


Physics at Charm Threshold:
Recent Results from CLEO-c & CESR-c
& Prospects for BESIII



David Asner, *Carleton University*
9 Oct 2006, presented at the
4th meeting of
FLAVOUR IN THE ERA OF THE LHC

What We Hope to Learn - I

- Precision CKM
 - Over constrain CKM with results from B-sector
 - Inconsistencies indicate New Physics
 - Precision charm measurements required for precision CKM results in B sector
- **Leptonic Charm Decays $D \rightarrow \ell^+ \nu$: Check QCD calculations including Lattice (LQCD)**
 - Measure decay constants f_D , f_{D^*}
 - Improved f_B possible from f_D measurement + LQCD
 - Important for $|V_{td}|$ and $|V_{ts}|$
- **Semileptonic decay rates & form-factors: Check QCD calculations**
 - Measurements of $|V_{cs}|$ and $|V_{cd}|$
 - Test theoretical form factor models in D meson decays
 - Impacts prediction of form factors for B meson decays
 - Important for $|V_{ub}|$ and $|V_{cb}|$
- **Hadronic Charm Decays**
 - Important for $|V_{cb}|$
 - Engineering numbers useful for other studies
 - B \rightarrow Charm is dominant, so knowing lots about charm is useful, e.g. absolute \mathcal{B} 's, resonant substructure, phases on Dalitz plots, especially versus CP eigenstates
 - Important for β and γ
 - Learn about Strong Interactions, esp. final state interactions
- **Lots of new CLEO-c results. Only time for the high-lights**

What We Hope to Learn - II

- Search for New Physics in Charm Sector
 - Very low SM rates for loop processes provide unique window to observe NP in rare charm processes (rare decays, CPV & mixing)
 - NP can introduce new particles into loop
 - Different sensitivity to NP than B and K sectors
 - Particles & couplings in rare charm processes are NOT the same as in rare B, K
- Rare Charm Decays
 - FCNC decays only occur in loop diagrams in SM: heavily GIM suppressed: $BF(c \rightarrow ull) \sim 10^{-8}$
- Charm Mixing
 - Mixing is Double Cabibbo suppressed & GIM mechanism suppressed
 - In SM $x \equiv \Delta m / \Gamma \lesssim y \equiv \Delta \Gamma / 2\Gamma$
 - Short distance $10^{-6} - 10^{-3}$, Long distance $10^{-3} - 10^{-2}$
 - New physics in loops implies $x \gg y$; long range effects complicate predictions.
 - Large CPV in mixing indicates NP
- CP Violation - Direct
 - CF & DCS decay: Direct CPV requires New Physics
 - Exception: interference between CF & DCS amplitudes to $D^{\pm} \rightarrow K_{S,L} \pi^{\pm}$
 - SM contribution due to K^0 mixing is $A_S = [^+]_S - [^-]_S \sim -3.3 \times 10^{-3}$; $A_S = -A_L$
 - New Physics could be ~%
 - SCS decay
 - expect $O(\lambda^4) \sim 10^{-3}$ from CKM matrix
 - New Physics could be ~%
- No new CLEO-c results. I'll mention prospects for BESIII in conclusion

Absolute Charm Branching Fractions

- $D\bar{D}$ production at threshold: used by Mark III, & more recently by CLEO-c & BESII.

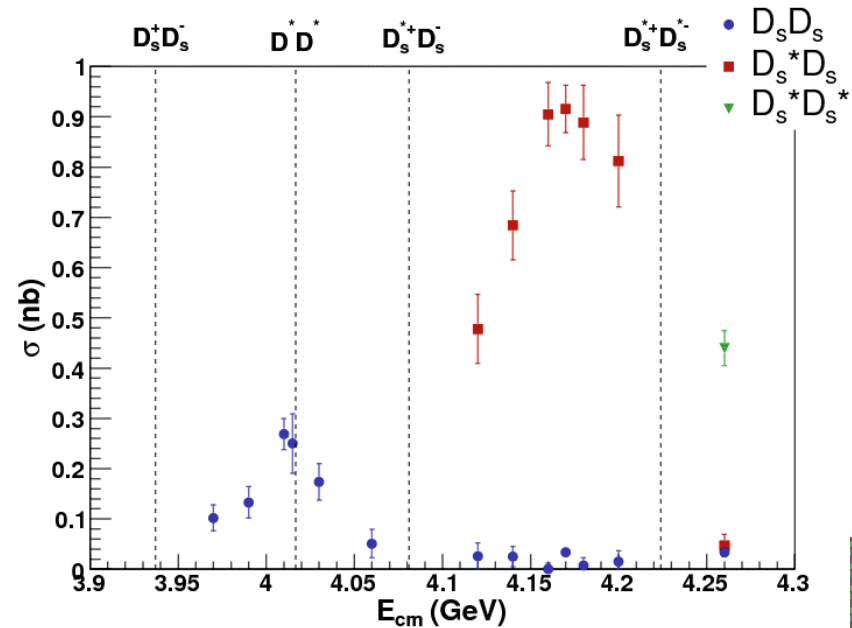
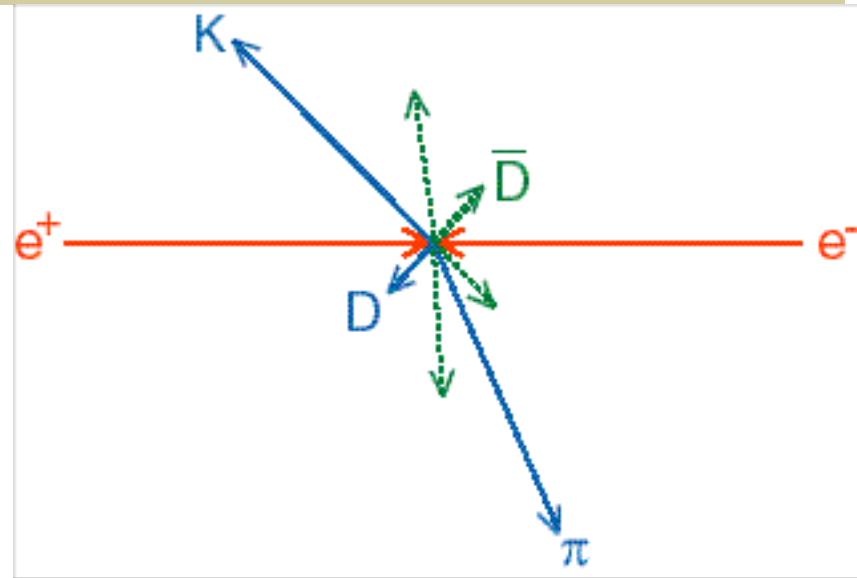
- Unique event properties
 - Only $D\bar{D}$ not $D\bar{D}x$ produced

- Large cross sections:

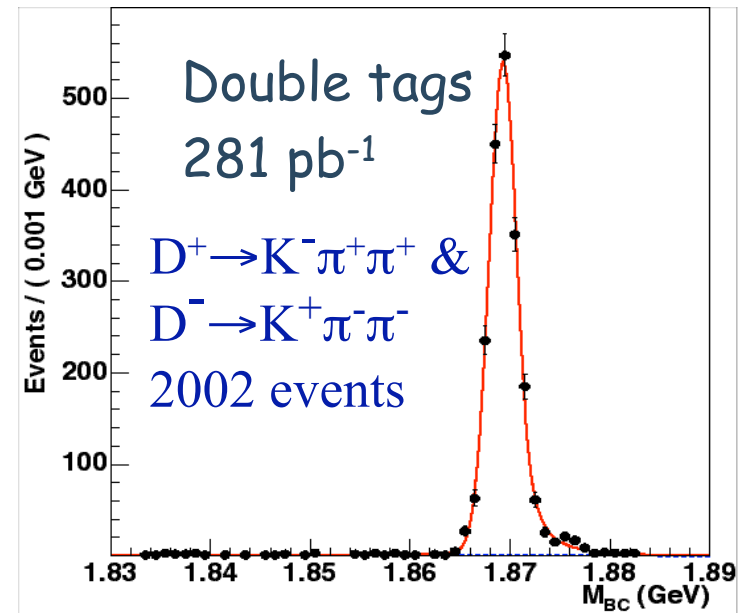
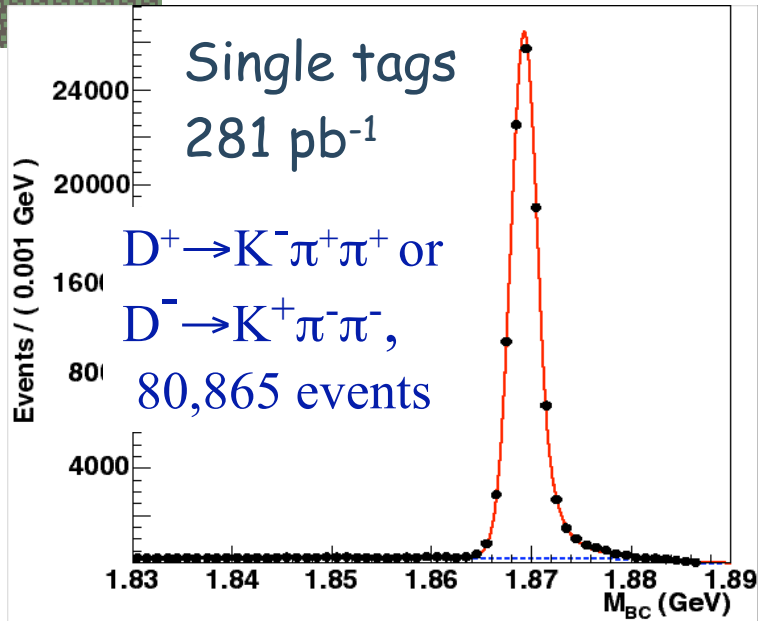
$$\left. \begin{aligned} \sigma(D^0\bar{D}^0) &= 3.72 \pm 0.09 \text{ nb} \\ \sigma(D^+D^-) &= 2.82 \pm 0.09 \text{ nb} \\ \sigma(D_S D_S^*) &= 0.9 \text{ nb} \end{aligned} \right\} \text{World Ave}$$

