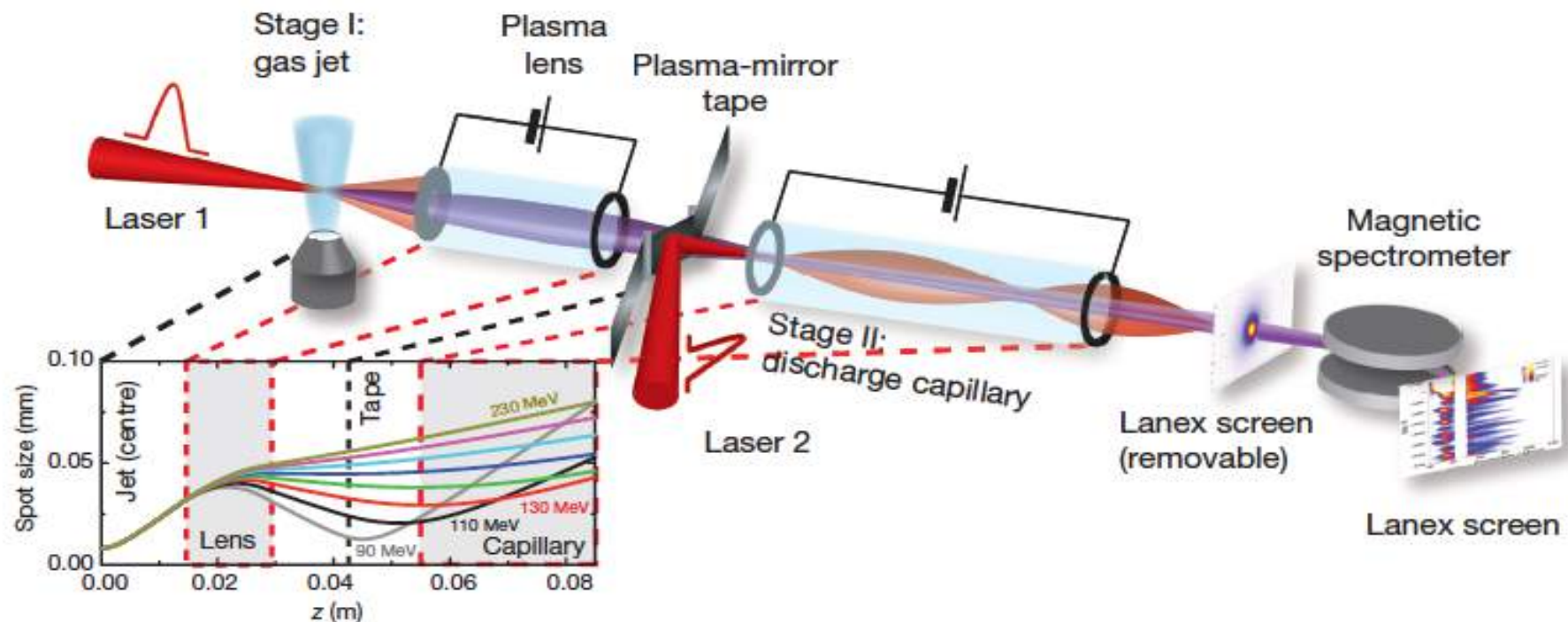
(Dated: November 18, 2014)



X. L. Xu et al., "Coherent phase space matching for staging plasma and traditional accelerator using longitudinally tailored plasma structure", arXiv:1411.4386v1

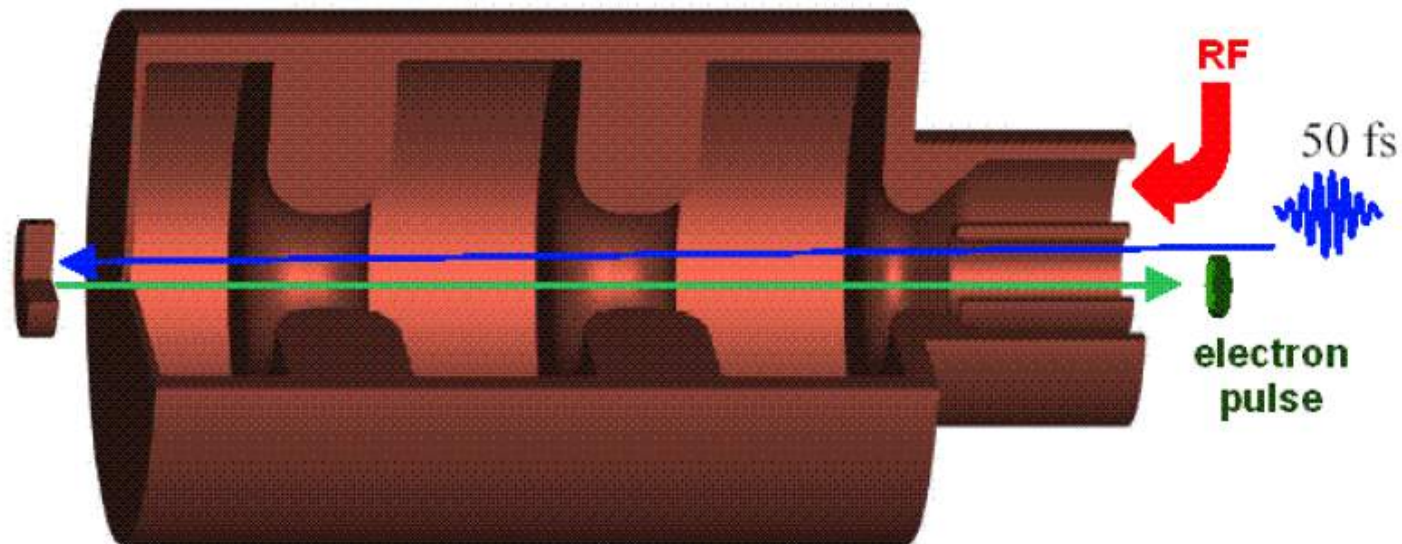
Multistage coupling of independent laser-plasma accelerators

S. Steinke¹, J. van Tilborg¹, C. Benedetti¹, C. G. R. Geddes¹, C. B. Schroeder¹, J. Daniels^{1,3}, K. K. Swanson^{1,2}, A. J. Gonsalves¹, K. Nakamura¹, N. H. Matlis¹, B. H. Shaw^{1,2}, E. Esarey¹ & W. P. Leemans^{1,2}



Injection schemes

- Self-injection.
- Optical injection.
- Density gradient injection.
- Ionization injection.
- Field ionization.
- External injection*.

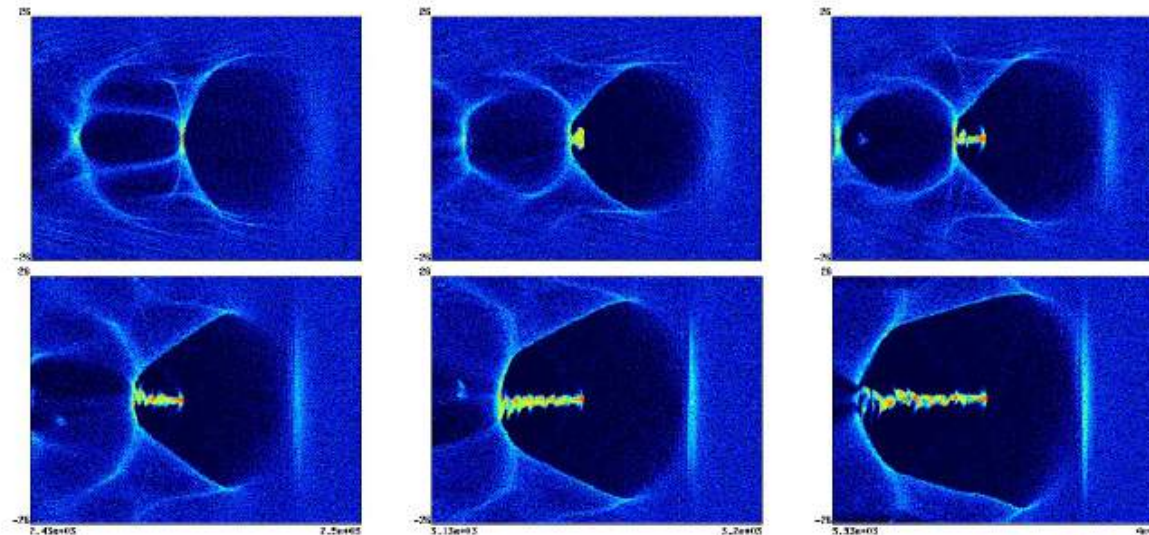


* C.E. Clayton and L. Serafini, IEEE Trans. Plas. Sci. **24**, 400 (1996)
 N.E. Andreev, S.V. Kuznetsov, Plas. Phys. Contr. Fus. **45**, 39 (2003)

Self-injection

Relays on wave breaking due to large amplitude fields, plasma wavefronts distortion, forward Raman scattering¹ and other non linear phenomena: very poor control on injected bunches.

