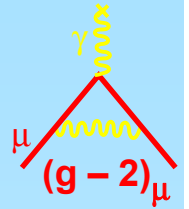


# Muon (g-2) to 0.25 ppm

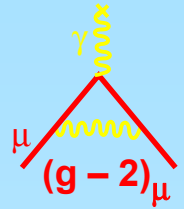


**James Miller**  
**(For the new Muon (g-2) Collaboration, E969)**  
**Department of Physics**  
**Boston University**

miller @ bu.edu

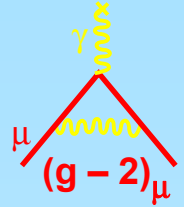
James Miller CERN Workshop October 2006





# Outline

- Brief theoretical motivation
- Comparison between theoretical prediction and experimental value from previous experiment: Case for x2 better experimental measurement
- Description of the proposed experiment: upgrades of the previous experiment



$$\vec{\mu}_s = g_s \left( \frac{e}{2m} \right) \vec{s}$$

For spin 1/2 particles:

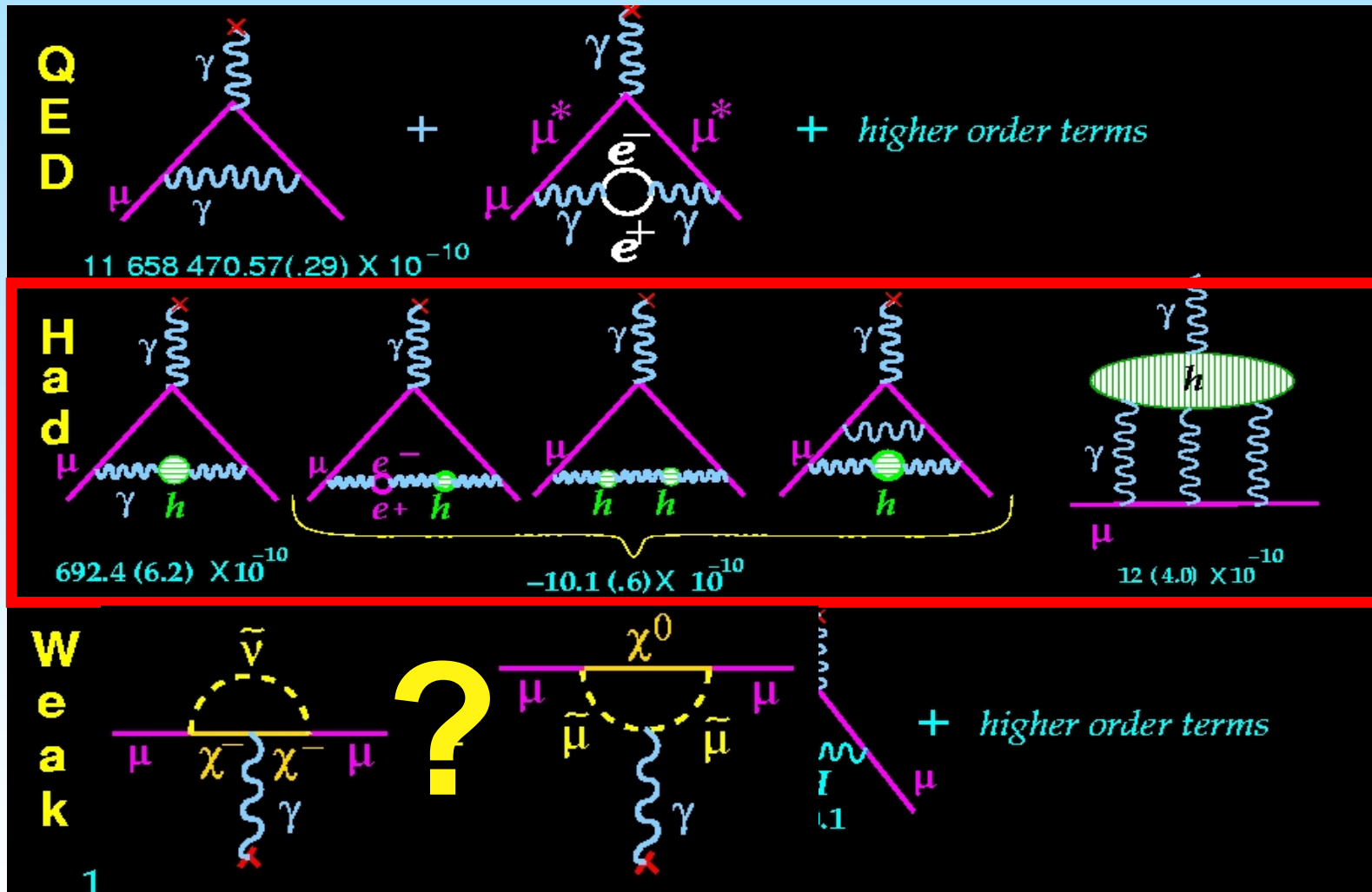
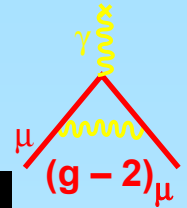
$$\mu = (1 + a) \frac{e\hbar}{2m}$$

Dirac + Pauli moment

$$a = \frac{g - 2}{2}$$

$$a = \frac{\alpha}{2\pi} = 0.00116$$

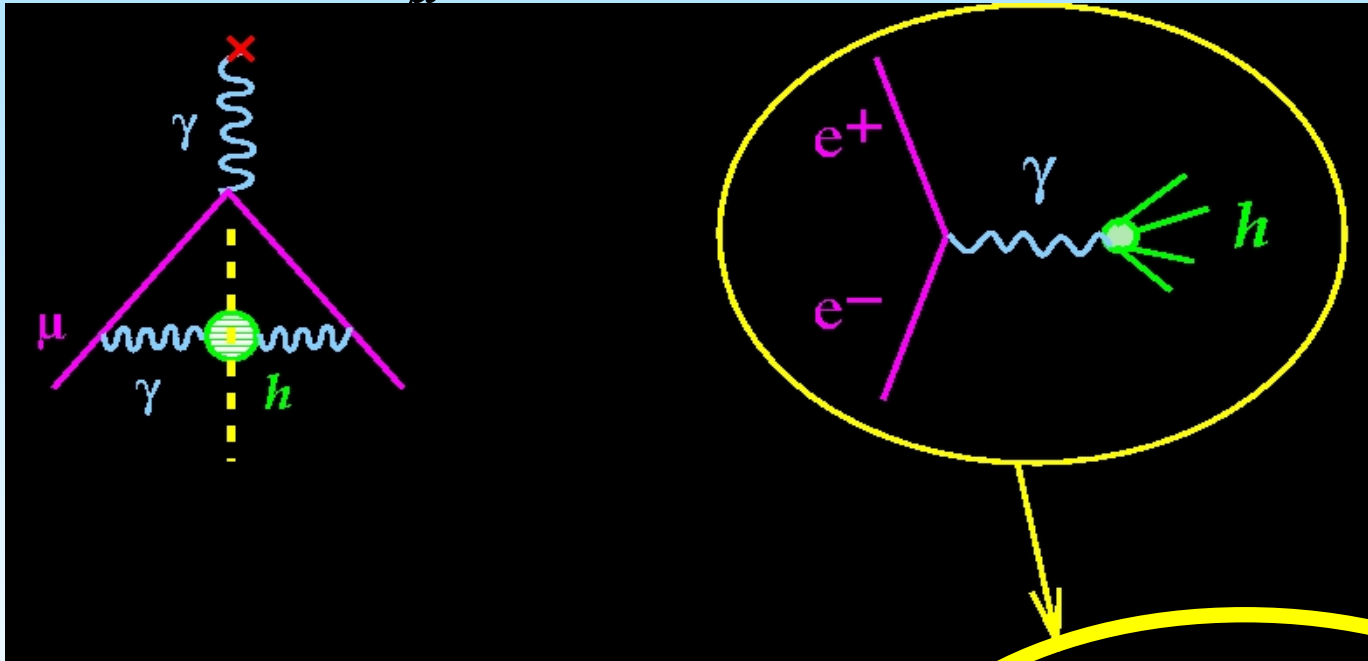
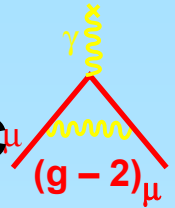
# Standard Model Value for the Muon Anomaly



**e vs.  $\mu$ : relative contribution of heavier things**

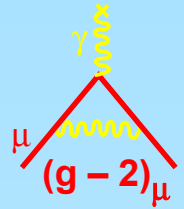
$$\left(\frac{m_\mu}{m_e}\right)^2 \simeq 40,000$$

There is a relationship between  $e^+e^-$  annihilation data and the lowest-order hadronic contribution to  $a_\mu$



