**COMPASS beyond 2020 Workshop** March 21-22, 2016

# Progress and opportunities of unpolarised Drell-Yan program

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## **Outline**

#### • **Progress made by Drell-Yan experiments in the past 20 years:**

- FNAL E866
- FNAL E906 (SeaQuest)
- CERN COMPASS
- **Opportunities for Drell-Yan processes with pion/kaon/antiproton beams:**
	- Nucleon  $x(s + \bar{s})$
	- Pion/kaon PDFs
	- Origin of Lam-Tung violation
	- Flavor dependence of nucleon Boer-Mulders functions
	- Pion/kaon/antiproton distribution amplitude
	- Flavor-dependent EMC effect
	- $\ddot{\phantom{a}}$  .
- **Feasibility for COMPASS (beyond 2020)**
- **Conclusions**



# Progress of Drell-Yan Experiments in the past

## Deep Inelastic Scattering (DIS) and Drell-Yan Processes



## Parton Distribution Function (PDF) of Proton: MMHT 2014 PDFs



L. A. Harland-Lang, A. D. Martin, P. Motylinski, R.S. Thorne, arXiv:1412.3989

## Light Antiquark Flavor Asymmetry: Drell-Yan Experiments

- Naïve Assumption:  $\bar{d}(x) = \bar{u}(x)$
- NMC (Gottfried Sum Rule):  $\left[\bar{d}(x)-\bar{u}(x)\right]dx \neq 0$
- NA51 (Drell-Yan, 1994):

 $d > \bar{u}$  at  $x = 0.18$ 

• E866/NuSea (Drell-Yan, 1998):

 $d(x)/\bar{u}(x)$  for  $0.015 \leq x \leq 0.35$ 





## Constraint of  $x(d - \bar{u})$  in Global Analysis



E. Pereza and E. Rizvib, arXiv:1208.1178

# Preliminary Results of  $d/\bar{u}(x)$ from E906 (SeaQuest)



## Dimuon Invariant-mass Distributions (2014 COMPASS DY)



## Dimuon  $x_1, x_2$  and  $p_T$  Distributions (2014 COMPASS DY)



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## Projections: COMPASS polarized DY

#### • 2015: ~80 000 DY events M>4 GeV/c<sup>2</sup> from NH3 target

• 2018: ~116 000 events (assuming same conditions, but 160 effective days)

Sivers asymmetry statistical error:~1.8%

Catarina Marques Quintans



## Large Uncertainty of  $x(s + \overline{s})$  at valence-quark region



arXiv:1412.3989

## Charged Kaon SIDIS *HERMES Collaboration, PRD 89, 097101 (2014)*



## $x(s+s)$  from SIDIS of kaons *HERMES Collaboration, PRD 89, 097101 (2014)*

![](_page_14_Figure_1.jpeg)

With the input of  $D_{Q}^{K}$  and  $D_{S}^{K}$  and non-strange quark distributions Q(x), S(x) is extracted.

#### Large Uncertainty in the extraction of  $x(s + s)$ *W.C. Chang and J.C. Peng, PRD 92, 054020 (2015)*

![](_page_15_Figure_1.jpeg)

Unfortunately  $D_{Q}^{K}$  and  $D_{S}^{K}$  are not well determined...  $\boxed{16}$ 

## Kaon Partonic Structure *NA3 Collaboration, PLB 93, 354 (1980)*

![](_page_16_Figure_1.jpeg)

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#### Valence-quark distribution functions in the kaon and pion *Chen, et al., arXiv:1602.01502*

Algebraic formulae for the dressed-quark propagators and pion and kaon Bethe-Salpeter amplitudes where SU(3) symmetry breaking is implemented.

![](_page_17_Figure_2.jpeg)

#### Valence-quark distribution functions in the kaon and pion *Chen, et al., arXiv:1602.01502*

![](_page_18_Figure_1.jpeg)

X

JLab 12  $\left[ \underline{8}, \underline{9} \right]$ . Furthermore, new mesonic Drell-Yan measurements at modern facilities could yield valuable information on  $\pi$  and K PDFs [10, [11], as could two-jet experiments at the large hadron collider  $[12]$ ; and, looking further ahead, an electron ion collider would be capable of providing access to pion and kaon structure functions through measurements of forward nucleon structure func-19tions  $[13, 14]$ .

