

# Theory of charm mixing

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- Theory & phenomenology of charm mixing
- Results on mixing and CPV parameters
- Bounds on New Physics in the  $\Delta C=2$  amplitude

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# Theory of meson mixing (i)

Time evolution of an unstable two-states system of CP-conjugated mesons:

$$i\hbar \frac{\partial}{\partial t} \begin{pmatrix} M \\ \bar{M} \end{pmatrix} = \left[ \begin{pmatrix} m & m_{12} \\ m_{12}^* & m \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma \end{pmatrix} \right] \begin{pmatrix} M \\ \bar{M} \end{pmatrix}$$

Eigenvectors:

$$|M_{1,2}\rangle = p|M\rangle \pm q|\bar{M}\rangle, \quad \frac{q}{p} = -\sqrt{\frac{m_{12}^* - \frac{i}{2}\Gamma_{12}^*}{m_{12} - \frac{i}{2}\Gamma_{12}}}, \quad |p|^2 + |q|^2 = 1$$

Eigenvalues:

$$m_{1,2} - \frac{i}{2}\Gamma_{1,2} = m - \frac{i}{2}\Gamma \mp \sqrt{\left(m_{12} - \frac{i}{2}\Gamma_{12}\right) \left(m_{12}^* - \frac{i}{2}\Gamma_{12}^*\right)}$$

$$\Gamma(x - iy) = 2\sqrt{\left(m_{12} - \frac{i}{2}\Gamma_{12}\right) \left(m_{12}^* - \frac{i}{2}\Gamma_{12}^*\right)} \quad \begin{aligned} \Gamma x &= \Delta m = m_2 - m_1 \\ 2\Gamma y &= \Delta\Gamma = \Gamma_2 - \Gamma_1 \end{aligned}$$

Meson mixing is characterized by three parameters

$$|m_{12}|, |\Gamma_{12}|, \Phi_{12} = \arg\left(\frac{\Gamma_{12}}{m_{12}}\right)$$

or

$$x, y, \left|\frac{q}{p}\right| \simeq 1 + \frac{1}{2}a_{\text{SL}}$$

# Theory of meson mixing (ii)

The two parametrizations are equivalent: one can pass from one to the other (with some effort)

$$x = \frac{\text{sgn}(\cos \Phi_{12})}{\sqrt{2}\Gamma} \sqrt{4|m_{12}|^2 - |\Gamma_{12}|^2 + \sqrt{(4|m_{12}|^2 + |\Gamma_{12}|^2)^2 - 16|m_{12}|^2|\Gamma_{12}|^2 \sin^2 \Phi_{12}}}$$

$$y = \frac{1}{2\sqrt{2}\Gamma} \sqrt{|\Gamma_{12}|^2 - 4|m_{12}|^2 + \sqrt{(4|m_{12}|^2 + |\Gamma_{12}|^2)^2 - 16|m_{12}|^2|\Gamma_{12}|^2 \sin^2 \Phi_{12}}}$$

$$\left| \frac{q}{p} \right| = \sqrt{\frac{1 - \delta}{1 + \delta}}, \quad \delta = \frac{2|m_{12}||\Gamma_{12}| \sin \Phi_{12}}{(\Gamma x)^2 + |\Gamma_{12}|^2}$$

**CP conservation in mixing corresponds to**

$$|q/p| = 1 \leftrightarrow \Phi_{12} = 0, \pi$$

**Notice that the phases of  $m_{12}$  (or  $\Gamma_{12}$ ) and  $q/p$  are phase-convention dependent, thus not observable**

# Time-dependent rates

Meson mixing produces time-dependent decay rates ( $\tau = \Gamma t$ ):

$$\Gamma (M(t) \rightarrow f) = \frac{1}{2} e^{-\tau} |A_f|^2 \left[ (1 + |\lambda_f|^2) \cosh(y\tau) + (1 - |\lambda_f|^2) \cos(x\tau) + 2 \operatorname{Re}(\lambda_f) \sinh(y\tau) - 2 \operatorname{Im}(\lambda_f) \sin(x\tau) \right]$$

In general, there are 4 rates ( $M \rightarrow f, \bar{M} \rightarrow f, M \rightarrow \bar{f}, \bar{M} \rightarrow \bar{f}$ ):

$$i) M \rightarrow \bar{M} : A_f \rightarrow \bar{A}_f, \lambda_f \rightarrow \lambda_f^{-1} \quad ii) f \rightarrow \bar{f} : A_f \rightarrow A_{\bar{f}}, \lambda_f \rightarrow \lambda_{\bar{f}}$$

