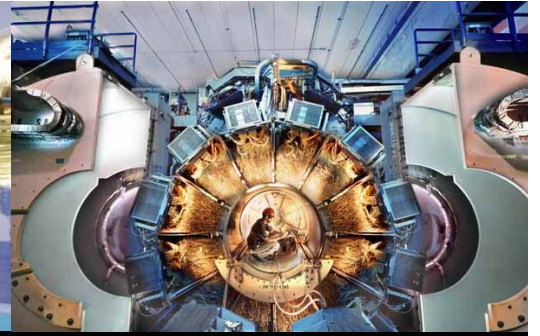


(C) Peter Ginter (2002).



# Rare Hadronic B decays

Adrian Bevan

Flavour physics in the LHC Era

10<sup>th</sup> October 2006



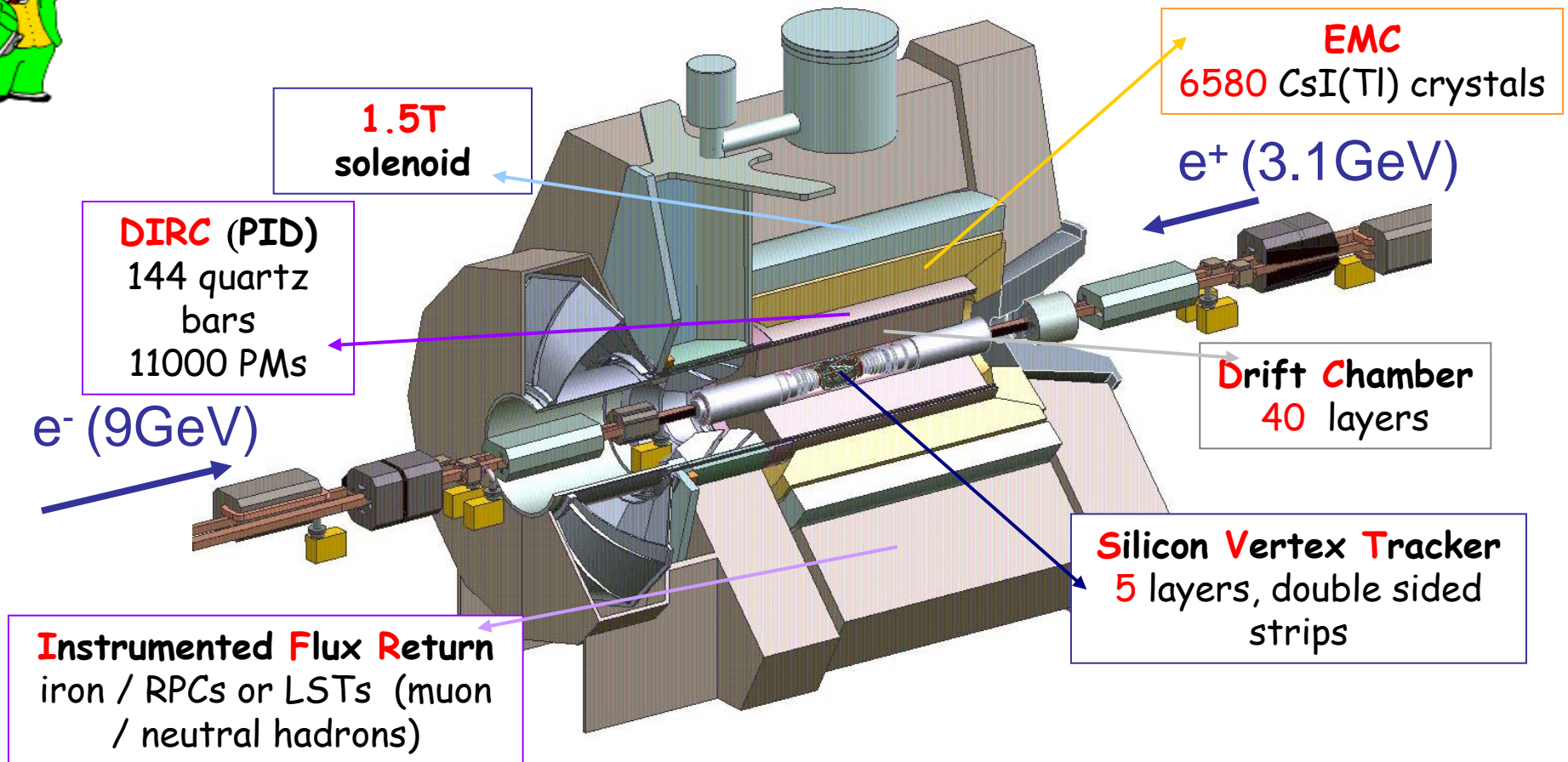
# Overview

- Motivation
- The BaBar Detector
- Isolating Signal Decays
- Results
  - Direct CPV
  - $B \rightarrow VV$  Results
    - $K^* \rho$
    - Constraining penguins in  $B \rightarrow \rho\rho$
    - $B \rightarrow \phi K^*$
    - Building a bigger picture
  - Constraining  $\Delta S$  with  $B \rightarrow PP$  decays
    - $B \rightarrow a_1 \pi$
    - $B \rightarrow \eta' V$
- Summary

# Motivation

- Rare hadronic B decays to PP, PV, VV final states provide a complicated and rich test bed for B physics theory calculations.
  - Branching Fractions.
  - Direct CP violation.
  - TDCPV (not covered – see G. Cavoto's talk)
  - Unitarity Triangle angles.
  - VV: polarisation, amplitude hierarchy, T-odd asymmetries, NP searches.
  - + much more...
- This is a small selection of results: BaBar sent O(40) papers on this subject to ICHEP '06.

# BaBar detector

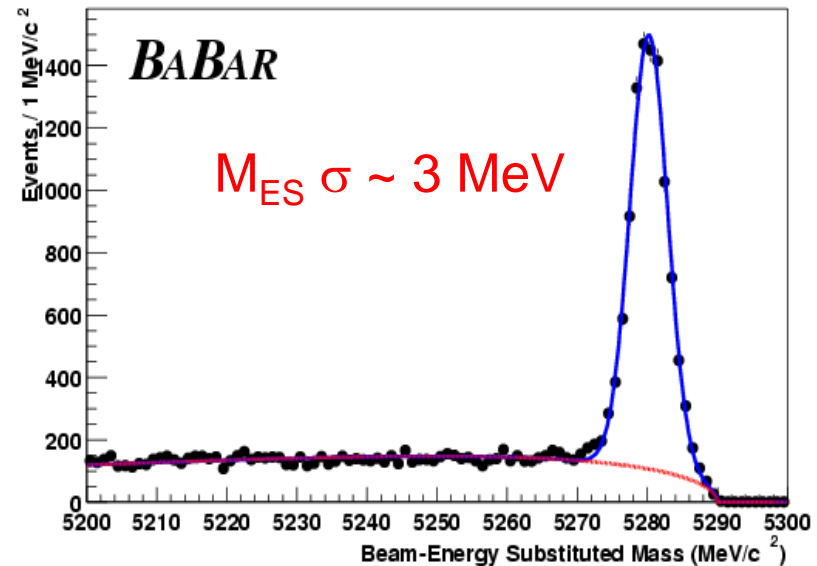
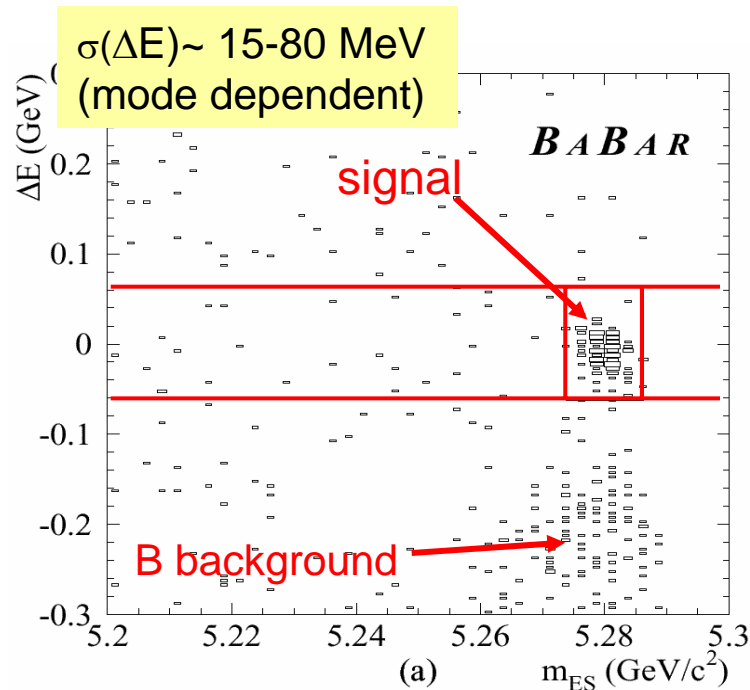


- Upgrading muon system to replace all remaining RPCs with LSTs for run 6.

