

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31

# Restrictions on the heavy supersymmetry parameter space and simplified parametric scenarios in the effective field theory approach

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## General remarks

Two approaches to precise calculations of the Higgs mass  $m_h$  and the Higgs mass spectrum

- fixed order (up to 3-loop) calculations of the complete diagram set in the "full" MSSM. Uses fixed-order evaluations of the renormalized self-energies in the Higgs propagator matrix.

Preferrable for low MSSM scale, where logs  $\sim$  power terms.

- resummation in the effective theories (EFT). Uses resummation of certain classes of diagrams in the zero external momentum approximation. MSSM particles decouple at  $M_{SUSY}$  scale, are integrated out at the thresholds. Pole masses of scalars are evaluated for the two-doublet effective potential transformed to the mass basis.

Preferrable for high MSSM scales, where large logs should be resummed.

Evaluations in our case

- resummed effective one-loop two-doublet Higgs potential ( $\overline{MS}$  scheme) in the generic mass basis

- moderate  $m_A$  scenario, rotation to the Higgs basis is not used for matching with the low-energy SM-like model at  $m_A$  scale, so not specifically corrections to  $m_h$  but full spectrum of  $m_h, m_H, m_A$  and  $m_{H^\pm}$  defines the mass basis.

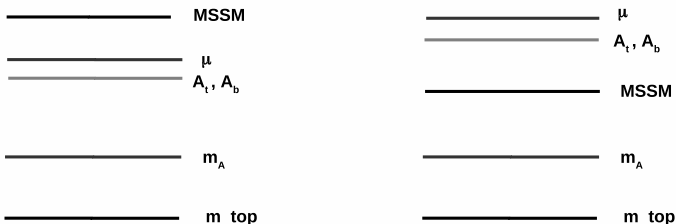
## Mass scales

The lightest CP-even MSSM Higgs boson mass  $m_h \sim 125 \text{ GeV}$

Five MSSM Higgs bosons:  $h, H, A, H^\pm,$

Calculation frameworks for  $m_h$ : effective potential decomposition in  $1/M_{SUSY}, \overline{MS}$  scheme, RGEs <sup>1</sup>

Mass scales for the  $\Delta\lambda_{\tau\tau}^{wf}$  scenario under consideration



Low-energy effective field theory at the scale higher than  $m_{top}$  is THDM. Higgsinos, gluino and EW gauginos are very heavy and decouple. Main corrections are due to squarks.

**Five-dimensional parameter space:**  $m_A, \tan \beta, M_{SUSY}, A_t = A_b, \mu$

<sup>1</sup>Haber,Hempfling,PR D48 4280 (1993); Sasaki,Carena,Wagner, NP B381 66 (1992); Akhmetzyanova,Dolgoplov,M.D. PR D71 075008 (2005); Phys.Part.Nucl. 37, 677 (2006); Lee,Wagner, PR D92, 075032 (2015) Carena,Haber,Low,Shah,Wagner PR D91 035003 (2015)

## THDM in the mass basis

Radiatively corrected Higgs sector of the MSSM is a THDM

$$\Phi_i = \begin{pmatrix} -i\omega_i^\pm \\ \frac{1}{\sqrt{2}}(v_i + \eta_i + i\chi_i) \end{pmatrix}, \quad \langle \Phi_i \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_i \end{pmatrix}, \quad i = 1, 2$$

$$\tan \beta = \frac{v_2}{v_1}, \quad v = \sqrt{v_1^2 + v_2^2} = 246 \text{ GeV}$$

where  $SU(2)$  states are related to mass states by means of two orthogonal rotations

$$\begin{pmatrix} \eta_1 \\ \eta_2 \end{pmatrix} = \mathcal{O}_\alpha \begin{pmatrix} h \\ H \end{pmatrix}, \quad \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} = \mathcal{O}_\beta \begin{pmatrix} G^0 \\ A \end{pmatrix}, \quad \begin{pmatrix} \omega_1^\pm \\ \omega_2^\pm \end{pmatrix} = \mathcal{O}_\beta \begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix}$$

where rotation matrix

$$\mathcal{O}_X = \begin{pmatrix} \cos X & -\sin X \\ \sin X & \cos X \end{pmatrix}, \quad X = \alpha, \beta. \quad (1)$$

## THDM Higgs potential in a generic basis

$$\begin{aligned}
 U_{eff}(\Phi_1, \Phi_2) = & -\mu_1^2(\Phi_1^\dagger\Phi_1) - \mu_2^2(\Phi_2^\dagger\Phi_2) - \mu_{12}^2(\Phi_1^\dagger\Phi_2) - (\mu_{12}^2)^*(\Phi_2^\dagger\Phi_1) \\
 & + \lambda_1(\Phi_1^\dagger\Phi_1)^2 + \lambda_2(\Phi_2^\dagger\Phi_2)^2 + \lambda_3(\Phi_1^\dagger\Phi_1)(\Phi_2^\dagger\Phi_2) + \lambda_4(\Phi_1^\dagger\Phi_2)(\Phi_2^\dagger\Phi_1) \\
 & + \frac{\lambda_5}{2}(\Phi_1^\dagger\Phi_2)^2 + \frac{\lambda_5^*}{2}(\Phi_2^\dagger\Phi_1)^2 + \lambda_6(\Phi_1^\dagger\Phi_1)(\Phi_1^\dagger\Phi_2) + \lambda_6^*(\Phi_1^\dagger\Phi_1)(\Phi_2^\dagger\Phi_1) \\
 & + \lambda_7(\Phi_2^\dagger\Phi_2)(\Phi_1^\dagger\Phi_2) + \lambda_7^*(\Phi_2^\dagger\Phi_2)(\Phi_2^\dagger\Phi_1)
 \end{aligned}$$

can be reduced to the potential in the mass basis ( $\lambda_{5,6,7}$  and  $\mu_{12}^2$  real)

$$U(h, H, A, H^\pm, G^0, G^\pm) = \frac{m_h^2}{2}h^2 + \frac{m_H^2}{2}H^2 + \frac{m_A^2}{2}A^2 + m_{H^\pm}^2H^+H^- + I(3) + I(4)$$

by means of explicit symbolic transformation for  $\lambda_1, \dots, \lambda_7$  in terms of mixing angles and pole masses<sup>2</sup>