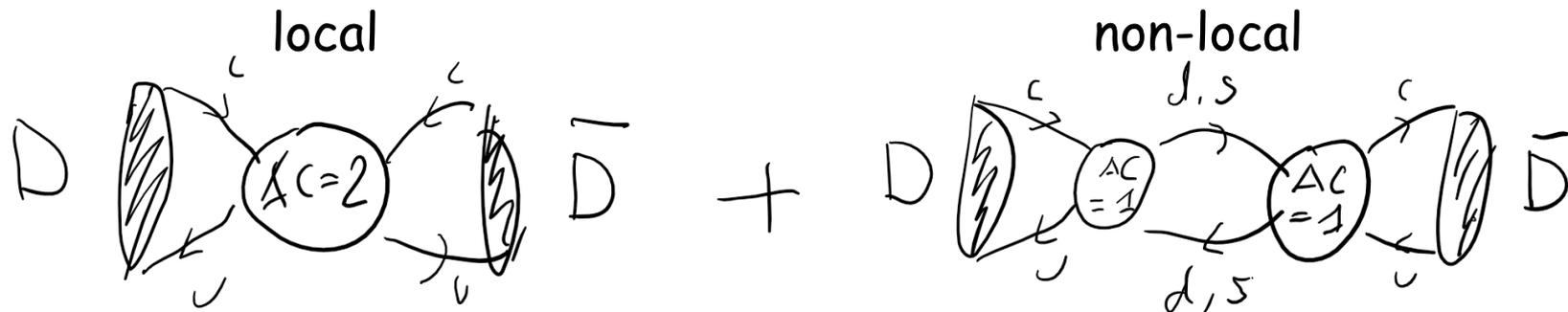
Two more observable parameters:

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}, \quad \lambda_{\bar{f}} = \frac{q}{p} \frac{\bar{A}_{\bar{f}}}{A_{\bar{f}}}$$

$$\arg(\lambda_f, \lambda_{\bar{f}}) \neq 0, \pi$$

**CP violation in the interference of mixed and unmixed decay amplitudes**

# Computing charm mixing



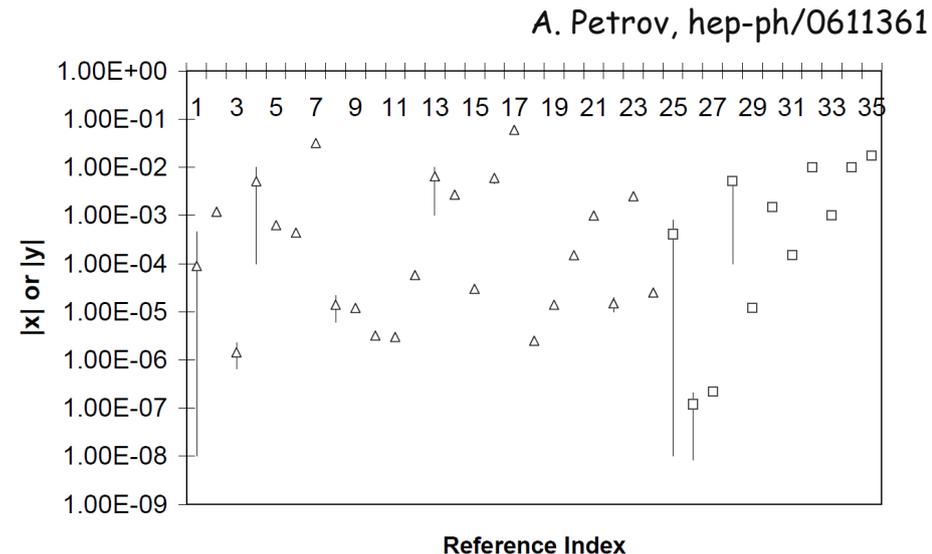
$$2M_D \left( m_{12} - \frac{i}{2} \Gamma_{12} \right) = \langle D | H_{\text{eff}}^{\Delta C=2} | \bar{D} \rangle + \int d^4x \langle D | T ( H_{\text{eff}}^{\Delta C=1}(x) H_{\text{eff}}^{\Delta C=1}(0) ) | \bar{D} \rangle$$

- \*  $\Gamma_{12}$  comes from the non-local term, while both contribute to  $m_{12}$
- \*  $H_{\text{eff}}^{\Delta C=2}$  contains the contribution of heavy particles ( $b$ , NP)

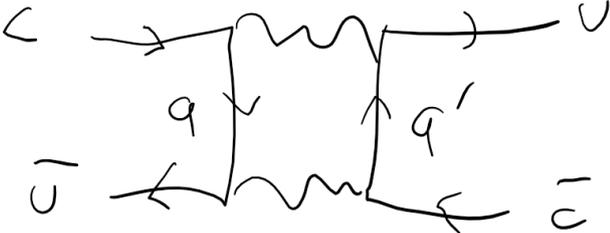
Attempts at computing  $x$  and  $y$ :

- OPE in  $\Lambda_{\text{QCD}}/m_c$ , but  $m_c \sim \Lambda_{\text{QCD}}$ : convergence,  $q$ - $h$  duality
- sum over hadronic states: too many states, needs assumptions

$$x, y \leq 10^{-2} \div 10^{-3} \ll 1$$



# Flavour structure of the amplitude

box diagram  =  $\lambda_q \lambda_{q'} D_{qq'}$

$$\lambda_q = V_{cq}^* V_{uq}$$

$$\lambda_s \sim \sin \theta_c$$

$$\lambda_b \sim (\sin \theta_c)^5$$

$$\lambda_d = -\lambda_s - \lambda_b$$

$$A^{\Delta C=2} = \sum_{q,q'=d,s,b} \lambda_q \lambda_{q'} D_{qq'} = \lambda_s^2 (D_{ss} + D_{dd} - 2D_{sd}) +$$

$$2\lambda_s \lambda_b (D_{bs} + D_{dd} - D_{bd} - D_{sd}) + \mathcal{O}(\lambda_b^2)$$

i) GIM and SU(3) suppression coincide: the leading term is quadratic in the SU(3) breaking  $\varepsilon$ , while the subleading one is linear

