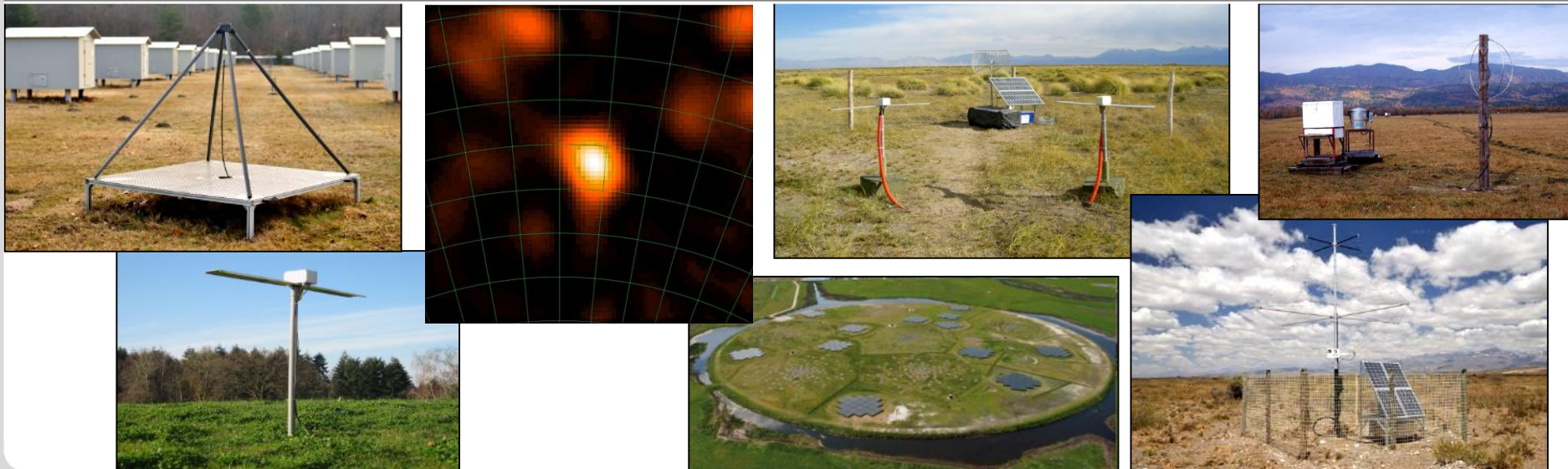


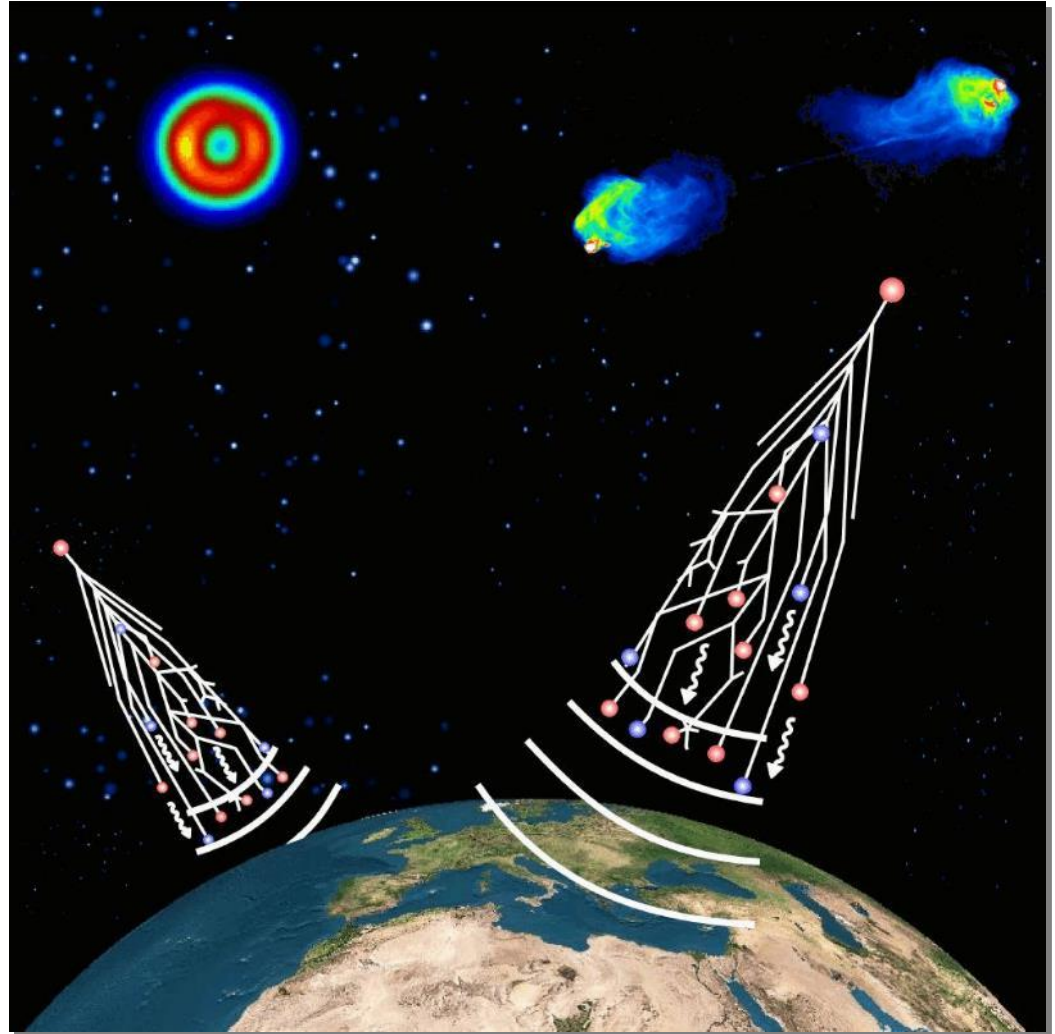
(VHF) Radio detection of cosmic rays – Achievements and future potential

Tim Huege (Karlsruhe Institute of Technology)

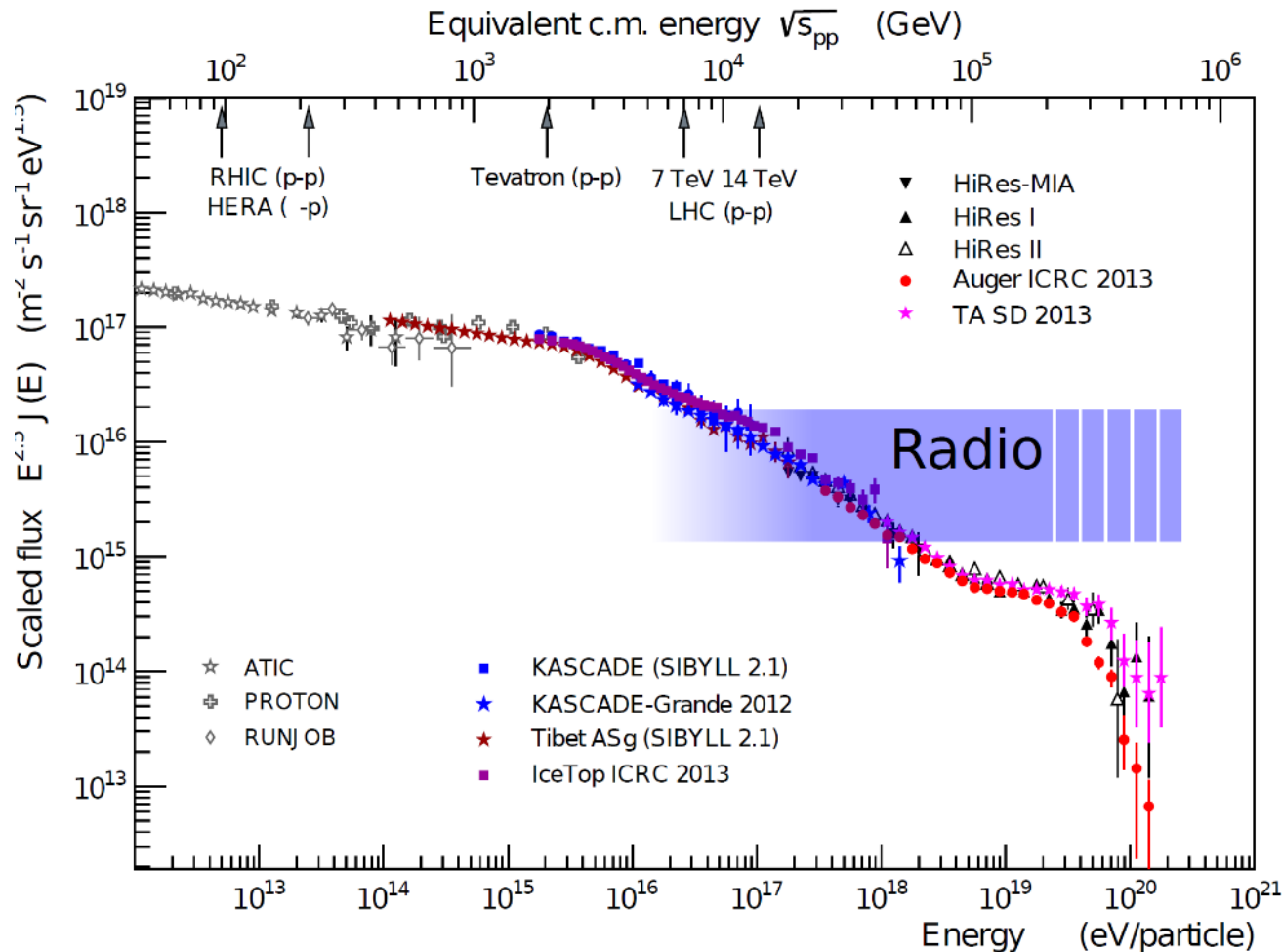


Contents

- achievements of radio detection
- what can radio do for (U)HECR science



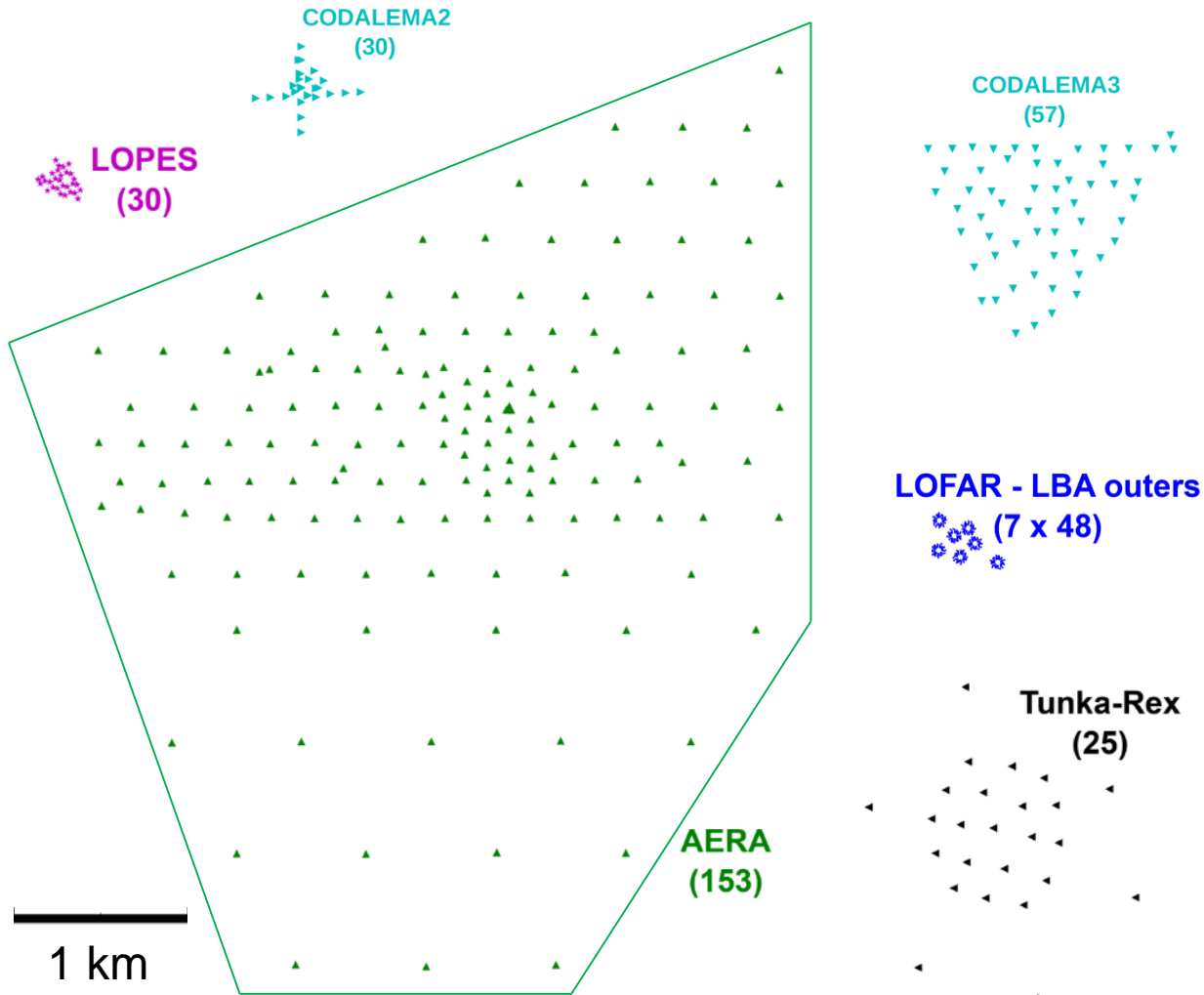
Radio detection of (U)HECR air showers



adapted from R. Engel

- most experience in VHF regime (30-80 MHz)
- low energies: radio signal hidden in Galactic noise
- very high energies: still need concepts to instrument largest areas

Comparison of ground experiments to scale



- from prototypes to large-scale experiments
- sparse vs. dense arrays

Strengths and limitations of radio detection

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- measures pure electromagnetic shower component
- no absorption in the atmosphere, calorimetric energy measurement
- near 100% duty cycle
- high angular resolution
- particle mass sensitivity
- simple (cheap) detectors
- required detector spacing
- direction-dependent threshold
- radio-backgrounds

A decade of radio-emission modelling

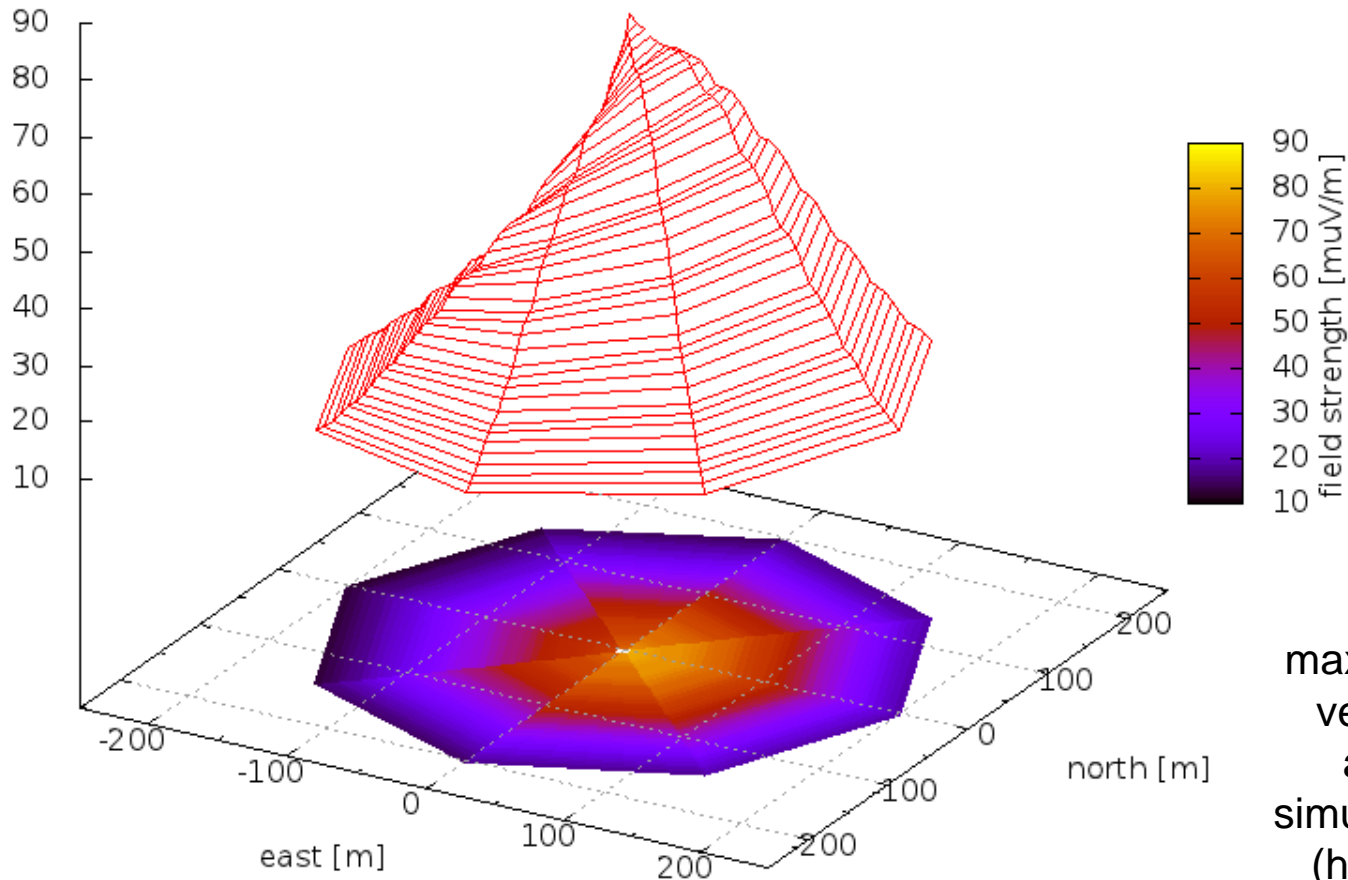
- | | |
|------------------|---|
| <p>■ MGMR</p> | <p>time-domain, analytic, parametrized shower, fast, free parameters, summing up „mechanisms“</p> |
| <p>■ EVA</p> | <p>time-domain, parameterisation of distributions derived from cascade equations or MC</p> |
| <p>■ SELFAS2</p> | <p>time-domain, shower from universality, summing up vector potentials for tracks</p> |
| <p>■ REAS3.1</p> | <p>time-domain, histogrammed CORSIKA showers, endpoint formalism</p> |
| <p>■ ZHAireS</p> | <p>time- and frequency-domain, Aires showers, ZHS formalism</p> |
| <p>■ CoREAS</p> | <p>time-domain, CORSIKA showers, endpoint formalism</p> |

more „microscopic“



**first principle
calculations**

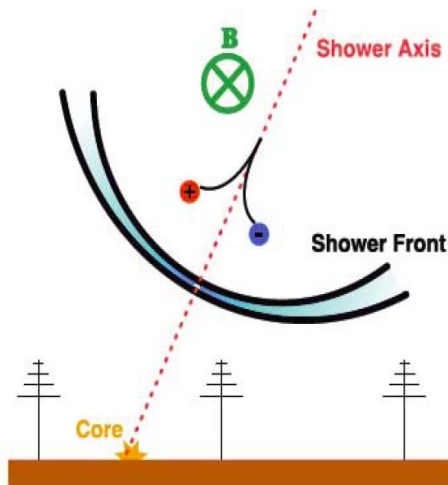
Complexity of radio-emission footprint



maximum amplitude of
vertical iron shower
at 40-80 MHz as
simulated with CoREAS
(higher frequencies:
Cherenkov ring)

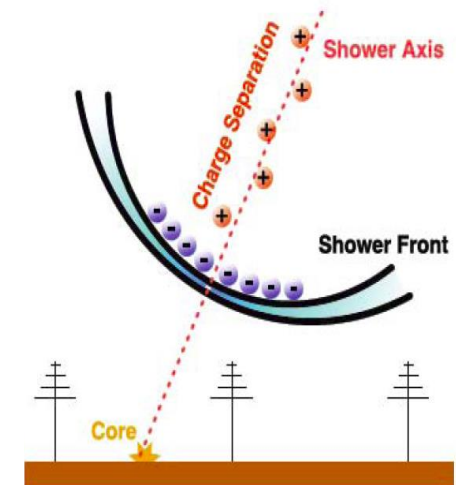
TH et al., ARENA2012

Macroscopic interpretation of radio emission



- primary effect: geomagnetic field induces *time-varying* transverse currents

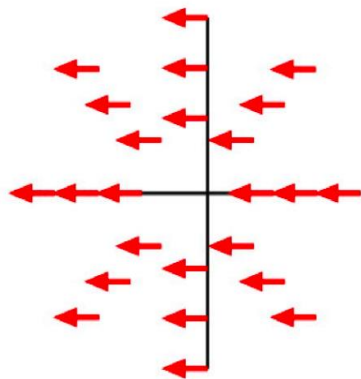
Kahn & Lerche (1967)



Askaryan (1962,1965)

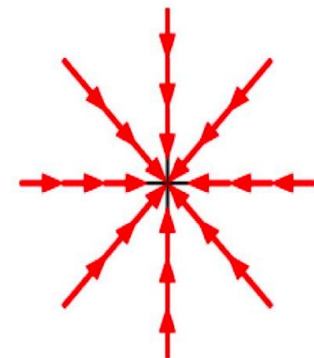
- secondary effect: *time-varying* net charge excess (Askaryan effect)

Pierre Auger Coll., Phys. Rev. D 89 (2014) 052002.