Continuum $\sim 14 \text{ nb}$

- Ease of B measurements using "double tags"
- $B_A = \# \text{ of } A / \# \text{ of } D's$



$D^+ \rightarrow K^- \pi^+ \pi^+$ at the ψ'' (CLEO-c)

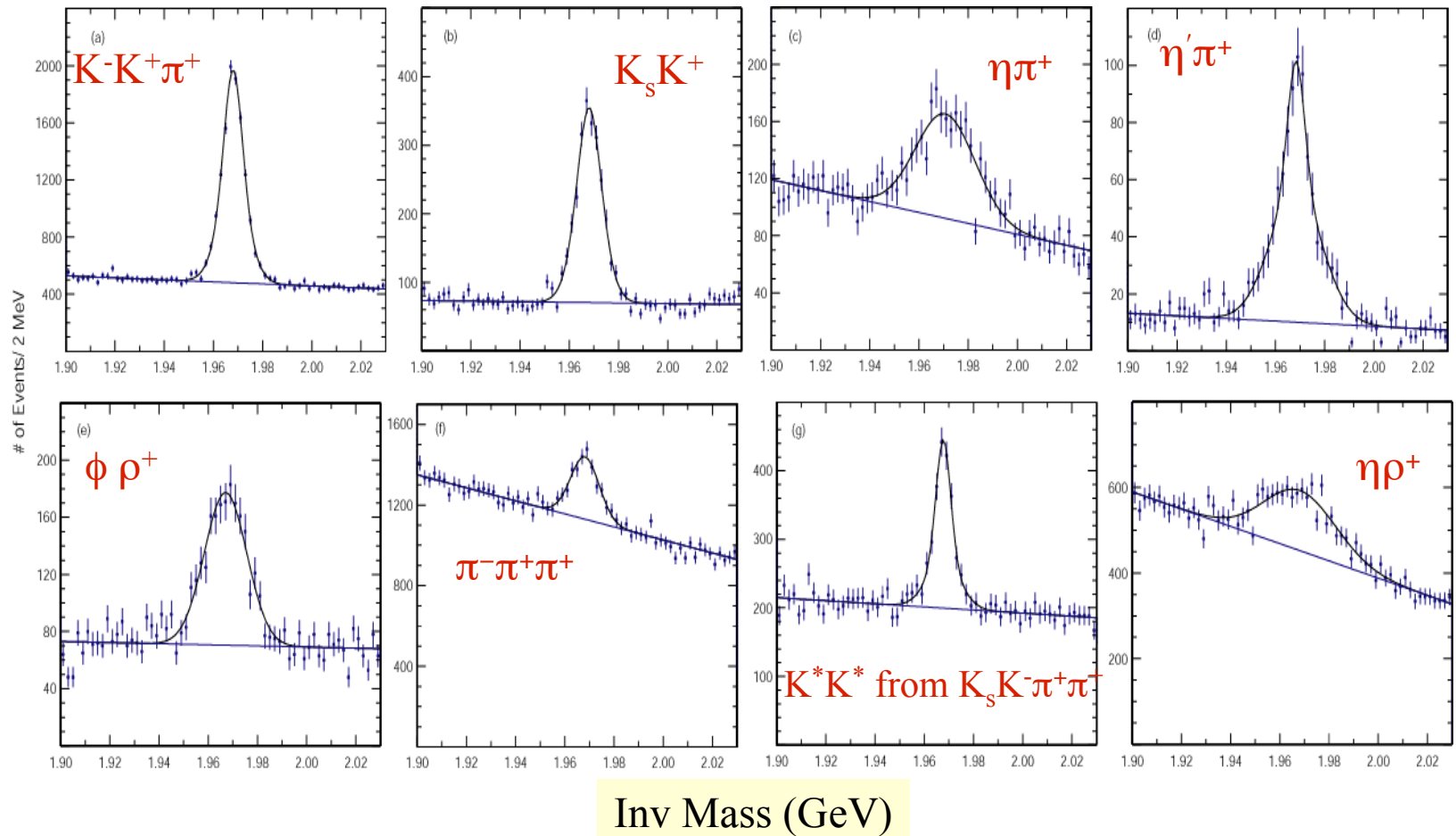


\mathcal{B} (%)	Error(%)	Source
$9.52 \pm 0.25 \pm 0.27$	3.9	CLEO-c (57 pb ⁻¹)
9.2 ± 0.6	6.5	PDG04
9.51 ± 0.34	3.6	PDG06

\mathcal{B} (%)	Error(%)	Source
$3.91 \pm 0.08 \pm 0.09$	3.1	CLEO-c (57 pb ⁻¹)
3.81 ± 0.09	2.4	PDG04
3.80 ± 0.07	1.8	PDG06

For 281pb⁻¹ (systematics limited):
2.2% projected error 1.8% projected error

CLEO-c D_s^+ Results at 4170 MeV



Total # of Tags = 19185 ± 325 (stat)

Single & Double D_S^+ Tags in 200 pb^{-1}

Single tags

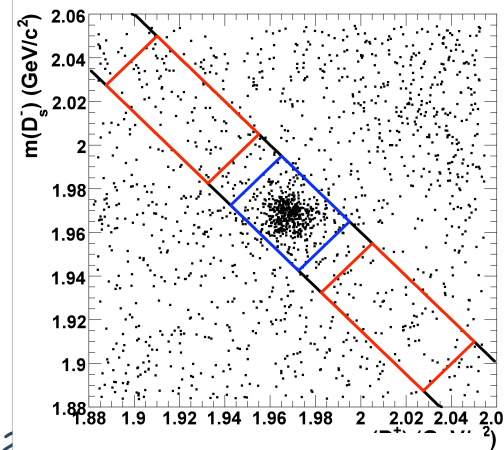
	$K_S K^+$	$K^- K^+ \pi^+$	$K^- K^+ \pi^+ \pi^0$	$\pi^+ \pi^+ \pi^-$	$\pi^+ \eta$	$\pi^+ \eta'$
D_S^+	1054.8 ± 39.4	4315.8 ± 88.8	1159.7 ± 84.5	969.5 ± 79.5	547.0 ± 49.8	361.8 ± 23.4
D_S^-	927.8 ± 37.3	4349.7 ± 88.7	1250.6 ± 84.4	946.7 ± 77.7	569.8 ± 49.7	371.5 ± 23.6

Double tags

	$K_S K^-$	$K^+ K^- \pi^-$	$K^+ K^- \pi^- \pi^0$	$\pi^- \pi^- \pi^+$	$\pi^- \eta$	$\pi^- \eta'$
$K_S K^+$	7.7	27.0	18.7	7.3	4.0	5.0
$K^- K^+ \pi^+$	18.0	104.7	43.7	30.7	12.0	8.0
$K^- K^+ \pi^+ \pi^0$	8.7	35.7	14.0	13.3	1.0	5.7
$\pi^+ \pi^+ \pi^-$	3.3	22.7	16.0	13.3	4.7	4.0
$\pi^+ \eta$	0.0	10.0	2.7	6.0	1.0	1.7
$\pi^+ \eta'$	3.0	10.0	3.0	3.7	1.0	0.0

Clean double tag signal

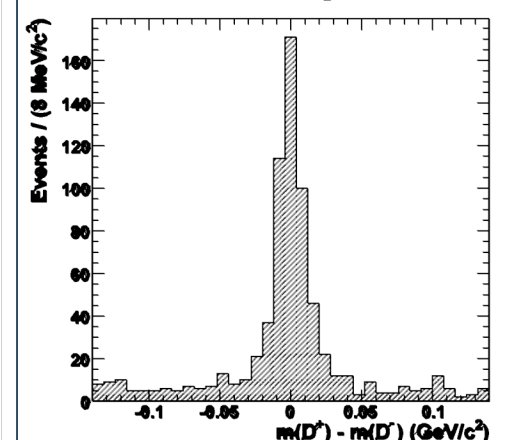
mass D_S^- (GeV)



9 Oct 2000

mass D_S^+ (GeV)