# Isolating signal events

- Beam energy is known very well at an  $e^+e^-$  collider like PEP-II.
  - use an energy difference and effective mass to select events:

$$\Delta E = E_B - E_{beam}^* \quad m_{ES} = \sqrt{(E_{beam}^*)^2 - P_B^2}$$

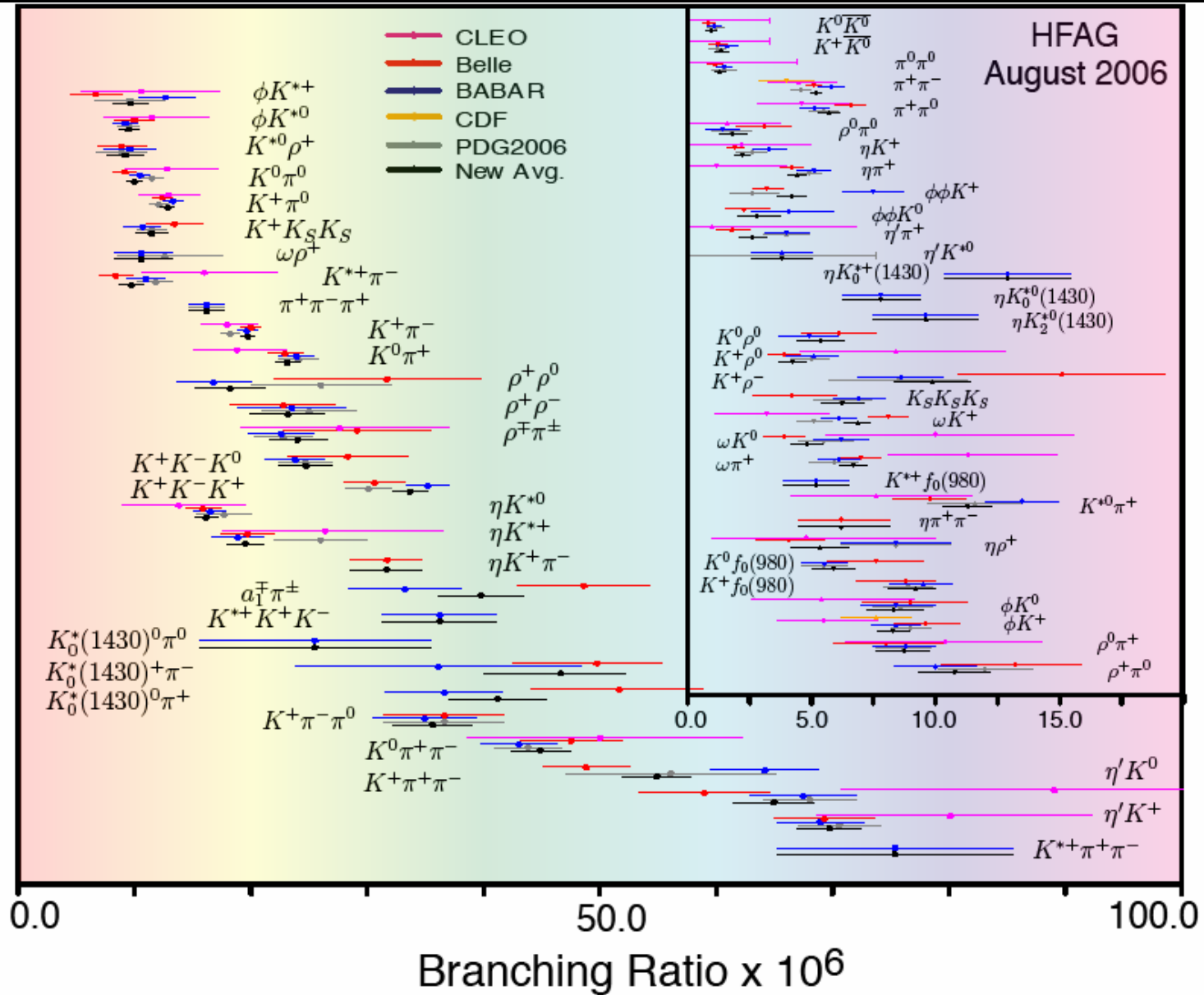


# Results



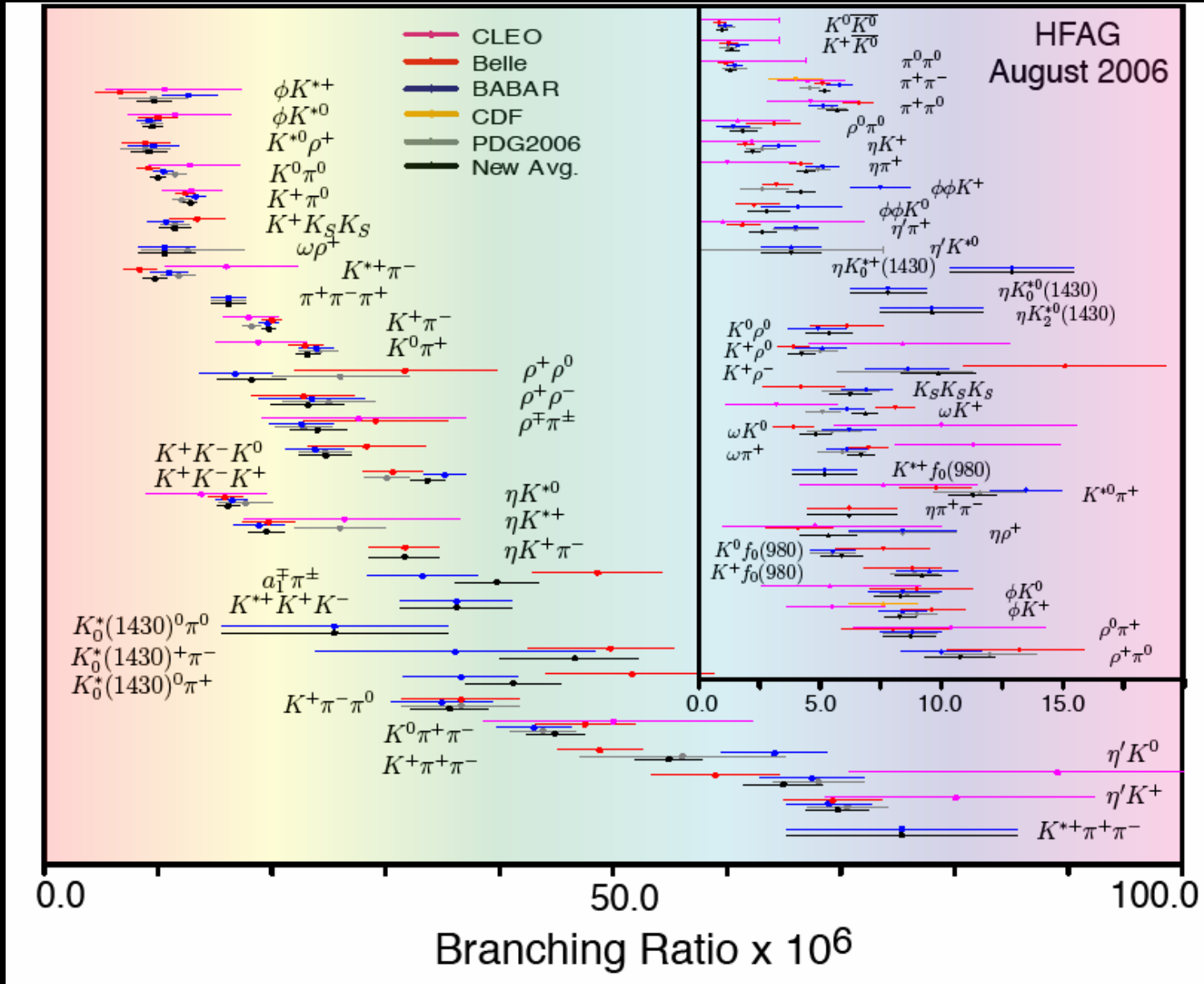
**Searching for needles in a haystack**

# The full range of measurements... is far too much to cover!



# Direct CP Violation searches

summarise only two of many results:  $K\pi$  and  $\pi^+\pi^-\pi^0$ .





# Direct CP violation

- Study difference between number of B (N) and anti-B ( $\bar{N}$ ) mesons decaying into the same final state.

$P(B \rightarrow f)$  compared to  $P(\bar{B} \rightarrow \bar{f})$

$$A_{CP} = \frac{\bar{N} - N}{\bar{N} + N}$$

- Need different weak ( $\phi$ ) and strong ( $\delta$ ) phases in the decay amplitudes of the B( $\bar{B}$ ) to the final state.

$$A_{CP} \propto - \sum_{i,j} A_i A_j (\sin[\phi_1 - \phi_2] \sin[\delta_1 - \delta_2])$$

- Expect large direct CP Violation when interfering amplitudes are of a similar magnitude.

# Direct CPV in $B \rightarrow K\pi$

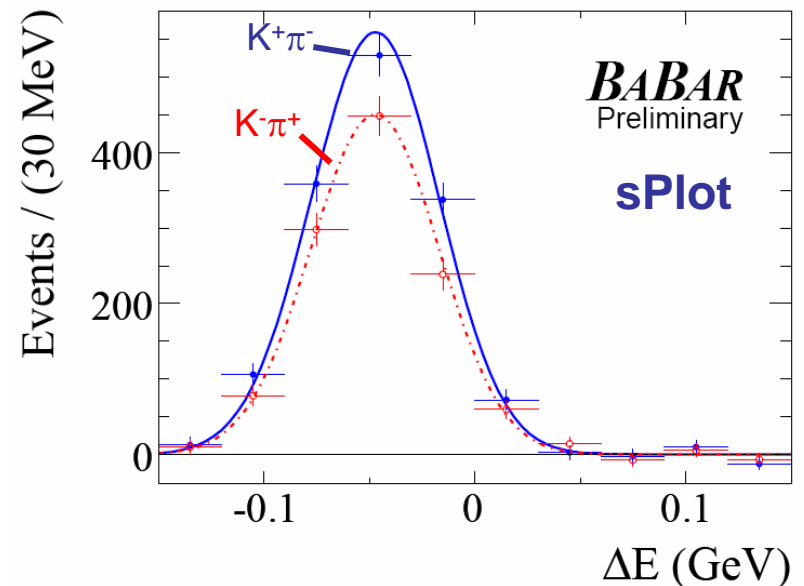
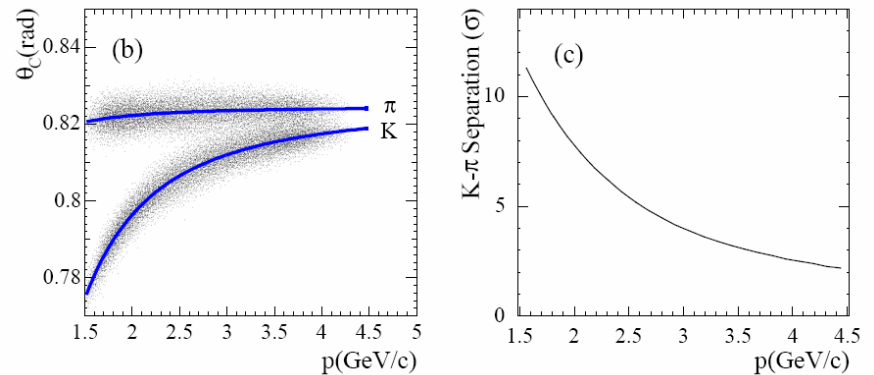
hep-ex/0607106