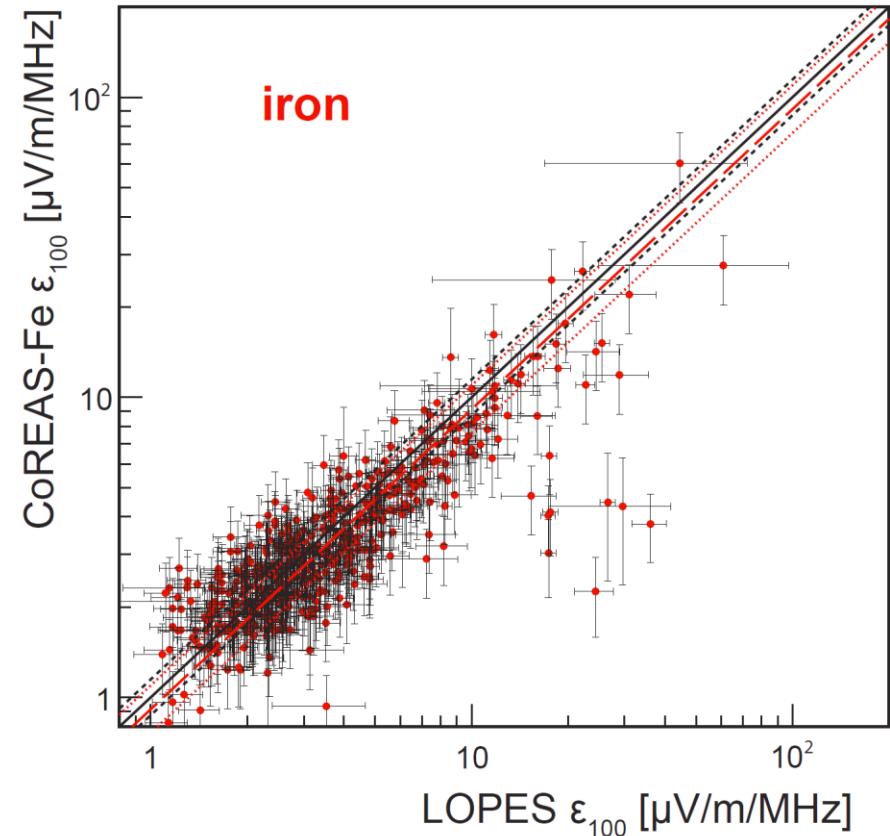
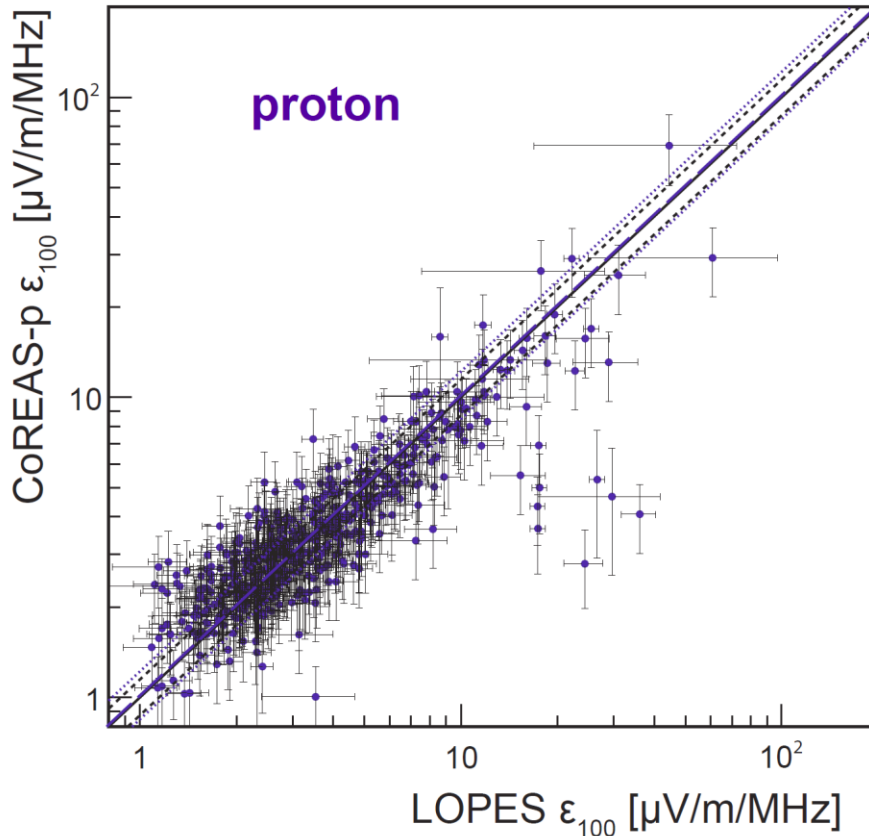
„ $\mathbf{v} \times \mathbf{B}$ “

Diagrams by H. Schoorlemmer & K.D. de Vries



„*radial*“

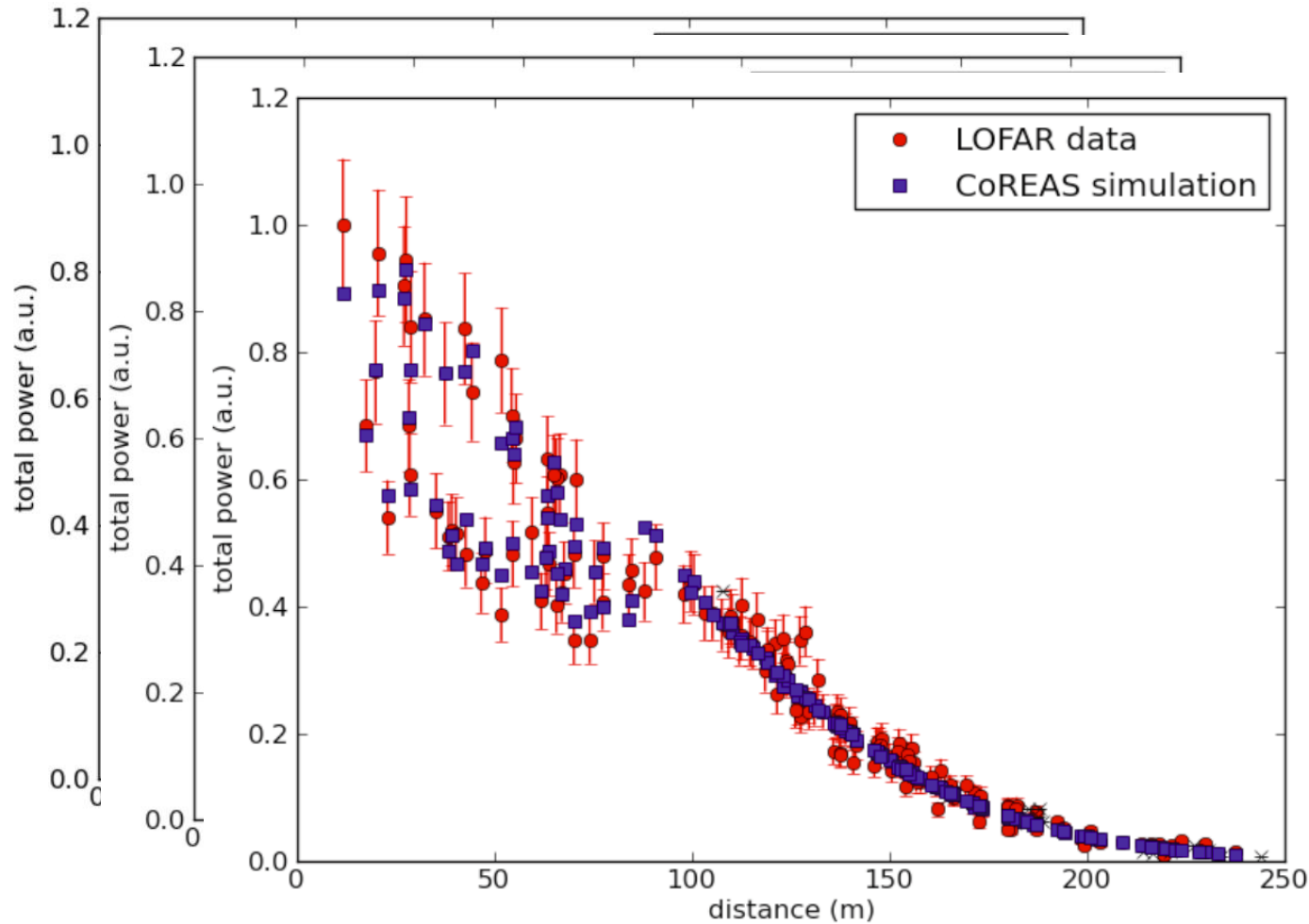
Comparison of simulations with LOPES data



- very good agreement, well within systematic uncertainties
- the absolute scale is predicted correctly!
- see also results from AERA & Tunka-Rex

LOPES Coll., Astropart.
Phys. 75 (2016) 72-74.

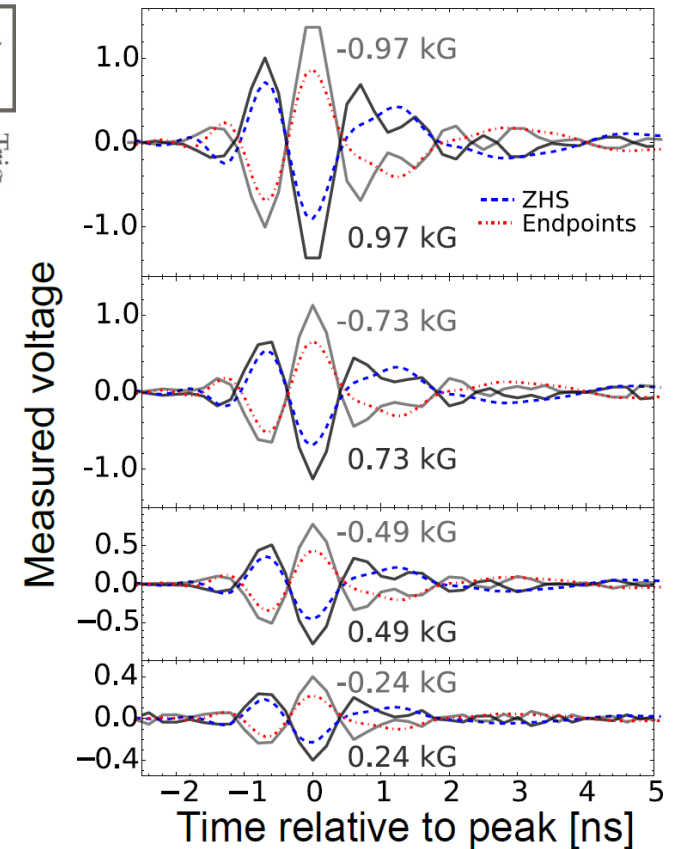
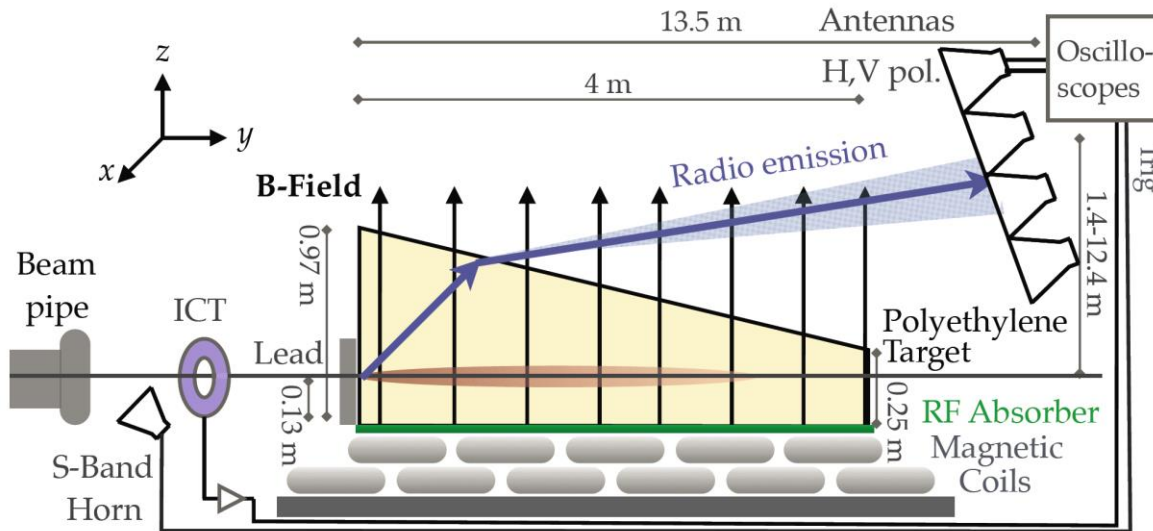
Comparison of simulations with LOFAR data



- measurement of individual shower with extreme level of detail
- data can be reproduced by simulations
- see geomagn., charge excess and Cherenkov effects

S. Buitink, A. Corstanje, J. E. Enriquez, et al., Phys. Rev. D 90 (2014) 082003.

Lab-Experiment: SLAC T-510



- electromagnetic particle shower in strong magnetic field, controlled conditions
- cross-check first-principle calculations
 - agree within systematic uncertainties ($\sim 35\%$)

Belov et al. (T-510 Collaboration), PRL116 (2016) 141103

Strengths and limitations of radio detection

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- no absorption in the atmosphere, calorimetric energy measurement
- near 100% duty cycle
- high angular resolution
- particle mass sensitivity
- simple (cheap) detectors
- required detector spacing
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- radio-backgrounds

emission well-understood, can be used to set energy scale

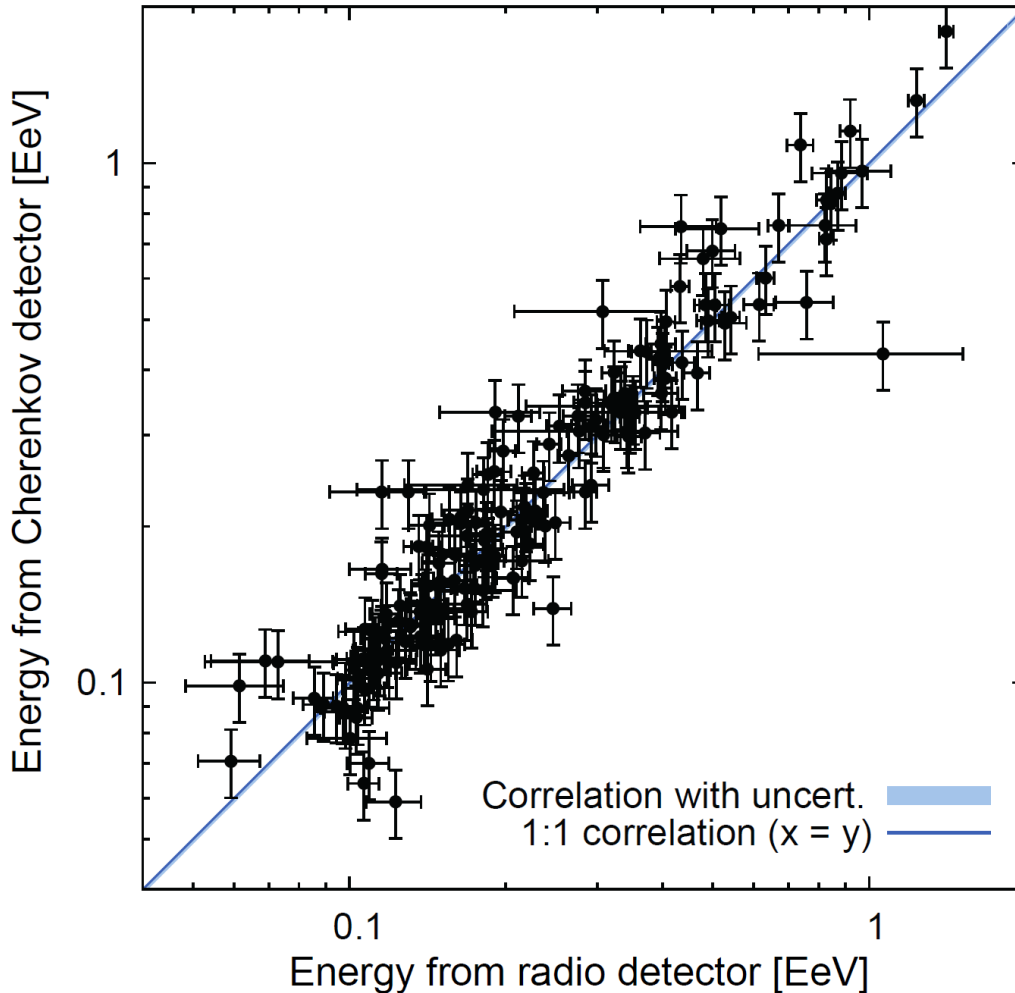
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direct comparison to FD, little influence of hadronic interactions

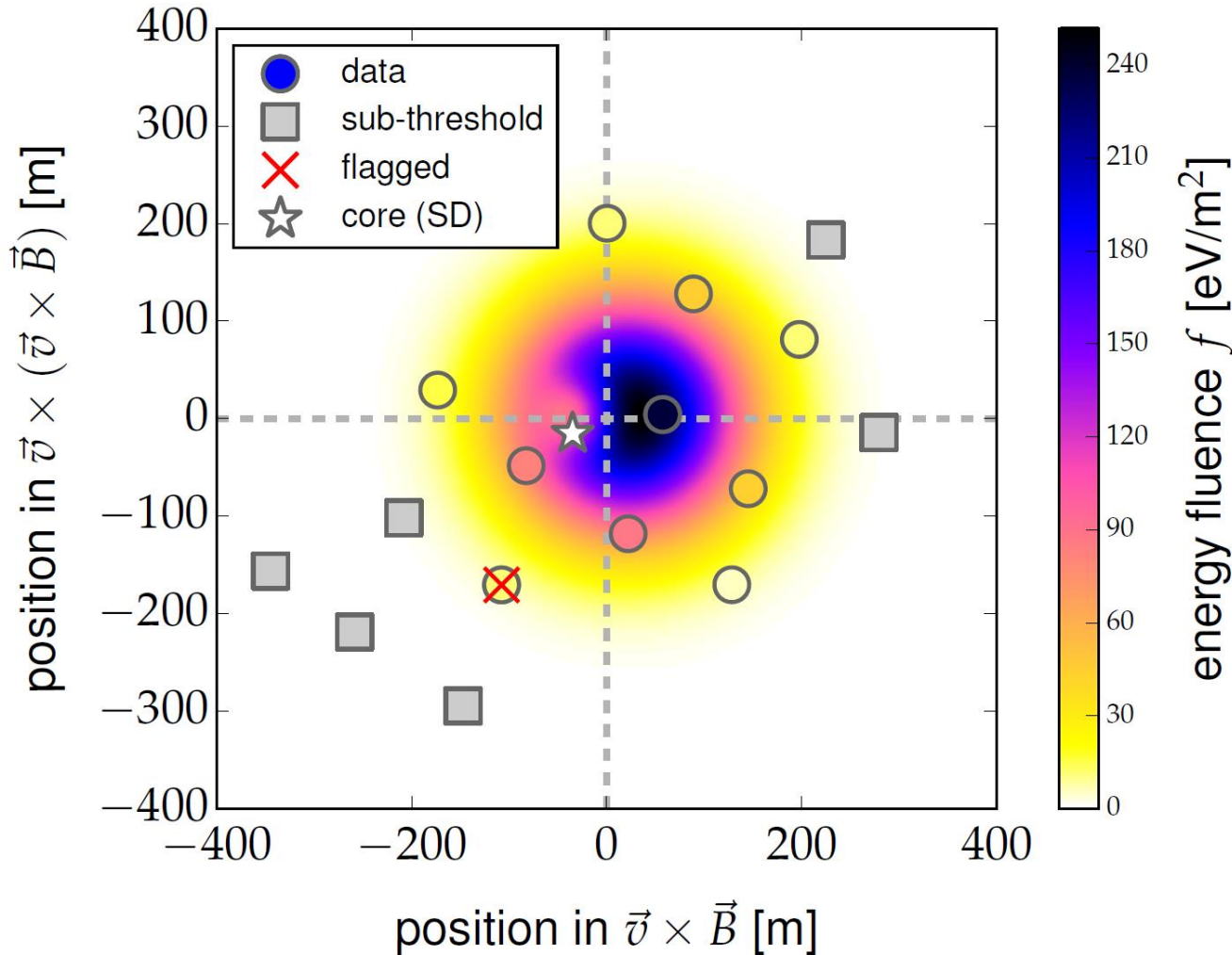
Tunka-Rex energy reconstruction



- use amplitude at characteristic lateral distance as energy estimator
 - accuracy: absolute scale fits nicely with CoREAS simulations
 - precision: 20% combined resolution of radio and optical Cherenkov detectors (~15% alone)
- see also comparable results from LOPES

Tunka-Rex Coll., JCAP (2016)
[arXiv:1509.05652](https://arxiv.org/abs/1509.05652).

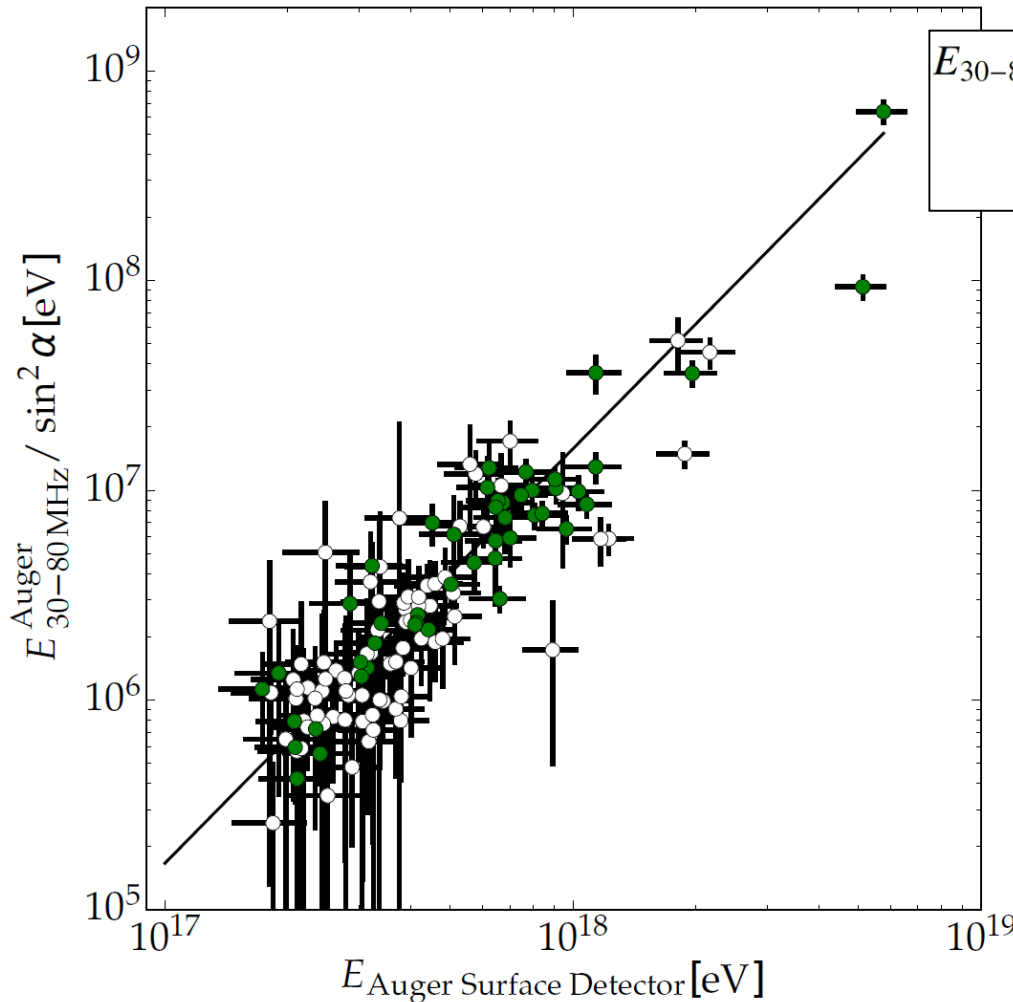
AERA energy reconstruction – radiation energy



- at each antenna calculate energy fluence from time-integration of Poynting flux
- then integrate energy fluence over area using 2D signal distribution model

Pierre Auger Coll., Phys Rev. D (2016), arXiv:1508.04267.