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<sup>2</sup>M.D.,Semenov, EJP C28, 223 (2003); Boudjema,Semenov, Phys.Rev. D66 095007 (2002), Gunion,Haber, PR D67 075019 (2003)

$$\begin{aligned}
\lambda_1 &= \frac{1}{2v^2} \left[ \left( \frac{s_\alpha}{c_\beta} \right)^2 m_h^2 + \left( \frac{c_\alpha}{c_\beta} \right)^2 m_H^2 - \frac{s_\beta}{c_\beta^3} \mu_{12}^2 \right] + \frac{1}{4} (\lambda_7 \tan^3 \beta - 3\lambda_6 \tan \beta), \\
\lambda_2 &= \frac{1}{2v^2} \left[ \left( \frac{c_\alpha}{s_\beta} \right)^2 m_h^2 + \left( \frac{s_\alpha}{s_\beta} \right)^2 m_H^2 - \frac{c_\beta}{s_\beta^3} \mu_{12}^2 \right] + \frac{1}{4} (\lambda_6 \cot^3 \beta - 3\lambda_7 \cot \beta), \\
\lambda_3 &= \frac{1}{v^2} \left[ 2m_{H^\pm}^2 - \frac{\mu_{12}^2}{s_\beta c_\beta} + \frac{s_{2\alpha}}{s_{2\beta}} (m_H^2 - m_h^2) \right] - \frac{1}{2} (\lambda_6 \cot \beta + \lambda_7 \tan \beta), \\
\lambda_4 &= \frac{1}{v^2} \left( \frac{\mu_{12}^2}{s_\beta c_\beta} + m_A^2 - 2m_{H^\pm}^2 \right) - \frac{1}{2} (\lambda_6 \cot \beta + \lambda_7 \tan \beta), \\
\lambda_5 &= \frac{1}{v^2} \left( \frac{\mu_{12}^2}{s_\beta c_\beta} - m_A^2 \right) - \frac{1}{2} (\lambda_6 \cot \beta + \lambda_7 \tan \beta),
\end{aligned}$$

massless goldstone  $G^0$  is ensured by

$$\text{Re} \mu_{12}^2 = s_\beta c_\beta \left( m_A^2 + \frac{v^2}{2} (2\text{Re} \lambda_5 + \text{Re} \lambda_6 \cot \beta + \text{Re} \lambda_7 \tan \beta) \right)$$

Inverse transformation for pole masses in terms of  $\lambda_i$

MSSM

$M_{\text{SUSY}}$ :  
 $m_{\text{top}}$ :

$$\begin{aligned}
\lambda_{1,2}^{\text{SUSY}} &= \frac{g_1^2 + g_2^2}{8}, & \lambda_3^{\text{SUSY}} &= \frac{g_2^2 - g_1^2}{4}, & \lambda_4^{\text{SUSY}} &= -\frac{g_2^2}{2}, & \lambda_{5,6,7}^{\text{SUSY}} &= 0. \\
\lambda_i &= \lambda_i^{\text{SUSY}} - \Delta \lambda_i & \Delta \lambda_i &= \Delta \lambda_i^{\text{thr}} + \Delta \lambda_k^{\text{LL}} \quad (i = 1, \dots, 7, k = 1, \dots, 4)
\end{aligned}$$

in the mass basis

$$\begin{aligned}
 m_h^2 &= s_{\alpha+\beta}^2 m_Z^2 + c_{\alpha-\beta}^2 m_A^2 - v^2 (\Delta\lambda_1 s_\alpha^2 c_\beta^2 + \Delta\lambda_2 c_\alpha^2 s_\beta^2 \\
 &\quad - 2(\Delta\lambda_3 + \Delta\lambda_4) c_\alpha c_\beta s_\alpha s_\beta + \text{Re}\Delta\lambda_5 (s_\alpha^2 s_\beta^2 + c_\alpha^2 c_\beta^2) \\
 &\quad - 2c_{\alpha+\beta} (\text{Re}\Delta\lambda_6 s_\alpha c_\beta - \text{Re}\Delta\lambda_7 c_\alpha s_\beta)), \\
 m_H^2 &= c_{\alpha+\beta}^2 m_Z^2 + s_{\alpha-\beta}^2 m_A^2 - v^2 (\Delta\lambda_1 c_\alpha^2 c_\beta^2 + \Delta\lambda_2 s_\alpha^2 s_\beta^2 \\
 &\quad + 2(\Delta\lambda_3 + \Delta\lambda_4) c_\alpha c_\beta s_\alpha s_\beta + \text{Re}\Delta\lambda_5 (c_\alpha^2 s_\beta^2 + s_\alpha^2 c_\beta^2) \\
 &\quad + 2s_{\alpha+\beta} (\text{Re}\Delta\lambda_6 c_\alpha c_\beta + \text{Re}\Delta\lambda_7 s_\alpha s_\beta)), \\
 \tan 2\alpha &= \frac{s_{2\beta} (m_A^2 + m_Z^2) + v^2 ((\Delta\lambda_3 + \Delta\lambda_4) s_{2\beta} + 2c_\beta^2 \text{Re}\Delta\lambda_6 + 2s_\beta^2 \text{Re}\Delta\lambda_7)}{c_{2\beta} (m_A^2 - m_Z^2) + v^2 (\Delta\lambda_1 c_\beta^2 - \Delta\lambda_2 s_\beta^2 - \text{Re}\Delta\lambda_5 c_{2\beta} + (\text{Re}\Delta\lambda_6 - \text{Re}\Delta\lambda_7) s_{2\beta})},
 \end{aligned}$$

or equivalent equations in the basis of  $SU(2)$  states<sup>3</sup>

$$\begin{aligned}
 m_{H,h}^2 &= \frac{1}{2} (m_A^2 + m_Z^2 + \Delta\mathcal{M}_{11}^2 + \Delta\mathcal{M}_{22}^2 \pm \sqrt{m_A^4 + m_Z^4 - 2m_A^2 m_Z^2 c_{4\beta} + C}), \\
 \tan 2\alpha &= \frac{2\Delta\mathcal{M}_{12}^2 - (m_Z^2 + m_A^2) s_{2\beta}}{(m_Z^2 - m_A^2) c_{2\beta} + \Delta\mathcal{M}_{11}^2 - \Delta\mathcal{M}_{22}^2},
 \end{aligned}$$

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<sup>3</sup>Djouadi, Maiani, Polosa, Quevillon, Riquer, EPJ C73 2650 (2013), JHEP 1506 168 (2015)

where, using the notation of Djouadi et al.