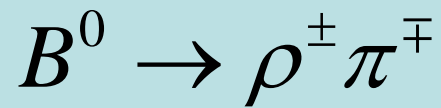
- $347 \times 10^6$  B pairs
- Charge of K in the final state tags the flavor of the B-meson.
- Use particle ID to separate K and  $\pi$  mesons.
- Calculate asymmetry:

$$\mathcal{A}_{K\pi} \equiv \frac{n_{K^-\pi^+} - n_{K^+\pi^-}}{n_{K^-\pi^+} + n_{K^+\pi^-}}$$

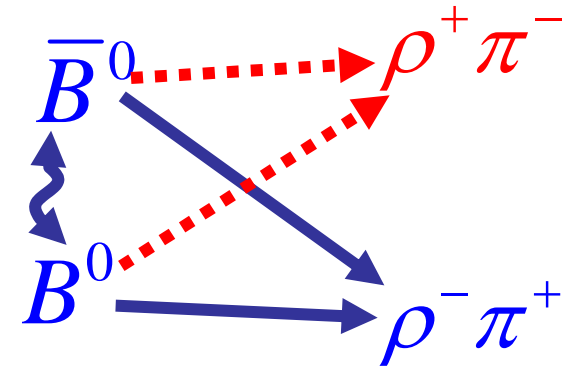
$$\mathcal{A}_{K\pi} = -0.108 \pm 0.024 \pm 0.008$$

- 2<sup>nd</sup> Manifestation of direct CPV observed (after  $\epsilon'$ ).



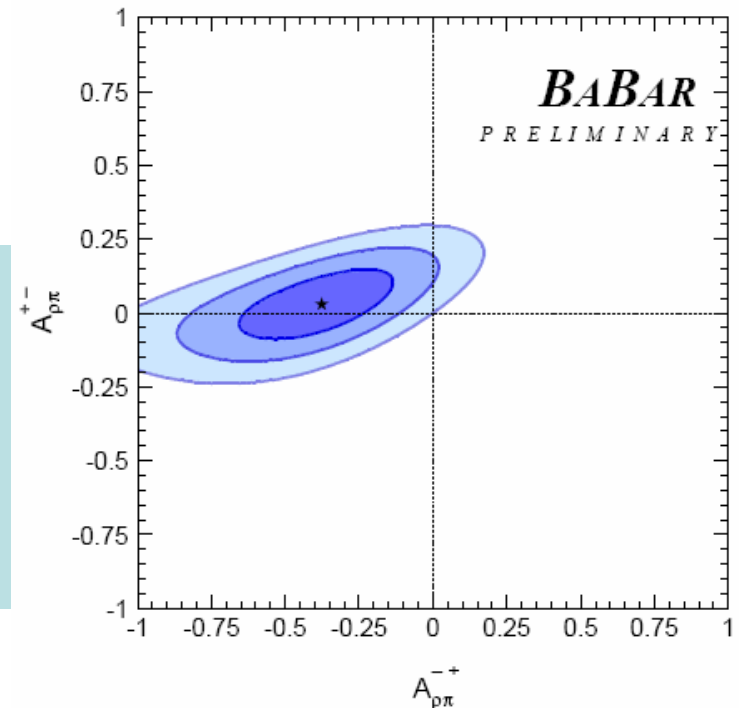


- Not a CP eigenstate.
- Can measure  $A_{CP}$  for both  $\rho^+\pi^-$  and  $\rho^-\pi^+$  final states.
- Results obtained from the TD Dalitz analysis for  $\alpha$ .
- Good channel to continue searching for direct CPV.

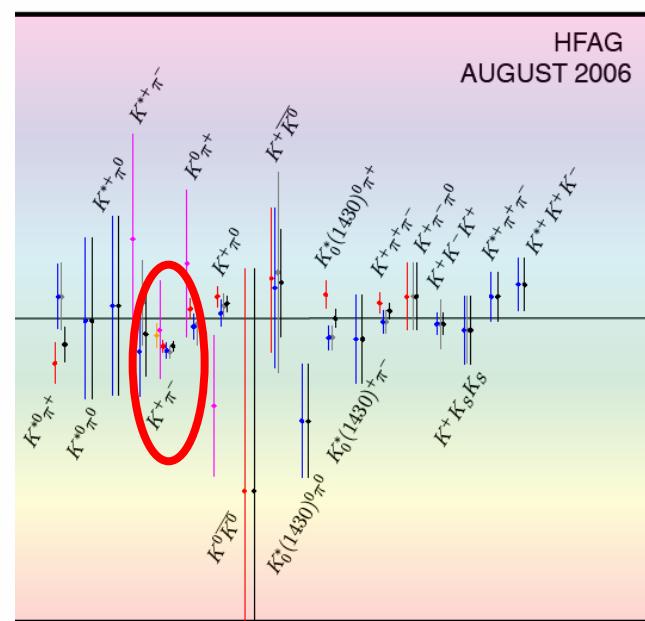
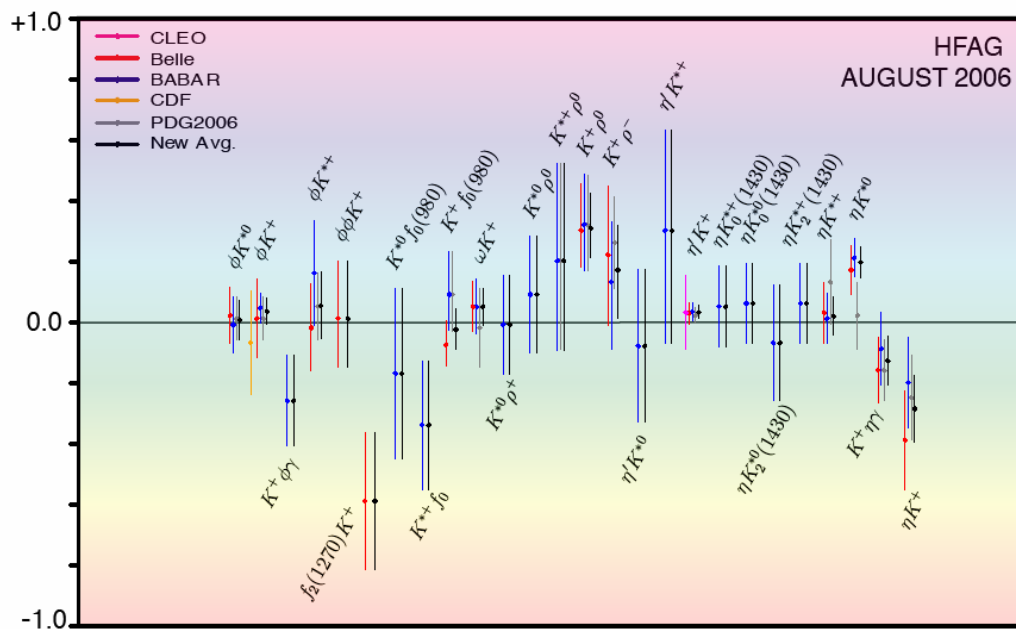


$$A_{\rho\pi}^{-+} = \frac{A_{\rho\pi} - C - A_{\rho\pi} \Delta C}{1 - C - A_{\rho\pi} \Delta C} = 0.03 \pm 0.07 \pm 0.03$$

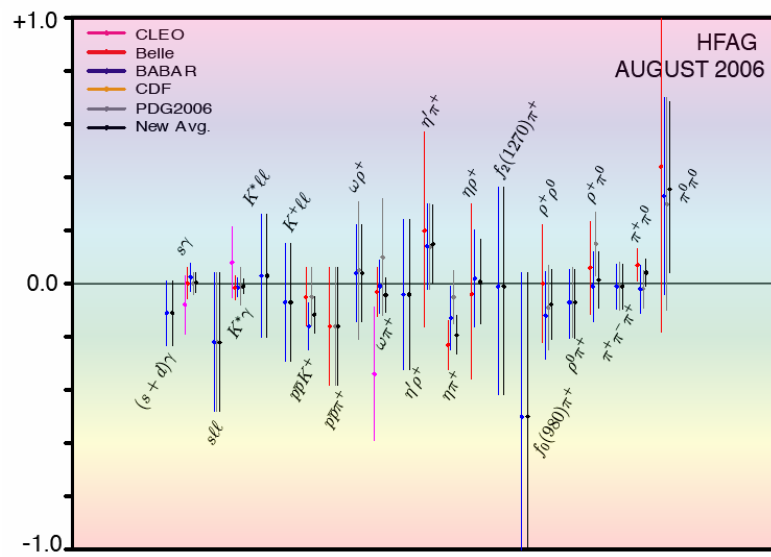
$$A_{\rho\pi}^{+-} = \frac{A_{\rho\pi} + C + A_{\rho\pi} \Delta C}{1 + C + A_{\rho\pi} \Delta C} = -0.38_{-0.16}^{+0.15} \pm 0.07$$