„Radiation energy“ as energy estimator



$$E_{30-80 \text{ MHz}} = (15.8 \pm 0.7 \text{ (stat)} \pm 6.7 \text{ (sys)}) \text{ MeV} \times \left(\sin \alpha \frac{E_{\text{CR}}}{10^{18} \text{ eV}} \frac{B_{\text{Earth}}}{0.24 \text{ G}} \right)^2. \quad (10)$$

- energy resolution ~17%
- of 10^{18} eV, only 10^7 eV go into radio signals
- radiation energy gives a calorimetric measurement of the energy in the electromagnetic cascade
- this value can be measured by any experiment, so cross-calibrate energy scales against the Auger scale

Piere Auger Coll., Phys Rev. Lett. (2016), arXiv:1605.02564.

Radiation energy and energy-scale calibration

Radiation Energy

$$E_{30-80 \text{ MHz}}$$

$$\propto \int A^2 d^2r$$

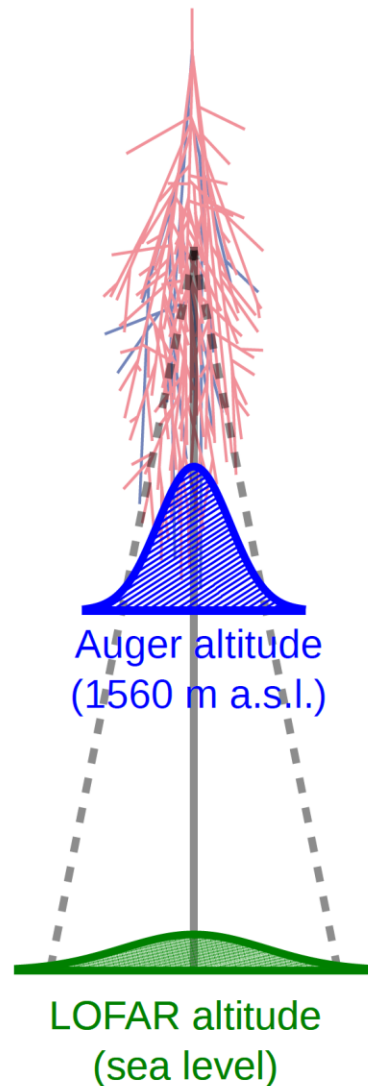
Amplitude at optimal lateral distance

A

The Radiation Energy reflects the calorimetric energy of the air shower. It is independent of observation altitude.

11.9 MeV

11.9 MeV



Auger altitude
(1560 m a.s.l.)

LOFAR altitude
(sea level)

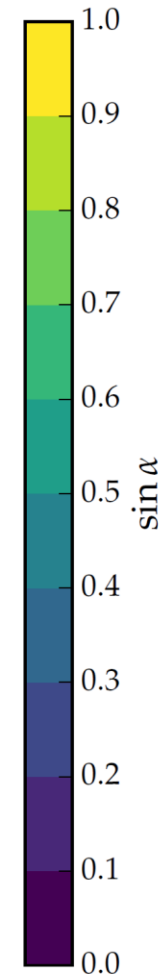
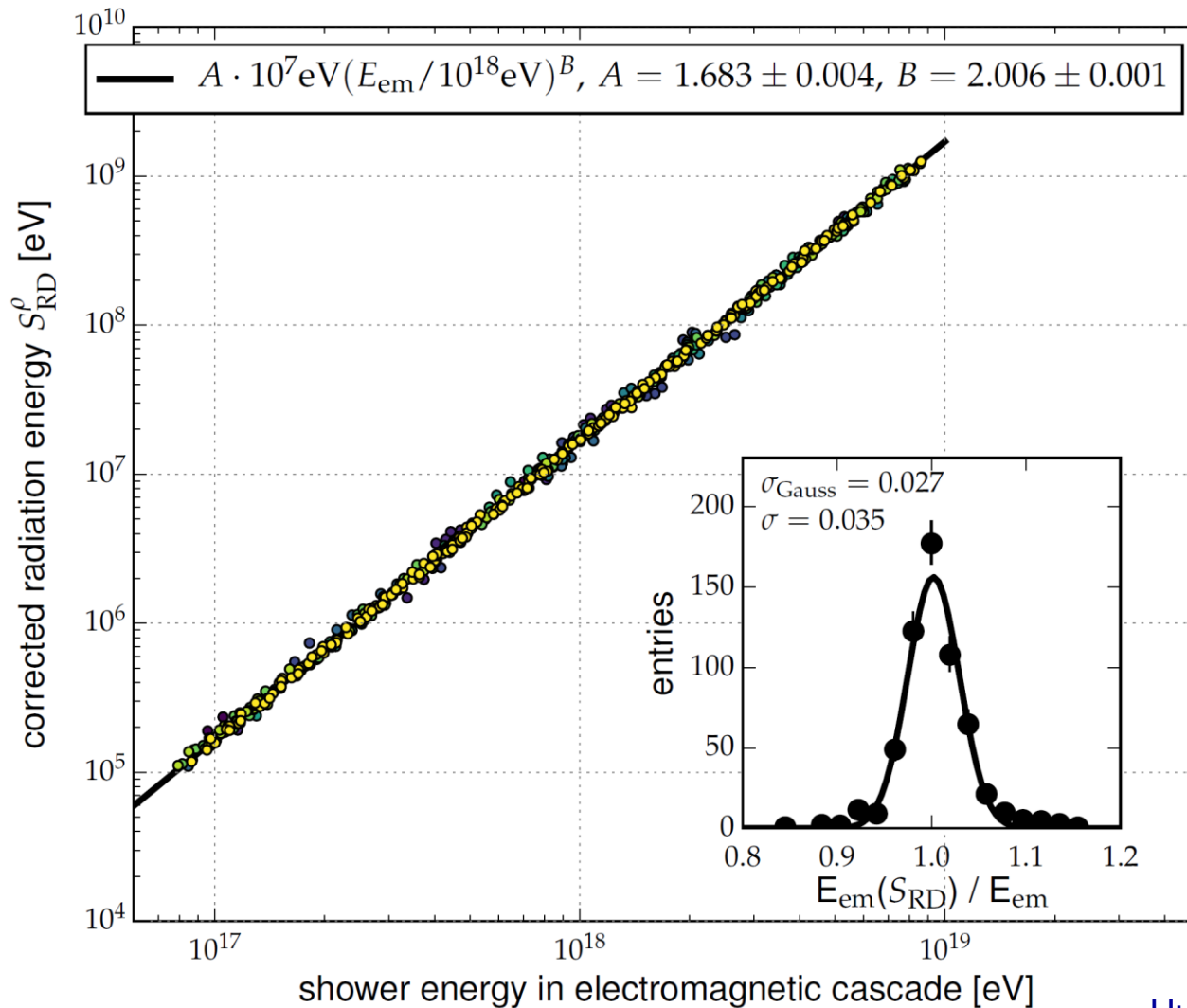
0.70 mV/m

0.56 mV/m

The optimal lateral distance and the amplitude measured there vary with observation altitude (even after charge-excess and zenith-angle correction).

Piere Auger Coll., Phys Rev. Lett. (2016), arXiv:1605.02564.

Radiation energy and electromagnetic energy



- radiation energy has been studied in detail
- very good correlation with electromagnetic energy, less than 5% intrinsic scatter

Glaser, Erdmann, Hörandel,
Huege, Schulz, JCAP 09 (2016) 024

Strengths and limitations of radio detection

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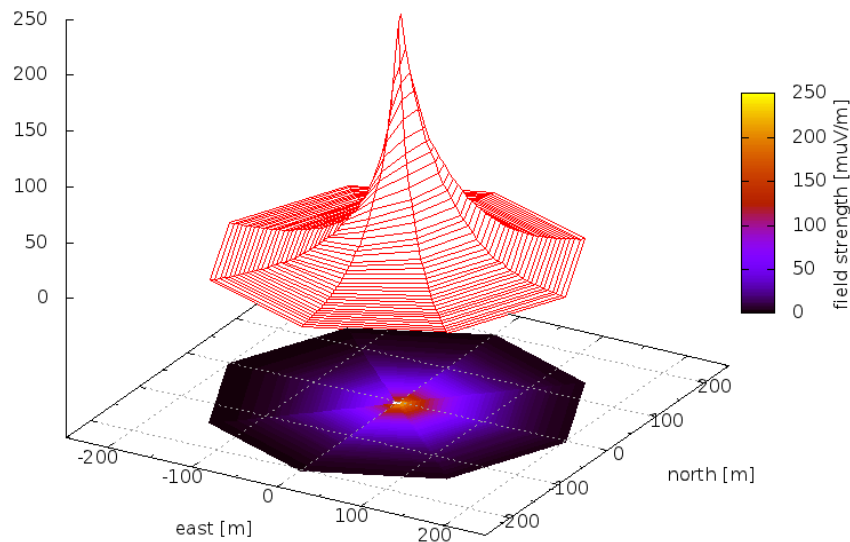
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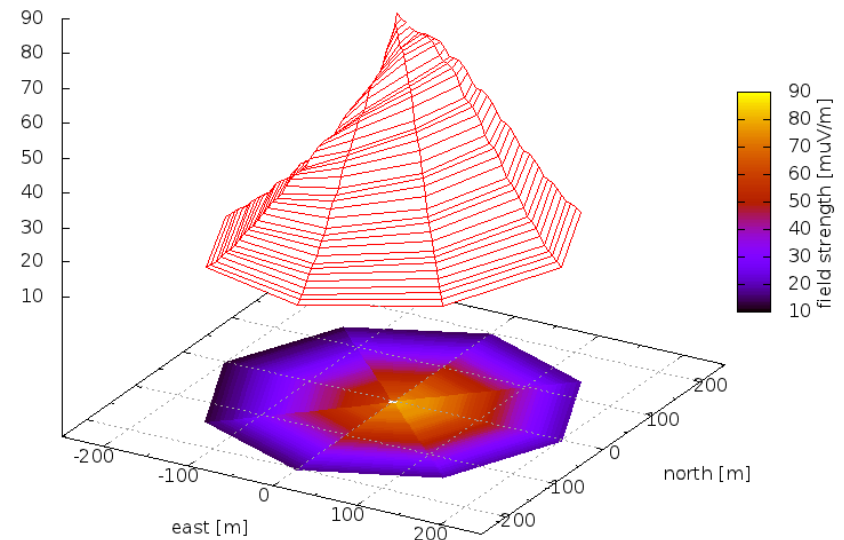
Lateral distribution as probe for composition

- relativistic forward beaming of emission: geometrical distance from source to observer influences emission pattern

TH et al., ARENA2012

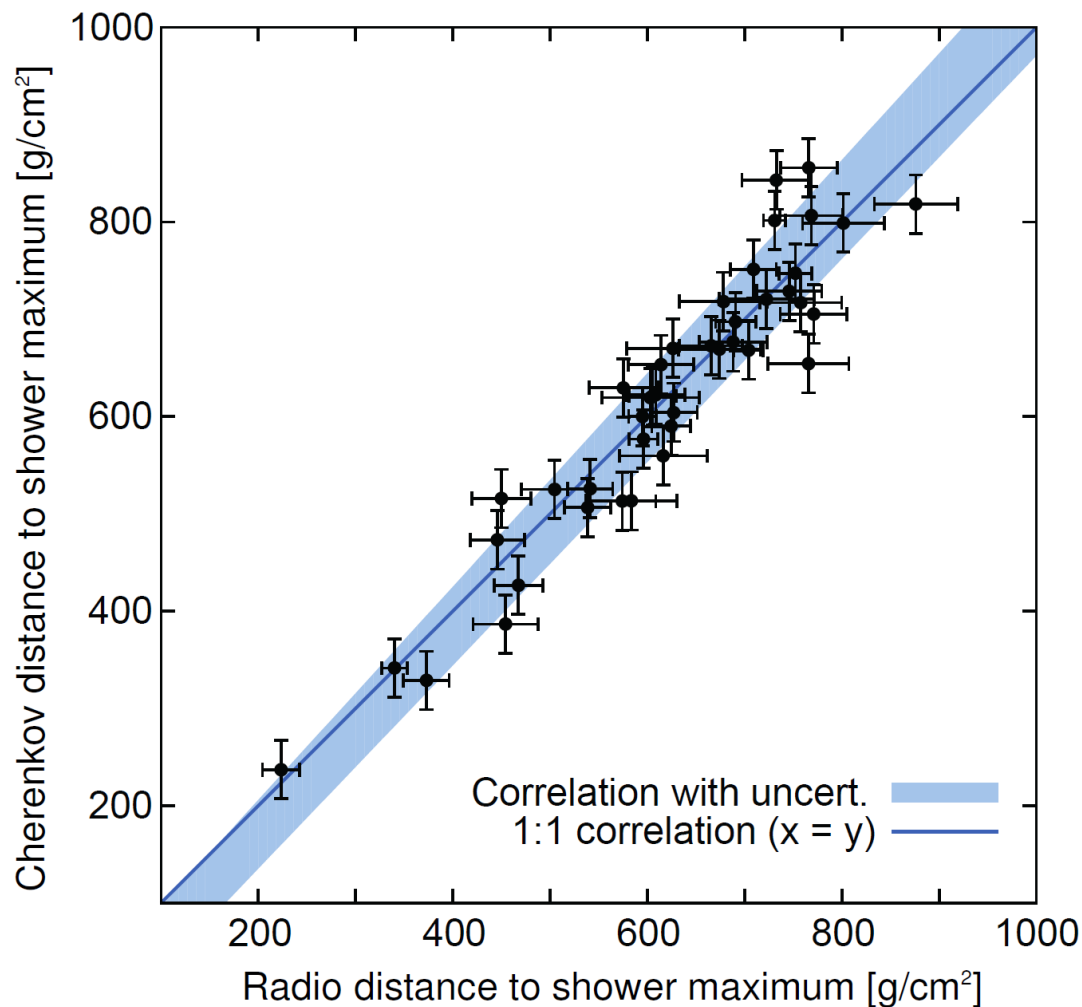


vertical proton shower
at 40-80 MHz
simulated with CoREAS



vertical iron shower
at 40-80 MHz
simulated with CoREAS

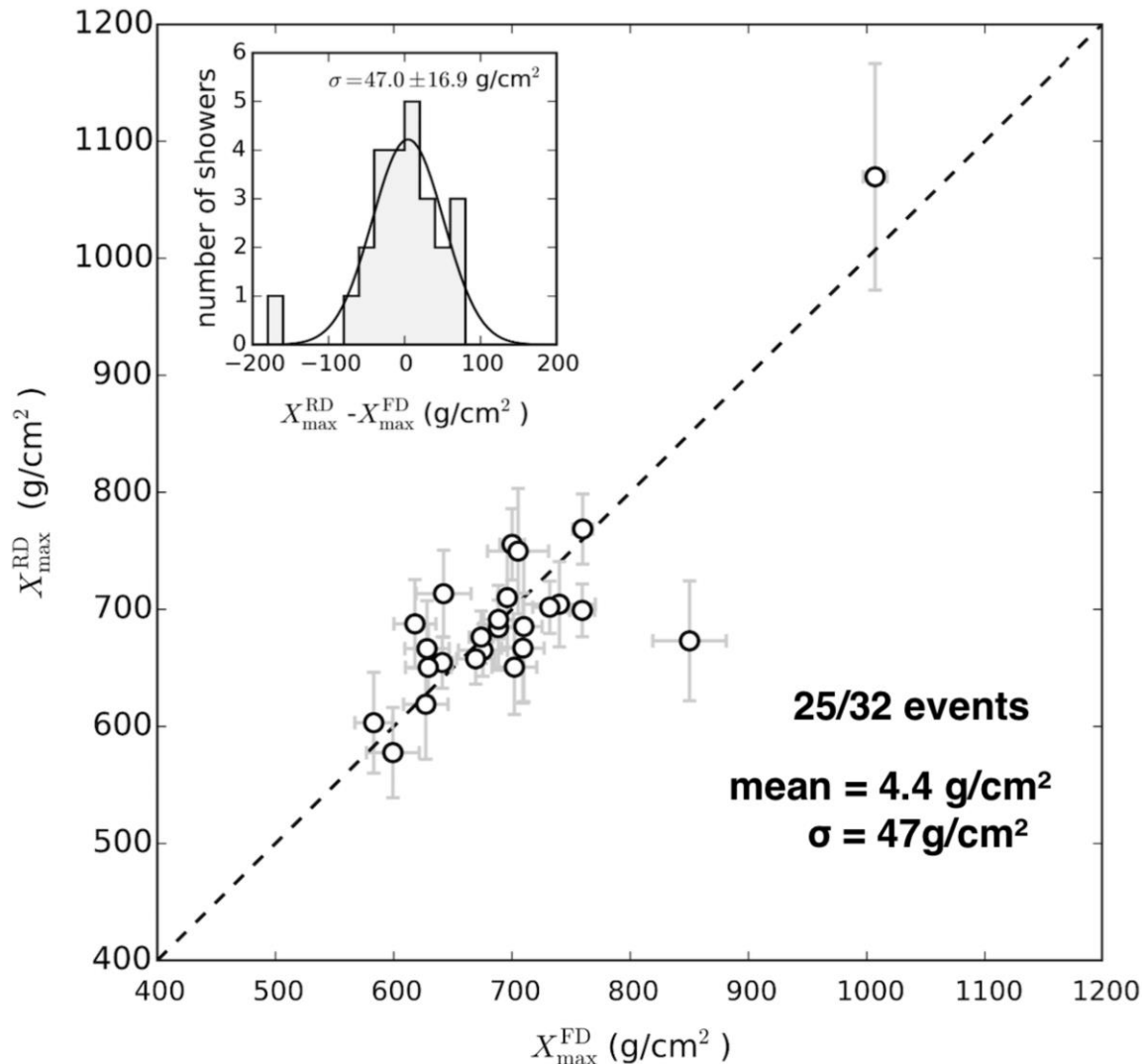
Experimental Xmax validation by Tunka-Rex



- slope of radio-LDF as Xmax estimator
- Xmax from optical Cherenkov detectors and radio antennas agrees very well
- combined Xmax resolution ~ 50 g/cm², Tunka alone ~ 28 g/cm²

Tunka-Rex Coll., JCAP (2016),
[arXiv:1509.05652](https://arxiv.org/abs/1509.05652).