All double tags

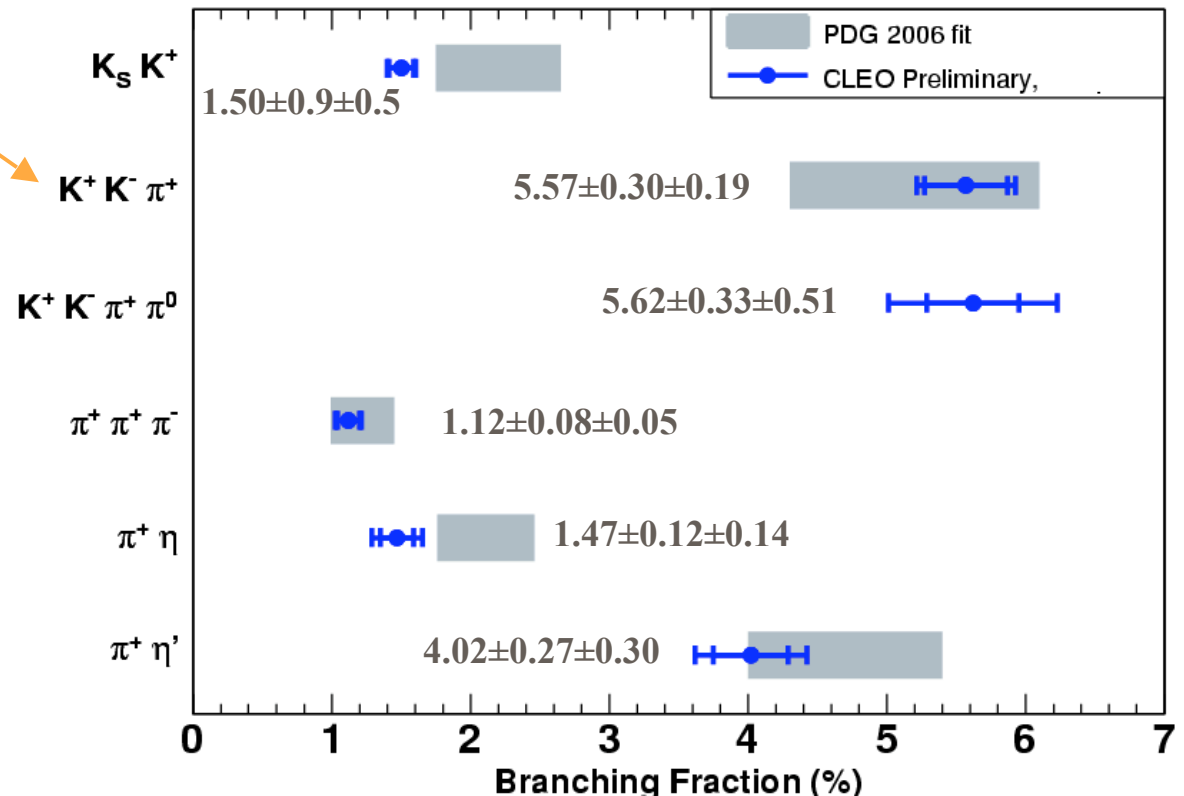
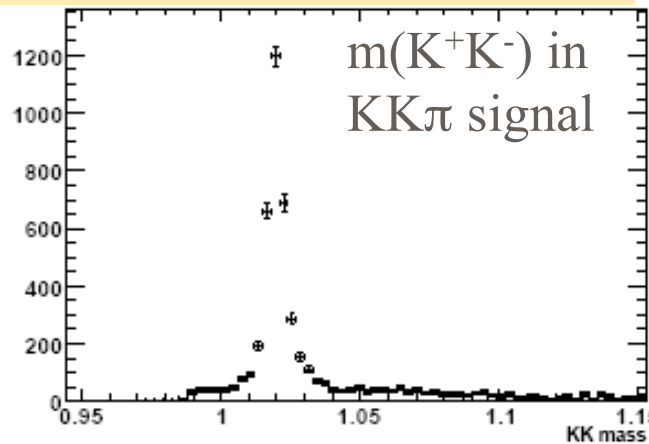


mass D_S^+ - mass D_S^-

David Asner

Absolute \mathcal{B} Results for D_S^+ 200 pb $^{-1}$

- About $\pm 6\%$ error
- $D_S \rightarrow \phi \pi^+$ is difficult to quote because of interferences in $KK\pi$ Dalitz plot - K^*K , $f_0 \pi$, etc...



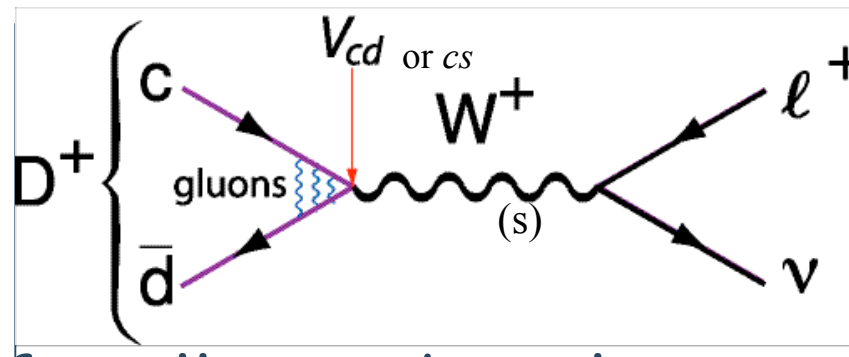
- Partial branching fraction ± 10 MeV around $m(\phi)$: $1.98 \pm 0.12 \pm 0.09$ %
- ± 20 MeV around $m(\phi)$: $2.25 \pm 0.13 \pm 0.12$ % (need x2 for $\phi \rightarrow K^+K^-$)

Leptonic Decays: $D_{(s)} \rightarrow \ell^+ \nu$

Introduction: Pseudoscalar decay constants

c and q can annihilate, probability is \propto to wave function overlap

Example :



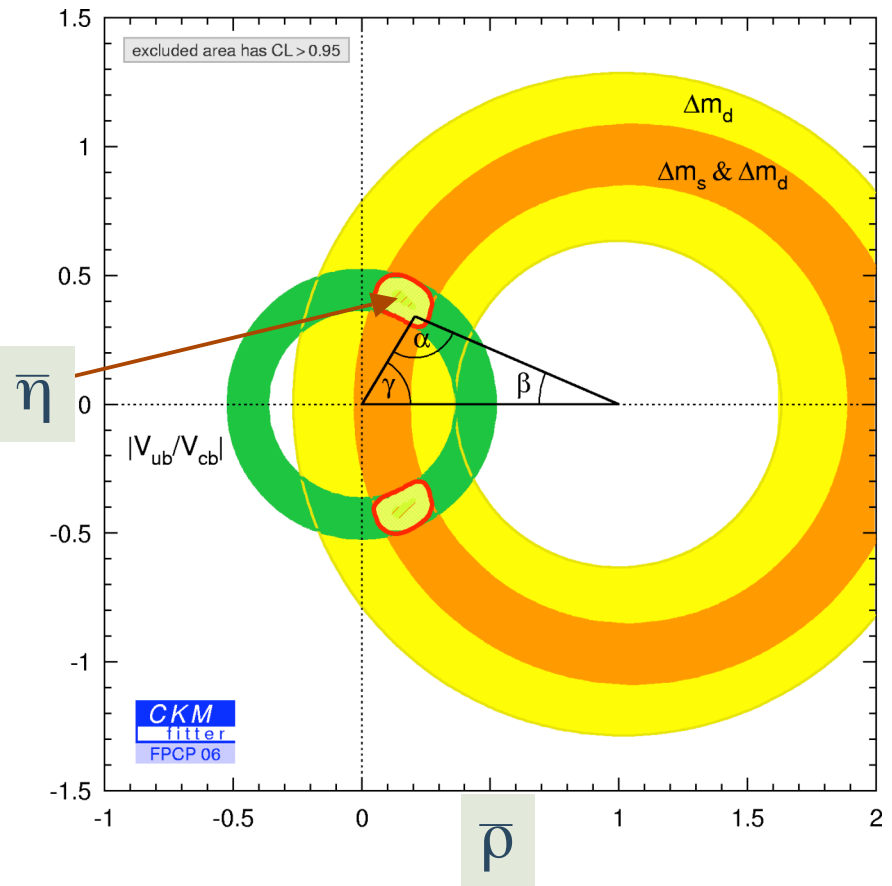
In general for all pseudoscalars:

$$\Gamma(P^+ \rightarrow \ell^+ \nu) = \frac{1}{8\pi} G_F^2 f_P^2 m_\ell^2 M_P \left(1 - \frac{m_\ell^2}{M_P^2}\right)^2 |V_{Qq}|^2$$

Calculate, or measure if V_{Qq} is known

Goals in Leptonic Decays

- Test theoretical calculations in strongly coupled theories in non-perturbative regime
- f_B & f_{B_s}/f_B needed to improve constraints from Δm_d & $\Delta m_s/\Delta m_d$. Hard to measure directly (i.e. $B \rightarrow \tau^+ \nu$ measures $V_{ub} f_B$), but we can determine f_D & f_{D_s} using $D \rightarrow \ell^+ \nu$ and use them to test theoretical models (i.e. Lattice QCD)



Constraints from V_{ub} , Δm_d , Δm_s & $B \rightarrow \tau^+ \nu$

New Measurements of f_{D_S}

- Two separate techniques
 - (1) Measure $D_S^+ \rightarrow \mu^+ \nu$ along with $D_S \rightarrow \tau^+ \nu$, $\tau \rightarrow \pi^+ \nu$.
 - Requires finding a D_S^- tag, a γ from either $D_S^{*-} \rightarrow \gamma D_S^-$ or $D_S^{*+} \rightarrow \gamma \mu^+ \nu$. Then finding the muon or pion using kinematical constraints
 - (2) Find $D_S^+ \rightarrow \tau^+ \nu$, $\tau \rightarrow e^+ \nu \nu$ opposite a D_S^- tag

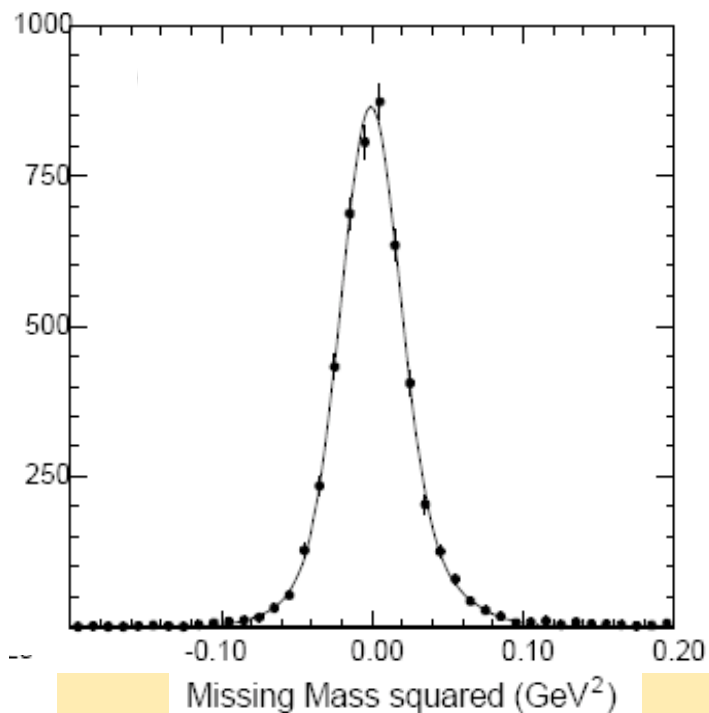
(1) Measurement of $D_S^+ \rightarrow \mu^+ \nu$