A. Falk et al., hep-ph/0110317

$$A^{\Delta C=2} \sim \lambda_s^2 \varepsilon^2 + 2\lambda_s \lambda_b \varepsilon + \mathcal{O}(\lambda_b^2)$$

ii) the leading term has no weak phase:  $m_{12}$  and  $\Gamma_{12}$  are real up to corrections suppressed by  $\lambda_b/\lambda_s \times 1/\varepsilon \sim 10^{-3}$ . **SM CP violation in mixing is negligible** (yet enhanced by SU(3) breaking w.r.t. the leading term)

# Measuring the mixing parameters

The smallness of  $x$ ,  $y$ ,  $\delta=(1-|q/p|^2)/(1+|q/p|^2)$ ,  $\lambda_b$ ,  $\arg(m_{12})$  and  $\arg(\Gamma_{12})$  makes charm mixing and CP violation rather peculiar

i) the relations between theoretical and phenomenological parameters become:

$$|m_{12}| = 2\Gamma x + \mathcal{O}(\delta^2), \quad |\Gamma_{12}| = \Gamma y + \mathcal{O}(\delta^2), \quad \sin \Phi_{12} = \frac{x^2 + y^2}{xy} \delta + \mathcal{O}(\delta^2)$$

ii) the decay rate time dependence can be expanded to the first few orders: for example, time-dependent decays to CP eigenstates become:

$$\Gamma(D(t)/\bar{D}(t) \rightarrow f) = e^{-\tau} |A_f|^2 \left[ 1 + \eta_{CP} \left| \frac{q}{p} \right|^{\pm 1} (y \cos \phi \mp x \sin \phi) \tau \right] = |A_f|^2 e^{-\Gamma_{D/\bar{D} \rightarrow f} t} + \mathcal{O}(x^2, y^2)$$

i.e. an exponential decay in terms of the effective rates

$$\Gamma_{D/\bar{D} \rightarrow f} = \Gamma \left[ 1 + \eta_{CP} \left| \frac{q}{p} \right|^{\pm 1} (y \cos \phi \mp x \sin \phi) \right]$$

which in turn are used to define the observables (e.g.  $f = K^+ K^-, \pi^+ \pi^-$ ):

$$y_{CP} = \eta_{CP} \frac{\Gamma_{\bar{D} \rightarrow f} + \Gamma_{D \rightarrow f}}{2\Gamma} - 1, \quad A_\Gamma = \frac{\Gamma_{D \rightarrow f} - \Gamma_{\bar{D} \rightarrow f}}{2\Gamma}$$

We are in the approximation and phase convention for which  $\frac{\bar{A}_f}{A_f} = 1$ ,  $\lambda_f \rightarrow \frac{q}{p}$ , so that CP violation in the interference of mixed and unmixed decays is controlled by  $\phi = \arg\left(\frac{q}{p}\right)$

In the same approximation, assuming that  $\Gamma_{12}$  is dominated by Cabibbo-allowed decays,  $\arg(\Gamma_{12}) = 0$ , hence the relation

$$\arg\left(\Gamma_{12} \frac{q}{p}\right) = \arg(y + i\delta x) \text{ becomes } \phi = \arg(y + i\delta x)$$

MC et al., hep-ph/0703204; Kagan&Sokoloff, 0907.3917

CP violation in the interference of mixed and unmixed decays is directly related to CP violation in mixing. In particular, one finds that

$$\arg(\phi) = 0 \quad \Leftrightarrow \quad \arg(\Phi_{12}) = 0 \quad \Leftrightarrow \quad \left|\frac{q}{p}\right| = 1$$

**Another example: time-dependent decays to “wrong-sign” non-CP eigenstate final states  $f$ . In general, 4 amplitudes:**

$$A_f = T_f e^{i\phi_f} [1 + r_f e^{i(\Delta_f + \Phi_f)}], \quad \bar{A}_{\bar{f}} = T_f e^{-i\phi_f} [1 + r_f e^{i(\Delta_f - \Phi_f)}],$$

$$A_{\bar{f}} = T_{\bar{f}} e^{i(\delta_f + \phi_{\bar{f}})} [1 + r_{\bar{f}} e^{i(\Delta_{\bar{f}} + \Phi_{\bar{f}})}], \quad \bar{A}_f = T_{\bar{f}} e^{i(\delta_f - \phi_{\bar{f}})} [1 + r_{\bar{f}} e^{i(\Delta_{\bar{f}} - \Phi_{\bar{f}})}]$$

