

Quantum Coherence and Charm

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*Full disclosure: member of
CLEO-c / BESIII / Belle II



**Quantum coherence analyses
allow us to form a more solid
foundation for our studies in
flavor physics...**

**They gives us unique access to
strong phases, and it's fun to
work with EPR-entangled
states in an HEP context !**

**→ It takes TWO amplitudes
to have a relative phase...**

Of course, our goal
is to find some flaw
in the structure of
the Standard Model...

We always seem to have
a few *hints* of failure;
the Standard Model bends
yet does not break !
(thus far...)

→ Phases are angles...



Outline

Introduction: Essentials

Overview of Older Results

Survey of Recent Results

Selected Issues Going Forward

Conclusion

relative
strong
phases



**Model
Independence**

**For a written overview, see my CKM2014 proceedings :
[arXiv:1411.7327](https://arxiv.org/abs/1411.7327)**

The Big Picture: Phase Inputs

Places where relative $D^0, D^{0\text{bar}}$ phases can show up:

- 1) Quantum-correlated (“EPR”) D pairs @ threshold: ψ (3770)
- 2) $D^0 - D^{0\text{bar}}$ mixing
- 3) $B \rightarrow DX$, with common $D^0, D^{0\text{bar}}$ final states [re: CKM γ]

Generally, 1) is viewed as a source of information to be input for use by 2) & 3) [more on this later...]

The relevant datasets are CLEO-c and BESIII :

→ Access to relative $D^0, D^{0\text{bar}}$ *strong phase differences*

→ Can obtain *model-independent results*

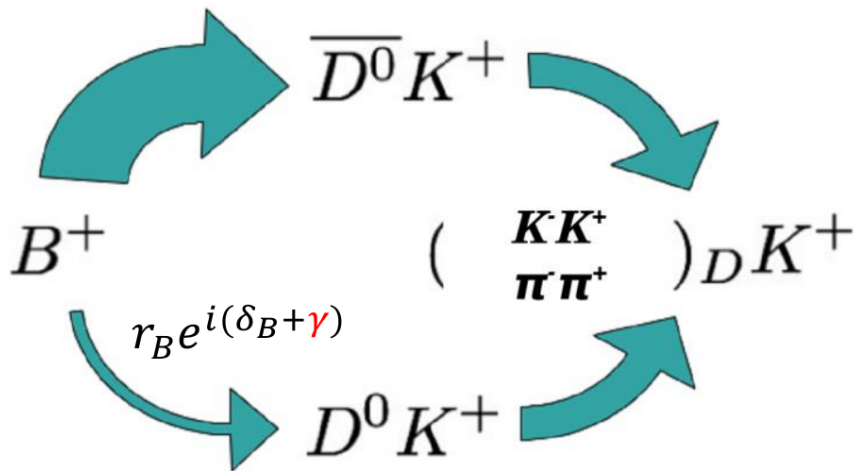
For 2) Rotate measured $K\pi$ mode x', y' parameters to get x, y

For 3) Reduce model-dep. of CKM γ from $B \rightarrow D^{(*)} K^{(*)}, D^{(*)} \pi$

Main Customer: CKM γ Extraction

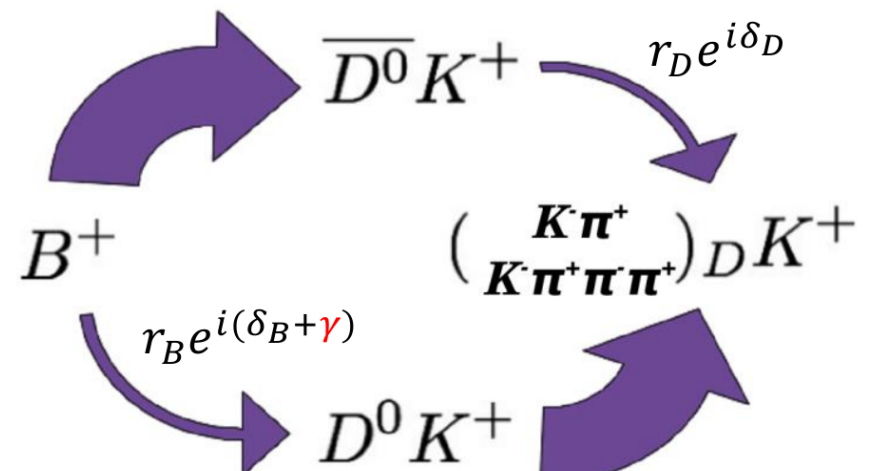
CKM Angle γ Measurement

◆ Gronau, London, Wyler (**GLW**)



Final states are CP eigenstates.
Interference is $O(10\%)$

◆ Atwood, Dunietz, Soni (**ADS**)



Final states are flavor modes ($K\pi, K3\pi$). CF and DCSD decays. Interference is large.

Borrowed from C. Wallace (LHC-b), talk @ Pheno 2014

Using The ψ (3770)

Threshold production of charm with $e^+e^- \rightarrow \psi$ (3770)

The ψ (3770) decays to *coherent* pair of D mesons

$$\psi(3770) \rightarrow \frac{1}{\sqrt{2}} \left[D^0(+z)\bar{D}^0(-z) - \bar{D}^0(+z)D^0(-z) \right]$$

$$\psi(3770) \rightarrow \frac{1}{\sqrt{2}} \left[D_{CP-}(+z)D_{CP+}(-z) - D_{CP+}(+z)D_{CP-}(-z) \right]$$

CP eigen-states: $D_{CP\pm} = [D^0 \pm \bar{D}^0]/\sqrt{2}$

Measure various combination of rates for:

one decay mode only \rightarrow “single tags”

two decay modes \rightarrow “double tags”

Easiest way to see access to relative phases:

\rightarrow Reconstruct one meson in a CP eigenstate: a “CP tag”

\rightarrow Projects 2nd meson into a $D^0, D^{0\text{bar}}$ superposition (Eq 2)

\rightarrow So, $D^0, D^{0\text{bar}}$ amplitudes to common final state interfere

Also can change the sign of interference ! Use CP+ or CP- tag

Decay Mode Jargon

Flavored

Flavored semileptonic	$K^-e^+\nu, K^-\mu^+\nu$	Pure CF
Flavored hadronic	$K^-\pi^+, K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$	CF + DCSD

Self-Conjugate

2-body CP eigenstate	$K^-K^+, \pi^+\pi^-, \dots$	SCS
2-body CP eigenstate	$K_S\pi^0, \dots$	CF + DCSD
Multi body	$K^+K^-\pi^+\pi^-, \pi^+\pi^-\pi^0$	SCS
Multi body	$K_S h^+h^-, K_L h^+h^-$	CF + DCSD
Neither	$K_S K^-\pi^+$	SCS

[Note: "Both" is not possible !]