$$a_0^2 > \gamma_p \approx \frac{\omega_0}{\omega_p}$$



Courtesy: C. Benedetti

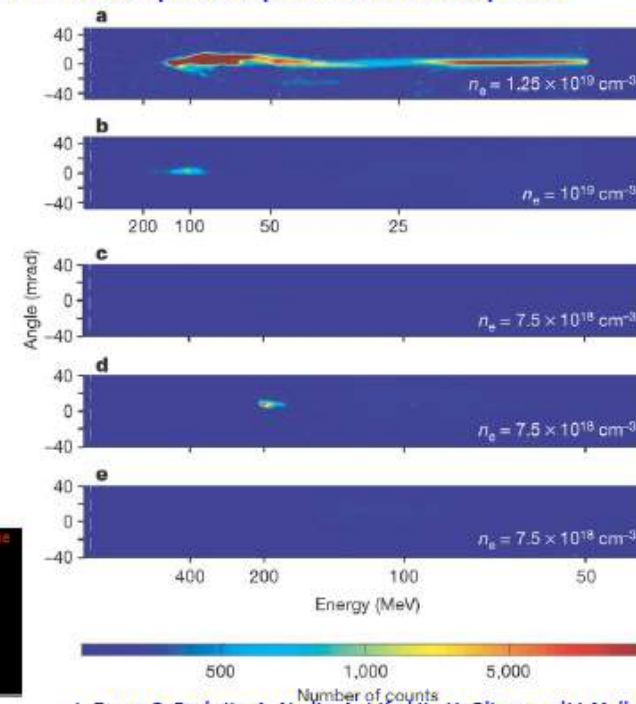
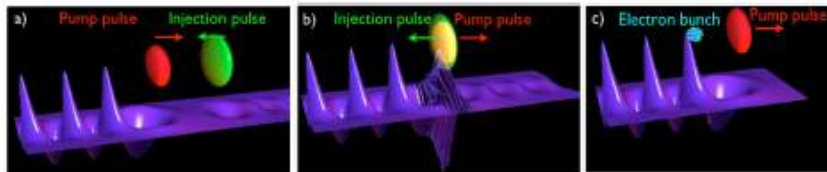
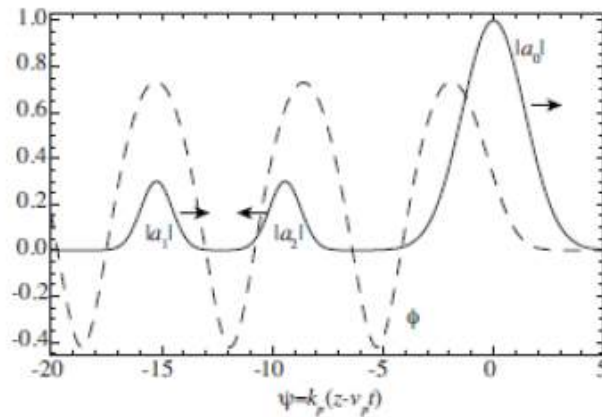
High charge bunches, “easy” to implement. Many experimental results.

[1] Modena, A., Z. Najmudin, A. E. Dangor, C. E. Clayton, K. A. Marsh, C. Joshi, V. Malka, C. B. Darrow, C. Danson, D. Neely, and F. N. Walsh, 1995, *Phys. Rev. Lett.* **75**, 3480.

Injection schemes

Optical injection: ponderomotive injection and colliding pulses

Two high intensity laser pulses¹ or three resonant lower energy laser pulses²: one pulse is the “pump” and drives the plasma wakefield; the others “push” background electrons into the accelerating bucket. Different blends but usually requires a complex experimental setup and a high degree of precision in space and time.



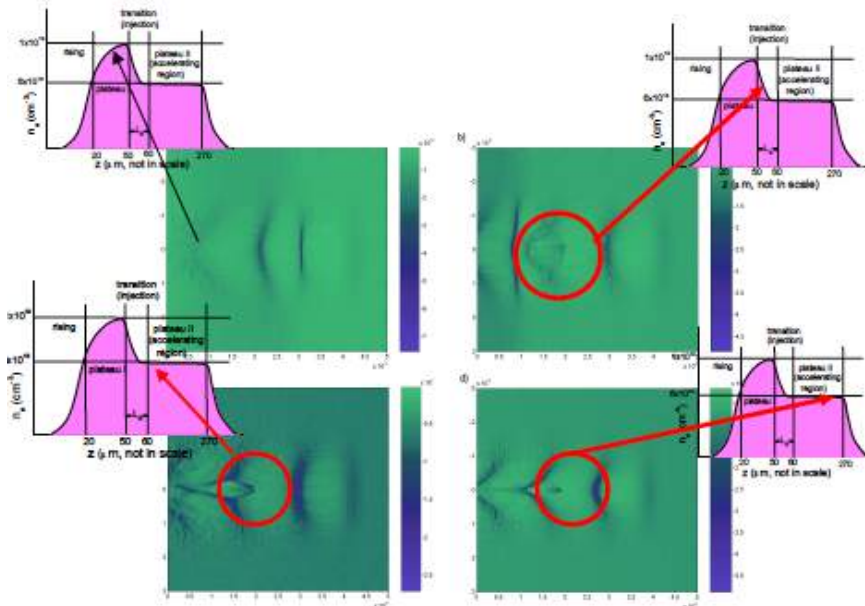
J. Faure, C. Rechatin, A. Norlin, A. Lifschitz, Y. Glinec, and V. Malka, *Nature* 444, 737 (2006).

[1] D. Umstadter, J. K. Kim and E. Dodd, 1996, *Phys. Rev. Lett.* **76** 2073.

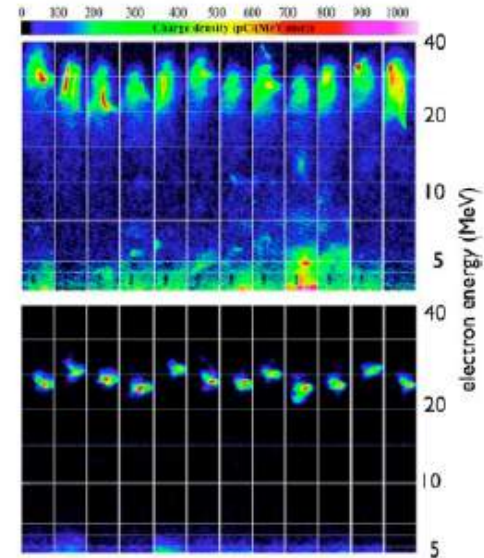
[2] E. Esarey, A. Ting, R. F. Hubbard, W. P. Leemans, J. Krall, and P. Sprangle, *Phys. Rev. Lett.* 79, 2682 (1997).

Density gradient injection

A decreasing plasma density¹ causes the plasma wavelength to increase so that background electrons are enclosed in the larger bubble.



V. Petrillo, L. Serafini and P. Tomassini, Phys. Rev. STAB **11**, 070703 (2008)

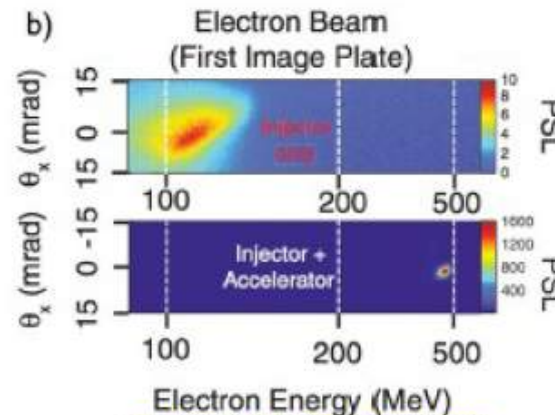
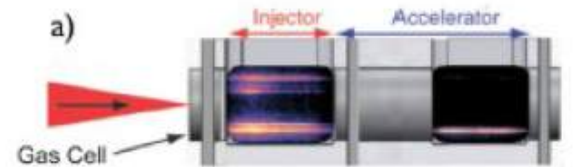
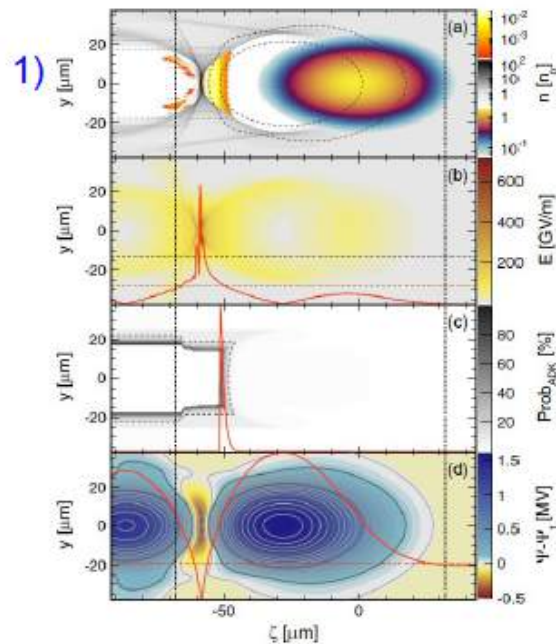


Schmid et al., Phys. Rev. STAB **13**, 091301 (2010).

[1] Bulanov, S., N. Naumova, F. Pegoraro, and J. Sakai, 1998, Phys. Rev. E **58**, R5257.

Injection by ionization/1

The plasma is composed by a mixture of gases, with different ionization energies. One is ionized by the wave driver and forms the plasma wave, the other is ionized either by the plasma field¹ or by an injection laser and the ionized electrons form the injected bunch. In LWFA this last technique takes the name of ionization injection².

