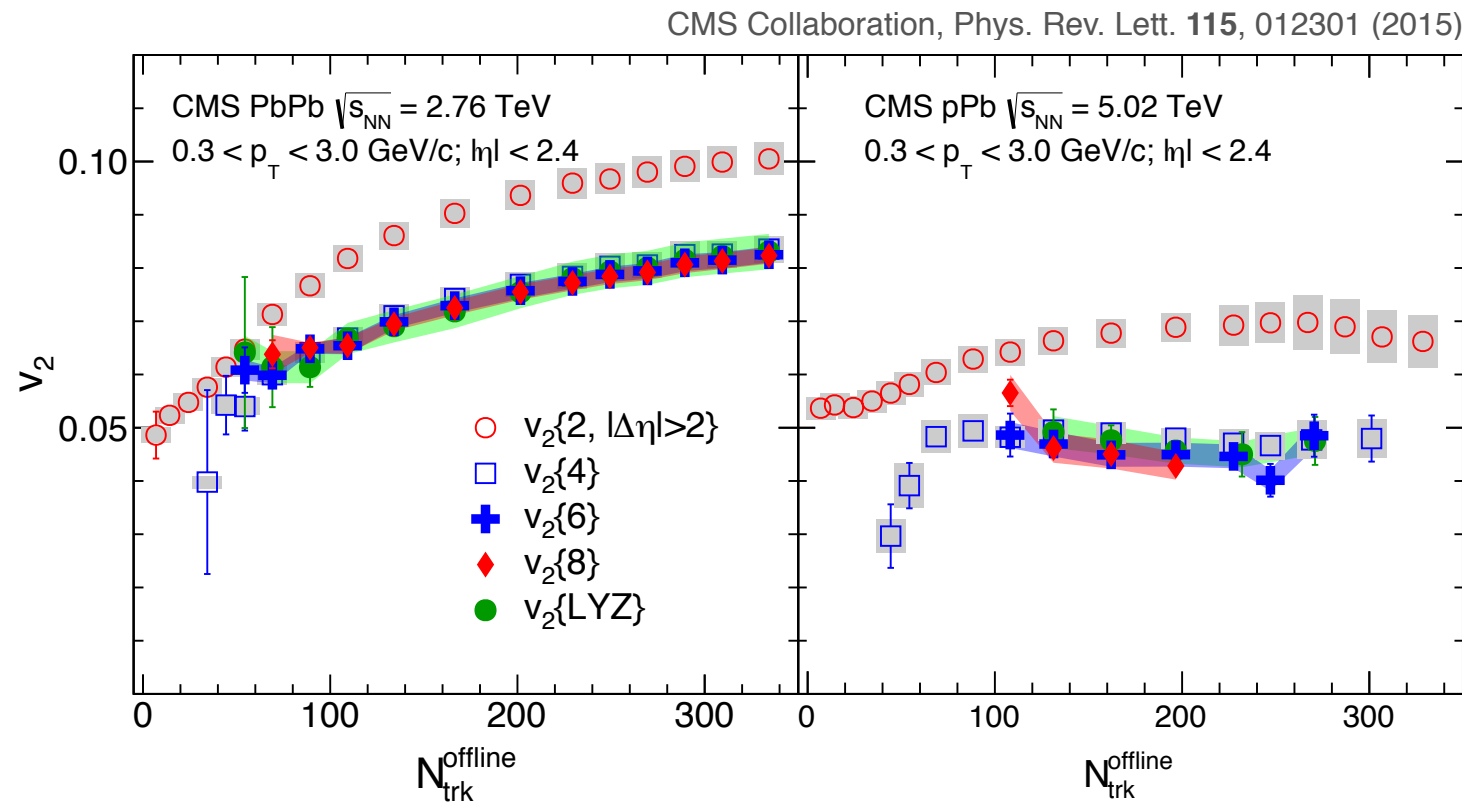


# Jet energy loss in small systems with finite-size effects and running coupling

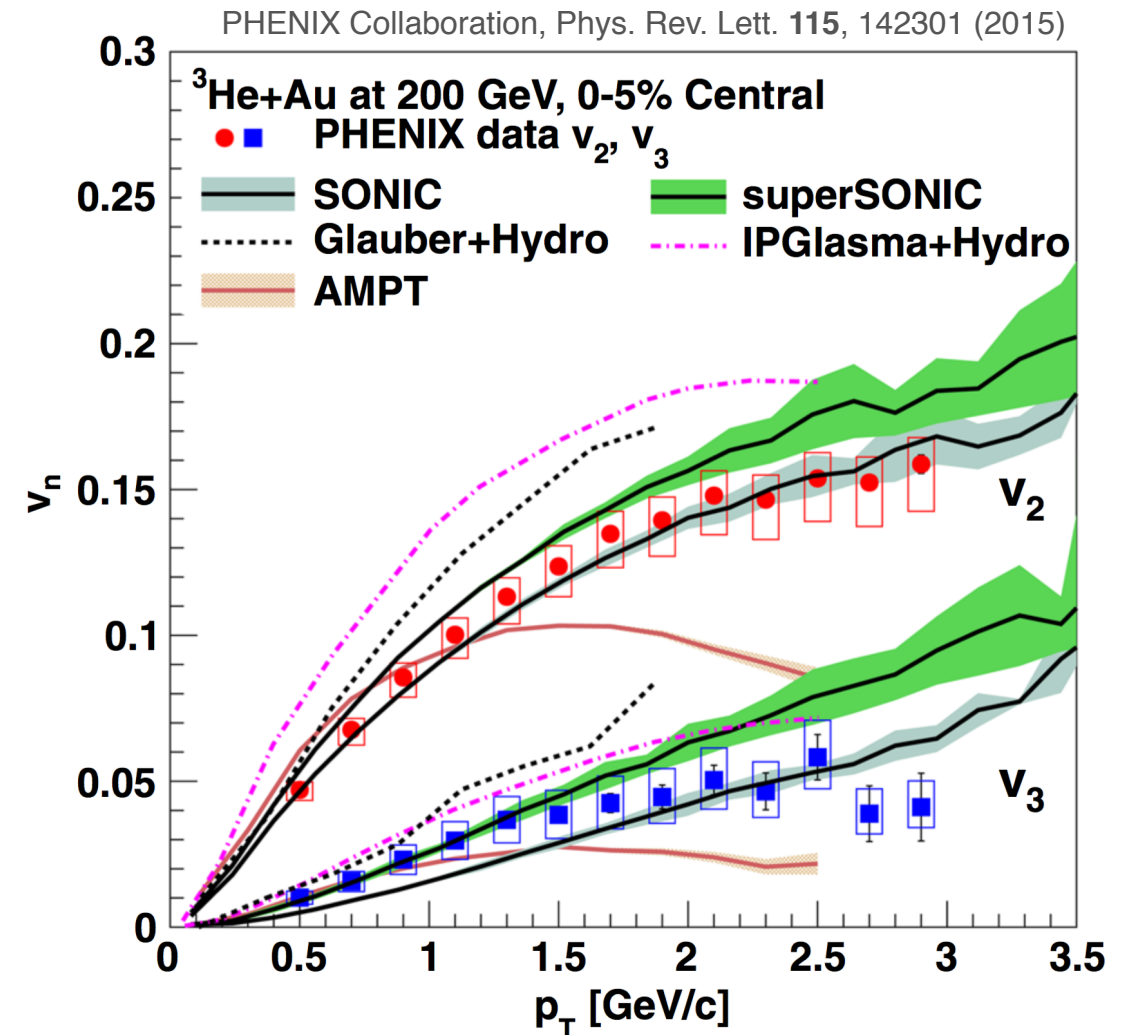
**Chanwook Park**

Collaboration with C. Shen, S. Jeon, C. Gale

# Collectivity in small systems



Pb-Pb/p-Pb CMS

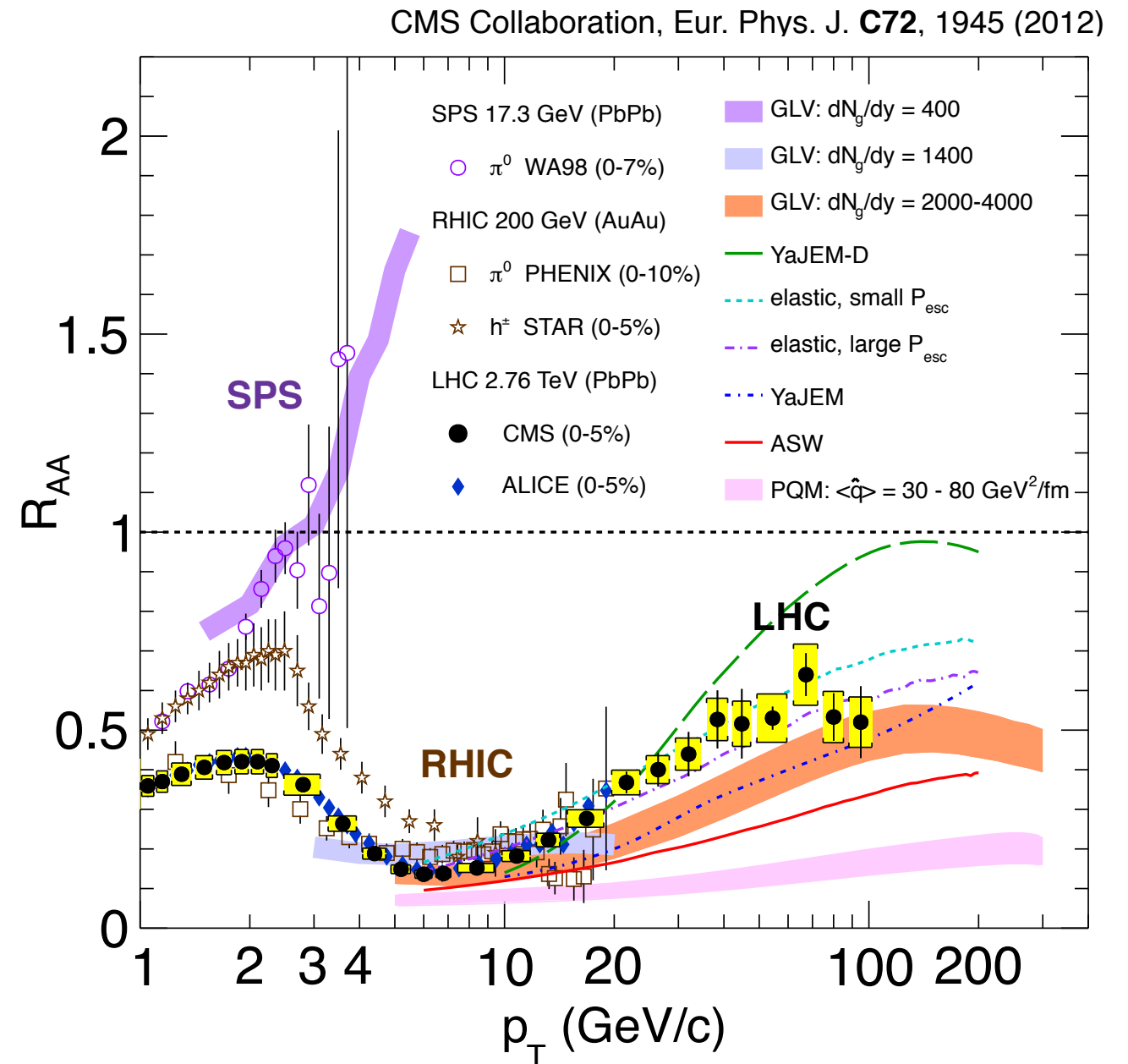


$^3\text{He-Au}$  at 200GeV PHENIX

- Collective behaviour was measured in central collisions of small systems
- This suggests strongly coupled medium in small systems