Kaon-induced Drell-Yan Process: *Avoiding Fragmentation Functions Uncertainty*

$$
K^{+}p(x_{f}) = u^{K}(x_{1})\overline{u}^{p}(x_{2}) + \overline{S^{K}(x_{1})S^{p}(x_{2})}
$$
  
\n
$$
K^{-}p(x_{f}) = \overline{u}^{K}(x_{1})u^{p}(x_{2}) + \overline{S^{K}(x_{1})S^{p}(x_{2})}
$$
  
\non-induced Drell-Yan cross sections will determine  
\nucleon strange quark structure  
\n(aon PDFs  
\n**Kaon beam and LH<sub>2</sub> target**

Kaon-induced Drell-Yan cross sections will determine

- nucleon strange quark structure
- kaon PDFs

*Kaon beam and LH<sup>2</sup> target*

![](_page_20_Figure_0.jpeg)

# Opportunity (2): Violation of Lam-Tung relation & Boer-Mulders Functions

### Drell-Yan decay angular distributions

![](_page_21_Figure_1.jpeg)

 $\theta$  and  $\phi$  are the decay polar and azimuthal angles of the  $\mu^*$  in the dilepton rest-frame

Collins-Soper frame

$$
\frac{d\sigma}{d\Omega} \propto (1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{V}{2} \sin^2 \theta \cos 2\phi)
$$
  
 
$$
\propto (W_T (1 + \cos^2 \theta) + W_L (1 - \cos^2 \theta) + W_\Delta \sin 2\theta \cos \phi + W_{\Delta\Delta} \sin^2 \theta \cos 2\phi)
$$

 $q\overline{q}$  annilation parton model:

$$
O(\alpha_s^0)
$$
  $\lambda=1$ ,  $\mu=\nu=0$ ;  $W_T = 1$ ,  $W_L = 0$ 

Lam-Tung relation (1978): test of QCD effect

Collinear pQCD:  $O(\alpha_s^1)$ ,  $W_L = 2W_{\Delta\Delta}$ ;  $1 - \lambda - 2\nu = 0$ 

#### NA10 @ CERN: Violation of Lam-Tung Relation *Z. Phys. 37 (1988) 545*

 $\pi$ <sup>-</sup>+W 140 GeV  $\pi$ 

 $\pi$ <sup>-+</sup>W 194 GeV

 $\pi$ <sup>-+</sup>W 286 GeV

![](_page_22_Figure_4.jpeg)

E615 @ FNAL: Violation of Lam-Tung Relation *PRD 39, 92 (1989)*  $252 - GeV \pi + W$ 

![](_page_23_Figure_1.jpeg)

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## Azimuthal Asymmetries Require Nontrivial Spin Correlation

The most general  $q\bar{q}$  spin density matrix

 $(q,\bar q) = \frac{1}{11} \text{ or } 1 + E$  $\{1 \otimes 1 + \overline{F}_i(\vec{\sigma} \bullet \vec{e}_i) \otimes 1 + \overline{G}_i 1 \otimes (\vec{\sigma} \bullet \vec{e}_i) + \overline{H}_{ii}(\vec{\sigma} \bullet \vec{e}_i) \otimes (\vec{\sigma} \bullet \vec{e}_i)\}$  $4<sup>1</sup>$  $\rho^{(q,q)} = \frac{1}{4} \{ 1 \otimes 1 + F_j(\vec{\sigma} \cdot \vec{e}_j) \otimes 1 + G_j 1 \otimes (\vec{\sigma} \cdot \vec{e}_j) + H_{ij}(\vec{\sigma} \cdot \vec{e}_i) \otimes (\vec{\sigma} \cdot \vec{e}_j) \}$ 22  $\sim$  11 \ Violation of LT relation:  $\kappa = -\frac{1}{4}(1 - \lambda - 2\nu) \approx \left\langle \frac{H_{22} - H_{11}}{1 + H_{33}} \right\rangle$  $H_{\infty}$  /  $\kappa = -\frac{1}{2}(1 - \lambda - 2\nu) \approx \left(\frac{H_{22} - H_{11}}{2}\right)$  $+$  H<sub>22</sub> /

Collinear case: 
$$
H_{11} = H_{22}
$$
,  $H_{23} = H_{32} = 0$ ,  $\kappa = 0$ 

Brandenburg, Nachtmann & Mirkes, ZPC 60 (1993) 697

Nonzero *K* requires *the correlation of the spins of quark and antiquark.* 

What will be the mechanism?