- Use $D_S^* D_S$ events with detected γ from $D_S^* \rightarrow \gamma D_S$ decay
- Reconstruct all particles from $e^+ e^- \rightarrow D_S^* D_S, \gamma, D_S$ (tag) + μ^+ except for the ν
- Kinematic fit (i) improves resolution & (ii) remove ambiguities
 - Constraints include: total p & E, tag D_S mass, $\Delta m = M(\gamma D_S) - M(D_S)$ [or $\Delta m = M(\gamma \mu \nu) - M(\mu \nu)$] = 143.6 MeV, E of D_S (or D_S^*) fixed
 - Lowest χ^2 solution in each event is kept. No χ^2 cut is applied

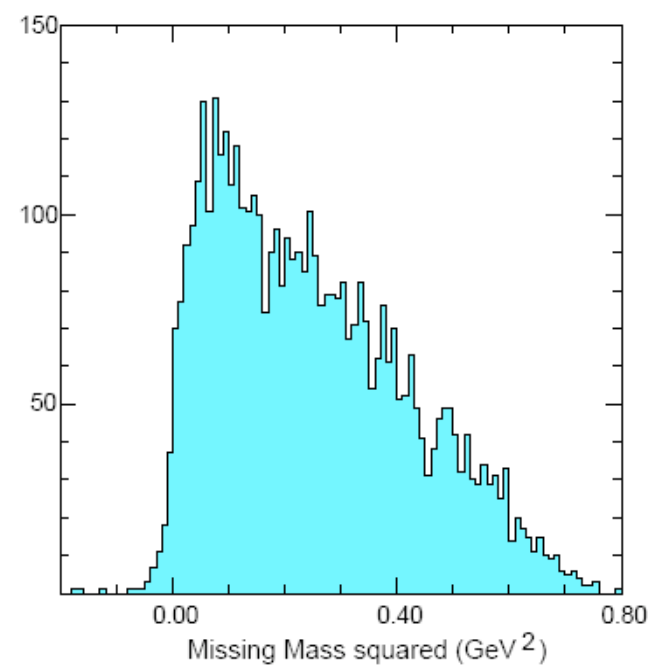
The MM^2

- To find the signal events, we compute

$$MM^2 = \left(E_{cm} - E_{D_s} - E_{\gamma} - E_{\mu} \right)^2 - \left(-\vec{p}_{D_s} - \vec{p}_{\gamma} - \vec{p}_{\mu} \right)^2$$



Signal $\mu\nu$



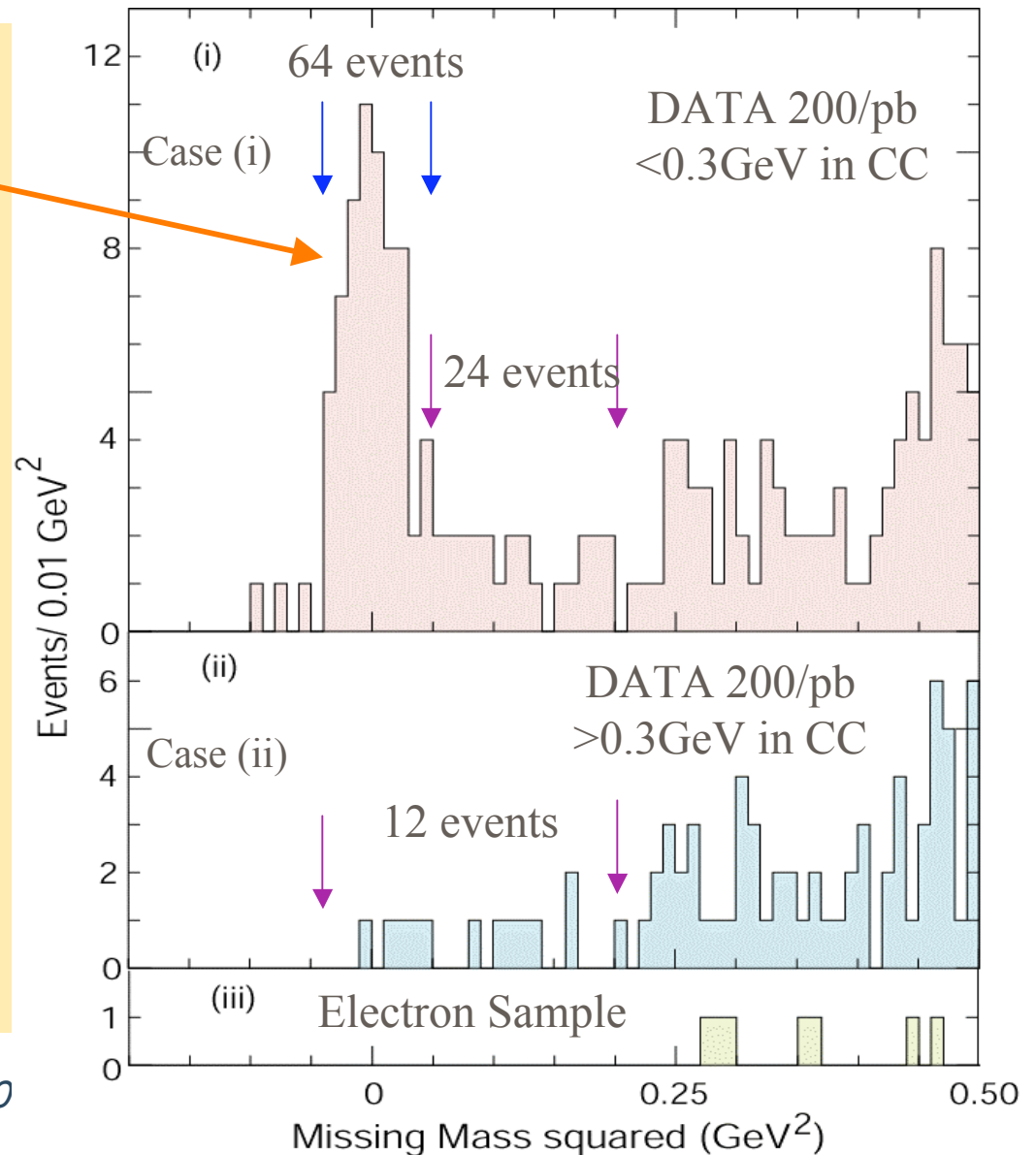
Signal $\tau\nu, \tau \rightarrow \pi\nu$

Define Three Classes

- Class (i), single track deposits < 300 MeV in calorimeter (consistent with μ) & no other $\gamma > 300$ MeV. (accepts 99% of muons and 60% of kaons & pions)
- Class (ii), single track deposits > 300 MeV in calorimeter & no other $\gamma > 300$ MeV (accepts 1% of muons and 40% of kaons & pions)
- Class (iii) single track consistent with electron & no other $\gamma > 300$ MeV

MM² Results from 200 pb⁻¹

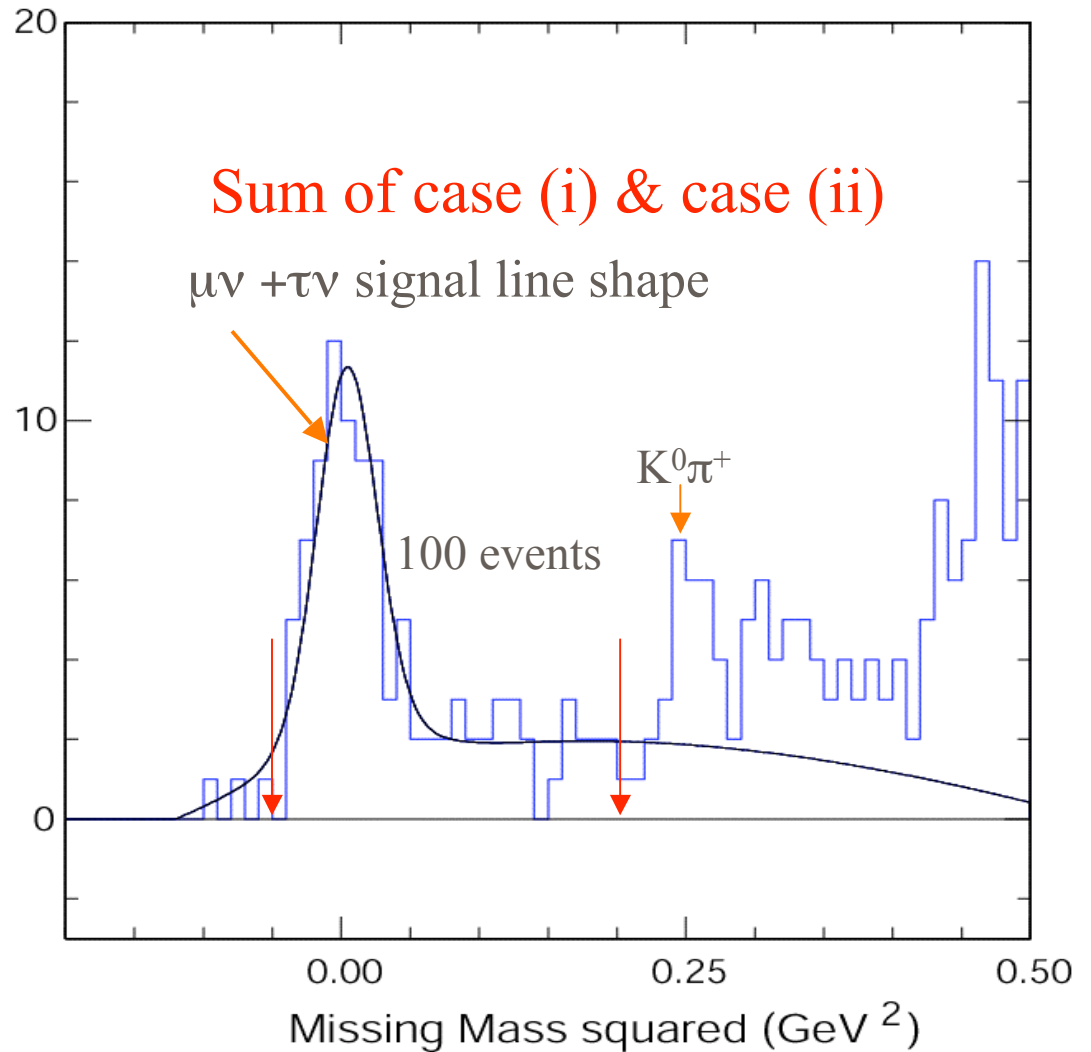
- Clear $D_S^+ \rightarrow \mu^+ \nu$ signal for case (i)
- Will show that events $< 0.2 \text{ GeV}^2$ are mostly $D_S \rightarrow \tau^+ \nu$, $\tau \rightarrow \pi^+ \nu$ in cases (i) & (ii)
- No $D_S \rightarrow e^+ \nu$ seen, case (iii)