**Consider CF  $A_f$  and DCS  $A_{\bar{f}}$  (e.g.  $K^-\pi^+$ ): neglecting subleading terms ( $r_f, r_{\bar{f}} = 0$ ), the weak phase difference of leading amplitudes ( $\phi_f = \phi_{\bar{f}}$ ) and expanding for small  $x, y, R_f = |T_{\bar{f}}/T_f|, \sin\theta_c$ , the time-dependent decay rates become:**

$$\Gamma(D(t) \rightarrow f) = e^{-\tau} |A_f|^2, \quad \Gamma(D(t) \rightarrow \bar{f}) = e^{-\tau} |A_f|^2 \left( R_f^2 + R_f (y'_+)_f \tau + \frac{(x'_+)_f^2 + (y'_+)_f^2}{4} \tau^2 \right),$$

$$\Gamma(\bar{D}(t) \rightarrow \bar{f}) = e^{-\tau} |\bar{A}_{\bar{f}}|^2, \quad \Gamma(\bar{D}(t) \rightarrow f) = e^{-\tau} |\bar{A}_{\bar{f}}|^2 \left( R_f^2 + R_f (y'_-)_f \tau + \frac{(x'_-)_f^2 + (y'_-)_f^2}{4} \tau^2 \right)$$

**where**  $(x'_\pm)_f = \left| \frac{q}{p} \right|^{\pm 1} (x'_f \cos \phi \pm y'_f \sin \phi), \quad (y'_\pm)_f = \left| \frac{q}{p} \right|^{\pm 1} (y'_f \cos \phi \mp x'_f \sin \phi)$  **and**

$$\begin{pmatrix} x'_f \\ y'_f \end{pmatrix} = \begin{pmatrix} \cos \delta_f & \sin \delta_f \\ -\sin \delta_f & \cos \delta_f \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

**Constrain the mixing parameters, but need two additional inputs:  $R_f, \delta_f$**

	Observable	Value	Correlation Coeff.				
WA	$y_{CP}$	$(0.835 \pm 0.155)\%$					
WA	$A_{\Gamma}$	$(-0.059 \pm 0.040)\%$					
Belle	$x$	$(0.53 \pm 0.19 \pm 0.06 \pm 0.07)\%$	1	0.054	-0.074	-0.031	
	$y$	$(0.28 \pm 0.15 \pm 0.05 \pm 0.05)\%$	0.054	1	0.034	-0.019	
	$ q/p $	$(0.91 \pm 0.16 \pm 0.5 \pm 0.6)$	-0.074	0.034	1	0.044	
	$\phi$	$(-6 \pm 11 \pm 3 \pm 4)^{\circ}$	-0.031	-0.019	0.044	1	
BaBar	$x$	$(0.16 \pm 0.23 \pm 0.12 \pm 0.08)\%$	1	0.0615			
	$y$	$(0.57 \pm 0.20 \pm 0.13 \pm 0.07)\%$	0.0615	1			
WA	$R_M$	$(0.0130 \pm 0.0269)\%$					
BaBar	$(x'_{+})_{K\pi\pi}$	$(2.48 \pm 0.59 \pm 0.39)\%$	1	-0.69			
	$(y'_{+})_{K\pi\pi}$	$(-0.07 \pm 0.65 \pm 0.50)\%$	-0.69	1			
	$(x'_{-})_{K\pi\pi}$	$(3.50 \pm 0.78 \pm 0.65)\%$	1	-0.66			
	$(y'_{-})_{K\pi\pi}$	$(-0.82 \pm 0.68 \pm 0.41)\%$	-0.66	1			
CLEO	$R_D$	$(0.533 \pm 0.107 \pm 0.045)\%$	1	0	0	-0.42	0.01
	$x^2$	$(0.06 \pm 0.23 \pm 0.11)\%$	0	1	-0.73	0.39	0.02
	$y$	$(4.2 \pm 2 \pm 1)\%$	0.	-0.73	1	-0.53	-0.03
	$\cos \delta_{K\pi}$	$(0.84 \pm 0.2 \pm 0.06)$	-0.42	0.39	-0.53	1	0.04
	$\sin \delta_{K\pi}$	$(-0.01 \pm 0.41 \pm 0.04)$	0.01	0.02	-0.03	0.04	1
BaBar	$R_D$	$(0.3030 \pm 0.0189)\%$	1	0.77	-0.87		
	$(x'_{+})^2_{K\pi}$	$(-0.024 \pm 0.052)\%$	0.77	1	-0.94		
	$(y'_{+})_{K\pi}$	$(0.98 \pm 0.78)\%$	-0.87	-0.94	1		
BaBar	$A_D$	$(-2.1 \pm 5.4)\%$	1	0.77	-0.87		
	$(x'_{-})^2_{K\pi}$	$(-0.020 \pm 0.050)\%$	0.77	1	-0.94		
	$(y'_{-})_{K\pi}$	$(0.96 \pm 0.75)\%$	-0.87	-0.94	1		
Belle	$R_D$	$(0.364 \pm 0.018)\%$	1	0.655	-0.834		
	$(x'_{+})^2_{K\pi}$	$(0.032 \pm 0.037)\%$	0.655	1	-0.909		
	$(y'_{+})_{K\pi}$	$(-0.12 \pm 0.58)\%$	-0.834	-0.909	1		
Belle	$A_D$	$(2.3 \pm 4.7)\%$	1	0.655	-0.834		
	$(x'_{-})^2_{K\pi}$	$(0.006 \pm 0.034)\%$	0.655	1	-0.909		
	$(y'_{-})_{K\pi}$	$(0.20 \pm 0.54)\%$	-0.834	-0.909	1		
CDF	$R_D$	$(0.351 \pm 0.035)\%$	1	-0.967	0.900		
	$(y'_{CPA})_{K\pi}$	$(0.43 \pm 0.43)\%$	-0.967	1	-0.975		
	$(x'_{CPA})^2_{K\pi}$	$(0.008 \pm 0.018)\%$	0.900	-0.975	1		
LHCb	$R_D$	$(0.3568 \pm 0.0058 \pm 0.0033)\%$	1	-0.894	0.77	-0.895	0.772
	$(y'_{+})_{K\pi}$	$(0.48 \pm 0.09 \pm 0.06)\%$	-0.894	1	-0.949	0.765	-0.662
	$(x'_{+})^2_{K\pi}$	$(6.4 \pm 4.7 \pm 3)10^{-5}$	0.77	-0.949	1	-0.662	0.574
	$(y'_{-})_{K\pi}$	$(0.48 \pm 0.09 \pm 0.06)\%$	-0.895	0.765	-0.662	1	-0.95
	$(x'_{-})^2_{K\pi}$	$(4.6 \pm 4.6 \pm 3)10^{-5}$	0.772	-0.662	0.574	-0.95	1