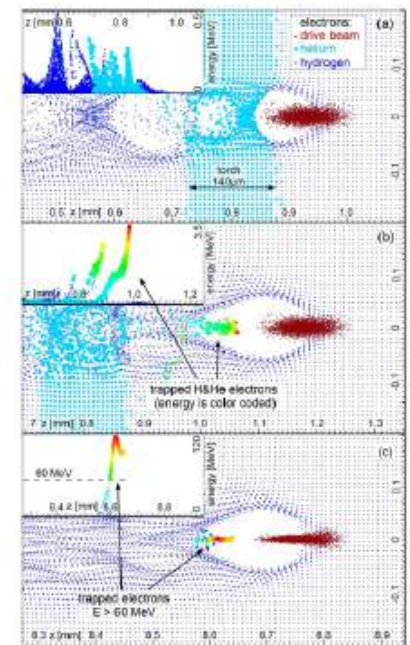
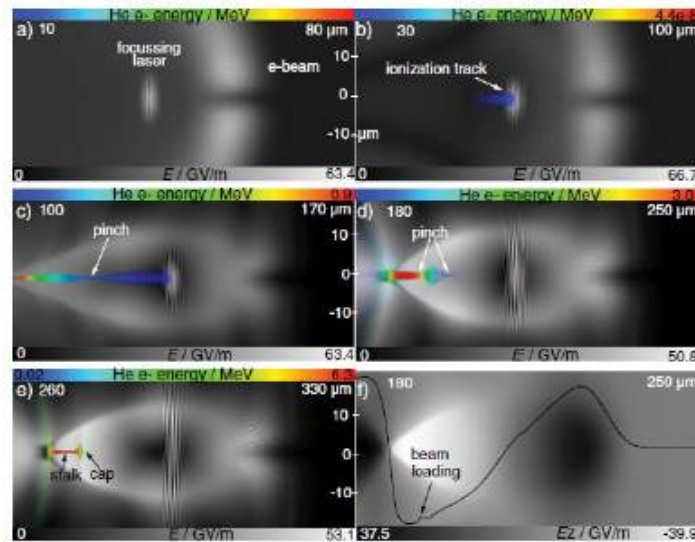


Pollock et al., Phys. Rev. Lett. 107, 045001 (2011).

- [1] A. Martinez de la Ossa, J. Grebenyuk, T. Mehrling, L. Schaper, and J. Osterhoff, Phys. Rev. Lett. **111**, 245003 (2013).
 [2] E. Oz, et al., Phys. Rev. Lett. **98**, 084801 (2007).

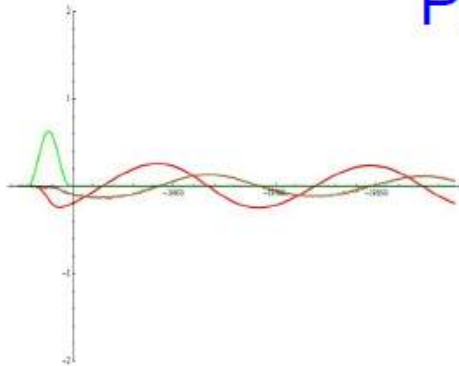
Injection by ionization/2

In PWFA, ionization injection is named Trojan Horse¹. A rather new mechanism, injection by plasma torch², is between ionization injection and density gradient.



- [1] B. Hidding, G. Pretzler, J. B. Rosenzweig, T. Königstein, D. Schiller, and D. L. Bruhwiler, *Phys. Rev. Lett.* **108**, 035001 (2012).
 [2] G. Wittig, et al., *Nuc. Inst. Meth. Phys. Res. A*, <http://dx.doi.org/10.1016/j.nima.2016.02.027> (in press).

Linear



Easier and more stable but beam loading can dominate the process. Requires the capability to manage bunches with a charge in the range from hundreds of fC to few pC.

$$a_0 \ll 1$$

$$\alpha = \frac{n_b}{n_0} \ll 1$$

$$\tilde{Q} = Qk_p^3 \ll 1$$

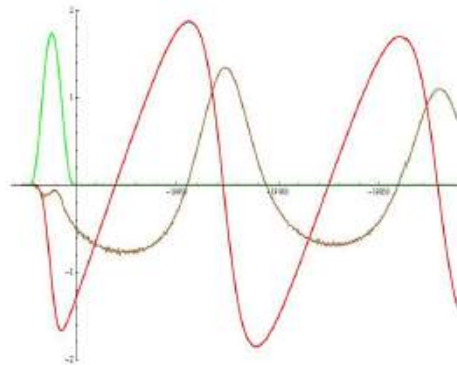
Plasma wave regime

$$a_0 \approx 1$$

$$\alpha \approx 1$$

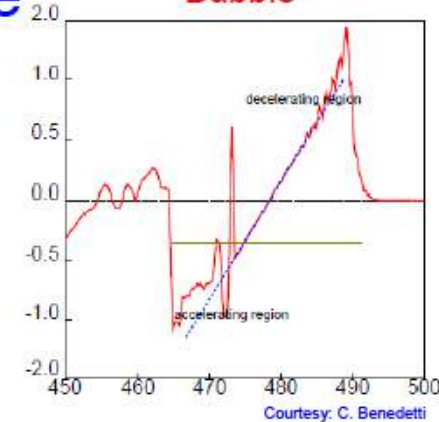
$$\tilde{Q} < 1$$

Quasi-linear



Fields are quite intense so performances can be very interesting. Beam loading is significant but manageable with bunch charges up to few tens of pC.

Bubble



Regime with wider diffusion because of ease in implementation. However, it's the least manageable, due to high sensitivity to jitters. Extremely intense fields for top performances; beam loading is usually not a problem up to few hundreds of pC.

$$a_0 \gg 1$$

$$\alpha > 1$$

$$\tilde{Q} > 1$$

Matching into plasma

It's easy to find matching conditions for bubble regime with negligible beam loading:

$$\sigma_{\text{tr,match}} = \sqrt[4]{\frac{2}{\gamma}} \sqrt{\frac{\epsilon_n}{k_p}}$$

Typical values are in the order of 0.1 – 1 μm .

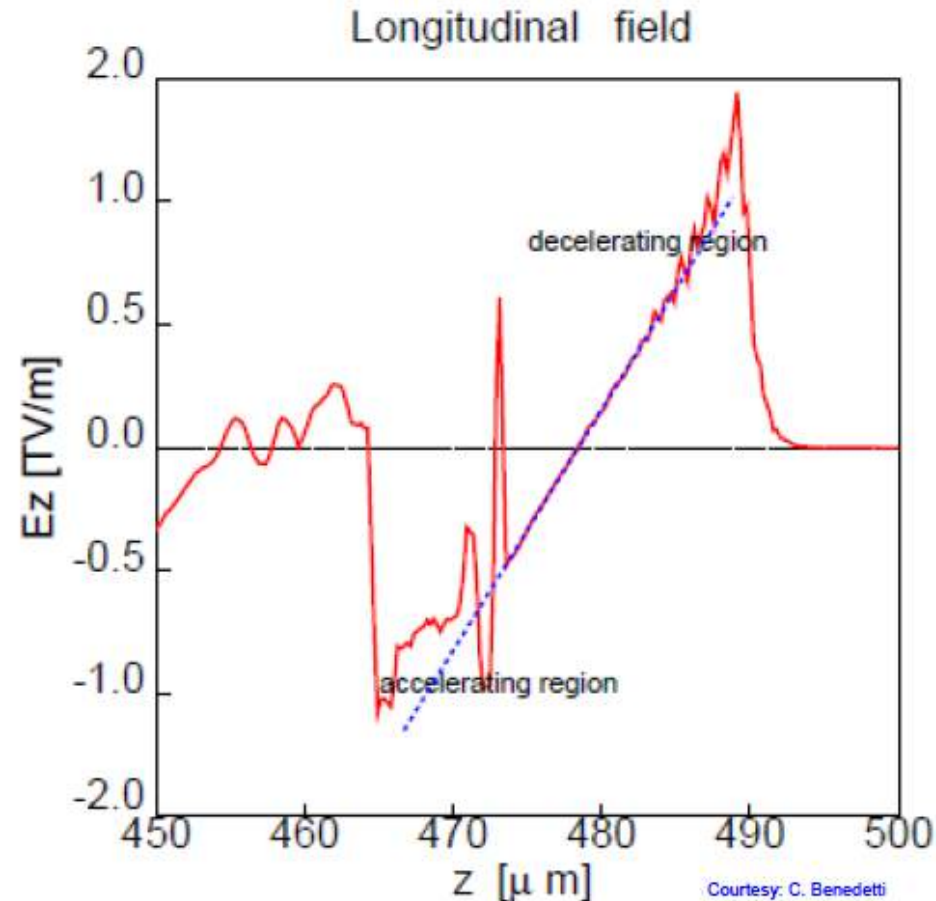
For a **quasi-linear** plasma wave regime matched spot-sizes have the same order of magnitude. If the plasma driver transverse size is always much larger than the beam size, transverse fields can be considered linear, although they depend on ζ .

In **linear regime** the same considerations on the nature of transverse fields hold true, **but beam loading is usually not negligible**, unless charge is very low.

Beam loading

Beam loading is the perturbation to the plasma fields due to the witness bunch self-fields. Generally speaking:

- Modifies the total fields acting on the witness.
- May reduce acceleration performances.
- May be used for reducing energy spread.
- Depends on witness current.
- Its effects depend on the intensity of plasma fields, hence also on plasma wave regime.
- Requires very fine tuning if used for reducing energy spread.