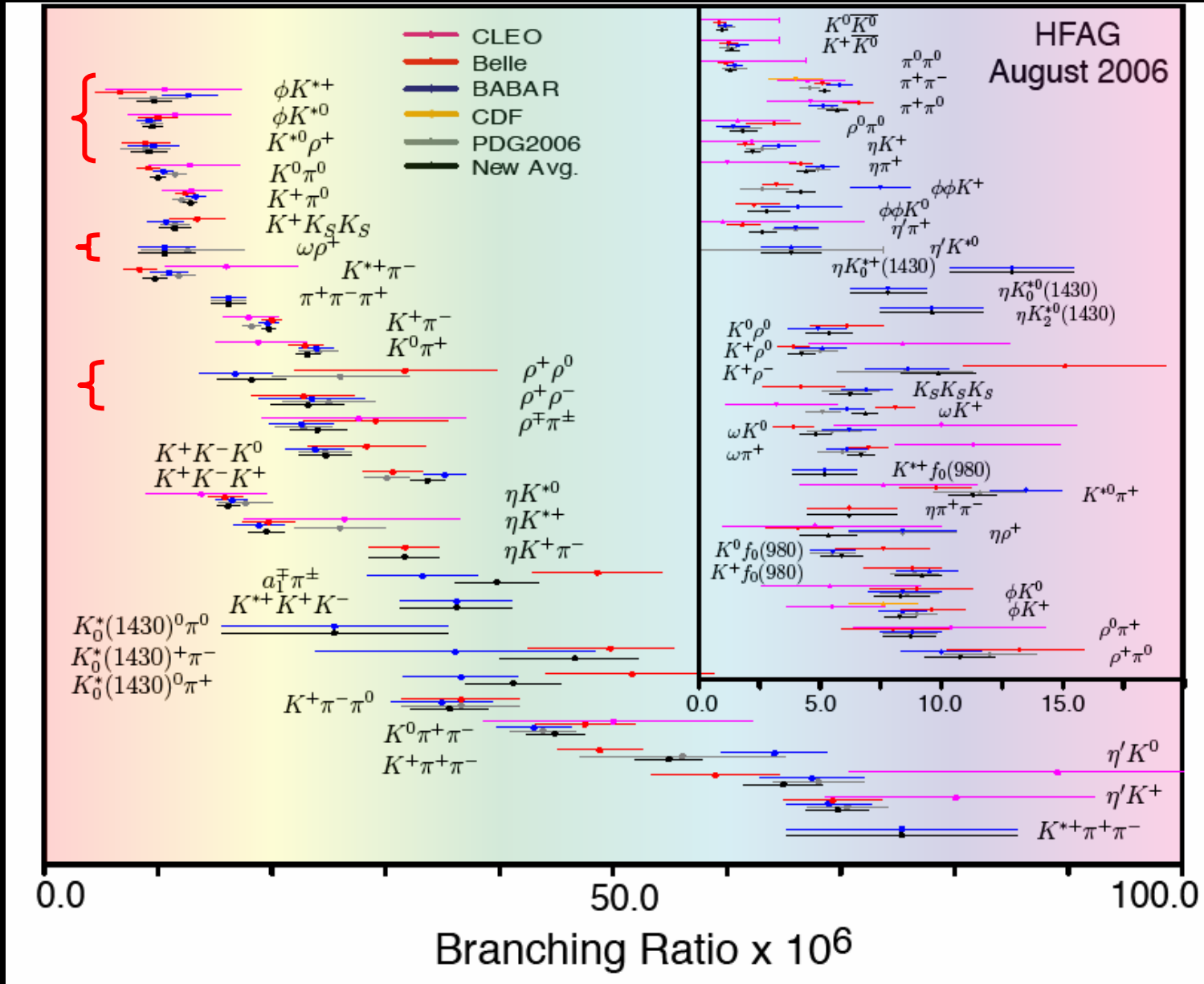
# Searches for Direct CP Violation in B decay



- The B-factories observed direct CPV in  $B \rightarrow K\pi$  decays in 2004.
- There are other modes with evidence for direct CPV
  - $B^+ \rightarrow \rho(770)^0 K^+$
  - $B^0 \rightarrow \pi^+ \pi^-$
  - $B^0 \rightarrow \pi^+ \pi^- \pi^0$
- and a massive effort to uncover more signals.

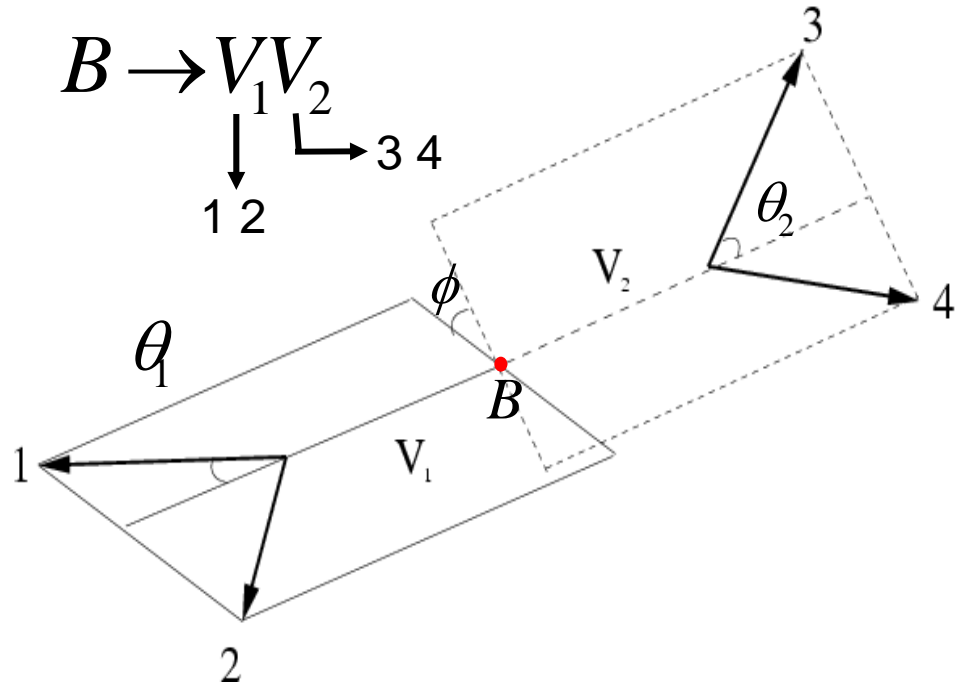


# B → VV final states.



# Angular analysis of $B \rightarrow VV$ decays

- 11 observables
  - 6 amplitudes,  $A_0, A_{+1}, A_{-1} + \text{C.C.}$
  - 5 phases
- Simplify analysis to separating transverse and longitudinal events when have low statistics.
  - Measure polarisation:  $f_L$
- Analogous to  $H \rightarrow ZZ \rightarrow l^+l^-l^+l^-$



$$\frac{d^3\Gamma}{d \cos \theta_1 d \cos \theta_2 d\Phi} \propto \left| \sum_{m=-1,0,1} A_m Y_{1,m}(\theta_1, \Phi) Y_{1,-m}(\theta_2, \Phi) \right|^2$$

$$\propto \left\{ \begin{array}{l} \frac{1}{4} \sin^2 \theta_1 \sin^2 \theta_2 (|A_{+1}|^2 + |A_{-1}|^2) + \cos^2 \theta_1 \cos^2 \theta_2 |A_0|^2 \\ + \frac{1}{2} \sin^2 \theta_1 \sin^2 \theta_2 [\cos 2\Phi \Re(A_{+1}A_{-1}^*) - \sin 2\Phi \Im(A_{+1}A_{-1}^*)] \\ + \frac{1}{4} \sin 2\theta_1 \sin 2\theta_2 [\cos \Phi \Re(A_{+1}A_0^* + A_{-1}A_0^*) - \sin \Phi \Im(A_{+1}A_0^* - A_{-1}A_0^*)] \end{array} \right\}$$

$$f_L = \frac{|A_0|^2}{\sum_{m=-1,0,1} |A_m|^2}$$

# Angular analysis of $B \rightarrow VV$ decays

- For low statistics / when  $A_0$  dominates:

$$\frac{d^2\Gamma}{\Gamma d\cos\theta_1 d\cos\theta_2} = \frac{9}{4} \left( \underbrace{f_L \cos^2\theta_1 \cos^2\theta_2}_{\text{Longitudinal}} + \frac{1}{4} (1 - f_L) \underbrace{\sin^2\theta_1 \sin^2\theta_2}_{\text{Transverse}} \right)$$

- Longitudinal and transverse polarisations generally have different efficiencies.
- Naive factorisation prediction is