# A Tool for studying QGP : Jets

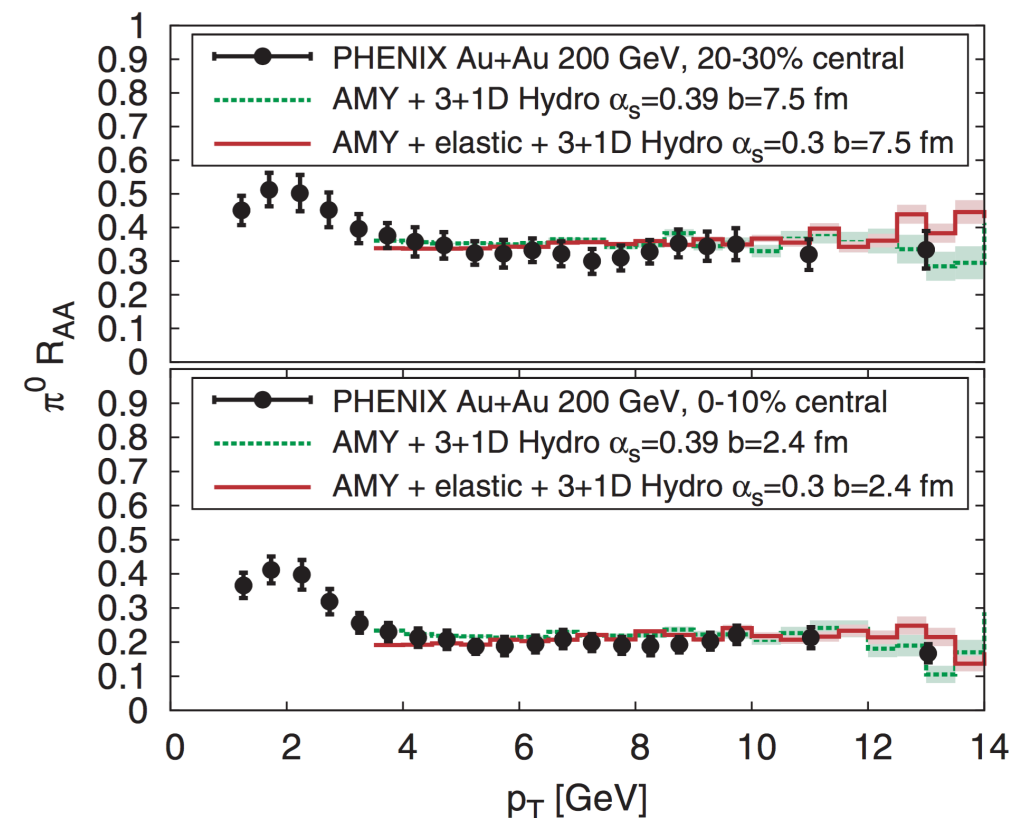
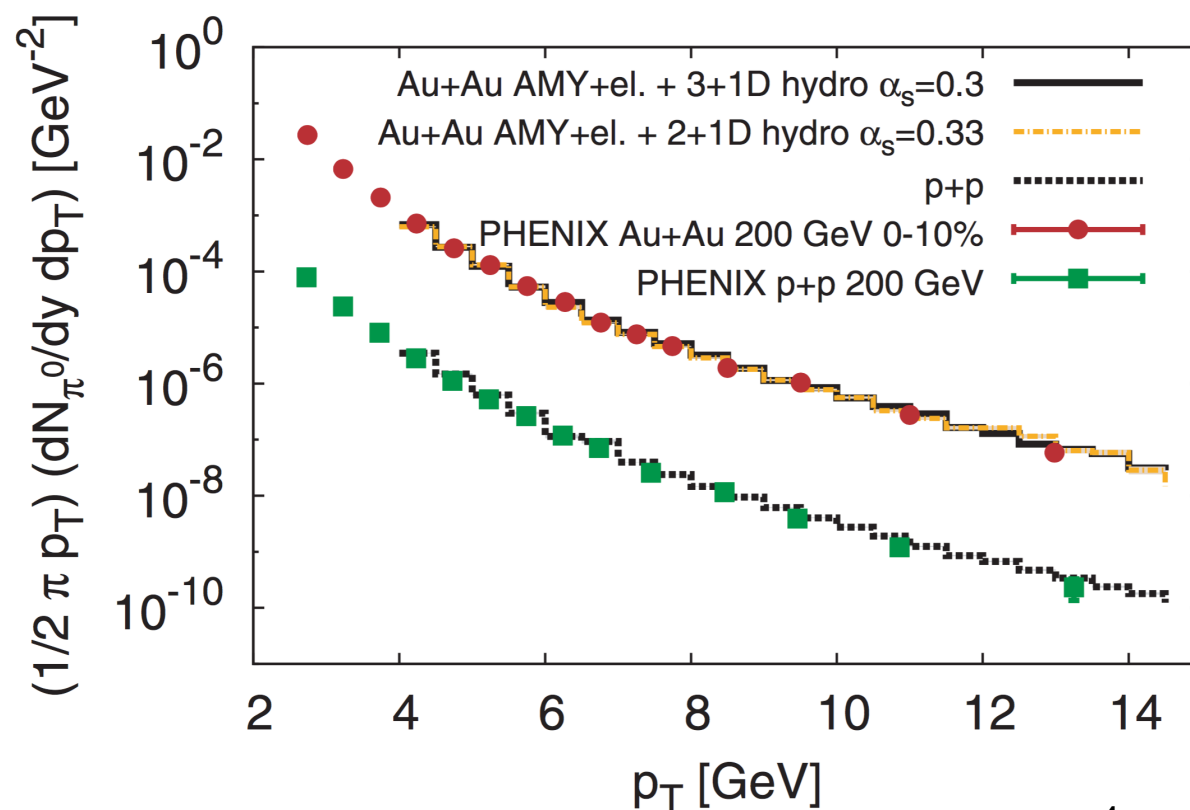
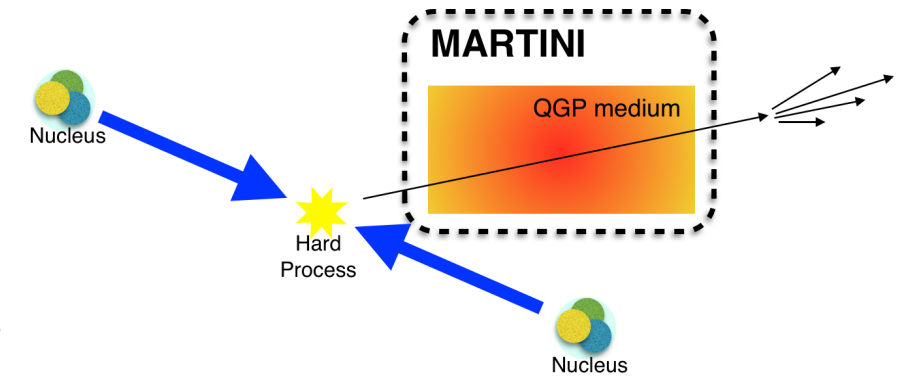
- Jet quenching : due to colour opacity of a strongly coupled medium
- Strong suppression in AA collisions was measured at RHIC and the LHC
- **Similar behaviour in small systems?**



# Jet-medium interaction

● **MARTINI** B. Schenke, S. Jeon, C. Gale, Phys. Rev. **C80**, 054913 (2009)

- Event generator for hard jets in heavy ion collisions
- Based on PYTHIA 8.2
- AMY(Arnold-Moore-Yaffe) radiation scheme as well as collisional processes
- E-by-E hydrodynamics background is available

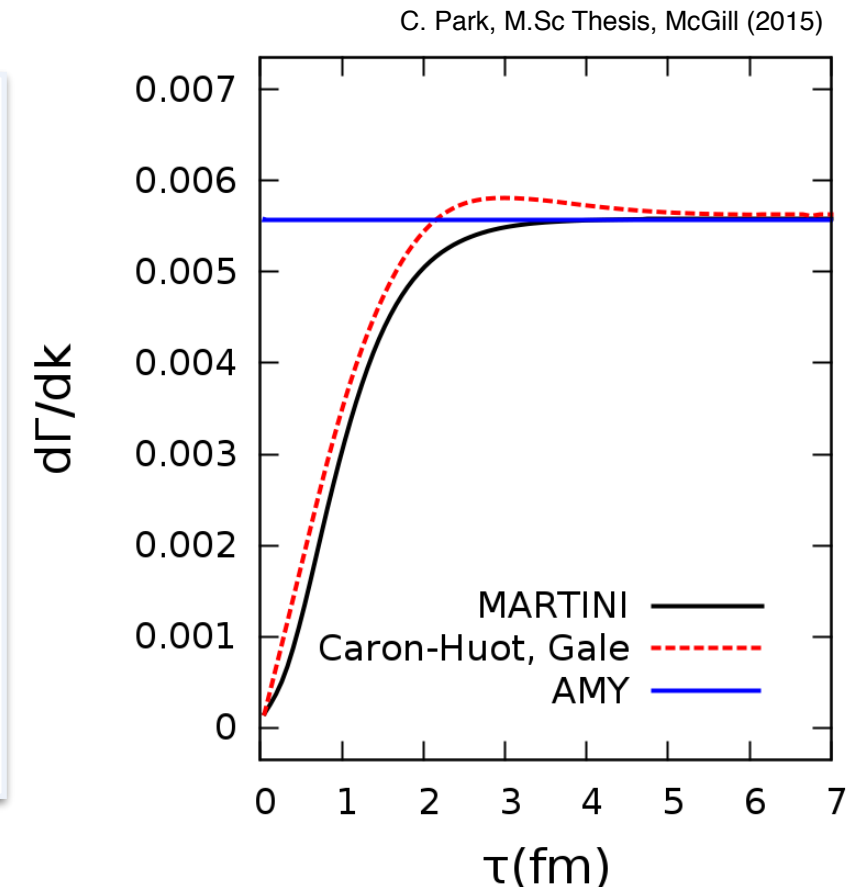
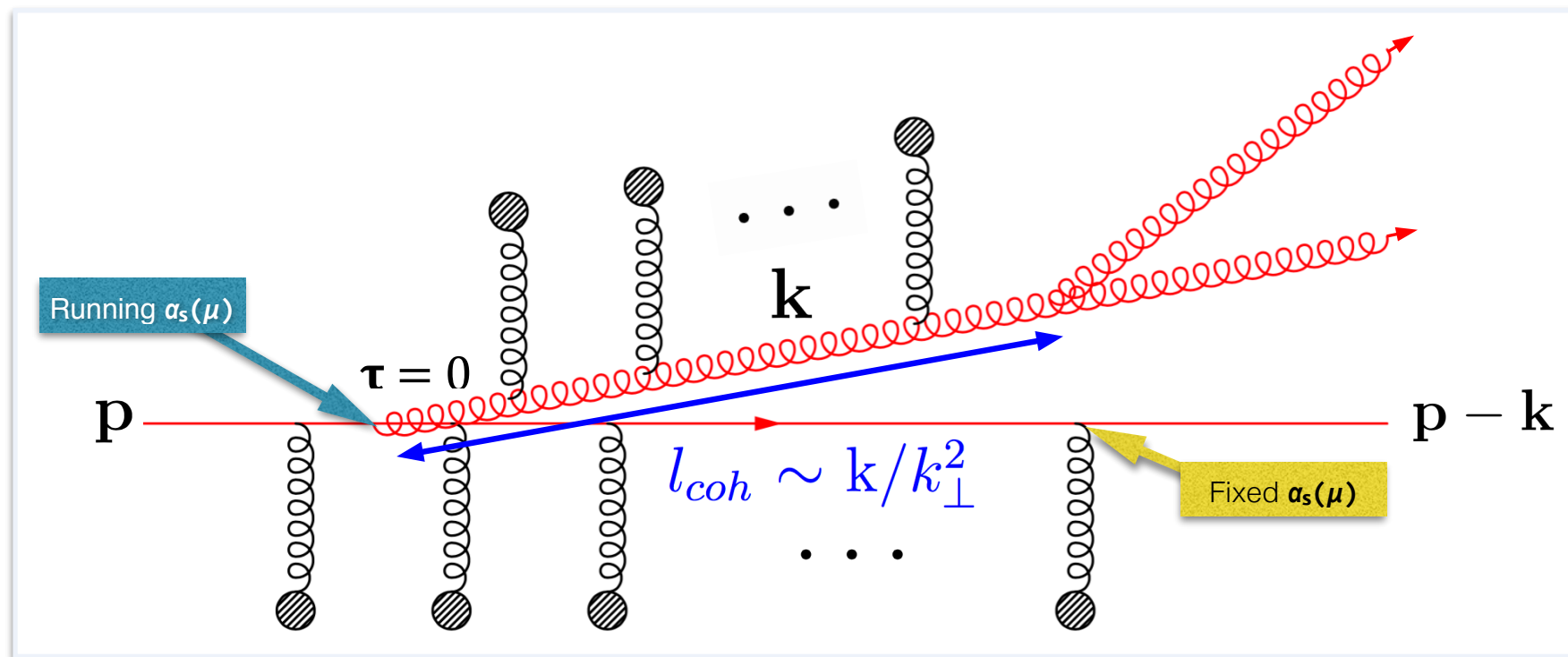