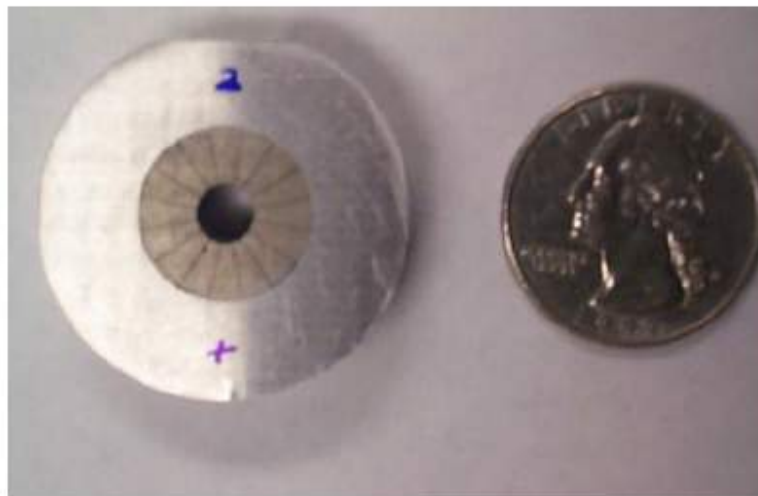


Beam Manipulation



Matching into/out of plasma/1

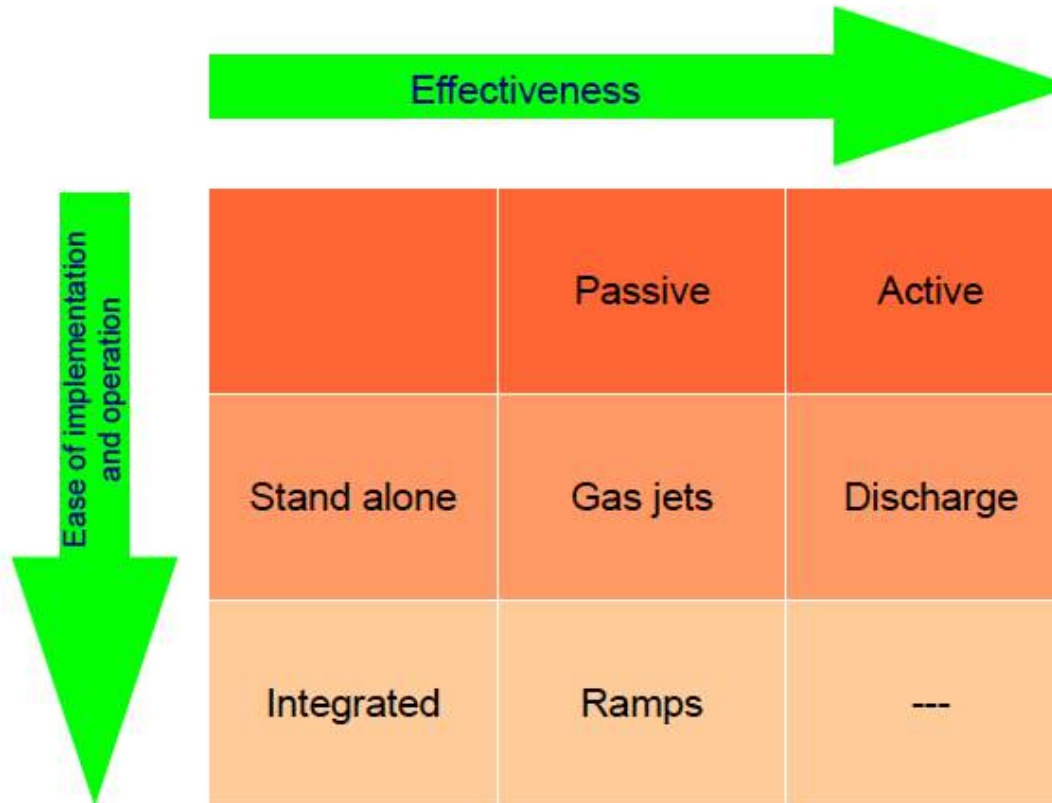
More conventional solutions: high performance beam optics like permanent magnet quadrupoles...



...reaching many hundreds of T/m gradients, adequate for energies up to few hundreds MeV.

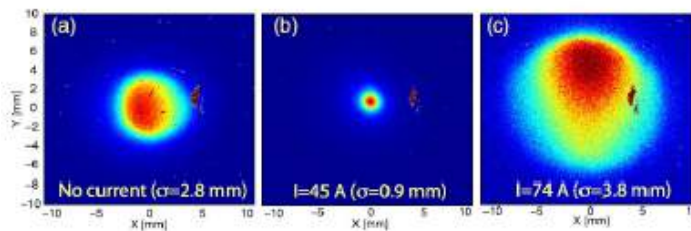
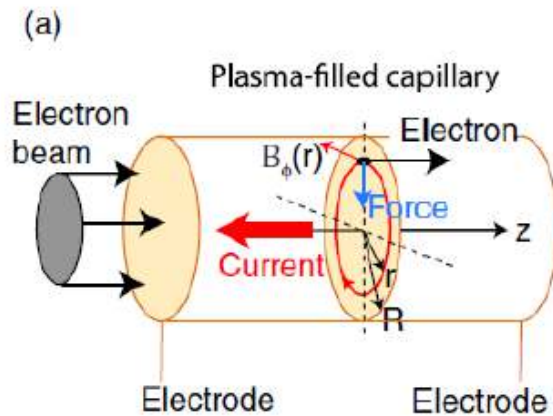
Matching into/out of plasma/2

Plasma lenses: classification



Stand alone, active plasma lens: discharge capillary¹

The beam goes through a capillary filled with gas, while a current is flowing in the capillary. If some (rather restrictive) conditions are met, the bunch is focused by the azimuthal magnetic field generated by the current density.



[1] J. van Tillborg, et al., Phys. Rev. Lett. **115**, 184802 (2015)

Favourable scaling

$$\partial B_\phi / \partial r = \mu_0 I_0 / (2\pi R^2)$$

able to easily reach thousands T/m gradients

Operation conditions:

$$\left(\frac{\sigma_z}{\sigma}\right)^2 J_{\text{beam}} \ll \frac{J_{\text{dis.}}}{2}$$

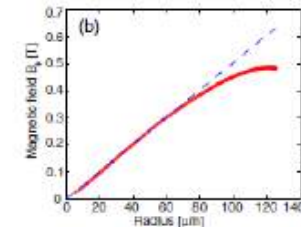
$$k_p \sigma \gg 1$$

$$k_p \sigma_z \ll 1$$

Requires a relatively long drift btw beam source and lens to operate correctly

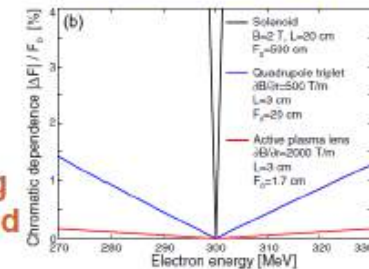
Effective only as a thin lens

Linear focusing field



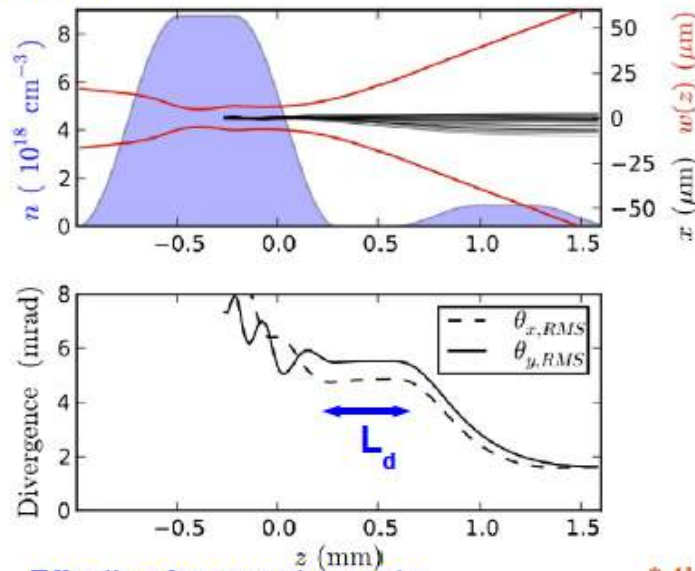
up to half R

Low chromaticity



Stand alone, passive plasma lens: gas jet¹

A gas jet, acting as plasma lens, is powered by the same laser extracting and accelerating the bunch



Density profile

$$n(z) = \begin{cases} n_1 & \text{for } z < 0 & \text{(First jet)} \\ 0 & \text{for } 0 < z < L_d & \text{(Drift space)} \\ n_2 & \text{for } L_d < z < L_d + L_2 & \text{(Second jet)} \end{cases}$$

Condition for optimal collimation*

$$\frac{\langle k_{\text{foc}} \rangle Z_R^2}{L_d + L_2} \tan \left(\frac{\langle k_{\text{foc}} \rangle Z_R^2}{L_d} - \frac{\langle k_{\text{foc}} \rangle Z_R^2}{L_d + L_2} \right) = 1$$

$$k_\beta = k_p / \sqrt{2\gamma}$$

Requires only one laser

Effective for energies up to

$$\gamma < \frac{3 a_0^2 Z_R^4}{5 L_d^2 w_0^2}$$

Easily tuned for different bunches

Adequate acceptance

* this relation was derived assuming a constant emittance during drift.

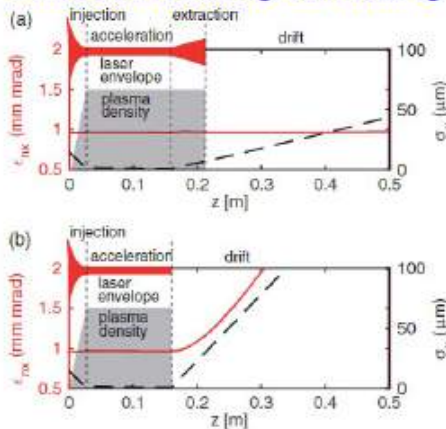
Beam loading may reduce effectiveness.