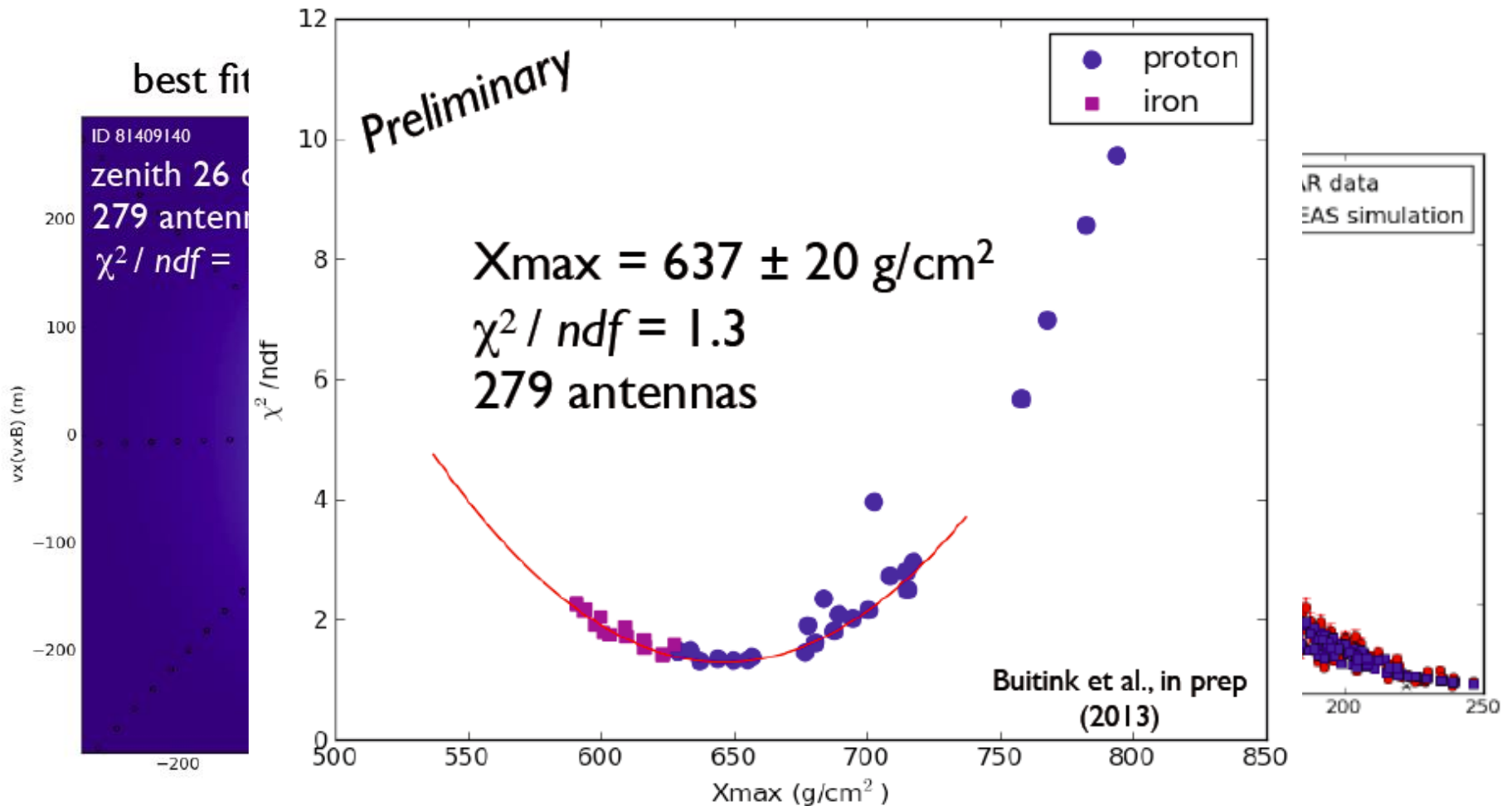
Experimental Xmax validation by Auger



- currently various reconstruction approaches being tested in AERA
- current combined FD-RD resolution of $\sim 45 \text{ g/cm}^2$, so AERA alone $< \sim 40 \text{ g/cm}^2$
- still room for improvement (only uses amplitude information)

F. Gaté for the Pierre Auger Coll., ARENA2016, arXiv:1609.06510

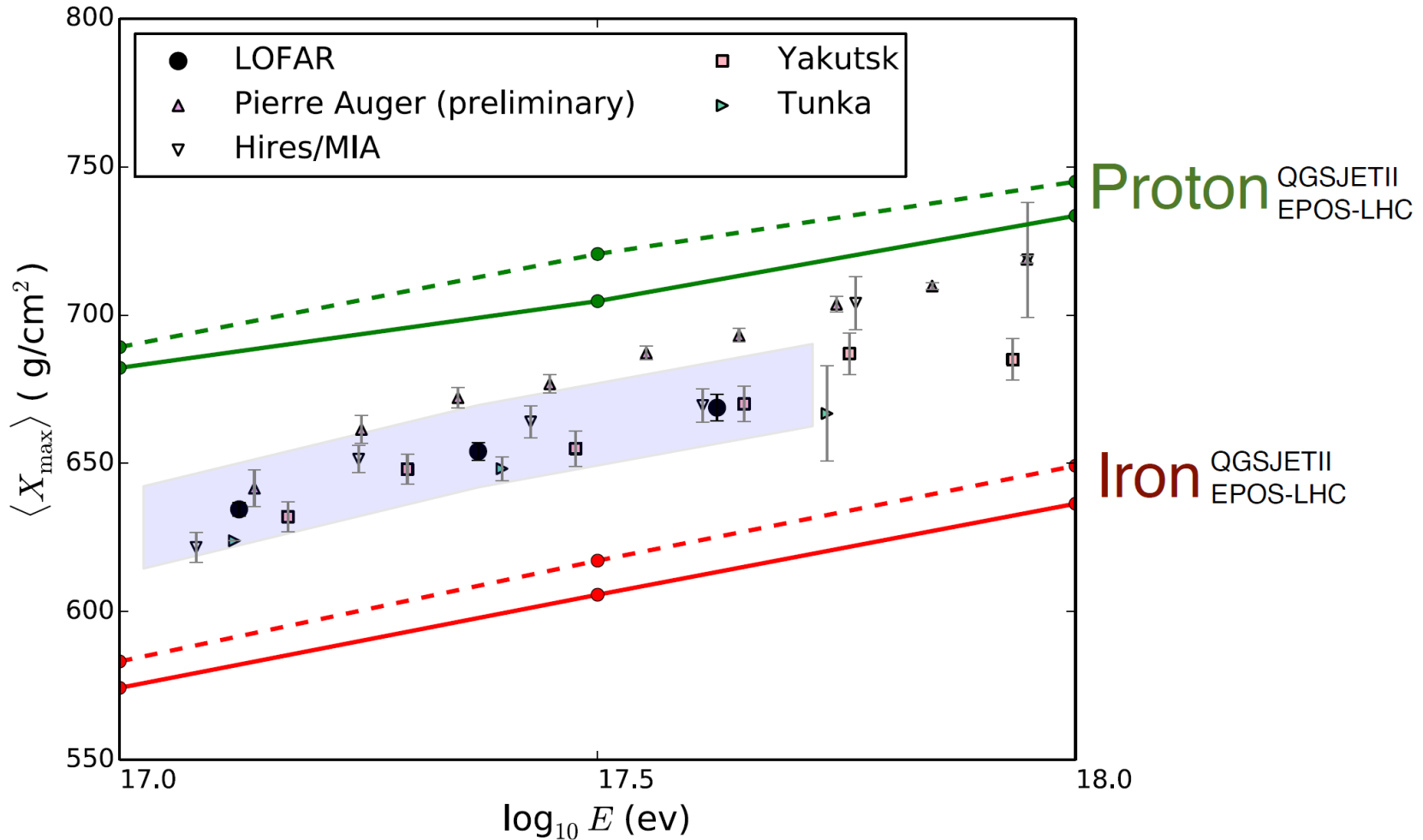
Global fit of particle and radio LDF with LOFAR



■ global fit to CoREAS simulations gives X_{max} to $\sim 17 \text{ g/cm}^2$

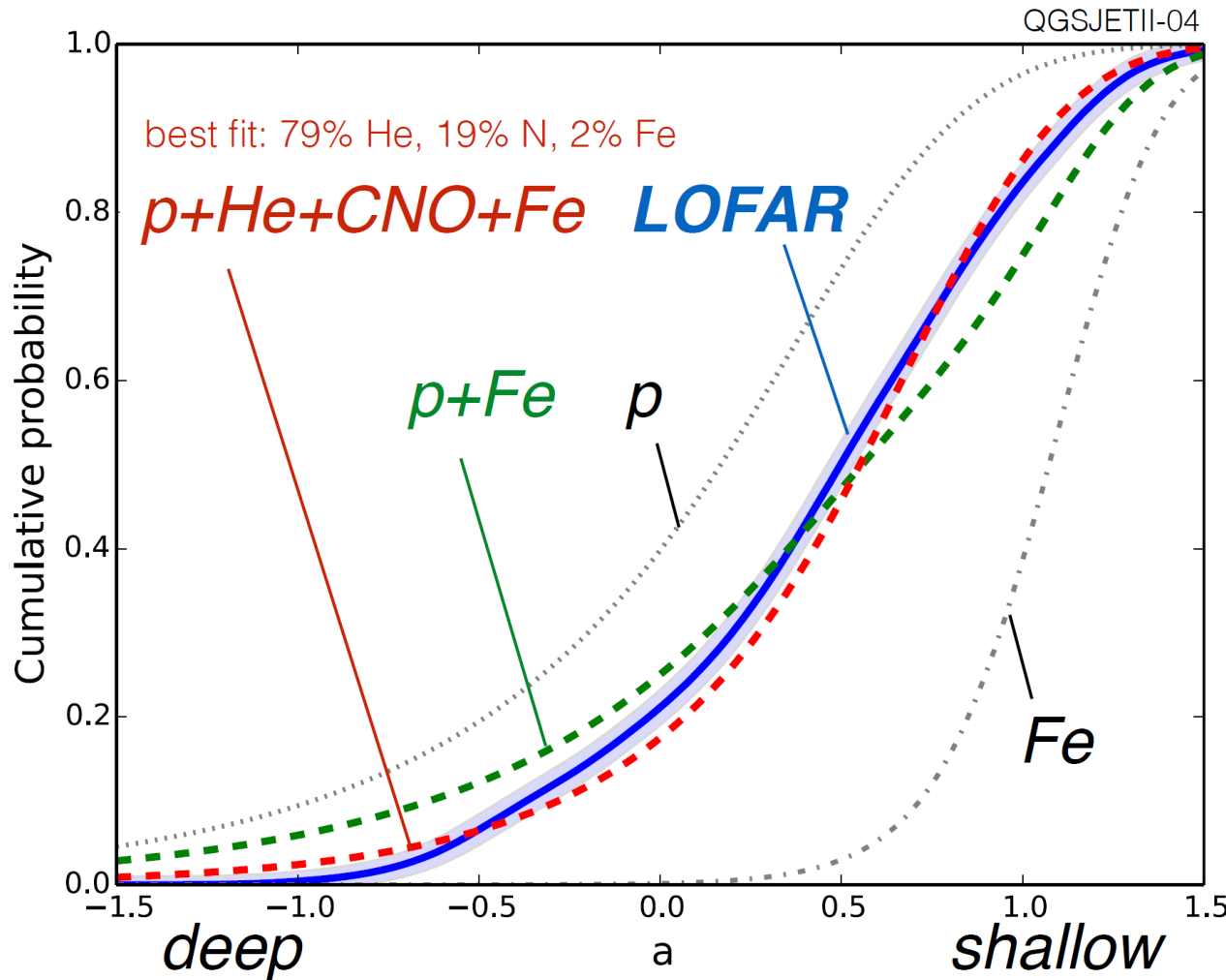
S. Buitink et al., Phys. Rev. D 90 (2014) 082003, S. Buitink et al. Nature 435 (2016) 70

Lofar $\langle X_{\max} \rangle$ results



S. Buitink et al. Nature 435 (2016) 70

LOFAR unbinned analysis



- compare measured distribution of
- $$a = \frac{\langle X_{\text{proton}} \rangle - X_{\text{shower}}}{\langle X_{\text{proton}} \rangle - \langle X_{\text{iron}} \rangle}$$
- with simulated distributions
 - result shows large fraction of light primaries at 10^{17} - $10^{17.5}$ eV

S. Buitink et al. Nature 435 (2016) 70

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- $\sigma < 0.5^\circ$
- $\sigma_{X_{\max}} < 20 \text{ g/cm}^2$ dense (< 40 sparse)

How expensive are individual detectors?

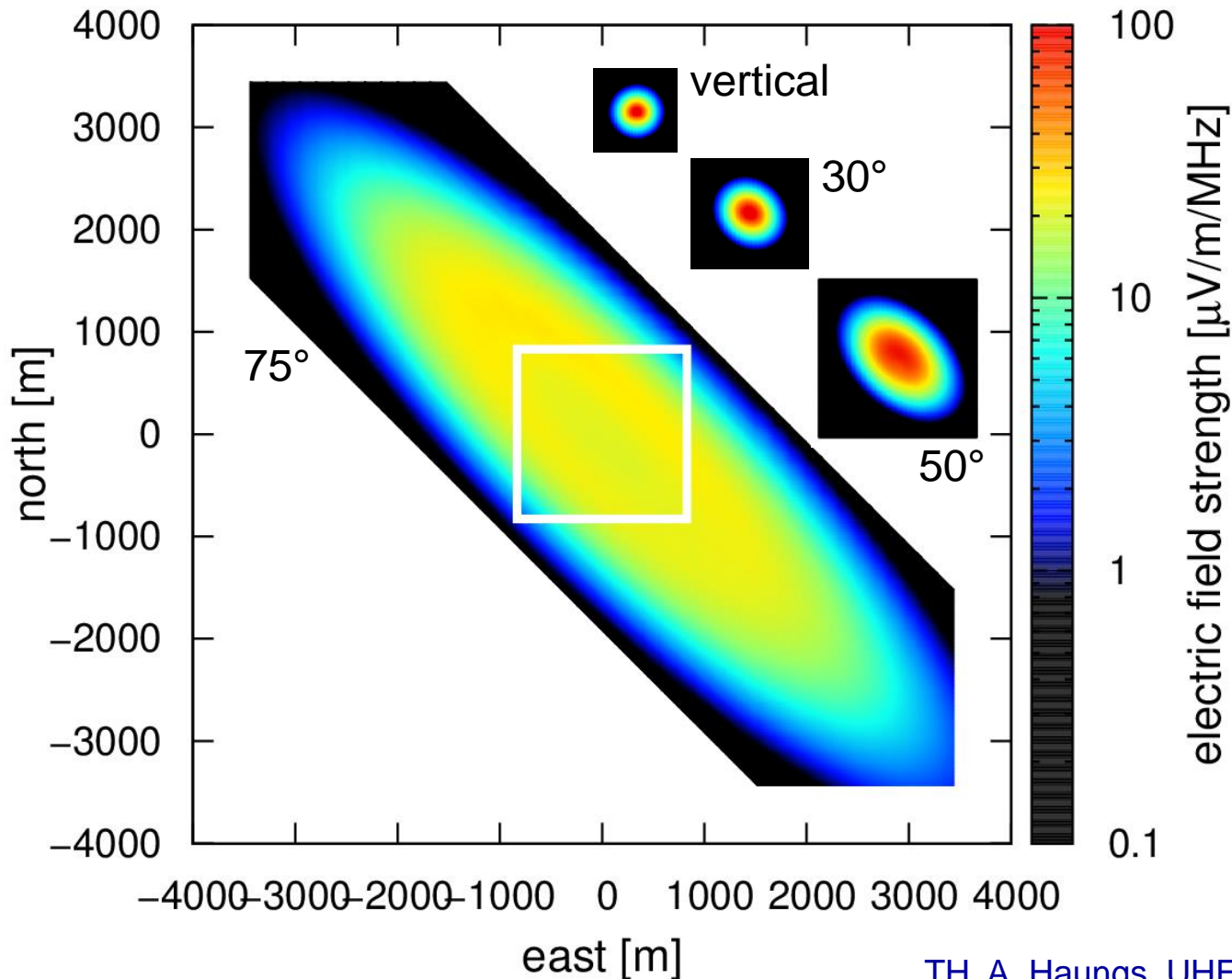


- antenna can be cheap, SALLA antenna plus low-noise amplifier costs <500 US\$
- digital electronics more expensive, but profit from Moore's law
- most expensive part is „infrastructure“ (power supply, communications, ...)
- sub-1000\$ for antenna plus digital electronics certainly seem feasible

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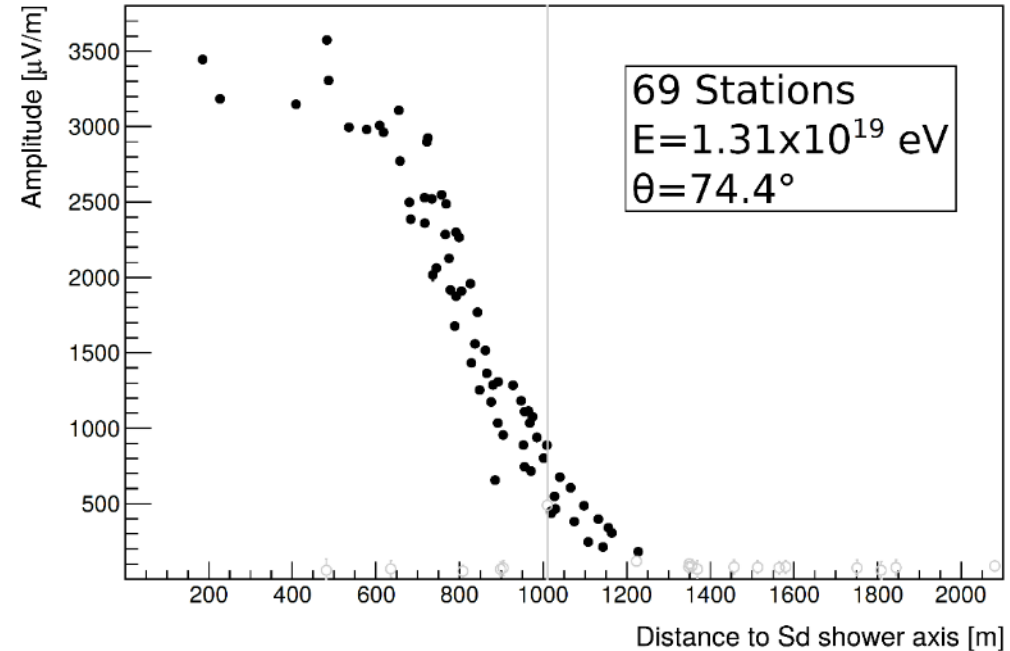
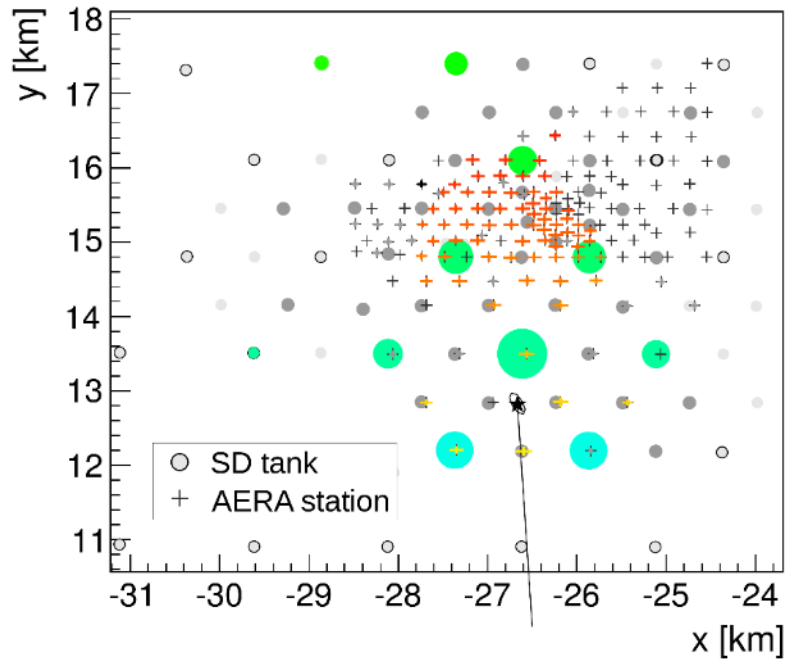
Required detector spacing – inclined showers



- large source distance leads to very large radio emission footprints in inclined air showers
- should be detectable with sparse arrays

TH, A. Haungs, UHECR2014, arXiv:1507.07769.

Large-scale showers measured by AERA



- air showers up to 83° zenith angle measured
- footprints with radii up to 2 km in shower plane
- detection with 1.5 km antenna grid would be sufficient

O. Kambeitz for the Pierre Auger Collaboration, ARENA2016 conference, arXiv:1609.05456

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Strengths and limitations of radio detection

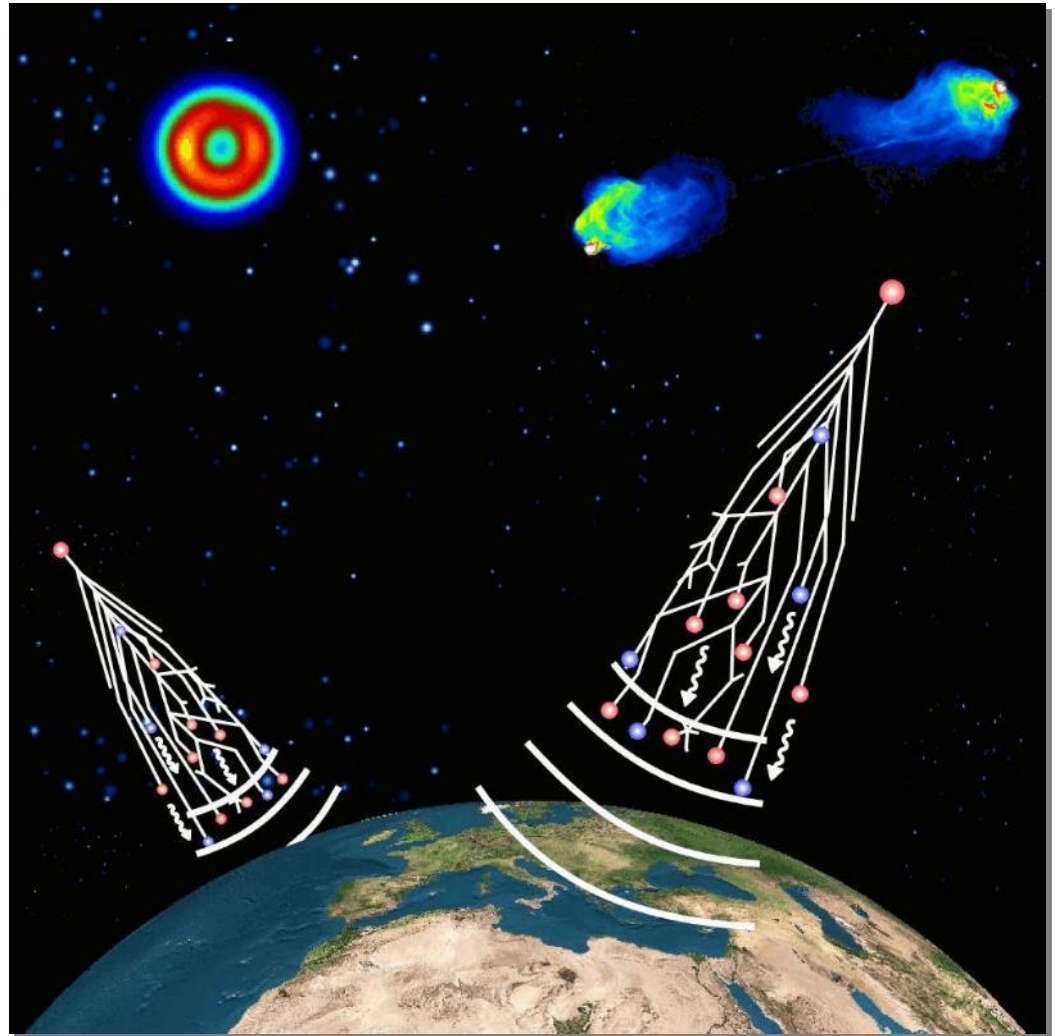
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- cut heavily or rely on simulations
- $E > 10^{17}$ eV, exploit external triggers