Blue modes: used for γ **Green : future?** **Black: tag only**

(? out-of-date now ?)

Shorthand: hadron "h" = K, π

CF : Cabibbo-Favored

right-sign Kaon: $D \rightarrow K^{\text{bar}} X + \text{c.c.}$

SCS : Singly-Cabibbo-Suppressed

DCSD : Double-Cabibbo-Suppressed (Decay) wrong-sign Kaon: $D \rightarrow K X + \text{c.c.}$

Multi-Body “Coherence Factors”

Simplified Two body:

$$|A_1 + A_2|^2 = |A_1|^2 + |A_2|^2 + 2 A_1 A_2 e^{-i\delta} \quad | \quad 1, 2 = \text{CF, DCSD}$$

Generalization \rightarrow Atwood-Soni :

Integrate over Dalitz plot; define real average amplitudes
[$\mathcal{A} \rightarrow A$ below]

BUT this requires a “fudge factor” of $\text{Re}^{-i\delta}$ for interference term

Simplified Multi body:

$$\int d \text{Dalitz} | \mathcal{A}_1 + \mathcal{A}_2 |^2 = | A_1 |^2 + | A_2 |^2 + 2 R e^{-i\delta} A_1 A_2 |$$

$$\text{Define: } R e^{-i\delta} = (\text{true cross-term}) / (\text{naïve} = A_1 A_2)$$

Note: $R < 1$ due to two reasons: varying phase & “ $|r(x)| \neq 1$ ”

$$r = A_2 / A_1 \quad A_{K^\pm \pi^\mp \pi^0}^2 = \int | \mathcal{A}_{K^\pm \pi^\mp \pi^0}(\mathbf{x}) |^2 d\mathbf{x}$$

$$R_{K\pi\pi^0} e^{-i\delta_D^{K\pi\pi^0}} = \frac{\int \mathcal{A}_{K^- \pi^+ \pi^0}(\mathbf{x}) \mathcal{A}_{K^+ \pi^- \pi^0}(\mathbf{x}) d\mathbf{x}}{A_{K^- \pi^+ \pi^0} A_{K^+ \pi^- \pi^0}}$$

From Tags to Physics

CP+ & CP- tags:

Switch of +- flips sign of interference term

Also used directly for γ , but *phases are trivial* [GLW]

Semileptonic flavor tags:

No interference; clean normalization [but pesky v...]

Hadronic flavor tags:

Normalization, modulo DCSD [easier than semilep for exp.]

Also modes we want to study for γ [ADS]

Multi-body self-conjugate

Modes we want to under study for γ [GGSZ]

Different analyses use different numbers of tag modes

CLEO $K^-\pi^+$ & CLEO-c, BESIII $K_S\pi^+\pi^-$ use *many* tags

BESIII $K^-\pi^+$ analysis uses only signal and CP tags

Experimental Output

$K^-K^+, \pi^+\pi^-$	GLW	$\delta = 0, \pi$	
$K^- \pi^+$	ADS	δ (R=1)	get from threshold charm...
$K^- \pi^+ \pi^0, K^- \pi^+ \pi^+ \pi^-, K_S K^- \pi^+$	ADS+	R, δ	
$K_S \pi^+ \pi^-, K_S K^+ K^-$	GGSZ	c_i, s_i	

R, δ are Atwood-Soni coherence factors for ADS modes

→ *No relative D^0 - $D^{0\text{bar}}$ phase* in separate $D^0, D^{0\text{bar}}$ Dalitz fits

e.g., if one fits N amplitudes to $D^0, D^{0\text{bar}}$ separately: [D^* -tagged @ B factory]
only gets $2(N-1) = 2N-2$ out of $2N-1$ relative phases

→ Also *avoid Dalitz models*

c_i, s_i are “Cartesian R, δ in Dalitz bins” for GGSZ modes

→ Here, relative D^0 - $D^{0\text{bar}}$ phase is trivial

(distinction due to self-conjugate modes, not changing basis to c_i, s_i !)

→ But we still *avoid Dalitz models*

QC for Pedestrians I - SKIP -

Simplest effect:

$$\psi(3770) \rightarrow [D_{CP+} D_{CP-} - D_{CP-} D_{CP+}] / \sqrt{2}$$

Like CP (++, --): cancels *Unlike CP* (+-, -+): doubled

My favorite general form:

* Ignore mixing for now *

$$\Gamma_{FG} / A_F^2 A_G^2 = [r_F^2 + r_G^2 + 2 r_F r_G R_F R_G \cos(\delta_G - \delta_F)]$$

or $1 + r_F^2 r_G^2 + \dots$: factor out A_i such that $r < 1$

→ $r_{F,G}$ (averaged) amplitude ratios: $\sim A(D^{0\text{bar}} \rightarrow F,G) / A(D^0 \rightarrow F,G)$

1 for CP eigenstates

$\sim \tan^2(\theta_C)$ for hadronic K^- modes [DCSD/CF]

0 for semileptonic → no interference

→ R, δ : Atwood-Soni coherence factors

$R=1; \delta = 0, \pi$ for CP eigenstates;

$R=1; \delta = ?$ for $K^- \pi^+$

Both non-trivial for multi-body hadronic

QC for Pedestrians II - SKIP -

Need some double-tag rate with two “non-trivial” modes to fully separate parameters

→ If not, get only $\text{Re}[R e^{-i\delta}] = R \cos \delta$, not separate (R, δ)
[Or, only c_i , not both c_i, s_i]

The reason that having two works is simple trigonometry:

$$\cos(\delta_2 - \delta_1) = \cos\delta_1 \cos\delta_2 - \sin\delta_1 \sin\delta_2$$

With this, one has enough observables to separate
(can still use modes where one $\delta_i = 0$)

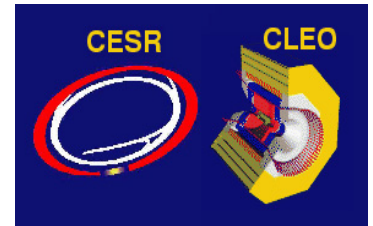
Two “non-trivial” modes ?