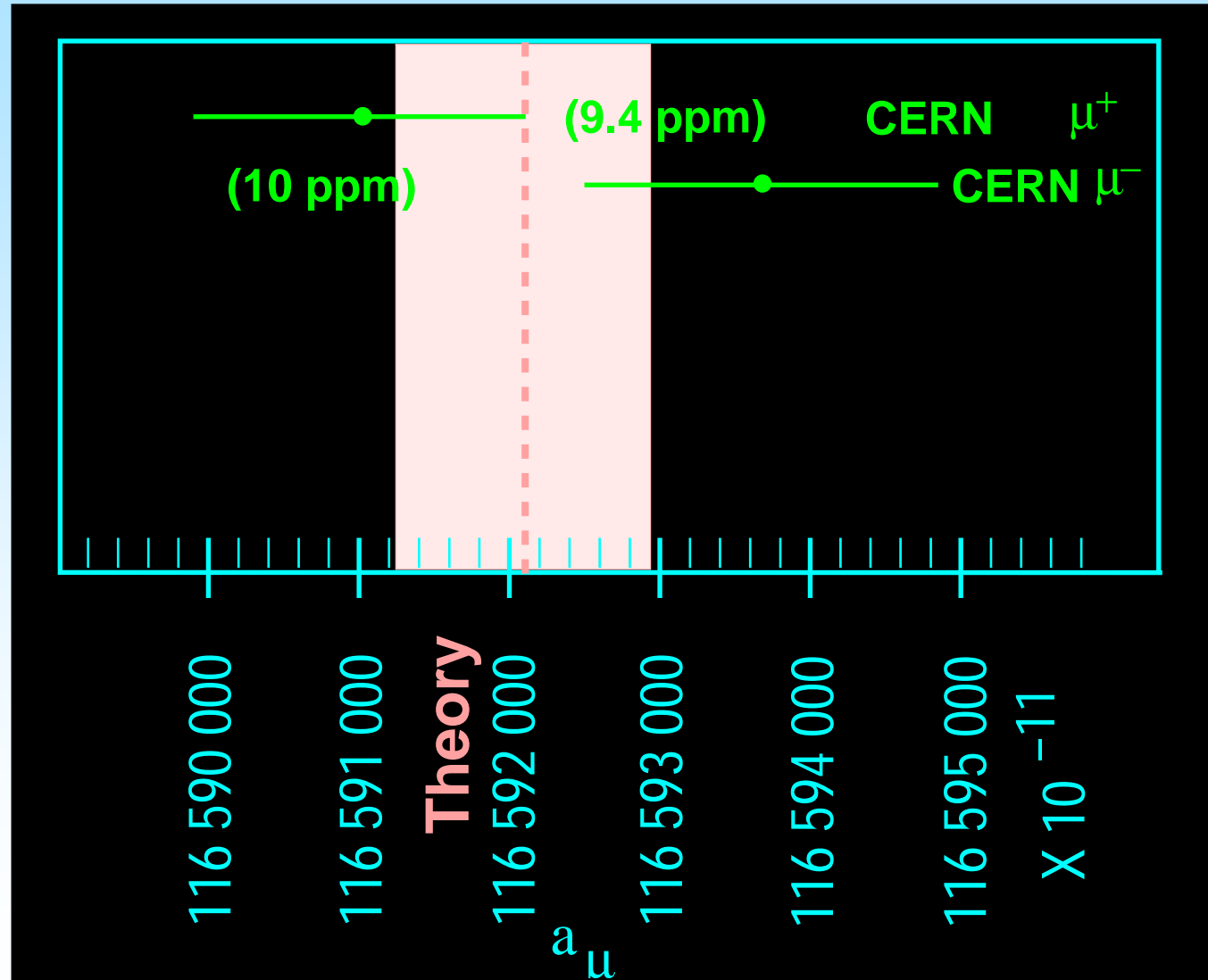
$$a_\mu(\text{had}) = \left( \frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^{\infty} \frac{ds}{s^2} K(s) \left( \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} \right)$$

# When we started in 1984, theory and experiment were known to about 10 ppm.



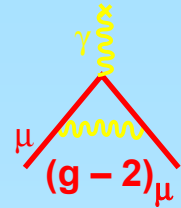
Theory uncertainty was ~ 9 ppm

Experimental uncertainty was 7.3 ppm (from the CERN g-2 measurement of the 1970's)





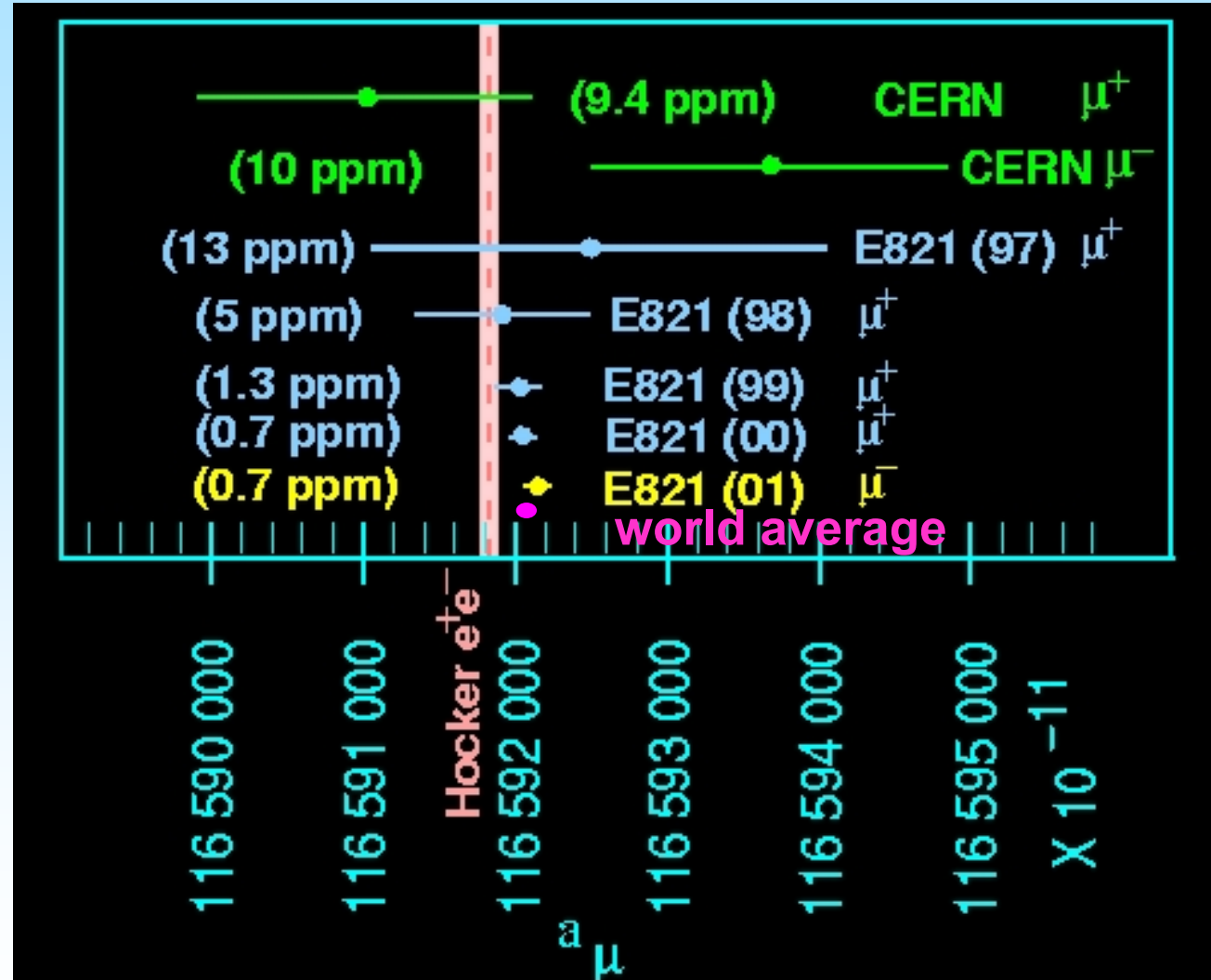
E821 achieved 0.5 ppm and the  $e^+e^-$  based theory is also at the 0.5 ppm level. Both can be improved.



All E821 results were obtained with a “blind” analysis.

$$\sigma_{\text{stat}} = \pm 0.46 \text{ ppm}$$

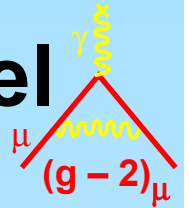
$$\sigma_{\text{syst}} = \pm 0.28 \text{ ppm}$$



$$a_\mu = 11\,659\,208(6) \times 10^{-10} \text{ (0.54 ppm)}$$



With an apparent discrepancy at the level  
of  $3.3 \sigma$  . . .



Have to work harder to improve the  
measurement and the theory value . . . .

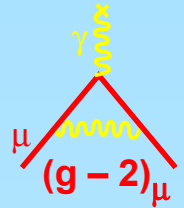
*Better  $e^+e^-$  scattering data*

*Better  $(g-2)$  data*



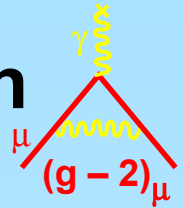
# A $(g-2)_\mu$ Experiment to $\pm 0.25$ ppm Precision

## –BNL E969 Collaboration



R.M. Carey, I. Logashenko, K.R. Lynch, J.P. Miller B.L. Roberts- **Boston University**; G. Bunce, W. Meng, W. Morse, P. Pile, Y.K. Semertzidis -**Brookhaven**; D. Grigoriev, B.I. Khazin, S.I. Redin, Yuri M. Shatunov, E. Solodov – **Budker Institute**; F.E. Gray, B. Lauss, E.P. Sichtermann – **UC Berkeley and LBL**; Y. Orlov – **Cornell University**; J. Crnkovic, P. Debevec, D.W. Hertzog, P. Kammel, S. Knaack, R. McNabb – **University of Illinois UC**; K.L. Giovanetti – **James Madison University**; K.P. Jungmann, C.J.G. Onderwater – **KVI Groningen**; T.P. Gorringer, W. Korsch – **U. Kentucky**, P. Cushman – **Minnesota**; Y. Arimoto, Y. Kuno, A. Sato, K. Yamada – **Osaka University**; S. Dhawan, F.J.M. Farley – **Yale University**

We measure the difference frequency between the spin and momentum precession, and B



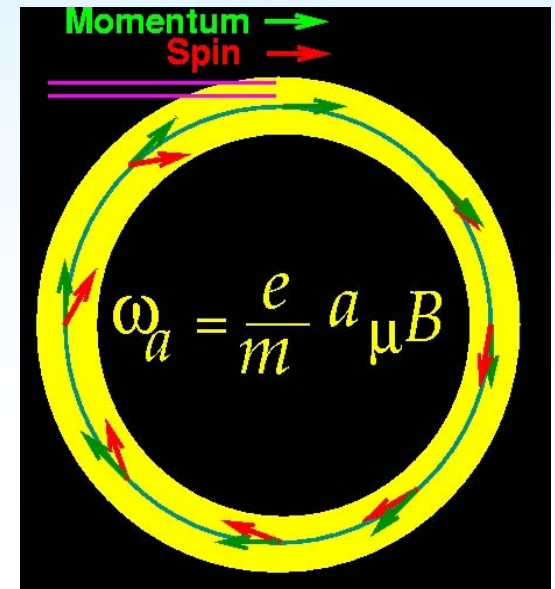
$$\omega_a = \omega_S - \omega_C = \left( \frac{g-2}{2} \right) \frac{eB}{m} \quad \langle \omega_a \rangle_\mu, \langle B \rangle_\mu$$