Sum of $D_S^+ \rightarrow \mu^+ \nu + \tau^+ \nu, \tau \rightarrow \pi^+ \nu$

Two sources of background

- A) Backgrounds under invariant mass peaks - Use sidebands to estimate
 - In $\mu^+ \nu$ signal region 2 background (64 signal)
 - Sideband bkgd 5.5 ± 1.9
- B) Backgrounds from real D_S decays, e.g.
 - $\pi^+ \pi^0 \pi^0$, or $D_S \rightarrow \tau^+ \nu, \tau \rightarrow \pi^+ \pi^0 \nu$... with $MM^2 < 0.2 \text{ GeV}^2$
 - none in $\mu \nu$ signal region.
 - Total of 1.3 additional events.
 - $B(D_S \rightarrow \pi^+ \pi^0) < 1.1 \times 10^{-3} < 0.1 \text{ evts}$
- Total background $< 0.2 \text{ GeV}^2$ is 6.8 events, out of the 100

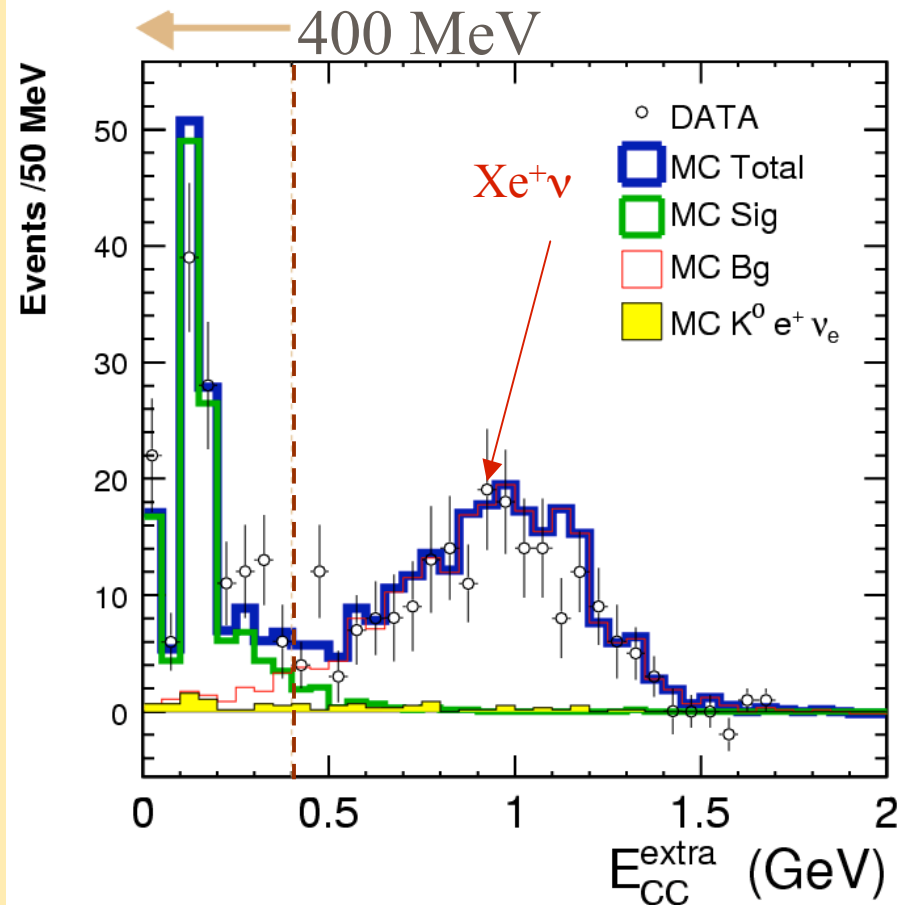


Branching Ratio & Decay Constant

- $D_S^+ \rightarrow \mu^+ \nu$
 - 64 signal events, 2 background, use SM to calculate $\tau \nu$ yield near 0 MM^2 based on known $\tau \nu / \mu \nu$ ratio
 - $B(D_S^+ \rightarrow \mu^+ \nu) = (0.657 \pm 0.090 \pm 0.028)\%$
- $D_S^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow \pi^+ \nu$
 - Sum case (i) $0.2 > MM^2 > 0.05 \text{ GeV}^2$ & case (ii) $MM^2 < 0.2 \text{ GeV}^2$. Total of 36 signal and 4.8 bkgrnd
 - $B(D_S^+ \rightarrow \tau^+ \nu) = (7.1 \pm 1.4 \pm 0.03)\%$
- By summing both cases above, find
$$B^{\text{eff}}(D_S^+ \rightarrow \mu^+ \nu) = (0.664 \pm 0.076 \pm 0.028)\%$$
- $f_{D_S} = 282 \pm 16 \pm 7 \text{ MeV}$
- $B(D_S^+ \rightarrow e^+ \nu) < 3.1 \times 10^{-4}$

Measuring $D_S^+ \rightarrow \tau^+ \nu$, $\tau^+ \rightarrow e^+ \nu \nu$

- $B(D_S^+ \rightarrow \tau^+ \nu) \cdot B(\tau^+ \rightarrow e^+ \nu \nu) \sim 1.3\%$ is "large" compared with expected $B(D_S^+ \rightarrow X e^+ \nu) \sim 8\%$
- Technique is to find events with an e^+ opposite D_S^- tags & no other tracks, with Σ calorimeter energy < 400 MeV
- No need to find γ from D_S^*
- $B(D_S^+ \rightarrow \tau^+ \nu) = (6.29 \pm 0.78 \pm 0.52)\%$
- $f_{D_S} = 278 \pm 17 \pm 12$ MeV



f_{D_s} & f_{D_s}/f_D

- **Weighted Average:** $f_{D_s} = 280.1 \pm 11.6 \pm 6.0$ MeV, the systematic error is mostly uncorrelated between the measurements (*More data is on the way & systematic errors are being addressed*)

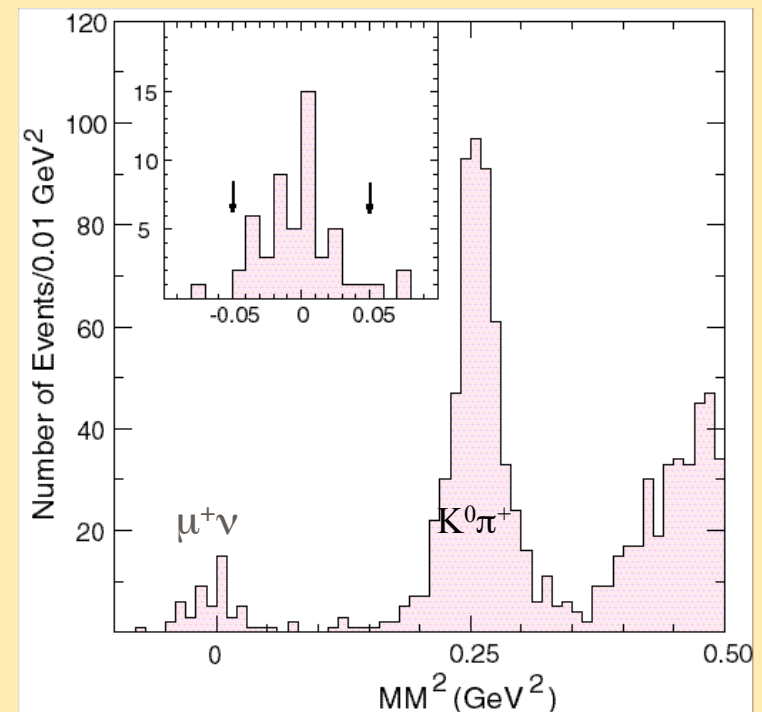
- Previously CLEO-c measured

[†]M. Artuso et al., Phys. Rev. Lett. 95 (2005) 251801

$$f_{D^+} = (222.6 \pm 16.7^{+2.3}_{-3.4}) \text{ MeV}^{\dagger}$$

- Thus $f_{D_s}/f_{D^+} = 1.26 \pm 0.11 \pm 0.03$
- $\Gamma(D_s^+ \rightarrow \tau^+ \nu) / \Gamma(D_s^+ \rightarrow \mu^+ \nu) = 9.9 \pm 1.7 \pm 0.7$, SM = 9.72, consistent with lepton universality

$D^+ \rightarrow \mu^+ \nu$



Comparisons with Theory

- Consistent with most models, more precision needed
- Using Lattice ratio find $|V_{cd}/V_{cs}| = 0.22 \pm 0.03$
- CLEO-c is most precise result to date for both f_{D_s} & f_{D^+}

CLEO preliminary

Lattice

PRL95,122002(2005)

QL (Taiwan)

PLB624,31(2005)

QL (UKQCD)

PRD64,094501(2001)

QL 23

PRD60,074501(1999)

QCD SR

hep-ph/0507241

QCD SR

hep-ph/0202200

Quark Model

PLB635,93(2006)