# Fitting the data

mostly from HFAG 2015, symmetrized errors

Different assumptions are possible:

*i) no CPV*

fit for  $x$  and  $y$  only

*ii) no direct CPV*

fit for  $x$ ,  $y$  and  $|q/p|$

*iii) CPV fully allowed*

fit for  $x$ ,  $y$ ,  $|q/p|$ ,  $\lambda_f$

+ hadronic parameters

(strong phases, amp. ratios)

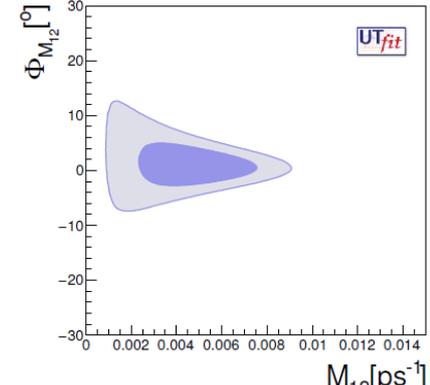
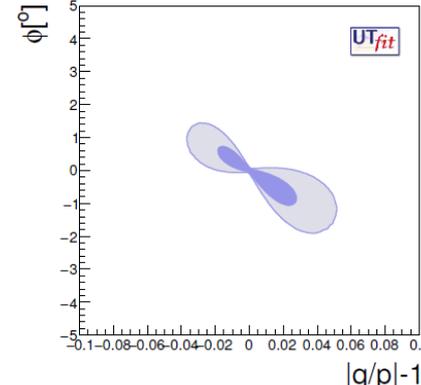
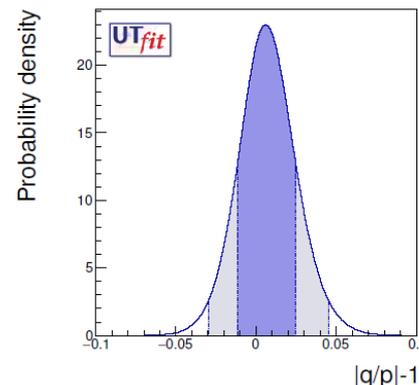
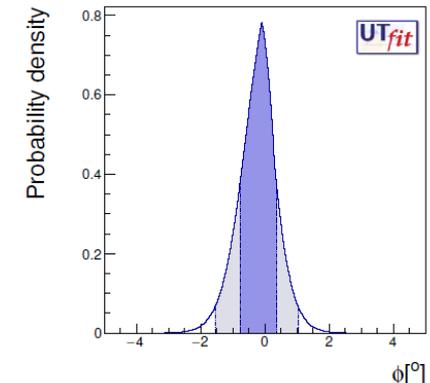
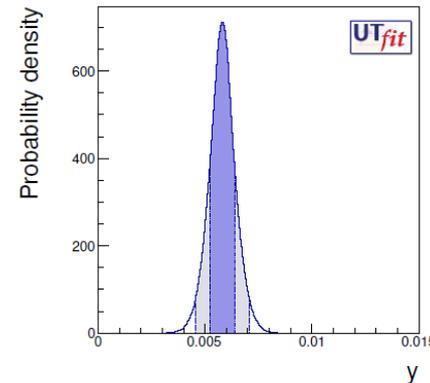
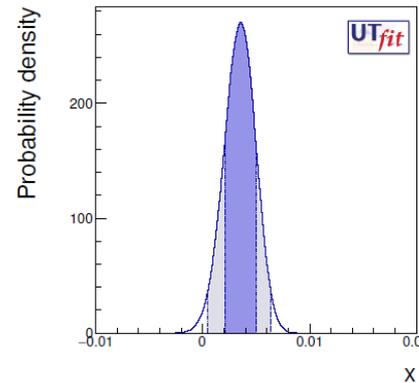
# fit results - no direct CPV

parameter	result @ 68% prob.	95% prob. range
$ M_{12} $ [ $\text{ps}^{-1}$ ]	$(4.3 \pm 1.8) \cdot 10^{-3}$	$[0.6, 7.5] \cdot 10^{-3}$
$ \Gamma_{12} $ [ $\text{ps}^{-1}$ ]	$(14.1 \pm 1.4) \cdot 10^{-3}$	$[11.1, 17.3] \cdot 10^{-3}$
$\Phi_{M_{12}}$ [ $^\circ$ ]	$(0.8 \pm 2.6)$	$[-5.8, 8.8]$
$x$	$(3.5 \pm 1.5) \cdot 10^{-3}$	$[0.5, 6.3] \cdot 10^{-3}$
$y$	$(5.8 \pm 0.6) \cdot 10^{-3}$	$[4.5, 7.1] \cdot 10^{-3}$
$ q/p  - 1$	$0.007 \pm 0.018$	$[-0.030, 0.045]$
$\phi$ [ $^\circ$ ]	$-0.21 \pm 0.57$	$[-1.53, 1.02]$