$$\mathcal{M}_Y^2 = \begin{pmatrix} \mathcal{M}_{11}^2 & \mathcal{M}_{12}^2 \\ \mathcal{M}_{21}^2 & \mathcal{M}_{22}^2 \end{pmatrix}, \quad \mathcal{M}_{ij}^2 = \frac{\partial^2 U}{\partial Y_i \partial Y_j}, \quad Y = \eta, \chi, \omega^\pm, \quad i, j = 1, 2$$

$$\mathcal{M}_\eta^2 = \begin{pmatrix} \mathcal{M}_{11}^2 & \mathcal{M}_{12}^2 \\ \mathcal{M}_{12}^2 & \mathcal{M}_{22}^2 \end{pmatrix} + \begin{pmatrix} \Delta \mathcal{M}_{11}^2 & \Delta \mathcal{M}_{12}^2 \\ \Delta \mathcal{M}_{12}^2 & \Delta \mathcal{M}_{22}^2 \end{pmatrix},$$

$$\mathcal{M}_{11}^2 = m_A^2 s_\beta^2 + m_Z^2 c_\beta^2, \quad \mathcal{M}_{22}^2 = m_A^2 c_\beta^2 + m_Z^2 s_\beta^2, \quad \mathcal{M}_{12}^2 = -s_\beta c_\beta (m_A^2 + m_Z^2),$$

$$\Delta \mathcal{M}_{11}^2 = -v^2 (\Delta \lambda_1 c_\beta^2 + \text{Re} \Delta \lambda_5 s_\beta^2 + \text{Re} \Delta \lambda_6 s_{2\beta}),$$

$$\Delta \mathcal{M}_{22}^2 = -v^2 (\Delta \lambda_2 s_\beta^2 + \text{Re} \Delta \lambda_5 c_\beta^2 + \text{Re} \Delta \lambda_7 s_{2\beta}),$$

$$\Delta \mathcal{M}_{12}^2 = -v^2 (\Delta \lambda_{34} s_\beta c_\beta + \text{Re} \Delta \lambda_6 c_\beta^2 + \text{Re} \Delta \lambda_7 s_\beta^2),$$

$$C = 4\Delta \mathcal{M}_{12}^4 + (\Delta \mathcal{M}_{11}^2 - \Delta \mathcal{M}_{22}^2)^2 - 2(m_A^2 - m_Z^2)(\Delta \mathcal{M}_{11}^2 - \Delta \mathcal{M}_{22}^2)c_{2\beta} - 4(m_A^2 + m_Z^2)\Delta \mathcal{M}_{12}^2 s_{2\beta}$$

Simplified representation for heavy  $CP$ -even Higgs boson mass if  $\Delta \mathcal{M}_{12}^2 = 0$

$$m_H^2 = m_A^2 + m_Z^2 - m_h^2 + \Delta \mathcal{M}_{11}^2 + \Delta \mathcal{M}_{22}^2 \quad (2)$$



# Post-Higgs MSSM scenarios

## 1. hMSSM scenario, uses simplified mixing matrix<sup>4</sup>

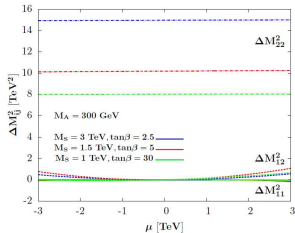
$\Delta\lambda_i$ : 1-loop ( $\epsilon$ -approximation); 1,2-loop (leading logarithms)

$$\Delta\mathcal{M}_{11} \sim 0, \quad \Delta\mathcal{M}_{12} \sim 0, \quad \Delta\mathcal{M}_{22} \neq 0$$

$$\Delta\mathcal{M}_{22}^2 = \frac{m_h^2(m_A^2 + m_Z^2 - m_h^2) - m_A^2 m_Z^2 c_{2\beta}^2}{m_Z^2 c_\beta^2 + m_A^2 s_\beta^2 - m_h^2},$$

$$m_H^2 = \frac{(m_A^2 + m_Z^2 - m_h^2)(m_Z^2 c_\beta^2 + m_A^2 s_\beta^2) - m_A^2 m_Z^2 c_{2\beta}^2}{m_Z^2 c_\beta^2 + m_A^2 s_\beta^2 - m_h^2},$$

$$\alpha = -\arctan\left(\frac{(m_Z^2 + m_A^2)s_\beta c_\beta}{m_Z^2 c_\beta^2 + m_A^2 s_\beta^2 - m_h^2}\right)$$



$$m_h = 123 - 129 \text{ GeV}$$

**Free parameters:**  $m_A, \tan\beta$

$\epsilon$ -approximation does not respect  $\lambda_i(\alpha, \beta, m_h, m_H, m_{H^\pm})$  transformation to the mass basis.

<sup>4</sup>Djouadi, Maiani, Polosa, Quevillon, Riquer, EPJ C73 2650 (2013), JHEP 1506 168 (2015);  
Maiani, Polosa, Riquer, PL B274 274 (2013)

2. Low-tb-high scenario<sup>5</sup> (FeynHiggs)  $0.5 \leq \tan \beta \leq 10$ ,  $150 \Gamma \ni B$   
 $\leq m_A \leq 500 \Gamma \ni B$

- 1) all fermionic superpartner masses  $\sim M_{\text{SUSY}}$ ;
- 2)  $M_{\text{SUSY}}$  variation range from several TeV for large  $m_A$  ( $\tan \beta$ ) up to 100 TeV for moderate  $m_A$  ( $\tan \beta$ ) with imposed constraints

$$\begin{aligned} \tan \beta \leq 2 & : X_t/M_{\text{SUSY}} = 2, & X_t = A_t - \mu/\tan \beta, \\ 2 < \tan \beta \leq 8.6 & : X_t/M_{\text{SUSY}} = 0.0375 \tan^2 \beta - 0.7 \tan \beta + 3.25, \\ 8.6 < \tan \beta & : X_t/M_{\text{SUSY}} = 0; \end{aligned}$$

- 3)  $A_t = 2 T \ni B$ ,  $\mu = 1.5 \text{ TeV}$ , gaugino mass  $M_2 = 2 \text{ TeV}$ .

3. EFT approach, Lee,Wagner, PR D92, 075032 (2015); Carena, Haber, Low, Shah, Wagner PR D91 035003 (2015). Uses SM $\rightarrow$ THDM matching at  $m_A$  scale in the Higgs basis or effective THDM potential in a generic basis.