Contents

- achievements of radio detection
- what can radio do for (U)HECR science

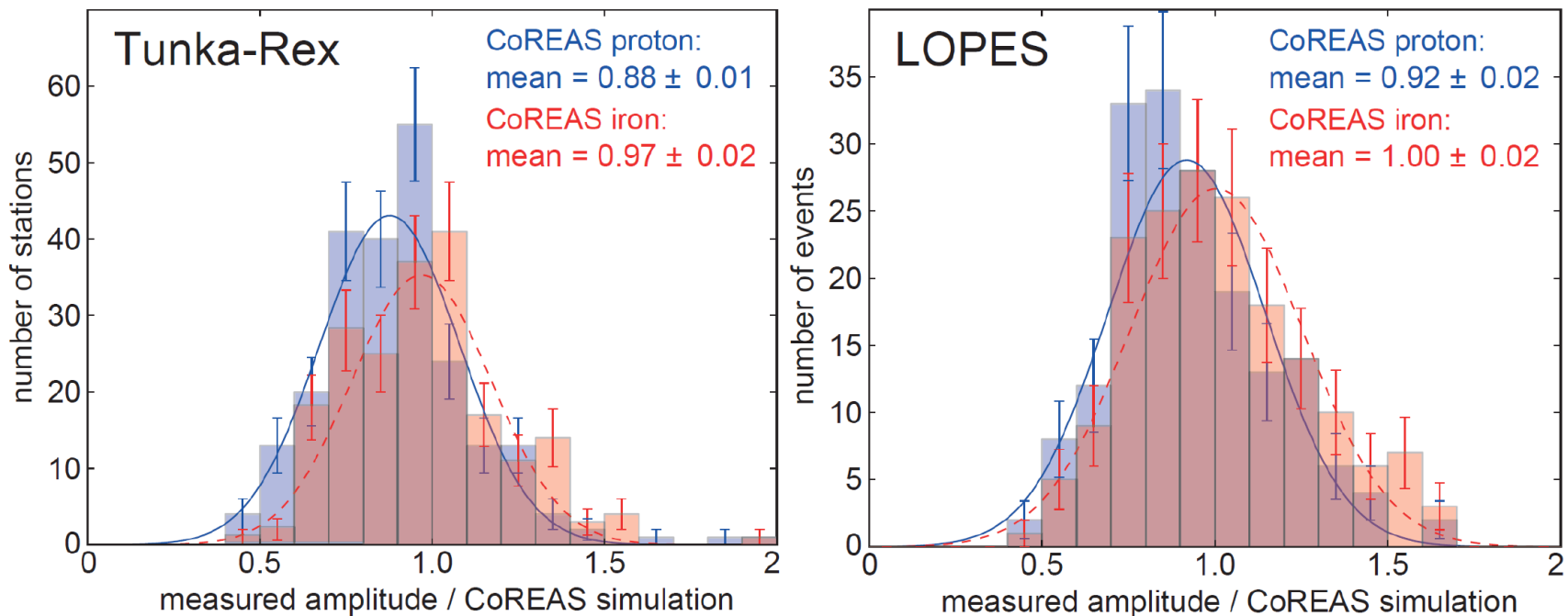


Improvement of hybrid measurements

- existing cosmic-ray detectors can often be equipped with radio antennas at limited cost (re-use „infrastructure“)
- incorporation of radio detectors provides many advantages
 - pure measurement of electromagnetic component
 - good energy resolution
 - Xmax measurements with 100% duty cycle
 - generally different systematic uncertainties
- caveat: for non-inclined showers detector spacing of ~200-300 m required, so interesting in energy range 10^{17} to few times 10^{18} eV

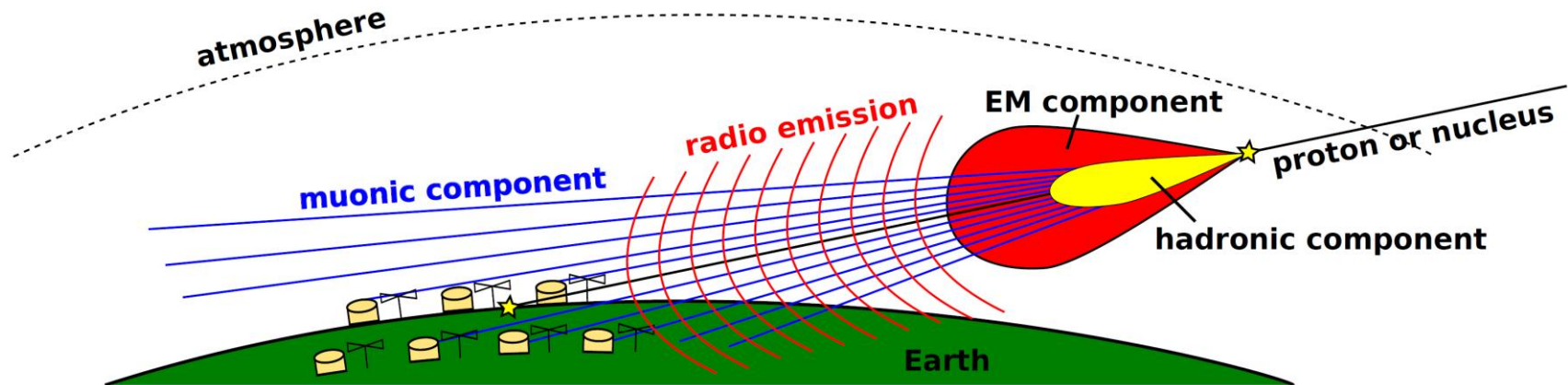
(Cross-)calibration of the energy scale

- many uncertainties in data interpretation are related to uncertainties of the absolute energy scale
- measuring radio emission allows calibrating the energy scale
 - among different experiments (e.g., Auger's radiation energy@ 10^{18} eV)
 - against first-principle calculations (within 10% seems feasible)



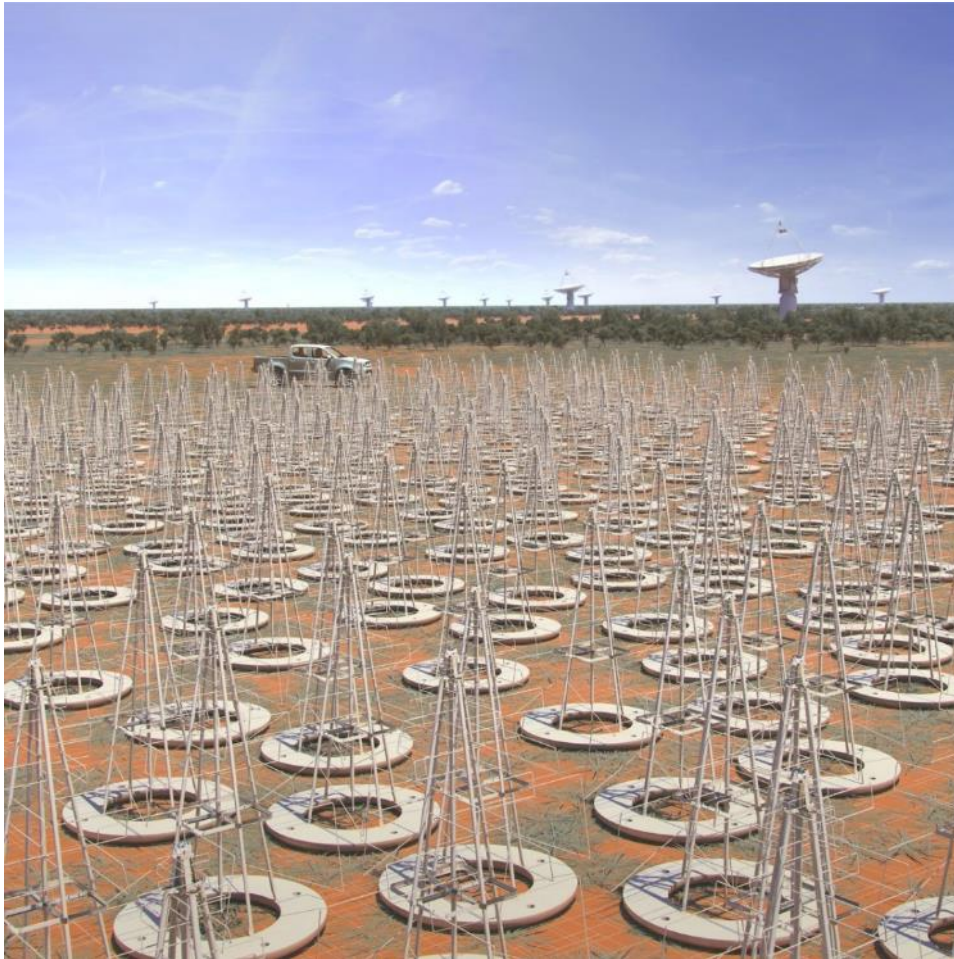
Tunka-Rex & LOPES Collaborations, ARENA 2016 and submitted to PLB

Radio measurements of inclined showers



- combined measurements of inclined showers with particle detectors and radio antennas are an attractive option
 - particle detectors measure muons, radio detectors measure em component
 - range $> \sim 10^{18}$ eV will be above Galactic noise
 - common detector grid spacing – can share infrastructure – lower cost
 - useful also as veto for neutrino-induced air showers (small footprint)
- radio detection generally seems to be the most favorable technique to measure the electromagnetic component of inclined air showers
- see also plans for GRAND experiment for detection of neutrinos

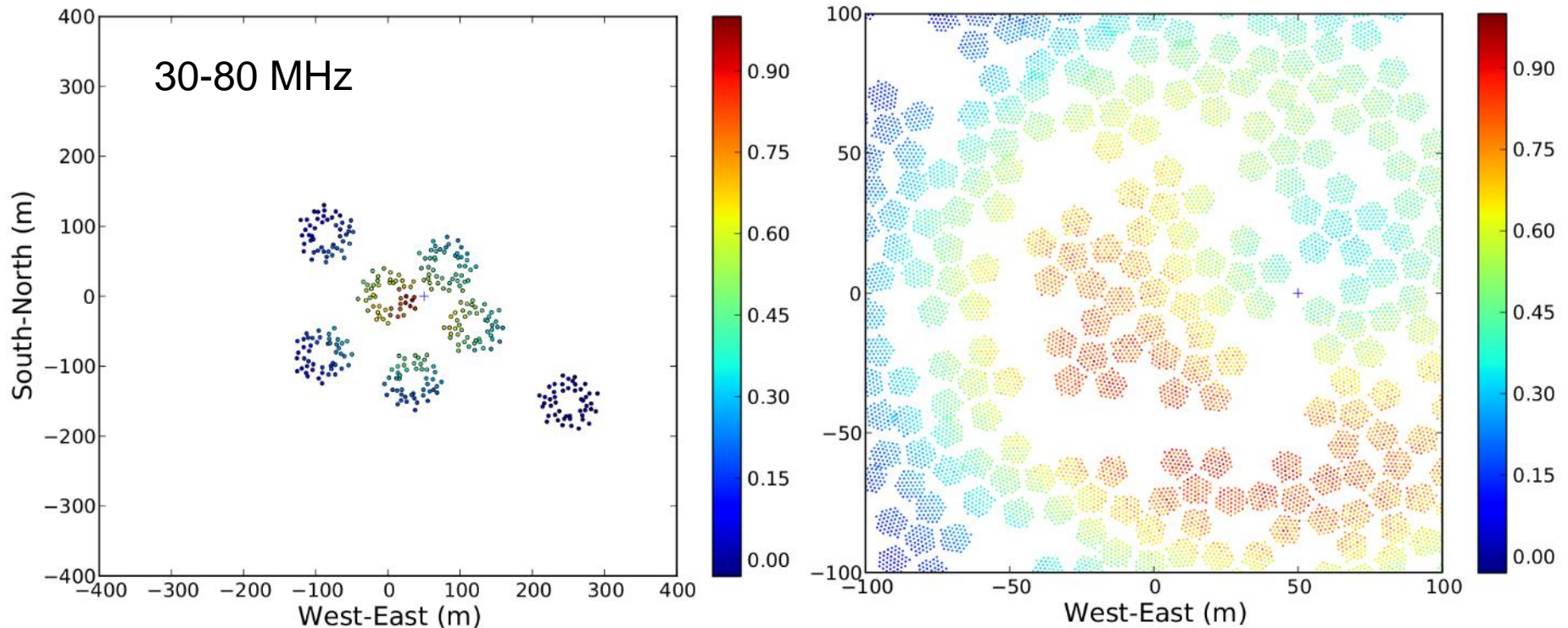
Very dense arrays - Square Kilometre Array



- in the final design stages
- to be built in western Australia
- first science 2020
- planned completion 2023
- >60,000 dual-polarized antennas within 750 m diameter
- bandwidth 50-350 MHz
- can be used for air shower detection with minor additions
- precision measurements in energy range of $\sim 10^{16.5}$ to $10^{18.5}$

TH et al., ARENA2016 conference, arXiv:1608.08869

SKA will provide precision measurements



- **Xmax determination with well below 10 g/cm^2 resolution predicted by simulation study based on LOFAR reconstruction approaches**

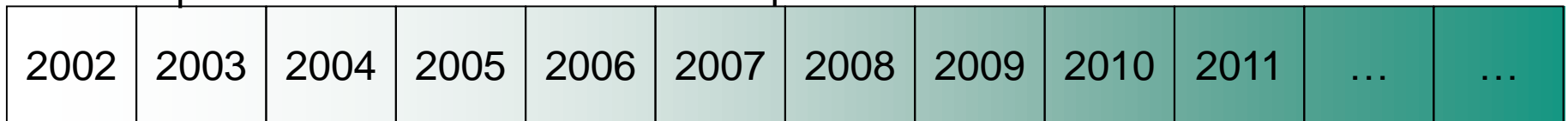
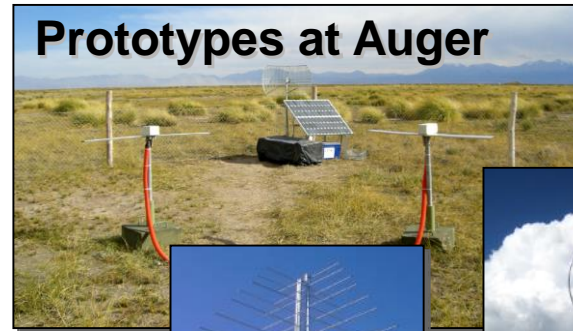
A. Zilles et al., ARENA2016 conference

Summary and conclusions

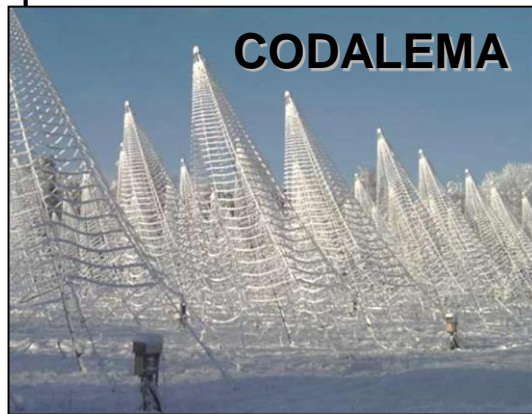
- radio detection of CRs has boomed and matured in the last decade
- we have clearly established
 - detailed understanding of complex radio emission physics (within 10%)
 - determination of arrival direction (well below 0.5°)
 - determination of air shower energy ($\sim 15\%$, room for improvement)
 - radio signal sensitivity to X_{\max} ($< 20 \text{ g/cm}^2$ for dense arrays and 40 g/cm^2 for sparse arrays, but with significant room for improvement)
- potential for application
 - high-duty-cycle energy & mass reconstruction in hybrid arrays
 - cross-calibration of the energy scale of cosmic-ray detectors
 - independent calibration of energy scale from first principle calculations
 - air shower physics via measurement of purely electromagnetic cascade

Backup slides

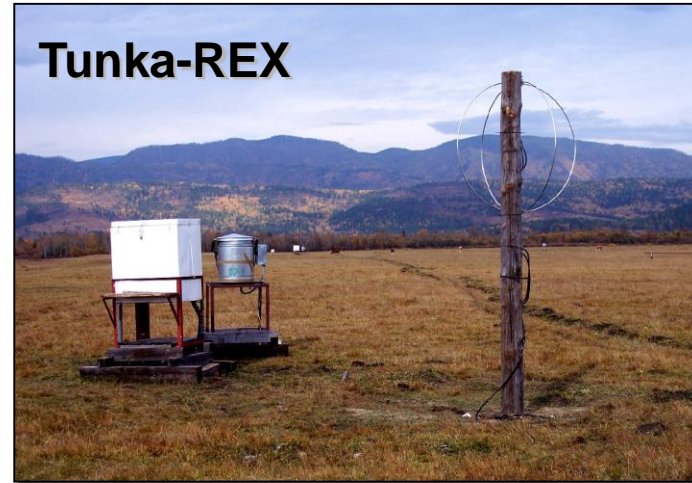
First-Generation modern MHz experiments



Falcke & Gorham propose „geosynchrotron approach“



Second-Generation modern MHz experiments



2010

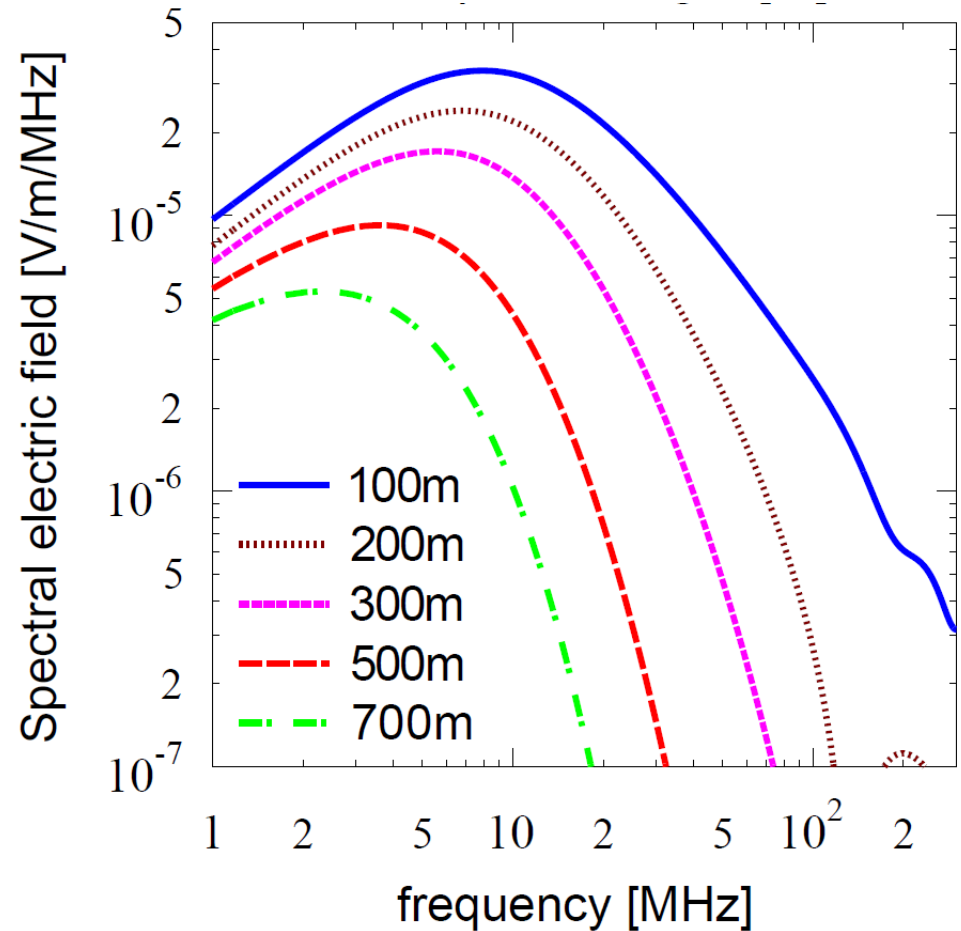
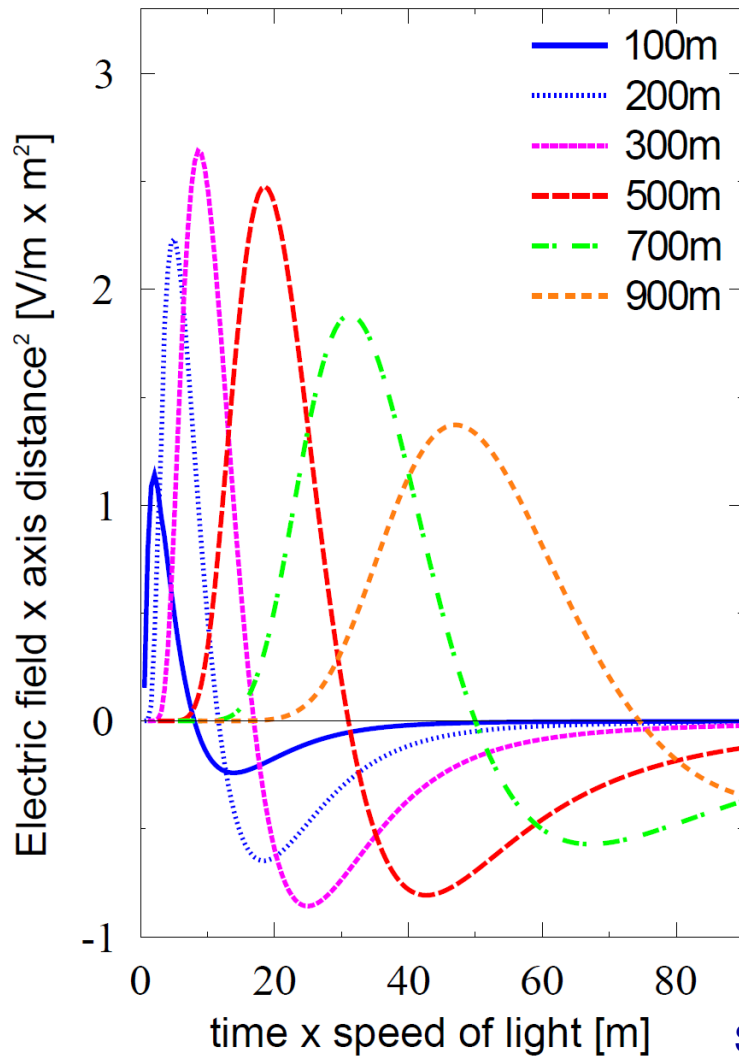
2011