[1] R. Lehe, C. Thury, E. Guillaume, A. Lifschitz, and V. Malka, Phys. Rev. STAB **17**, 121301 (2014)

Integrated, passive plasma lens: plasma ramps & driver focusing/defocusing

A tapering at the end (beginning) of the plasma channel acts as a plasma lens and defocuses (focuses) the bunch performing matching. Moreover, the focusing (defocusing) of the driver helps in performing the process.

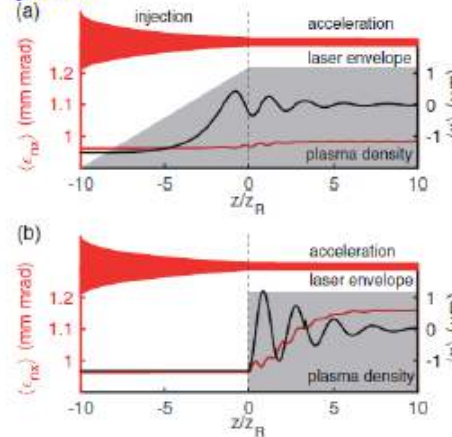
Emittance conservation and adiabatic focusing/defocusing



Linear regime

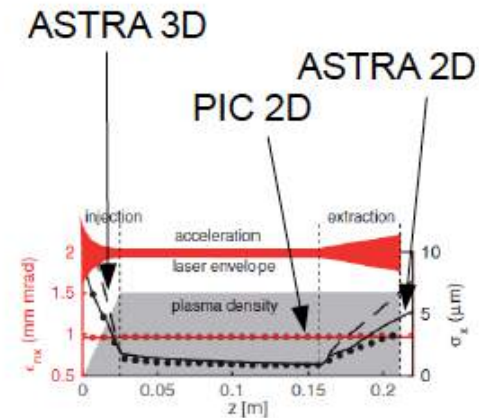
Negligible beam loading

Tolerance to beam position jitters



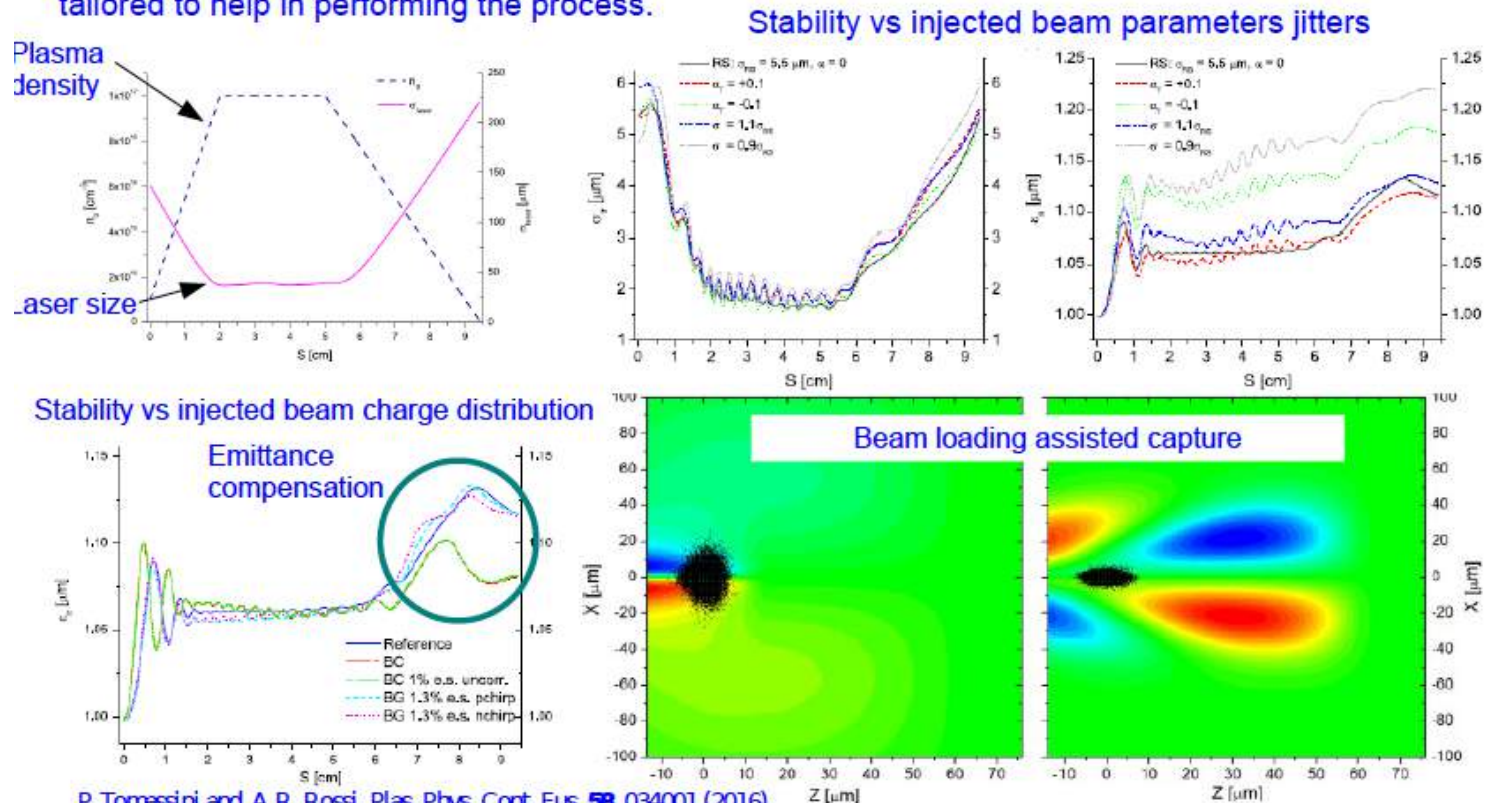
Optimal focusing strength longitudinal profile

$$K(z) = K_0 / (1 + gz)^4$$



Integrated, passive plasma lens: plasma ramps & tailored driver focusing/defocusing in hollow capillary

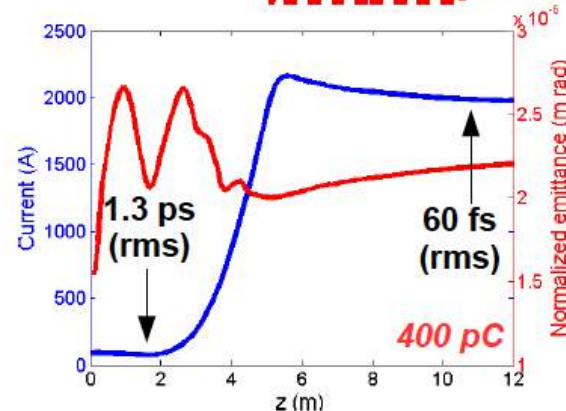
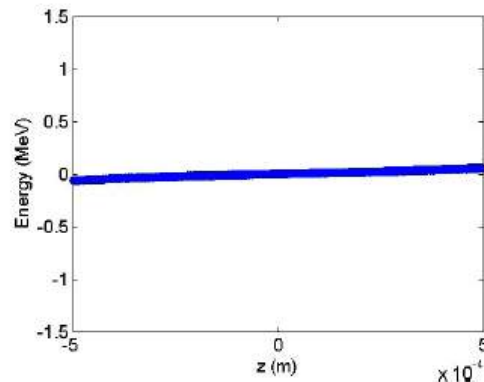
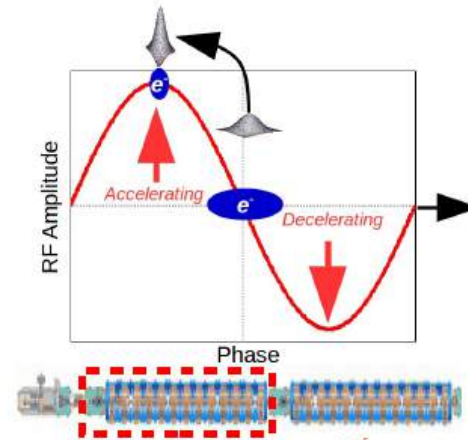
A tapering at the end (beginning) of the plasma channel acts as a plasma lens and defocuses (focuses) the bunch performing matching. Moreover, the focusing (defocusing) of the driver is tailored to help in performing the process.



P. Tomassini and A.R. Rossi, *Plas. Phys. Cont. Fus.* **58**, 034001 (2016).
 A.R. Rossi, et al., *Nuc. Met. Phys. Res. A*, <http://dx.doi.org/10.1016/j.nima.2016.02.015> (in press)

Ultra-short electron beams

- Current demands require high current beams
 - ✓ **PWFA-LWFA**: high wakefield amplitude (i.e. high driver density), low energy spread (i.e. short witness).
 - ✓ **Advanced radiation sources**: high peak currents (FEL), short beams (broadband THz radiation).
- Velocity bunching @ SPARC_LAB
 - ✓ **RF structure embedded in solenoid fields for emittance compensation**

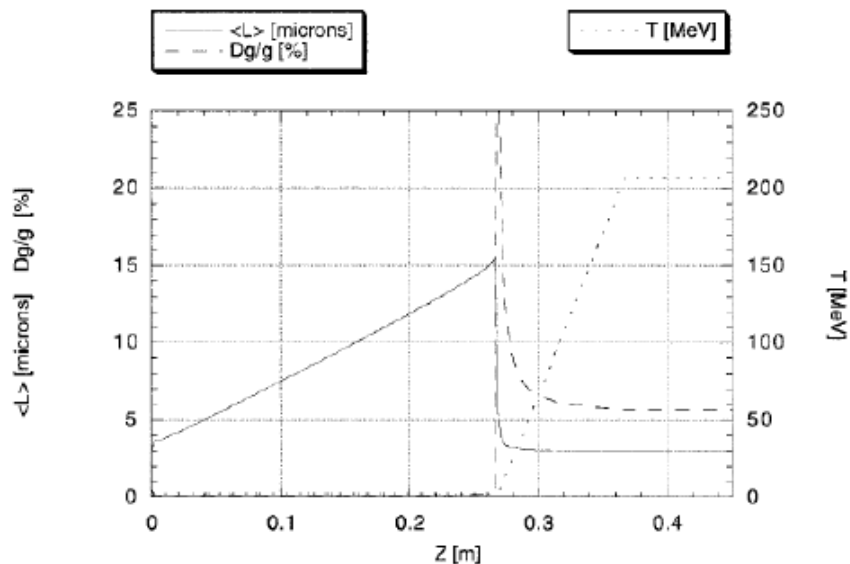


Serafini, L., M. Ferrario. "Velocity bunching in photo-injectors." AIP conference proceedings. 2001.