Quark Model

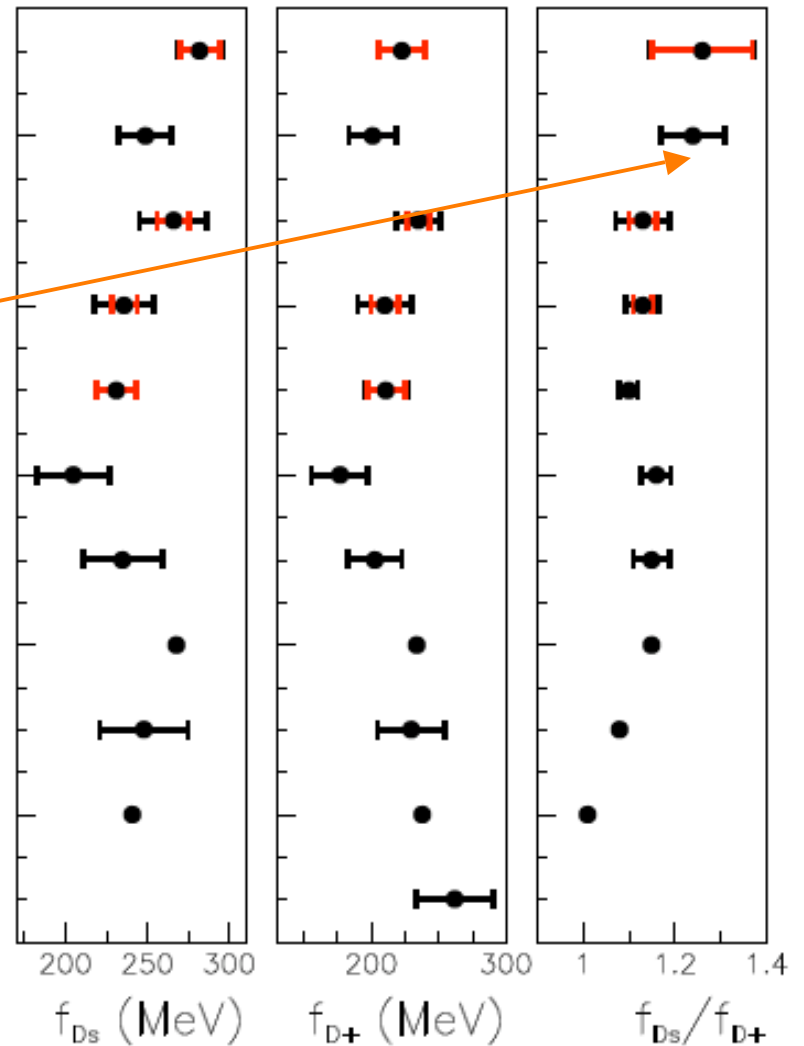
PLB596,84(2004)

Potential Model

Braz.J.Phys.34,297(2004)

Isospin Splittings

PRD47,3059(2004)

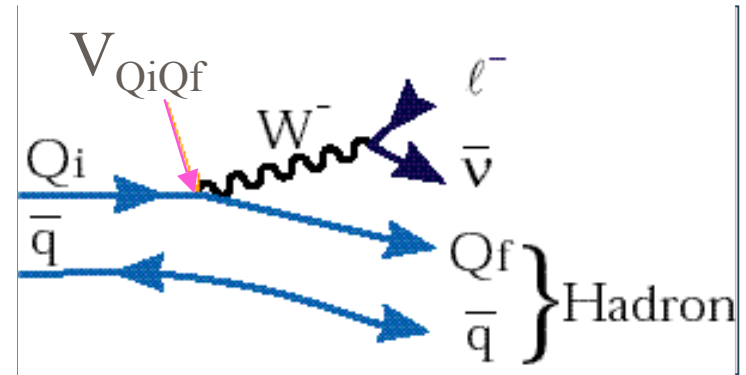


Goals in Semileptonic Decays

- Either take V_{cq} from other information & test theory, or use theory & measure V_{cq}
 - V_{cs} use $D \rightarrow K(K^*)l\nu$ to measure form-factor shapes to distinguish among models & test lattice QCD predictions
 - V_{cd} use $D \rightarrow \pi(\rho)l\nu$
- V_{cd} & V_{cs} with precise unquenched lattice calc + V_{cb} would provide an important unitarity check
- Use $D \rightarrow \pi l\nu$ (& $\rho l\nu$) to get form-factor for $B \rightarrow \pi l\nu$ (& $\rho l\nu$) and use HQET to get V_{ub}

Exclusive Semileptonic Decays

- ◆ Best way to determine magnitudes of CKM elements, in principle is to use semileptonic decays. Decay rate $\propto |V_{Q_i Q_f}|^2$



- ◆ How $V_{us}(\lambda)$ and $V_{cb}(A)$ have been determined

- ◆ Kinematics: $q^2 = (p_D^\mu - p_{hadron}^\mu)^2 = m_D^2 + m_P^2 - 2E_P m_D$

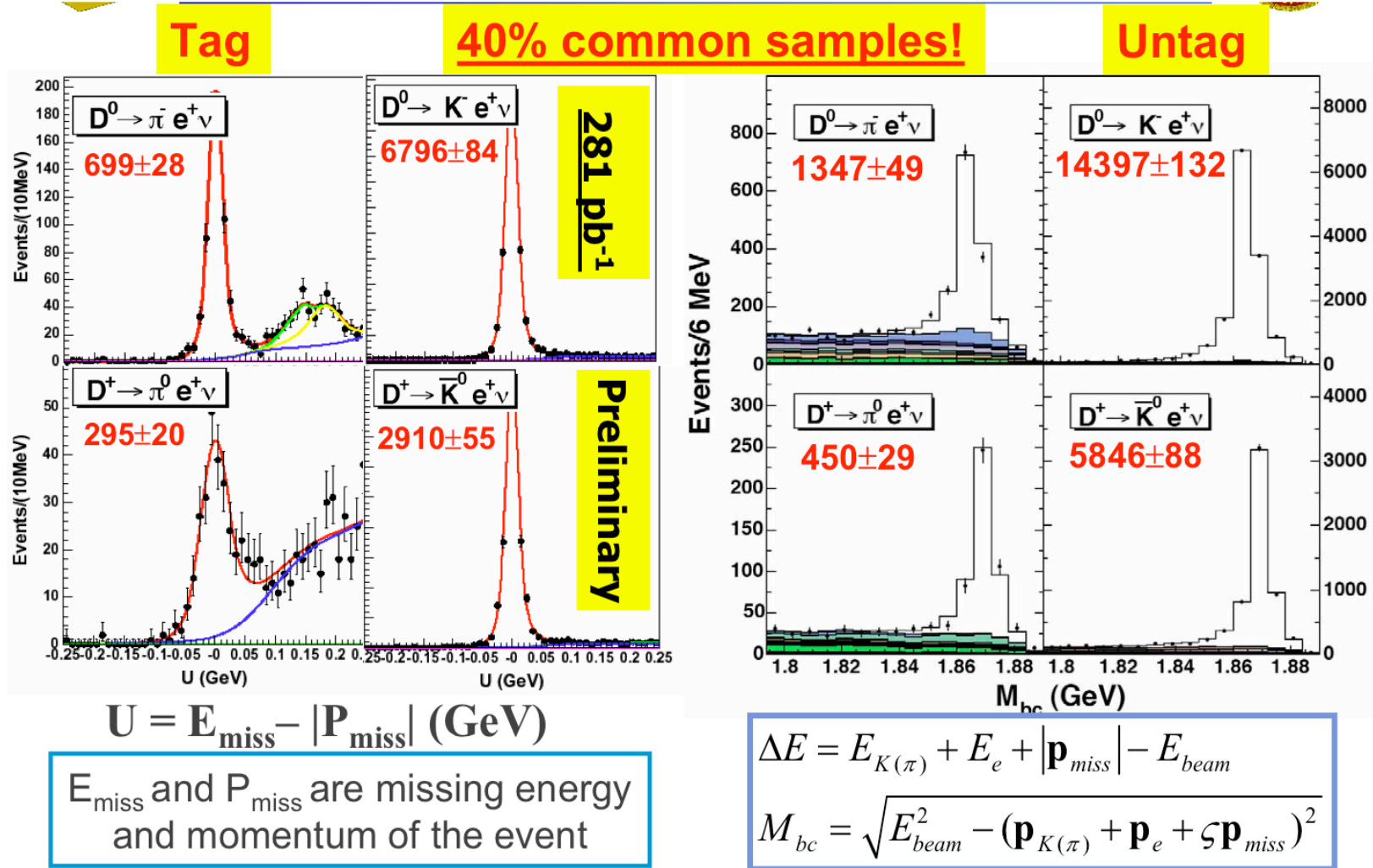
- ◆ Matrix element in terms of form-factors (for $D \rightarrow$ Pseudoscalar $l + \nu$)

$$\langle P(P_P) | J_\mu | D(P_D) \rangle = f_+(q^2)(P_D + P_P)_\mu + f_-(q^2)(P_D - P_P)_\mu$$

- ◆ For $\lambda = e$, $f_-(q^2) \rightarrow 0$:

$$\frac{d\Gamma(D \rightarrow P e \nu)}{dq^2} = \frac{|V_{cq}|^2 P_P^3}{24\pi^3} |f_+(q^2)|^2$$

$D^0/D^+ \rightarrow K/\pi e \nu$ Tag & Untag



$D^0/D^+ \rightarrow K/\pi e \nu$ BF (Tag & Untag)

40% common samples, do NOT average them!