- Can be different values of n in $K^-(n\pi)^+$ analyses
- Can even be different bins (i) in $K_S \pi^+ \pi^- c_i, s_i$ analyses

CLEO-c Results

CLEO-c Data : 0.8 fb⁻¹ @ $\Psi(3770)$ & 0.6 fb⁻¹ @ 4170 MeV 2003 - 08

$K^-\pi^+$	281 pb ⁻¹ (updated below)	PRL 100, 221801 (2008); PRD, 78, 012001 (2008) [= more details]
$K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$	818 pb ⁻¹	PRD 80, 031105(R) (2009)
$K_S\pi^+\pi^-$	818 pb ⁻¹	PRD 80, 032002 (2009)
$K_{S,L}h^+h^-$	818 pb ⁻¹	PRD 82, 112006 (2010)
$K_S K^+\pi^-$	818 pb ⁻¹ *	PRD 85, 092016 (2012)
$K^-\pi^+$	→ 818 pb ⁻¹	PRD 86, 112001 (2012)
$K^+K^-\pi^+\pi^-$	818 pb ⁻¹ **	PRD 85, 122002 (2012) { isobar analysis; but <i>first</i> D, D ^{bar}



also use high-E continuum { * + 15 fb⁻¹ ~10 GeV
** + 24 fb⁻¹ ~10 GeV & 600 pb⁻¹ 4.17 GeV

Today's Main Topics

BESIII Results

Dataset : 2.92 fb^{-1} 2010 - 11 (1 2/3 years) \rightarrow 3.5x CLEO-c
Future ability : $\sim 4 \text{ fb}^{-1}$ / running year [note: $\mathcal{L}_{2011} \gg \mathcal{L}_{2010}$]

BESIII	$K^-\pi^+$	2.92 fb^{-1}	PLB 734, 227 (2014)
	$K_S\pi^+\pi^-$	2.92 fb^{-1}	Preliminary @ APS, Apr 2014

[Will use first as an example; second analysis is in backup slides...]

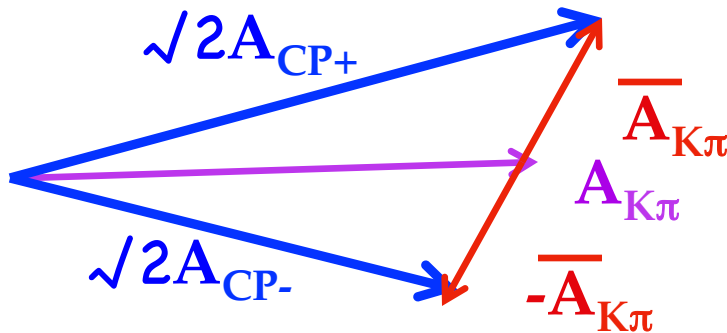
CLEO-c "Legacy" Results

$K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$	818 pb^{-1}	PLB 731, 197 (2014)
$\pi^+\pi^-\pi^0, K^+K^-\pi^0$	818 pb^{-1}	PLB 740, 1 (2015)
$\pi^+\pi^+\pi^-\pi^-, \pi^+\pi^-\pi^0, K^+K^-\pi^0$	818 pb^{-1}	PLB 747, 9 (2015)

[CLEO-c data analyzed by past members, after collaboration disbanded]

Also: 2016 joint analysis of CLEO-c Legacy = LHC-b for $K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$

Simplified Picture: (simple = no mixing)



Amplitude triangle:

$$CP_{\pm} = CF \pm DCSD$$

[DCSD enhanced for visibility !]

**Complex ratio
DCSD/CF amplitude**

$$\frac{\langle K^- \pi^+ | \overline{D}^0 \rangle}{\langle K^- \pi^+ | D^0 \rangle} = -r e^{-i\delta_{K\pi}}$$

Flip CP of tag: reverses interference term

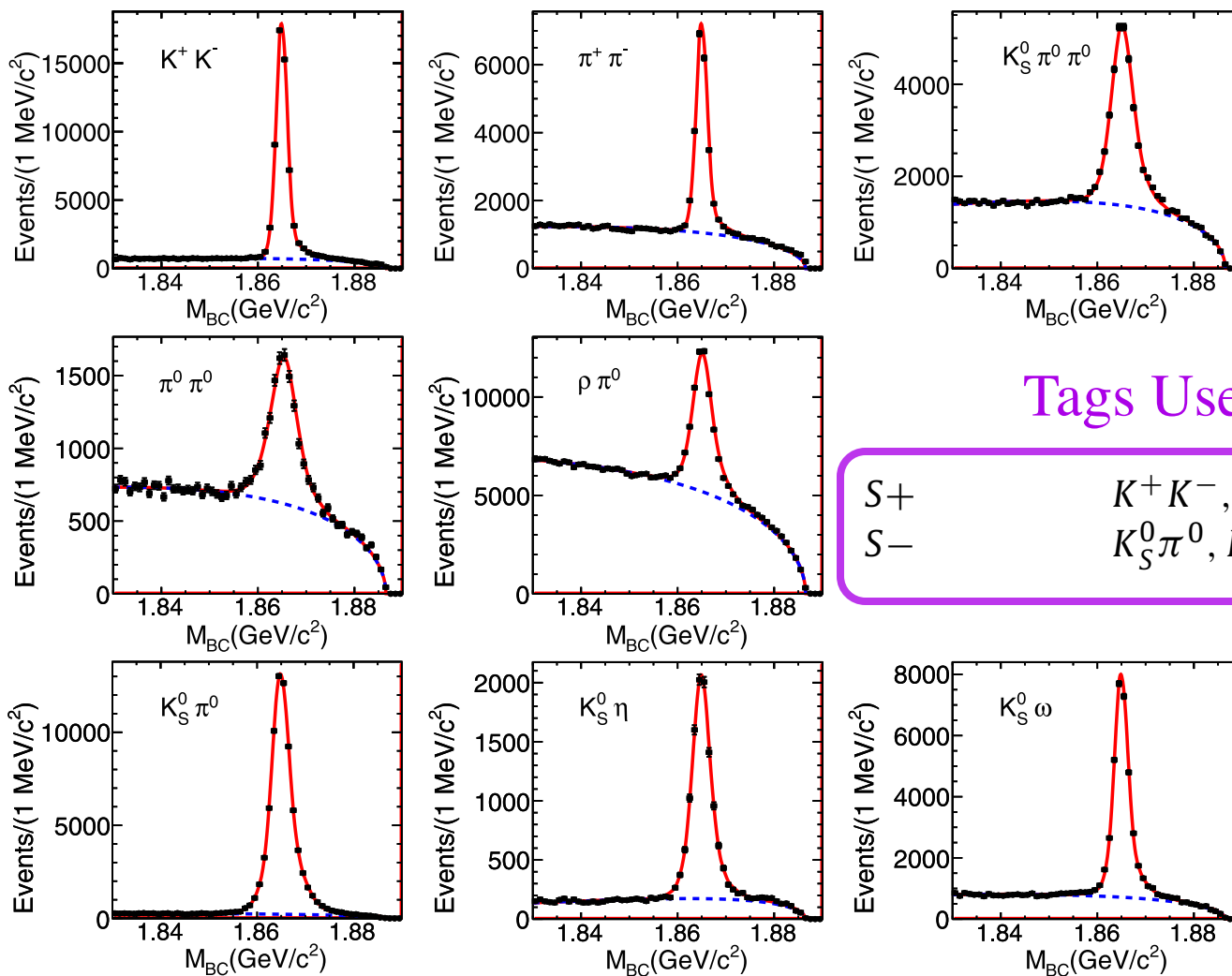
CP-tagged rate asymmetry (essentially) measures $r \cos \delta$

$$\begin{aligned} \mathcal{A}_{CP} &= [|A_{CP-}|^2 - |A_{CP+}|^2] / [|A_{CP-}|^2 + |A_{CP+}|^2] \\ &= r \cos \delta \quad (+ D \text{ mixing corrections: } y, R_{WS}) \end{aligned}$$