Ferrario, M. et al. "Experimental demonstration of emittance compensation with velocity bunching." PRL 104.5 2010.

Longitudinal compression

Longitudinal compression is possible when a bunch has an energy much lower than the resonant one, i.e. when the witness is (initially) much slower than the plasma wake¹, by velocity bunching².



M. Ferrario, T. C. Katsouleas, L. Serafini, and Ilan Ben Zvi, IEEE Trans. Plas. Sci. 28, (2000).

- Linear regime
- No beam loading

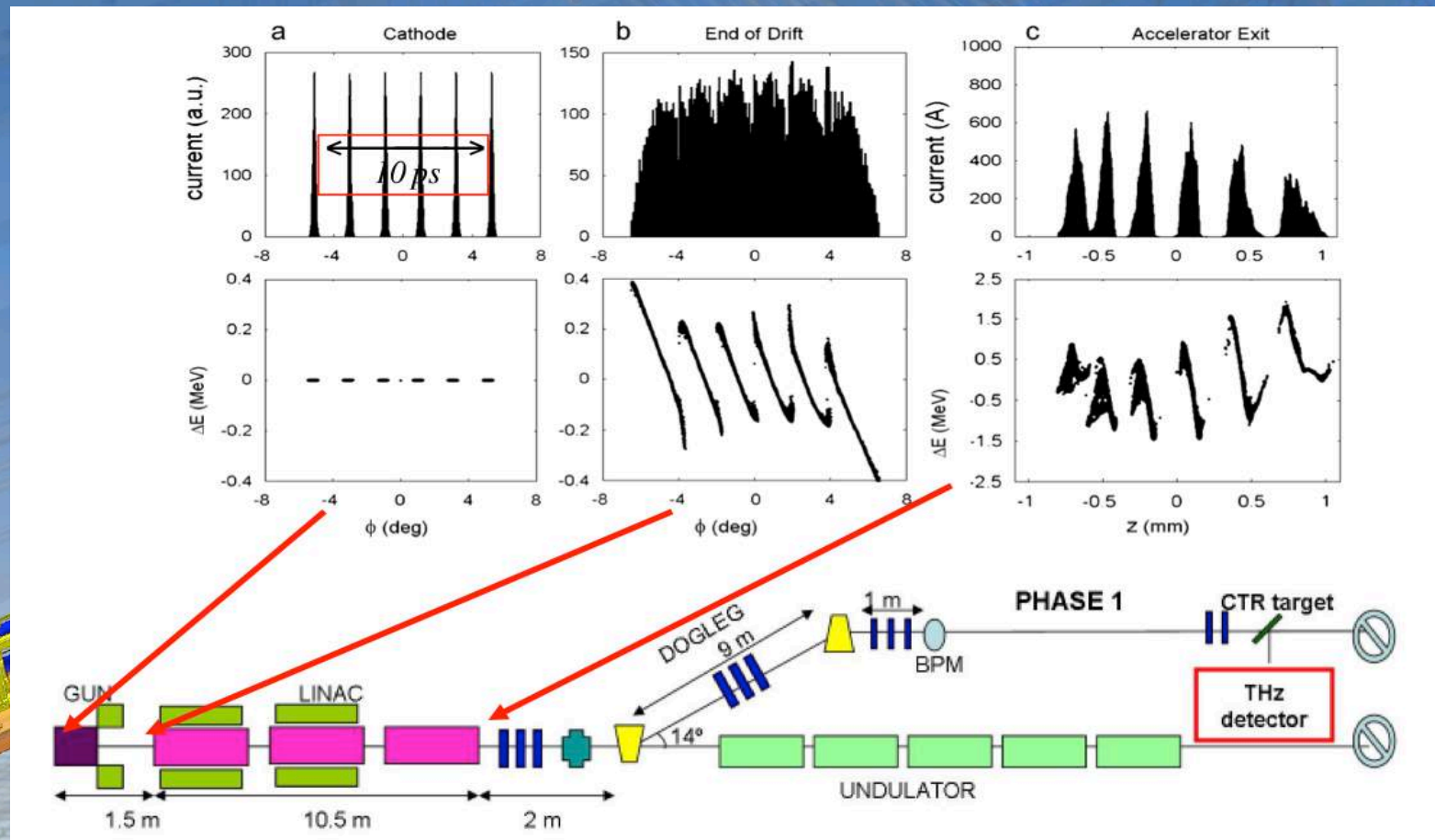
Further readings:

- S.V. Kuznetsov and N.E. Andreev, Plas. Phys. Rep. **27**, 372 (2001).
- N.E. Andreev and S.V. Kuznetsov, Plas. Phys. Cont. Fus. **45**, A39 (2003)
- S.V. Kuznetsov, Plas. Phys. Rep. **32**, 282 (2006).
- N.E. Andreev, et al., Nuc. Inst. Meth. Phys. Res. A **653**, 66 (2011).

[1] J.L. Bobin, in Proc. of the ECFA-CAS/CEFN-In-2P3-IRF/CEA-EPS Workshop, p. 58 (1987). C.S. Liu and V.K. Tripathi, *Interaction of electromagnetic waves with electron beams and plasmas*, World Scientific, Singapore, 1994.

[2] L. Serafini and M. Ferrario, LNF-00/036, 2000. L. Serafini and M. Ferrario, AIP Conf. Proc. **581**, 87 (2001).

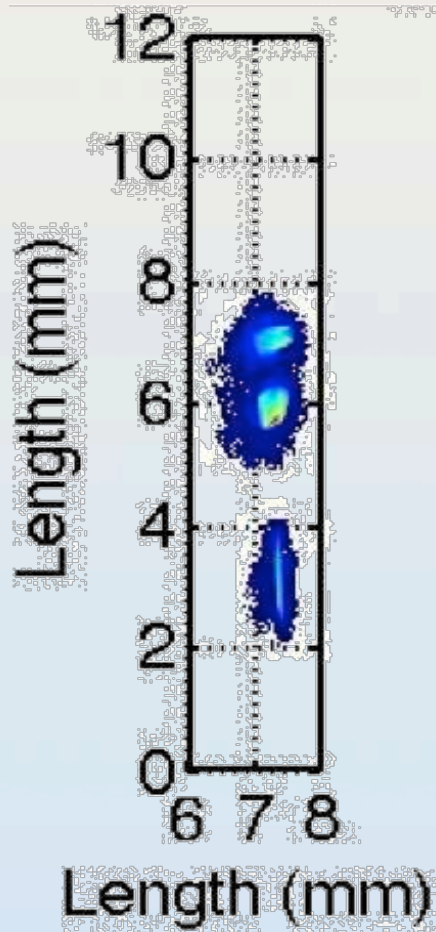
Laser Comb technique: generation of a train of short bunches



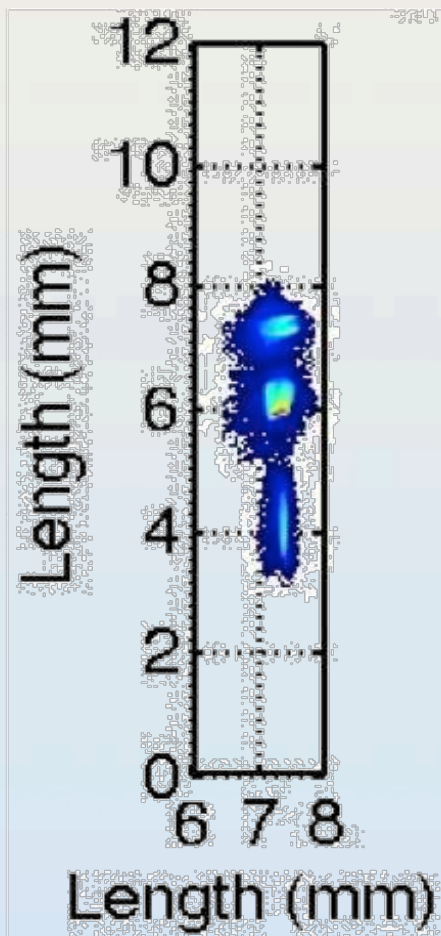
- P.O.Shea et al., Proc. of 2001 IEEE PAC, Chicago, USA (2001) p.704. (Low charge regime only)
- M. Ferrario, et al., Int. J. of Mod. Phys. B, 2006 (High charge, Beam Echo)