- $y$  well determined,  $x$  still uncertain
- $|q/p|$  is well compatible with 1
- phases are all compatible with 0

**NO EVIDENCE FOR CPV**  
**...YET...**

UTfit, 1402.1664, L. Silvestrini, CHARM 2015

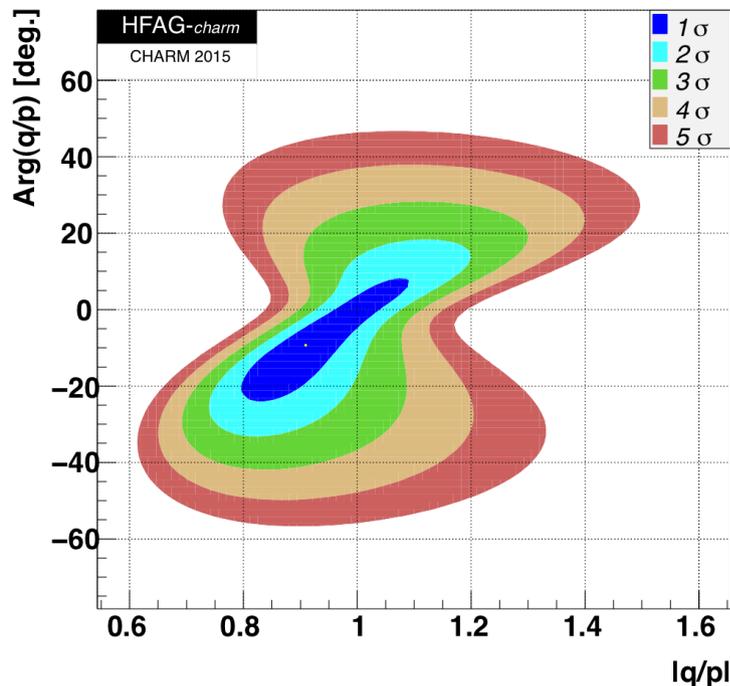
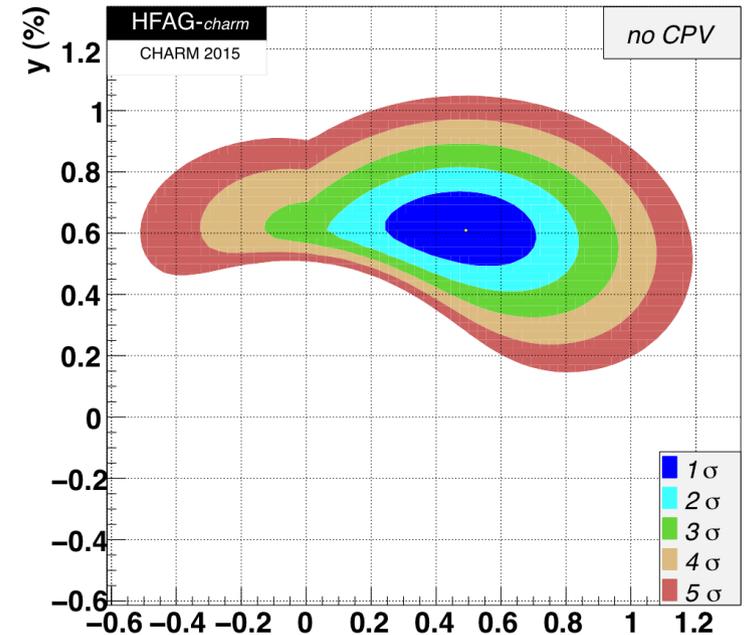


**Bayesian Fit**  
Floated parameters:

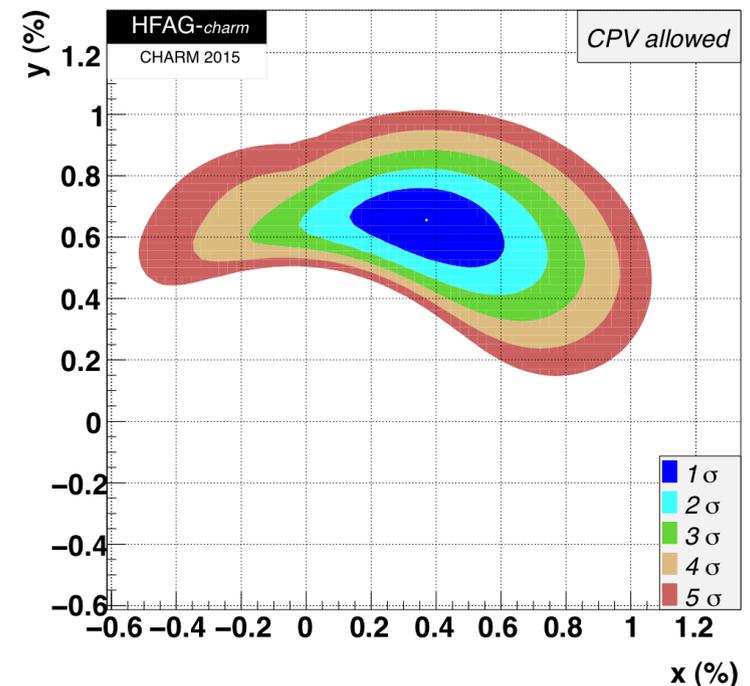
$$x, y, \left| \frac{q}{p} \right|, R_{K\pi}, \delta_{K\pi}, \delta_{K\pi\pi}$$