← measure

← extract

First BESIII Quantum Coherence result : *straightforward analysis*



Tags Used: 5 CP+, 3 CP-

S+	$K^+K^-, \pi^+\pi^-, K_S^0\pi^0\pi^0, \pi^0\pi^0, \rho^0\pi^0$
S-	$K_S^0\pi^0, K_S^0\eta, K_S^0\omega$

$$\mathcal{A}_{K\pi}^{CP} \equiv \frac{\mathcal{B}_{D^{S-} \rightarrow K^- \pi^+} - \mathcal{B}_{D^{S+} \rightarrow K^- \pi^+}}{\mathcal{B}_{D^{S-} \rightarrow K^- \pi^+} + \mathcal{B}_{D^{S+} \rightarrow K^- \pi^+}}$$

$S+$ ($S-$) denotes the CP -even (CP -odd) eigenstate.

Direct result : *

$$\mathcal{A}_{CP} = (12.7 \pm 1.3 \pm 0.7)\%$$

$$2r \cos \delta_{K\pi} + y = (1 + R_{WS}) \cdot \mathcal{A}_{K\pi}^{CP}$$

Using external inputs for $r_{K\pi}$, R_{WS} , y , we extract :

$$\cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$$

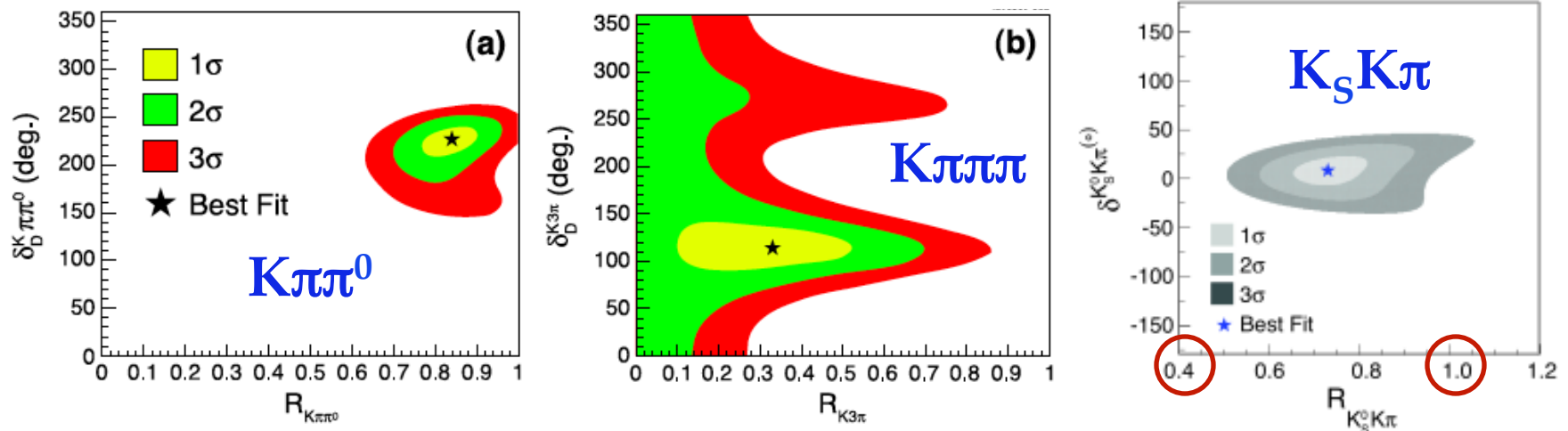
Compare to CLEO-c:

$$\cos \delta_{K\pi} = 0.81^{+0.22}_{-0.18} {}^{+0.07}_{-0.06} \quad (\text{no external inputs})$$

$$\cos \delta_{K\pi} = 1.15^{+0.19}_{-0.17} {}^{+0.00}_{-0.08} \quad (\text{w/ external inputs})$$

* HFAG can use this, I believe: they now omit final $\delta_{K\pi}$ due to external inputs ...

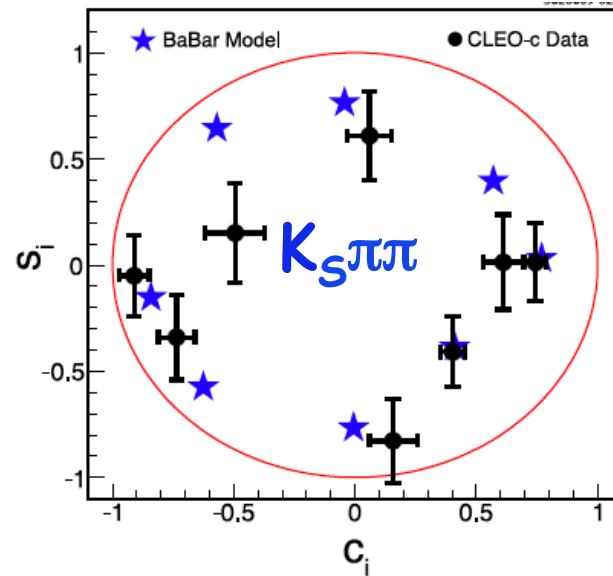
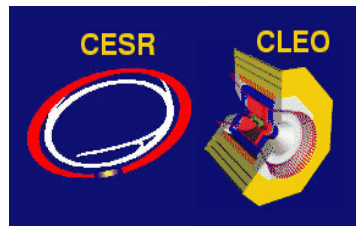
Original CLEO-c Coherence Factors



Small R for $K\pi\pi$: still useful for r_B !