2012

2013



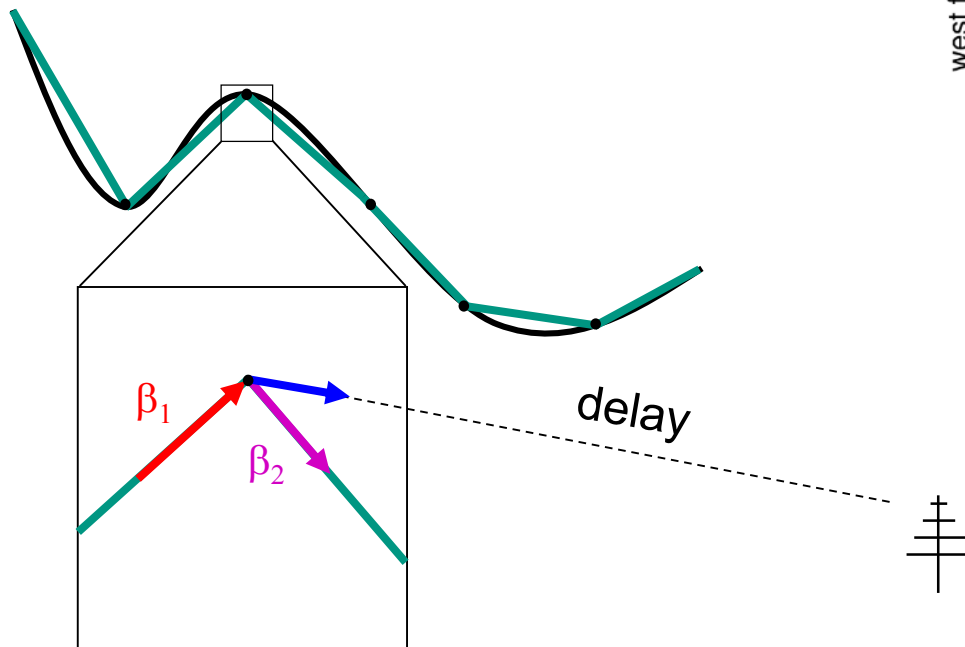
Broad-band pulses – mostly in MHz regime



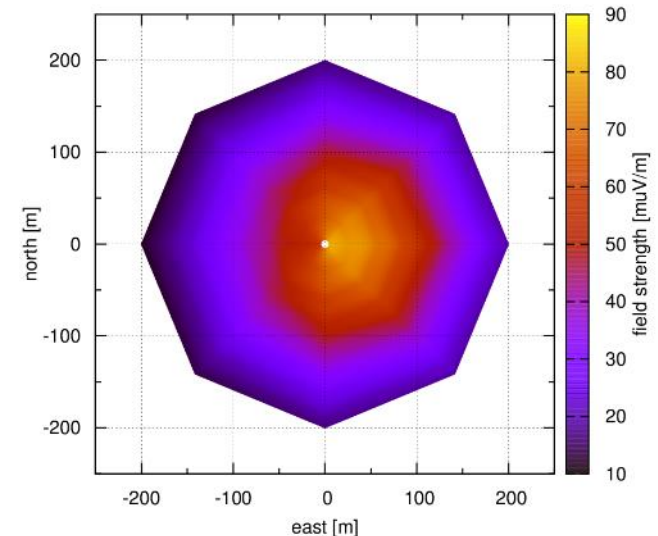
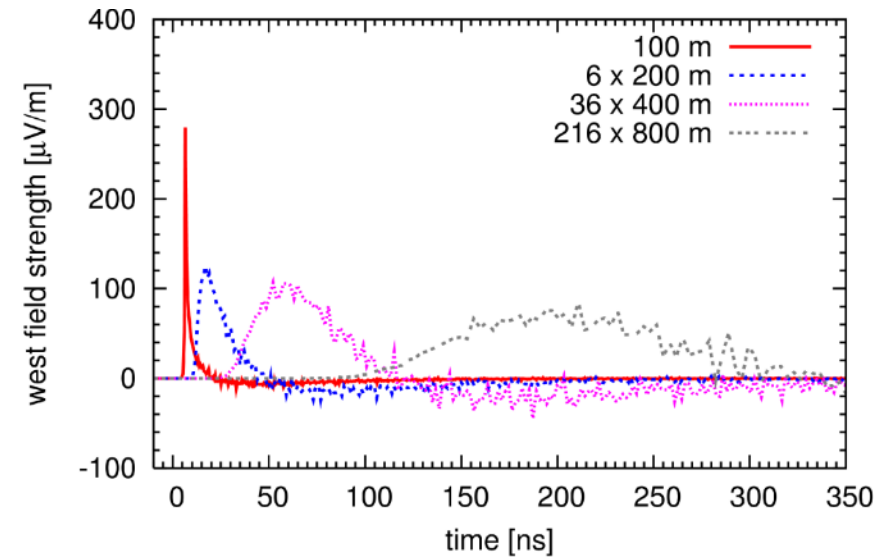
Scholten, Werner, Rusydi, *Astropart. Phys.* 29 (2008) 94–103.

Radio emission simulations – a vital tool

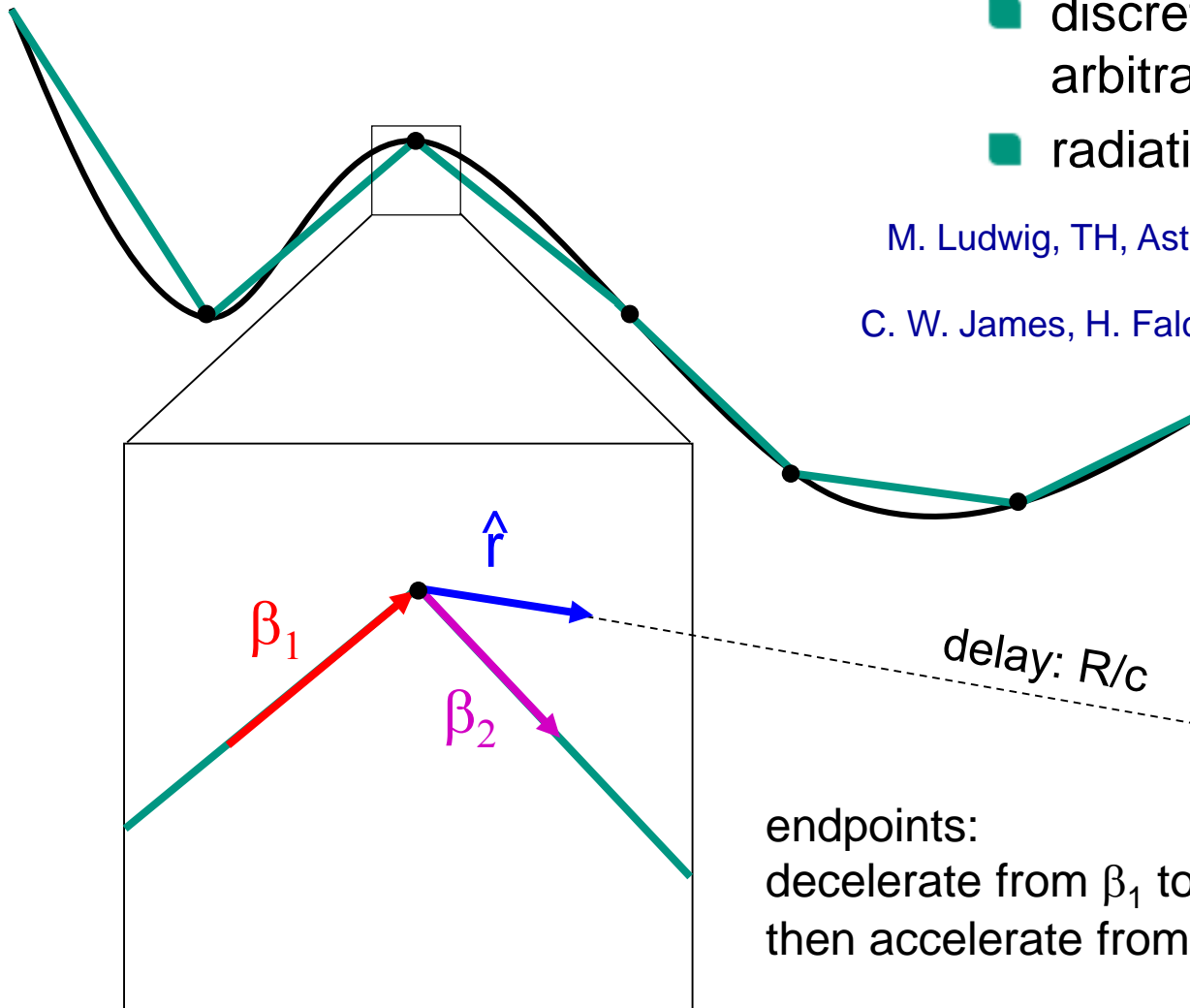
- full-scale air shower Monte Carlo
- „endpoint formalism“ for the calculation of radio emission
- codes CoREAS and ZHAireS



James, Falcke, Huege, Ludwig, Phys. Rev. E. 84, 056602
Ludwig & Huege, Astrop. Physics 34, 438-446



CoREAS: endpoint formalism plus shower sim

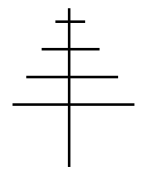


- discrete formulation for arbitrarily complex motion
- radiation *only* from endpoints

M. Ludwig, TH, *Astropart. Phys.* 34 (2011) 438–446.

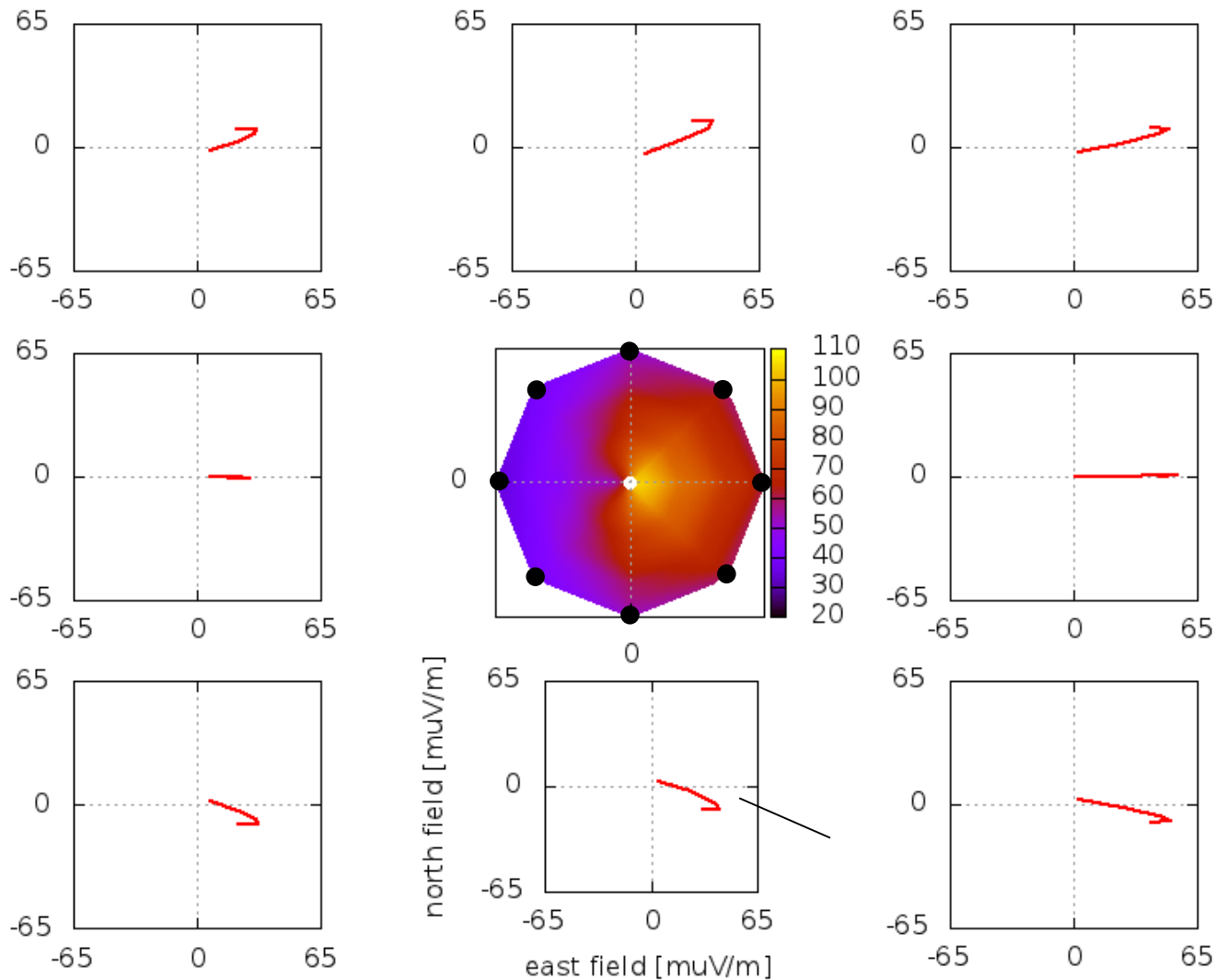
C. W. James, H. Falcke, TH, M. Ludwig, *Phys. Rev. E* 84 (2011) 056602.

endpoints:
decelerate from β_1 to rest
then accelerate from rest to β_2



antenna

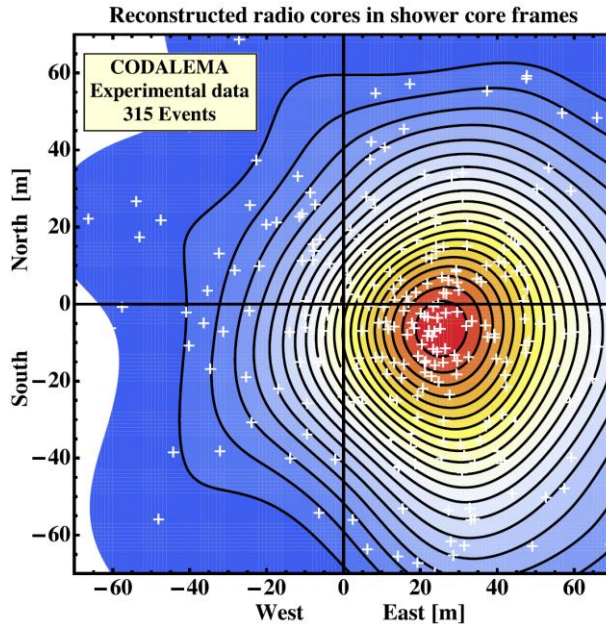
Complexity of signal polarization



- complex time evolution of electric field vector
- superposition of geomagnetic and charge excess emission

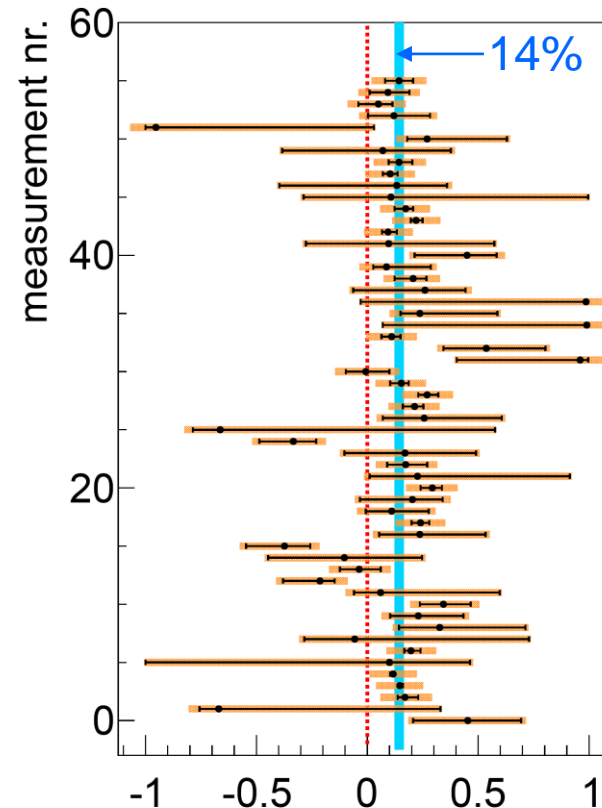
CoREAS simulations,
TH et al., see id 548

Geomagnetic seen by all – but charge excess?



- CODALEMA reports core-shift \leftrightarrow east-west asymmetry \leftrightarrow charge-excess at ICRC 2011

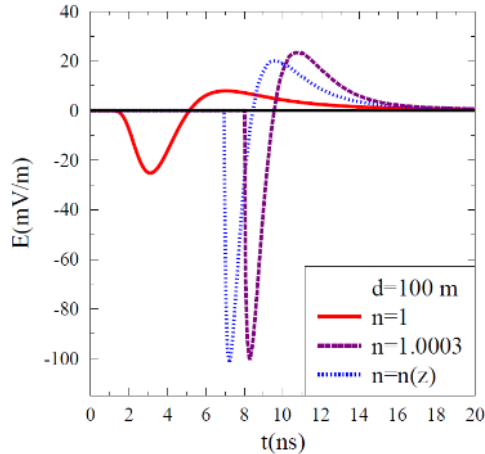
CODALEMA Coll., Astropart. Phys. 69 (2015) 50–60.



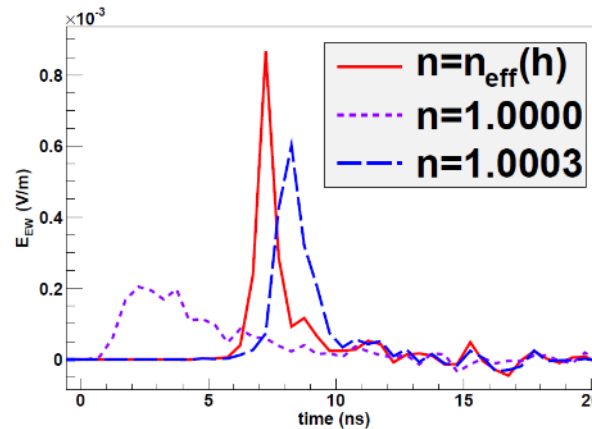
- AERA quantifies radial component to $14 \pm 2\%$

Pierre Auger Coll., Phys. Rev. D 89 (2014) 052002.

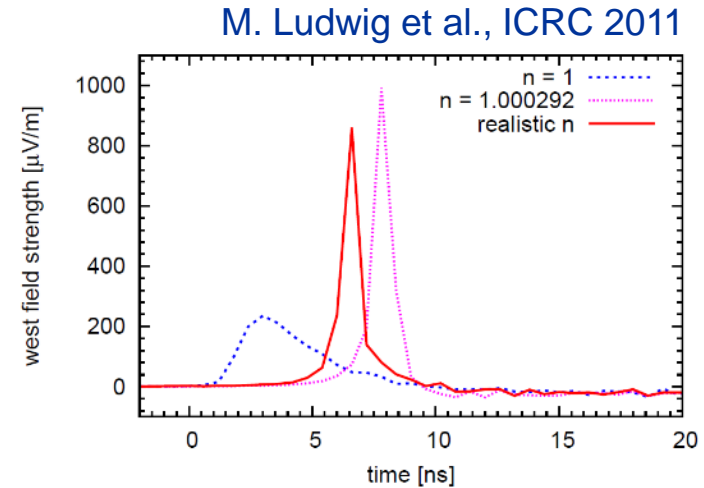
Refractive index effects



K.D. de Vries et al,
PRD (2010)

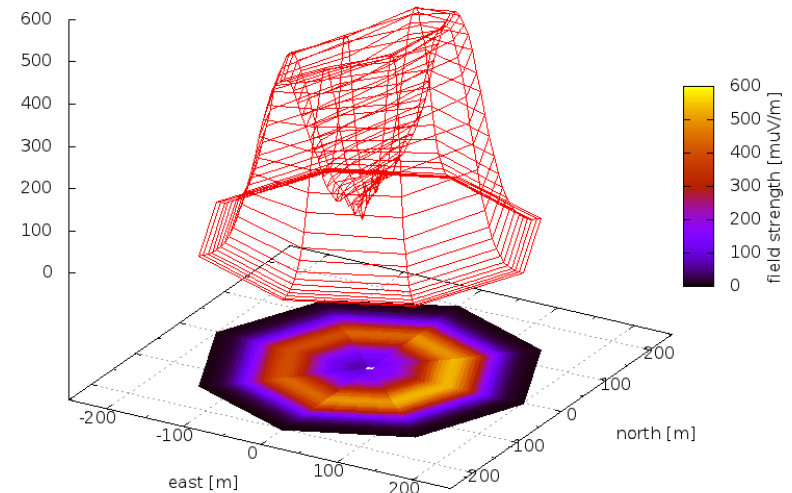


Alvarez-Muniz et al.,
Astrop. Phys. (2011)