With an electric quadrupole field for vertical focusing

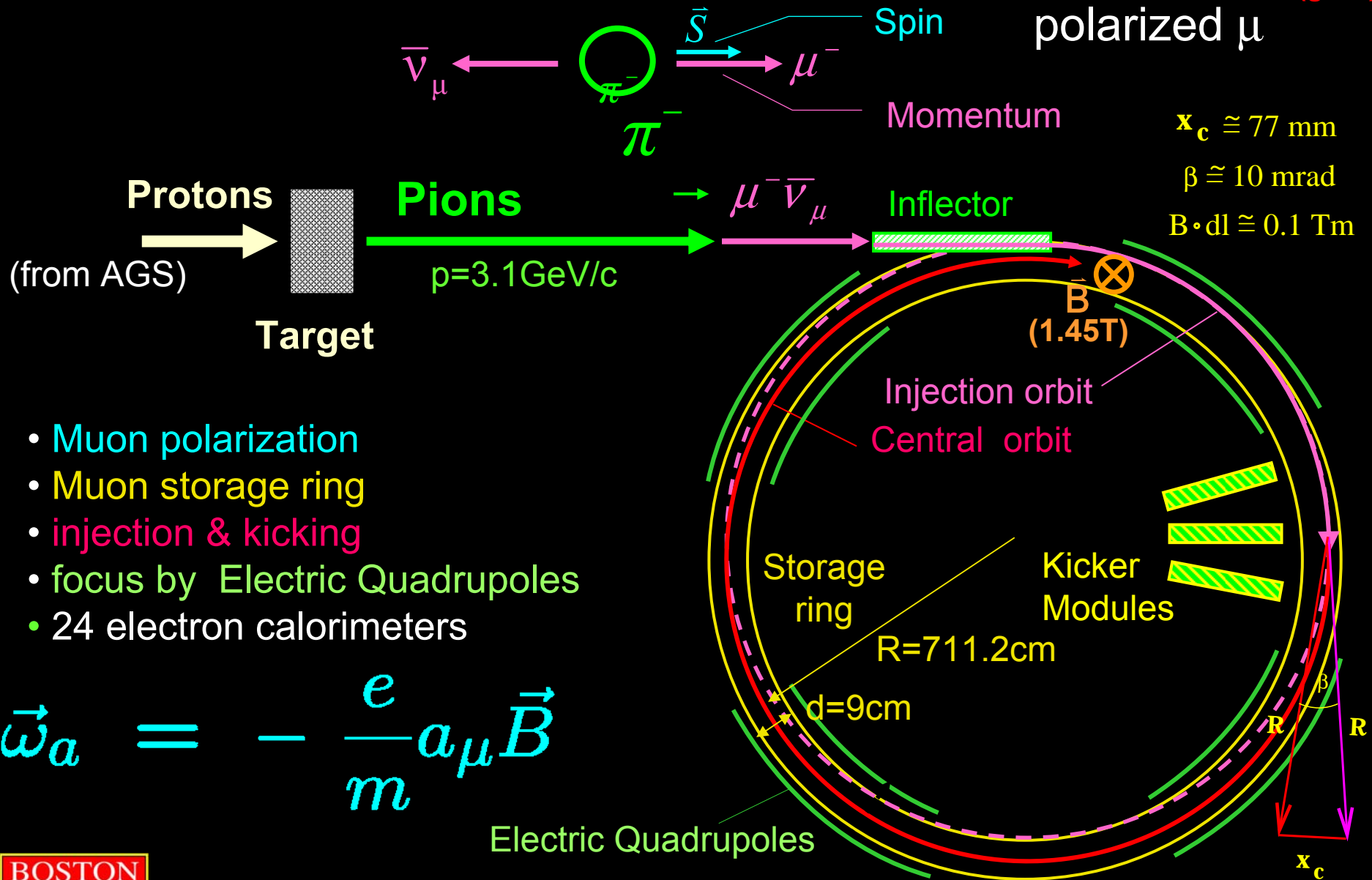
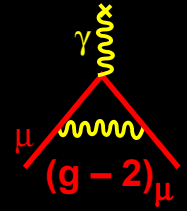
$$\vec{\omega}_a = - \frac{e}{m} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

$$\gamma_{\text{magic}} = 29.3$$

$$p_{\text{magic}} = 3.09 \text{ GeV}/c$$



# Experimental Technique

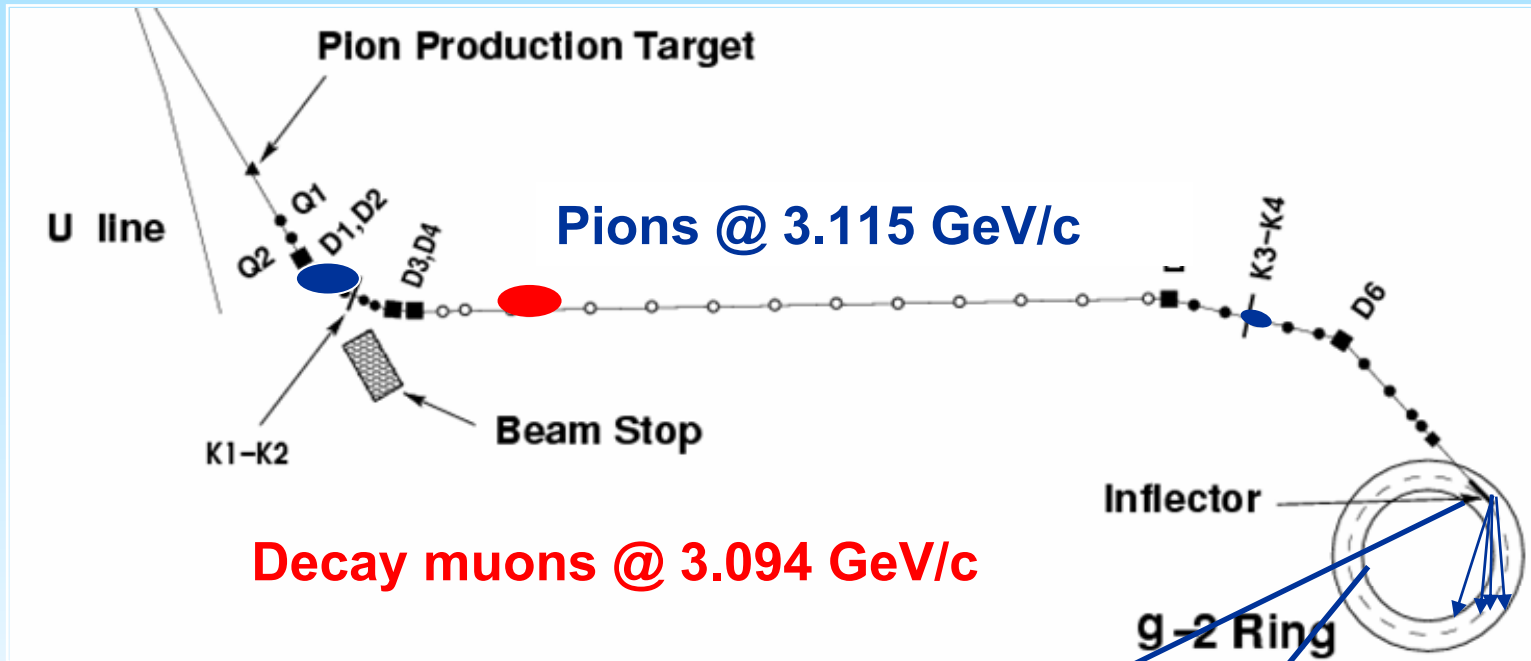
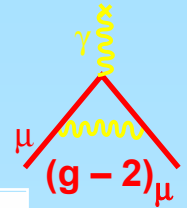


- Muon polarization
- Muon storage ring
- injection & kicking
- focus by Electric Quadrupoles
- 24 electron calorimeters

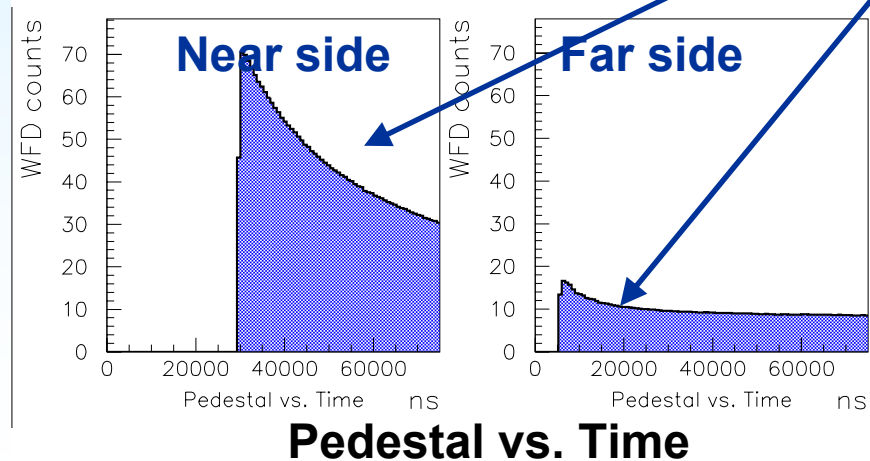
$$\vec{\omega}_a = - \frac{e}{m} a_\mu \vec{B}$$