Or, we could bin across Dalitz plot

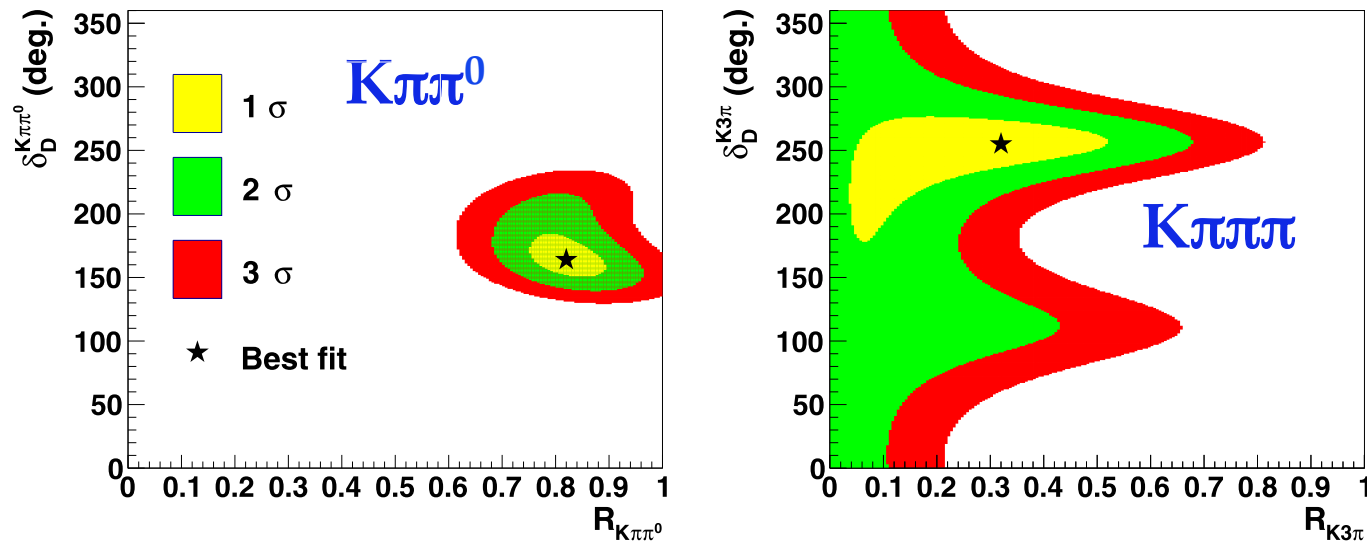
c_i and s_i : bin-averaged
 $\langle R \cos \delta \rangle$ and $\langle R \sin \delta \rangle$



$K^- (n\pi)^+$ Update

PLB 731, 197
(2014) 818 pb⁻¹

CLEO-c “Legacy data” publication → not a collaboration result
(but I personally believe it to be of equal quality)



Note:
 $K\pi\pi\pi$ best fit
now in other
lobe...

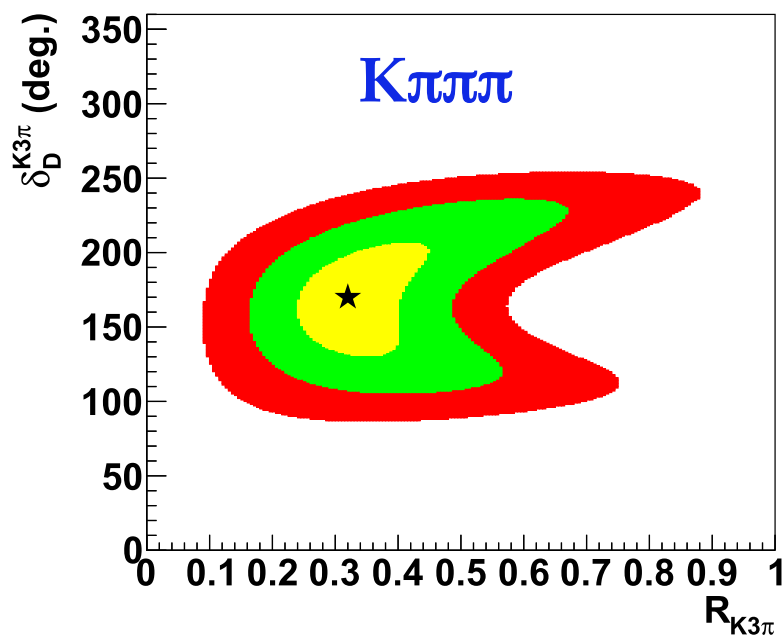
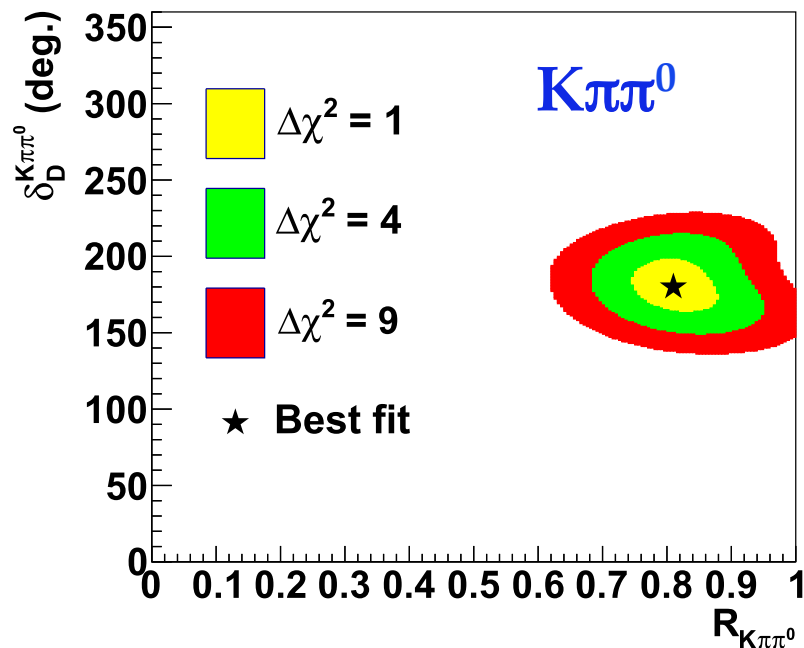
- Now includes $K_S\pi^+\pi^-$ tags
- Updated external inputs (BF, mixing, $K\pi$)

$K\pi\pi\pi$ updated again in
PLB 757, 520
(2016) Now including LHCb data...

$K^- (n\pi)^+$ Update II

PLB 757, 520
(2016) 818 pb⁻¹
+ LHCb data

Combined fit to: CLEO-c “Legacy data”
+ LHC-b data for D mixing



Note: now $K\pi\pi\pi$ “lobes”
are almost gone...