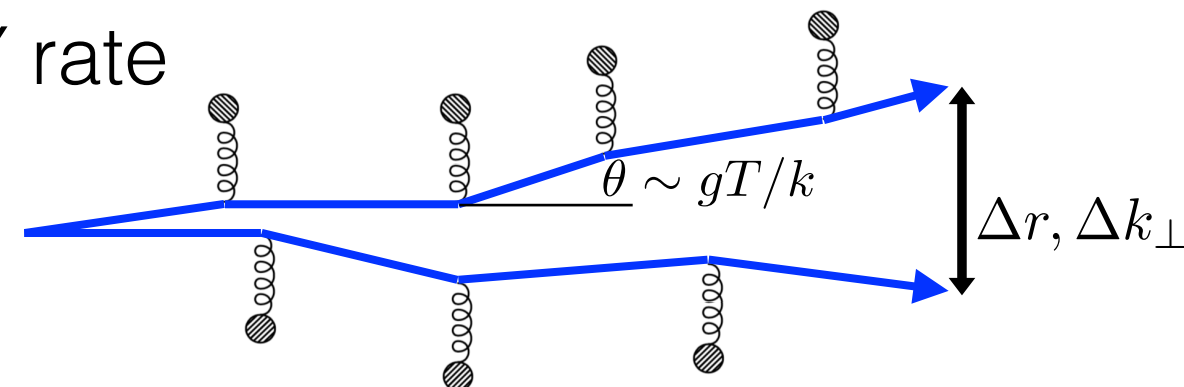
# New developments in MARTINI

- Finite-size effects on radiation

S. Caron-Huot and C. Gale, Phys. Rev. C82, 064902 (2010)



- Finite formation time of radiation  
: Time dependence is applied in AMY rate
- Implementation : Random walk  
(separation condition  $\Delta r \Delta k_{\perp} > \frac{1}{2}$ )



# New developments in MARTINI

- Running coupling

C. Young, B. Schenke, S. Jeon, and C. Gale, Nucl. Phys. A910-911, 494 (2013)

- Origin of  $g_s$  in the AMY rate

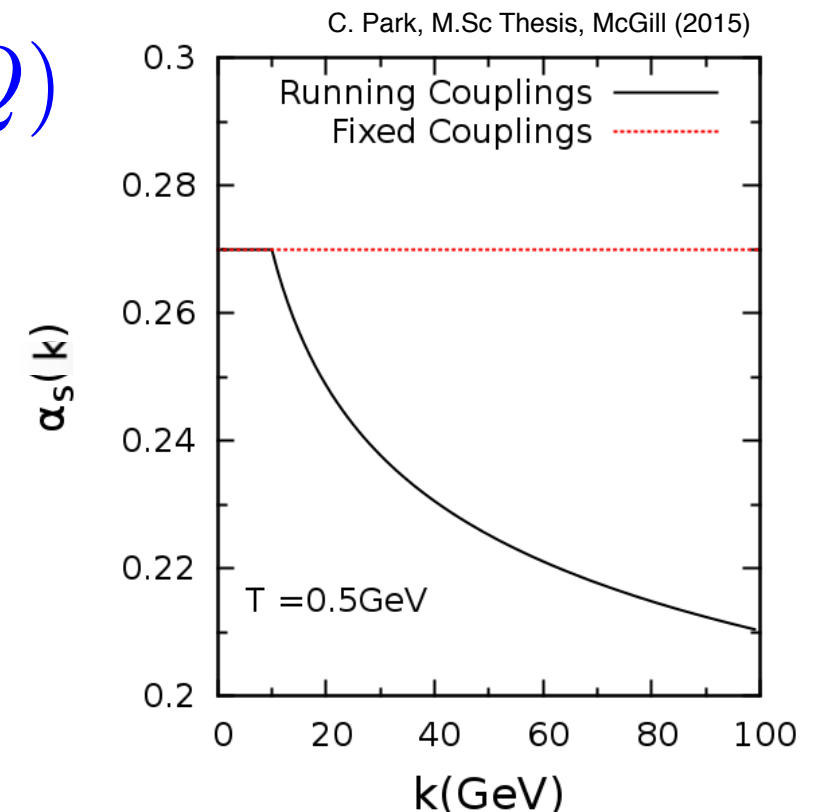
$$\frac{d\Gamma(p, k)}{dk} = \frac{C_s g_s^2}{16\pi p^7} \frac{1}{1 \pm e^{-k/T}} \frac{1}{1 \pm e^{-(p-k)/T}} \times \left\{ \begin{array}{ll} \frac{1+(1-x)^2}{x^3(1-x)^2} & q \rightarrow qq \\ N_f \frac{x^2+(1-x)^2}{x^2(1-x)^2} & g \rightarrow qq \\ \frac{1+x^4+(1-x)^4}{x^3(1-x)^3} & g \rightarrow gg \end{array} \right\} \\ \times \int \frac{d^2 \mathbf{h}}{(2\pi)^2} 2\mathbf{h} \cdot \text{Re } \mathbf{F}(\mathbf{h}, p, k),$$

- $g_s^2$ : Gluon radiation vertex  $\rightarrow g_s^2 = 4\pi\alpha_s(Q)$

- In MARTINI,  $Q \sim \langle |k_\perp| \rangle = (\hat{q}k)^{\frac{1}{4}}$

$$\langle k_\perp^2 \rangle = \hat{q} l_{coh} \rightarrow \langle k_\perp^2 \rangle = k / \langle k_\perp^2 \rangle$$

- $g_s^2$  in the integral equation  
: elastic scattering (soft)  $\rightarrow$  fixed



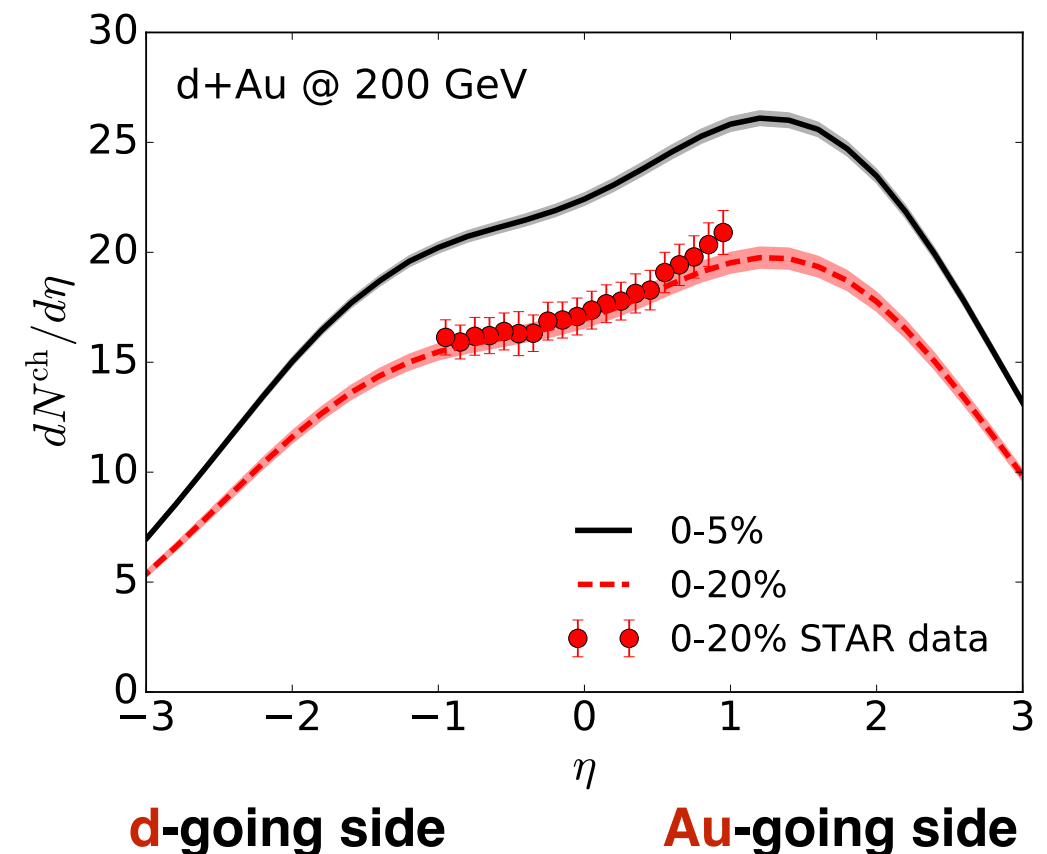
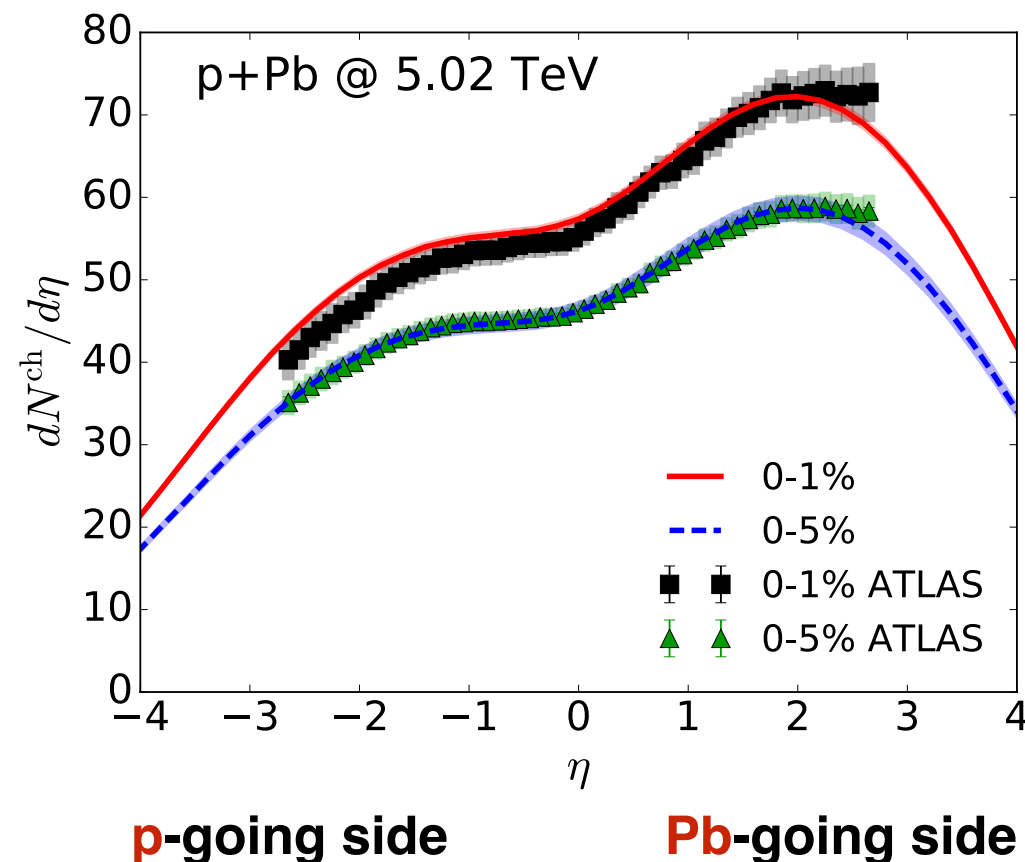
# 3+1D hydrodynamic simulations

## MUSIC

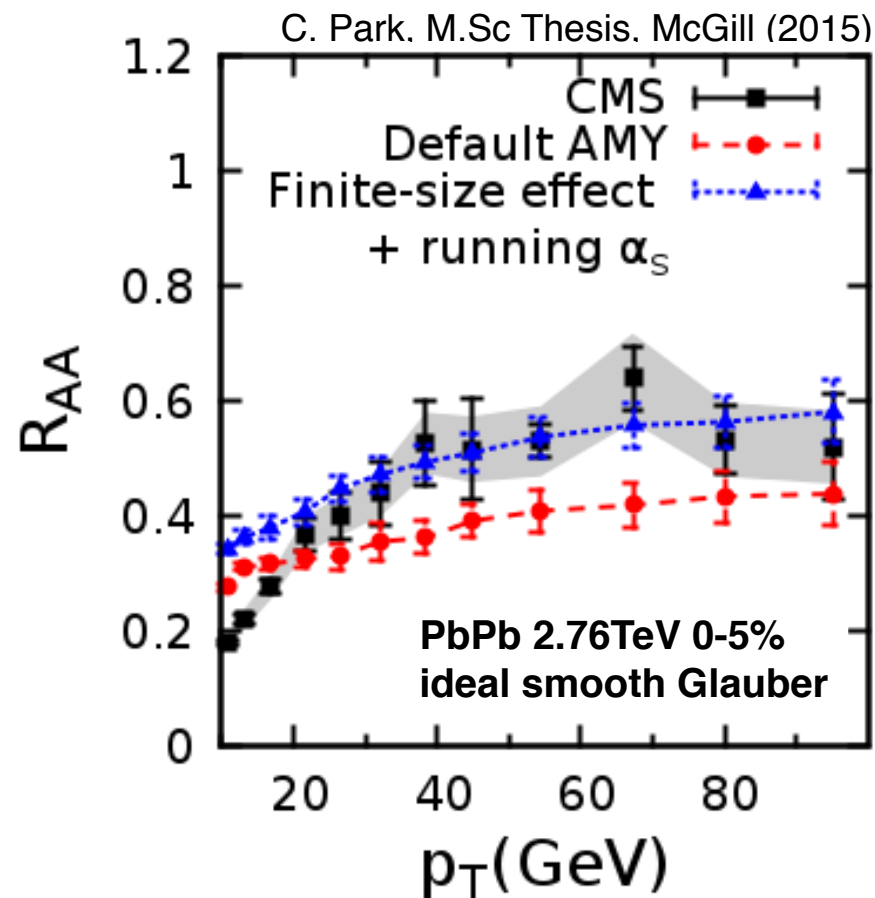
B. Schenke, S. Jeon, C. Gale, Phys. Rev. C82, 014903 (2009)