Electric Quadrupoles

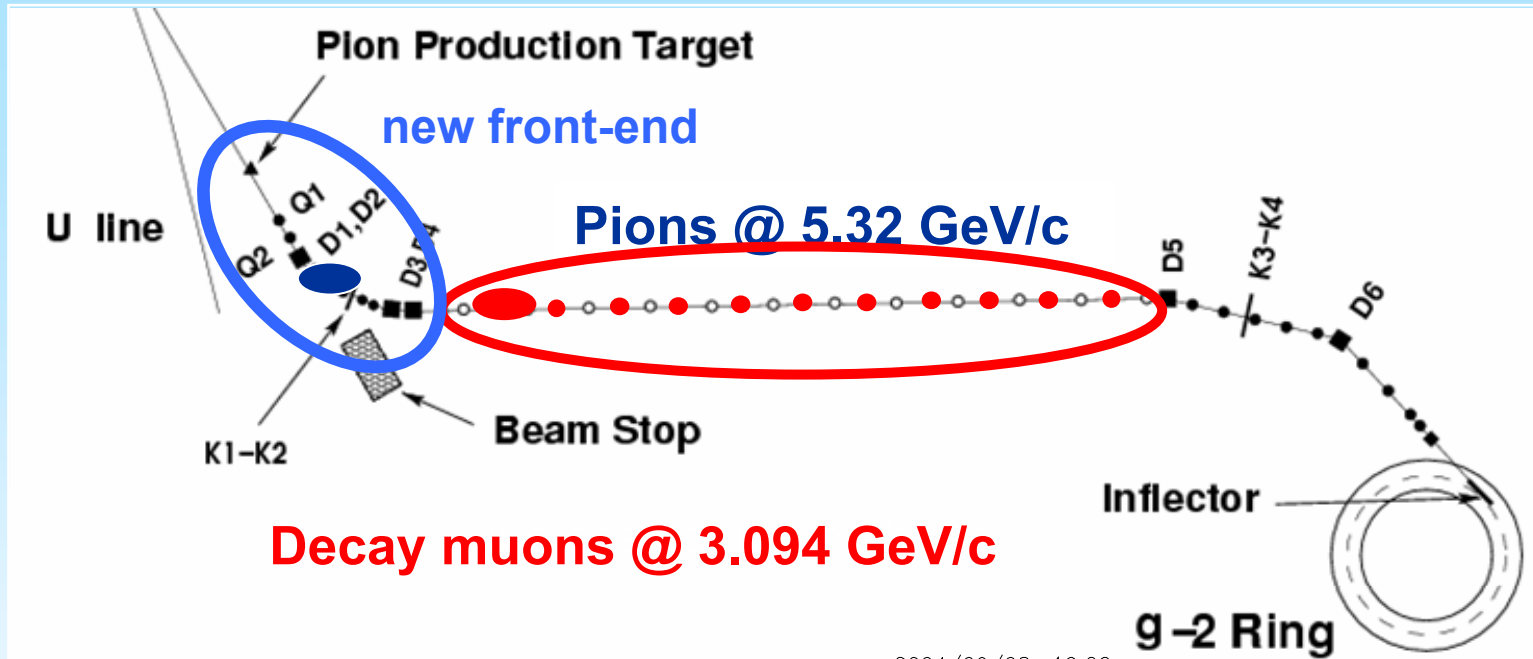
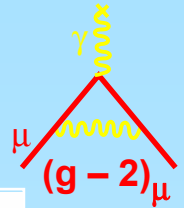
# E821: used a “forward” decay beam



This baseline limits how early we can fit data



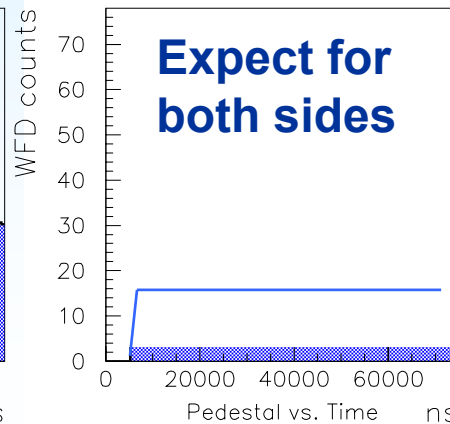
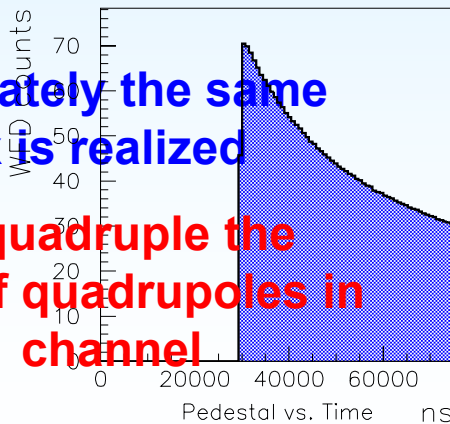
# E969: may use a “backward” decay beam



2004/09/08 12.22

Approximately the same muon flux is realized

Then we quadruple the number of quadrupoles in the decay channel



Expect for both sides

No hadron-induced prompt flash

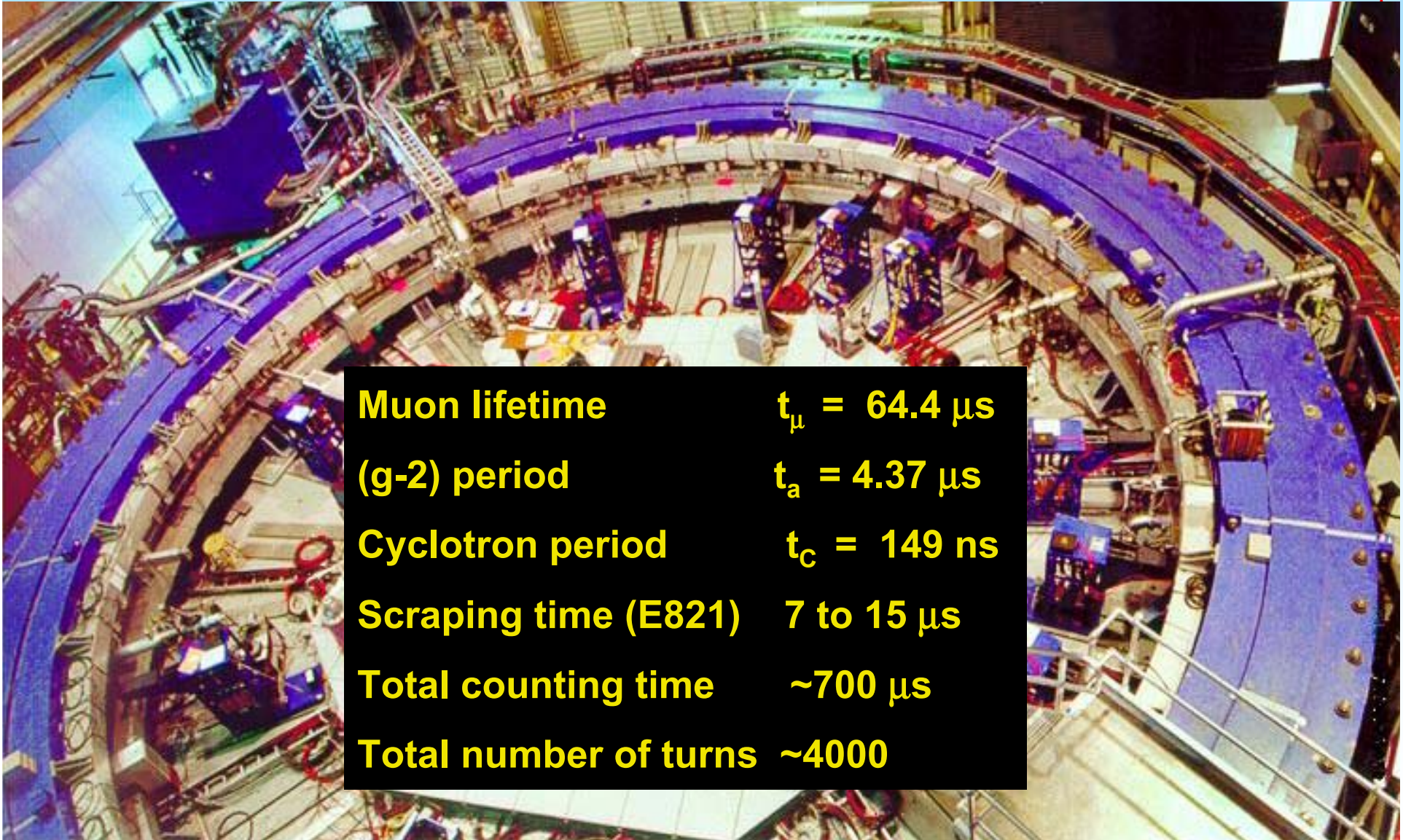
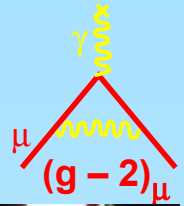
**x 1  
more  
muons**