$\pi^+\pi^-\pi^0$ & $K^+K^-\pi^0$ CP Fractions

PLB 740, 1
(2015) 818 pb⁻¹

More CLEO-c “Legacy data” results

CP fraction for a mixed-CP final state:

$$F_+ = N(\text{CP}+) / [N(\text{CP}+) + N(\text{CP}-)]$$

These states act similar to CP eigenstates, but suffer from a statistical “Dilution factor” of $w = (2F_+ - 1)$

If the CP-content is nearly pure (F_+ is near 1 or 0), then the loss is small

Results:

$$\pi^+ \pi^- \pi^0: F_+ = 0.968 \pm 0.017 \pm 0.006$$

$$K^+ K^- \pi^0: F_+ = 0.731 \pm 0.058 \pm 0.021$$

The three-pion mode is nearly pure:
acts *almost* like a CP-eigenstate

$\pi^+\pi^-\pi^+\pi^-$ CP Fraction & More

PLB 747, 9
(2015) 818 pb⁻¹

These CLEO-c “Legacy data” results also imake use of more complx non-CP-eigenstate $K_S \pi^+ \pi^-$ & $K_L \pi^+ \pi^-$ tags

Results:

$$\pi^+ \pi^- \pi^+ \pi^- : \quad F_+ = 0.737 \pm 0.028$$

The new tags can be used to update the previous modes

$$\text{New } \pi^+ \pi^- \pi^0 : \quad F_+ = 1.014 \pm 0.045 \pm 0.022$$

$$\text{Combined} : \quad F_+ = 0.973 \pm 0.017$$

$$\text{New } K^+ K^- \pi^0 : \quad F_+ = 0.734 \pm 0.106 \pm 0.054$$

$$\text{Combined} : \quad F_+ = 0.732 \pm 0.055$$

$K_S X$ vs. $K_L X$ Rate Asymmetries

Another somewhat related topic, also involving phases

Study rate asymmetries for specific mode pairs of the form :

$K_S n\pi$ & $K_L n\pi$

The K_S & K_L wave-functions lead to net amplitudes that are sums and differences of the CF and DCSD amplitudes
→ up to 10% effects, depending on a relative phase

Some results from CLEO-c ; many more in progress @ BESIII

Selected Issues I

Places to make progress on existing ideas:

→ Use data to un-rotate mixing results for multi-body modes !
e.g., $K\pi\pi^0$: “Atwood-Soni for mixing” [Bondar et al. 2010]

→ Explore suggestion to use Charm mixing as a *SOURCE* of strong phase information [Harnew & Rademacker 2014, 2015]

And, of course:

Maintain a lively $D \leftrightarrow B$ interchange & forge ahead !

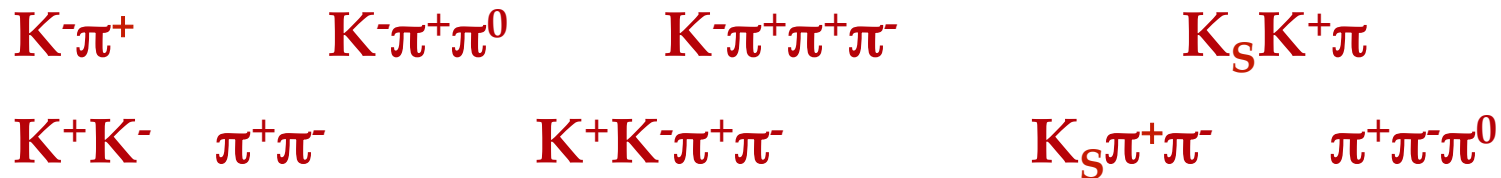
Selected Issues II

Places to Be Careful...

- Efficiencies vary across D Dalitz plots
Charm and B factories differ; we traffic in corrected variables
Current methods accurate? Need Dalitz models to do well?
So, take care if using A-S coherence factors or CP fractions!
- Are studies of D mixing, D CPV, K_S CPV effects complete?
[Probably; see excellent review by Matteo Rama, CKM14, Vienna]
- Assumptions of SM re: CPV could be more explicit
e.g., GGSZ assumes no *weak phase* between CF & DCSD (?)
- Take care with Kaon regeneration and Kaon interactions!

Everything is a Special Case ! (almost)

So if you were confused, you're probably not alone...



$K^- \pi^+$ only δ ; $K^- \pi^+ \pi^0$, $K^- \pi^+ \pi^+ \pi^-$ have both R & δ

Multi-body Self-conjugate modes:

If no CPV, only $2(n-1)$ isobar phases, not $2n-1$

Need threshold data only to avoid model dependence;
there is no “essential” D^0 - $D^{0\text{bar}}$ phase

4-body: more complicated angular momenta than 3-body

K_S modes: CF and DCSD give K^0 , $K^{0\text{bar}}$, not K_S directly

Conclusions

Unique access to strong phases & ability to extract model-independent results with charm at threshold

- Started with many CLEO-c Results, added “legacy” results
- Perhaps a tiny bit more activity with CLEO-c “legacy data” ?
- Now, the 3.5x larger BESIII dataset is producing results

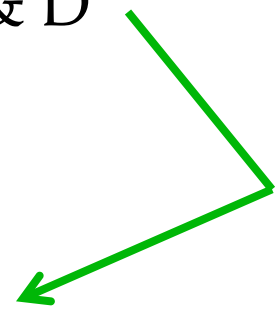
Many modes in progress...stay tuned!

Interest of B physics users remains high

- LHCb is a *huge* addition to older B-factory data
- But... e^+e^- will return soon with Belle II [beams stored !]
- Important to keep active interaction between B & D

Future prospects are bright

- More precision, new modes, new variables !
- Need to maintain threshold analysis manpower



Selected Theory References: Insights, Old & New

Quantum Correlations

Goldhaber & Rosner, Phys. Rev. D15, 1254 (1977)

Xing, Phys. Rev. D55, 196 (1997)

Gronau, Grossman & Rosner, Phys.Lett. B508, 37 (2001)

Atwood & Petrov, Phys. Rev. D71, 054032 (2005) [2002 eprint: hep-ph/0207165]

Asner & Sun, Phys. Rev. D73, 034024 (2006); E: ibid, D77, 019901 (2008)

DCSD mixing background cancels for correlated D pairs

Bigi & Sanda, Phys. Lett. B171, 320 (1986) [see Ref. 5 for other contributors...]

“Attention PDG” : $K_S \neq 1/2$ of K^0 or $K^{0\text{bar}}$

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D^0 Mixing with $K_S K \pi$

Malde & Wilkinson, Phys. Lett. B701, 353 (2011)

D^0 Mixing as the Source of Phase Info for CKM γ with “DK” modes

Harnew & Rademacker, Phys. Lett. B 728, 296 (2014)

Harnew & Rademacker, JHEP 03, 169 (2015)

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B physics: CKM Υ with “DK” modes

Bigi & Sanda, Phys. Lett. B211, 213 (1988)

The Grand Pre-Cursor

Gronau & London, Phys. Lett. B253, 483 (1991)

“GLW”: SCS CP-eigenstates

Gronau & Wyler, Phys. Lett. B265, 172 (1991)

Atwood, Eilam, Gronau & Soni, Phys. Lett. B341, 372 (1995). “pre-ADS”

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Atwood & Soni, Phys. Rev. D68, 033003 (2003) Coherence factors

Giri, Grossman, Soffer & Zupan, Phys. Rev. D68, 054018 (2003) “GGSZ”: $K_S \pi \pi$

Bondar. Proc. of BINP Special Analysis Meeting on Dalitz Analysis (2002) [first “GGSZ”]

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CF multi-body: larger strong phases?