#### Brandenburg, Nachtmann & Mirkes [Z. Phy. C 60 (1993) 697]: QCD Vacuum Effect

![](_page_25_Figure_1.jpeg)

#### Boer [PRD 60, 014012 (1999)]: Hadronic Effect, Boer-Mulders Functions

Spin-orbit correlation of transversely polarized *noncollinear partons* inside an unpolarized hadron

![](_page_26_Figure_2.jpeg)

- Boer-Mulders Function  $h_1^{\perp}$  : a correlation between quark's  $k_T$  and transverse spin  $S_T$  in an unpolarized hadron
- $h_1^{\perp}$  can lead to an azimuthal dependence with  $-\infty h_1^{\perp}(N)h_1^{\perp}(\pi)$  $2$  and  $\sim$  2 •  $h_1^{\perp}$  can lead to an azimuthal dependence with  $\frac{V}{\sim} \propto h_1^{\perp}(N) \overline{h_1}^{\perp}(\pi)$

![](_page_26_Figure_5.jpeg)

$$
h_1^{\perp}(x, k_T^2) = C_H \frac{\alpha_T}{\pi} \frac{M_C M_H}{k_T^2 + M_C^2} e^{-\alpha_T k_T^2} f_1(x),
$$
  

$$
\nu = 16\kappa_1 \frac{p_T^2 M_C^2}{(p_T^2 + 4M_C^2)^2}, \quad \kappa_1 = C_{H_1} C_{H_2} / 2
$$
  

$$
\kappa = \frac{V}{2} \rightarrow 0 \text{ for large } |k_T|
$$

Consistency of factorizati on in term of TMD s

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#### Chen & Li [PLB 726 (2013) 262] Breaking of Factorization by Glauber Gluons

![](_page_27_Figure_1.jpeg)

![](_page_27_Figure_2.jpeg)

## Theoretical Interpretations of Lam-Tung Violation in pion-induced DY

![](_page_28_Picture_150.jpeg)

Measurements with different beams  $\pi$ ,  $p$ ,  $K$ ,  $\overline{p}$  over wide kinematical ranges

would help differentiating the origin of Lam-Tung violation.

*Kaon and antiproton beams*

#### Consistency of LT relation in p+p and p+d DY: *E866 (PRL 99 (2007) 082301; PRL 102 (2009) 182001)*

![](_page_29_Figure_1.jpeg)

#### Boer-Mulders functions from unpolarized pD and pp Drell-Yan data  $\sigma_{UU} \propto f_{1}^{(A,\bar{q})} f_{1}^{(\text{B,q})} + h_{1}^{\perp(A,\bar{q})} h_{1}^{\perp(\text{B,q})} \cos 2 \phi$

![](_page_30_Figure_1.jpeg)

Sign of BM functions and flavor dependence?

### Lu, Ma & Schimdt [PLB 639 (2006) 494]: Flavor separation of the Boer–Mulders functions

![](_page_31_Figure_1.jpeg)

![](_page_32_Figure_0.jpeg)

# Opportunity (3): Distribution amplitudes

### CIP (PRL 43, 1219, (1979)) : Longitudinally Polarized Photon at large  $x_1$

 $[W_T(1+\cos^2\theta)+W_L(1-\cos^2\theta)+W_{\Delta}\sin 2\theta\cos\phi+W_{\Delta\Delta}\sin^2\theta\cos 2\phi]$  $d\sigma$  $d\Omega$  $\frac{\partial}{\partial \Omega} \propto [W_T (1 + \cos^2 \theta) + W_L (1 - \cos^2 \theta) + W_{\Delta} \sin 2\theta \cos \phi + W_{\Delta \Delta} \sin^2 \theta \cos 2\phi]$ 

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![](_page_33_Figure_2.jpeg)

## CIP (PRL 58, 2523 (1987)) :  $\pi W \rightarrow J/\psi X$

Sign of  $q\bar{q}$  annihilation dominating?