> x 2.5

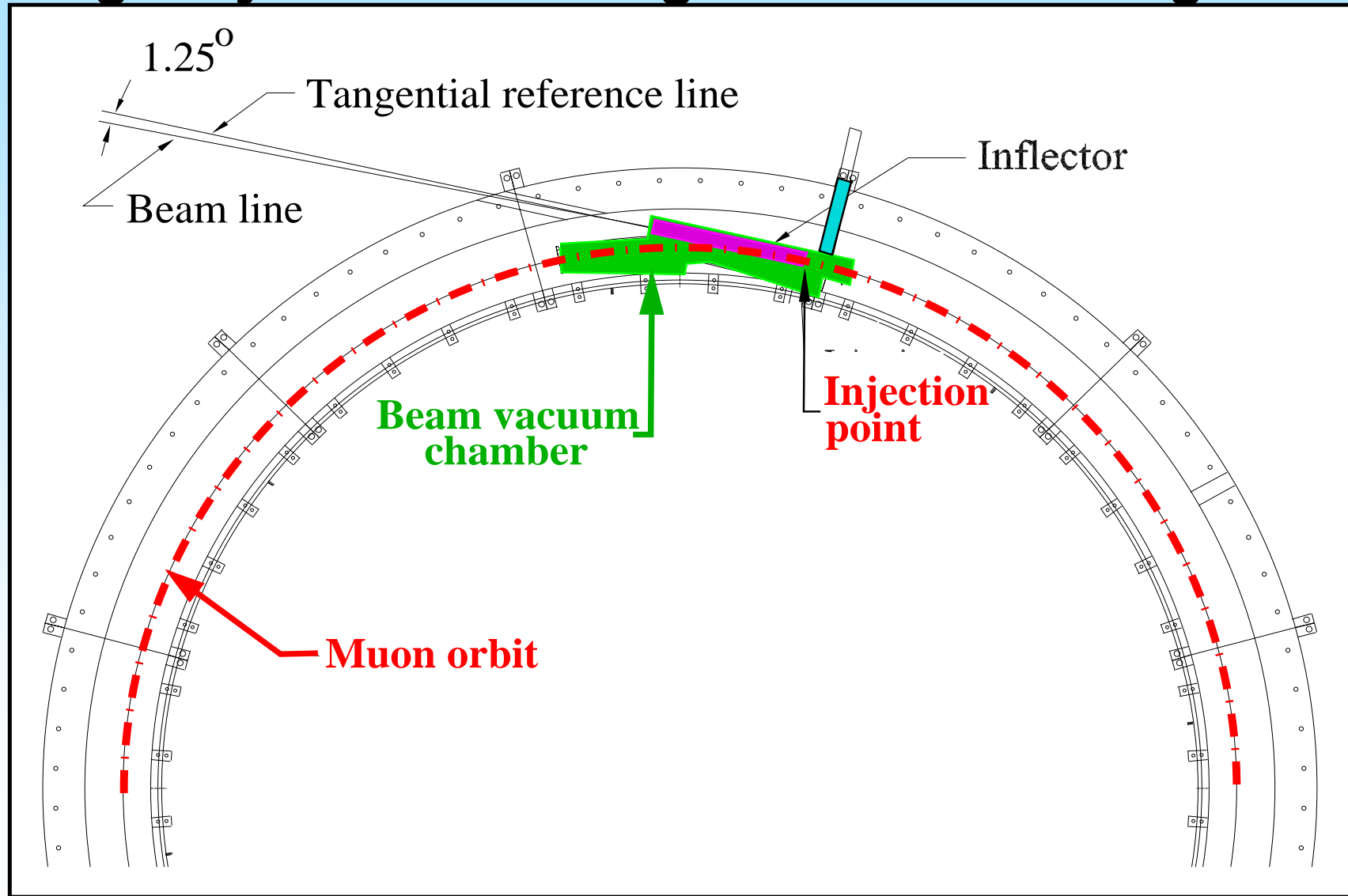


# The 700 ton $(g-2)_\mu$ precision storage ring ( $B=1.45$ T, $R=7.1$ m)



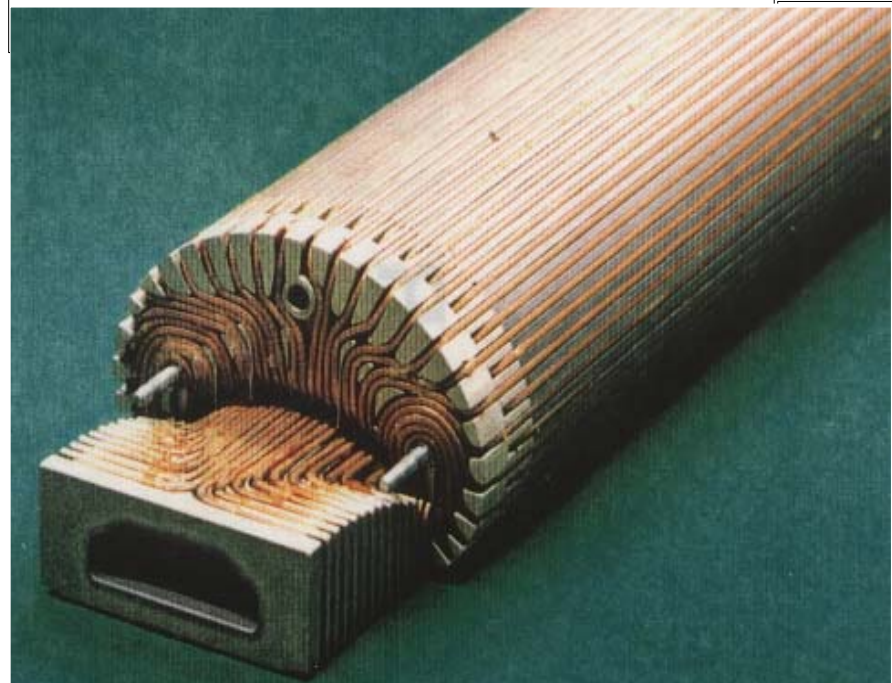
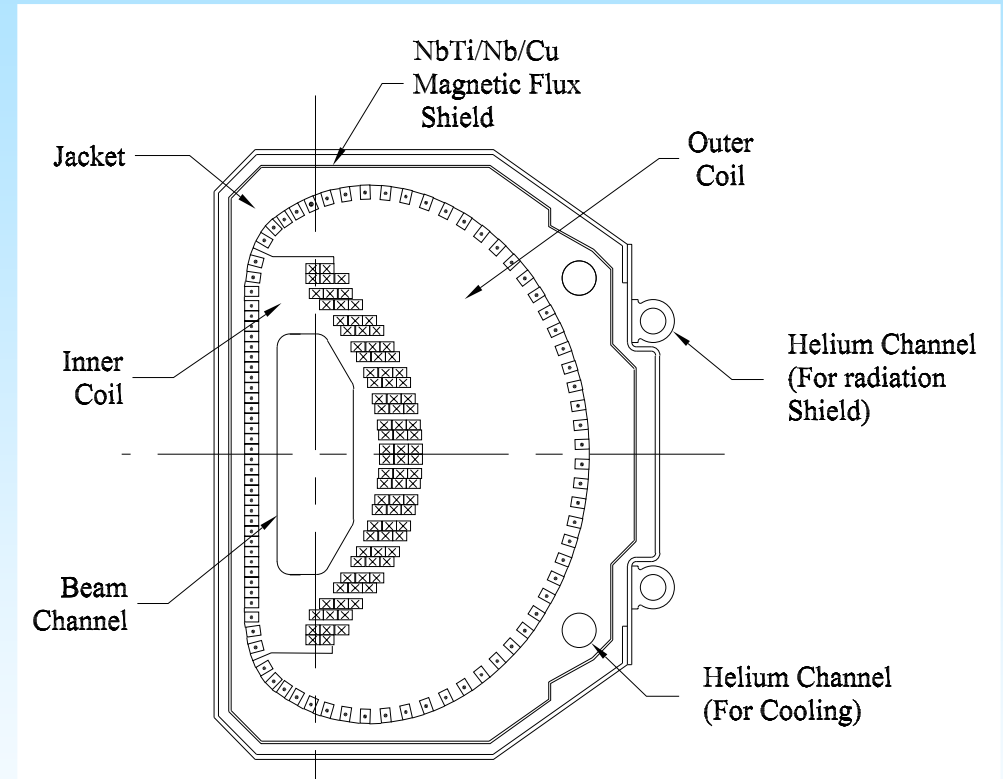
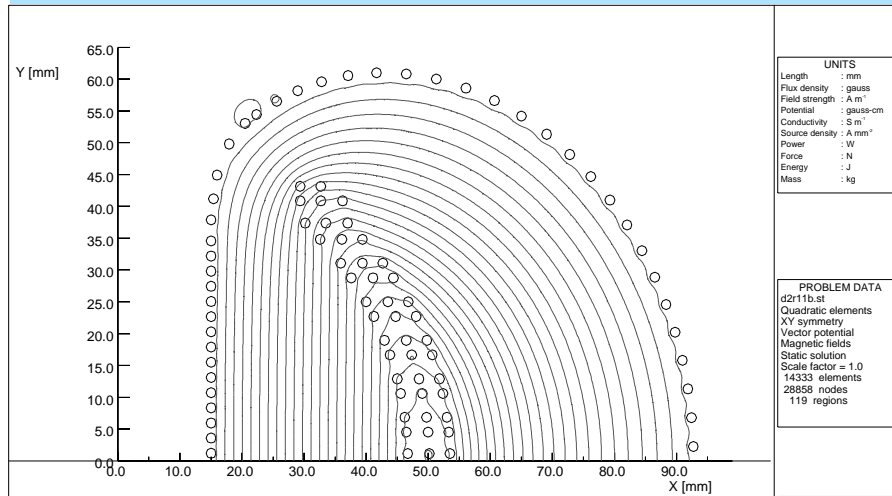
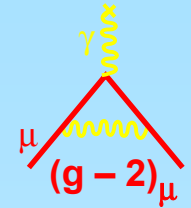
**Muon lifetime**  $t_\mu = 64.4 \mu\text{s}$   
**(g-2) period**  $t_a = 4.37 \mu\text{s}$   
**Cyclotron period**  $t_c = 149 \text{ ns}$   
**Scraping time (E821)** 7 to 15  $\mu\text{s}$   
**Total counting time**  $\sim 700 \mu\text{s}$   
**Total number of turns**  $\sim 4000$