Bondar & Poluektov, Eur. Phys. J. C 55, 51 (2008)

optimizing GGSZ

Grossman, Ligeti & Soffer PRD 67, 071301 (2003)

“GLS”: non-eigenstate SCS

Bondar & Gershon Phys. Rev. D 70, 091503 (2004)

$B \rightarrow D^{*0}K$, with $D^{*0} \rightarrow D^0\pi^0, D^0\gamma$

Selected Theory References: Corrections

Early Explorations of D Mixing

Meca & Silva, Phys. Rev. Lett. 81, 1377 (1998)
Amorim, Santos & Silva Phys. Rev. D 59, 056001 (1999)

D mixing and CKM γ from $K_S\pi\pi$; Model-independent D mixing from multi-body modes

Bondar, Poluektov, & Vorobiev Phys. Rev. D 82, 034033 (2010)

D mixing and CKM γ from $B \rightarrow DK, D\pi$

Rama Phys. Rev. D 89, 014021 (2014)

D Direct CPV and CKM γ from $B \rightarrow DK$

Martone & Zupan, Phys. Rev. D 87, 034005 (2013)
Bhattacharya, Gronau, London & Rosner Phys. Rev. D 87, 074002 (2013)
Wang Phys. Rev. Lett. 110, 061802 (2013)

CPV in K_S & CKM γ

Grossman & Savastio JHEP 03, 008 (2014)

K_S decay time acceptance and CPV in tau, D

Bigi & Sanda Phys. Lett. B 625, 47 (2005)
Grossman & Nir JHEP 04, 002 (2012)

K_S detector interactions & B, D CPV

Ko, Won, Golob, Pakhlov Phys. Rev. D 84, 111501(R) (2011)

Classic “GGSZ mode”; better precision than CLEO-c
Preliminary results presented @ APS meeting, Apr 2014

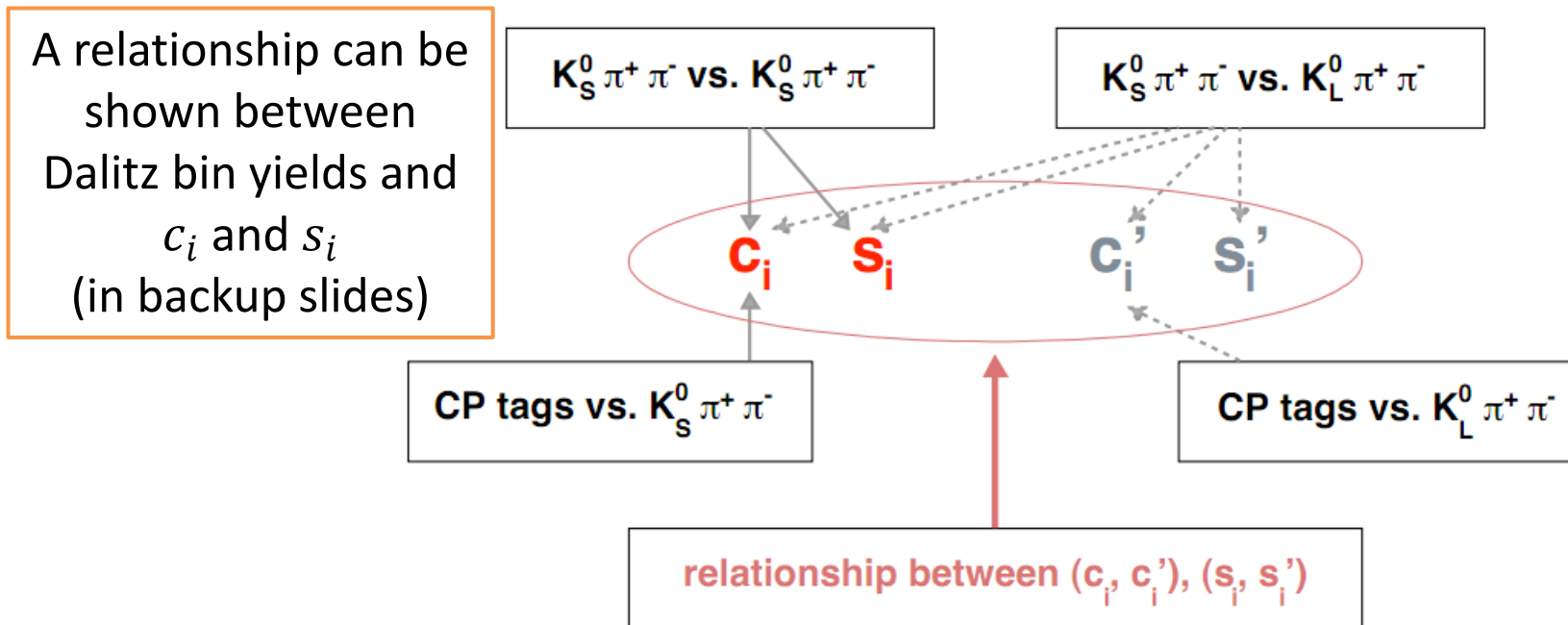
$K_S\pi^+\pi^-$ is the main topic: extract c_i, s_i
 $K_L\pi^+\pi^-$ is also used: extract c'_i, s'_i
relate to c_i, s_i with model corrections.