D Decay	Tag	Br. Frac. (%)	Untag	PDG (%)
$D^0 \rightarrow K^- e^+ \nu$	$3.58 \pm 0.05 \pm 0.05$	$3.56 \pm 0.03 \pm 0.11$		3.62 ± 0.16
$D^0 \rightarrow \pi^- e^+ \nu$	$0.309 \pm 0.012 \pm 0.006$	$0.301 \pm 0.011 \pm 0.010$		0.311 ± 0.030
$D^+ \rightarrow \bar{K}^0 e^+ \nu$	$8.86 \pm 0.17 \pm 0.20$	$8.75 \pm 0.13 \pm 0.30$		7.2 ± 0.8
$D^+ \rightarrow \pi^0 e^+ \nu$	$0.397 \pm 0.027 \pm 0.028$	$0.383 \pm 0.025 \pm 0.016$		0.38 ± 0.19

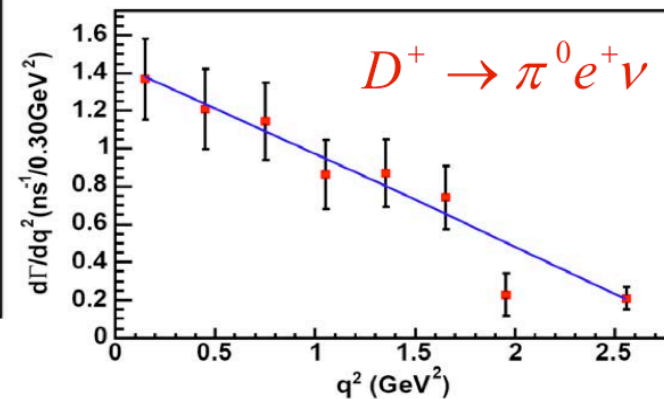
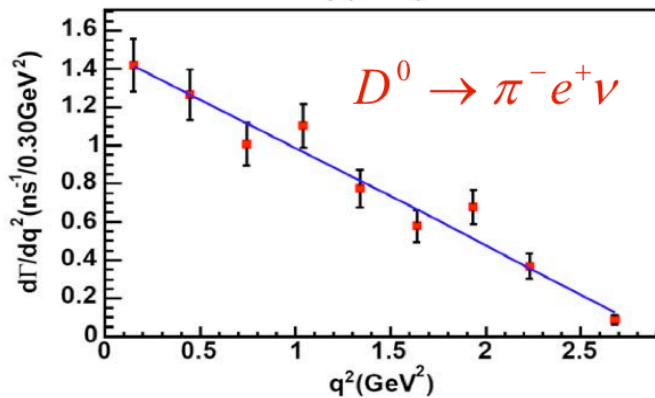
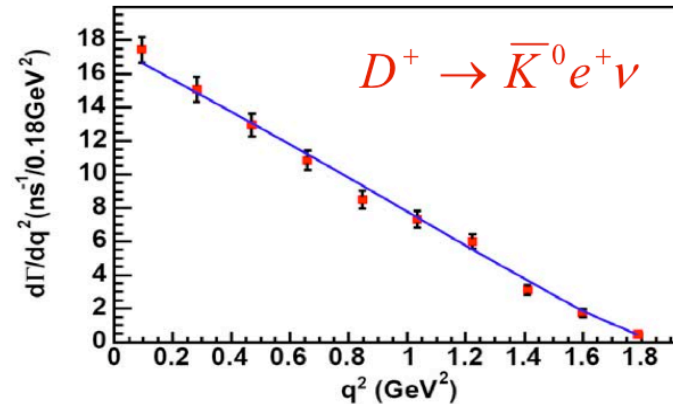
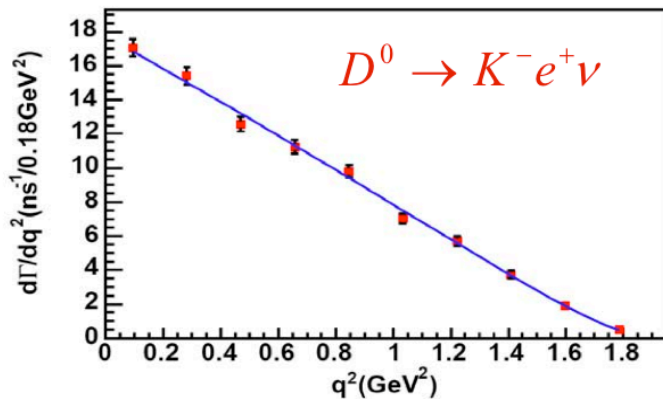
281 pb⁻¹

Ratio	Measured (%)	PDG (%)	Ratio	Measured
$\frac{D^0 \rightarrow \pi^- e^+ \nu}{D^0 \rightarrow K^- e^+ \nu}$	$8.5 \pm 0.3 \pm 0.1$	8.6 ± 0.7	$\frac{\Gamma(D^0 \rightarrow \pi^- e^+ \nu)}{\Gamma(D^+ \rightarrow \pi^0 e^+ \nu)}$	$1.95 \pm 0.15 \pm 0.14$ $1.99 \pm 0.15 \pm 0.10$
$\frac{D^+ \rightarrow \pi^0 e^+ \nu}{D^+ \rightarrow \bar{K}^0 e^+ \nu}$	$4.4 \pm 0.3 \pm 0.1$	$4.6 \pm 1.4 \pm 1.7$	$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu)}$	$1.02 \pm 0.02 \pm 0.02$ $1.03 \pm 0.02 \pm 0.04$

Preliminary

Form Factor Fit (Tag)

Preliminary



281 pb⁻¹ at $\Psi(3770)$

Simple Pole Model

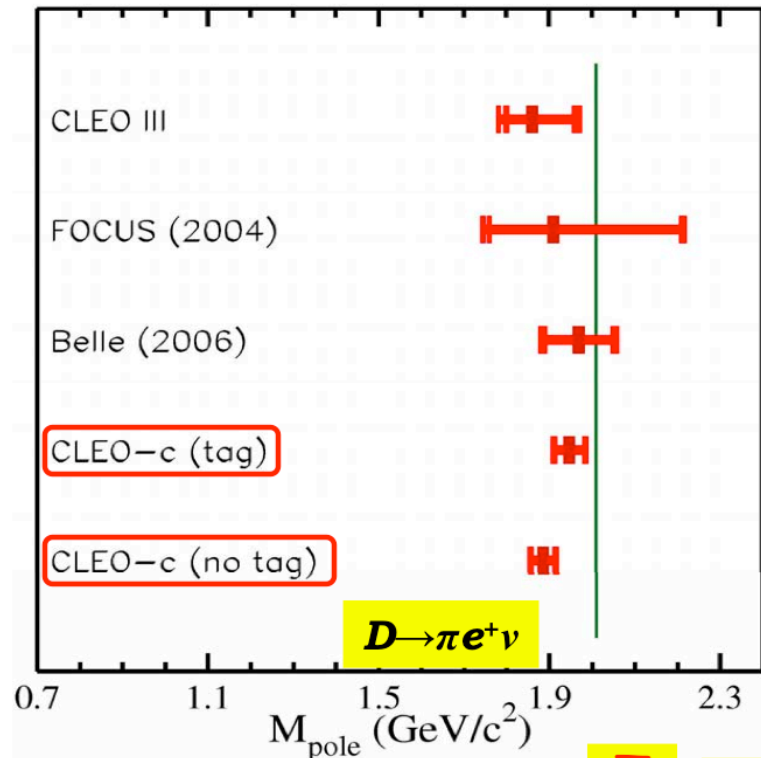
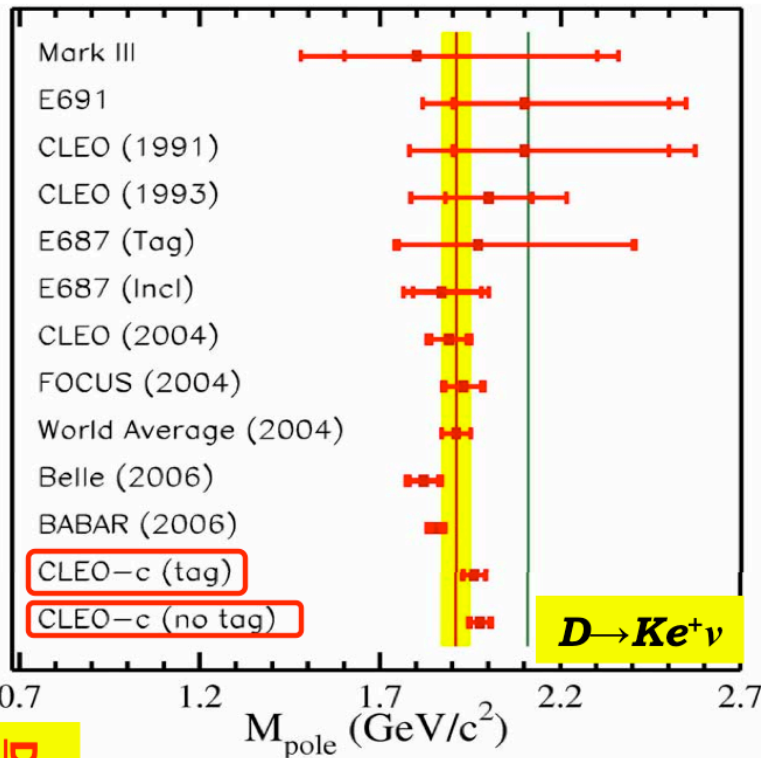
$$f^+(q^2) = \frac{f^+(0)}{(1 - q^2/m_{pole}^2)}$$

Modified Pole Model

$$f^+(q^2) = \frac{f^+(0)}{(1 - q^2/m_{pole}^2)(1 - \alpha q^2/m_{pole}^2)}$$

Hill series expansion (Phys. Lett. B 633, 61 (2006))

Form Factors (Tag/Untag)



Don't average!