We use the approach which in the following is denominated as ' $\Delta\lambda_{F,D}^{\text{wfr}}$  scenario'<sup>6</sup> Has been used for the case of explicit CP violation (Workshop on CP Studies and Non-Standard Higgs Physics, CERN Report 2006-009).

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<sup>5</sup>S. Heinemeyer, LHC-HXSWG-3, E. Bagnashi *et al.*, LHCHXSWG-INT-2015-004; J.R. Espinosa and R. J. Zhang, JHEP, 0003, 26 (2000).

<sup>6</sup>Akhmetzyanova,Dolgoplov, M.D., PR D71, 075008 (2005)

## $\Delta\lambda_{F,D}^{\text{wfr}}$ scenario

### Set of corrections:

- 1-loop resummed threshold, wave-function renormalization
- non-leading  $D$ -terms
- 2-loop electroweak and QCD<sup>7</sup>
- Yukawa

For instance,

$$\begin{aligned}\lambda_1 = & \frac{g_2^2 + g_1^2}{8} + \frac{3}{32\pi^2} \left[ h_b^4 \frac{|A_b|^2}{M_{\text{SUSY}}^2} \left( 2 - \frac{|A_b|^2}{6M_{\text{SUSY}}^2} \right) - h_t^4 \frac{|\mu|^4}{6M_{\text{SUSY}}^4} + \right. \\ & \left. + 2h_b^4 l + \frac{g_2^2 + g_1^2}{4M_{\text{SUSY}}^2} (h_t^2 |\mu|^2 - h_b^2 |A_b|^2) \right] + \Delta\lambda_1^{\text{wfr}} + \\ & + \frac{1}{768\pi^2} (11g_1^4 + 9g_2^4 - 36(g_1^2 + g_2^2)h_b^2) l - \Delta\lambda_1[2 - \text{loop}],\end{aligned}$$

where  $l = \log(M_{\text{SUSY}}^2/\sigma^2)$  and  $\Delta\lambda_1^{\text{wfr}}$ ,  $\Delta\lambda_1[2 - \text{loop}]$  are

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<sup>7</sup>Haber,Hempfling,Hoang, ZP C75 539 (1997); Carena,Espinosa,Quiros,Wagner PL B355 209 (1995); Heinemeyer,Hollik,Weiglein, EPJC C9 343 (1999); Pilaftsis,Wagner, NP B553 3 (1999)

wfr terms

$$\Delta \lambda_1^{\text{wfr}} = \frac{1}{2}(g_1^2 + g_2^2)A'_{11}, \quad \Delta \lambda_2^{\text{wfr}} = \frac{1}{2}(g_1^2 + g_2^2)A'_{22},$$

$$\Delta \lambda_3^{\text{wfr}} = -\frac{1}{4}(g_1^2 - g_2^2)(A'_{11} + A'_{22}), \quad \Delta \lambda_4^{\text{wfr}} = -\frac{1}{2}g_2^2(A'_{11} + A'_{22}), \quad \Delta \lambda_5^{\text{field}} = 0,$$

$$\Delta \lambda_6^{\text{wfr}} = \frac{1}{8}(g_1^2 + g_2^2)(A'_{12} - A'_{21}^*) = 0, \quad \Delta \lambda_7^{\text{wfr}} = \frac{1}{8}(g_1^2 + g_2^2)(A'_{21} - A'_{12}^*) = 0,$$

where  $A'$

$$A'_{ij} = -\frac{3}{96\pi^2 M_{\text{SUSY}}^2} \left( h_t^2 \begin{bmatrix} |\mu|^2 & -\mu^* A_t^* \\ -\mu A_t & |A_t|^2 \end{bmatrix} + h_b^2 \begin{bmatrix} |A_b|^2 & -\mu^* A_b^* \\ -\mu A_b & |\mu|^2 \end{bmatrix} \right) \times \\ \times \left( 1 - \frac{1}{2}l \right).$$

two-loop terms

$$\Delta \lambda_1[2 - \text{loop}] = -\frac{3}{16\pi^2} h_b^4 \frac{1}{16\pi^2} \left( \frac{3}{2} h_b^2 + \frac{1}{2} h_t^2 - 8g_S^2 \right) (X_b l + l^2) + \\ + \frac{3}{192\pi^2} h_t^4 \frac{1}{16\pi^2} \frac{|\mu|^4}{M_{\text{SUSY}}^4} (9h_t^2 - 5h_b^2 - 16g_S^2) l$$

## Benchmark parameter sets

4.  $m_h^{\text{alt}} (m_h^{\text{mod+}})^8 \quad A/M_{\text{SUSY}} = 2.45(1.5)$

## 5. Small $\mu$ scenario

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Input parameter set in the following evaluations is in most cases identical to Bagnaschi et al, 'Benchmark scenarios', LHCHSWG-INT-2015-004 unless otherwise specified.

## Simplified mixing matrix (hMSSM)

MSSM parameter sets

$(i; j)$	$j$		$M_{SUSY}$ [TeV]	
$i, \tan \beta$	1	1.5	3	3.5
1	2	6	5	10
	3.5	3.1	8.3	8
2.5	2	4	5.5	10
	6.5	6.5	14	8.5
5	2.2	3	5	5
	(7; 10)	(-5; 5)	(-5; 5)	(-5; 5)
30	1.4	1.7	0	0.5
	(-2; 2)	(-3; 3)	(-9; 9)	(-11; 11)

Таблица : Parameter sets

$(i; j) \equiv (\tan \beta, M_{SUSY}, A, \mu)_{ij}$ , where  $i, j = 1, \dots, 4$ ,  $m_h = 123 - 128$  GeV,  $m_A = 300$  GeV, in [TeV]. The sets (2;3),(3;2),(4;1) correspond to Djouadi et al, 2013.

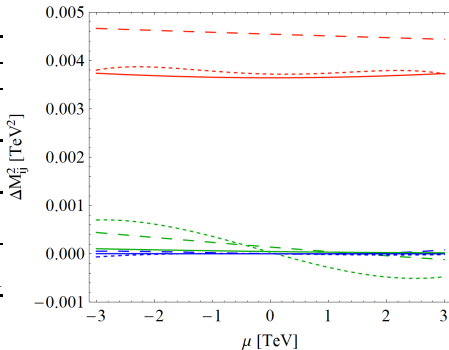


Рис. :  $\Delta \mathcal{M}_{11}^2$  - green,  $\Delta \mathcal{M}_{12}^2$  - blue,  $\Delta \mathcal{M}_{22}^2$  - red, (3;3) - long-dashed line, (4;2) - dashed line, (4;4) - solid line.