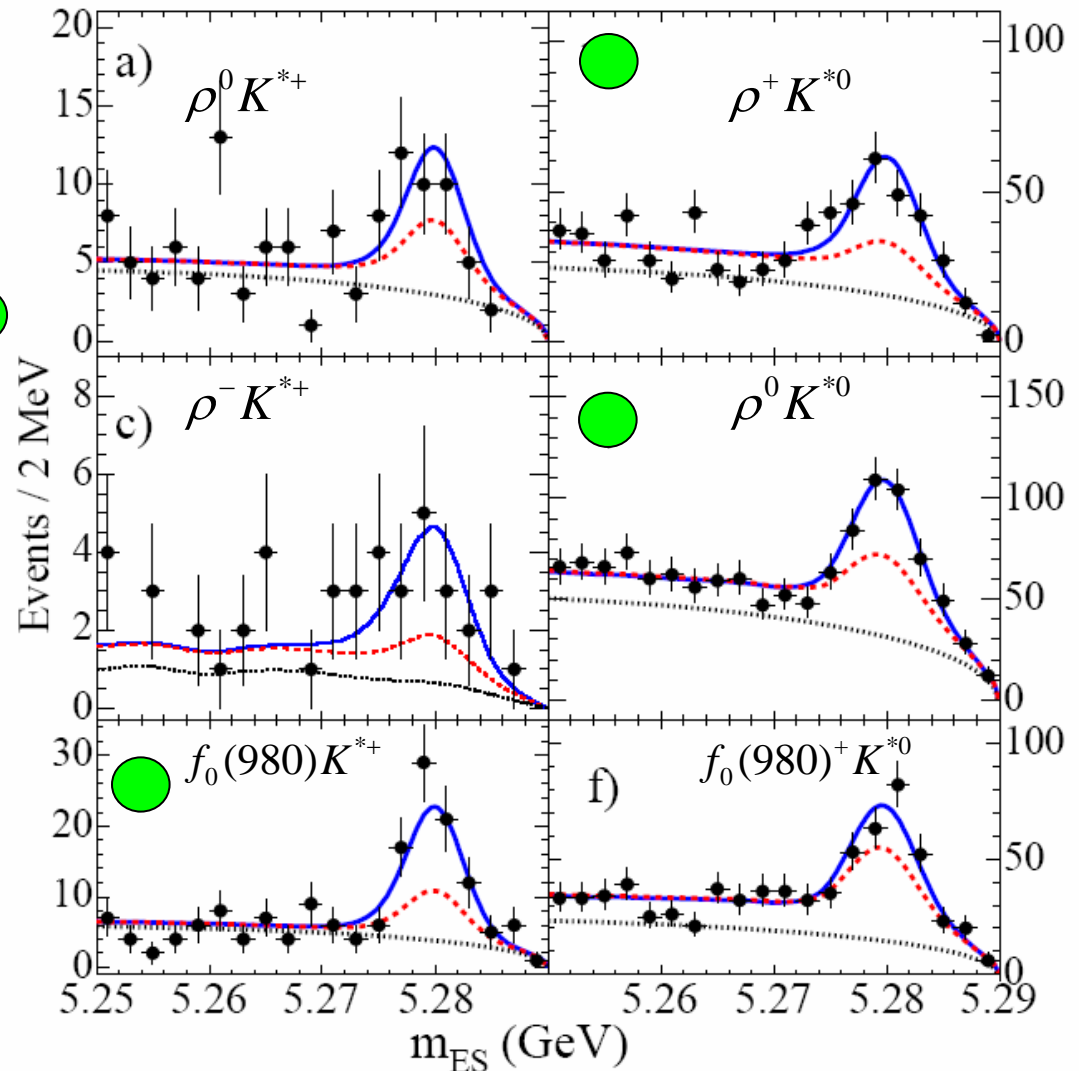
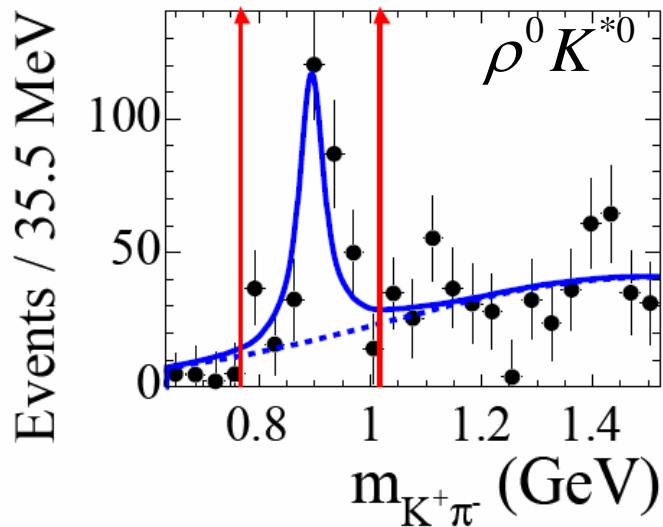
$$f_L \approx 1 - \left( \frac{m_v}{m_b} \right)^2 \approx O(1)$$

- Can also search T-odd (CP violating) asymmetries using triple products and new physics signatures. Easy to do if no single amplitude dominates the final state.
- Hierarchy of amplitudes predicted in SM.

# $B \rightarrow K^* \rho$

hep-ex/0607057

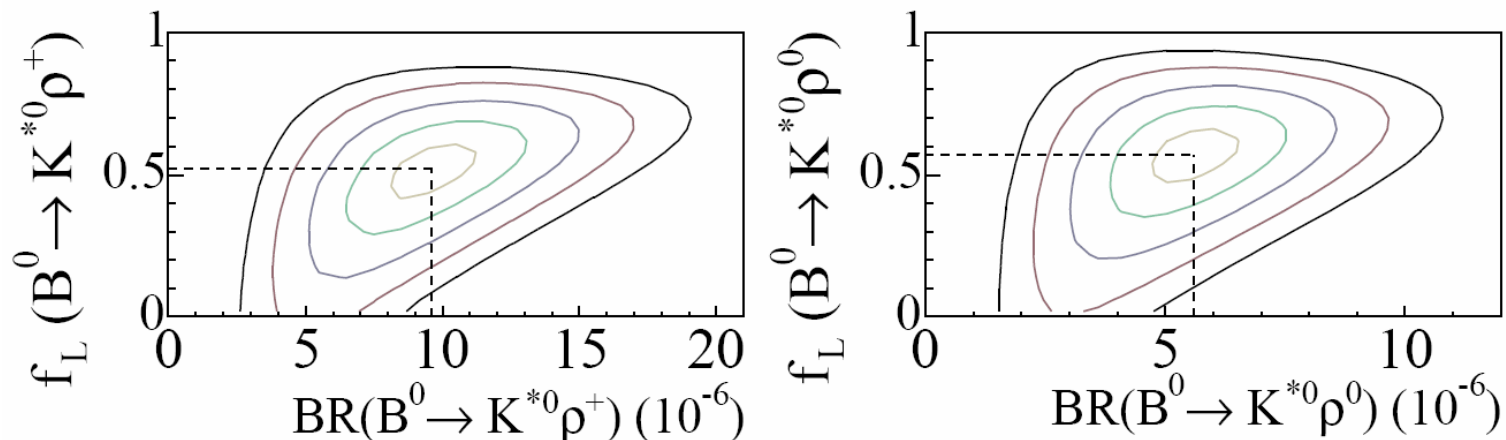
- $232 \times 10^6$  B Pairs
- $BF \sim \text{few } 10^{-6}$ .
- 2 VV modes and  $f_0 K^{*+}$  have been observed. ●
- Understanding non-resonant  $K\pi$  background is critical for these analyses.





# B → K\* ρ

hep-ex/0607057



Mode	$n_{sig}$	$S(\sigma)$	$\mathcal{B}(10^{-6})$	$f_L$	$\mathcal{A}_{CP}$
$\rho^0 K^{*+}$		2.5	$3.6^{+1.7}_{-1.6} \pm 0.8$ (6.1)	$[0.9 \pm 0.2]$	–
$\rightarrow \rho^0 K^{*+}_{K^+\pi^0}$	$19^{+16}_{-15}$	1.3	$3.2^{+2.7}_{-2.4} \pm 0.9$	$[0.8^{+0.3}_{-0.5}]$	–
$\rightarrow \rho^0 K^{*+}_{K^0_S\pi^+}$	$32^{+19}_{-17}$	2.1	$3.8^{+2.2}_{-2.1} \pm 0.9$	$[1.0 \pm 0.3]$	–
$\rho^+ K^{*0}$	$194 \pm 29$	7.1	$9.6 \pm 1.7 \pm 1.5$	$0.52 \pm 0.10 \pm 0.04$	$-0.01 \pm 0.16 \pm 0.02$
$\rho^- K^{*+}_{K^+\pi^0}$	$60^{+25}_{-22}$	1.6	$5.4^{+3.8}_{-3.4} \pm 1.6$ (12.0)	$[-0.18^{+0.52}_{-1.74}]$	–
$\rho^0 K^{*0}$	$185 \pm 30$	5.3	$5.6 \pm 0.9 \pm 1.3$	$0.57 \pm 0.09 \pm 0.08$	$0.09 \pm 0.19 \pm 0.02$
$f_0(980) K^{*+}$		5.0	$5.2 \pm 1.2 \pm 0.5$	–	$-0.34 \pm 0.21 \pm 0.03$
$\rightarrow f_0(980) K^{*+}_{K^+\pi^0}$	$40^{+13}_{-12}$	3.8	$6.2^{+2.1}_{-1.9} \pm 0.7$	–	$-0.50 \pm 0.29 \pm 0.03$
$\rightarrow f_0(980) K^{*+}_{K^0_S\pi^+}$	$37^{+14}_{-12}$	3.2	$4.2^{+1.5}_{-1.4} \pm 0.5$	–	$-0.13 \pm 0.30 \pm 0.01$
$f_0(980) K^{*0}$	$83 \pm 19$	3.5	$2.6 \pm 0.6 \pm 0.9$ (4.3)	–	$-0.17 \pm 0.28 \pm 0.02$