Three bunches: witness position tuning

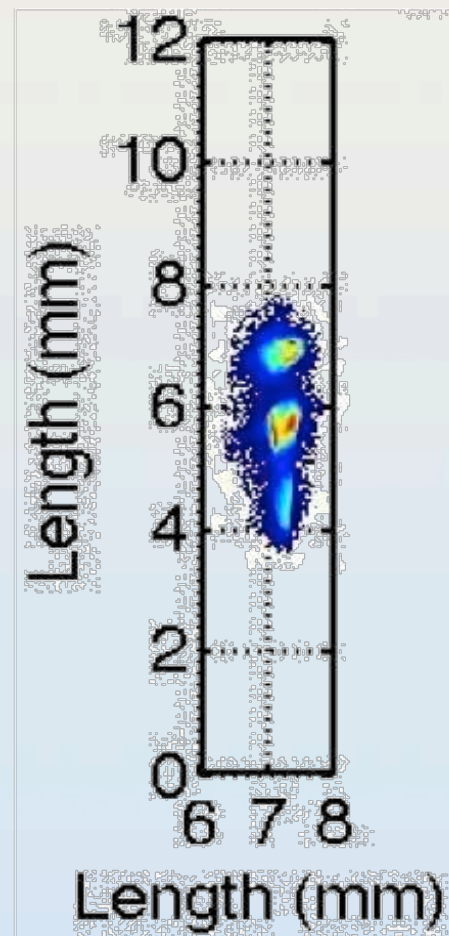
+ 1.67 ps



Reference



- 1.67 ps

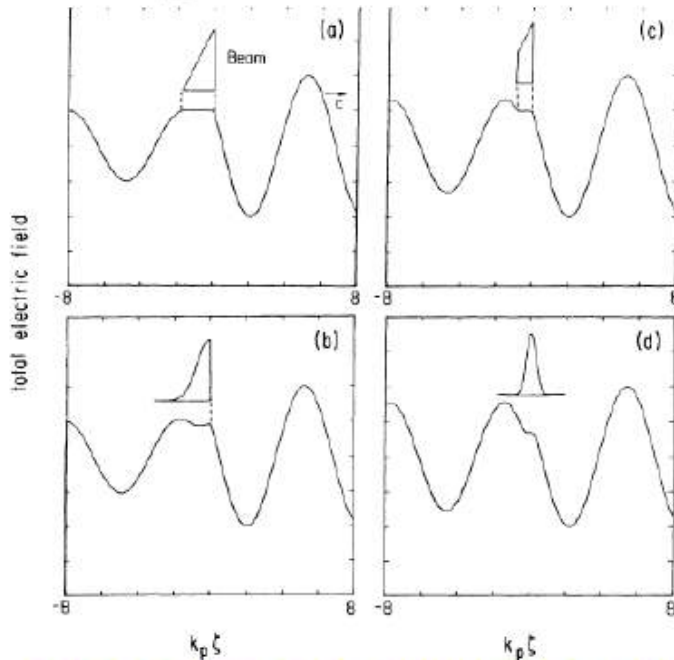


Energy spread control by beam loading

One way to limit energy spread in plasma is to “flatten out” the longitudinal field along the bunch by properly tailoring the beam loading.

Optimal beam profile for linear regime

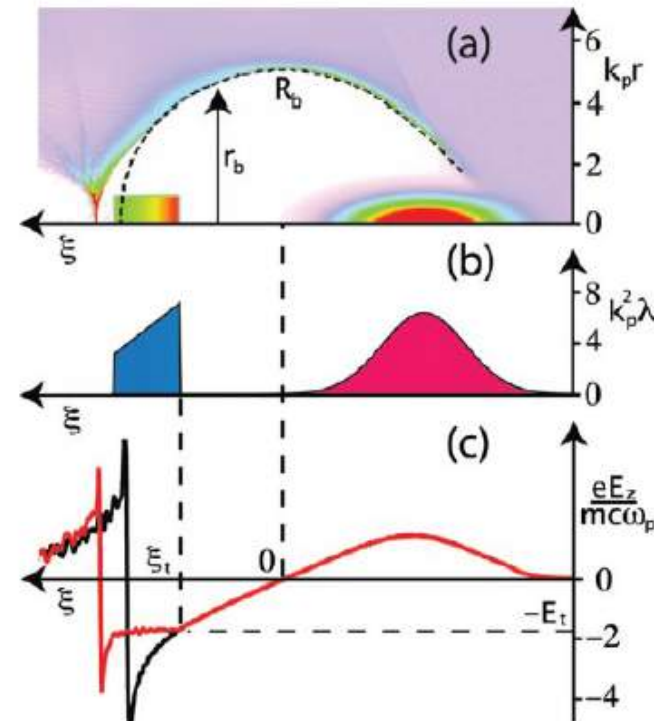
$$\rho_b(\xi) = -\frac{k_p E_0}{4\pi} [(k_p \cos k_p \xi_0)\xi + (\sin k_p \xi_0 - k_p \xi_0 \cos k_p \xi_0)]$$



T. Katsuleas, S. Wilks, P. Chen, J. M. Dawson and J. J. Su, *Particle Accelerators* **22**, 81 (1985)

Optimal beam profile for non-linear regime

$$\lambda(\xi) = E_i^2 + \frac{r_b^2}{4} = \frac{R_b^4 + r_i^4}{8r_i^2} - \sqrt{\frac{R_b^4 - r_i^4}{8r_i^2}} (\xi - \xi_i)$$



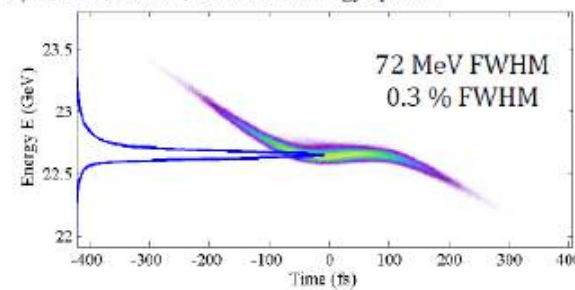
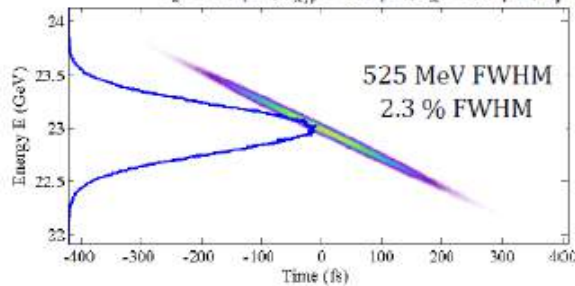
M. Tzoufras, et al., *Phys. Plas.* **16**, 056705 (2009)

Energy spread control by plasma dechirper¹

Following the idea of corrugated pipe dechirper², it is possible to arrange plasma density in order to act as a plasma dechirper.

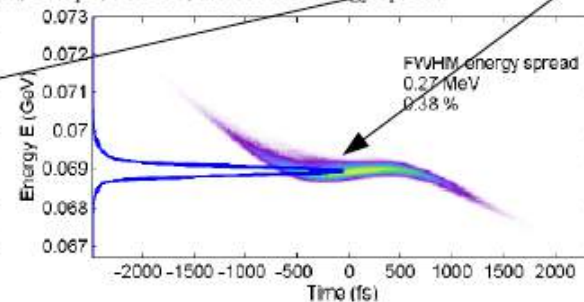
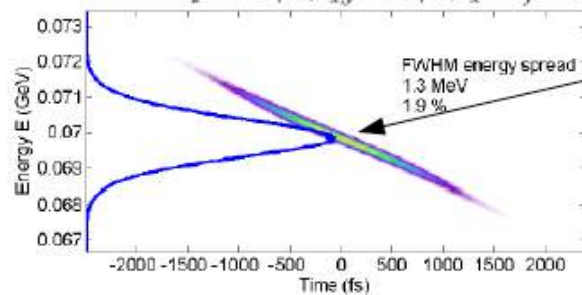
FACET beam parameters

$\sigma_z = 25 \mu\text{m}$, $\sigma_{x,y} = 30 \mu\text{m}$, $\epsilon_x = 50 \mu\text{m}$, $\epsilon_y = 5 \mu\text{m}$, 2 nC, 23 GeV, 1.0 % rms energy spread



ATF beam parameters:

$\sigma_z = 150 \mu\text{m}$, $\sigma_{x,y} = 50 \mu\text{m}$, $\epsilon_x = \epsilon_y = 1 \mu\text{m}$, 150 pC, 70 MeV, 1.0 % rms energy spread