- 3+1D : Suitable for studying non-trivial longitudinal dynamics and rapidity dependence of jet observables
- Event-by-event simulation + MC Glauber initial condition

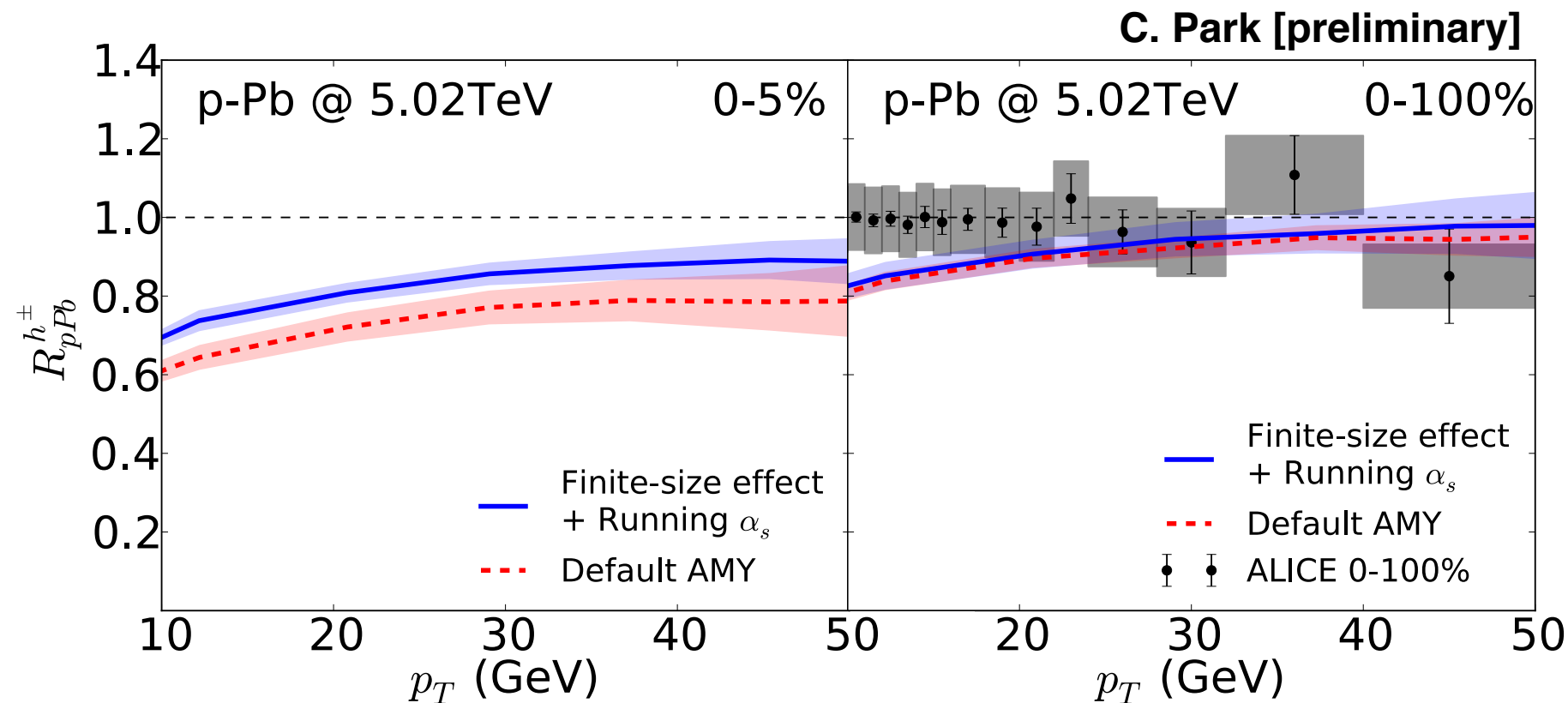
C. Shen et al. arXiv:1609.02590v1 [nucl-th]



# Finite-size effects & running coupling



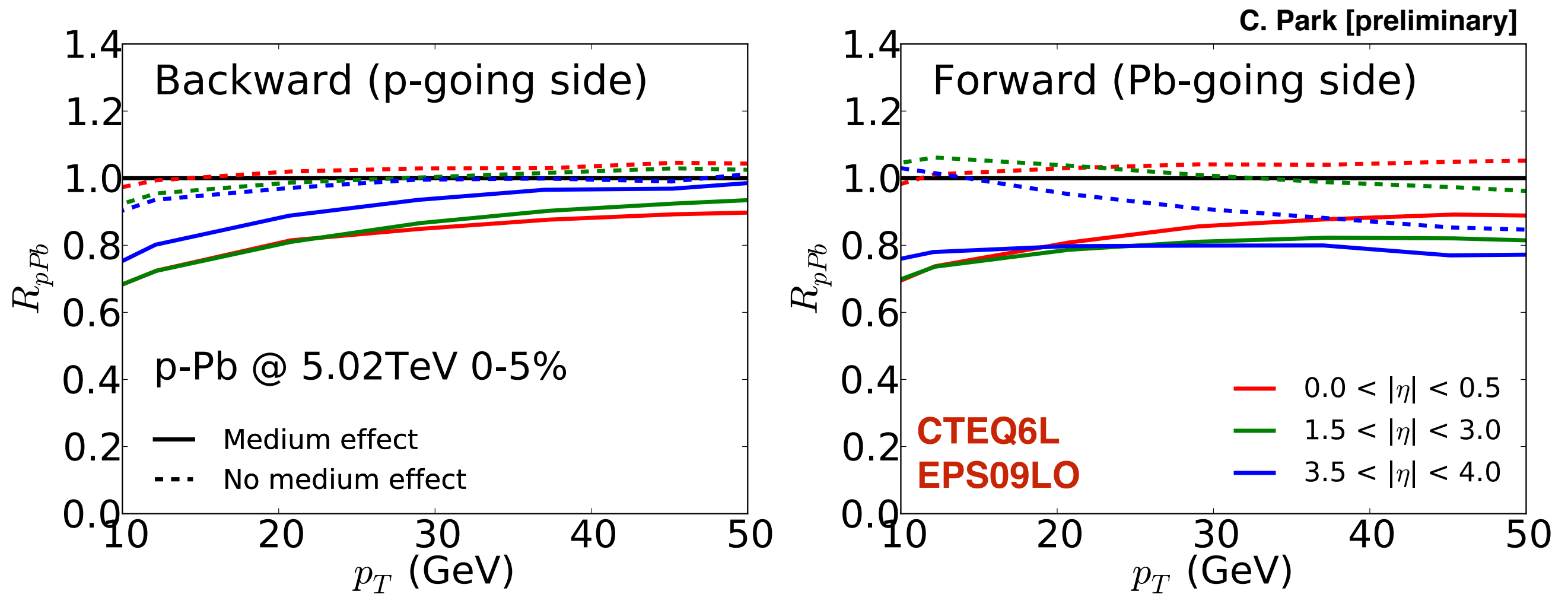
Pb-Pb @ 2.76TeV



p-Pb@ 5.02TeV

- Two effects give constant shifts in  $R_{AA}$  &  $R_{pA}$
- For large systems, the new prescriptions were favoured, but underestimated ALICE data @ 10-20GeV in small systems.

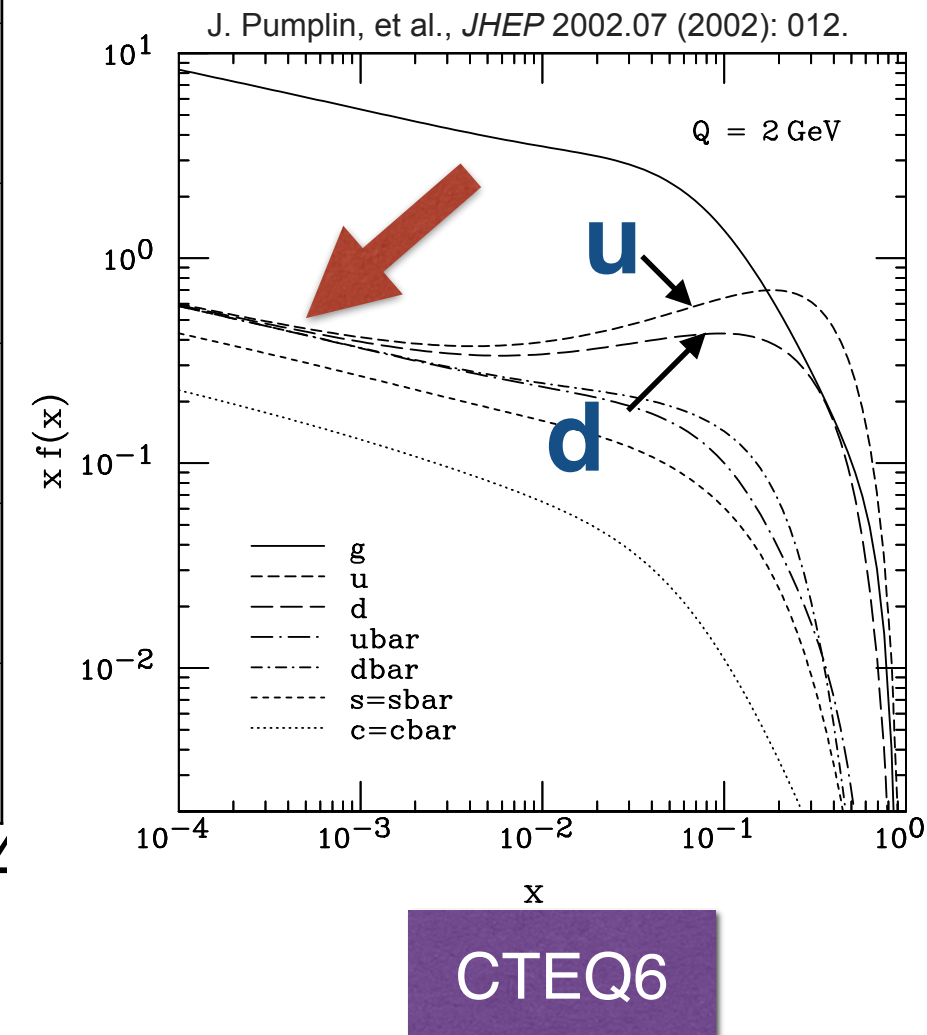
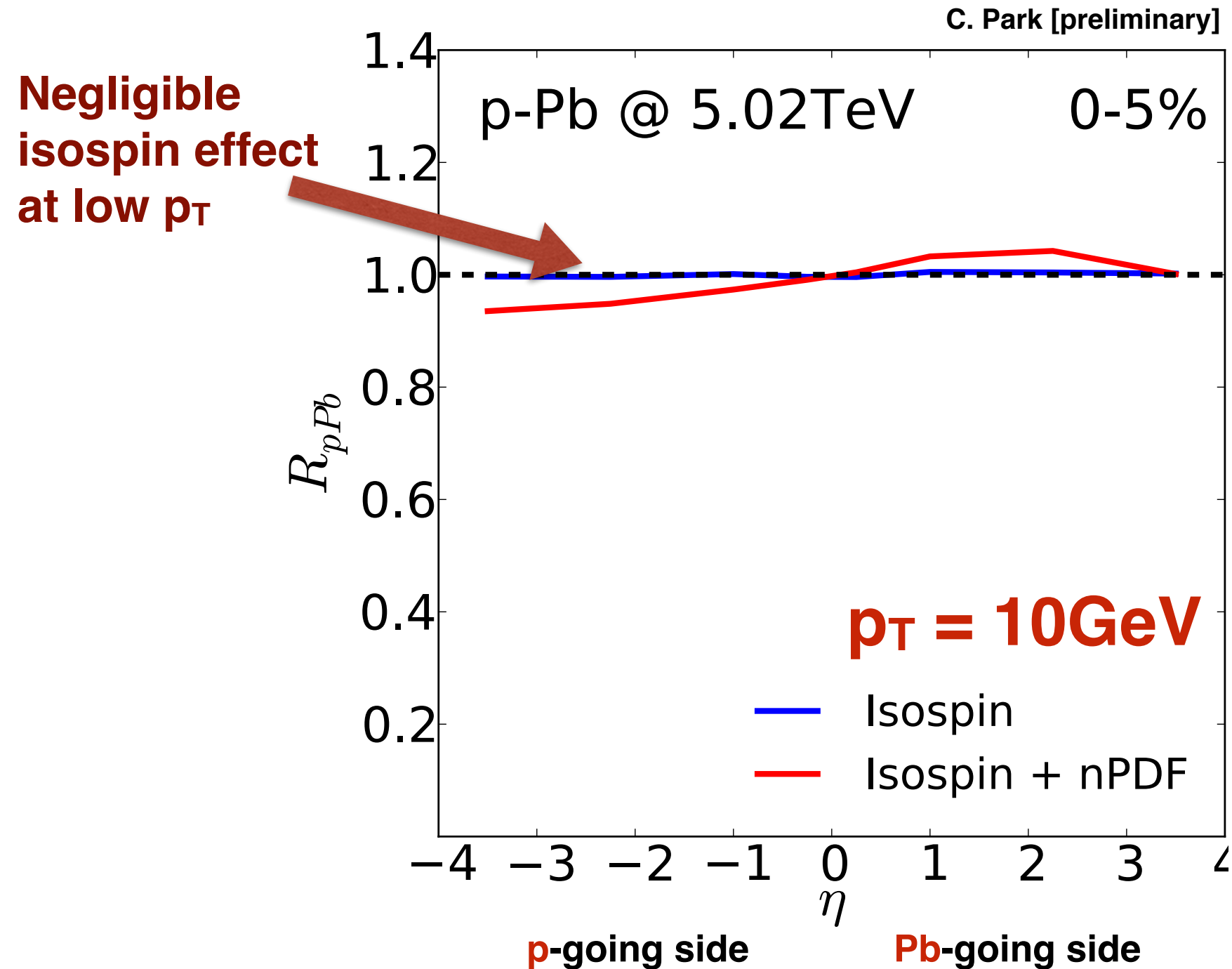
# Rapidity dependent energy loss