# Constraining Penguins in $B^0 \rightarrow \rho^+ \rho^-$

Beneke et al., Phys.Lett. B638 (2006) 68-73

- Relate the penguin contribution in  $\rho^+ \rho^-$  to  $K^{*0} \rho^+$  using SU(3) symmetry:

$$C_{\text{long}} = \frac{2r \sin \delta \sin(\beta + \alpha)}{1 - 2r \cos \delta \cos(\beta + \alpha) + r^2},$$

$$S_{\text{long}} = \frac{\sin 2\alpha + 2r \cos \delta \sin(\beta - \alpha) - r^2 \sin 2\beta}{1 - 2r \cos \delta \cos(\beta + \alpha) + r^2},$$

$$R = \frac{\left( \frac{|V_{cd}| f_\rho}{|V_{cs}| f_{K^*}} \right)^2 \cdot \frac{\Gamma_{L,CP\text{-averaged}}(B^\pm \rightarrow K^{*0} \rho^+)}{\Gamma_{L,CP\text{-averaged}}(B^0 \rightarrow \rho^+ \rho^-)}}{F r^2}$$

$$= \frac{1}{1 - 2r \cos \delta \cos(\beta + \alpha) + r^2}.$$

$r = |P/T|$

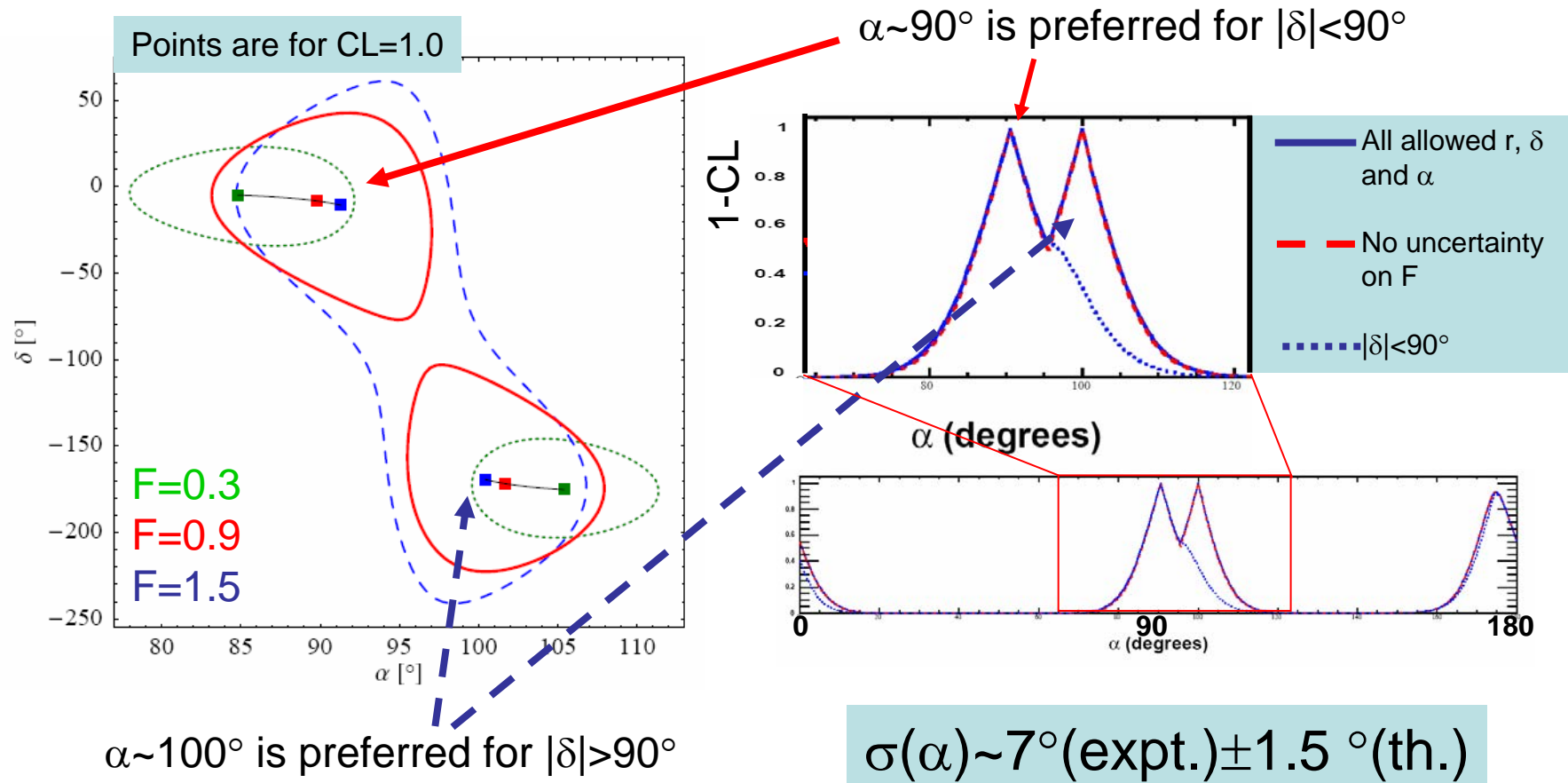
$\delta$  = strong phase difference between P and T

F = Correction for SU(3) breaking effects not included in the decay constants

- The error on  $\alpha$  and  $\delta$  don't depend strongly on F and  $\sigma(F)$ : Variance always suppressed by a factor of  $r^2$ .
- Produces usual ambiguities in 0-180°.
- Also get 2 fold ambiguities in  $\delta$ .
- Remove one ambiguity in  $\delta$  by assuming  $|\delta| < 90^\circ$ .

# Constraints using the Beneke et al. model

- For the standard model solution of  $\alpha$ :



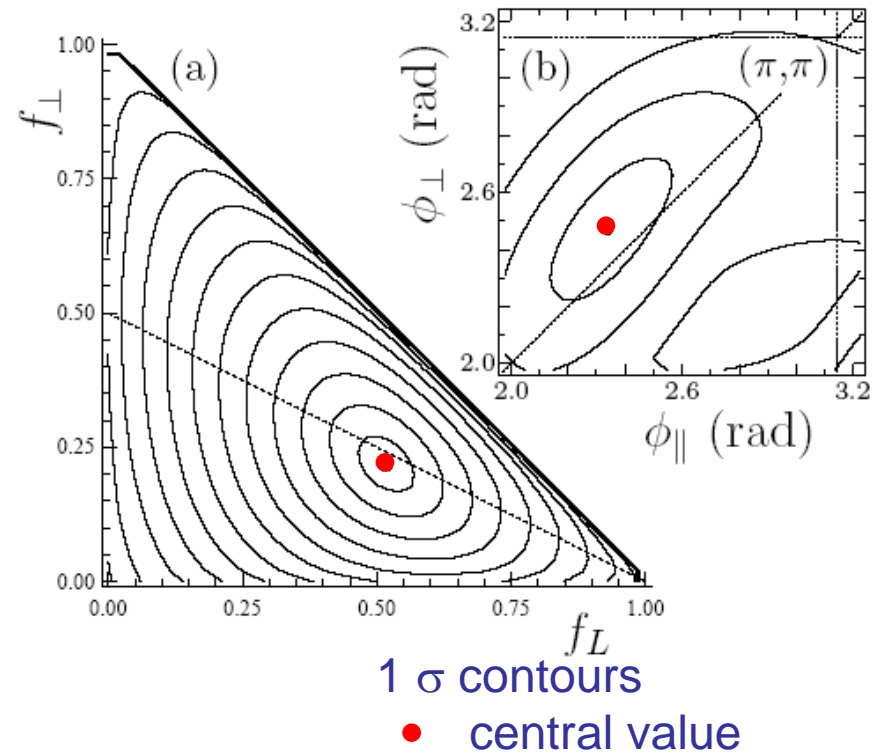
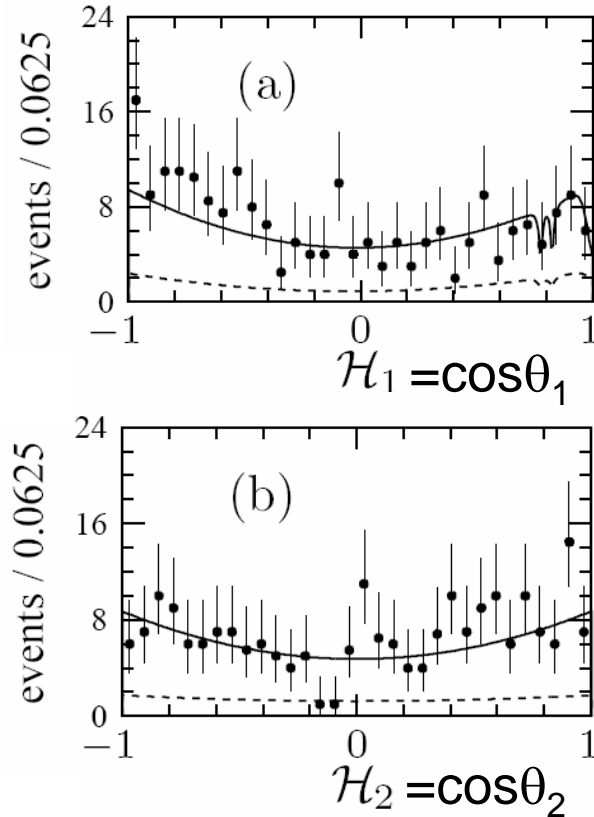
- c.f. Isospin constraint on  $\alpha \sim 18^\circ$ .
- Error predominantly from measurement of S and C ( $\alpha_{\text{eff}}$ ).