For  $\tan \beta > 5$  and  $M_{SUSY} > 1$  TeV mixing is weakly dependent on  $\mu$  at some fixed  $A$  respecting  $m_h = 125$  GeV, so  $\Delta \mathcal{M}_{11,12}^2 = 0$  is a satisfactory approximation. For the full 5-dim parameter space  $m_A, \tan \beta, \mu, A_{t,b} = A, M_S$  such approximation is not always valid. Best agreement is reached at  $M_{SUSY} \geq 3.5$  TeV and  $\tan \beta \sim 30$ .

Mixing matrix elements for  $\tan\beta > 5$  and  $M_{SUSY} > 1$  TeV,  $\Delta\lambda_{F,D}^{wfr}$  scenario

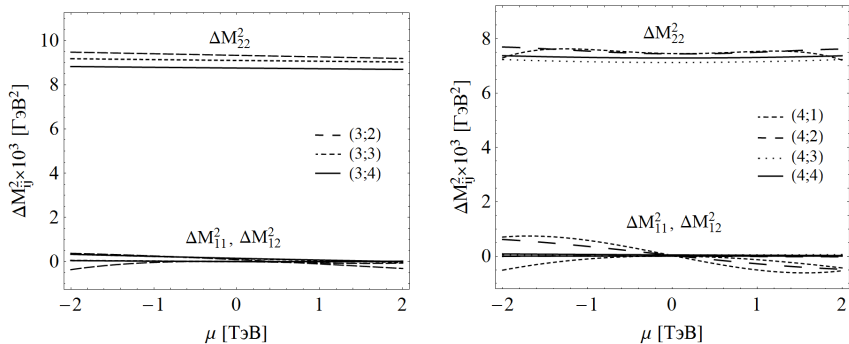


Рис. :  $(i,j)=(\text{column},\text{line number})$  denotes the parameter set as indicated in the Table.  $\mu$  in TeV,  $\Delta M_{ij}$  in GeV.

## 2. Comparison of hMSSM (dashed) and $\Delta\lambda_{F,D}^{\text{vfr}}$ (solid) scenarios

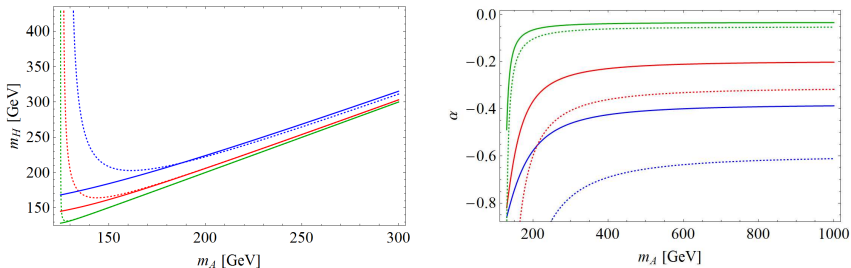


Рис. : (2;4) - blue, (3;4) - red, (4;4) - green.

Max departure of  $\alpha$  value is 0.047 (37%) at large  $\tan\beta = 30$  and 0.312 (50%) at small  $\tan\beta = 2.5$ . For heavy CP-even scalar  $H$  departure is 0.004 GeV (0.1%) at  $\tan\beta = 30$  and 4.009 GeV (1.3%) at  $\tan\beta = 2.5$ .



3. Comparison of hMSSM with  $\Delta\lambda_{F,D}^{\text{wfr}}$  without additional constraints,  $M_{SUSY} = 500$  GeV.

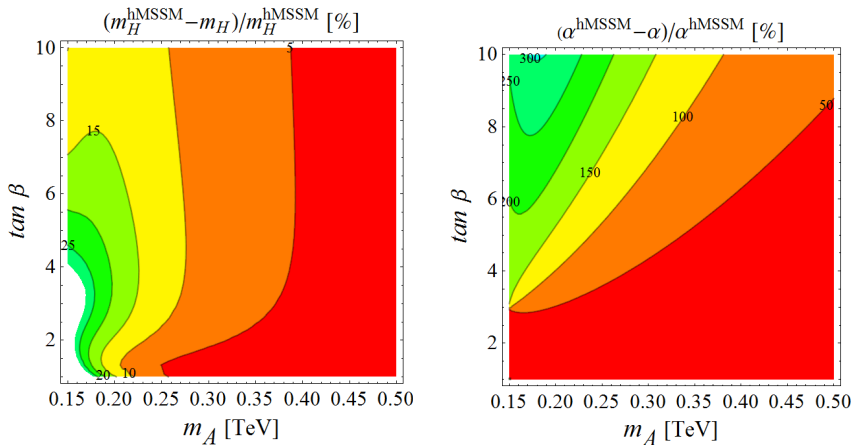


Рис. : Relative differences of  $m_H$  and  $\alpha$ .  $m_h = 125$  GeV,  $\mu = 1.5$  TeV,  $A = 2$  TeV

3. Comparison of hMSSM with  $\Delta\lambda_{F,D}^{\text{wfr}}$  using the constraint of 'low-tb-high' scenario  
 $M_{SUSY} = (0.0375 \tan^2 \beta - 0.7 \tan \beta + 3.25)/X_t$