# fit results - no CPV, full CPV

Parameter	No CPV	No direct CPV in DCS decays	CPV-allowed	95% CL Interval
$x$ (%)	$0.49^{+0.14}_{-0.15}$	$0.44^{+0.14}_{-0.15}$	$0.37 \pm 0.16$	[0.06, 0.67]
$y$ (%)	$0.61 \pm 0.08$	$0.60 \pm 0.07$	$0.66^{+0.07}_{-0.10}$	[0.46, 0.79]
$\delta_{K\pi}$ (°)	$6.9^{+9.7}_{-11.2}$	$3.6^{+10.4}_{-12.1}$	$11.8^{+9.5}_{-14.7}$	[-21.1, 29.3]
$R_D$ (%)	$0.349 \pm 0.004$	$0.348 \pm 0.004$	$0.349 \pm 0.004$	[0.342, 0.357]
$A_D$ (%)	—	—	$-0.39^{+1.01}_{-1.05}$	[-2.4, 1.5]
$ q/p $	—	$1.002 \pm 0.014$	$0.91^{+0.12}_{-0.08}$	[0.77, 1.14]
$\phi$ (°)	—	$-0.07 \pm 0.6$	$-9.4^{+11.9}_{-9.8}$	[-28.3, 12.9]
$\delta_{K\pi\pi}$ (°)	$18.1^{+23.3}_{-23.8}$	$20.3^{+24.0}_{-24.3}$	$27.3^{+24.4}_{-25.4}$	[-23.3, 74.8]
$A_\pi$	—	$0.10 \pm 0.14$	$0.10 \pm 0.15$	[-0.19, 0.38]
$A_K$	—	$-0.14 \pm 0.13$	$-0.15 \pm 0.14$	[-0.42, 0.12]
$x_{12}$ (%)	—	$0.44^{+0.14}_{-0.15}$	—	[0.13, 0.69]
$y_{12}$ (%)	—	$0.60 \pm 0.07$	—	[0.45, 0.74]
$\phi_{12}$ (°)	—	$0.2 \pm 1.7$	—	[-4.1, 4.6]



HFAG 2015



# New Physics in the $\Delta C=2$ amplitude

NP enters through the local ME  $\langle D | H_{eff}^{\Delta C=2} | \bar{D} \rangle$

$$H_{eff}^{\Delta C=2} = \sum_{i=1}^5 C_i(\mu) Q_i(\mu) + \sum_{i=1}^3 \tilde{C}_i(\mu) \tilde{Q}_i(\mu) + H.c.$$

$$Q_1 = \bar{u}_L^\alpha \gamma_\mu c_L^\alpha \bar{u}_L^\beta \gamma^\mu c_L^\beta \quad (\text{SM})$$

$$Q_2 = \bar{c}_R^\alpha u_L^\alpha \bar{c}_R^\beta u_L^\beta$$

$$Q_3 = \bar{c}_R^\alpha u_L^\beta \bar{c}_R^\beta u_L^\alpha$$

$$Q_4 = \bar{c}_R^\alpha u_L^\alpha \bar{c}_L^\beta u_R^\beta$$

$$Q_5 = \bar{c}_R^\alpha u_L^\beta \bar{c}_L^\beta u_R^\alpha$$

$$\tilde{Q}_1 = \bar{c}_R^\alpha \gamma_\mu u_R^\alpha \bar{c}_R^\beta \gamma^\mu u_R^\beta$$

$$\tilde{Q}_2 = \bar{c}_L^\alpha u_R^\alpha \bar{c}_L^\beta u_R^\beta$$

$$\tilde{Q}_3 = \bar{c}_L^\alpha u_R^\beta \bar{c}_L^\beta u_R^\alpha$$

**7 new operators beyond SM involving quarks with different chiralities**

$H_{eff}$  can be recast in terms of the high-scale  $C_i(\Lambda)$

-  $C_i(\Lambda)$  can be extracted from the data (one by one)

	95% upper limit (GeV <sup>-2</sup> )	Lower limit on $\Lambda$ (TeV)
$\text{Im}C_D^1$	$[-1.4, 2.0] \cdot 10^{-14}$	$7.1 \cdot 10^3$
$\text{Im}C_D^2$	$[-2.5, 1.7] \cdot 10^{-15}$	$20.0 \cdot 10^3$
$\text{Im}C_D^3$	$[-2.4, 3.5] \cdot 10^{-14}$	$5.3 \cdot 10^3$
$\text{Im}C_D^4$	$[-5.2, 7.7] \cdot 10^{-16}$	$36.0 \cdot 10^3$
$\text{Im}C_D^5$	$[-5.3, 7.9] \cdot 10^{-15}$	$11.2 \cdot 10^3$