M. Ludwig et al., ICRC 2011

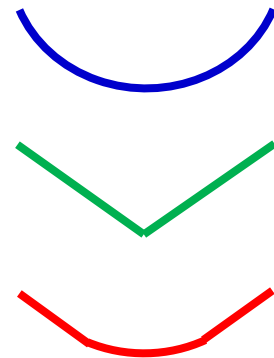
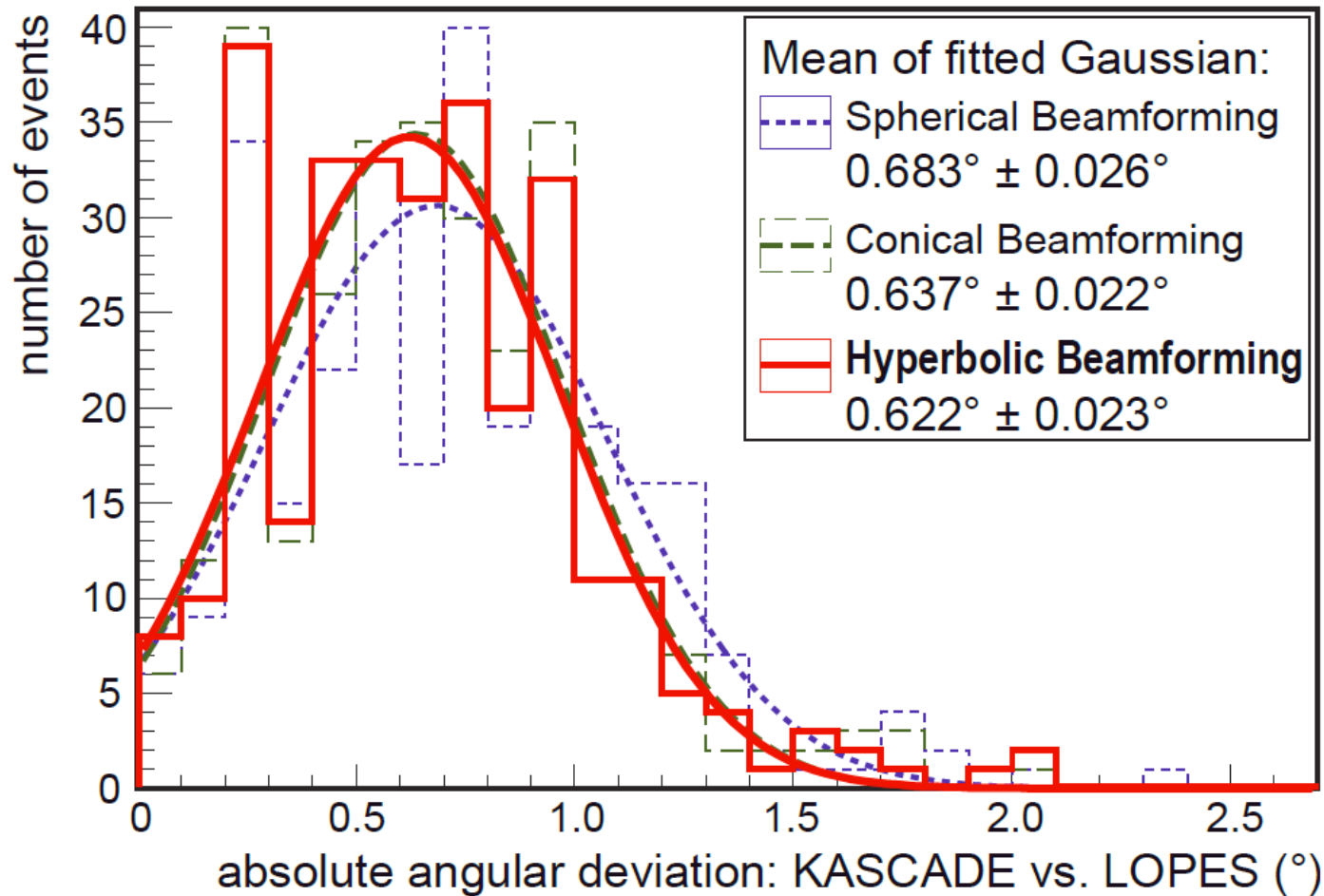
- time compression of radio pulses along the Cherenkov angle
 - power at high frequencies, up to several GHz
 - Cherenkov ring arises



TH et al., ARENA2012

300-1200 MHz

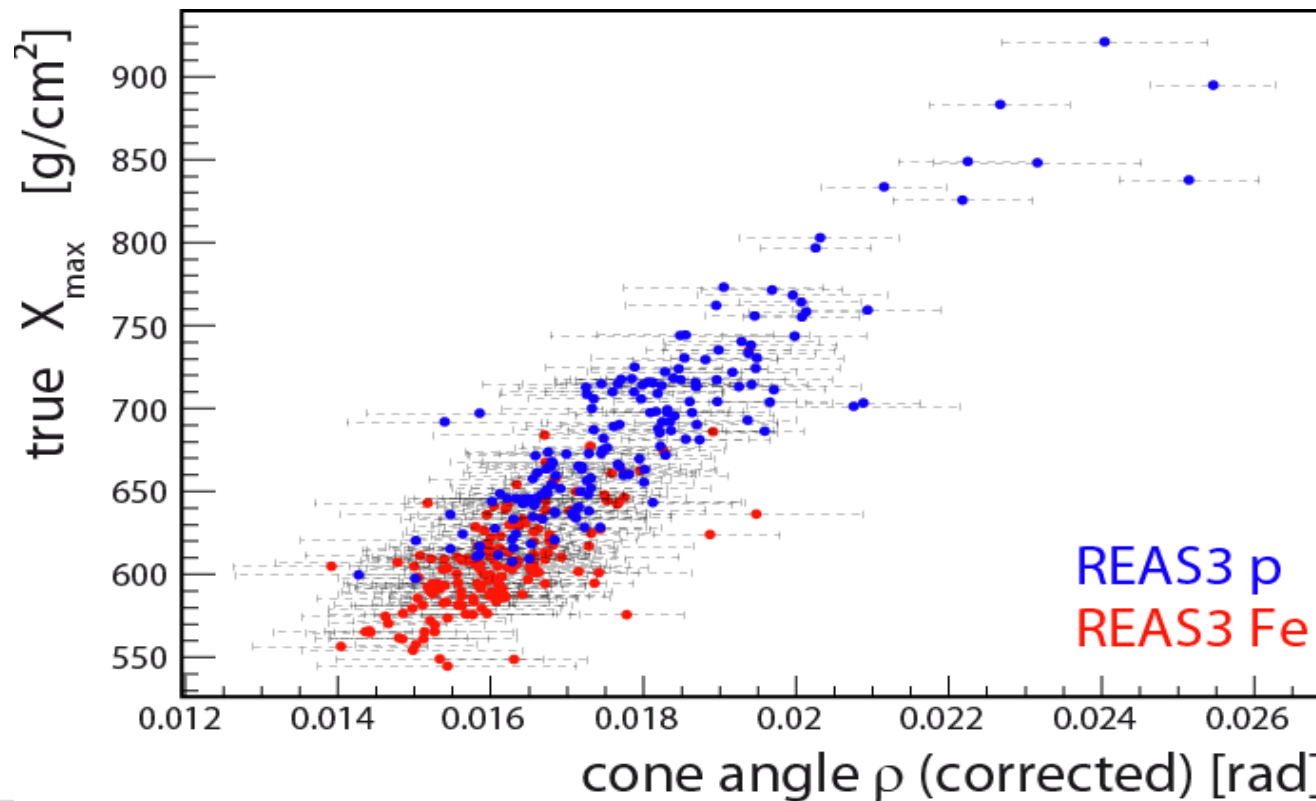
Accuracy of direction reconstruction



■ from simulations:
LOPES
alone better
than 0.1°

X_{\max} reconstruction with cone angle

- X_{\max} proportional to ρ after correction for zenith angle
 - precision: $\sim 30 \text{ g/cm}^2$ for REAS3 simulations without noise
 - precision: $\sim 200 \text{ g/cm}^2$ for LOPES measurements



LOPES,
ICRC 2011

External versus self-triggering

■ external triggering works well

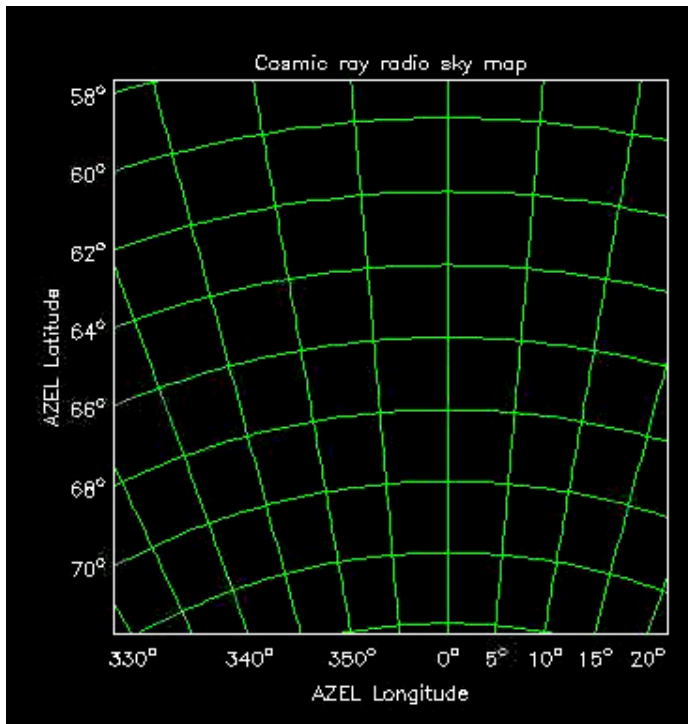
- LOPES
- CODALEMA
- AERA
- LOFAR

Is a self-triggering stand-alone radio detector what we really need? Do we not strive to do hybrid measurements anyway?

■ self-triggering is very challenging

- transient noise (RFI)
- it has been done successfully
 - TREND
 - AERA prototype and AERA
 - CODALEMA-III
- but: radio trigger purity is very low
 - need coincidence with other detector for clear identification
 - or need to use many details of radio signal (LDF, polarization) to identify air showers - what is realistic in a low-level trigger?

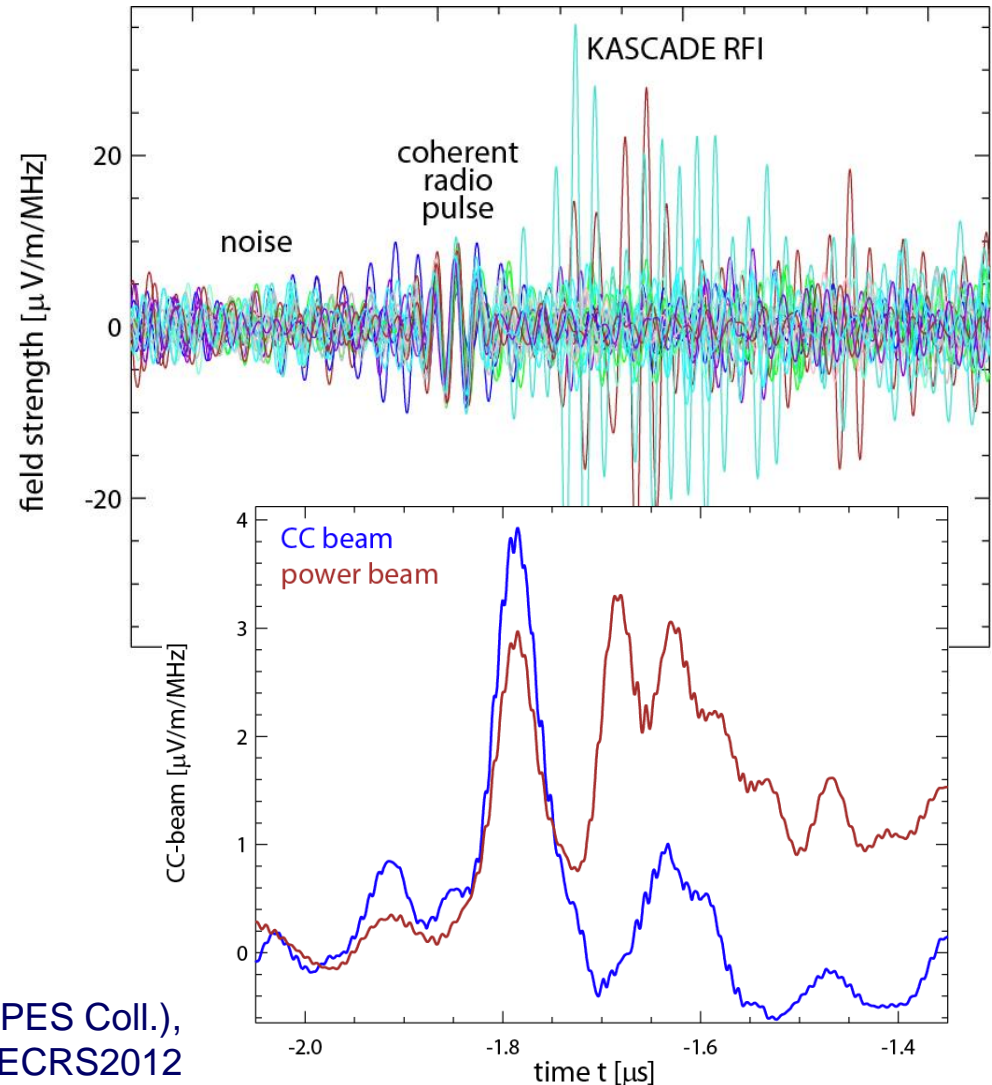
Direction reconstruction with interferometry



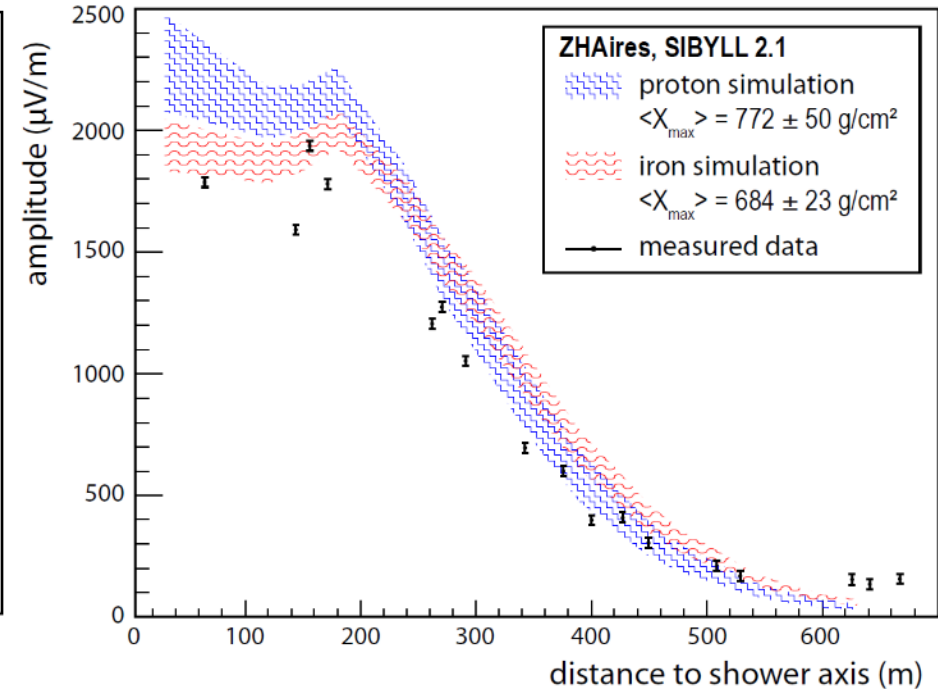
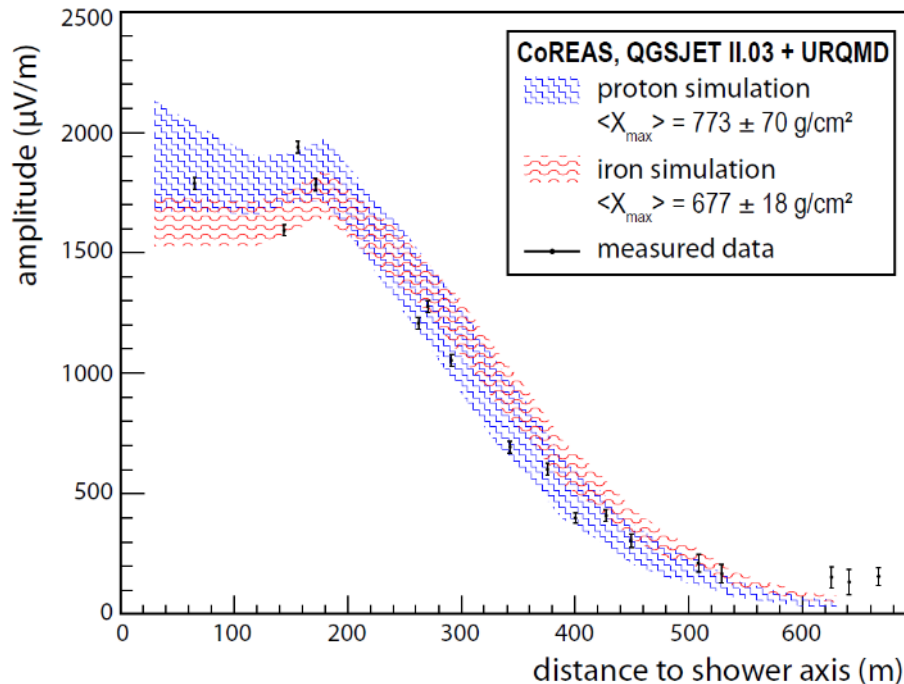
Sky map of a cosmic ray radio flash

H. Falcke et al. (LOPES Coll.), Nature 2005

F.G. Schröder et al. (LOPES Coll.), ECRS2012



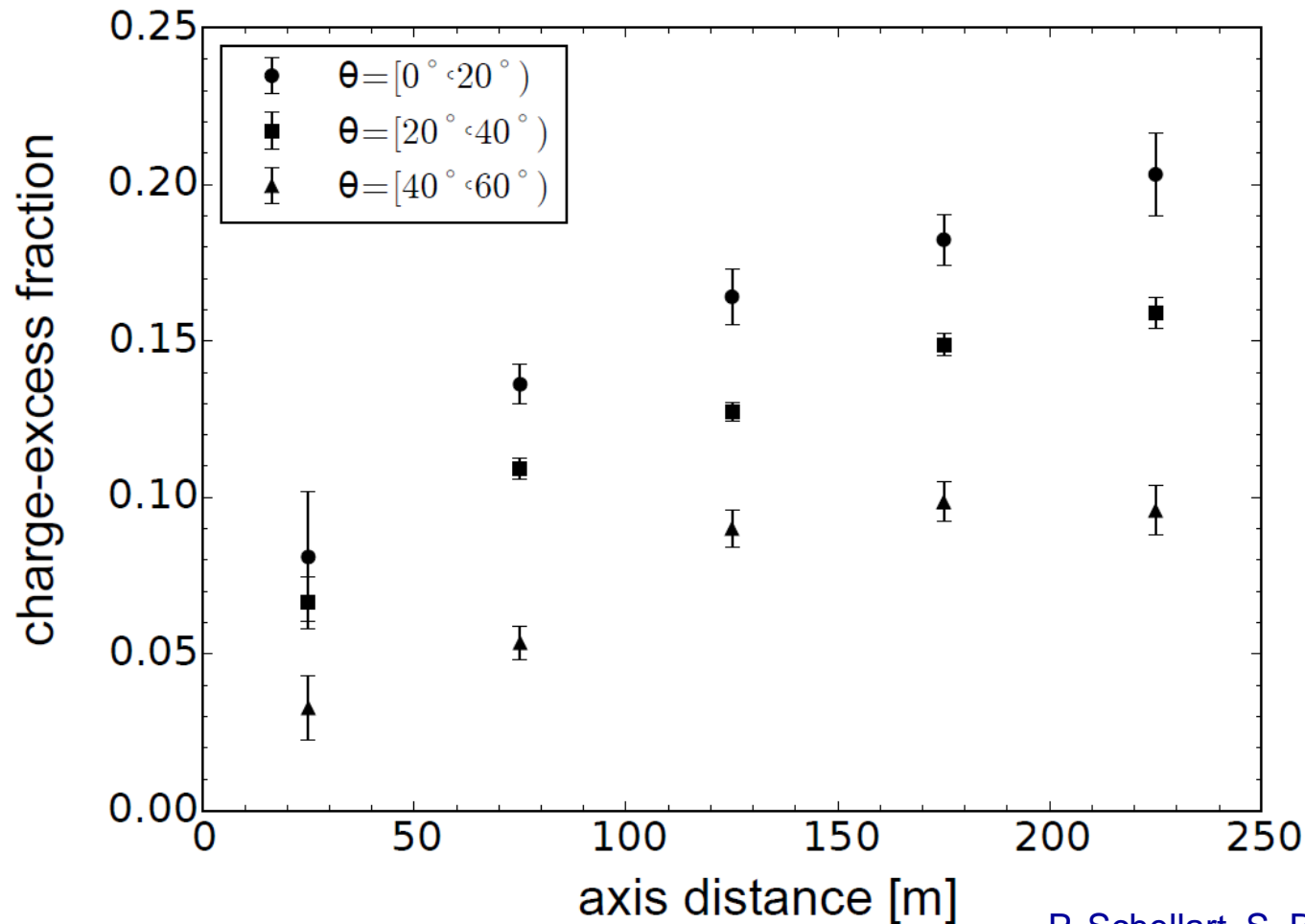
Comparison of simulations with AERA data



- AERA provides detailed, well-calibrated event data
- simulations can reproduce measurements
 - absolute amplitude
 - complex LDF

Pierre Auger Collaboration, ICRC2013, id #899

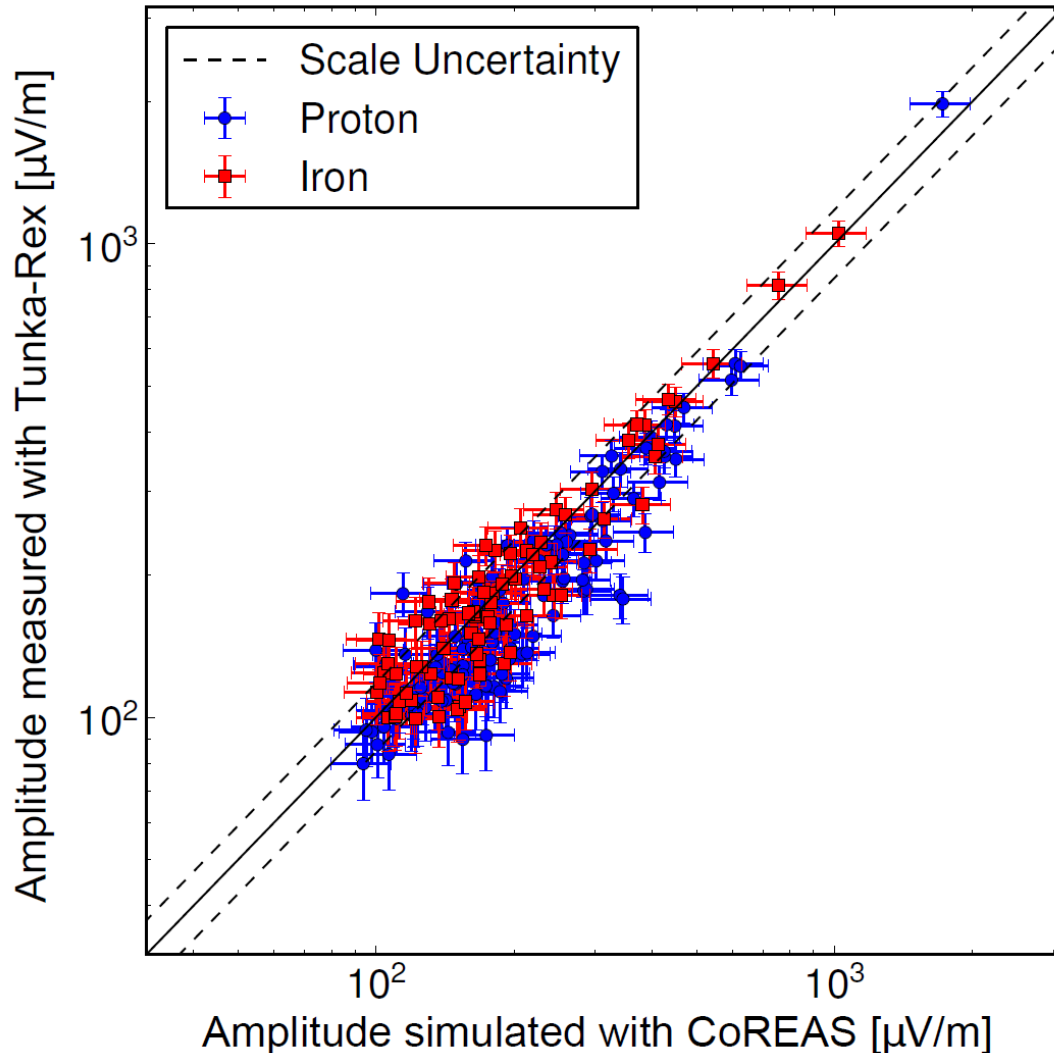
Charge excess contribution is not a constant