- Net effect : Convolution of medium effect + nuclear PDF + isospin
- Better understanding of their effects in rapidity directions is required.

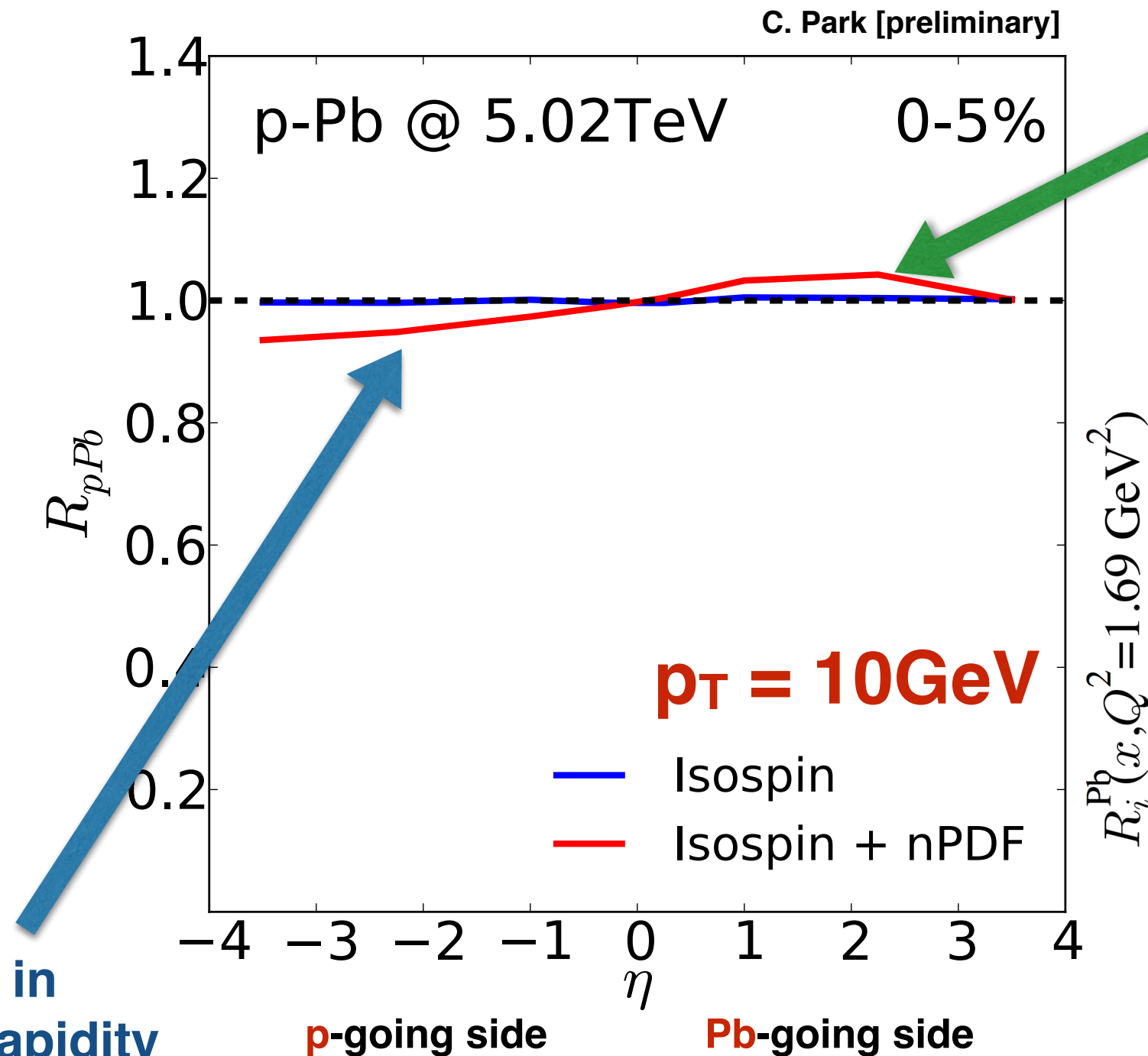
# Rapidity dependent energy loss

- Dominant nuclear PDF effect in low  $p_T$   $R_{pPb}$



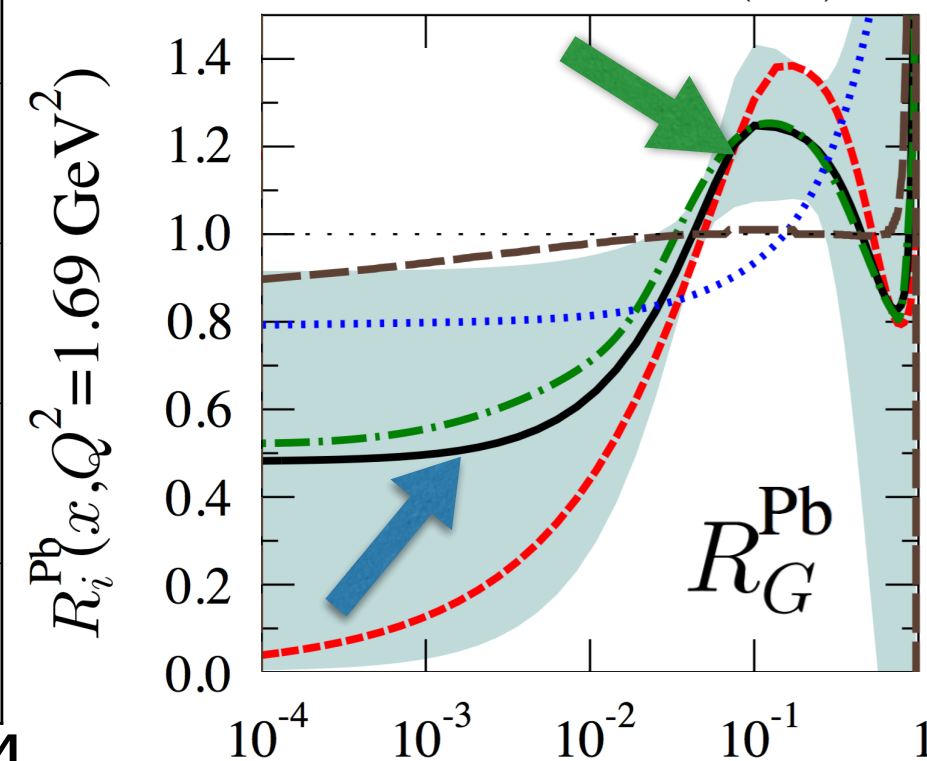
# Rapidity dependent energy loss

- Dominant nuclear PDF effect in low  $p_T$   $R_{pPb}$



Anti-shadowing  
 $x \sim 0.1$  from Pb

K.J. Eskola, et al., *JHEP* 2009.04 (2009): 065.



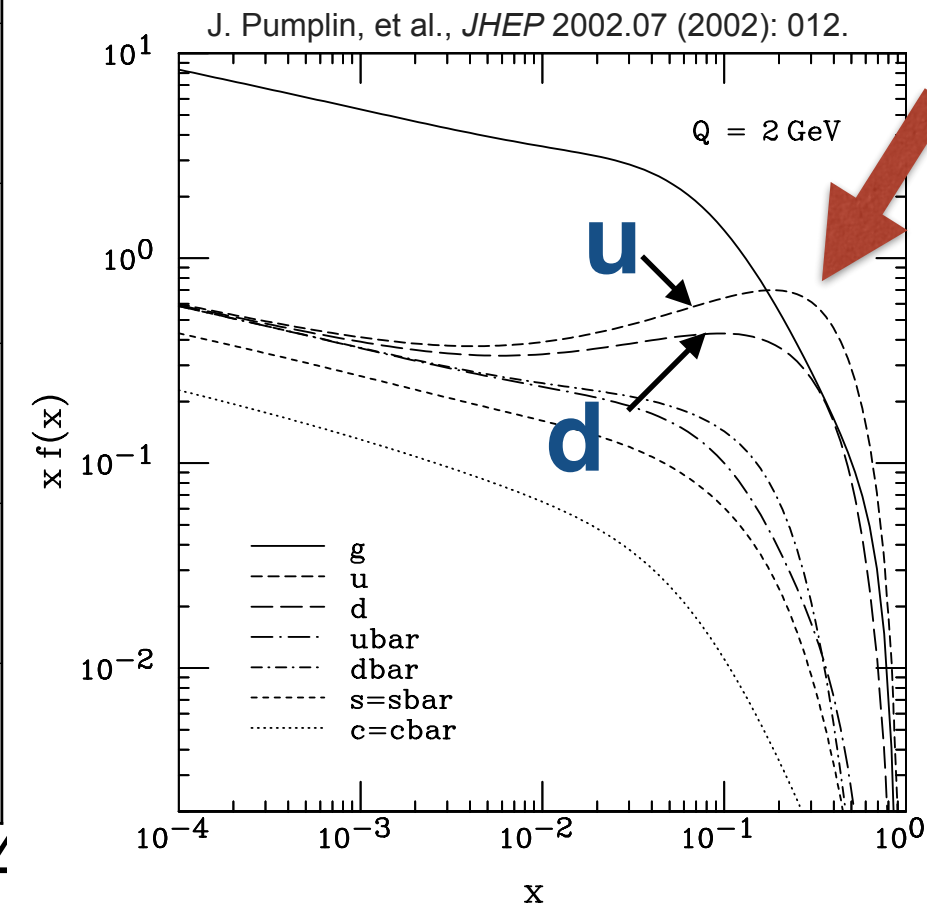
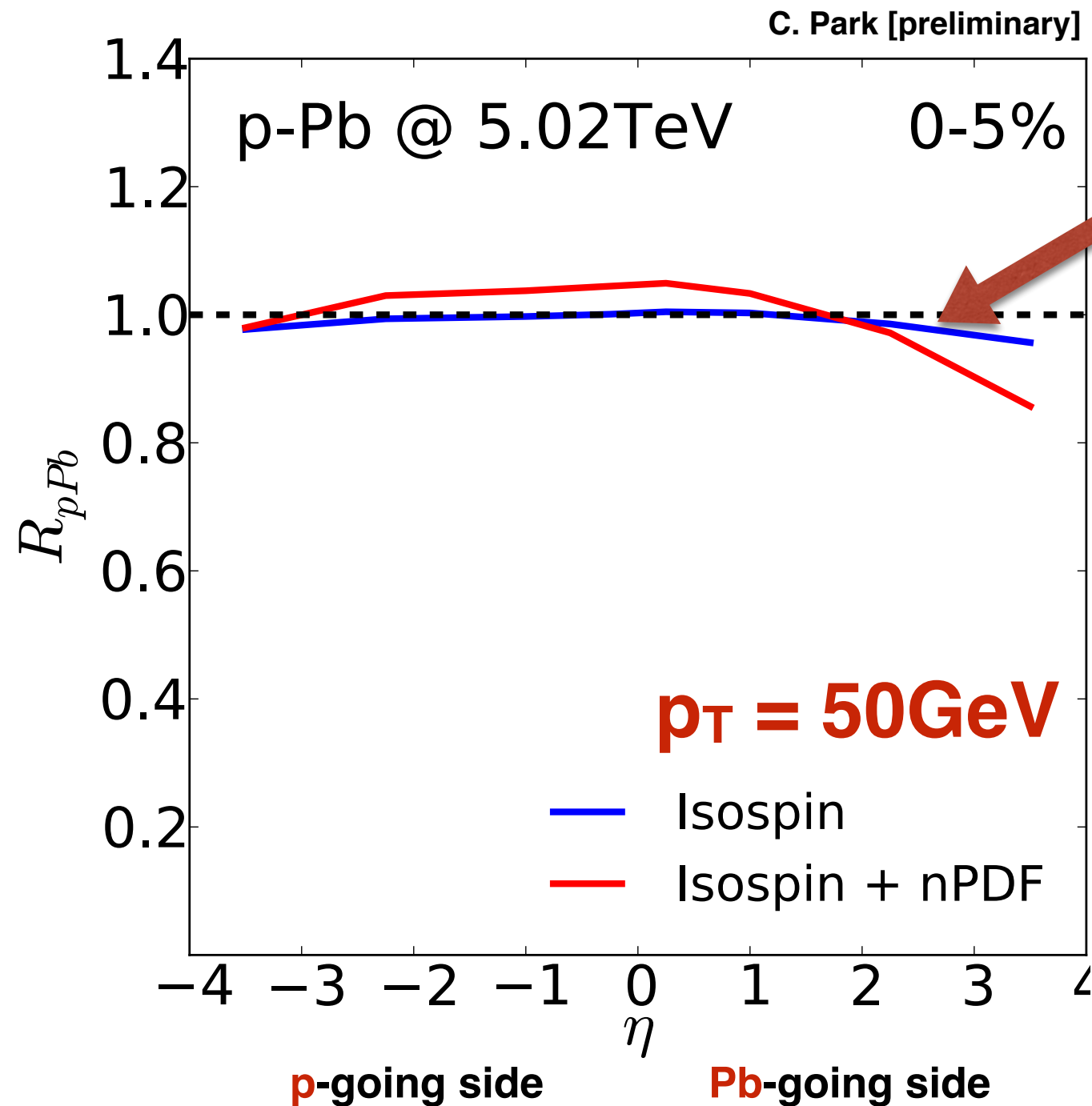
EPS09LO