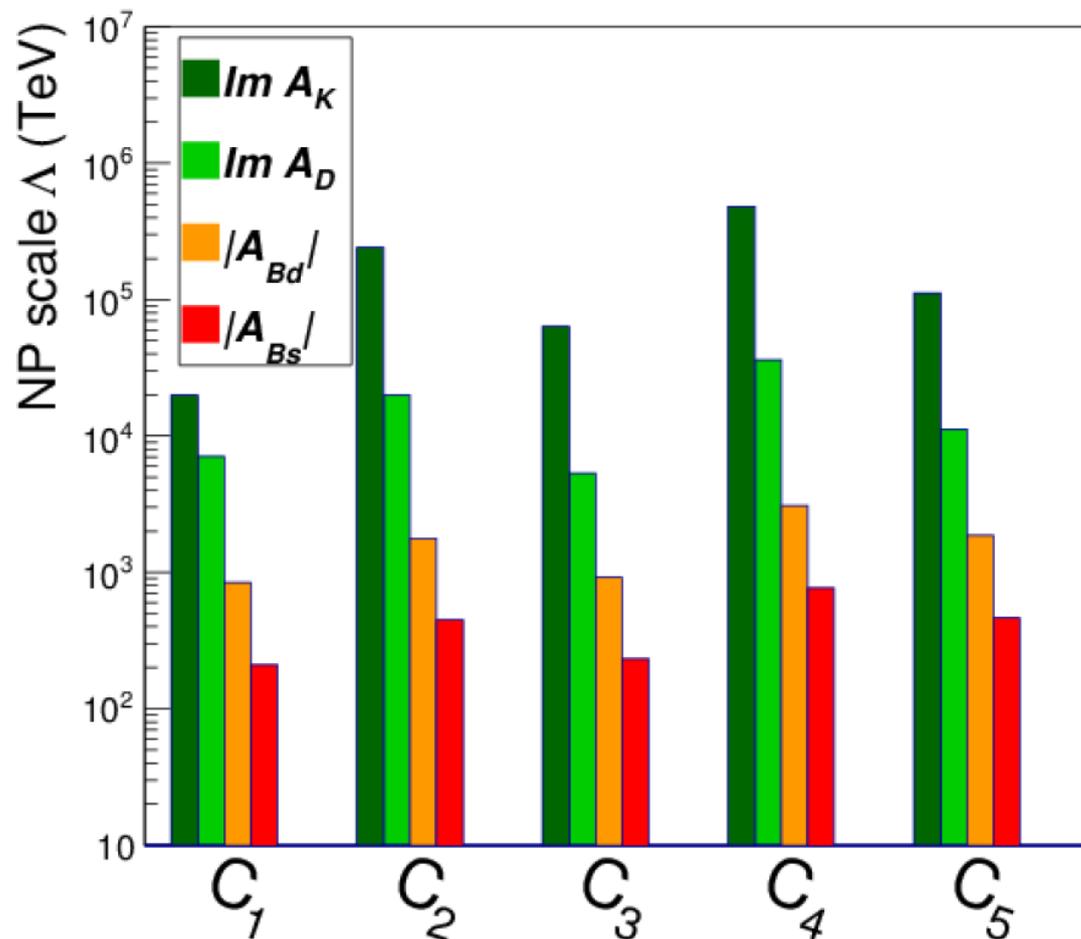
- the NP scale  $\Lambda$  is defined as:

$$\Lambda = \sqrt{\frac{L \times F_i}{C_i(\Lambda)}}$$

NP loop ( $L$ ) and flavour ( $F_i$ )  
couplings are model dependent:  
shown NP scales assume  $L=1$  and  
 $|F_i|=1$  with arbitrary phases

# Comparison with other meson mixing

$\Lambda$ (TeV)	K CPV	D CPV	$B_d$ CPC	$B_s$ CPC
lower bound	$4.8 \times 10^5$	$3.6 \times 10^4$	$3.1 \times 10^3$	760



# Summary

A precise calculation of the  $D$ - $\bar{D}$  mixing parameters is not feasible at present. A technique for computing long-distance contributions is eagerly awaited

Yet the flavour structure of mixing and decay amplitudes is such that (i) SM CPV in mixing is very small, (ii) CPC measurements, CPV in mixing, and CPV in the interference of mixed and unmixed decays can all be combined to constrain the mixing parameters

No sign of deviation from the SM so far (i.e. no CPV in mixing found). Yet CPV in  $\bar{D}$ - $D$  mixing shows its NP sensitivity by putting a strong lower bound on the scale of NP with generic flavour structure and  $O(1)$  couplings

# Backup

# Comparison with other meson mixing

$\Lambda$  (TeV)

K

D

$B_d$

$B_s$

FC~1

$5 \times 10^5$

$3.5 \times 10^4$

$3.3 \times 10^3$

880

FC~SM

113

8.5

21

27