![](_page_34_Figure_2.jpeg)

 $d^2\sigma/d\cos\theta d\phi \propto 1 + \lambda \cos^2\theta + \mu \sin 2\theta \cos\phi$ 

![](_page_34_Figure_5.jpeg)

FIG. 4. The  $J/\psi$  decay angular distribution vs  $\cos\theta$  for the five regions of  $\phi$ , and summed over all  $\phi$  in the highest  $x_F$  bin,  $0.95 \le x_F \le 1.0$ . The histograms are the result of the fit described in the text. (a)  $-\pi < \phi < -0.6\pi$ , (b)  $-0.6\pi < \phi$  $<-0.2\pi$ , (c)  $-0.2\pi < \phi < 0.2\pi$ , (d)  $0.2\pi < \phi < 0.6\pi$ , (e)  $0.6\pi$  $\langle \phi \rangle \langle \pi, (f) - \pi \langle \phi \rangle \langle \pi,$ 

 $+\frac{1}{2}v\sin^2\theta\cos 2\phi$ .

#### Brandenburg et al. (PRL 73, 939 (1994)) Higher-twist Effect & Pion Distribution Amplitude

![](_page_35_Figure_1.jpeg)

$$
\frac{Q^2 d\sigma (\pi^- N \to \mu^+ \mu^- X)}{dQ^2 dQ_T^2 dx_L d\Omega} = \frac{1}{(2\pi)^4} \frac{1}{64} \int_0^1 dx_u G_{u/N}(x_u) \int_0^1 dx_{\bar{u}} \frac{x_{\bar{u}}}{1 - x_{\bar{u}} + Q_T^2/Q^2} |M|^2
$$
  
 
$$
\times \delta(x_L - x_{\bar{u}} + x_u - Q_T^2 s^{-1} (1 - x_{\bar{u}})^{-1})
$$
  

$$
M = \int_0^1 dz \phi(z, \tilde{Q}^2) T, \qquad \times \delta(Q^2 - s x_u x_{\bar{u}} + Q_T^2 (1 - x_{\bar{u}})^{-1}) + \{u \to \bar{d}, \bar{u} \to d\}.
$$

**Pion distribution amplitude**: distribution of LC momentum fractions in the lowest-particle number valence Fock state.  $36$ 

### Brandenburg et al. (PRL 73, 939 (1994)) Pion Distribution Amplitude

![](_page_36_Figure_1.jpeg)

#### Brandenburg et al. (PRL 73, 939 (1994)): Pion/Kaon/Antiproton Distribution Amplitude

The coefficient functions  $\lambda$ ,  $\mu$ , and  $\nu$  are large  $x > 0.5$ are very sensitive to the shape of the projectile's distribution amplitude  $\phi(z, \tilde{Q}^2)$ , the basic hadron wave function which describes the distribution of light-cone momentum fractions in the lowest-particle number valence Fock state. Measurements of meson form factors [12] and other exclusive and semiexclusive processes [16] at large momentum transfer can only provide global constraints on the shape of  $\phi(z, \tilde{Q}^2)$ ; in contrast, the angular dependence of the lepton pair distributions can be used to provide local measurements of the shapes of these hadron wave functions. Detailed measurements of the angular distribution of leptons as a function of both x and  $Q_T$  for the reactions  $Hp \rightarrow l + l^{-}X$  for the whole range of fixed target beams  $H = \pi$ , K,  $\bar{p}$ , p, and n will open up a new window on the structure of hadrons at the amplitude level.

#### *Kaon and antiproton beams*  $\overline{\phantom{a}}$  38

# $\pi N \to \gamma^* N$  (Exclusive Drell-Yan)

*E.R. Berger, M. Diehl, B. Pire, PLB 523 (2001) 265*

![](_page_38_Figure_2.jpeg)

$$
\tau = \frac{Q^2}{2pq} \approx \frac{Q^2}{s - M_N^2} \qquad \eta = \frac{(p - p')^+}{(p + p')^+}
$$

$$
\frac{d\sigma}{dQ'^2 dt d(\cos\theta) d\varphi}
$$

$$
= \frac{\alpha_{\text{em}}}{256\pi^3} \frac{\tau^2}{Q'^6} \sum_{\lambda',\lambda} |M^{0\lambda',\lambda}|^2 \sin^2\theta,
$$