# Rapidity dependent energy loss

- Isospin effect and anti-shadowing in high  $p_T$   $R_{pPb}$

high  $p_T$   
= larger  $x$



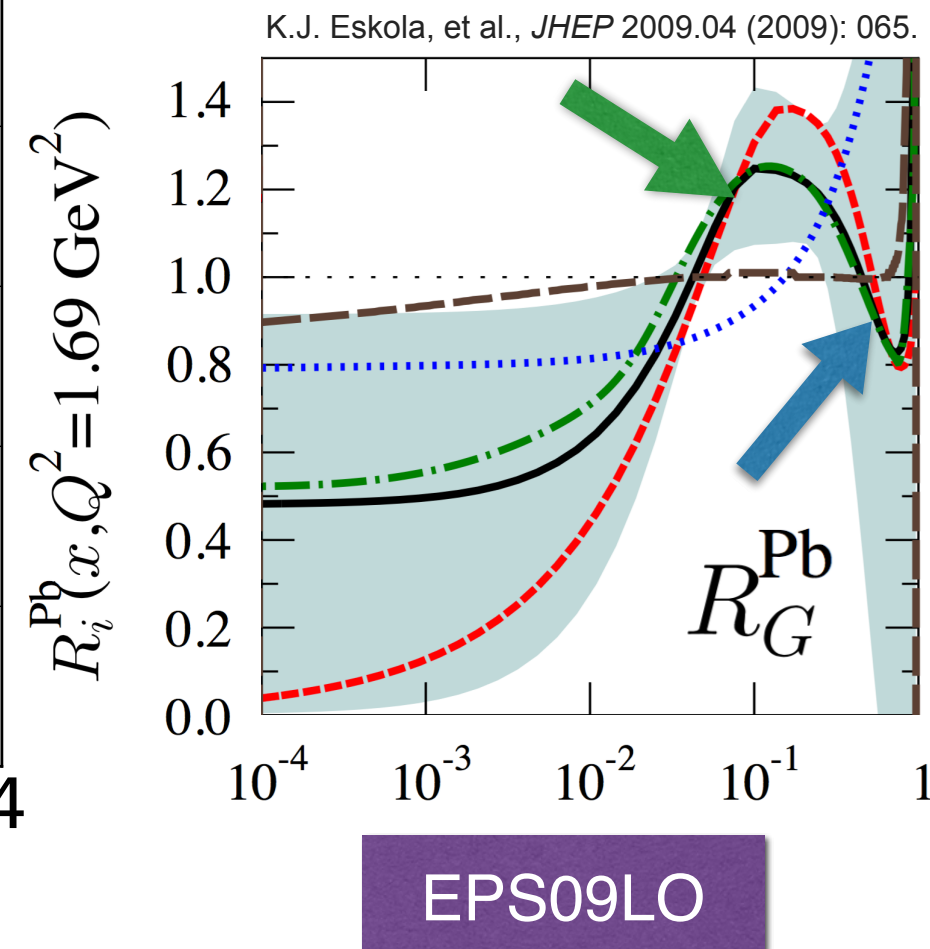
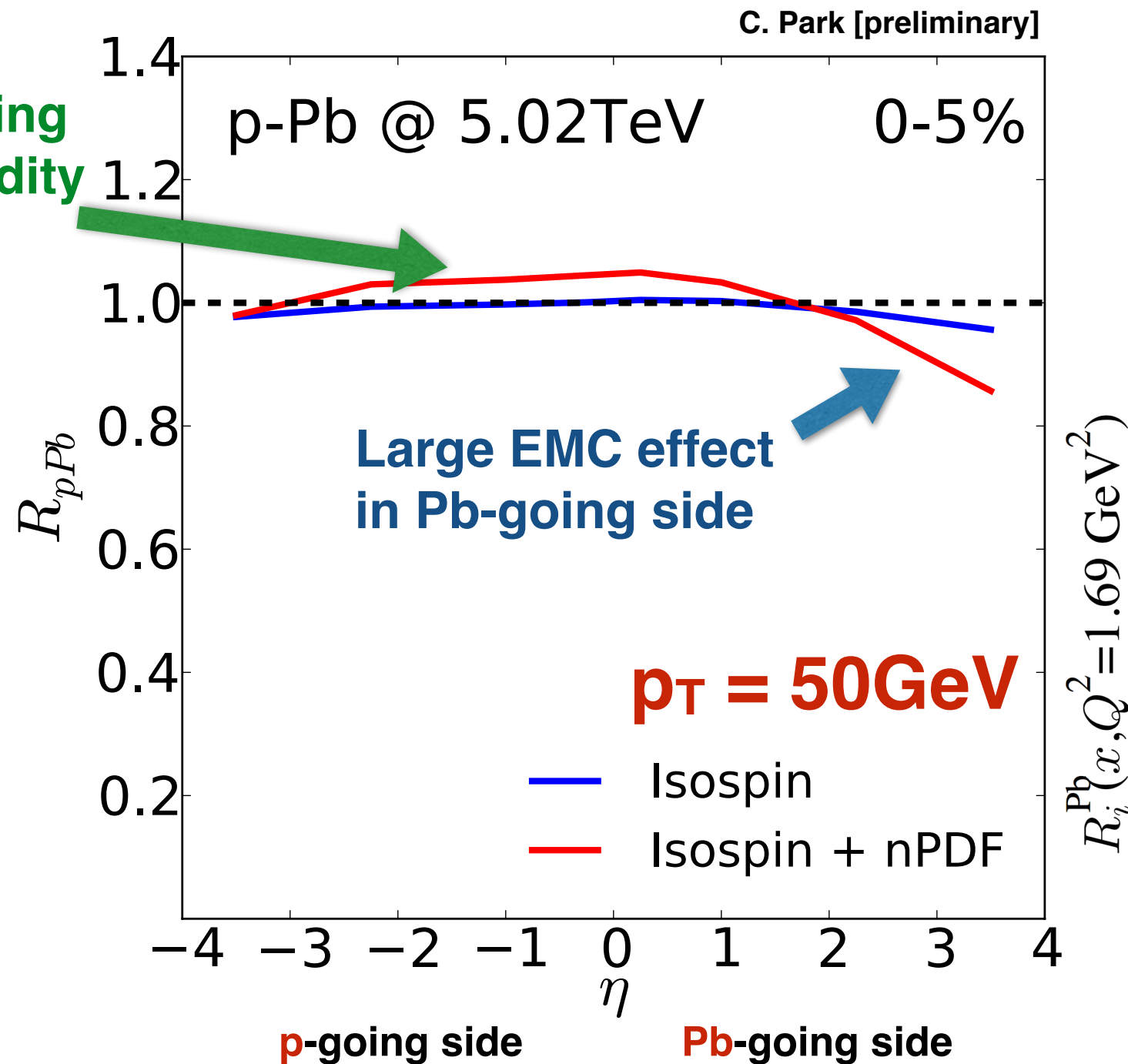
CTEQ6