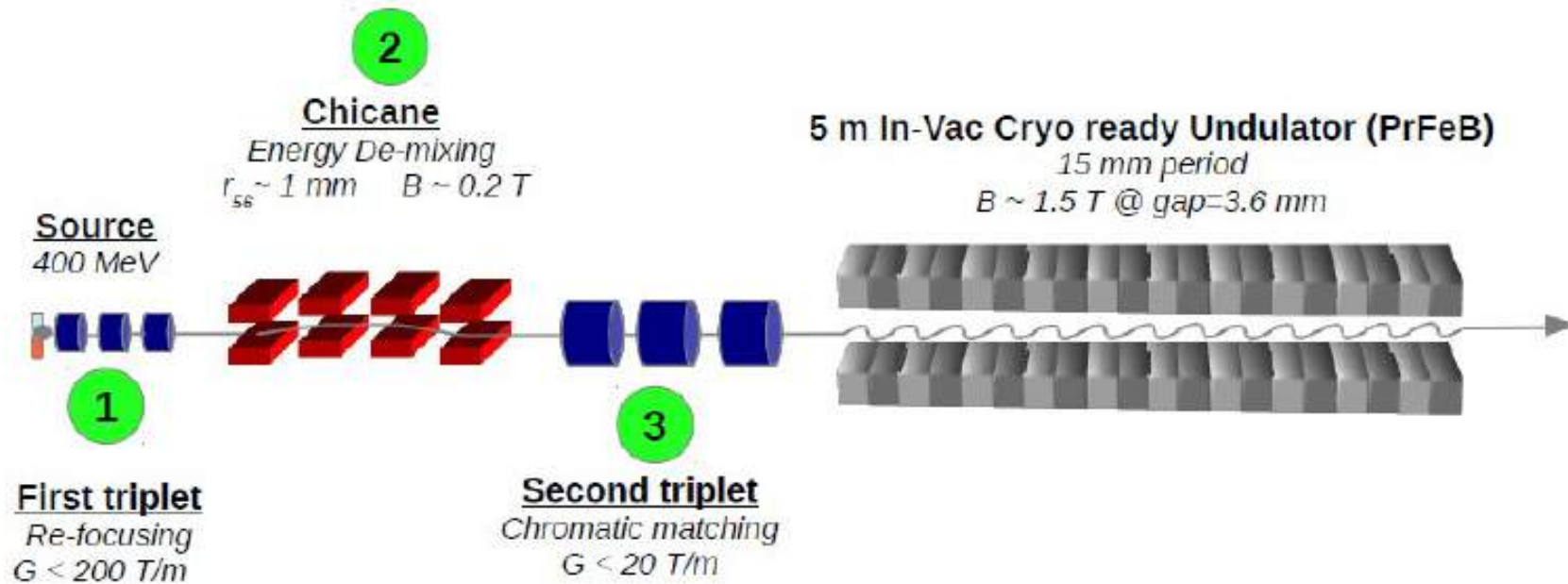
Works only for positive chirps

Uncorrelated energy spread is (irreversibly) increased

Tuning may still be quite critical

[1] V. Wacker, private communication (2015).

[2] K.L.F. Bane and G. Stupakov, Nuc. Inst. Meth. Phys. Res. **690**, 106 (2012). S. Antipov, et al., Phys. Rev. Lett. **112**, 114801 (2014).

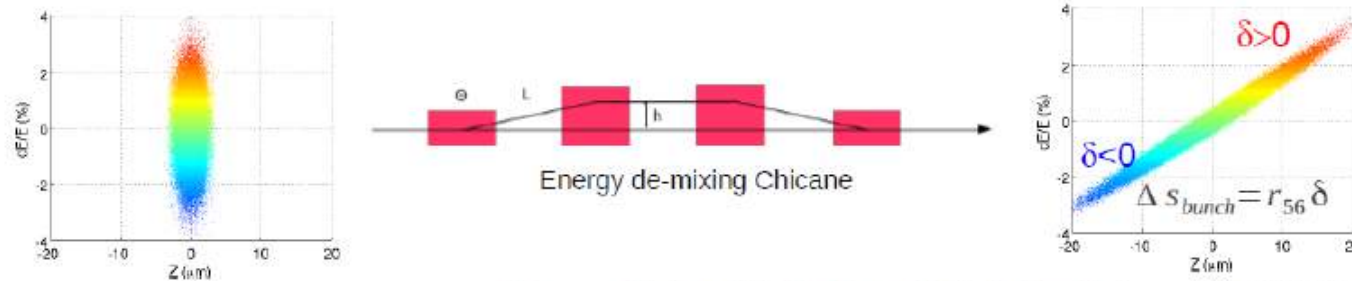


[1] A. Loulergue, M. Labat, C. Evain, C. Benabderrahmane, V. Malka and M.E. Couprie, *New J. Phys.* **17**, 023028 (2015).

Chromatic Matching

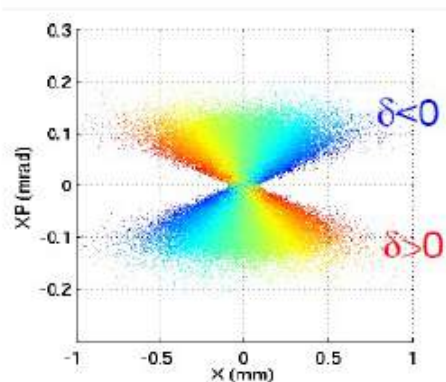
Assume a bunch with high energy spread and divergence. After first focusing use a chicane to stretch the bunch and realize an energy sorting (chirp):

Longitudinal phase space

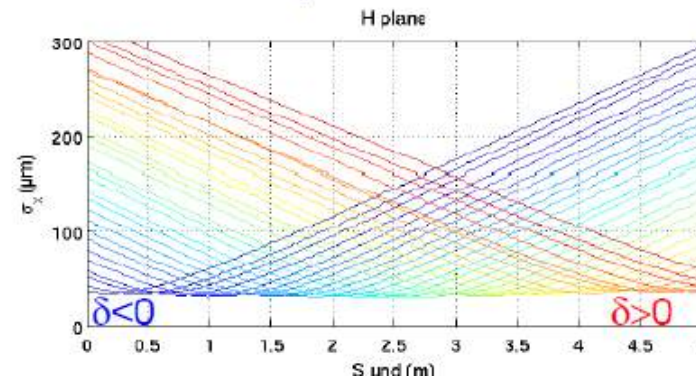


Pictures source: A. Loulergue, LWFA electron beam manipulations for FEL amplification, presented at EAAC 2015.

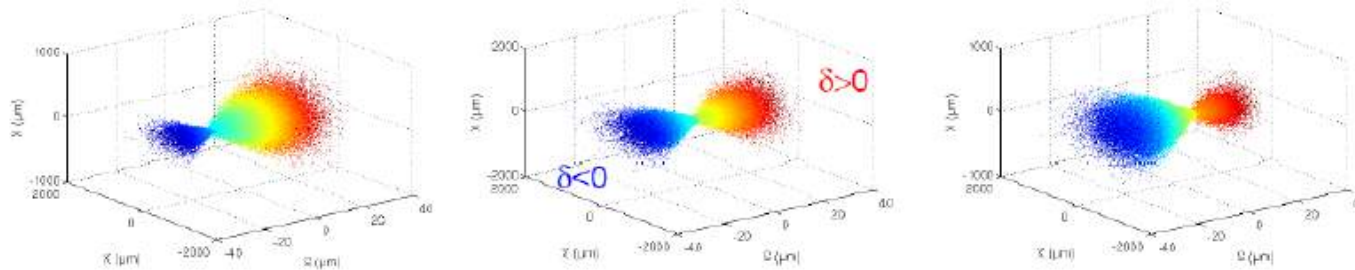
Transverse phase spaces



If the beam is focused, each quasi-monochromatic slice will have a waist at a different position.



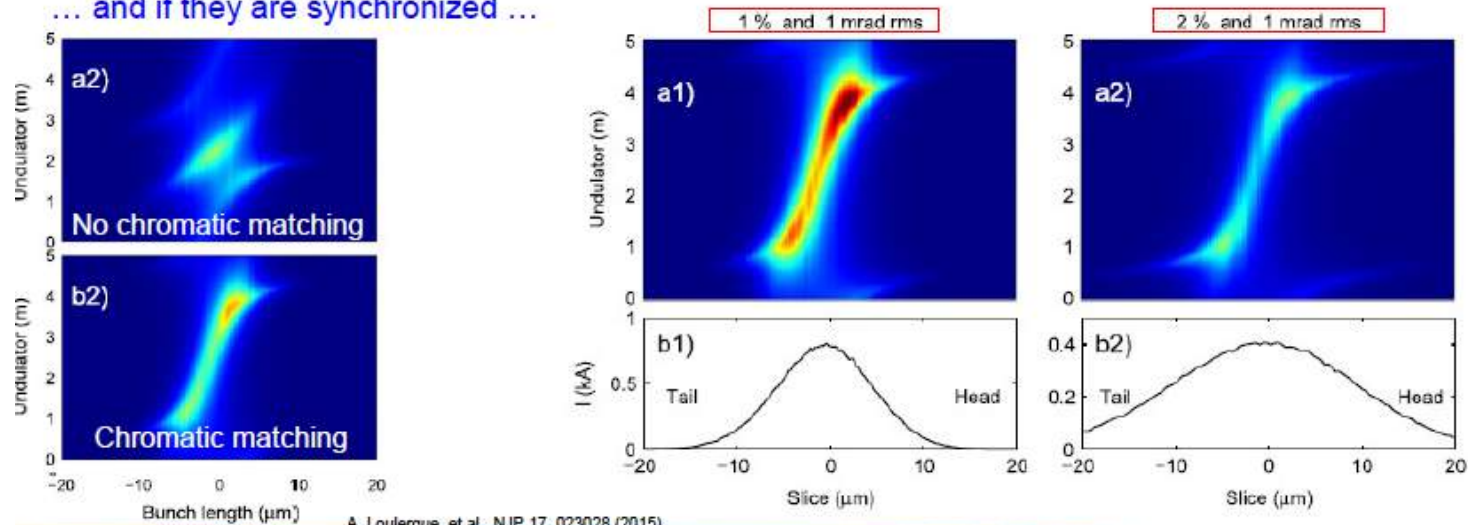
The waist slips along the bunch from the tail to the head...



Source: A. Loulergue, LWFA electron beam manipulations for FEL amplification, presented at EAAC 2015.

... pretty much like the FEL radiation ...

... and if they are synchronized ...



A. Loulergue, et al., NJP 17, 023028 (2015).

- Alban Mosnier wp2
 - Brigitte Cros wp3
- Enrica Chiadroni wp5
 - Jens Osterhoff wp9
- Andrea Mostacci wp12
 - Andrea Renato Rossi