- depends on shower azimuth angle and observer lateral distance

P. Schellart, S. Buitink, A. Corstanje, et al.,
JCAP 10 (2014) 14.

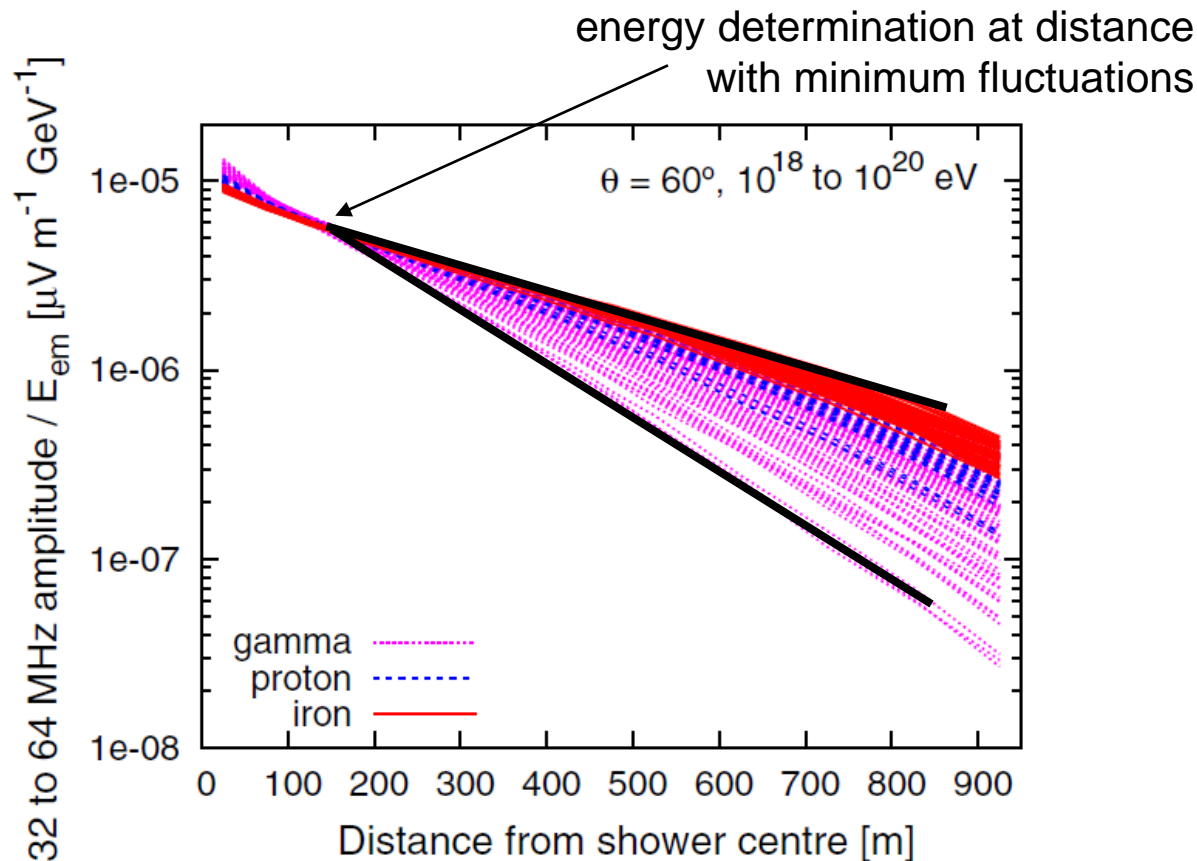
Comparison of simulations with Tunka-Rex data



- very good agreement between CoREAS simulations and Tunka-Rex data

Tunka-Rex Coll., Nucl. Instr. Meth. A 802 (2015) 89–96.

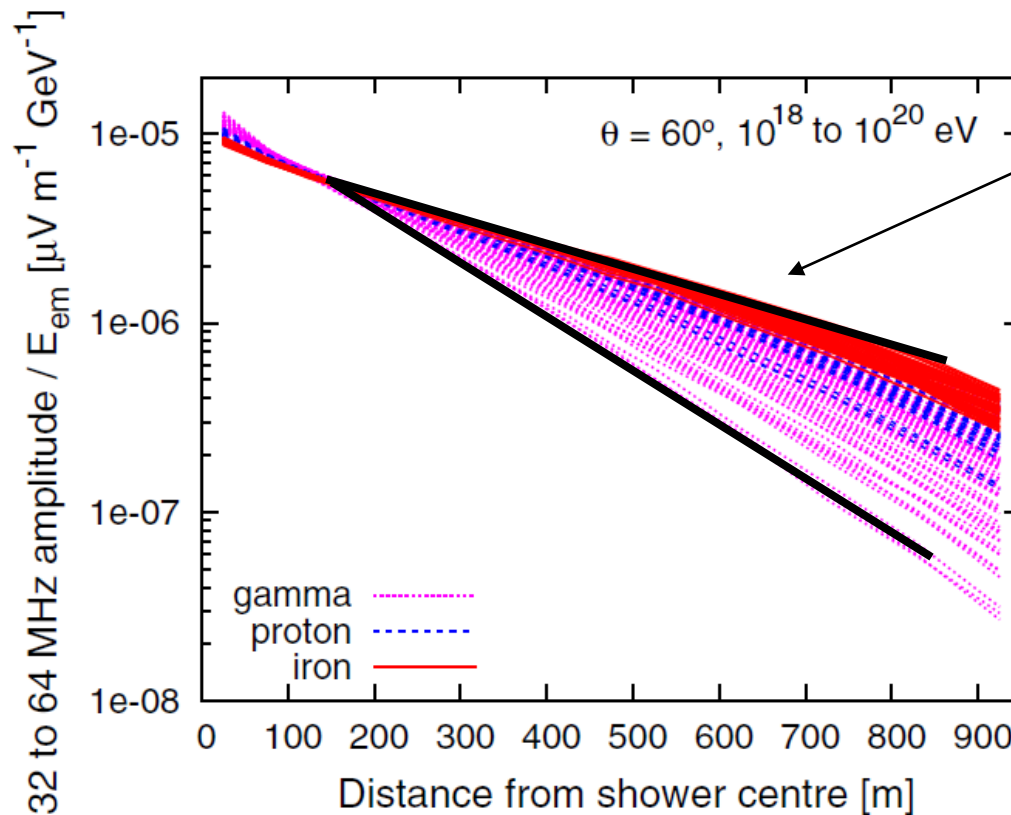
Expected energy sensitivity of radio detection



TH, Ulrich, Engel
(Astrop. Phys. 2008)

- linear scaling & characteristic distance for best energy estimate

Expected energy sensitivity of radio detection

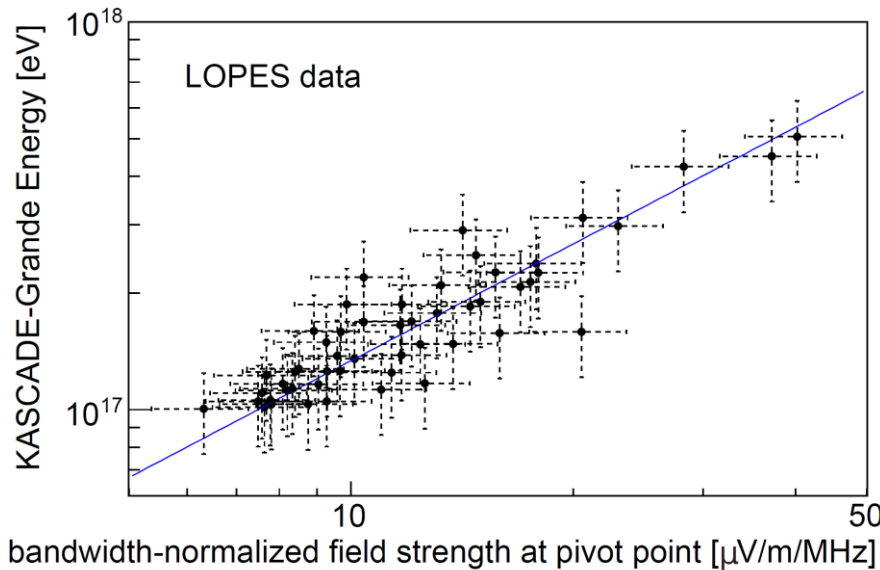


Xmax determination from slope of radio-LDF (better 2D signal distribution function)

- Fe** – flat
- p** – steeper, fluctuating
- γ** – steepest, fluctuating

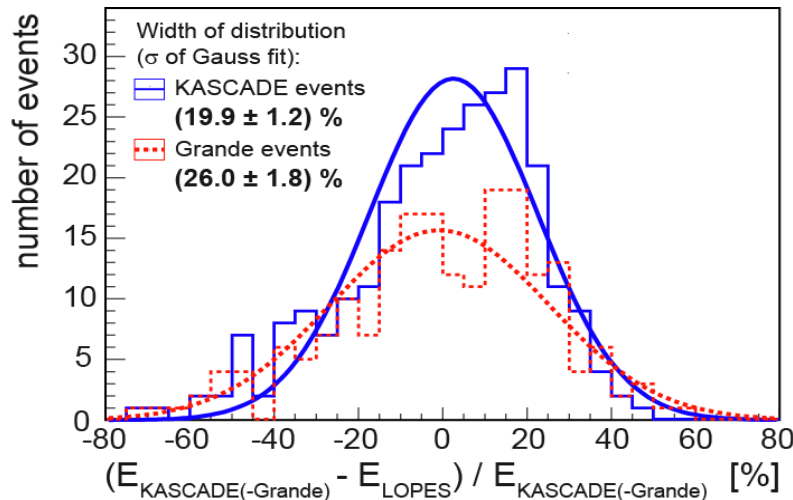
TH, Ulrich, Engel
(Astrop. Phys. 2008)

LOPES energy reconstruction



- linear correlation with 20-25% combined LOPES-KASCADE-Grande energy resolution
 - radio probably better, limited by KASCADE-Grande energy uncertainty of $\sim 20\%$
 - simulations: $\sim 8\%$ intrinsic

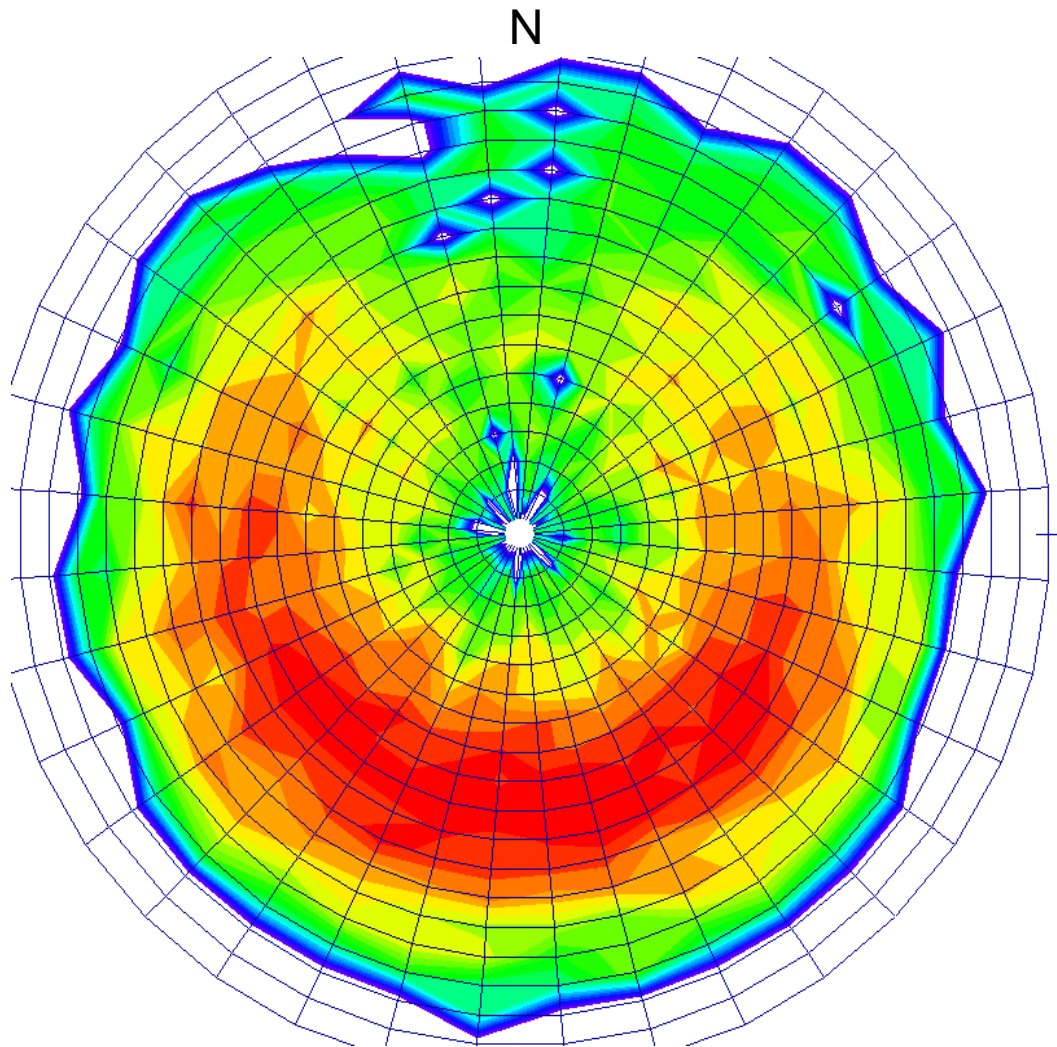
LOPES Coll., Phys. Rev. D 90 (2014) 062001.



- also works with interferometric analysis, yielding again $\sim 20\%$ uncertainty

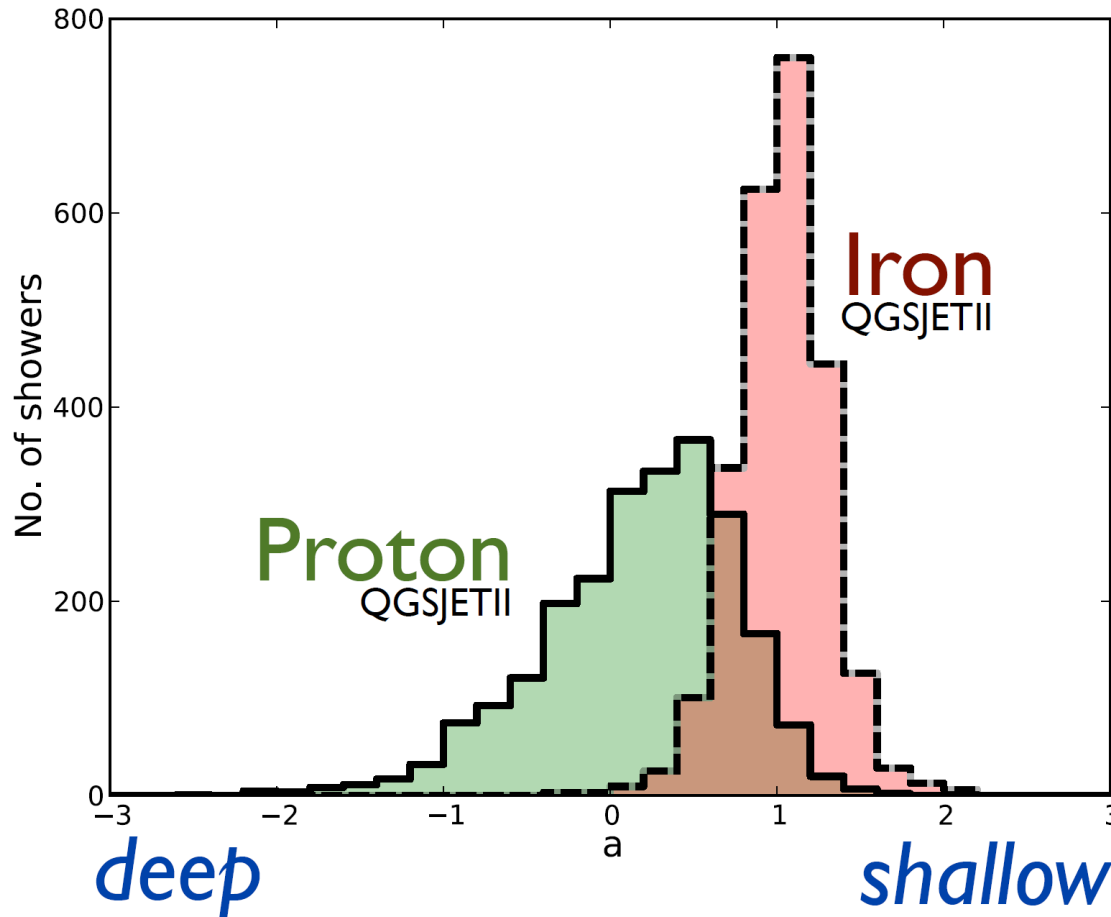
F.G. Schröder et al. (LOPES Coll.), ARENA2012

Direction-dependence of geomagnetic emission



- the dominant emission contribution scales with $\sin(\text{geomagnetic angle})$
- this leads to direction-dependent threshold – but with a well-defined characteristic

LOFAR unbinned analysis



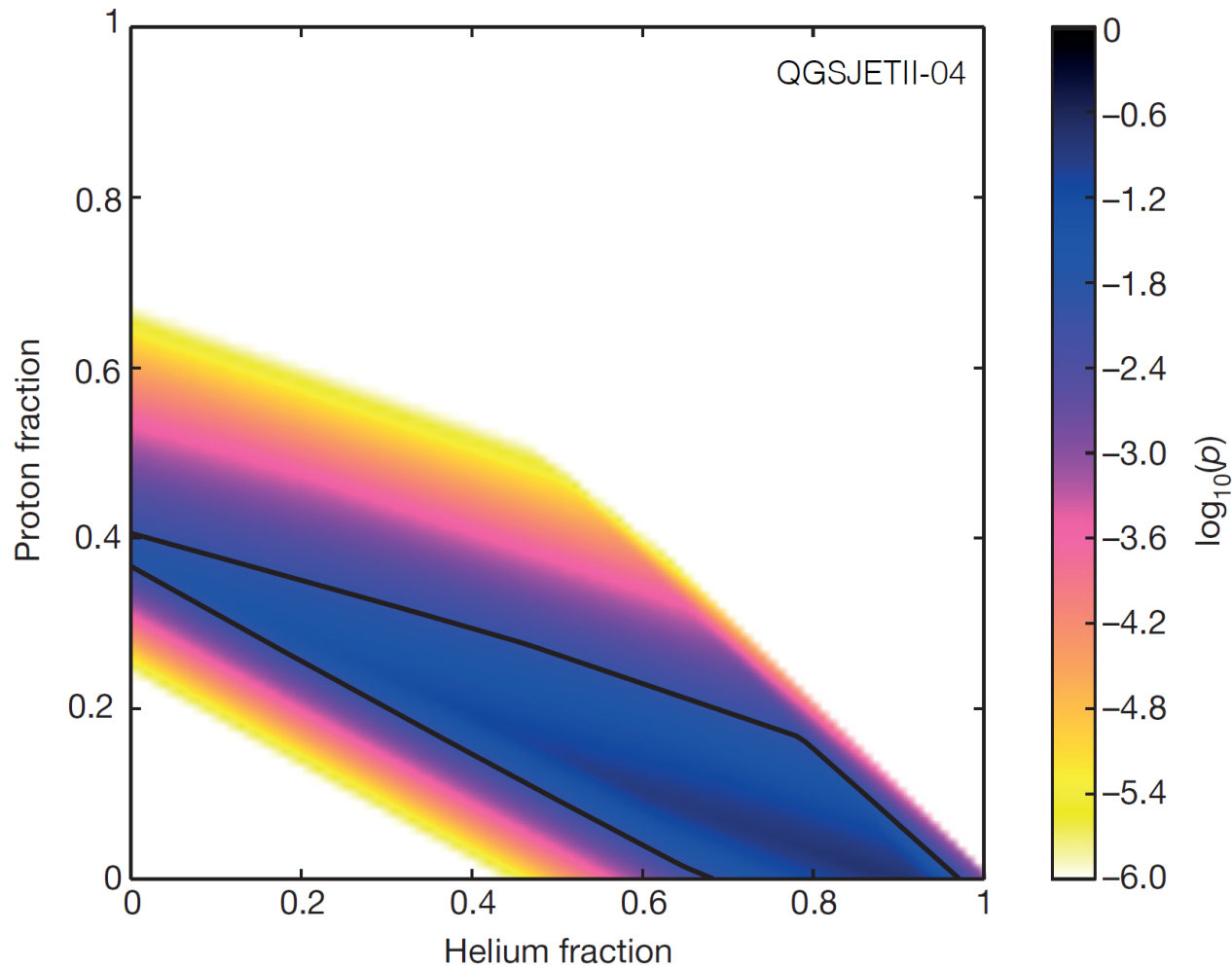
- use X_{\max} distribution rather than just mean
- for each shower determine value

$$a = \frac{\langle X_{\text{proton}} \rangle - X_{\text{shower}}}{\langle X_{\text{proton}} \rangle - \langle X_{\text{iron}} \rangle}$$

- compare cumulative a-distribution with simulations based on various composition assumptions

S. Buitink et al. Nature 435 (2016) 70

LOFAR four-component model scan



Total fraction of light elements ($p+He$) in $[0.38, 0.98]$ at 99% C.L.