# Rapidity dependent energy loss

- Isospin effect and anti-shadowing/EMC in high  $p_T$   $R_{pPb}$

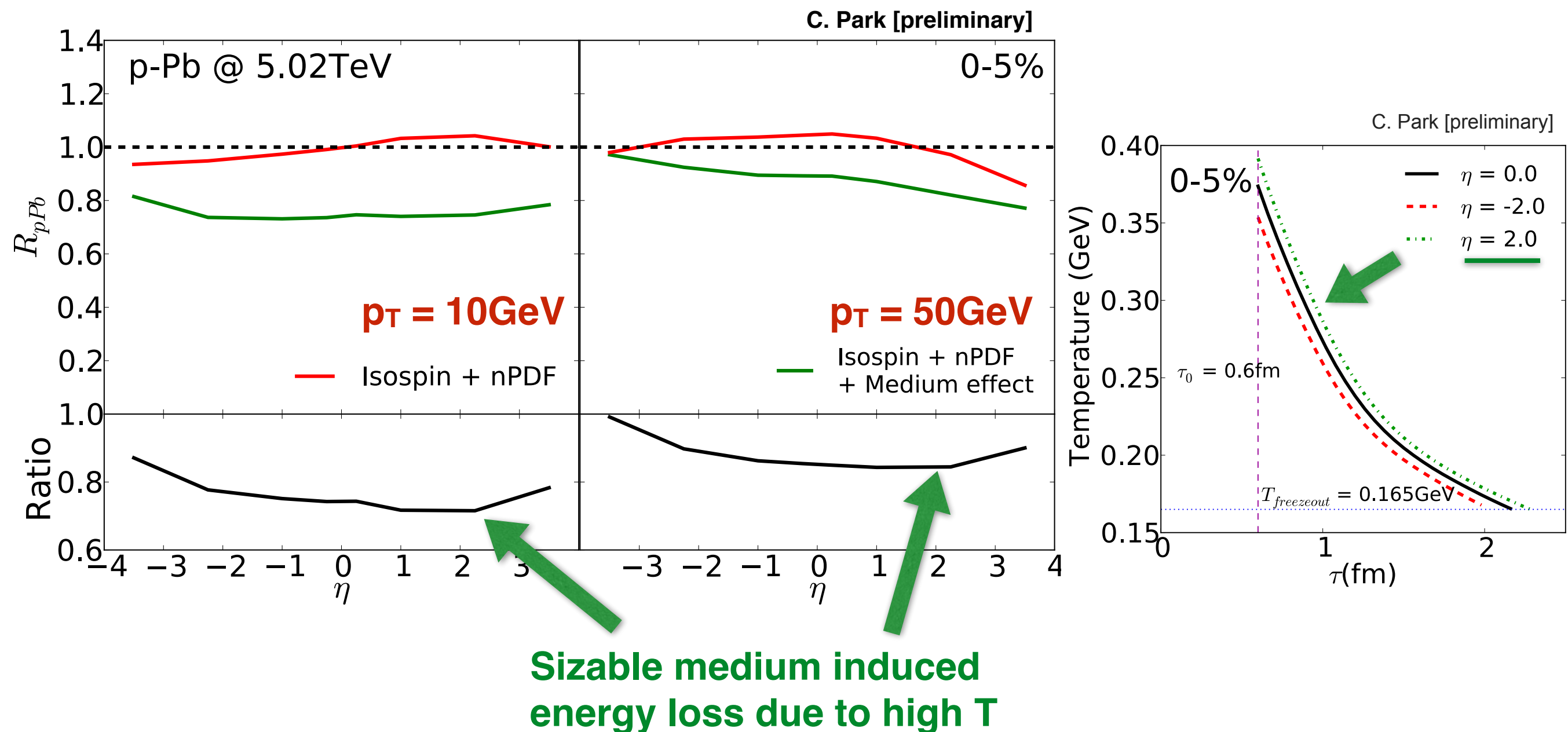
high  $p_T$   
= larger  $x$

Anti-shadowing  
at broad rapidity  
range

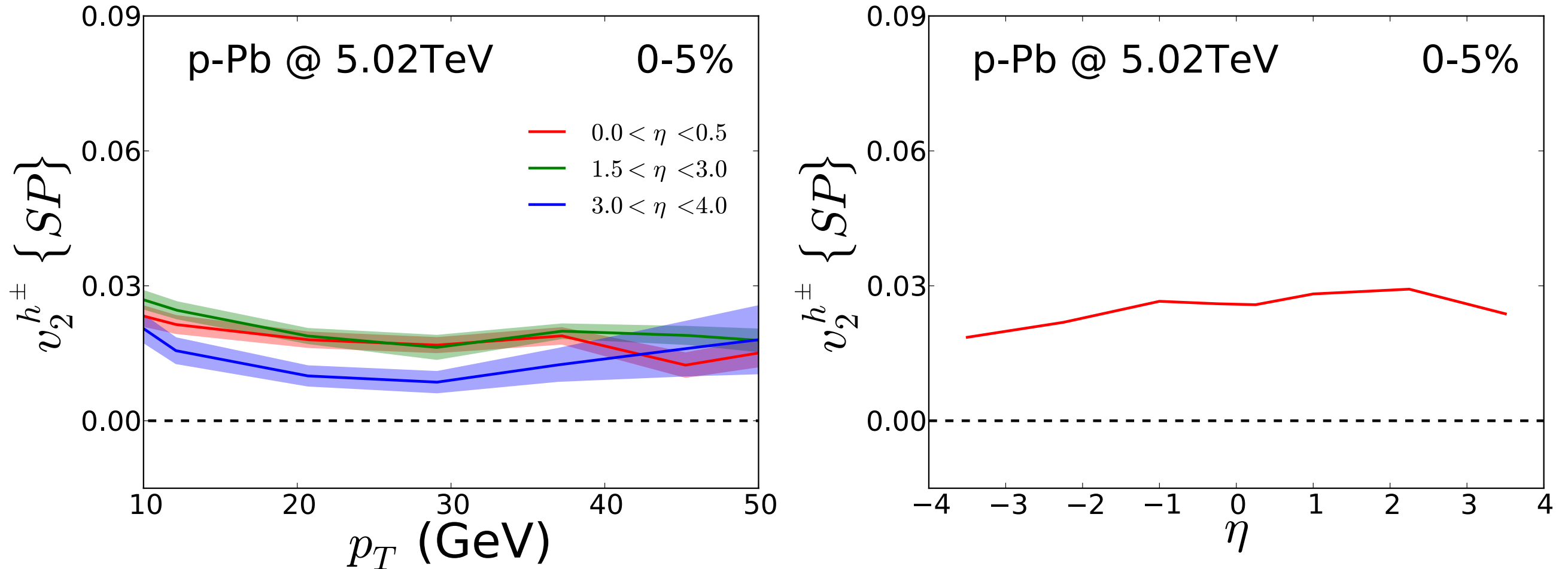


# Rapidity dependent energy loss

- Net QGP medium energy loss related to temperature and energy
  - a clear signature of QGP droplet in central collisions is predicted



# Charged hadron $v_2$ at high $p_T$



- Scalar product method; reference flow integrated from 0.3 - 3 GeV
- 1~3%  $v_2$  in central p-Pb collisions
- Medium induced energy loss dependency on integrated  $v_2$

# Conclusion

- Finite-size effect and running coupling for the radiation are essential to describe  $R_{AA}$  in large systems.
- A 3+1D medium in the small system offers the opportunity to study the key physics that governs different rapidity regimes. e.g. nPDF, isospin, and medium induced energy loss
- We predict sizable energy loss in central collisions of small systems due to the formation of the QGP droplet.
- We predict non-zero  $v_2$  in central collisions of small systems having energy loss dependency.
  - Next work : jet reconstruction to find missing energy in small systems

# Backup

# AMY integral equation

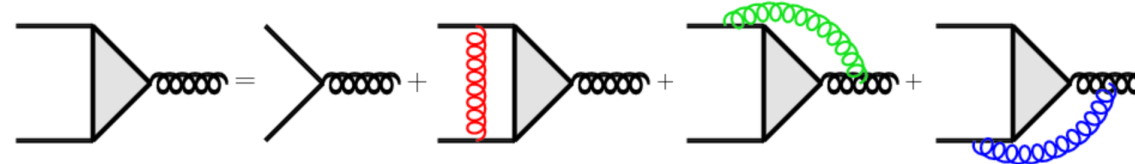


Image by G. Qin

**Integral equation**

$$2\mathbf{h} = i\delta E(\mathbf{h}, p, k)\mathbf{F}(\mathbf{h}) + g_s^2 \int \frac{d^2\mathbf{q}_\perp}{(2\pi)^2} C(\mathbf{q}_\perp) \left\{ (C_s - C_A/2)[\mathbf{F}(\mathbf{h}) - \mathbf{F}(\mathbf{h} - k\mathbf{q}_\perp)] \right. \\ \left. + (C_A/2)[\mathbf{F}(\mathbf{h}) - \mathbf{F}(\mathbf{h} + P\mathbf{q}_\perp)] + (C_s - C_A/2)[\mathbf{F}(\mathbf{h}) - \mathbf{F}(\mathbf{h} - (p - k)\mathbf{q}_\perp)] \right\}$$

Differential rate to exchange  $\mathbf{q}_\perp$

$$C(\mathbf{q}_\perp) = \frac{m_D^2}{\mathbf{q}_\perp^2(\mathbf{q}_\perp^2 + m_D^2)}, \quad m_D^2 = \frac{g_s^2 T^2}{6}(2N_c + N_f).$$

Energy difference  $\delta E$

$$\delta E(\mathbf{h}, p, k) = \frac{\mathbf{h}^2}{2pk(p - k)} + \frac{m_k^2}{2k} + \frac{m_{p-k}^2}{2(p - k)} - \frac{m_p^2}{2p}$$

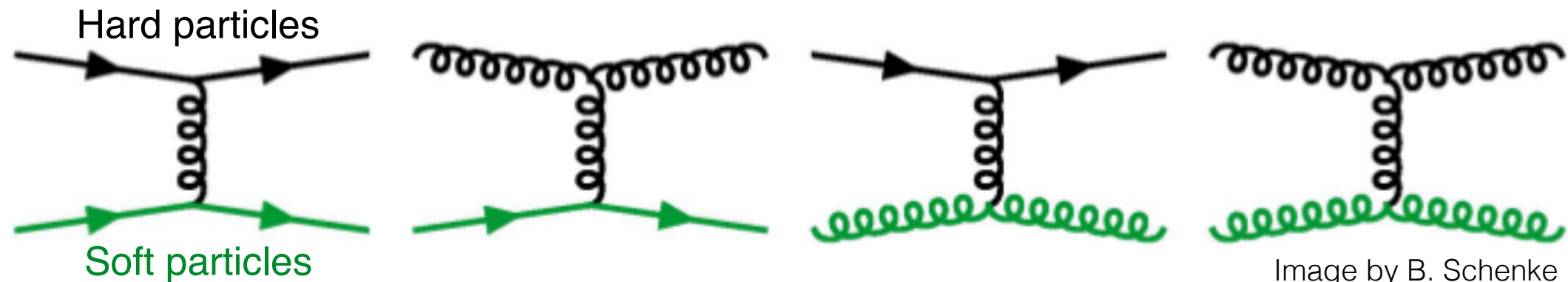
**AMY radiative rate**

$$\frac{d\Gamma(p, k)}{dk} = \frac{C_s g_s^2}{16\pi p^7} \frac{1}{1 \pm e^{-k/T}} \frac{1}{1 \pm e^{-(p-k)/T}} \times \left\{ \begin{array}{ll} \frac{1+(1-x)^2}{x^3(1-x)^2} & q \rightarrow qg \\ N_f \frac{x^2+(1-x)^2}{x^2(1-x)^2} & g \rightarrow qq \\ \frac{1+x^4+(1-x)^4}{x^3(1-x)^3} & g \rightarrow gg \end{array} \right\} \\ \times \int \frac{d^2\mathbf{h}}{(2\pi)^2} 2\mathbf{h} \cdot \text{Re } \mathbf{F}(\mathbf{h}, p, k),$$