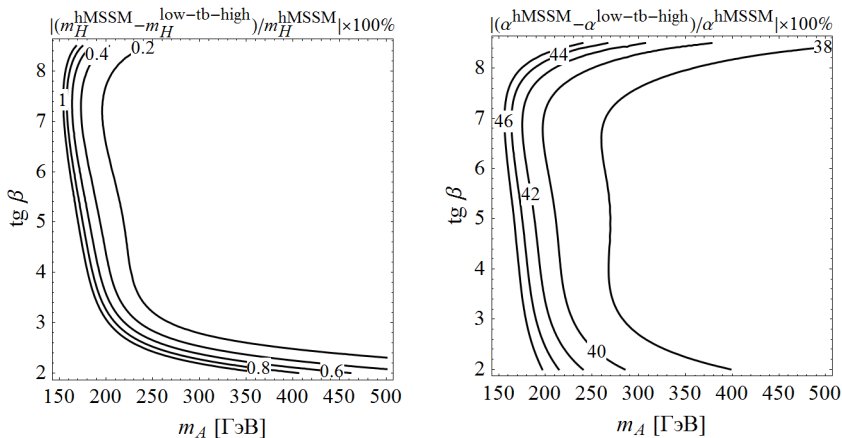
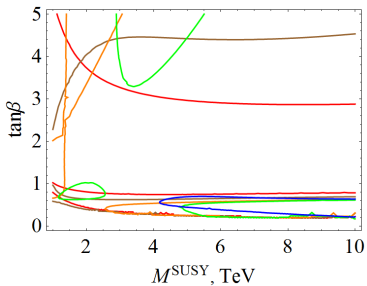
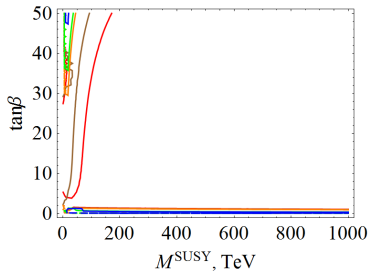
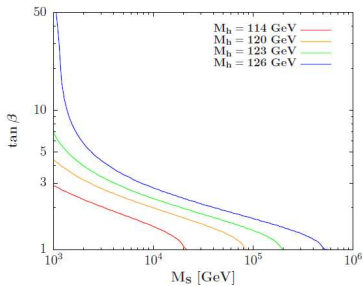


Рис. : Relative differences of  $m_H$  and  $\alpha$ .  $m_h = 125$  GeV,  $\mu = 1.5$  TeV,  $A = 2$  TeV

# Comparison of Orsay+Rome evaluation (HXSWG meeting, March 1995) based on hMSSM with $\Delta\lambda_{F,D}^{wfr}$ scenario



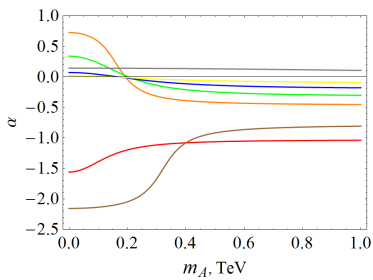
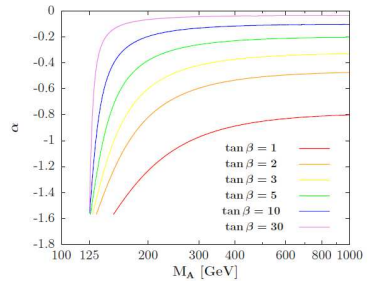
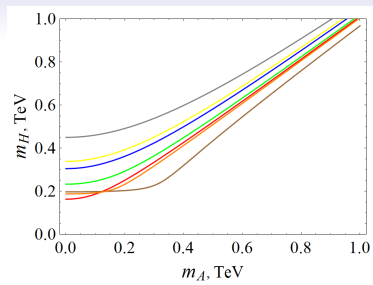
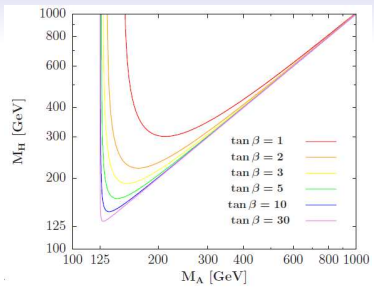
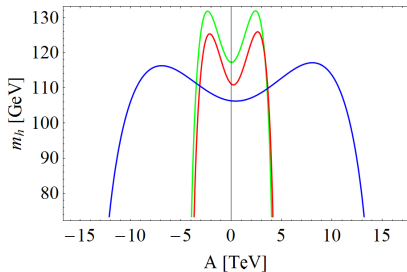


Рис. :

$m_h$  dependence on  $A = A_{t,b}$  in  $\Delta\lambda_{F,D}^{wfr}$  scenario.



**Рис. :**  $m_h$  dependence on  $A = A_{t,b}$  at  $m_A = 300$  GeV,  $\mu = 1$  TeV for the tree sets (1)  $M_{SUSY} = 3$  TeV,  $\tan\beta = 2.5$  (blue); (2)  $M_{SUSY} = 1.5$  TeV,  $\tan\beta = 5$  (red); (3)  $M_{SUSY} = 1$  TeV,  $\tan\beta = 30$  (green). With a limited set of  $\Delta\lambda_i^a$  corrections curves have the same shape, but are 5-10 GeV lower.

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31

3D surfaces of  $m_h = 125$  GeV at low and high  $\tan \beta$  in  $M^{SUSY}, \mu, A$  space for  $m_A = 0.3$  TeV and  $m_A = 1$  TeV.  $\Delta\lambda_{F,D}^{ufr}$  scenario.

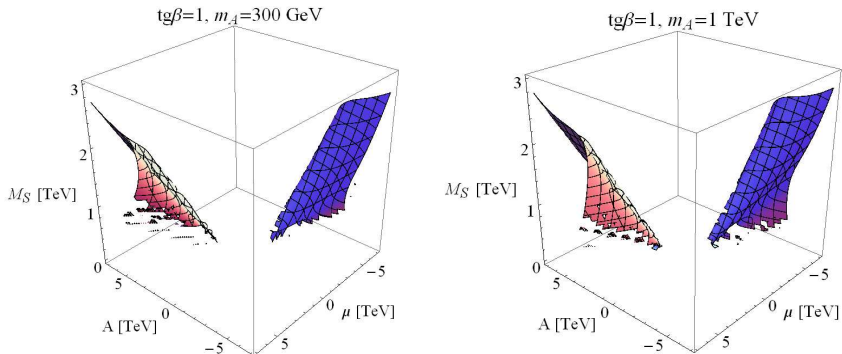


Рис. : Surface of  $m_h = 125$  GeV,  $\tan \beta = 1$ ,  $m_A = 300$  GeV (left) and 1 TeV (right)