# The incident beam must enter through the magnet yoke and through an inflector magnet





# The E821 inflector magnet had closed ends which lost half the beam.



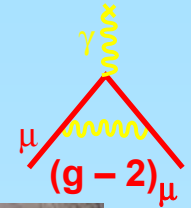
Length = 1.7 m

Central field = 1.45 T

Open end prototype, built and tested

→ X2 Increase in Beam

# E821 Electron Detectors were Pb-scintillating fiber calorimeters read-out by 4 PMTs: signals summed



**muon momentum**

**muon spin**

**Sci-Fi Calorimeter module**

**Measures Energy and time**

**spin forward, more high energy e**

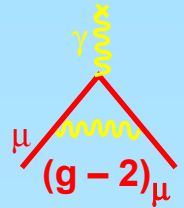
**spin backward, less high energy e**

**400 MHz digitizer**



**New experiment needs segmented detectors for pileup reduction.**

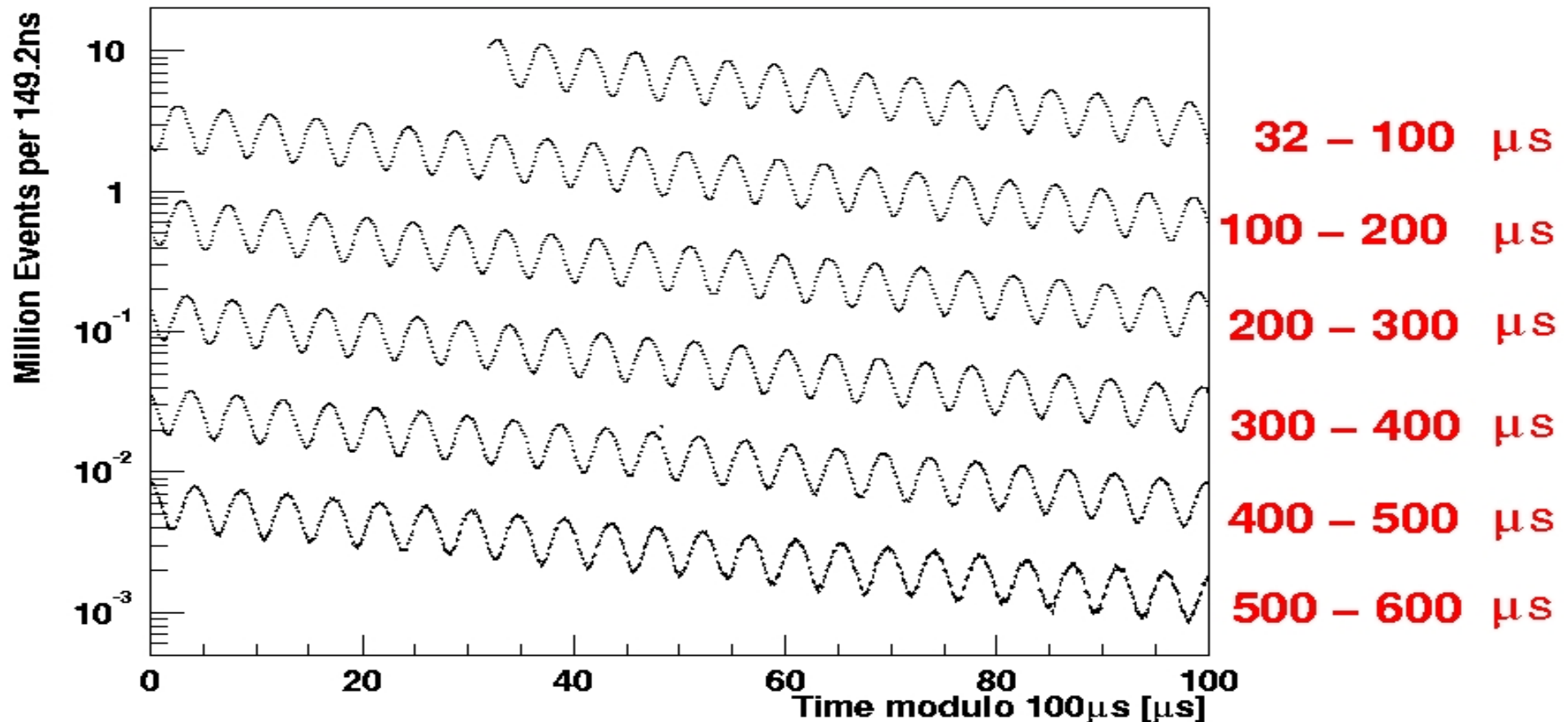
We count high-energy  $e^-$  or  $e^+$  from muon decays as a function of time. Shown here:



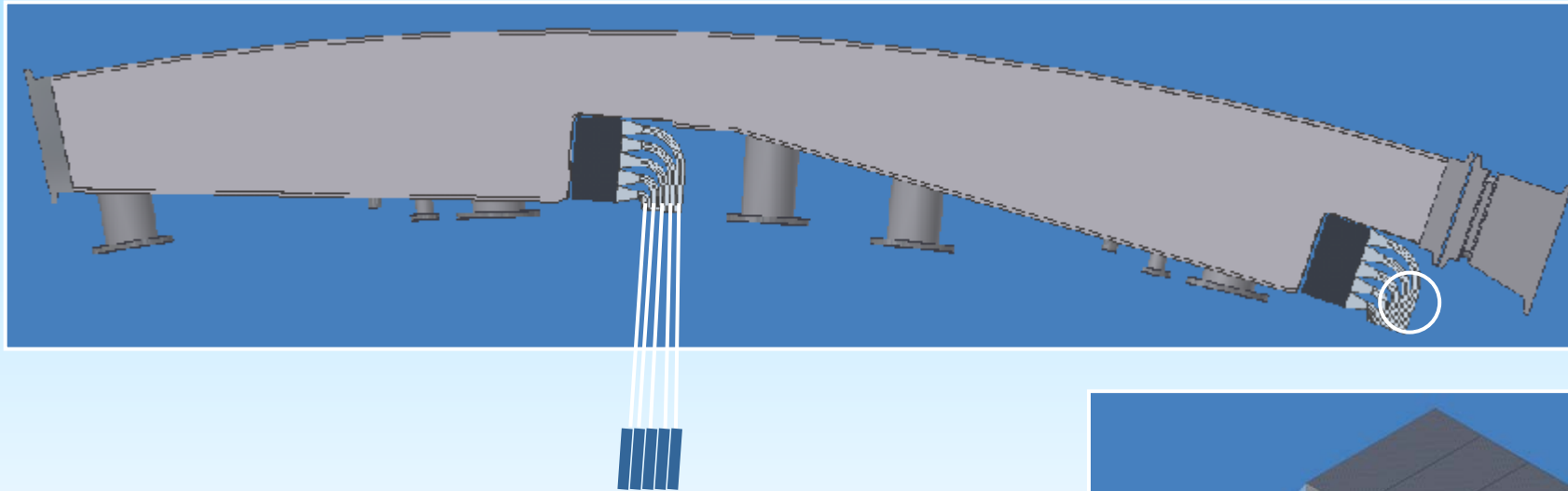
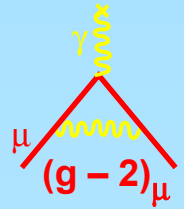
$$4 \times 10^9 e^-, E_{e^-} \geq 1.8 \text{ GeV}$$

$$f(t) \simeq N_0 e^{-\lambda t} [1 + A \cos(\omega_a t + \phi)]$$

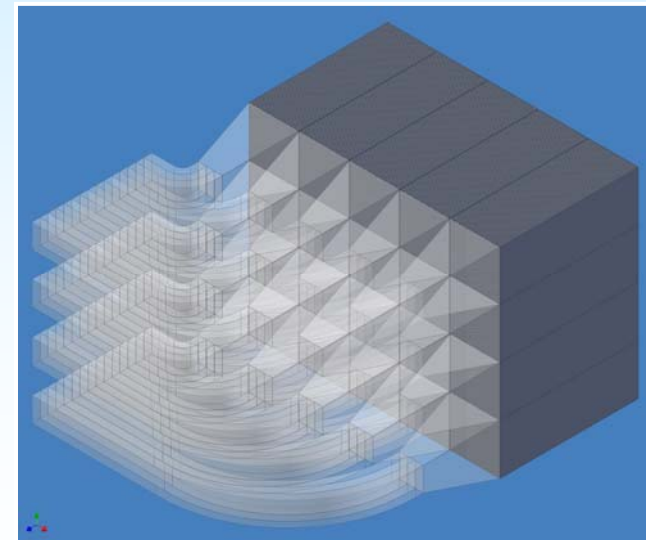
electron time spectrum (2001)



# New segmented detectors of tungsten/scintillating- fiber ribbons to handle pile-up

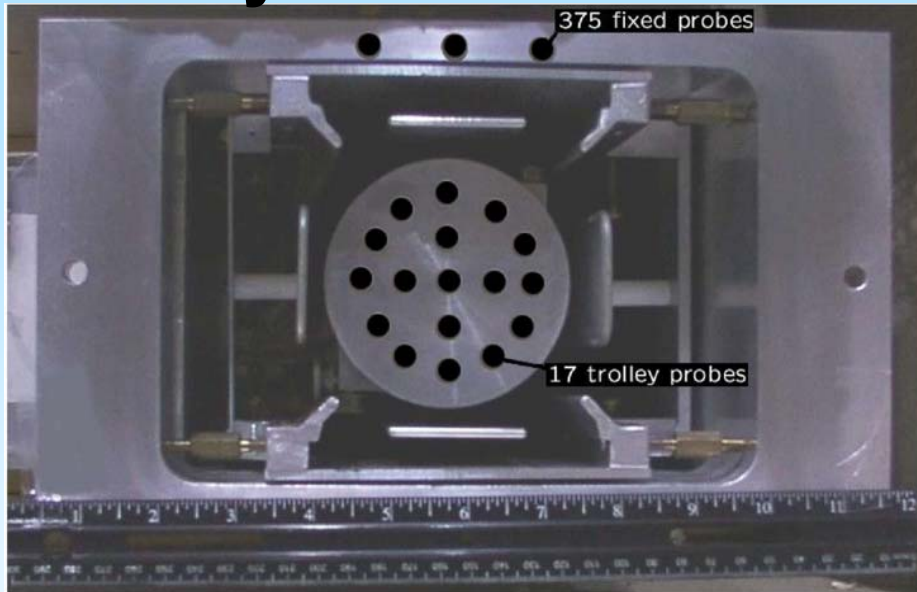
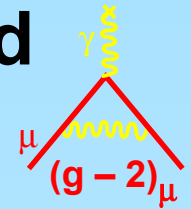


- System fits in available space
- Prototype under construction
- Again the bases will be gated.



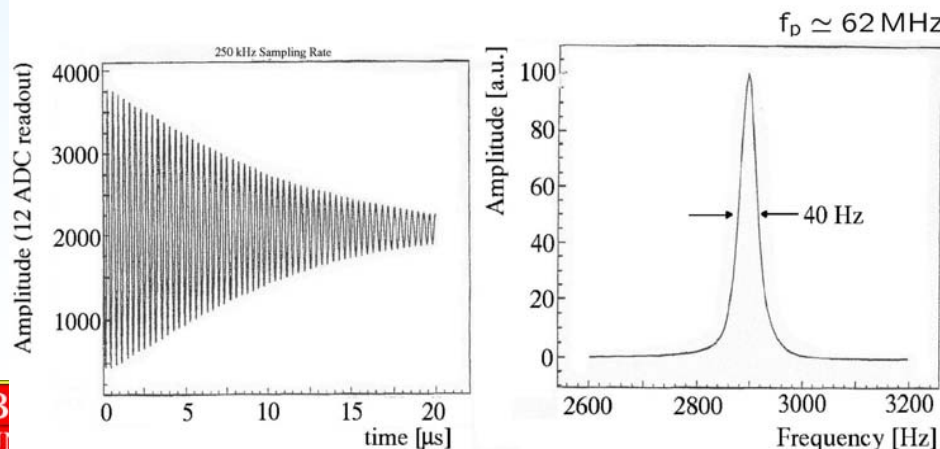


# The magnetic field is measured and controlled using pulsed NMR and the free-induction decay.



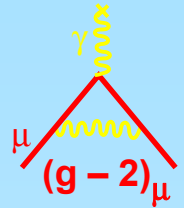
- Calibration to a spherical water sample that ties the field to the Larmor frequency of the free proton  $\omega_p$ .
- Fixed probes, above and below storage region, monitor the field between trolley mappings.
- So we measure  $\omega_a$  and  $\omega_p$

Free induction decay signals:

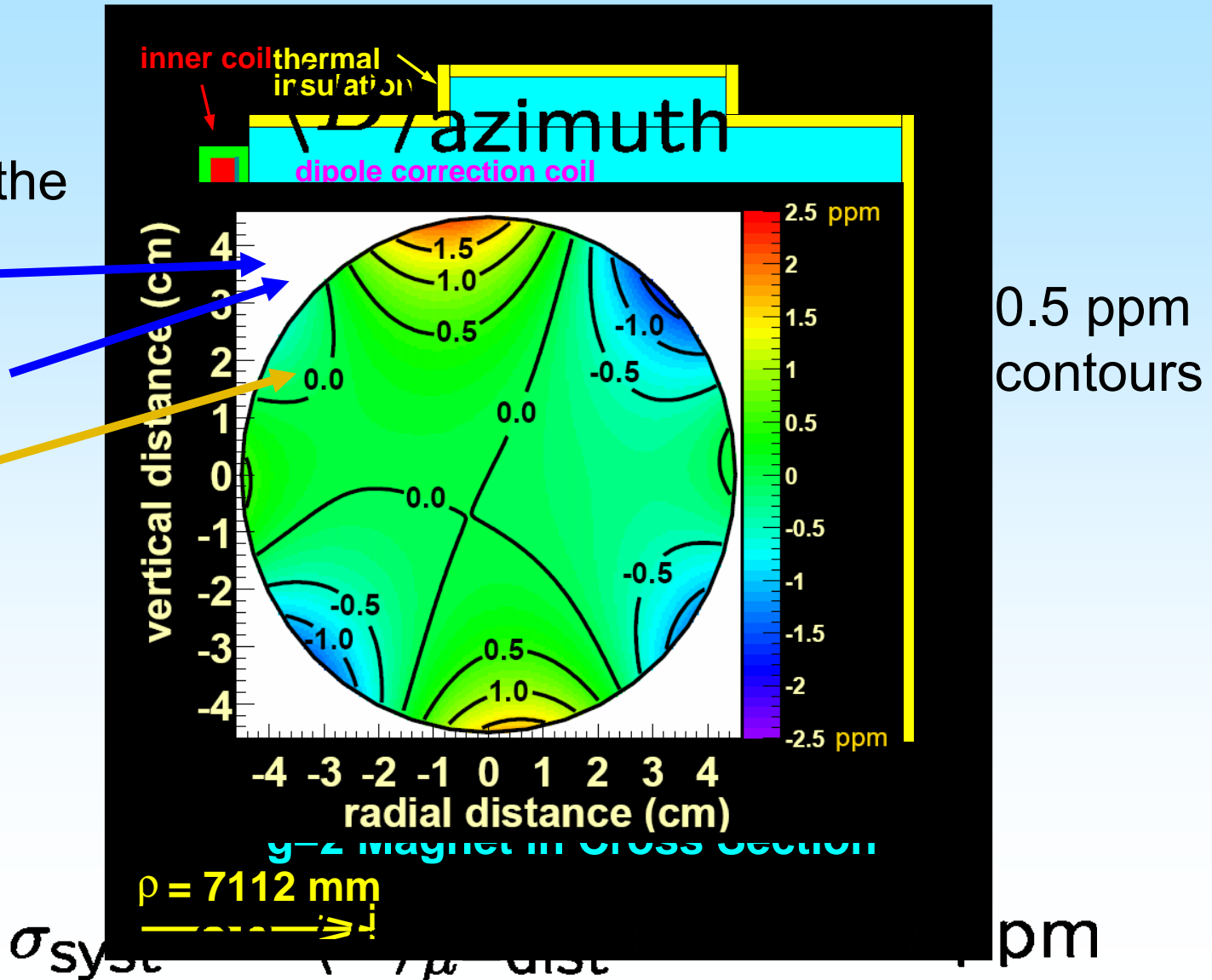


$$a_{\mu} = \frac{\frac{\omega_a}{\omega_p}}{\frac{\mu_{\mu}}{\mu_p}} = \frac{\omega_a}{\omega_p} \frac{\mu_p}{\mu_{\mu}}$$

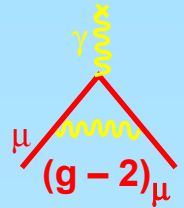
# The $\pm 1$ ppm uniformity in the average field is obtained with special shimming tools.



We can shim the  
**dipole**,  
**quadrupole**  
**sextupole**



# E969 needs 4 times more stored muons than E821.



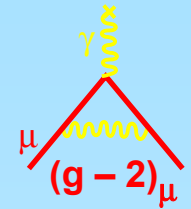
- Open Inflector X2
  - Backward Beam ? X1
  - Quadruple the Quadrupoles X 2.5-3
- 
- Beam increase design factor >X 5

Forward beam: higher muon flux , but no increase in flash over E821

Backward beam: flash eliminated



# Systematic errors on $\omega_a$ (ppm)



| $\sigma_{\text{systematic}}$ | 1999        | 2000        | 2001        |
|------------------------------|-------------|-------------|-------------|
| <b>Pile-up</b>               | <b>0.13</b> | <b>0.13</b> | <b>0.08</b> |
| <b>AGS Background</b>        | <b>0.10</b> | <b>0.01</b> | *           |
| <b>Lost Muons</b>            | <b>0.10</b> | <b>0.10</b> | <b>0.09</b> |
| <b>Timing Shifts</b>         | <b>0.10</b> | <b>0.02</b> | <b>0.02</b> |
| <b>E-Field, Pitch</b>        | <b>0.08</b> | <b>0.03</b> | *           |
| <b>Fitting/Binning</b>       | <b>0.07</b> | <b>0.06</b> | *           |
| <b>CBO</b>                   | <b>0.05</b> | <b>0.21</b> | <b>0.07</b> |
| <b>Beam Debunching</b>       | <b>0.04</b> | <b>0.04</b> | *           |
| <b>Gain Change</b>           | <b>0.02</b> | <b>0.13</b> | <b>0.13</b> |
| <b>total</b>                 | <b>0.3</b>  | <b>0.31</b> | <b>0.21</b> |

Detector segmentation and lower energy-threshold required for pile-up rejection with higher rates

Beam manipulation

Simulation of effects of island length, wider islands

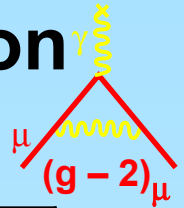
# Systematic errors on $\omega_p$ (ppm)



| Source of Uncertainty                                     | 1998       | 1999       | 2000        | 2001        |
|---|------------|------------|-------------|-------------|
| Absolute Calibration                                      | 0.05       | 0.05       | 0.05        | 0.05        |
| Calibration of Trolley                                    | 0.3        | 0.20       | 0.15        | 0.09        |
| Trolley Measurements of $B_0$                             | 0.1        | 0.10       | 0.10        | 0.05        |
| Interpolation with the fixed probes                       | 0.3        | 0.15       | 0.10        | 0.07        |
| Inflector fringe field uncertainty from muon distribution | 0.2        | 0.20       | -           | -           |
| Other*  |            | 0.15       | 0.10        | 0.10        |
| <b>Total</b>  | <b>0.5</b> | <b>0.4</b> | <b>0.24</b> | <b>0.17</b> |

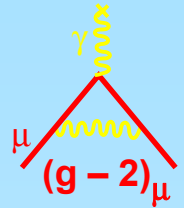
\*higher multipoles, trolley voltage and temperature response, kicker eddy currents

# The error budget for E969 represents continuation of improvements already made during E821



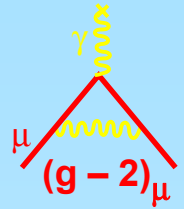
| Systematic uncertainty (ppm)      | 1998 | 1999 | 2000 | 2001 | E969 Goal |
|-----------------------------------|------|------|------|------|-----------|
| Magnetic field – $\omega_p$       | 0.5  | 0.4  | 0.24 | 0.17 | 0.1       |
| Anomalous precession – $\omega_a$ | 0.8  | 0.3  | 0.31 | 0.21 | 0.1       |
| Statistical uncertainty (ppm)     | 4.9  | 1.3  | 0.62 | 0.66 | 0.2       |
| Total Uncertainty (ppm)           | 5.0  | 1.3  | 0.73 | 0.72 | 0.25      |

- **Field improvements:** better trolley calibrations, better tracking of the field with time, temperature stability of room, improvements in the hardware
- **Precession improvements** will involve new scraping scheme, lower thresholds, more complete digitization periods, better energy calibration, increased detector segmentation



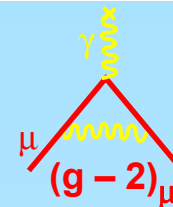
## Summary

- E821 Achieved a precision of  $\pm 0.5$  ppm
- There appears to be a discrepancy between experiment and  $e^+e^-$  based theory  $\rightarrow$  **hint of new physics?**
- E969 proposes to achieve a precision down to  $\pm 0.25$  ppm (factor of 2 improvement) with 4x as many muons
- Lots of continuing work worldwide on the hadronic theory piece, both experimental and theoretical.

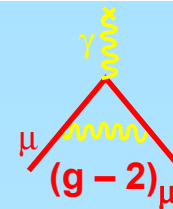


## Outlook:

- E969 is being considered by the national U.S. Particle Physics Project Prioritization Panel (P5): recommendation due this week!
- We hope that our friends in the theory,  $e^+e^-$  and  $\tau$  communities will continue to work on the hadronic contribution to  $a_\mu$
- If both theory and experiment can improve by a factor of 2, the stage is set for another potential confrontation between theory and experiment.