Aggressive use of tags, including partial reconstruction

All results preliminary; as presented at April 2014 AP meeting

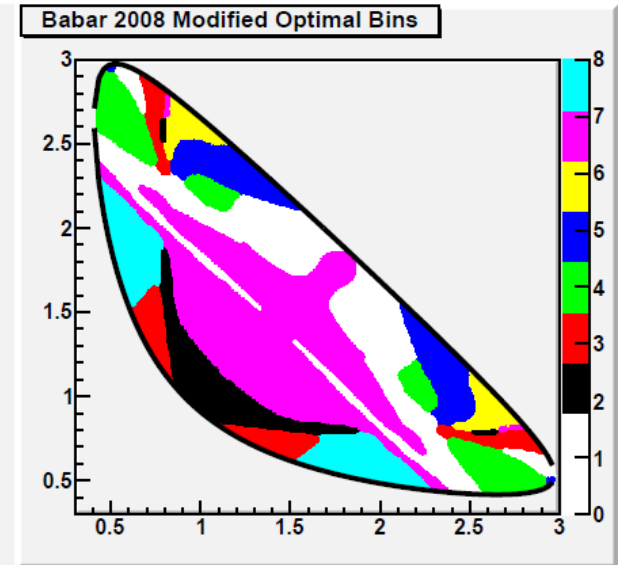
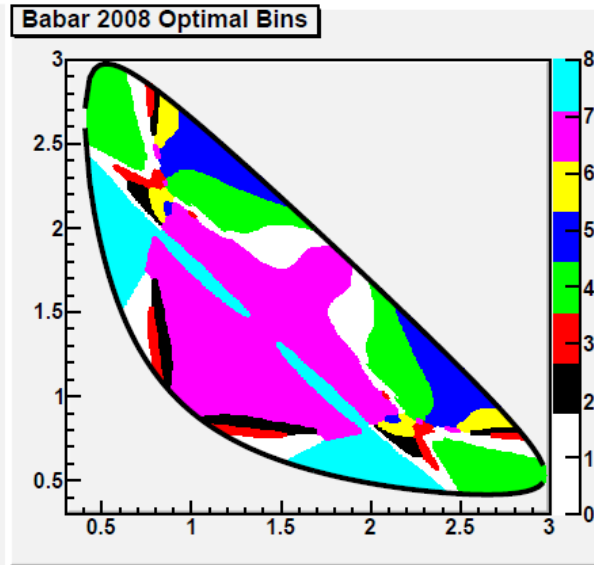
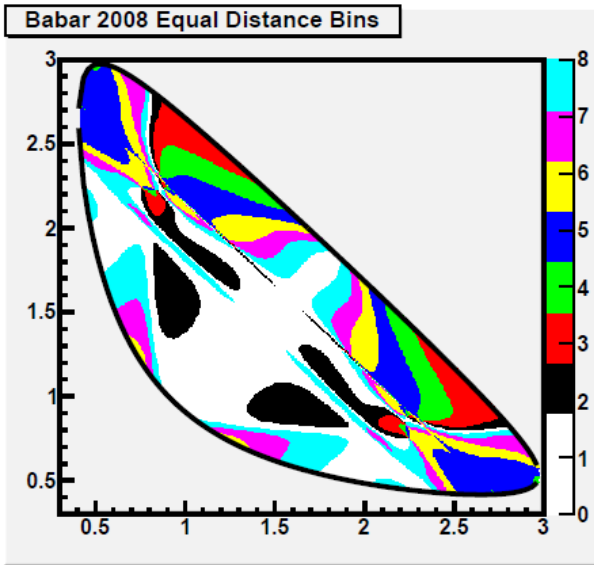
Preliminary $K_S \pi^+ \pi^-$ Results

We can calculate c_i and s_i from double tags of $D^0 \rightarrow K_S \pi^+ \pi^-$ vs $D^0 \rightarrow (K_{S,L} \pi^+ \pi^-$ or CP eigenstates)



Only c_i, s_i from $K_S \pi^+ \pi^-$ is used to calculate γ .

However adding in $D^0 \rightarrow K_L \pi^+ \pi^-$ we can calculate c'_i, s'_i and use how they relate to c_i, s_i to further constrain our results in a Global fit.



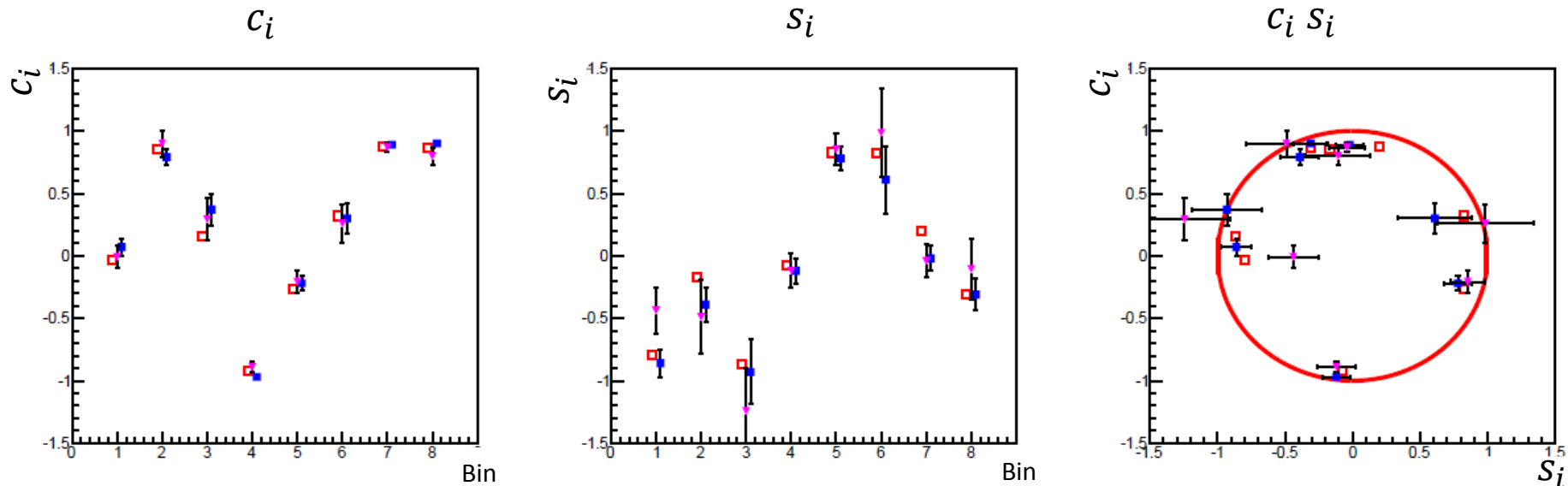
Result of splitting the Dalitz phase space into 8 equally spaced phase bins based on the BaBar 2008 Model.

Starting with the equally spaced bins, bins are adjusted to optimize the sensitivity to γ . A secondary adjustment smooths binned areas smaller than detector resolution.

Similar to the “optimal binning” except the expected background is taken into account before optimizing for γ sensitivity.

Source: CLEO Collaboration, *Physical Review D*, vol 82., pp. 112006 - 112035

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Bins	C_i		S_i	
	BES-III	CLEO-c	BES-III	CLEO-c
1	0.066 ± 0.066	-0.009 ± 0.088	-0.843 ± 0.119	-0.438 ± 0.184
2	0.796 ± 0.061	0.900 ± 0.106	-0.357 ± 0.148	-0.490 ± 0.295
3	0.361 ± 0.125	0.292 ± 0.168	-0.962 ± 0.258	-1.243 ± 0.341
4	-0.985 ± 0.017	-0.890 ± 0.041	-0.090 ± 0.093	-0.119 ± 0.141
5	-0.278 ± 0.056	-0.208 ± 0.085	0.778 ± 0.092	0.853 ± 0.123
6	0.267 ± 0.119	0.258 ± 0.155	0.635 ± 0.293	0.984 ± 0.357
7	0.902 ± 0.017	0.869 ± 0.034	-0.018 ± 0.103	-0.041 ± 0.132
8	0.888 ± 0.036	0.798 ± 0.070	-0.301 ± 0.140	-0.107 ± 0.240

***Only statistical uncertainty is listed

BESIII
Preliminary

□ Model prediction
● BESIII
▼ CLEO-c

Consistent agreement with CLEO-c measurements.

Source: CLEO Collaboration, Physical Review D, vol 82., pp. 112006 - 112035

Improved errors w.r.t. CLEO-c

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