Decay Mode	M _{pole} (Tag)	M _{pole} (Untag)
$D \rightarrow Ke\nu$ (av. D^0 & D^+)	$1.96 \pm 0.03 \pm 0.01$	$1.98 \pm 0.03 \pm 0.02$
$D \rightarrow \pi e\nu$ (av. D^0 & D^+)	$1.95 \pm 0.04 \pm 0.02$	$1.88 \pm 0.03 \pm 0.02$

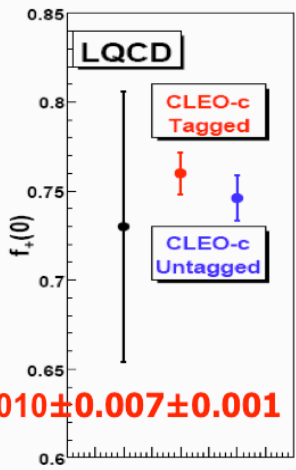
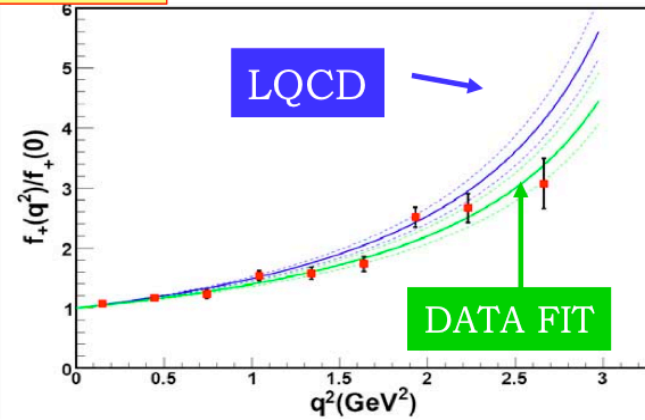
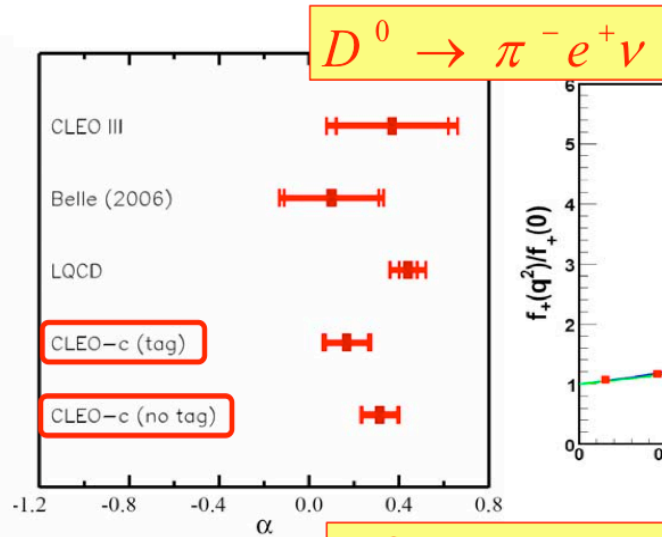
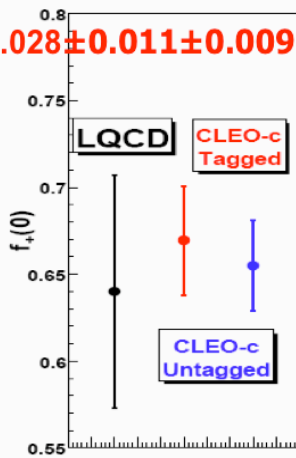
Preliminary

281 pb⁻¹

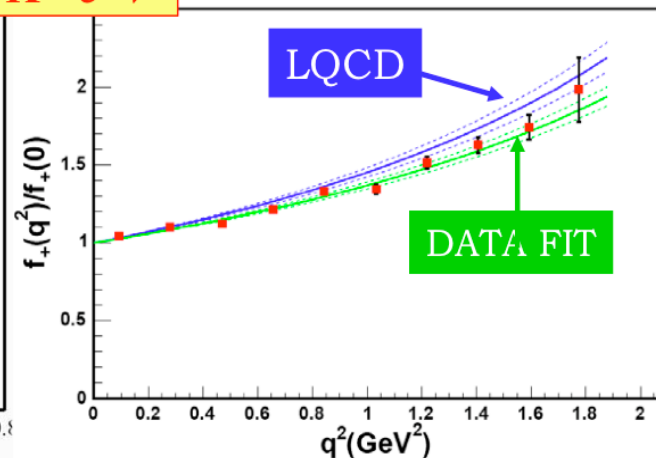
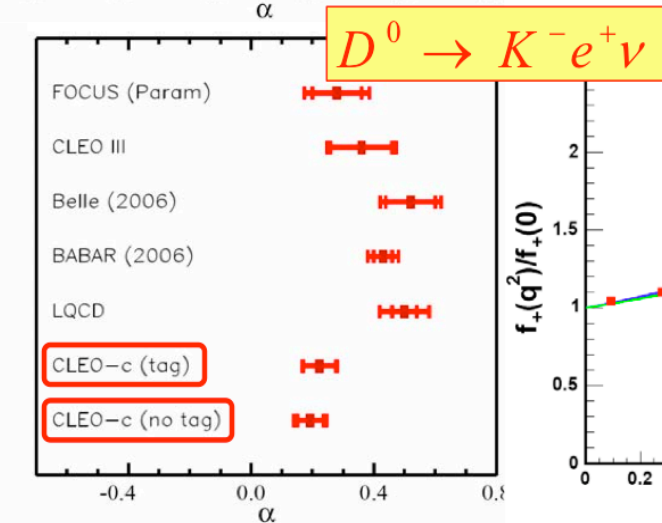
Form Factors & Test of LQCD

$0.670 \pm 0.028 \pm 0.011 \pm 0.009$

281 pb⁻¹ Preliminary



$0.760 \pm 0.010 \pm 0.007 \pm 0.001$



V_{cs} and V_{cd} Results

Combine $|V_{cx}|f_+(0)$ values from fits with unquenched LQCD results for $f_+(0)$
 (Phys. Rev. Lett. 94, 011601 (2005)) to extract $|V_{cs}|$ and $|V_{cd}|$.

Decay Mode	$ V_{cx} \pm (\text{stat}) \pm (\text{syst}) \pm (\text{theory})$	PDG Value
$D \rightarrow \pi e \nu$ (tag)	$0.234 \pm 0.010 \pm 0.004 \pm 0.024$	
$D \rightarrow \pi e \nu$ (untag)	$0.229 \pm 0.007 \pm 0.005 \pm 0.024$	0.224 ± 0.012
$D \rightarrow K e \nu$ (tag)	$1.014 \pm 0.013 \pm 0.009 \pm 0.106$	
$D \rightarrow K e \nu$ (untag)	$0.996 \pm 0.008 \pm 0.015 \pm 0.104$	0.976 ± 0.014

Preliminary

Tag/Untag: 40% of comment sample. **DO NOT AVERAGE!!!**
 Expt. uncertainties $V_{cs} < 2\%$ $V_{cd} \sim 4\%$ LQCD uncertainty 10%

Since V_{cs} ($W \rightarrow cs$ LEP) and V_{cd} (νN) are well measured, good agreement between PDG and CLEO-c results is primarily a check of the LQCD value for $f_+(0)$. Nevertheless, the most precise & robust V_{cs} & V_{cd} determinations using semileptonic decays to date.

Looking forward to 2010

Where will Charm physics be in 2010?

- Hadronic Branching Ratios
 - D^0 and D^+ branching ratios systematics limited at (1-2)% **CLEO-c**
 - D_s^+ branching ratios statistics limited at 6% **CLEO-c**
 - **CLEO-c** will improve to ~4%
 - **BESIII** will improve to (1-2)%
- Decay constants: statistics limited
 - D^+ 7.5% for 281 pb^{-1} at 3770. **CLEO-c**
 - **CLEO-c** will improve to (4-5)%
 - **BESIII** will improve to (1-2)%
 - Ultimate systematic limit may be ~1%
 - D_s 4.1% for 200 pb^{-1} at 4170. **CLEO-c**
 - **CLEO-c** will improve to (2-3)%
 - **BESIII** can improve
 - Ultimate systematic limit may be ~2%
- Semileptonic Decays
 - Branching ratio of Cabibbo favored $D^0 \rightarrow K e \nu$ known to 2% **CLEO-c**
 - Branching ratio of Cabibbo suppressed $D^0 \rightarrow \pi e \nu$ known to 4% **CLEO-c**
 - **CLEO-c** will improve to (2-3)%
 - **BESIII** can improve
 - Ultimate systematics limit for Semileptonic BR may be 1-2%
 - $V_{cs} \sim 2\%$, $V_{cd} \sim 4\%$ **CLEO-c**
 - **CLEO-c** will improve $V_{cd} \sim 2\%$

- CP tagged Dalitz plot analyses e.g. $D^0 \rightarrow CP$ vs. $D^0 \rightarrow K_S \pi^+ \pi^-$ **Important for γ**
 - Statistics starved until at least $\sim 10 \text{ fb}^{-1}$
 - **CLEO-c** can limit sys err on $\gamma < 3^\circ$
- Rare Decays
 - **CLEO-c** sensitivity 10^{-5} - 10^{-6}
 - **BESIII** sensitivity 10^{-6} - 10^{-7}
 - Standard Model rates $\sim 10^{-8}$
 - **Need Super Flavor Factory @ $\sim 4 \text{ GeV}$**
- Charm Mixing
 - Exploiting the quantum coherent initial state **CLEO-c** will measure $\cos \delta \sim \pm 0.1$
 - **BESIII** sensitivity to $\gamma = \Delta\Gamma/2\Gamma \sim \text{few} \times 10^{-3}$
 - **Need (Upgraded) LHC-b or Super B** to cover full range of SM expectations
- CP Violation
 - **BESIII** sensitive to asymmetry in $D^+ \rightarrow K_{S,L} \pi^+$ $\sim \text{few} \times 10^{-3}$. Approximately SM expectation.
 - **Need (Upgraded) LHC-b or Super B** to reach SM expectation in SCS decays.

CLEO-c will complete most measurements needed for precision CKM. New Physics searches require more statistics than anticipated at **BESIII**

The End



Form-Factor Parameterizations

- In general

$$f_+(q^2) = \frac{f_+(0)}{1-\alpha} \frac{1}{1-q^2/m_{pole}^2} + \frac{1}{\pi} \int_{(M_D+m)^2}^{\infty} dq'^2 \frac{\text{Im}(f(q'^2))}{q'^2 - q^2}$$

- Modified Pole

$$f_+(q^2) = \frac{f_+(0)}{\left(1 - q^2/m_{pole}^2\right)\left(1 - \alpha q^2/m_{pole}^2\right)}$$

- Series Expansion

$$f_+(q^2) = \frac{1}{P(q^2)\phi(q^2, t_0)} \sum_{k=0}^{\infty} a_k(t_0) [z(q^2, t_0)]^k$$

$$t_{\pm} \equiv \left(M_D \pm m_{\pi(K)}\right)^2, \quad z(q^2, t_0) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$

Hill & Becher, Phys. Lett. B 633, 61 (2006)