# $B \rightarrow \phi K^*$

PRL 93 (2004) 231804

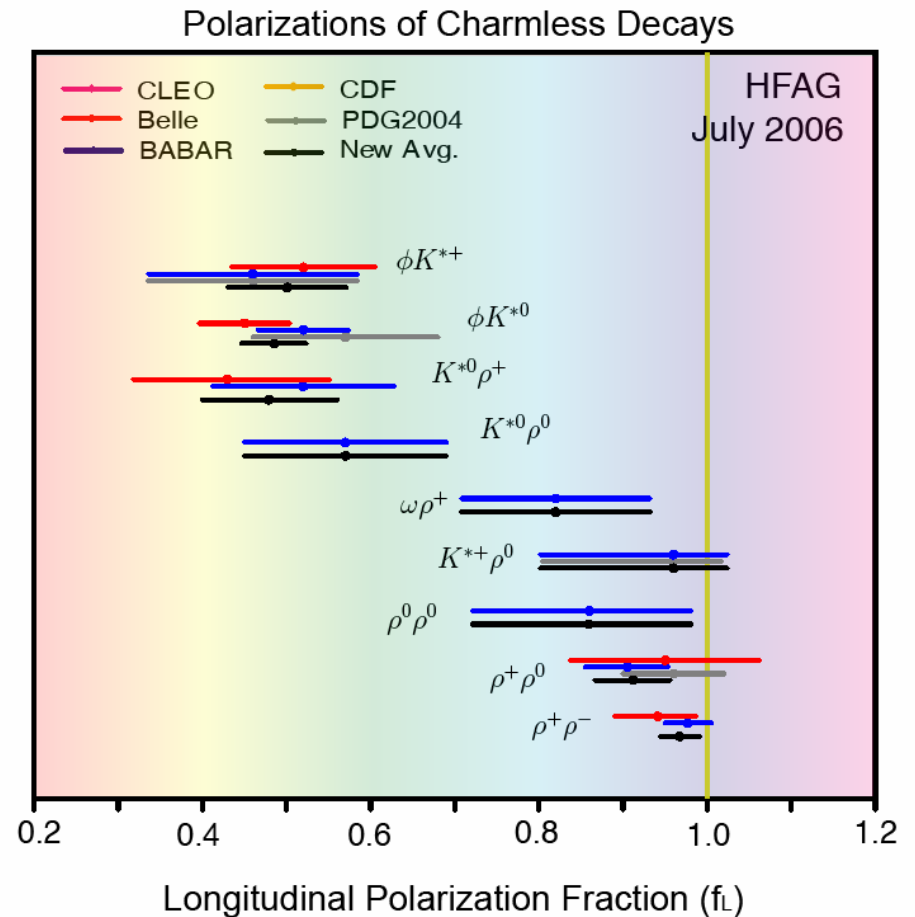
- $227 \times 10^6$  B pairs
- Transversity analysis
- Obtain a small  $f_L$ .

Fit parameter	Fit result	Correlation
$n_{\text{sig}}$ (events)	$201 \pm 20 \pm 6$	
$f_L$	$0.52 \pm 0.05 \pm 0.02$	} -46%
$f_{\perp}$	$0.22 \pm 0.05 \pm 0.02$	



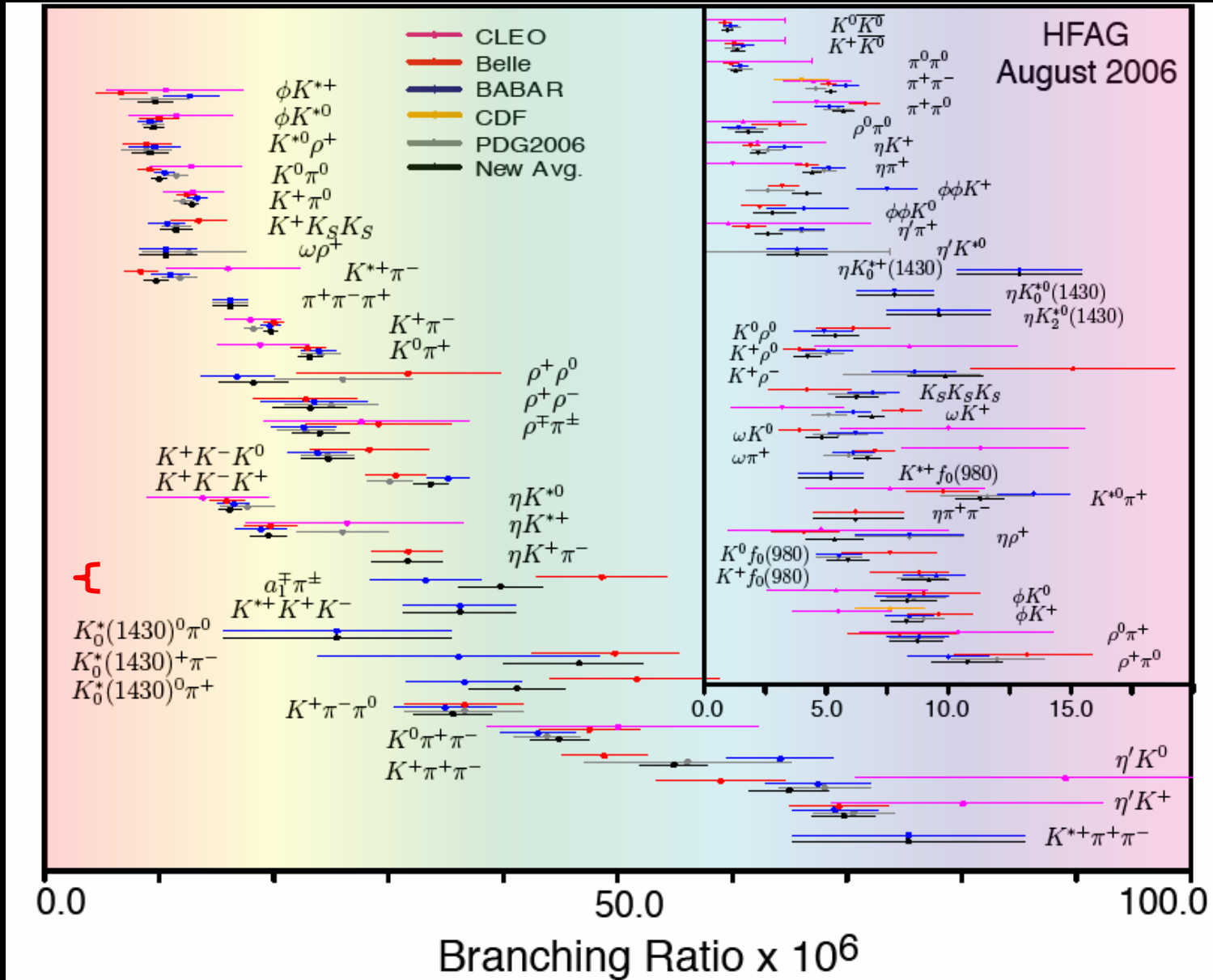
# Overview of $f_L$ in $B \rightarrow VV$ decays

- Some decays follow naive expectations with large  $f_L$ .
- Some don't!
  - $\phi K^*$
  - some of the  $\rho K^*$  modes
- Important to finish building the picture:
  - What is  $f_L$  for other  $B \rightarrow VV$  modes?
  - What is  $f_L$  for AV modes?
    - Searched for  $a_1\rho$ .
  - What additional contributions can explain this pattern?
- Can use  $K^{*0}\rho^+$  obtain model dependent constraints on  $\alpha$ .
- Also have performed searches for other  $VV$  final states (e.g.  $\omega\omega$  etc).



$K^*\rho$  hep-ex/0607057  
 $\phi K^*$  PRL **93** (2004) 231804  
 $a_1\rho$  PRD **74** (2006) 031104  
 $\rho\rho$  hep-ex/0607098, 0607097, 0607092  
 $\omega X$  PRD **74** (2006) 051102

# B → PP, PV, PA.



# B → PP

PRD 73 071102 (2006)  
PRD 74 051106 (2006)

- Can use  $B \rightarrow \eta\eta, \eta'\eta', \eta'\eta, \eta'\pi^0, \eta\pi^0$  to bound  $\Delta S = \sin 2\beta - \sin 2\beta_{\text{eff}}$  in the golden s-penguin modes  $B \rightarrow \eta'K^0$  and  $\phi K^0$ .
- All final states have neutrals to reconstruct.

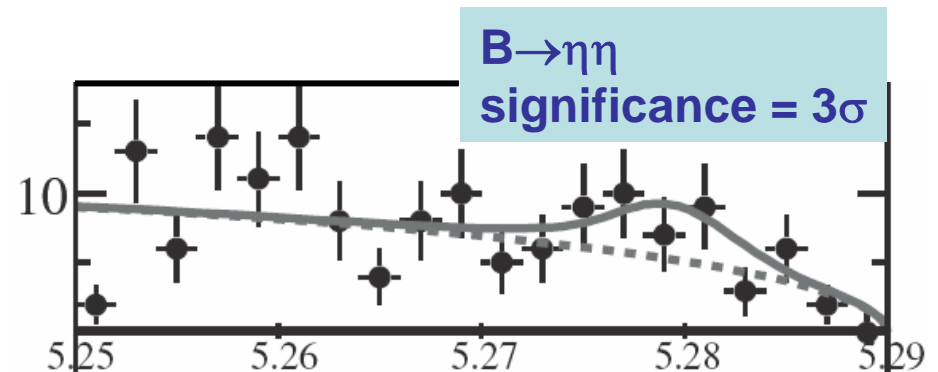
$$B(\eta\eta) = (1.1^{+0.5}_{-0.4} \pm 0.1) \times 10^{-6}$$