$$
\begin{aligned}\n\frac{d u}{d\kappa}(\xi, \eta, t) \\
&= \frac{8}{3} \alpha_S \int_{-1}^{1} dz \, \frac{\phi_\pi(z)}{1 - z^2} \\
&\times \int_{-1}^{1} dx \left[ \frac{e_d}{\xi - x - i\epsilon} - \frac{e_u}{\xi + x - i\epsilon} \right] \\
&\times \left[ \widetilde{H}^d(x, \eta, t) - \widetilde{H}^u(x, \eta, t) \right], \text{39}\n\end{aligned}
$$

![](_page_39_Figure_0.jpeg)

# Opportunity (4): Flavor-dependent EMC effect

### Cloet et. al (PRL 102, 252301, 2009): Flavor dependence of the EMC effect?

![](_page_40_Figure_1.jpeg)

**CBT model:** the iso-vector  $\rho^0$  mean-field generated in Z≠N

Dutta et al. (PRC 83, 04220, 2011): Pion-induced Drell-Yan and the flavor-dependent EMC effect

![](_page_41_Figure_1.jpeg)

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#### Dutta et al. (PRC 83, 04220, 2011): Pion-induced Drell-Yan and the flavor-dependent EMC effect

![](_page_42_Figure_1.jpeg)

![](_page_43_Picture_0.jpeg)

# Feasibility for COMPASS (Beyond 2020)

![](_page_44_Picture_0.jpeg)

![](_page_44_Picture_1.jpeg)

![](_page_44_Picture_2.jpeg)

High-intensity pion beam<br>High-intensity kaon beam<br>High-intensity antiproton beam

# **COMPASY**

# Dimuon Vertex Distributions (2014 DY)

![](_page_45_Figure_2.jpeg)

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#### Fraction of particles in the positive or negative M2-Hadron-beam at COMPASS target http://www.staff.uni-mainz.de/jasinsk/index.htm

fraction of protons over beammomentum fraction of pi+ over beammomentum fraction of K+ over beammomentum  $0.02F$ 11  $0.6$  $0.018$  $0.9$  $+$   $K^+$  |  $p$  0.5  $\pi$  0.014  $0.8$  $0.4$  $0.012$  $0.7$  $0.01$  $0.3$  $0.6$  $0.008$  $0.006$  $0.2$  $0.5$  $0.004$  $0.1$  $0.4$  $0.002$ تتتنبأ المتماز بمنطق بماعتين تتميل بربر المربوط بالنفر بالمروز  $\mathbf{0}$ οE 250 100 150 200 250 300 350 100  $\overline{150}$  $\overline{200}$  $300$  $350$ 400 150  $\overline{200}$ 250 300 350 400 100 fraction of K- over beammomentum fraction of p bar over beammomentum fraction of pi- over beammomentum 0.985F  $0.025$  $^{\sim}2.5\%$  $0.024$  $0.98$ **1x108/sec** $0.023$  $0.02$ *p* |  $\sqrt{2}$  $\mathbb{R}$   $\mathbb{$  $\pi$  0.021  $0.015$ 0.97  $0.02$  $~97\%$  $0.01$  $0.019$  $~^{\sim}1\%$  $0.965$  $0.018$ 0.005 0.017 0.96  $0.016$ ilini biri biri biri ba . . . . . . . . . .  $\Omega$ 100 150 200 250 300 350 400 100 150 200 250 300 350 400 100 150 200 250 300 350 400

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## Beam PID: CEDAR (Cerenkov Differential Counters with Achromatic Ring Focus)

![](_page_47_Figure_1.jpeg)

#### Takahiro Sawada

Estimation of #DY

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#### Attenuation of hadron beams in target materials

#### **Primary**  <sup>−</sup> **Beam Flux into each target**

![](_page_48_Picture_265.jpeg)

Final configuration: 7-cm Al target, 267 mm from the beam plug. Pion interaction length (Aluminum) = 50.64 cm 7.0 cm = 13.8 % of pion interaction length

#### **Al (7cm) + W**

![](_page_48_Figure_8.jpeg)

#### Estimation of #DY **Attenuation of beam hadrons in material** Takahiro Sawada

Assumption:

K- : 2.5 % x 0.5 (PID efficiency)

anti-p : 1% x 0.8 (PID efficiency)

#### <sup>−</sup> **Beam Flux into each target**

![](_page_49_Picture_280.jpeg)

#### $\bar{p}$  Beam Flux into each target

![](_page_49_Picture_281.jpeg)

# Expected Statistical Precision of Dimuon Angular Distributions

WPAS

4 < *Mμμ*< 9 *GeV/c<sup>2</sup>*

![](_page_50_Figure_2.jpeg)

# Expected Statistical Precision of Dimuon Angular Distributions

 $\overline{\text{MPA}}$ 

4 < *Mμμ*< 9 *GeV/c<sup>2</sup>*

![](_page_51_Figure_2.jpeg)

## Improved CEDAR:

Expected Statistics of Unpolarized Drell-Yan Events

**NH<sup>3</sup> Al (7cm) W**  $\pi^-$  beam <sup>−</sup> **beam 140,000 27,100 270,000** <sup>−</sup> **beam 1,750 350 3,700 beam 1,260 220 1,800** DY (  $4 < M_{\mu\nu} < 9$  *GeV/c*<sup>2</sup>) 140-day data taking, with the efficiencies of 2015 DY run. **NA3 21,220 700 E615 27,977 E537 387 NA10 284,200**

COMPASS could improve the existing statistics of  $\pi$ , K and  $\bar{p}$ induced DY by a factor of **2-10**!

### **WHAT ABOUT A RF SEPARATEDp BEAM ???**

First and very preliminary thoughts, guided by

- recent studies for P326
- CKM studies by J.Doornbos/TRIUMF, e.g. http://trshare.triumf.ca/~trjd/rfbeam.ps.gz

E.g. a system with two cavities:

![](_page_53_Figure_5.jpeg)

 $\Delta\Phi = 2\pi$  (L f / c) ( $\beta_1$ <sup>-1</sup> -  $\beta_2$ <sup>-1</sup>) with  $\beta_1$ <sup>-1</sup> -  $\beta_2$ <sup>-1</sup> = (m<sub>1</sub><sup>2</sup>-m<sub>2</sub><sup>2</sup>)/2p<sup>2</sup>

#### **Base rough estimates on acceptance values for RF separated K<sup>+</sup> beam (as provided by J.Doornbos)**

![](_page_54_Picture_91.jpeg)

As the p kick is more favourable than for  $K^+$ , I assume that 80% of p pass beyond the beam stopper.

![](_page_54_Picture_3.jpeg)

Acceptance  $10\pi$  usterad, 2 GeV/c

#### **VERY PRELIMINARY CONCLUSION**

H.W.Atherton formula tells us : 0.42 p / int.proton / GeV

Assume target efficiency of 40%

Then for 10<sup>13</sup> ppp on target one obtains:

 $0.4 \cdot 10^{13} \cdot 0.42 \cdot \pi \cdot 10^{-5} \cdot 2 \cdot 0.8$  ppp = **8 10<sup>7</sup> ppp** 

for a total intensity probably not exceeding 10<sup>13</sup> ppp, knowing that  $e^-$  and  $\pi$  are well filtered, but K<sup>+</sup> only partly.

Due to 10<sup>8</sup> limit on total flux, max antiproton flux remains limited by purity (probably about 50%). Hence  $\approx$  **5 10<sup>7</sup> ppp** 

RF/Separated Kaon/antiproton : Expected Statistics of Unpolarized Drell-Yan Events

#### A flux of **1x107 /sec** for kaon/antiproton is assumed.

DY (  $4 < M_{\mu\nu} < 9$  *GeV/c*<sup>2</sup>) 140-day data taking, with the efficiencies of 2015 DY run.

![](_page_56_Picture_122.jpeg)

COMPASS could improve the existing statistics of K and  $\bar{p}$ induced DY by a factor of **50-100**!

## Conclusions

- Drell-Yan process is a powerful tool to explore the partonic structures of nucleons and (unstable) mesons.
- Drell-Yan program with Improved CEDAR/RFseparated beam and  $LH_2/LD_2/n$ uclear targets will bring unique opportunities for COMPASS to address many important unresolved issues in understanding the flavor and TMD structures of proton, antiproton, pion, kaon and nuclei.