# Collisional process

All the possible 2-2 scattering diagrams



Matrix elements

$$|\mathcal{M}|_{qq}^2 = \frac{4}{9}g^4 \frac{s^2 + u^2}{t^2},$$

$$|\mathcal{M}|_{qg}^2 = 2g^4 \left(1 - \frac{su}{t^2}\right),$$

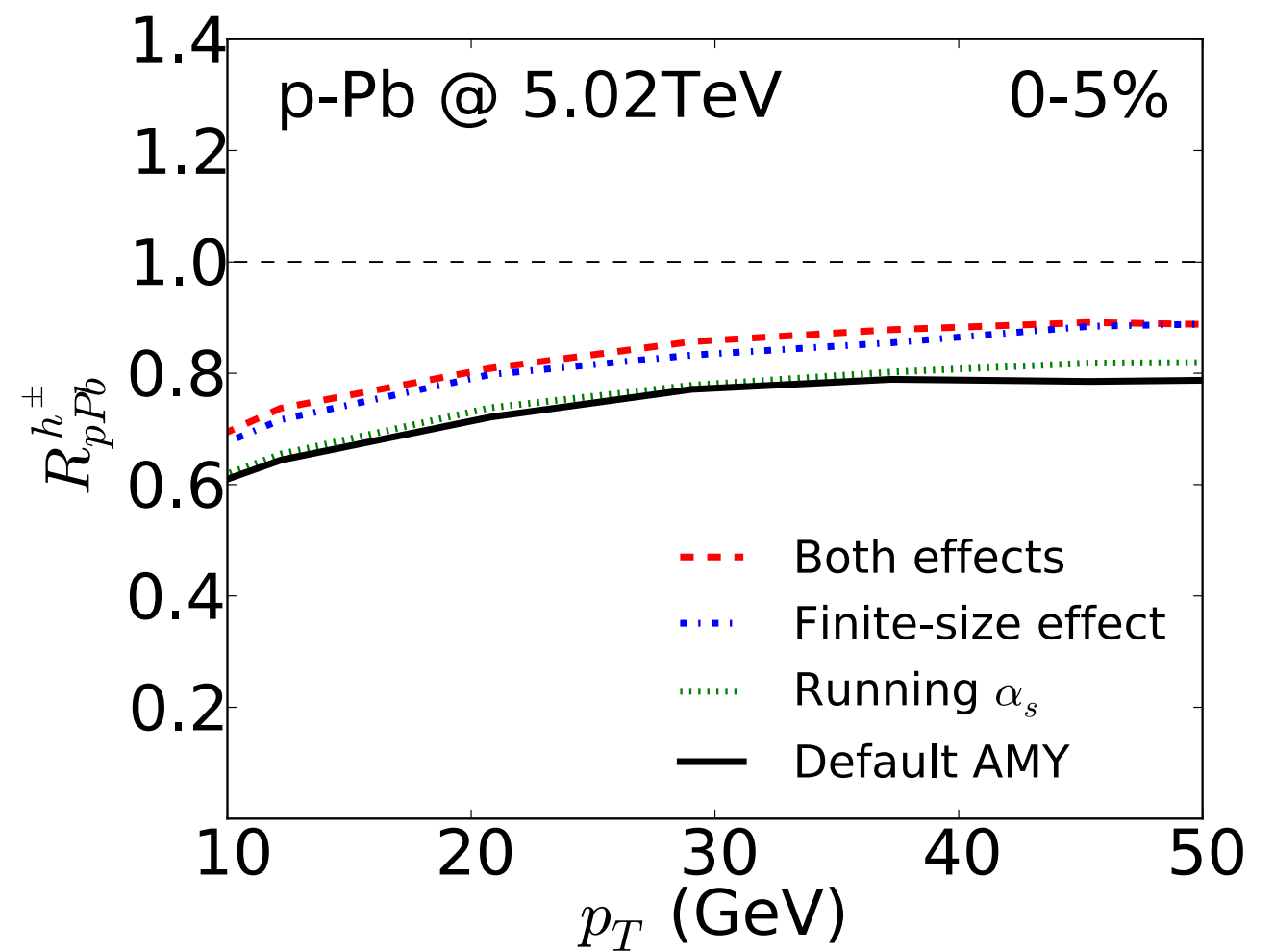
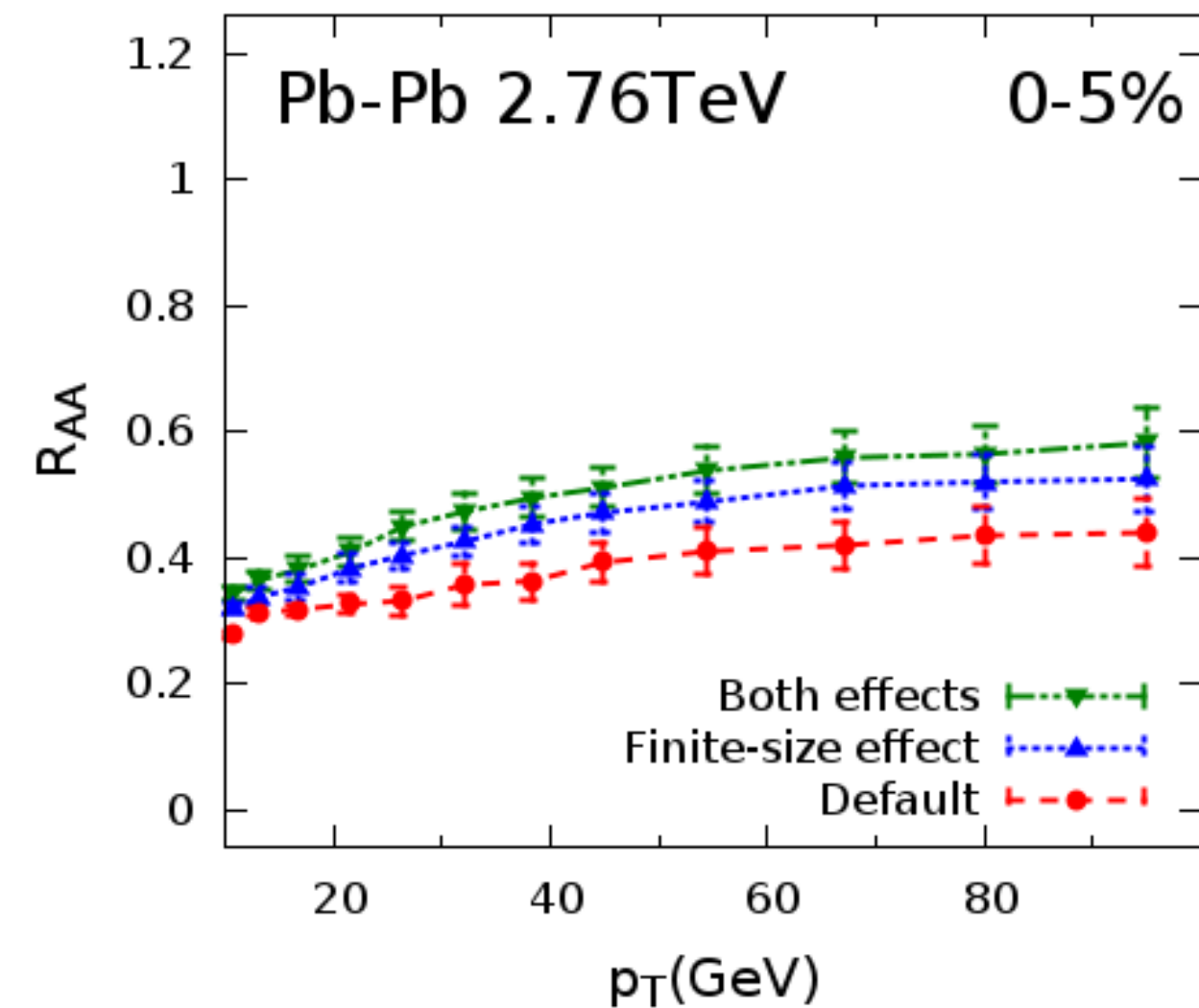
$$|\mathcal{M}|_{gq}^2 = 2g^4 \left(1 - \frac{su}{t^2}\right),$$

$$|\mathcal{M}|_{gg}^2 = \frac{9}{2}g^4 \left(\frac{17}{8} - \frac{su}{t^2}\right)$$

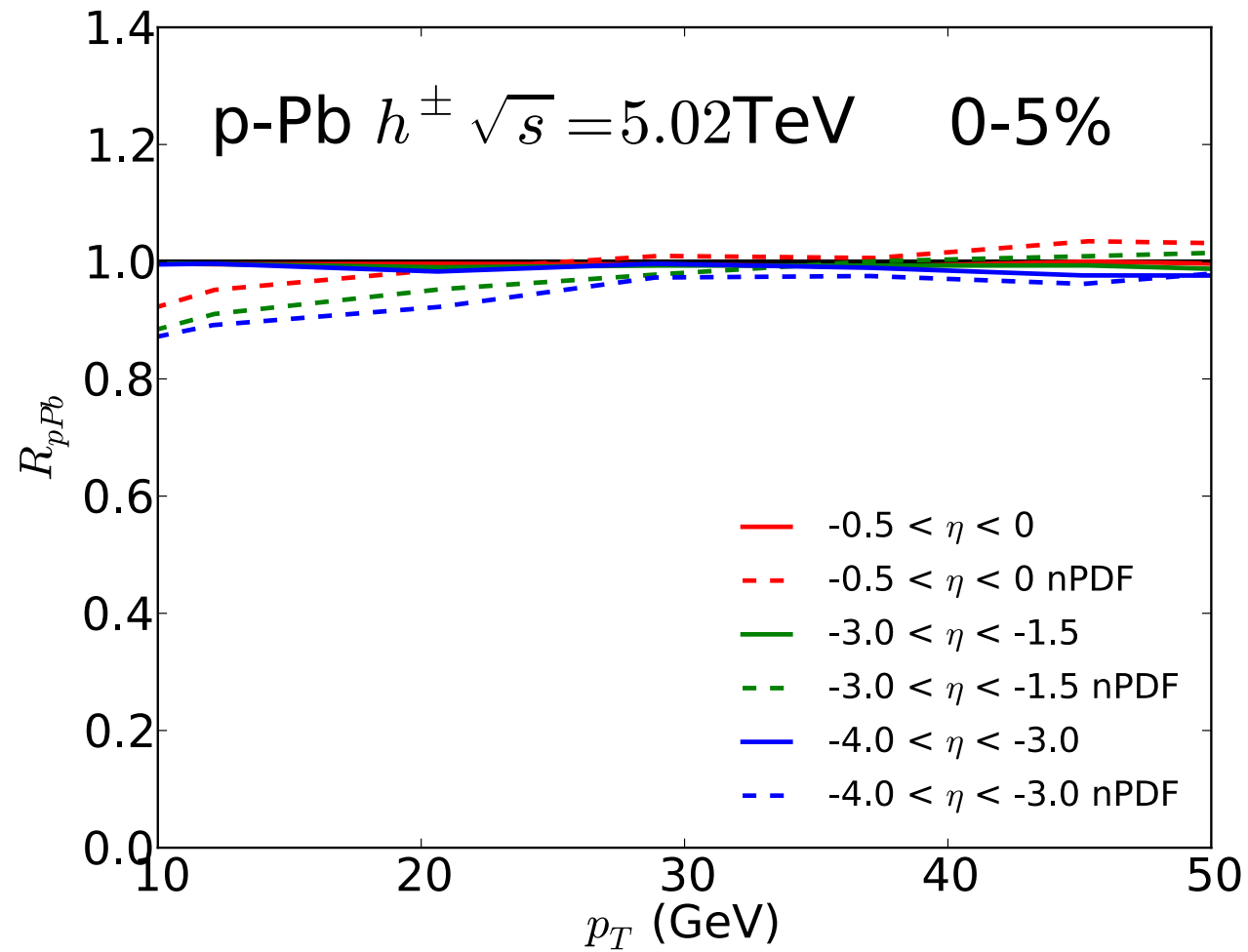
**2-2 scattering  
rate**

$$\frac{d\Gamma_{\text{el}}}{d\omega}(E, \omega, T) = d_k \int_{kk'} \frac{2\pi}{4pp'} \delta(p - p' - \omega) \delta(k' - k - \omega) \\ \times |\mathcal{M}|^2 f(k, T) (1 \pm f(k', T)),$$

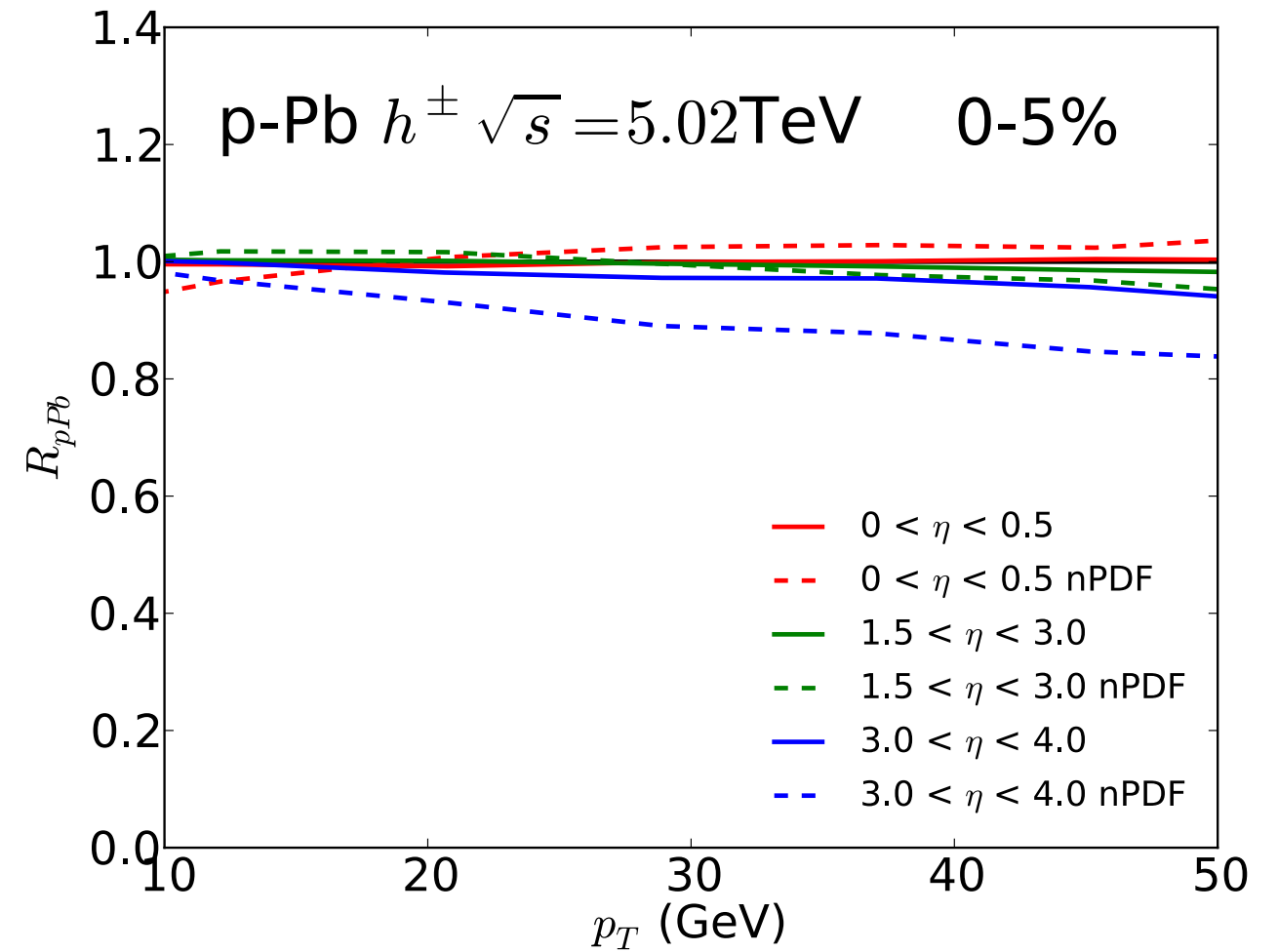
# Finite-size effects & running coupling



# Isospin & nuclear PDF



**p-going side**



**Pb-going side**