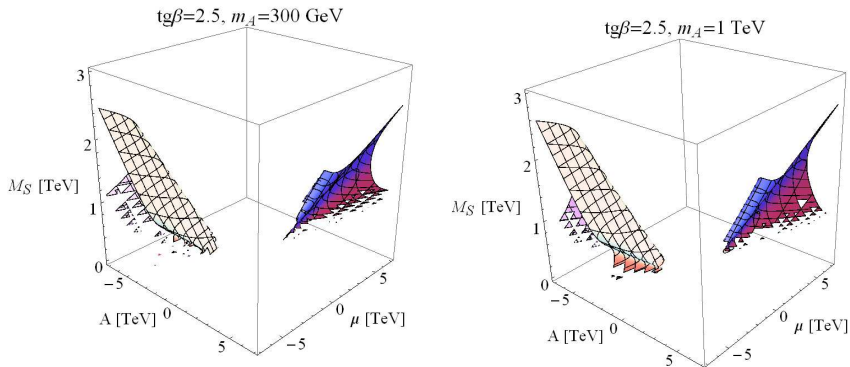


Рис. : Surface of  $m_h = 125 \text{ GeV}$ ,  $\tan\beta = 2.5$ ,  $m_A = 300 \text{ GeV}$  (left) and  $1 \text{ TeV}$  (right)

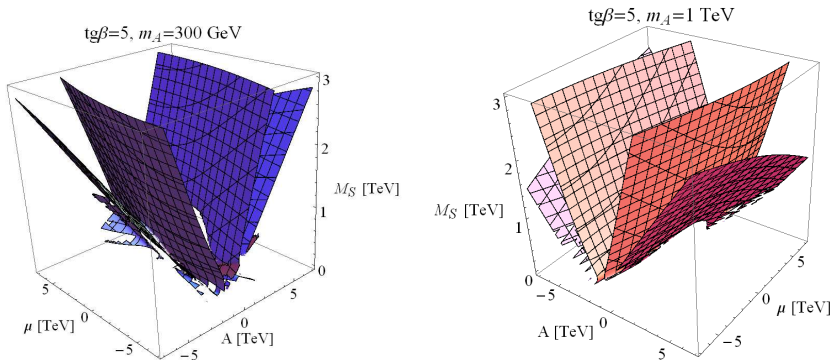


Рис. : Surface of  $m_h = 125 \text{ GeV}$ ,  $\tan\beta = 5$ ,  $m_A = 300 \text{ GeV}$  (left) and  $1 \text{ TeV}$  (right). Right 3D plot is rotated 90 degrees.



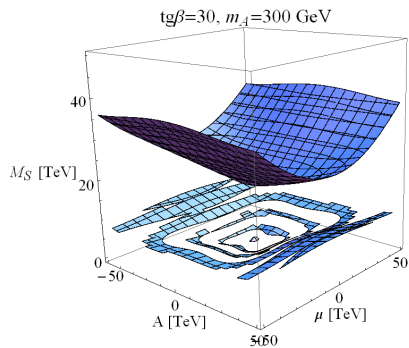
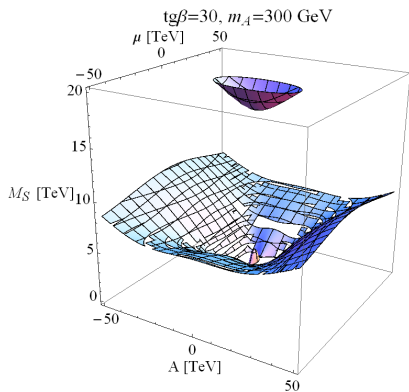
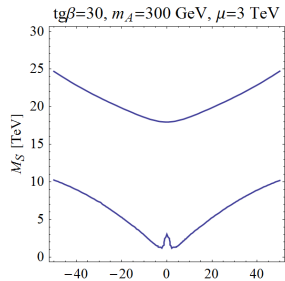
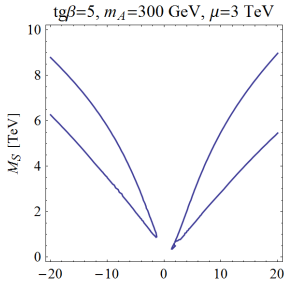
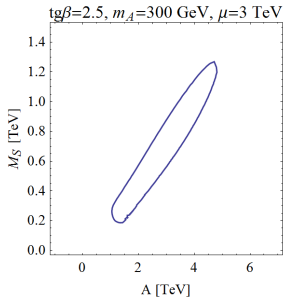
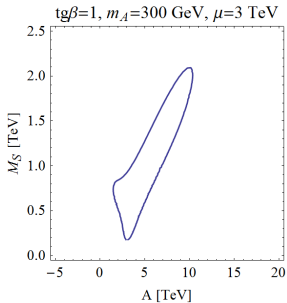
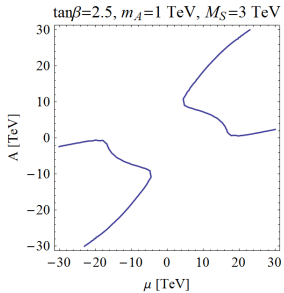
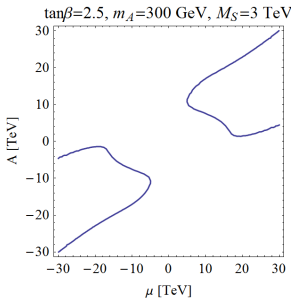
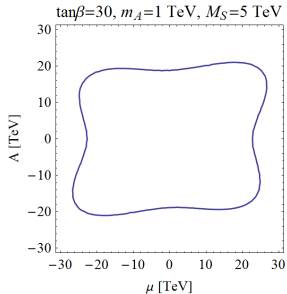
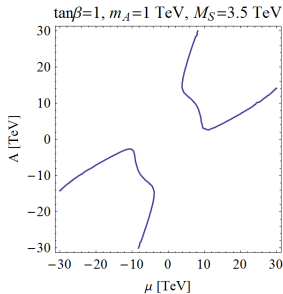


Рис. : Surface of  $m_h = 125 \text{ GeV}$ ,  $\tan\beta = 30$ ,  $m_A = 300 \text{ GeV}$  (left),  $A$ ,  $\mu$  formally extended beyond a perturbative calculation framework

Contours of  $m_h = 125$  GeV at low and high  $\tan\beta$  in  $M^{SUSY}$ ,  $A$  plane for  $m_A = 0.3$  TeV and  $m_A = 1$  TeV.  $\Delta\lambda_{F,D}^{wfr}$  scenario.



Contours of  $m_h = 125$  GeV at low and high  $\tan\beta$  in  $\mu, A$  plane for  $m_A = 0.3$  TeV and  $m_A = 1$  TeV.  $\Delta\lambda_{F,D}^{\text{wfr}}$  scenario.



Contours of  $m_h = 125$  GeV at low and high  $\tan\beta$  in  $\mu, A$  plane for  $m_A = 0.3$  TeV and  $m_A = 1$  TeV.  $\Delta\lambda_{F,D}^{\text{ufr}}$  scenario.