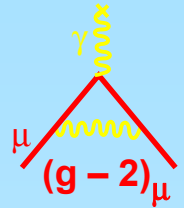


**Thanks to the organizers of this  
excellent conference!**



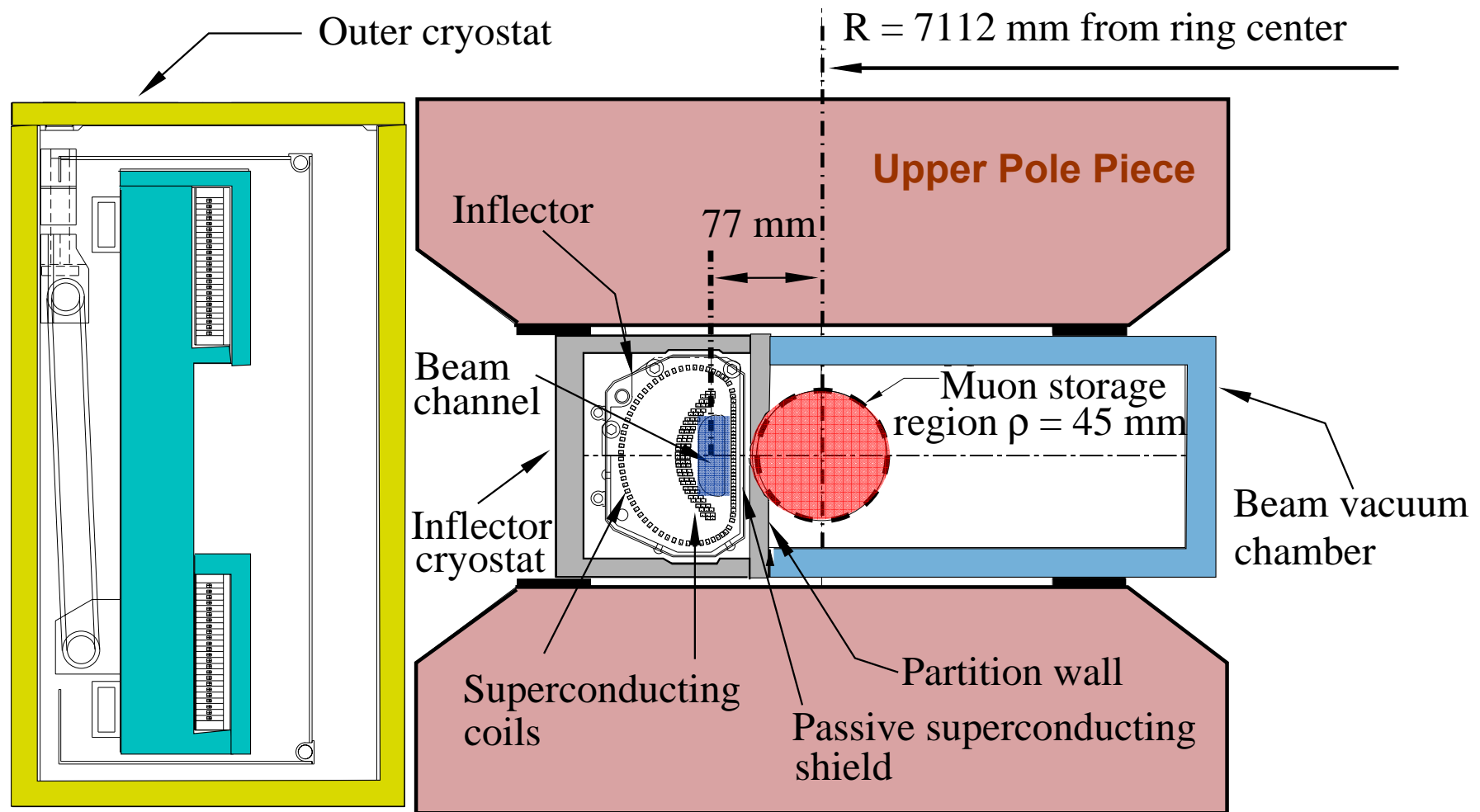
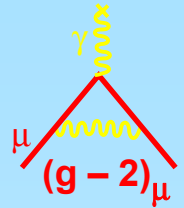


# E969 Builds on the apparatus and Experience of E821

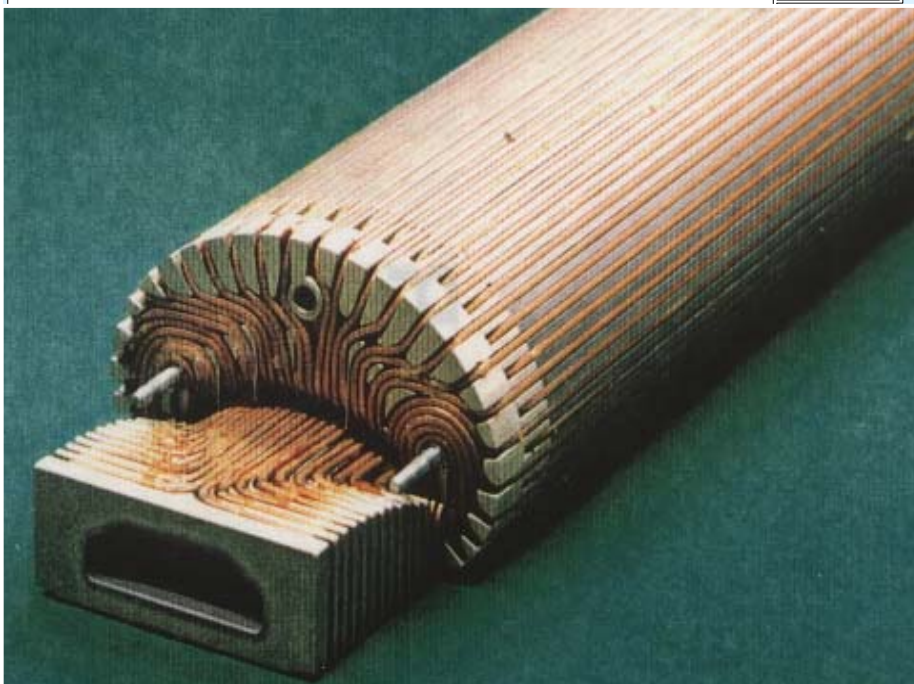
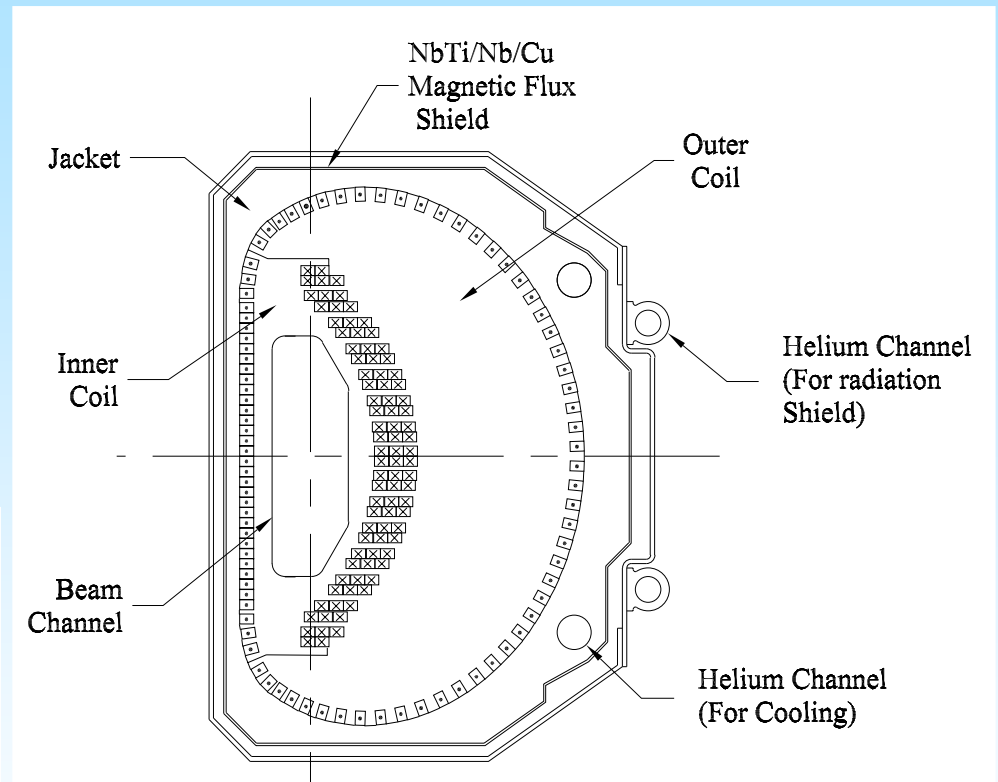
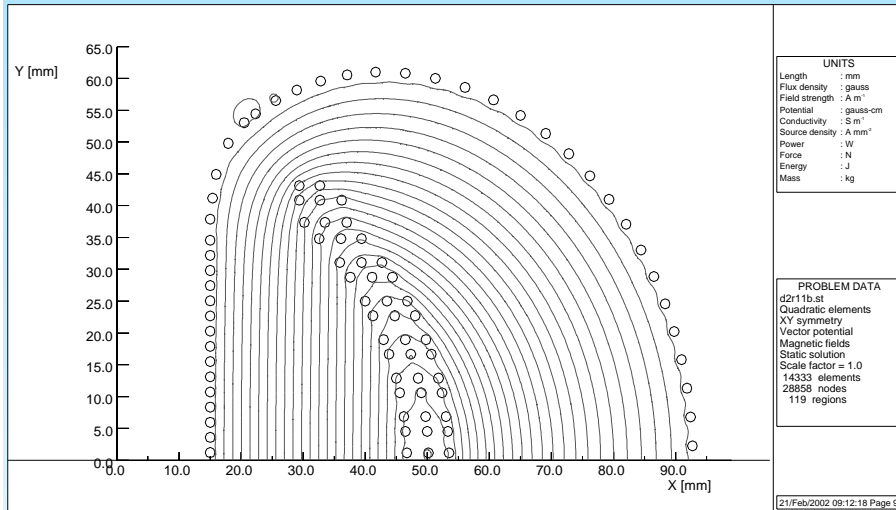
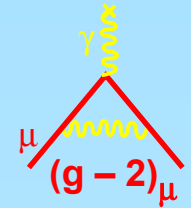


1. AGS Proton Beam 12 – bunches from the AGS 60 Tp total intensity
2.  $0^\circ \pi$  Beam
3.  $\pi$  decay channel
4.  $\mu$  Beam injected into the ring through a superconducting inflector
5. Fast Muon Kicker
6. Precision Magnetic Storage Ring
7. Electron calorimeters, custom high-rate electronics and wave-form digitizers

# The mismatch between the inflector exit and the storage aperture + imperfect kick causes coherent beam oscillations



# The E821 inflector magnet had closed ends which lost half the beam.



Length = 1.7 m

Central field = 1.45 T

Open end prototype, built and tested

→ **X2 Increase in Beam**



The fast kicker is the major new feature not in the CERN experiment. Kicker Modulator is an