$$B(\eta'\eta') < 2.4 \times 10^{-6}$$

$$B(\eta'\eta) < 1.7 \times 10^{-6}$$

$$B(\eta\pi^0) < 1.3 \times 10^{-6}$$

$$B(\eta'\pi^0) < 2.1 \times 10^{-6}$$



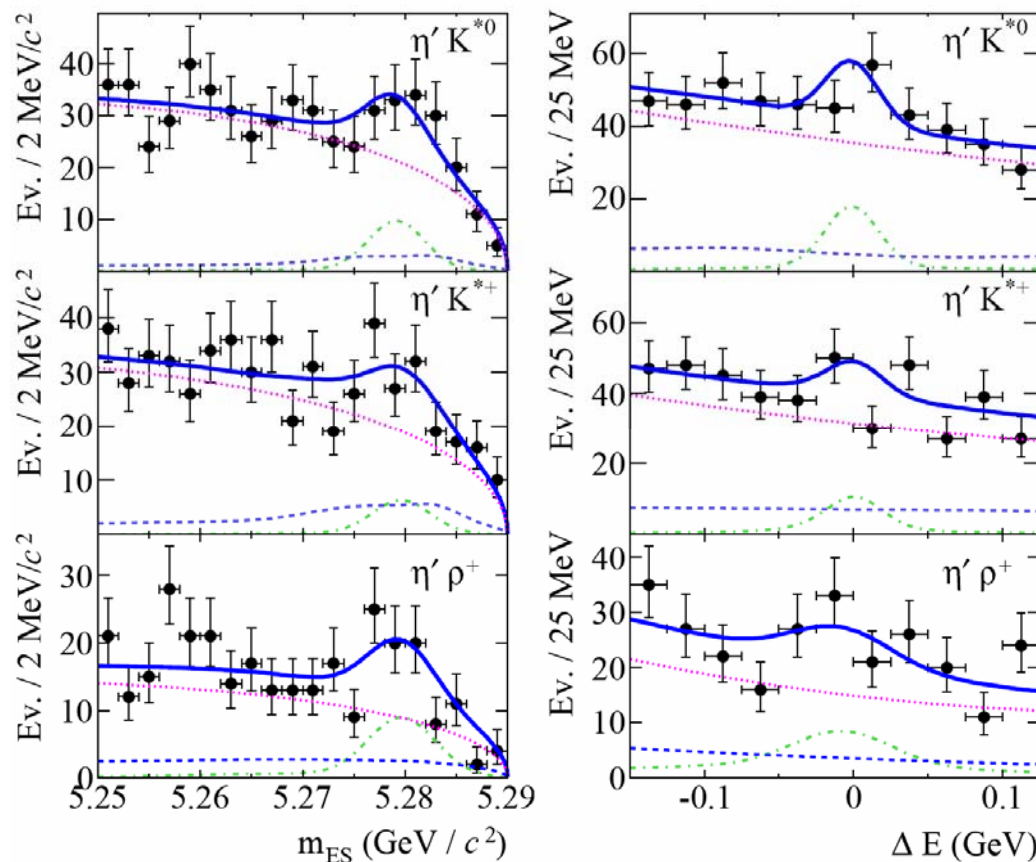
$$|\Delta S(\eta'K^0)| < 0.15$$

$$|\Delta S(\phi K^0)| < 0.38$$

# B → η'V

hep-ex/0607109

- Useful in understanding the decay  $\eta'K^0$ .
- both  $\eta'K^*$  and  $\eta'\rho$  provide additional tests of theoretical calculations.



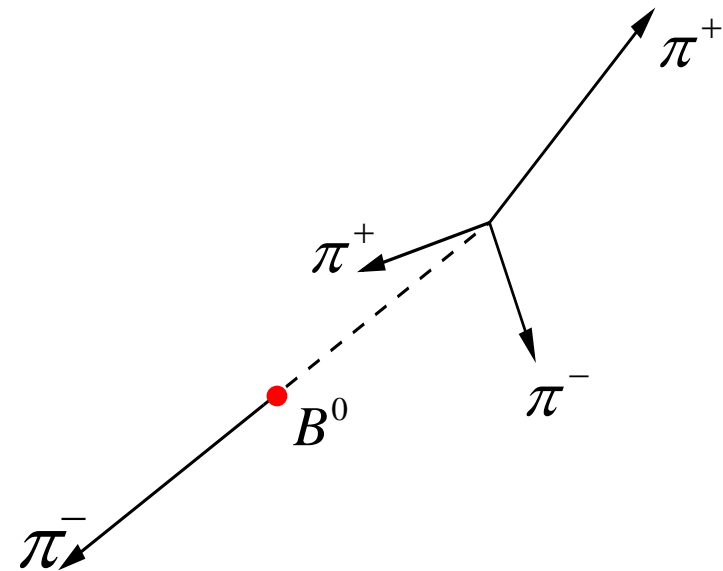
Mode	$n$ (ev.)	Bias (ev.)	$\epsilon$ (%)	$\prod \mathcal{B}_i$ (%)	$S(\sigma)$	$\mathcal{B}(10^{-6})$	$\mathcal{A}_{ch}$
$B \rightarrow \eta'K^*$					5.6	$4.1_{-0.9}^{+1.0} \pm 0.5$	
$B^0 \rightarrow \eta'K^{*0}$					4.3	$3.8 \pm 1.1 \pm 0.5$	$-0.08 \pm 0.25 \pm 0.02$
$B^+ \rightarrow \eta'K^{*+}$					3.6	$4.9_{-1.7}^{+1.9} \pm 0.8 (< 7.9)$	$0.30_{-0.37}^{+0.33} \pm 0.02$
$B^0 \rightarrow \eta'\rho^0$	$15_{-8}^{+11}$	$+11.2 \pm 5.7$	$22.8 \pm 1.4$	17.5	0.3	$0.4_{-0.9-0.6}^{+1.2+1.6} (< 3.7)$	
$B^0 \rightarrow \eta'f_0(980)(f_0 \rightarrow \pi^+\pi^-)$	$-3_{-4.0}^{+6.0}$	$-3.8 \pm 2.0$	$25.4 \pm 1.6$	17.5	0.2	$0.1_{-0.4-0.4}^{+0.6+0.9} (< 1.5)$	
$B^+ \rightarrow \eta'\rho^+$	$57_{-15}^{+16}$	$+11.5 \pm 5.8$	$13.0 \pm 1.0$	17.5	3.2	$8.7_{-2.8-1.3}^{+3.1+2.3} (< 14)$	$-0.04 \pm 0.28 \pm 0.02$



# $B^0 \rightarrow a_1(1260)\pi$

- First seen in 2004
- Difficult analysis
  - $a_1$  not well known.
  - Some disagreement on its width in PDG.
  - Decays to  $\rho\pi$  and  $\sigma\pi$  final states have been reported.
  - $\tau$  data from CLEO give the most information on this.
  - Possible backgrounds include  $a_2(1320)\pi$ ,  $\pi(1300)\pi$ .
- Interesting prospects for model dependent CKM constraints
  - Can be used to measure  $\alpha$ .
  - Not yet clear how effective a measurement will be.
    - need  $a_1K$ ,  $K_1\pi$  decays as well.

PRD 73 (2006) 057502



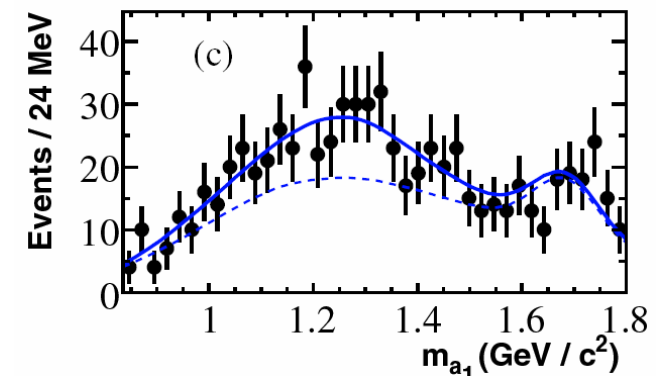
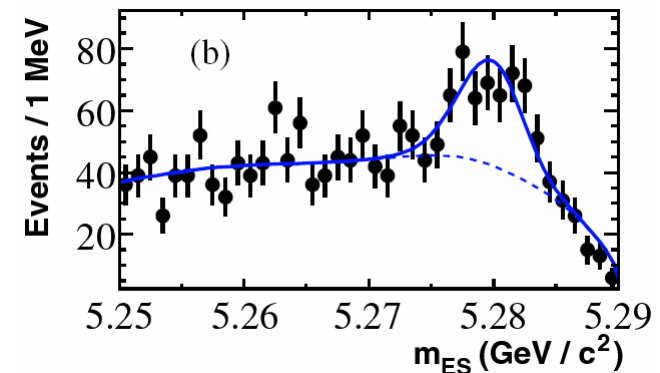
Angular correlations discriminate between signal and background

- BaBar uses the angle between the bachelor  $\pi$  and the normal to the  $a_1 \rightarrow 3\pi$  decay plane:  $(\cos A)$ .

# $B^0 \rightarrow a_1(1260)\pi$

PRL 71, 051082 (2006)

- Fit  $m_{ES}$ ,  $\Delta E$ , Fisher,  $m_{a_1}$ ,  $\cos A$ .
- backgrounds from
  - $e+e^- \rightarrow qq$
  - inclusive B background
  - $B^0 \rightarrow a_2^+(1320)\pi^-$
- $B^0 \rightarrow \pi^+(1300)\pi^-$  negligible
- Reconstruction efficiency:
  - $\varepsilon=11.7\%$
- Dominant systematic errors:
  - PDF shape (6.2%)
  - $\rho^0\rho^0$ ,  $\rho\pi\pi$ ,  $4\pi$  background.
- Assume  $BF(a_1 \rightarrow \rho^0\pi)=0.5$ , and  $B(a_1 \rightarrow \pi^+\pi^-\pi^+)=B(a_1 \rightarrow \pi^+\pi^0\pi^0)$ .



$$BF = (33.2 \pm 3.8 \pm 3.0) \times 10^{-6}$$

$$N_{signal} = 421 \pm 48 \text{ events}$$

218 million  $B\bar{B}$  pairs

# Summary

- Lots of results on rare hadronic B decays.
  - The spectrum of branching fractions provides theorists reference points to tune calculations.
  - Observation of direct CPV was a triumph of B-physics and we need to continue this effort to see other signals in  $B^0$  decays and find direct CP violation in  $B^+$  decay.
  - $B \rightarrow VV$  decays have provided an interesting polarisation puzzle to solve.
  - Also obtain interesting model dependent constraints on UT.
  - Starting to produce interesting bounds on SM pollution in  $\eta'K^0$  and  $\phi K^0$  using PP decays.
- Much more not discussed ... Dalitz analyses, TDCPV, CPV in  $\eta'K^0$  etc.
- Lots more work to do in this exciting area into the multi- $\text{ab}^{-1}$  realm!