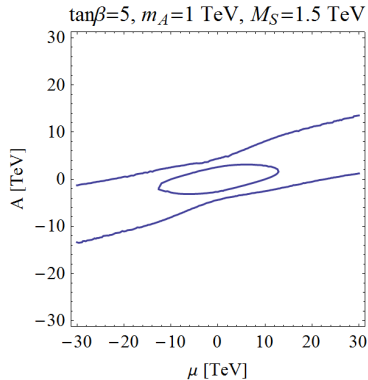
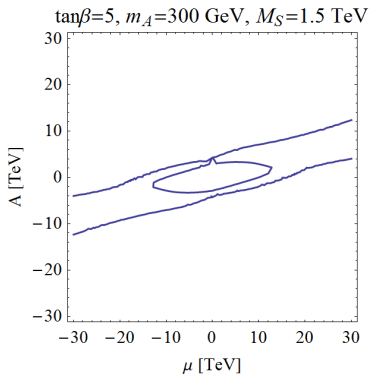


Fig. : Contours of  $m_h = 125$  GeV,  $m_A = 300$  GeV (left) and  $m_A = 1$  TeV (right)

Domains of  $m_h$  in the  $\mu, A$  plane for  $A_{t,b}=2$  TeV and  $\mu=1.5$  TeV.  $\Delta\lambda_{F,D}^{\text{wfr}}$  scenario.

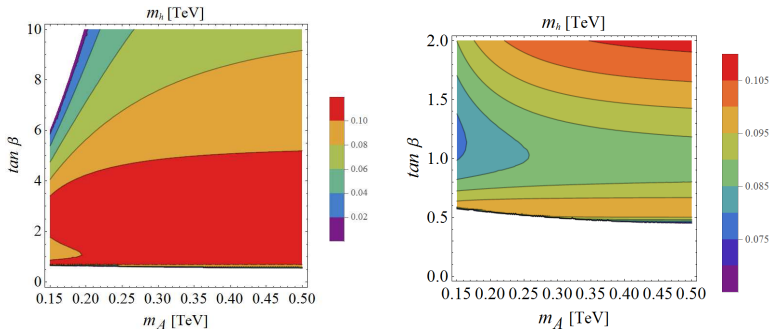


Рис. :  $M_{SUSY} = 500$  GeV (left) and 750 GeV (right).

Domains of  $m_h$  in the  $\mu, A$  plane for  $A_{t,b} = 2$  TeV and  $\mu = 1.5$  TeV.  $\Delta\lambda_{F,D}^{\text{wfr}}$  scenario.

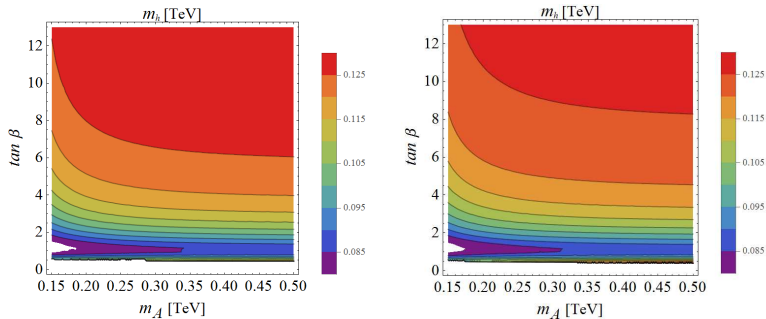


Рис. :  $M_{SUSY} = 1$  TeV (left) and 1.25 TeV (right).

#### 4. Heavy $CP$ -even H branching ratios for $m_h^{\text{alt}}$ and $m_h^{\text{mod+}}$ parameter sets

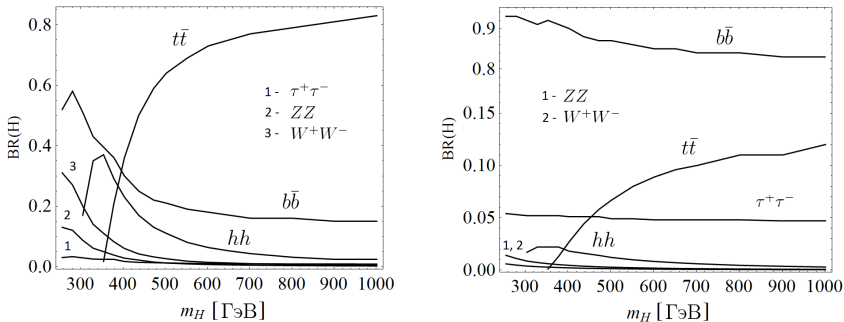


Рис. :  $m_h = 124 - 126$  GeV,  $M_{\text{SUSY}} = 1.5$  TeV and  $\mu = 200$  GeV or 1 TeV. Left panels:  $\tan \beta = 4$ ,  $A = 2.45 M_{\text{SUSY}}$  ( $m_h^{\text{alt}}$  scenario); right panels  $\tan \beta = 10$ ,  $A = 1.5 M_{\text{SUSY}}$  ( $m_h^{\text{mod+}}$  scenario). Results are stable with respect to higgs superfield parameter  $\mu$  variation.

## Summary

- Sensitivity of all results to radiative corrections is as a rule high. Reduction of multidimensional MSSM parameter space, although very attractive for qualitative interpretations, should be carefully performed if possible in some restricted regions only
- For low  $\tan\beta \leq 3$  parameter sets  $M_{SUSY}$  top value is restricted at the level of a few (3–4) TeV.
- For high  $\tan\beta \geq 30$  an ambiguity of  $M_{SUSY}$  is observed, both heavy (TeV) and extremely heavy (20–30 TeV) scales are possible. However, with this observation one should not get involved by high  $\tan\beta$  in the range  $m_{H^\pm} \leq 400$  GeV because of specific  $t\bar{t} \rightarrow H^\pm \rightarrow 6$  jets which are not observed.
- Some 'tuning' of results for comparisons could be useful. Deviations are significant. Direct comparisons of two-doublet effective potentials (e.g. evaluation of  $\lambda_1, \dots, \lambda_7$  for a given set of input parameters) are not obvious since they are defined for different bases (in particular generic  $(v_1, v_2)$  basis and Higgs basis  $(0, v)$ ), so different potential forms can give identical mass spectrum and couplings.